

Resummed Jet Bin Predictions

Xiaohui Liu

work with R. Boughezal, F. Petriello, F. Tackmann and J. Walsh - 1312.4535

LoopFest 2014
New York City College of Technology

See also

XL, F. Petriello - 1210.1906, 1303.4405

I. Stewart, F. Tackmann, J. Walsh and S. Zuberi - 1307.1808

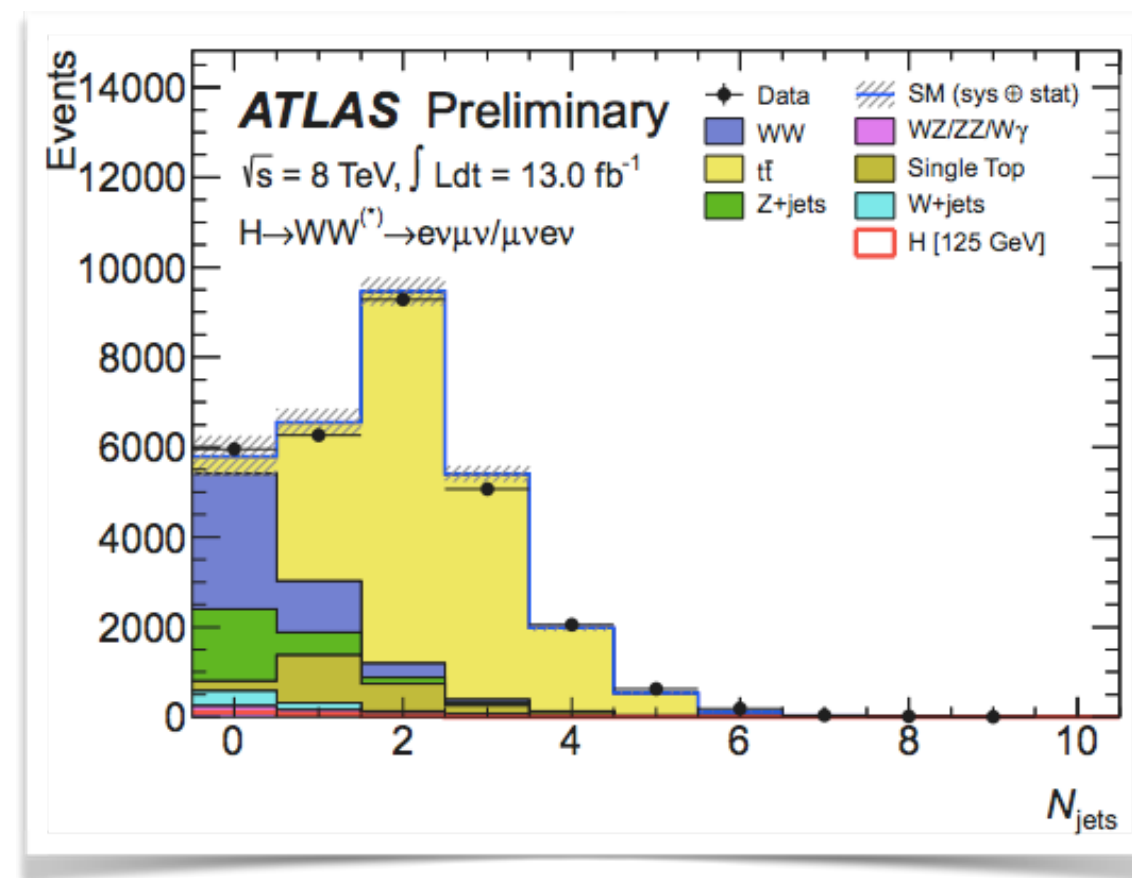
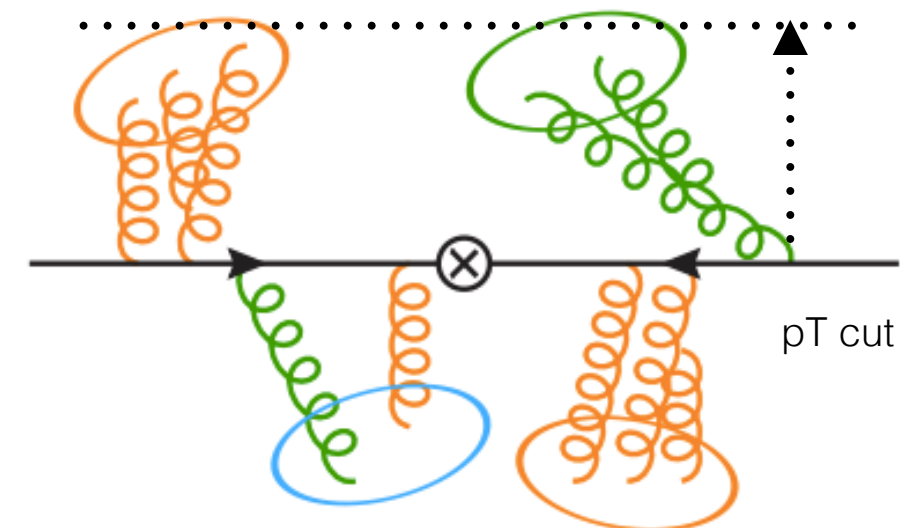


Outline

- Motivation
- $H + 0\text{-jets}$ and $H + 1\text{-jet}$ Cross Sections
- Conclusions

Motivation for Jet Bins

- Extensively used in LHC analyses
- HWW
 - anti-kT jet algorithm, $R \sim 0.4$
 - low pT cut $\sim 25 - 30\text{GeV}$
 - efficient in suppressing the backgrounds



[ATLAS-CONF-2012-158]

Motivation for Jet Bins

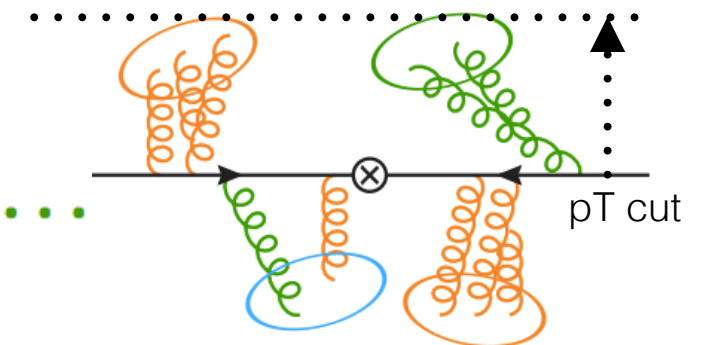
- Extensively used in LHC analyses
 - HWW
 - anti-kT jet algorithm, $R \sim 0.4$
 - low pT cut $\sim 25 - 30\text{GeV}$
 - efficient in suppressing the backgrounds
 - large theory uncertainties

Source (0-jet)	Signal (%)	Bkg. (%)
Inclusive ggF signal ren./fact. scale	13	-
1-jet incl. ggF signal ren./fact. scale	10	-
PDF model (signal only)	8	-
QCD scale (acceptance)	4	-
Jet energy scale and resolution	4	2
W+jets fake factor	-	5
WW theoretical model	-	5
Source (1-jet)	Signal (%)	Bkg. (%)
1-jet incl. ggF signal ren./fact. scale	26	-
2-jet incl. ggF signal ren./fact. scale	15	-
Parton shower/ U.E. model (signal only)	10	-
b-tagging efficiency	-	11
PDF model (signal only)	7	-
QCD scale (acceptance)	4	2
Jet energy scale and resolution	1	3
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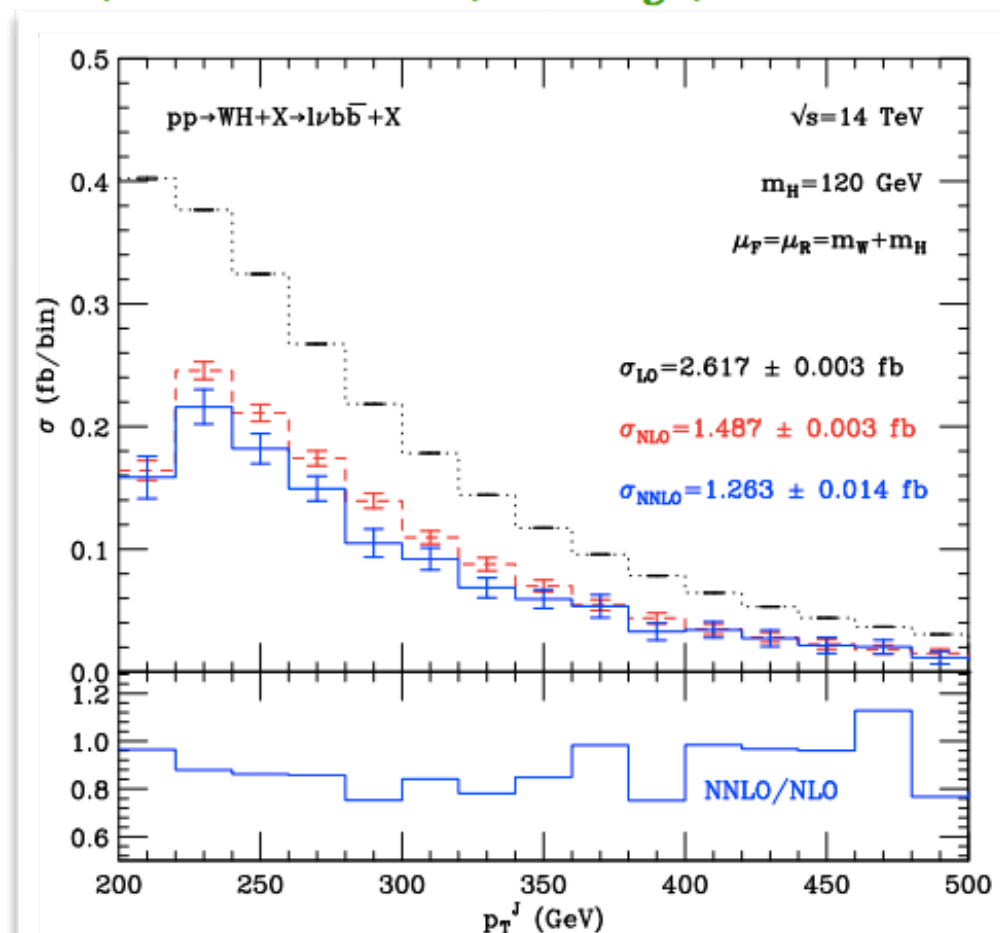
Theoretical Issues with Jet Veto

- Low p_T jet veto restricts emissions to be soft and collinear
- leads to large Sudakov logs

$$\alpha_s(L^2 + L + 1) + \alpha_s^2(L^4 + L^3 + L^2 + L + 1) + \dots$$



$$L = \log(p_{T\text{cut}}/Q)$$



[Ferrera, Grazzini, Tramontano - 1107.1164]

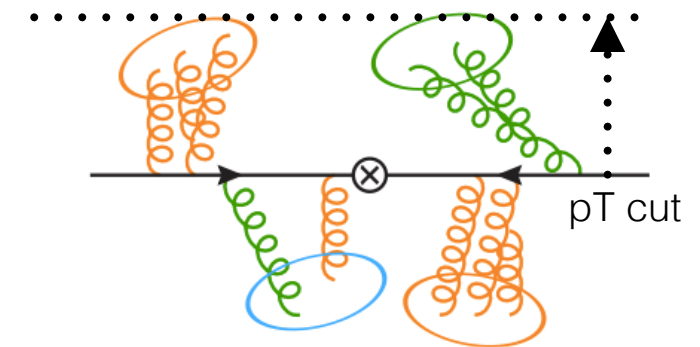
from inclusive NLO: +30% [Han, Willenbrock - 1990]

to jet veto: - 50%

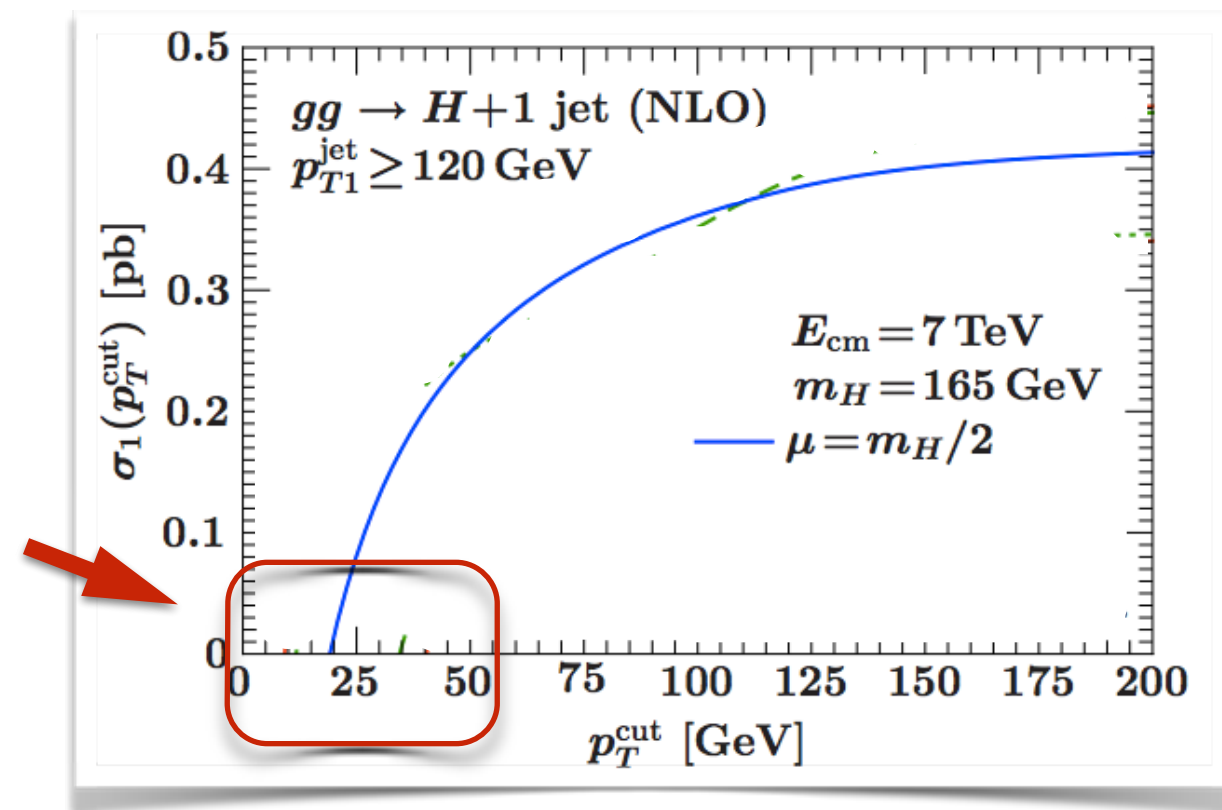
due to the jet veto logs L !

Theoretical Issues with Jet Veto

- Low p_T jet veto restricts emissions to be soft and collinear
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- unreliable perturbative predictions

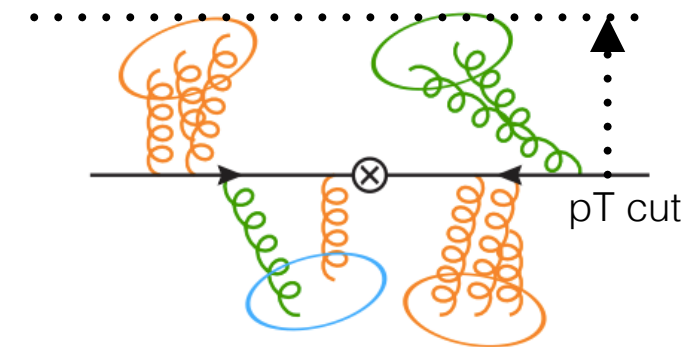


miss large higher order corrections



Theoretical Issues with Jet Veto

- Low p_T jet veto restricts emissions to be soft and collinear
- leads to large Sudakov logs
- unreliable perturbative predictions
- unreliable uncertainty estimation

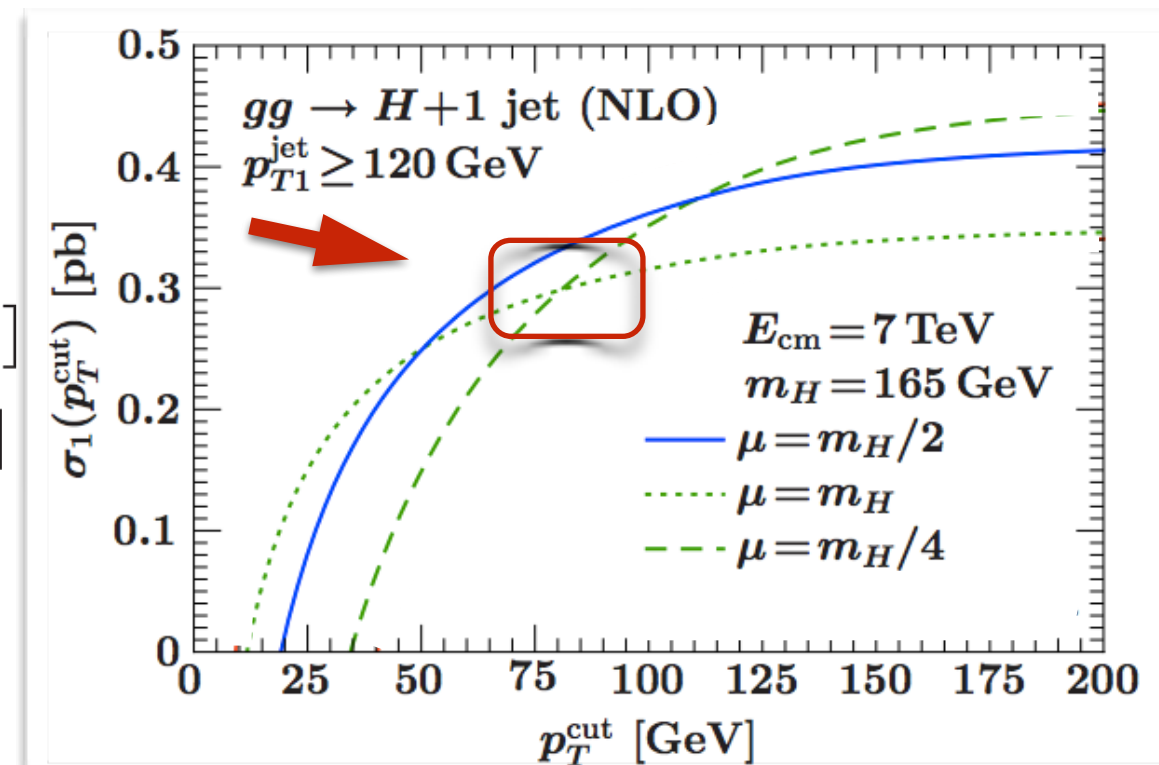


accidental cancellation

$$\sigma_{\geq 1}(p_{T_1}^{\text{jet}} \geq 120 \text{ GeV}) = (0.31 \text{ pb}) [1 + 2.9\alpha_s + \mathcal{O}(\alpha_s^2)]$$

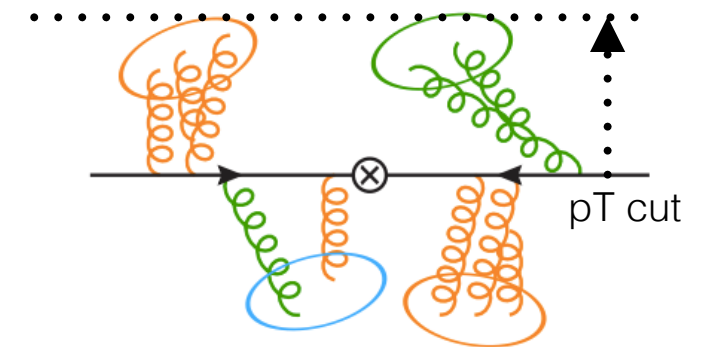
$$\sigma_{\geq 2}(p_{T_1}^{\text{jet}} \geq 120 \text{ GeV}, p_{T_2}^{\text{jet}} \geq 60 \text{ GeV}) = (0.31 \text{ pb}) [3.7\alpha_s + \mathcal{O}(\alpha_s^2)]$$

$$\sigma_N = \sigma_{\geq N} - \sigma_{\geq N+1}$$



Theoretical Issues with Jet Veto

- Low p_T jet veto restricts emissions to be soft and collinear
- leads to large Sudakov logs
- unreliable perturbative predictions
- unreliable uncertainty estimation
- large theoretical errors

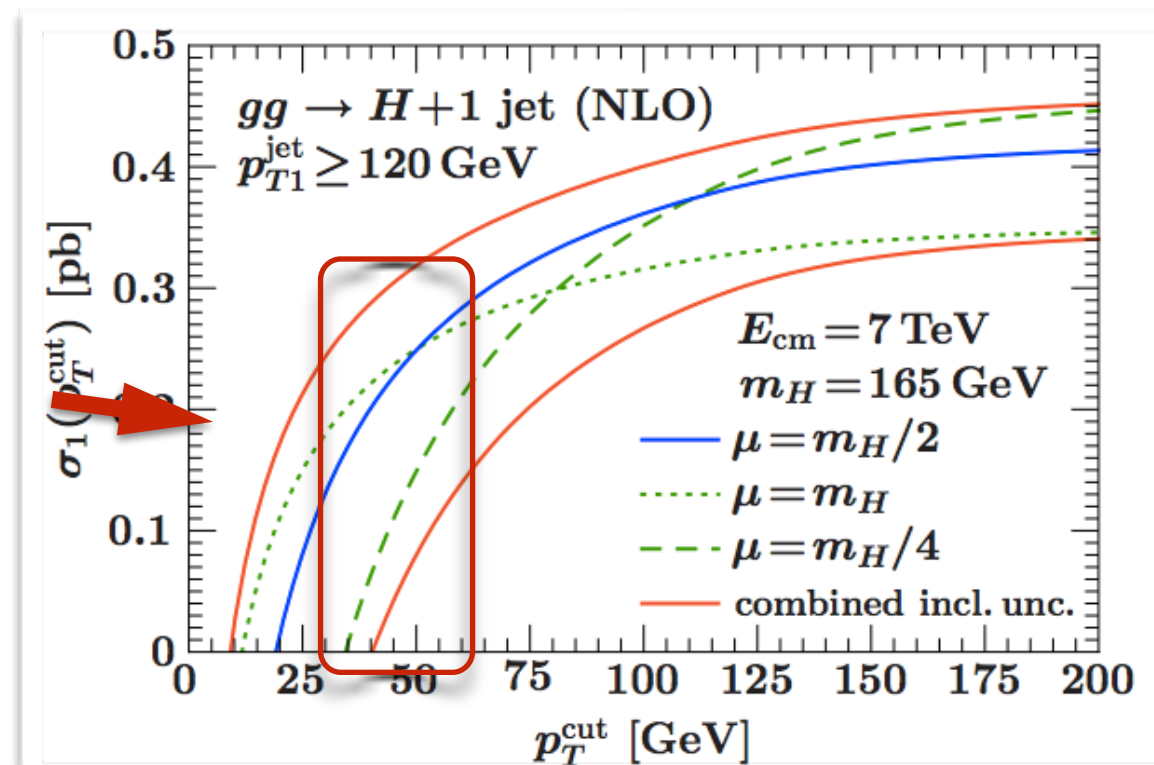


ST prescription used by ATLAS and CMS

$$\Delta_N^2 = \Delta_{\geq N}^2 + \Delta_{\geq N+1}^2$$

$$\sigma_N = \sigma_{\geq N} - \sigma_{\geq N+1}$$

[Stewart and Tackmann-1107.2117]



Theoretical Issues with Jet Veto

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[Stewart and Tackmann-1107.2117]



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[ATLAS-CONF-2012-158]

Theoretical Issues with Jet Veto

- Low p_T jet veto restricts emissions to be soft and collinear

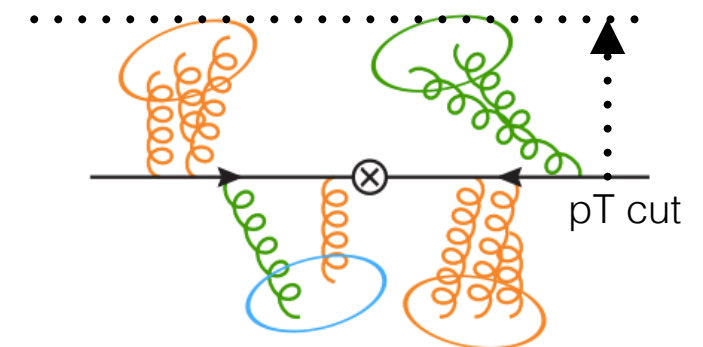
- leads to large Sudakov logs

- unreliable perturbative predictions

- unreliable uncertainty estimation

- large theoretical errors

- need to be resummed



$$\begin{aligned}
 & \sim 1 \\
 & + \alpha_s L^2 + \alpha_s L + \alpha_s \text{ NLO} \\
 & + \alpha_s^2 L^4 + \alpha_s^2 L^3 + \alpha_s^2 L^2 + \alpha_s^2 L + \alpha_s^2 \text{ NNLO} \\
 & + \alpha_s^3 L^6 + \alpha_s^3 L^5 + \alpha_s^3 L^4 + \alpha_s^3 L^3 + \alpha_s^3 L^2 + \dots \\
 & \text{LL} \quad \text{NLL} \quad \text{NNLL}
 \end{aligned}$$

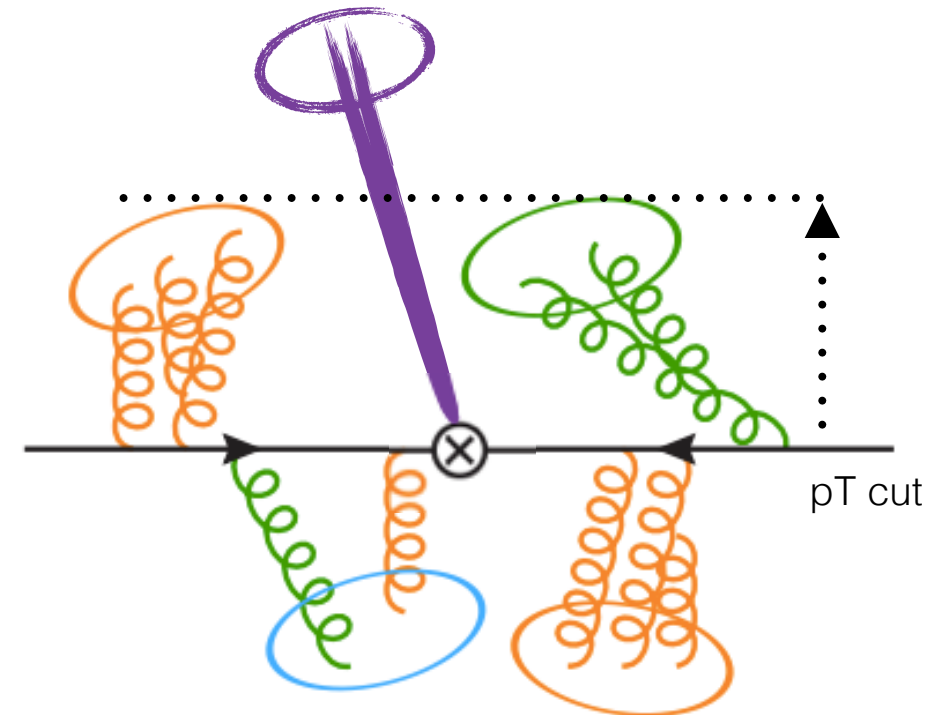
Efforts on Jet Vetoes

- H + 0-jets
 - Banfi, Monni, Salam, Zanderighi - 1203.5773, 1206.4996, NNLL + NNLO
 - Becher, Neubert, Rothen - 1205.3806, 1307.0025, NNLL' + NNLO + π^2
 - Stewart, Tackmann, Walsh, Zuberi - 1307.1808, NNLL' + NNLO + π^2
 - Alioli and Walsh - 1311.5234, Clustering Logs,
 - Moulton and Stewart - 1405.5334, interfering with H \rightarrow W+W-
- H + 1-jet
 - XL, Petriello - 1210.1906, 1303.4405, NLL' + NLO
 - Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535, (beyond NLL') + NLO, (H+0+1j)
- VH + 0-jets
 - Li, Li, Shao - 1309.5015, NNLL + NLO + π^2
 - Li, XL - 1401.2149, (beyond NNLL) + NNLO + π^2

Efforts on Jet Vetoes

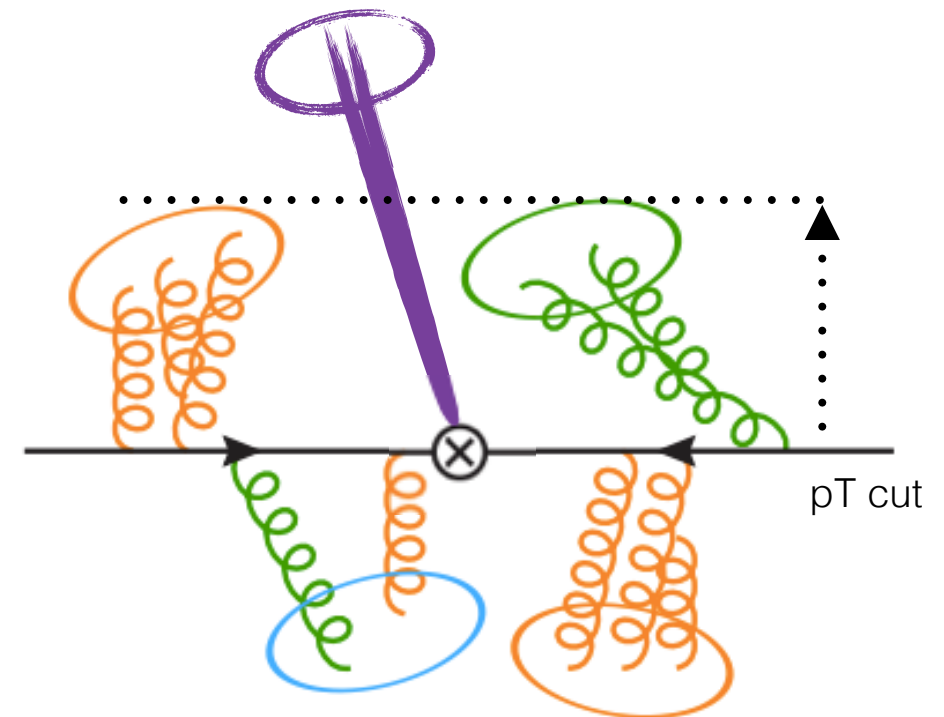
- Factorization

$$\begin{aligned}
 2 \ln^2 \frac{p_T^{\text{cut}}}{m_H} &= 2 \ln^2 \frac{m_H}{\mu} \\
 &+ 4 \ln \frac{p_T^{\text{cut}}}{\mu} \ln \frac{\nu}{m_H} \\
 &+ 2 \ln \frac{p_T^{\text{cut}}}{\mu} \ln \frac{\mu p_T^{\text{cut}}}{\nu^2}
 \end{aligned}$$



Efforts on Jet Vetoes

- Factorization
 - kT type jet algorithm tends to group soft and energetic radiations near the beam into different jets, large rapidity separation
 - anti-kT tends to group central energetic radiations in to jets first. The soft radiations will only see the overall pre-determined jet directions



Becher, Neubert, Rothen - 1205.3806, 1307.0025

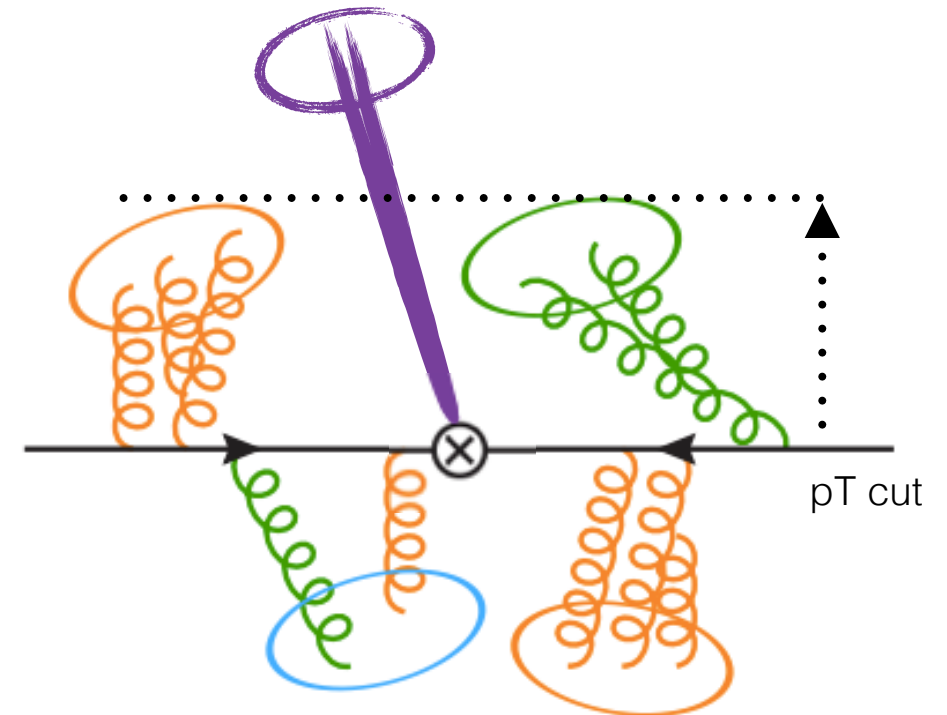
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Efforts on Jet Vetoes

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 \end{aligned}$$



$$\sigma_0(p_T^{\text{cut}}) = H(Q, \mu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) S^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) J(R, p_T^J R, \mu)$$

Efforts on Jet Vetoes

- Factorization

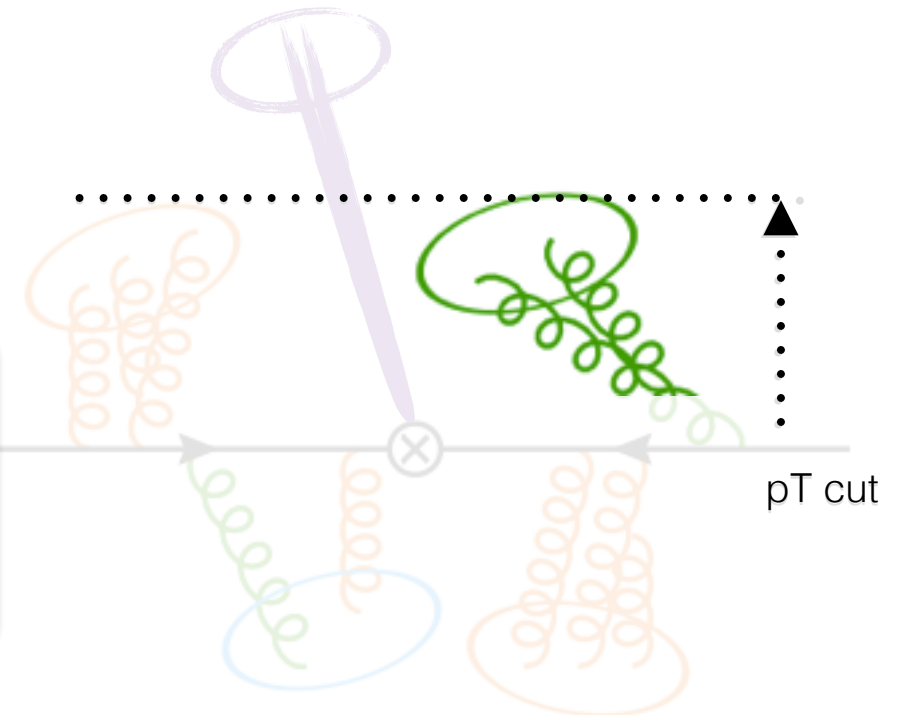
$$2 \ln^2 \frac{p_T^{\text{cut}}}{m_H} = 2 \ln^2 \frac{p_T^{\text{cut}}}{m_H} + 2 \ln \frac{p_T^{\text{cut}}}{\mu} \ln \frac{p_T^{\text{cut}}}{\nu^2}$$

$$\sigma_0(p_T^{\text{cut}}) = \underline{H(Q, \mu)} B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) S^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) J(R, p_T^J R, \mu)$$

Efforts on Jet Vetoes

- Factorization

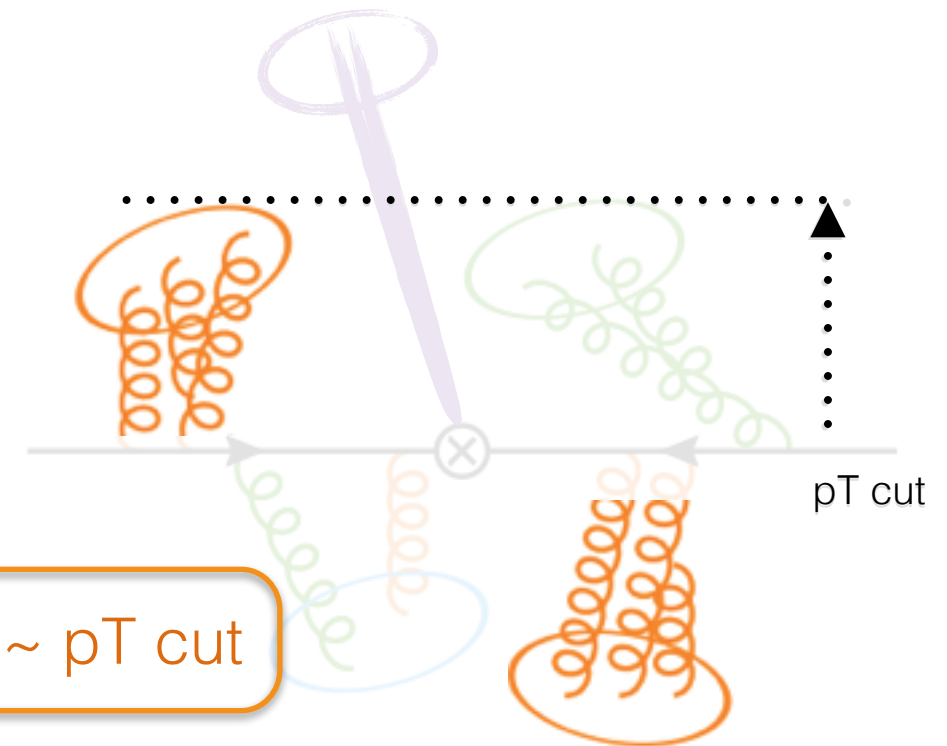
- * initial state energetic radiations with transverse momentum $\sim p_T$ cut
- * includes pdf information



$$\sigma_0(p_T^{\text{cut}}) = H(Q, \mu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) S^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) J(R, p_T^J, \mu)$$

Efforts on Jet Vetoes

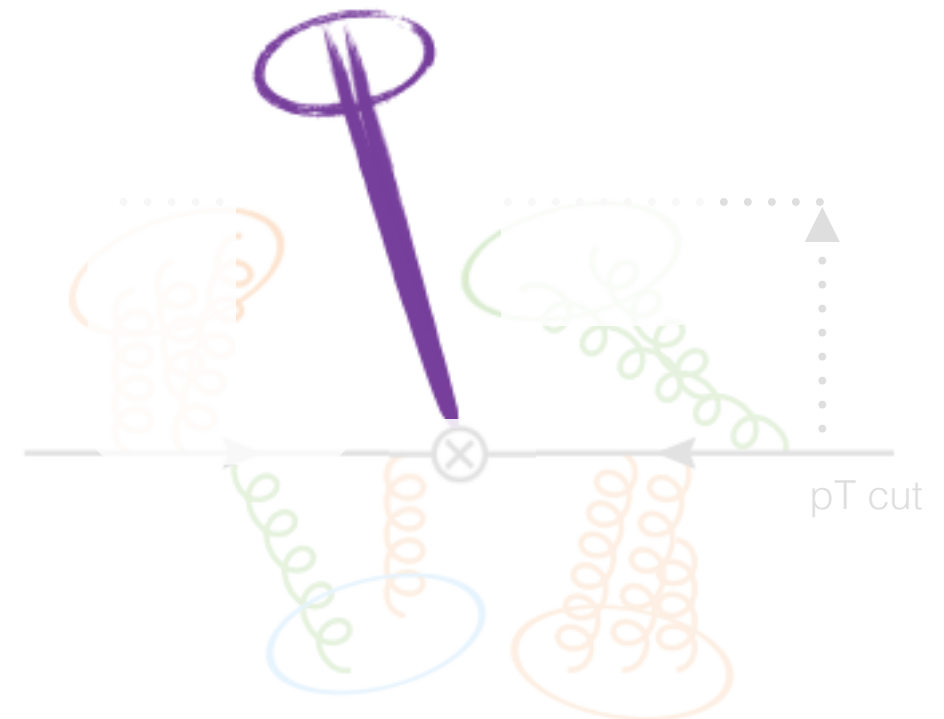
- Factorization



$$\sigma_0(p_T^{\text{cut}}) = H(Q, \mu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) S^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) J(R, p_T^J, \mu)$$

Efforts on Jet Vetoes

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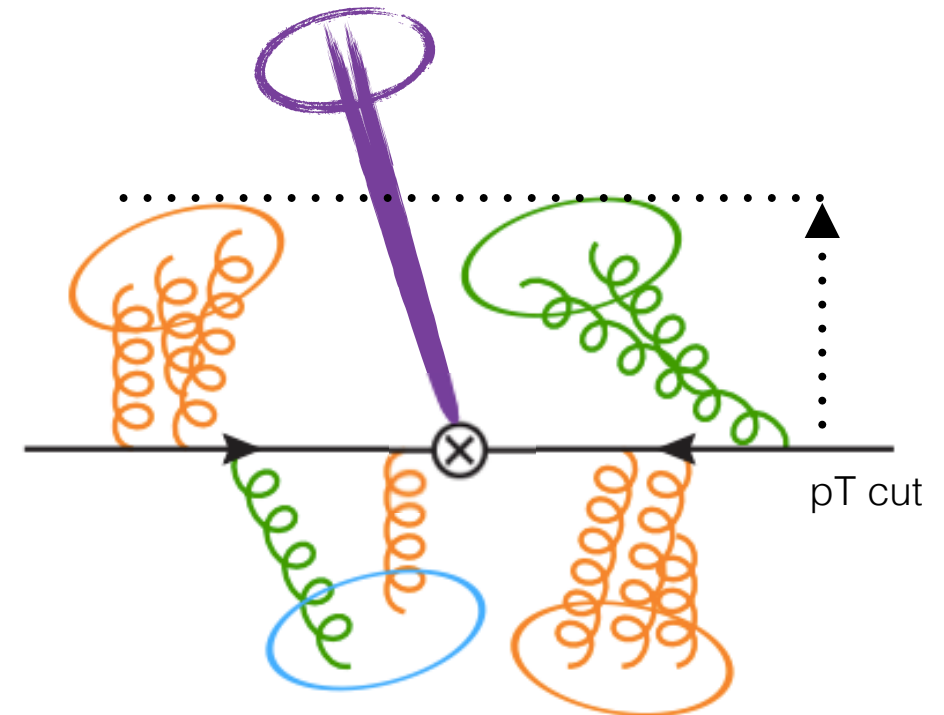


$$\sigma_0(p_T^{\text{cut}}) = H(Q, \mu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) S^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) J(R, p_T^J R, \mu)$$

- * Final state energetic radiations
- * Required energetic jets ($p_{TJ} \sim m_H$)
experimentally $p_{TJ} \sim p_T^{\text{cut}}$
will come back to this point later

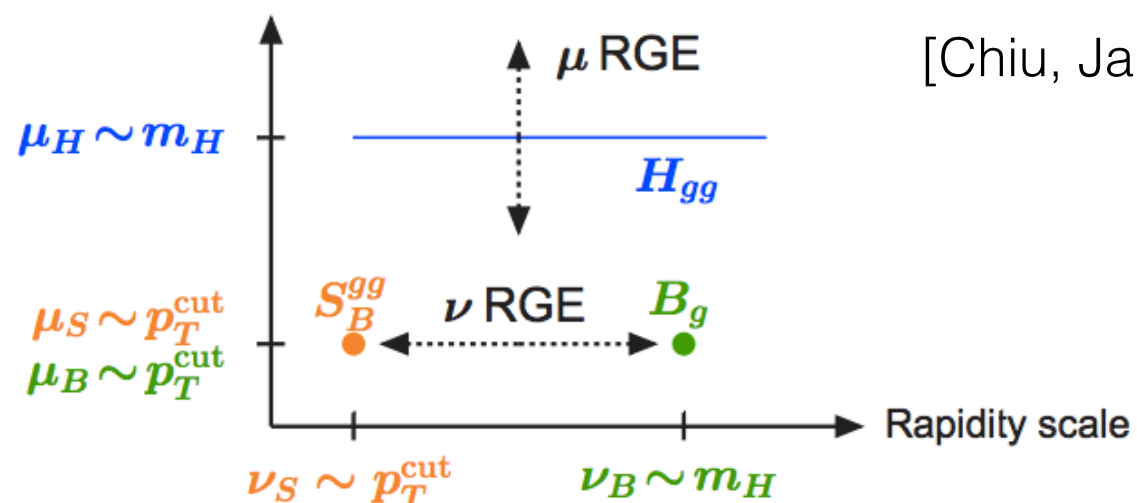
Efforts on Jet Vetoes

- Factorization
- Resummation
 - logs resummed via RG equations similar to DGLAP for pdfs



$$\sigma_0(p_T^{\text{cut}}) = H(Q, \mu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) B^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) S^{\text{jet}}(R, p_T^{\text{cut}}, \mu, \nu) J(R, p_T^J, \mu)$$

Renormalization scale

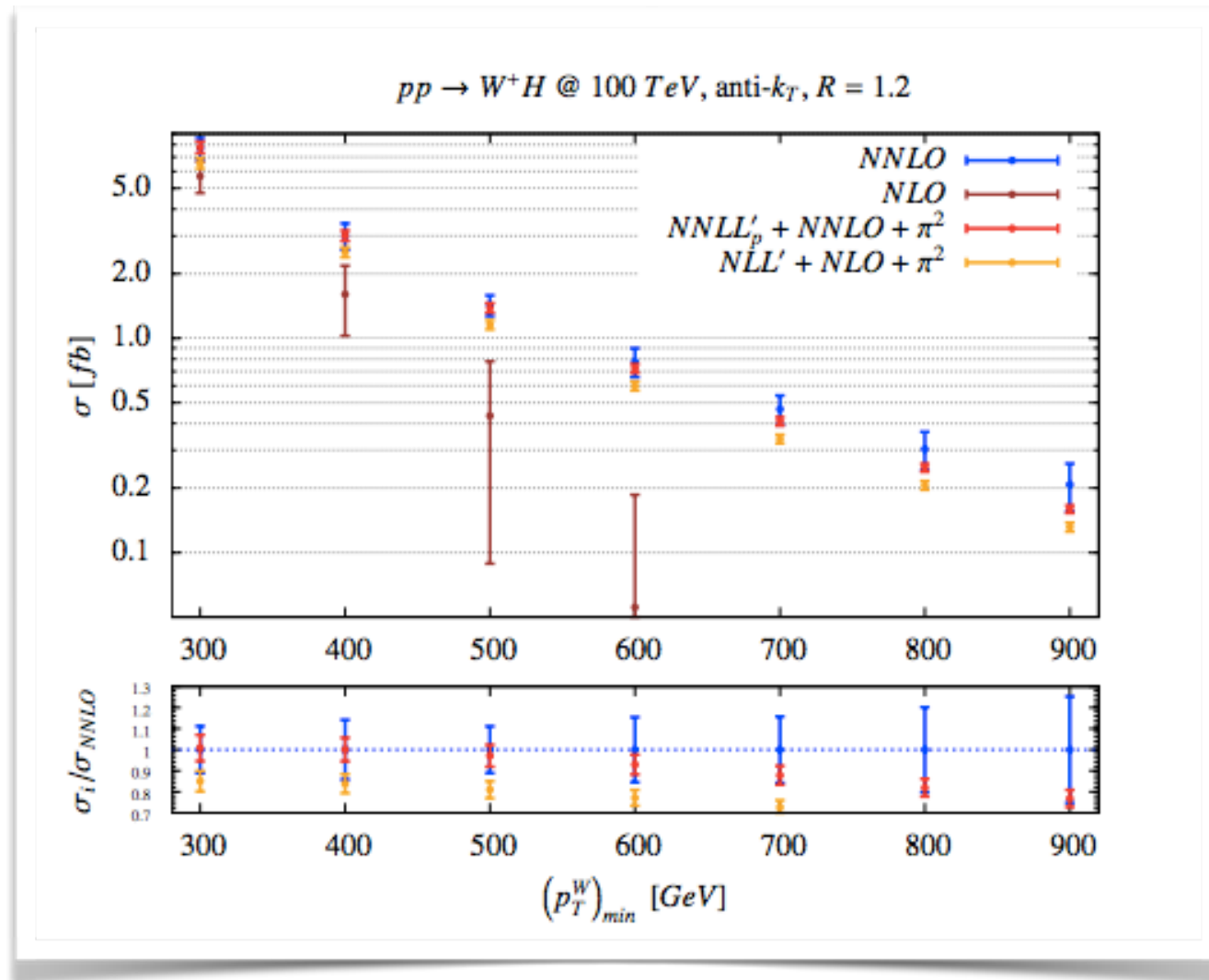


[Chiu, Jain, Neill and Rothstein, 2011]

alternative approach based on collinear anomaly
[Becher, Neubert]

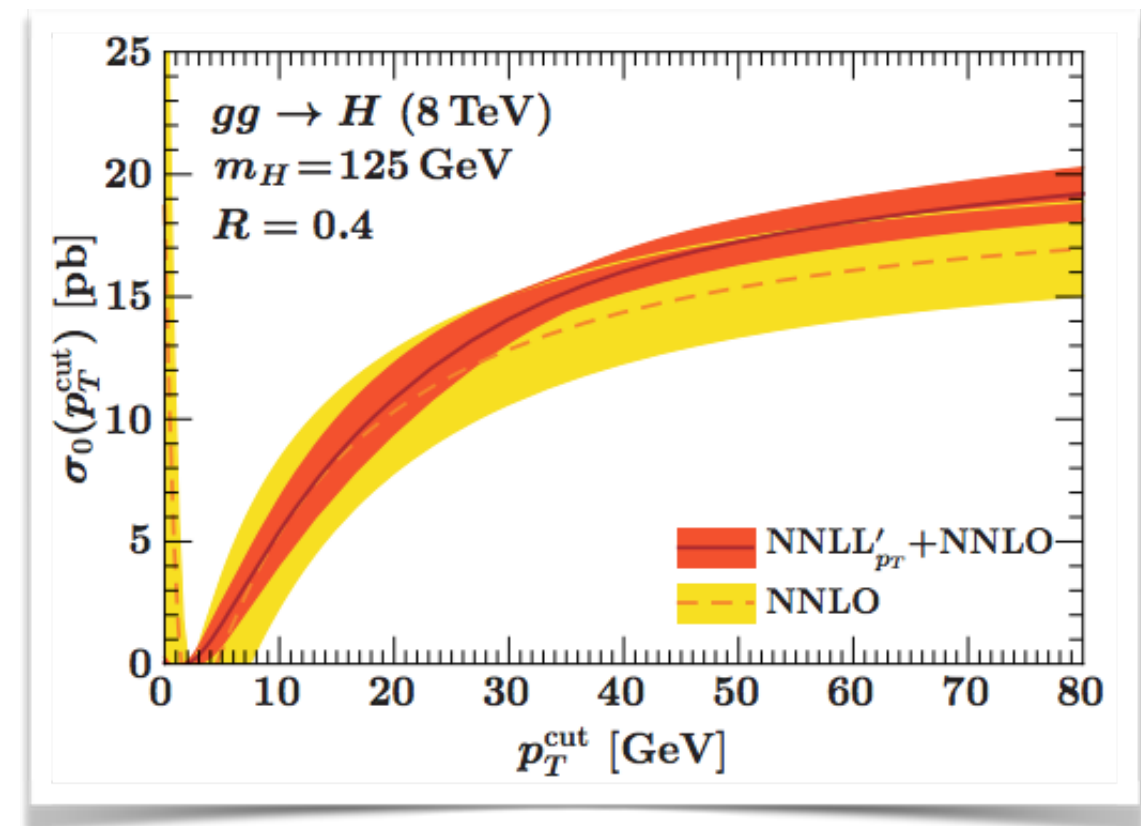
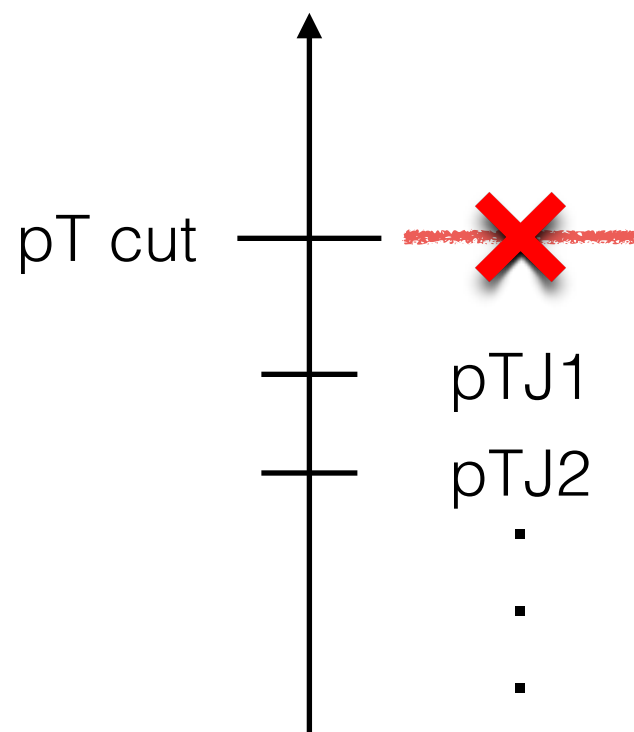
Higgs on future colliders

- Boosted Higgs @ future colliders $p_T \text{ veto} = 30\text{GeV}$
- resummation stabilizes the perturbative series
- resummation reduces the scale uncertainties



H + 0-jets and H + 1-jet

- H + 0-jets
 - keep events with no jet $p_T > p_T^{\text{cut}}$
 - NNLL' + NNLO + π^2



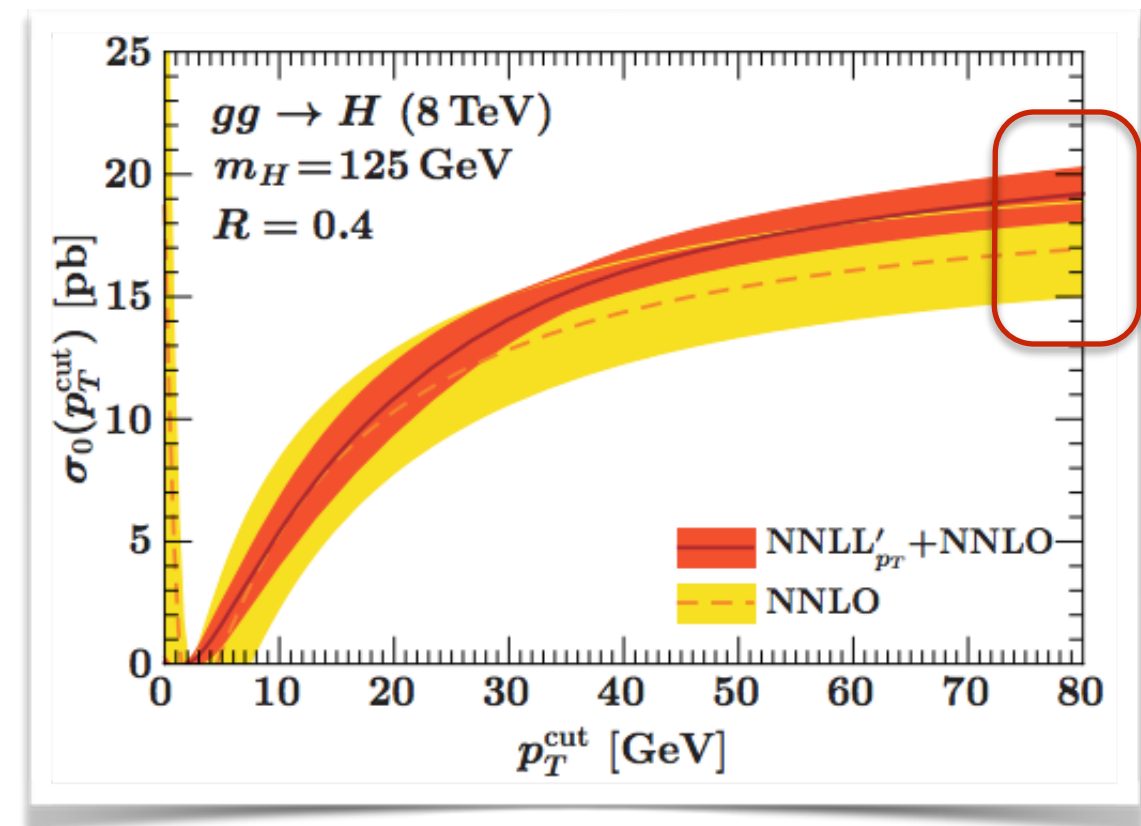
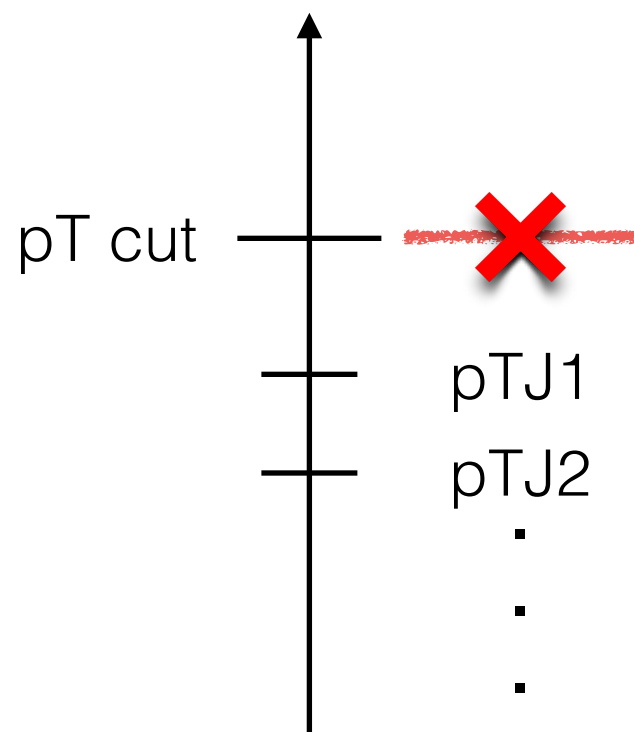
[Stewart, Tackmann, Walsh, Zuberi - 1307.1808]

see also, Becher, Neubert, Rothe - 1307.0025

H + 0-jets and H + 1-jet

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- keep events with no jet $p_T > p_T \text{ cut}$
- NNLL' + NNLO + π^2

π^2 resummation also enhanced the inclusive cross section

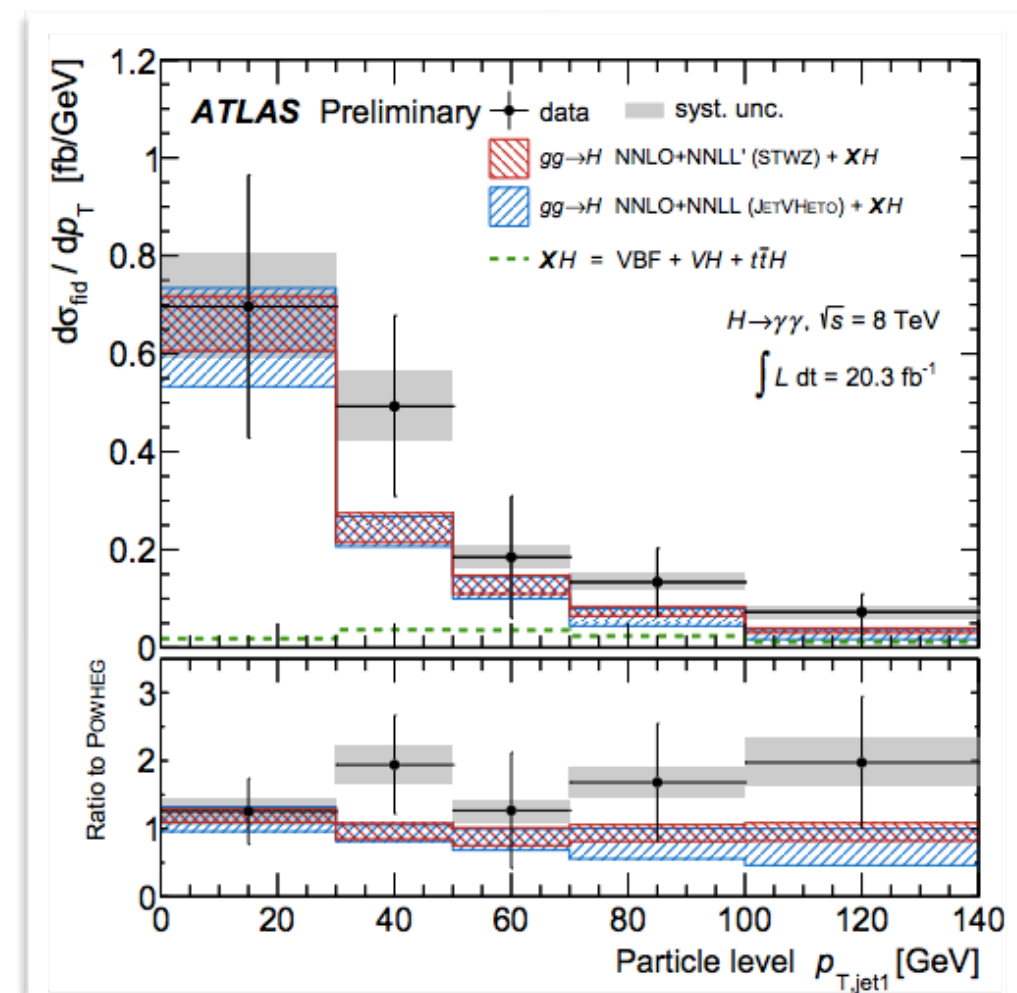
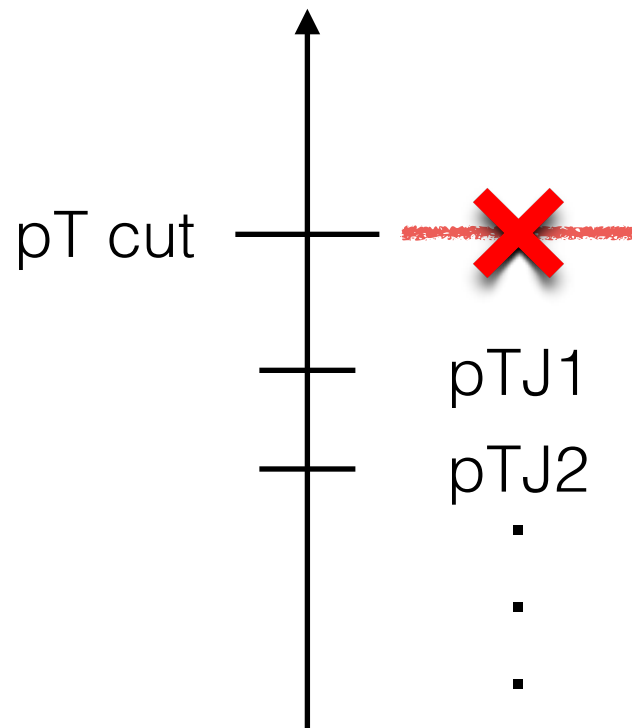


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H + 0-jets and H + 1-jet

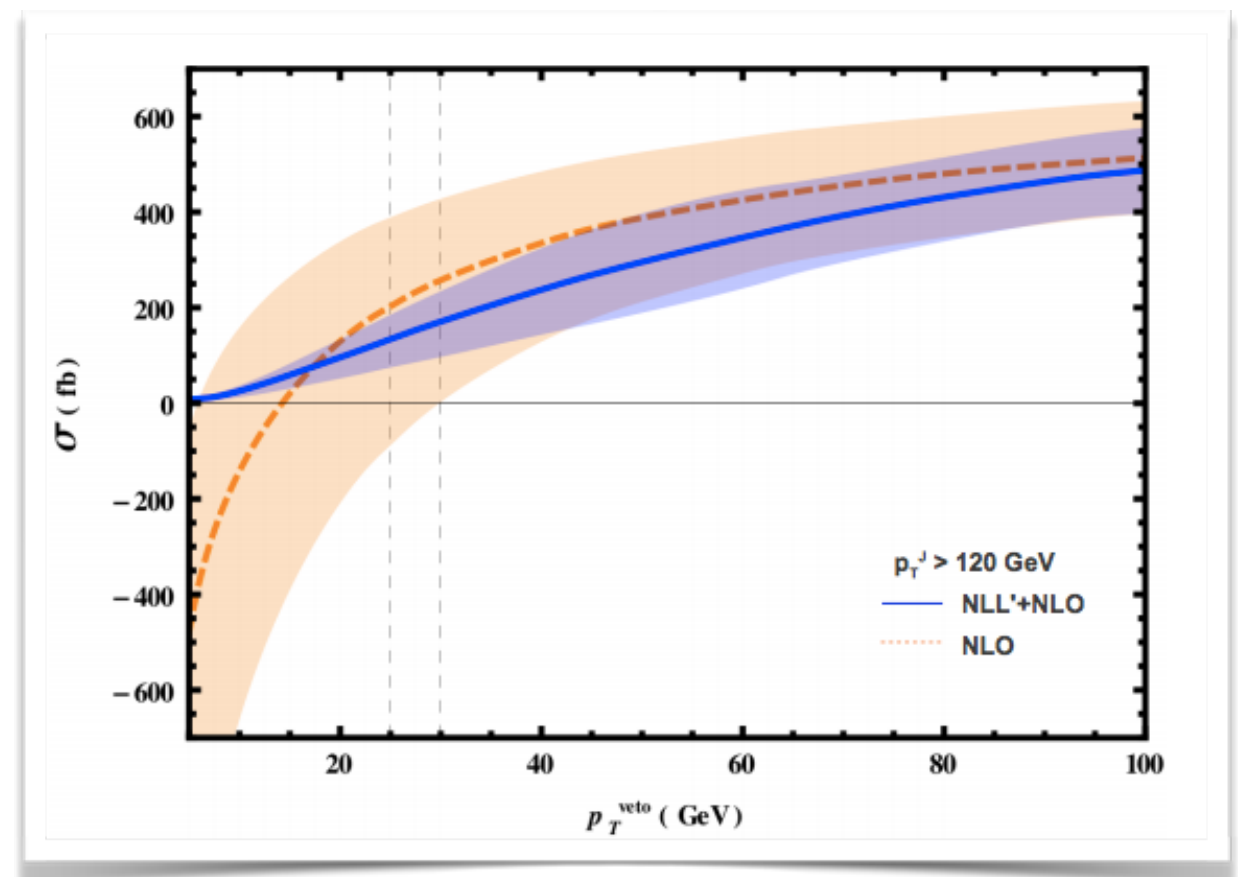
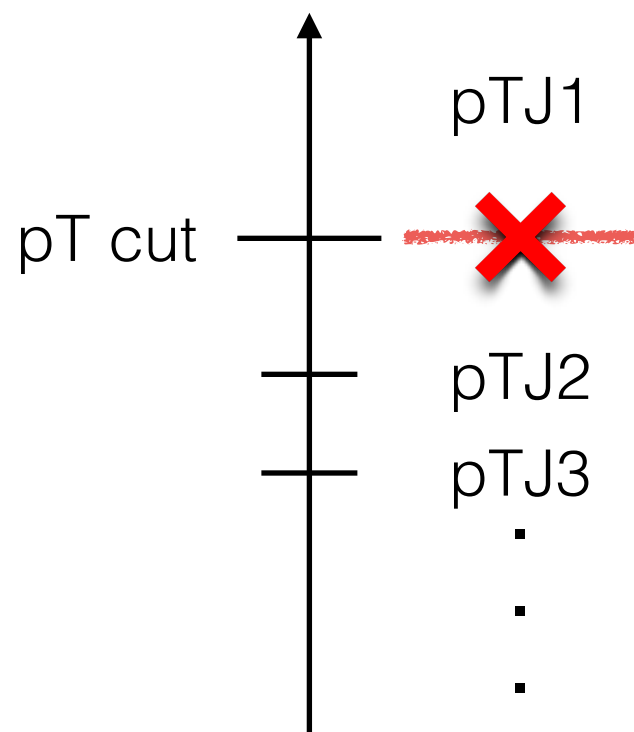
- H + 0-jets
 - keep events with no jet $p_T > p_T \text{ cut}$
- NNLL' + NNLO + π^2
- inclusive 1-jet ($p_{TJ} \ll m_H$)



[ATLAS-CONF-2013-072]

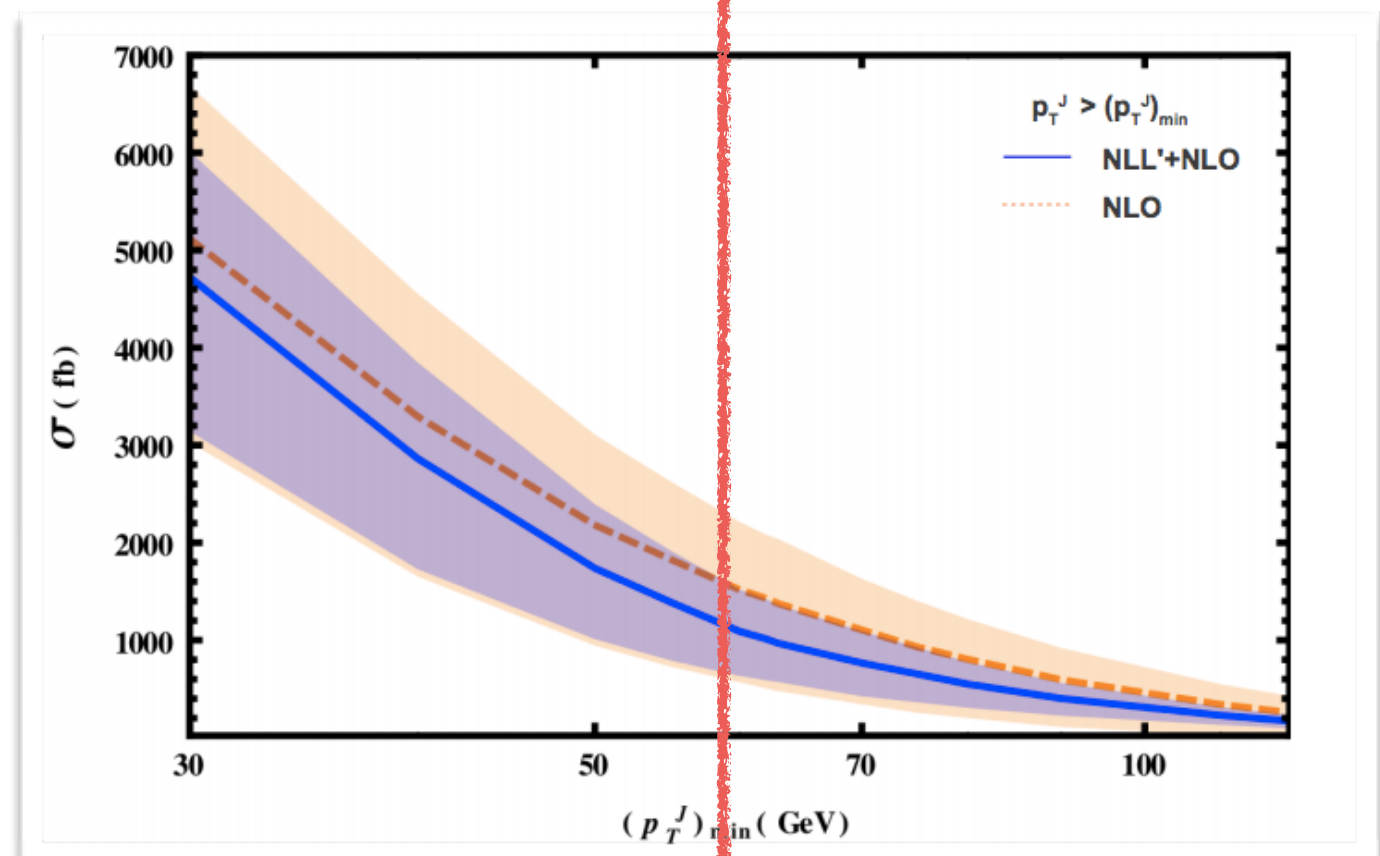
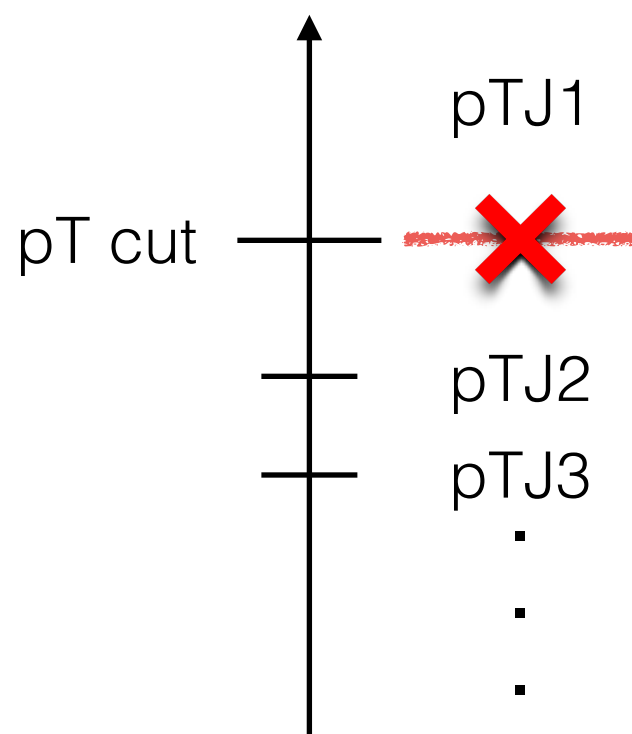
H + 0-jets and H + 1-jet

- H + 1-jet
 - keep events with no 2nd jet $p_T > p_T \text{ cut}$
 - factorization hold exact for $p_{TJ1} \sim m_H$



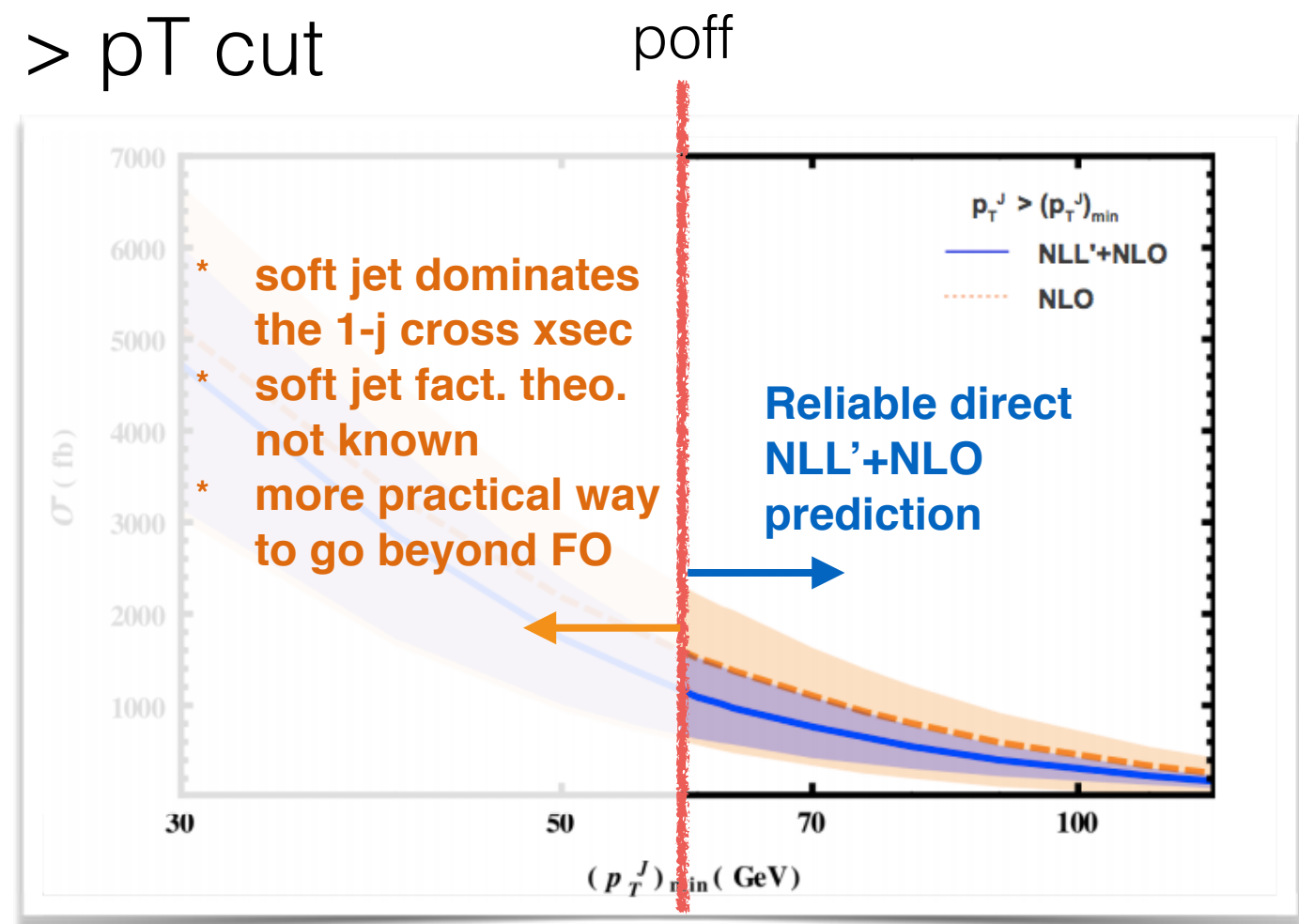
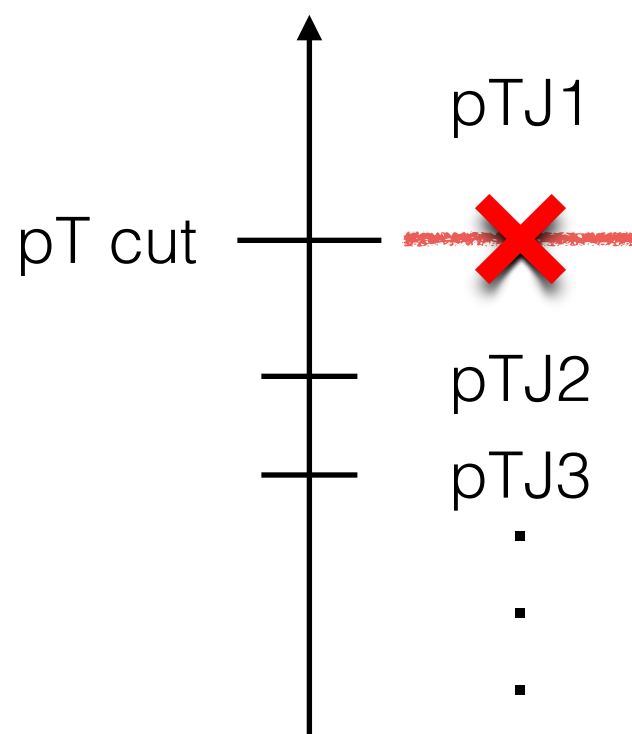
H + 0-jets and H + 1-jet

- H + 1-jet
 - keep events with no 2nd jet $p_T > p_T \text{ cut}$
 - experimentally, $p_{TJ} > p_T \text{ cut}$



H + 0-jets and H + 1-jet

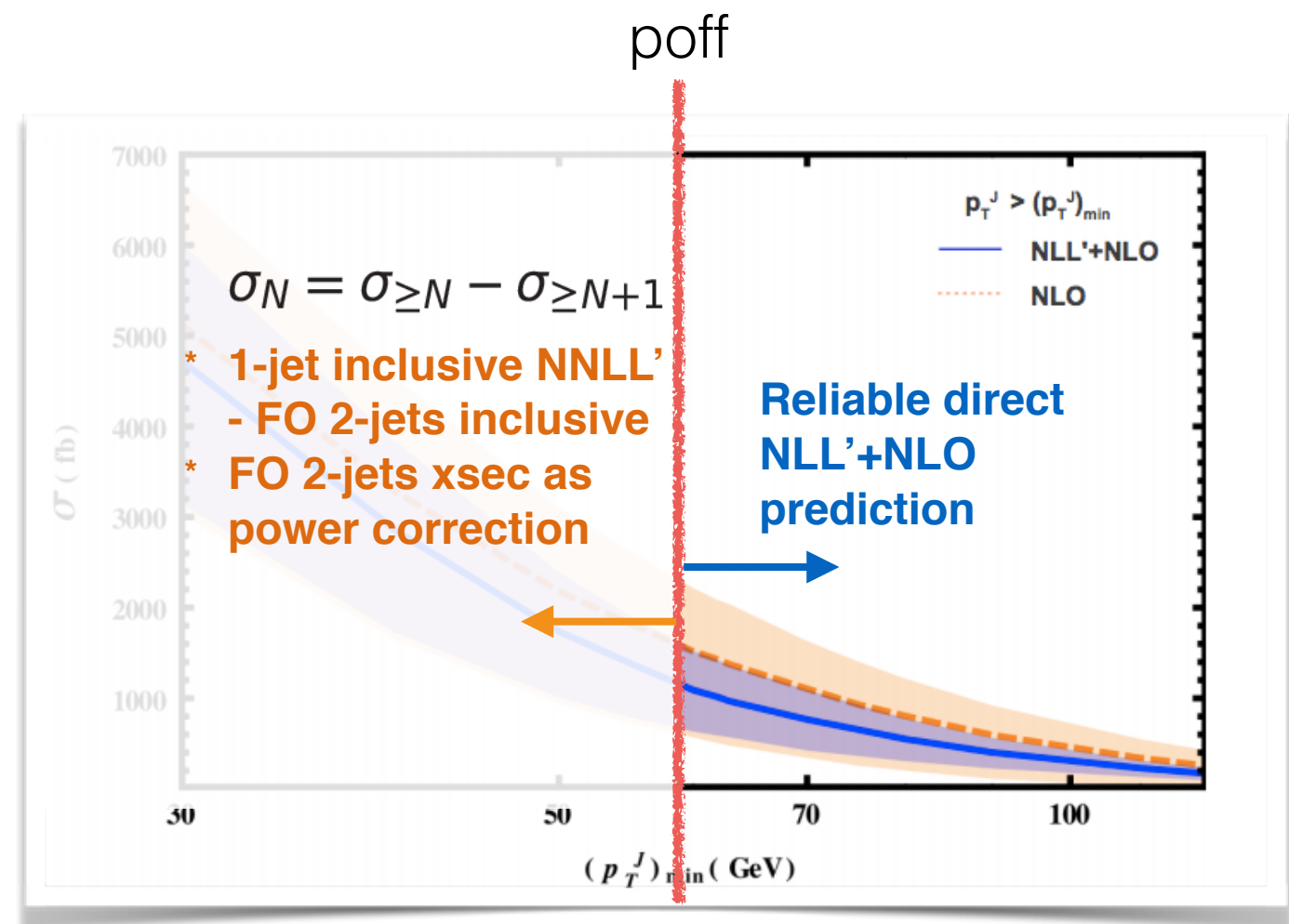
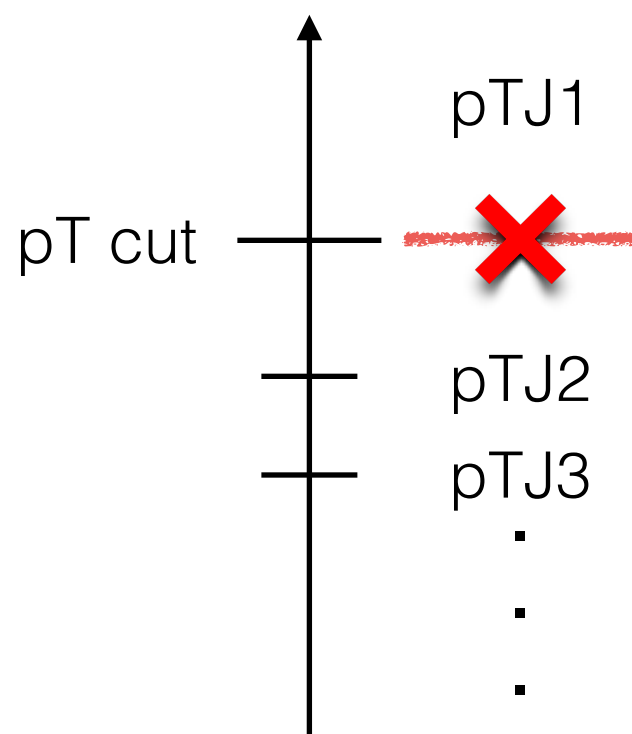
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H + 0-jets and H + 1-jet

- H + 1-jet
- resummation improved H + 1-jet (full spectrum)

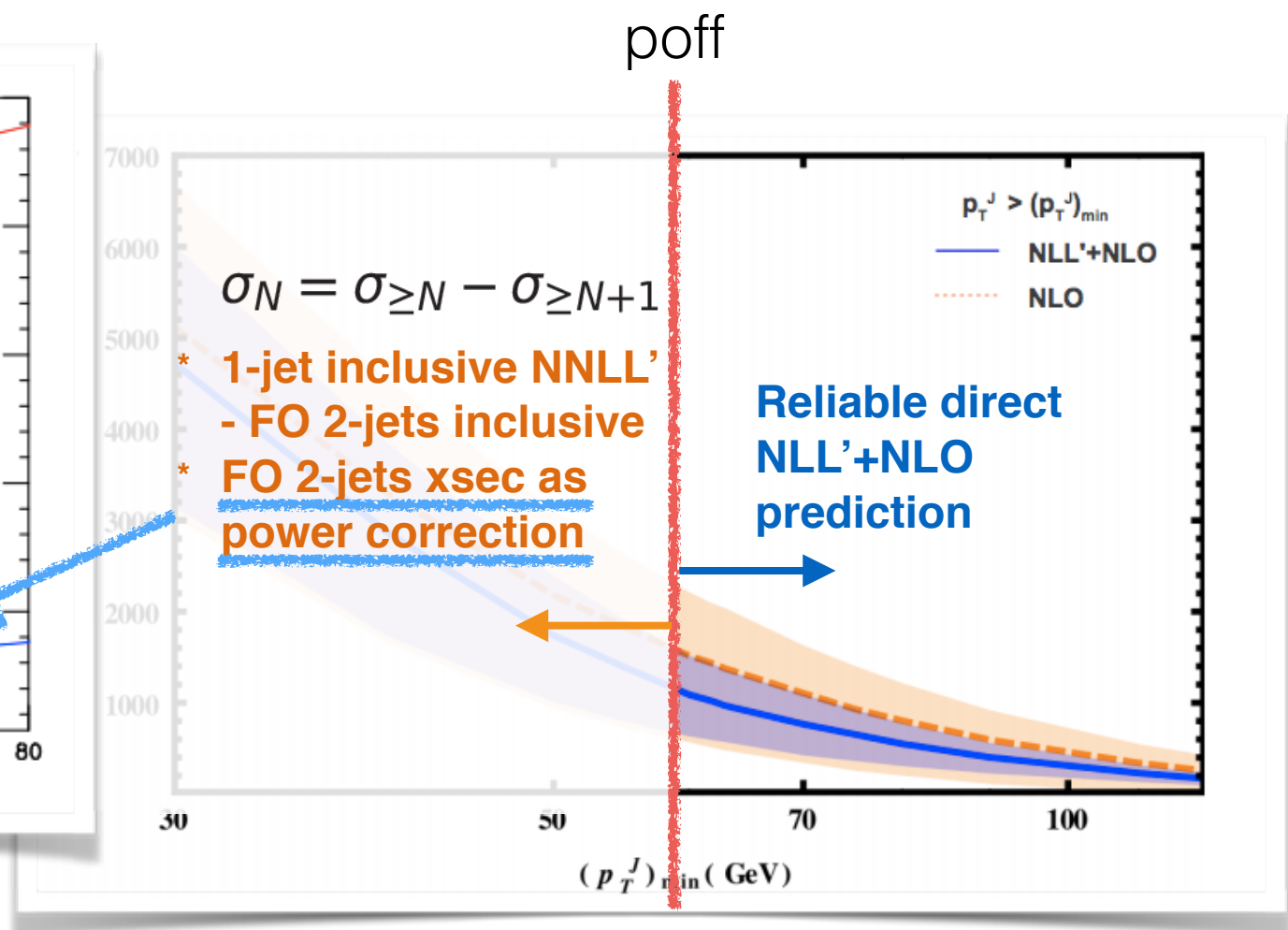
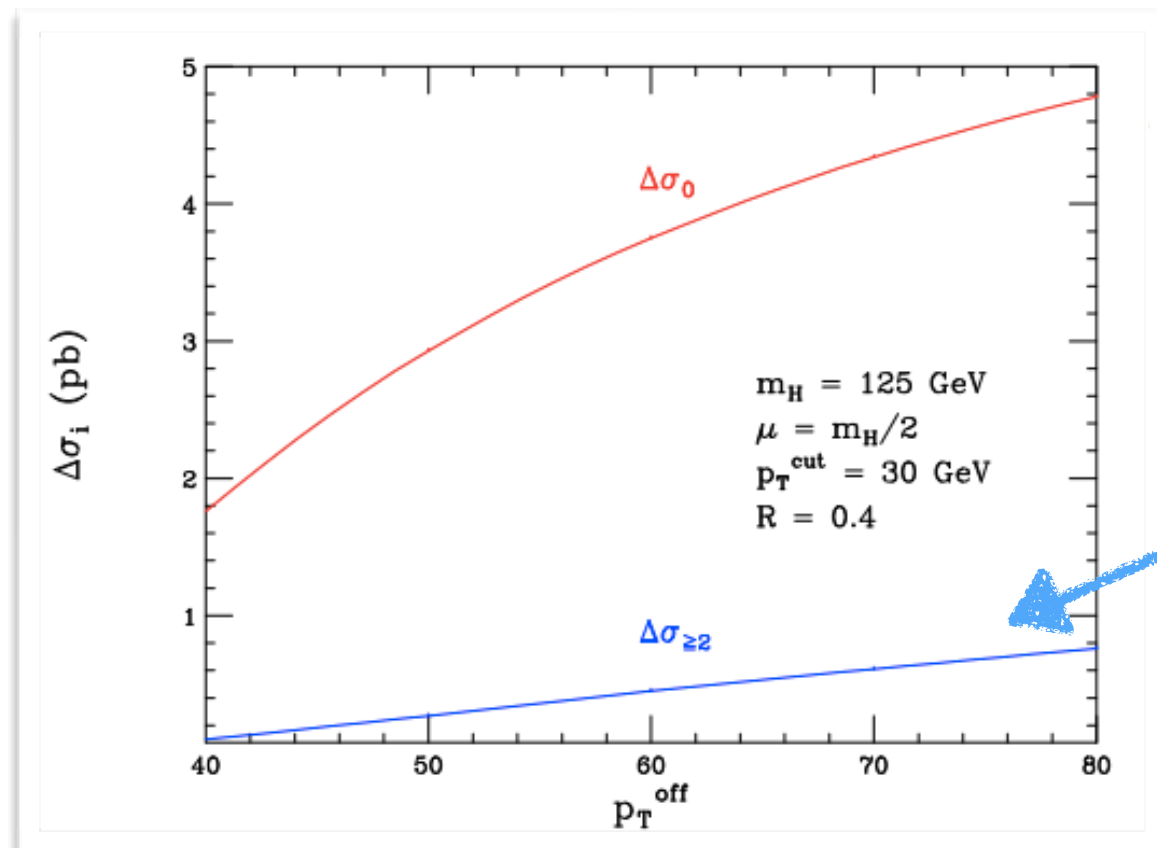
[Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]



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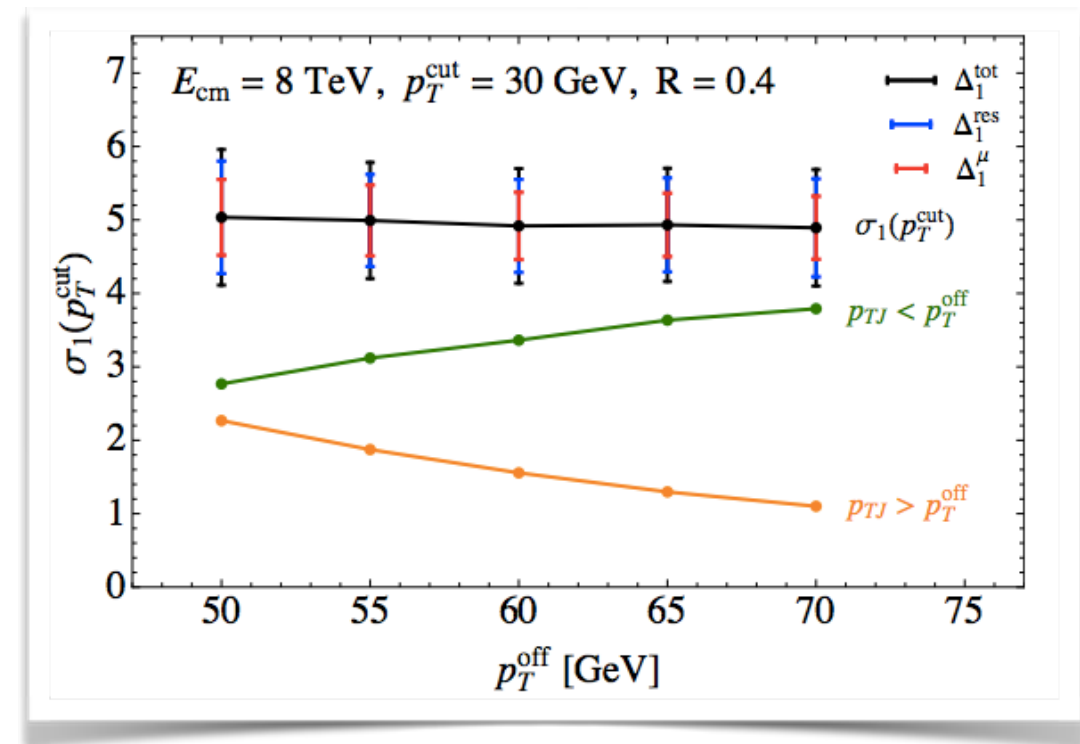
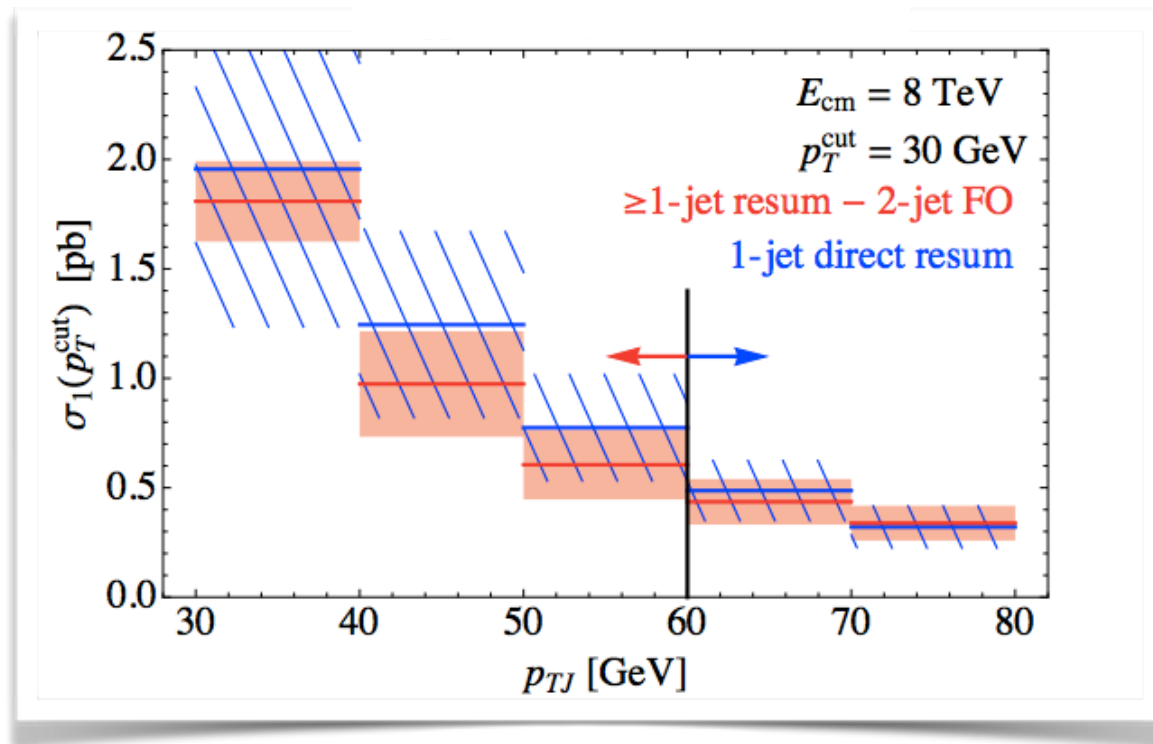


H + 0-jets and H + 1-jet

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[Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]

- testing matching



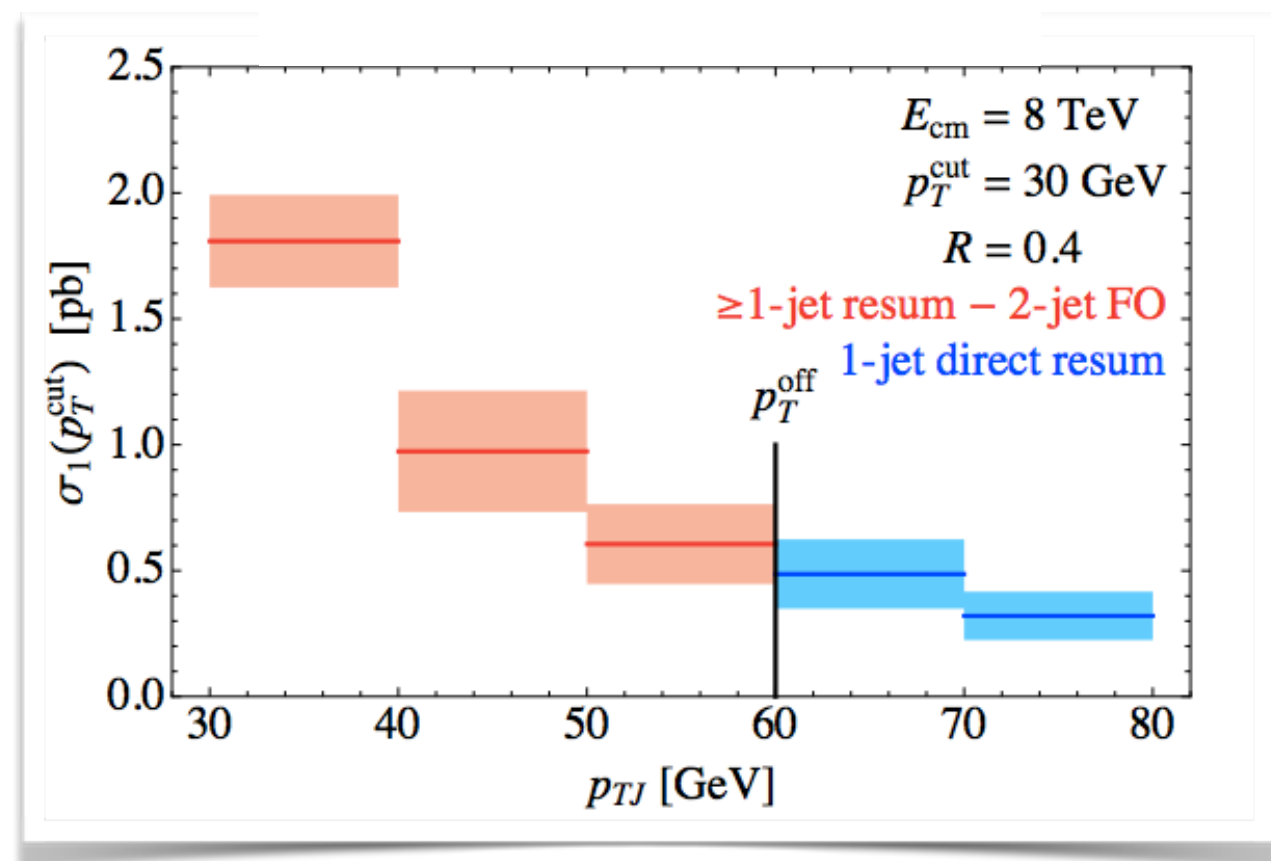
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[Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]

- pTJ spectrum

- NNLO H
- NLO 2-jets



H + 0-jets and H + 1-jet

- Combining jet bins

[Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]

- covariance matrices

- a general uncertainty parameterization

yield uncertainty (collective scale variation) + migration uncertainty (fully anti-correlated)

$$\begin{array}{l}
 \text{0-jets} \\
 \text{1-jet} \\
 \text{>2-jets}
 \end{array}
 \begin{pmatrix}
 (\Delta_0^y)^2 & \Delta_0^y \Delta_1^y & \Delta_0^y \Delta_{\geq 2}^y \\
 \Delta_0^y \Delta_1^y & (\Delta_1^y)^2 & \Delta_1^y \Delta_{\geq 2}^y \\
 \Delta_0^y \Delta_{\geq 2}^y & \Delta_1^y \Delta_{\geq 2}^y & (\Delta_{\geq 2}^y)^2
 \end{pmatrix}
 :
 \begin{pmatrix}
 \Delta_{0 \text{ cut}}^2 & -\Delta_{0 \text{ cut}}^2 + C_{01 \text{ cut}} & -C_{01 \text{ cut}} \\
 -\Delta_{0 \text{ cut}}^2 + C_{01 \text{ cut}} & \Delta_{0 \text{ cut}}^2 + \Delta_{1 \text{ cut}}^2 - 2C_{01 \text{ cut}} & -\Delta_{1 \text{ cut}}^2 + C_{01 \text{ cut}} \\
 -C_{01 \text{ cut}} & -\Delta_{1 \text{ cut}}^2 + C_{01 \text{ cut}} & \Delta_{1 \text{ cut}}^2
 \end{pmatrix}$$

H + 0-jets and H + 1-jet

- Combining jet bins

[Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]

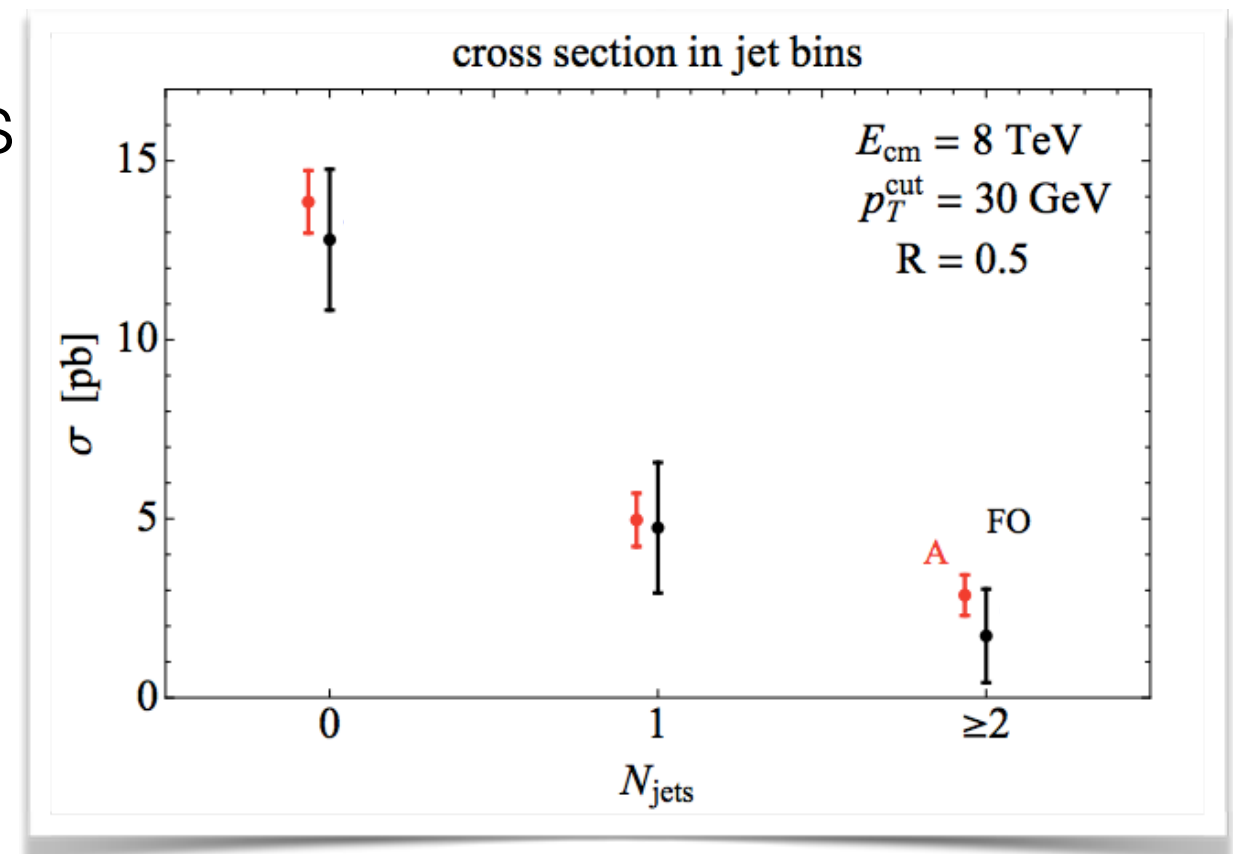
- covariance matrices
- a general uncertainty parameterization

$$C^{\text{ATLAS}} = \begin{pmatrix} 1.49 & -0.39 & 0.20 \\ -0.39 & 0.88 & -0.04 \\ 0.20 & -0.04 & 0.32 \end{pmatrix} \text{ pb}^2$$

$$C^{\text{CMS}} = \begin{pmatrix} 0.76 & 0.09 & 0.20 \\ 0.09 & 0.55 & 0.01 \\ 0.21 & 0.01 & 0.32 \end{pmatrix} \text{ pb}^2$$

H + 0-jets and H + 1-jet

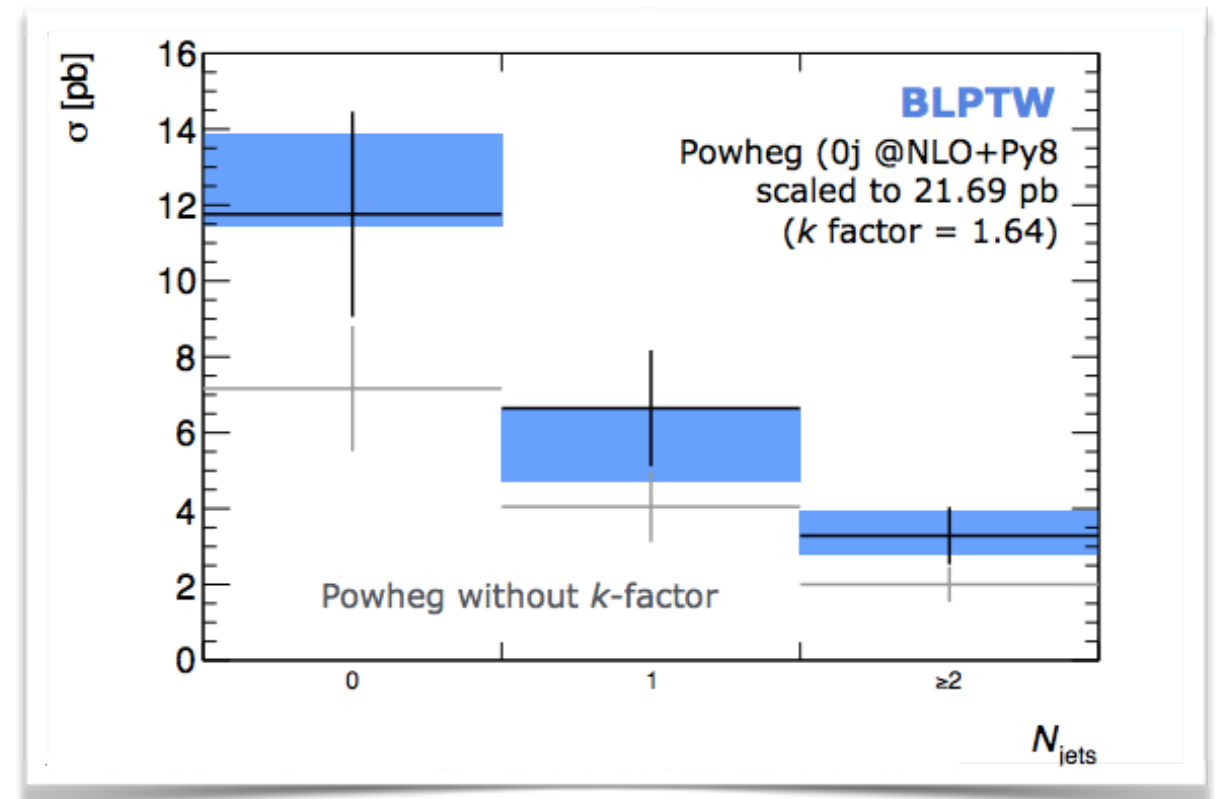
- Combining jet bins [Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]
- covariance matrices
- any uncertainty can be calculated from the matrices
- jet bin uncertainties



H + 0-jets and H + 1-jet

- Combining jet bins
- covariance matrices
- any uncertainty can be calculated from the matrices
- jet bin uncertainties

[Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]



[Gillberg - talk @ Jet binning uncertainties in ggF, 2014]

H + 0-jets and H + 1-jet

- Combining jet bins

[Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]

- covariance matrices

- any uncertainty can be calculated from the matrices

- jet bin uncertainties

- WW signal strength $\mu = \frac{\sigma_{\text{obs}}}{\sigma_{\text{exp}}}$

$$\frac{\Delta^{\text{th}, y} \mu}{\mu} = \frac{\Delta^{\text{th}, y} \sigma_{\text{exp}}}{\sigma_{\text{exp}}}$$

$$\Delta\sigma_{\text{exp}} = \left[(\epsilon_0^{\text{exp}})^2 \Delta_0^2 + (\epsilon_1^{\text{exp}})^2 \Delta_1^2 + 2\epsilon_0^{\text{exp}} \epsilon_1^{\text{exp}} \text{cov}(0, 1) \right]^{1/2}$$

H + 0-jets and H + 1-jet

- Combining jet bins [Boughezal, XL, Petriello, Tackmann, Walsh - 1312.4535]
- covariance matrices
- any uncertainty can be calculated from the matrices
- jet bin uncertainties
- WW signal strength

$$\Delta_{\text{FO}}^{\text{th}, y} \mu = 0.12$$



$$\Delta_{\text{A}}^{\text{th}, y} \mu = 0.07$$

Table 13: Leading uncertainties on the signal strength μ for the combined 7 and 8 TeV analysis.

Category	Source	Uncertainty, up (%)	Uncertainty, down (%)
Statistical	Observed data	+21	-21
Theoretical	Signal yield ($\sigma \cdot \mathcal{B}$)	+12	-9
Theoretical	WW normalisation	+12	-12
Experimental	Objects and DY estimation	+9	-8
Theoretical	Signal acceptance	+9	-7
Experimental	MC statistics	+7	-7
Experimental	W+ jets fake factor	+5	-5
Theoretical	Backgrounds, excluding WW	+5	-4
Luminosity	Integrated luminosity	+4	-4
Total		+32	-29

Reduced by nearly a factor of 2!

Conclusions

- Formalisms for exclusive 0-jets and 1-jet bin cross sections have been built up
- Systematic scheme for combining 0-jets and 1-jet bins have been set up
 - can be applied directly to Higgs analyses
 - halves the theoretical uncertainties
 - can be applied to $W/Z + \text{jets}$ as a testing ground

Thanks