

# Flavor physics in the LHC era

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**Alexey A. Petrov**

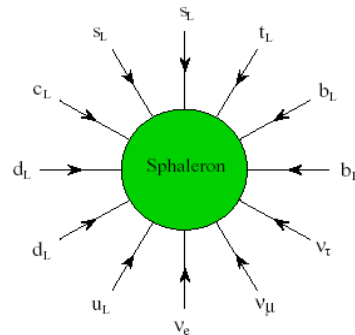
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# 1. Introduction: building the Universe

## ★ Sakharov's conditions for matter-antimatter asymmetry of the Universe

- ✓ Baryon (and lepton) number - violating processes  
to **generate** asymmetry

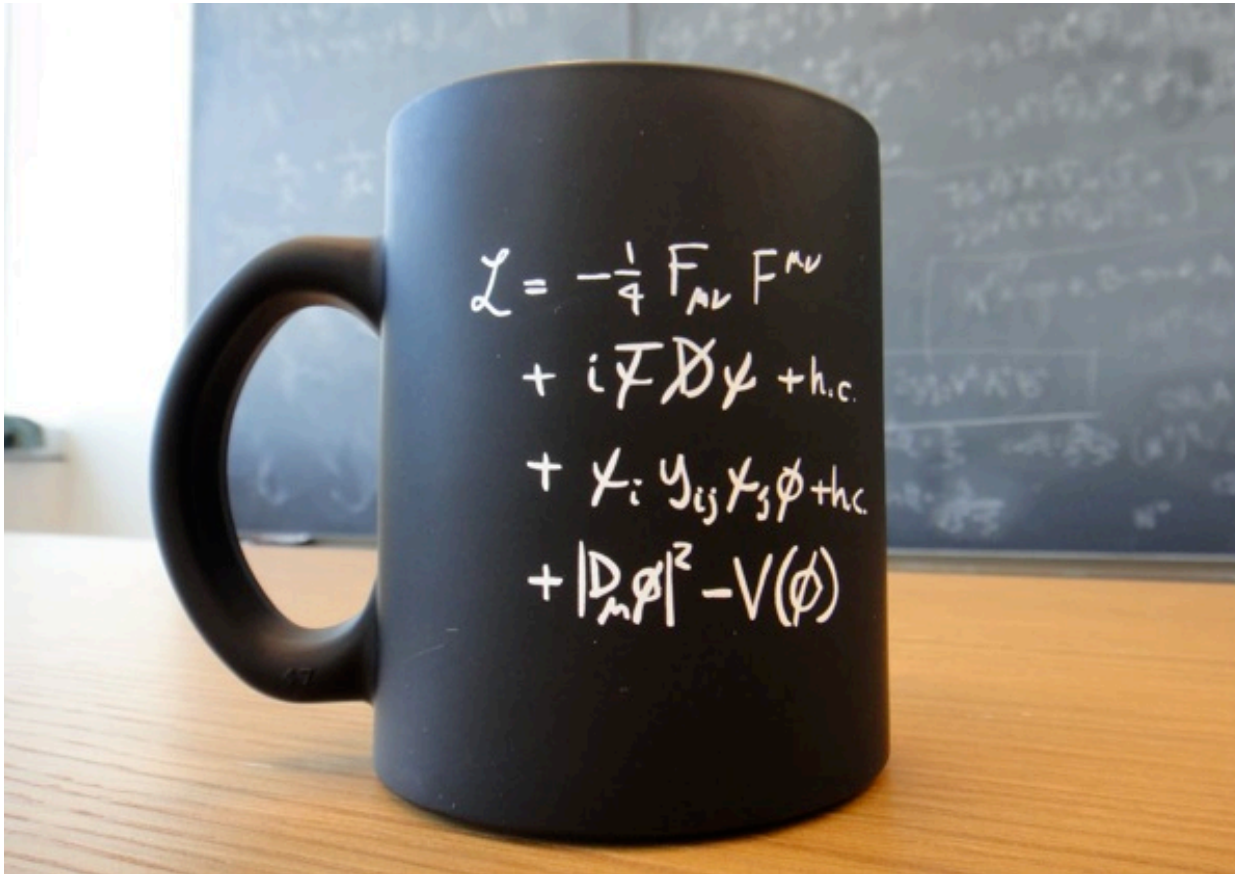


$$\Delta B = 3, \Delta L = 3, \\ B - L \text{ conserved}$$

- ✓ Universe that evolves out of thermal equilibrium  
to **keep** asymmetry from **being washed out**
- ✓ “Microscopic CP-violation”  
to **keep** asymmetry from **being compensated in the “anti-world”**

This CAN be tested experimentally

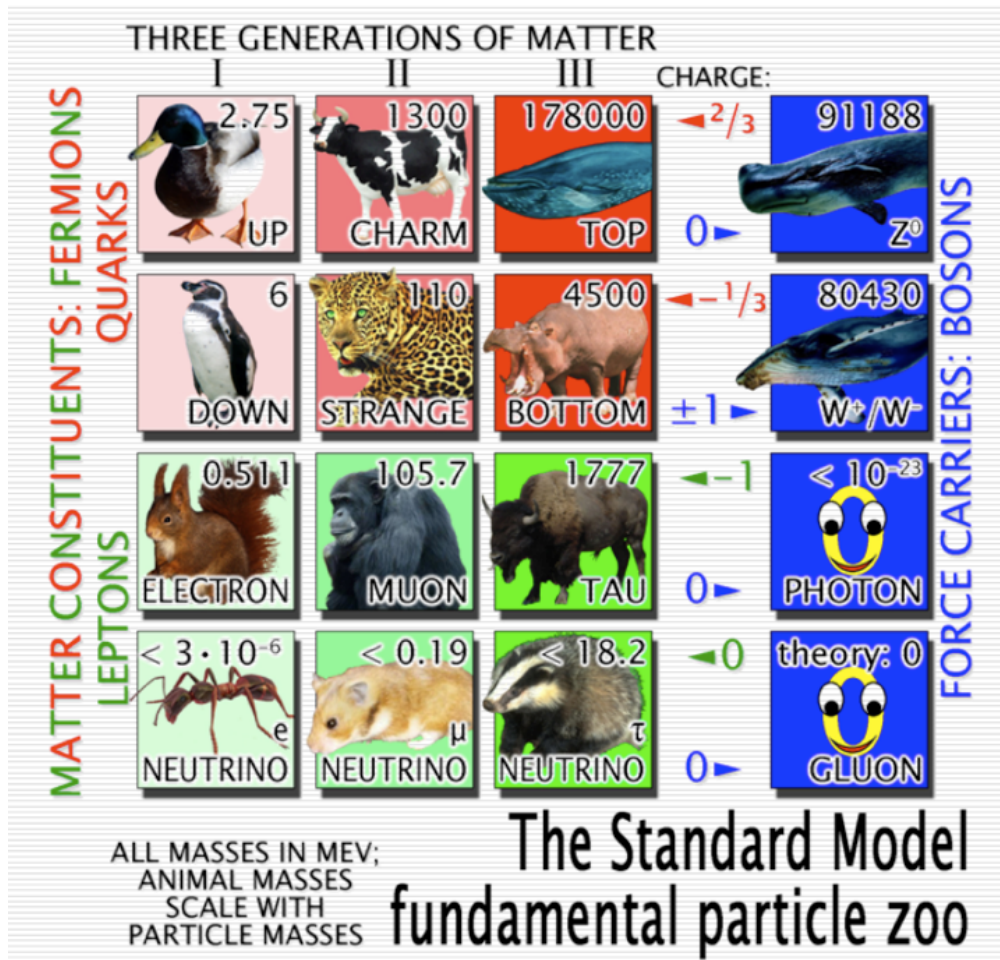
# SM is a very constrained theory



CKM mechanism for SM CP-violation has been established



# Matter sector: experimental data



E. Lunghi

## ★ Ratios of masses of quarks and leptons

- quarks

$$\frac{m_d}{m_u} \simeq 2, \quad \frac{m_s}{m_d} \simeq 21, \\ \frac{m_t}{m_c} \simeq 267, \quad \frac{m_c}{m_u} \simeq 431, \quad \frac{m_t}{m_u} \simeq 1.2 \times 10^5.$$

- leptons

$$\frac{m_\tau}{m_\mu} \simeq 17, \quad \frac{m_\mu}{m_e} \simeq 207.$$

## ★ Quark mixing (CKM) matrix parameters

$$V_{ud} \sim 1, V_{us} \sim 0.2, V_{cb} \sim 0.04, V_{ub} \sim 0.004$$

## Flavor Problem:

- ★ Why generations? Why only 3? Are there only 3?
- ★ Why hierarchies of masses and mixings?
- ★ Can there be transitions between quarks/leptons of the same charge but different generations?

# Solutions to the flavor problem?



*"Frankly, I even find it hard to believe  
some of the things I've been coming up with."*

## 2. "Fundamental" flavor physics: model building

★ GUT models: leptonic/quark Yukawas are related

★ Flavor symmetries

SM Lagrangian is  $SU(3)^5$ -invariant in the limit  $y_i \rightarrow 0$

- Yukawas arise as a result of spontaneous breaking of a subgroup of  $SU(3)^5$ ?

- continuous flavor symmetries

- discrete flavor symmetries

- accidental flavor symmetries

- numerology?  $m_e + m_\mu + m_\tau = \frac{2}{3}(\sqrt{m_e} + \sqrt{m_\mu} + \sqrt{m_\tau})^2$

★ Dynamical approaches

★ Geometric approaches (localization in extra dimension)

# Dynamical mechanisms: 2HDM

Notice that an extra scalar boson can help to solve the flavor puzzle:

$$\mathcal{L}_2 = -y_\psi \bar{\psi}_L \psi_R \phi_1 - y_\chi \bar{\chi}_L \chi_R \phi_2 + \text{h.c.}$$

Then assuming  $\tan \beta \gg 1$

$$\frac{m_\chi}{m_\psi} = \frac{y_\chi}{y_\psi} \frac{v_2}{v_1} = \frac{y_\chi}{y_\psi} \tan \beta \gg 1$$

So it looks like we can solve the flavor puzzle by just having more scalar bosons, letting all Yukawa couplings be  $\mathcal{O}(1)$  and  $\tan \beta \gg 1$

Top quark: Das, Kao, Phys. Lett. B 392 (1996) 106.

Xu, Phys. Rev. D44, R590 (1991).

Blechman, AAP, Yeghiyan, JHEP 1011 (2010) 075

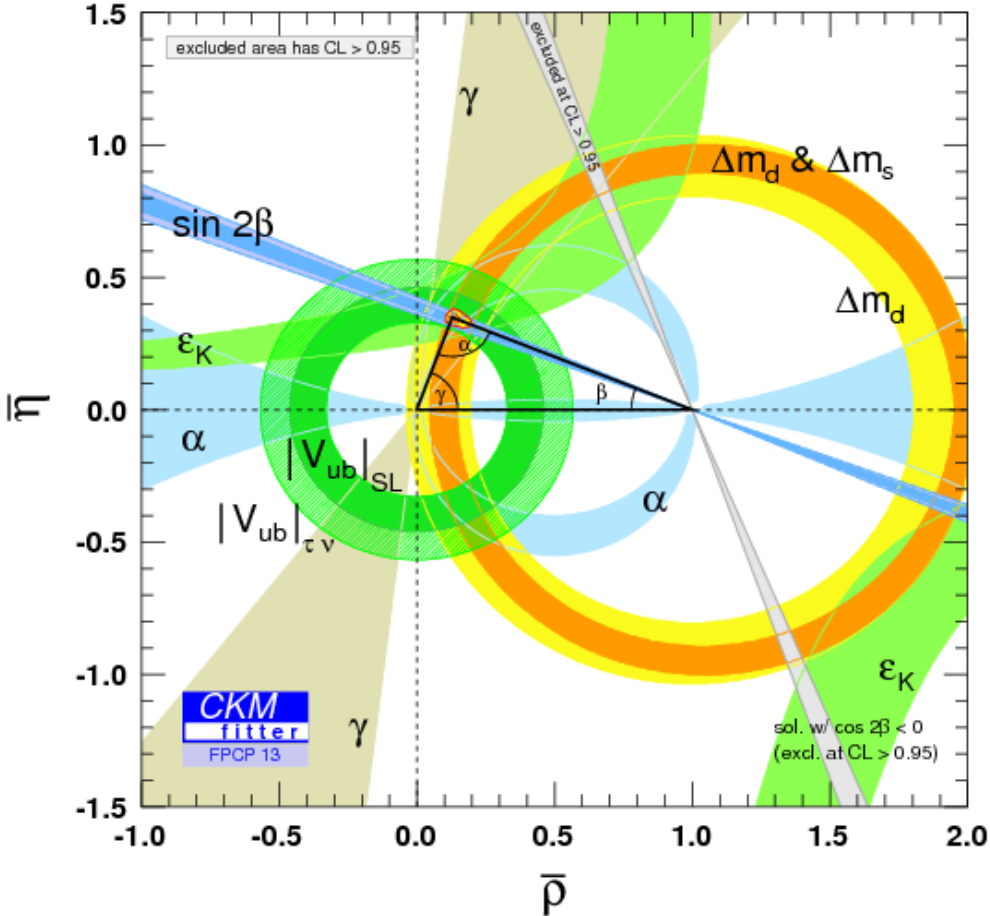
### 3. “Applied” flavor physics: model testing

★ How can one use flavor data to test New Physics models?

1. Processes **allowed** in the Standard Model **at tree level**
  - relations, valid in the SM, but not necessarily in general
  - processes where SM rates and uncertainties are known
  - example: CKM triangle relations
2. Processes **forbidden** in the Standard Model **at tree level**
  - example: penguin-mediated decays, B(D)-mixing, etc.
3. Processes **forbidden** in the Standard Model **to all orders**
  - example:  $D^0 \rightarrow p^+ \pi^- \nu$



### 3a. Processes allowed in the SM at tree level



## Some issues with exclusive/inclusive determinations of Vub...

## 3b. Processes forbidden in the SM at tree level

★ Let's look at some examples

- ★ Rare leptonic decays of  $B_s$  mesons
- ★  $B_s$  mixing: SM vs New Physics
- ★ CP-violating asymmetries in charm

## A. Rare leptonic decays of $B_s$ mesons

- Weak effective hamiltonian for  $B_s \rightarrow \mu^+ \mu^-$  is simple

$$\mathcal{H}_{eff} = \frac{G_F}{\sqrt{2}} V_{tb} V_{ts}^* C_{10}^{eff} \bar{s} \gamma_\mu (1 - \gamma_5) b \bar{\ell} \gamma^\mu \gamma_5 \ell$$

- Other operators (e.g.  $Q_9$ ) do not contribute due to vector current conservation

$$\langle 0 | \bar{s} \gamma_\mu (1 - \gamma_5) b | B_s(p) \rangle = -i f_B p_\mu$$



$$i p_\mu \langle \mu^+ \mu^- | \bar{\ell} \gamma^\mu \ell | B_s(p) \rangle = \langle \mu^+ \mu^- | \bar{\ell} \not{p} \ell | B_s \rangle = 0$$

$$i p_\mu \langle \mu^+ \mu^- | \bar{\ell} \gamma^\mu \gamma_5 \ell | B_s(p) \rangle = \langle \mu^+ \mu^- | \bar{\ell} \not{p} \gamma_5 \ell | B_s \rangle \propto m_\mu$$

One non-perturbative parameter: lattice

# Rare leptonic decays of $B_s$ mesons: SM

★ Very clean prediction in the Standard Model (one non-perturbative parameter)

$$\mathcal{B}r_{B_s \rightarrow \mu^+ \mu^-}^{(SM)} = \frac{1}{8\pi^5} \cdot \frac{M_{B_s}}{\Gamma_{B_s}} \cdot (G_F^2 M_W^2 m_\mu f_{B_s} |V_{ts}^* V_{tb}| \eta_Y Y(\bar{x}_t))^2 \left[ 1 - 4 \frac{m_\mu^2}{M_{B_s}^2} \right]^{1/2}$$

Buras, Carlucci,  
Gori, Isidori

$$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(SM)} = (3.65 \pm 0.06) R_{t\alpha} R_s \times 10^{-9} = (3.65 \pm 0.23) \times 10^{-9}$$

Bobeth, Gorbahn,  
Hermann, Misiak,  
Stamou, Steinhauser  
(2014)

$$R_s = \left[ \frac{f_{B_s} [MeV]}{227.7} \right]^2 \left[ \frac{|V_{cb}|}{0.0424} \right]^2 \left[ \frac{|V_{tb}^* V_{ts} / V_{cb}|}{0.980} \right]^2 \frac{\tau_{B_s} [ps]}{1.615} \quad R_{t\alpha} = R_t^{3.06} R_\alpha^{-0.18}$$

$$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(LD)} \sim 6 \times 10^{-11}$$

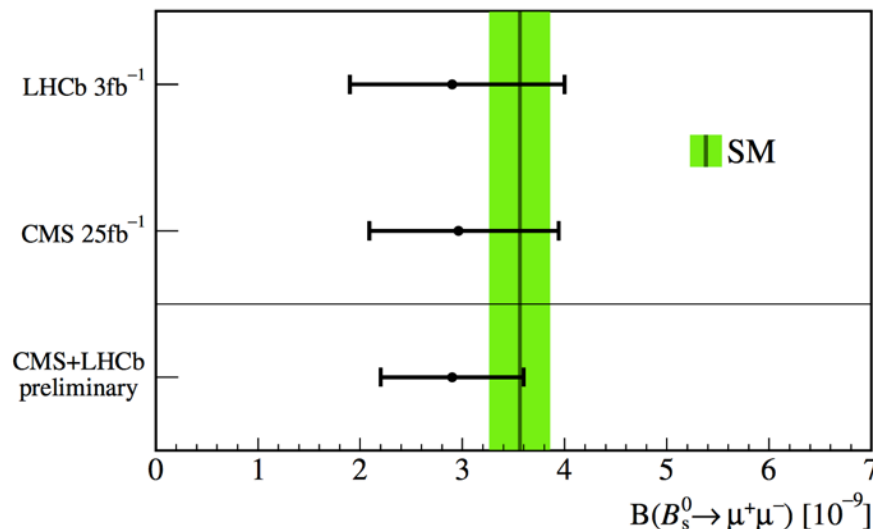
Golowich, Hewett,  
Pakvasa, AAP, Yeghiyan

Experiment (LHCb/CMS):  $\overline{\mathcal{B}}_{s\mu} = (2.9 \pm 0.7) \times 10^{-9}, \quad \overline{\mathcal{B}}_{d\mu} = (3.6_{-1.4}^{+1.6}) \times 10^{-10}.$



# Rare leptonic decays of $B_s$ mesons: SM

## ➤ Experiment:



## ➤ Comments:

★ Standard Model rate for  $B_s \rightarrow \mu^+\mu^-$  is known at NNLO in QCD + two loops in EW

★ Standard Model rate for  $B_s \rightarrow \mu^+\mu^-$  is helicity suppressed

- additional photon emission is enhanced by  $\frac{\mathcal{B}(B_s \rightarrow \gamma \ell^+ \ell^-)}{\mathcal{B}(B_s \rightarrow \ell^+ \ell^-)} \propto \alpha \frac{m_B^2}{m_\ell^2}$

★  $B_s \rightarrow \mu^+\mu^-$  is not sensitive to vector-like New Physics (e.g. vector  $Z'$ )

Aditya, Healey, AAP  
arXiv:1212.4166 [hep-ph]

Many NP models give contributions to both  $B_s$ -mixing and  $B_s \rightarrow \mu^+\mu^-$  decay: **correlate!!!**

# Mixing vs rare decays: some models

► Consider RPV SUSY:  $\mathcal{W}_{\mathcal{R}} = \frac{1}{2}\lambda_{ijk}L_iL_jE_k^c + \lambda'_{ijk}L_iQ_jD_k^c + \frac{1}{2}\lambda''_{ijk}U_i^cD_j^cD_k^c$ .

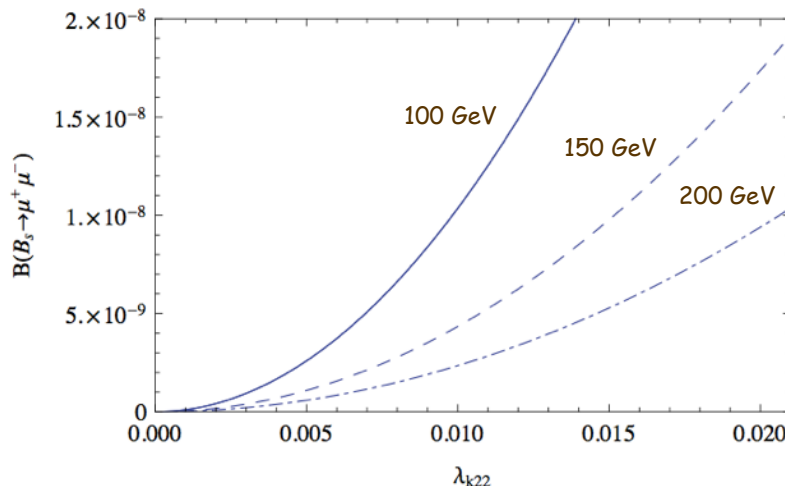
Mixing:  $\mathcal{L}_R = -\lambda'_{i23}\tilde{\nu}_{i_L}\bar{b}_R s_L - \lambda'_{i32}\tilde{\nu}_{i_L}\bar{s}_R b_L + \text{H.c.},$

$$\Delta M_{B_s}^{(\mathcal{R})} = \frac{5}{24}f_{B_s}^2 M_{B_s} F(C_3, B_3) \sum_i \frac{\lambda'_{i23}\lambda_{i32}^*}{M_{\tilde{\nu}_i}^2},$$

Rare decay:  $\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(\mathcal{R})} = \frac{f_{B_s}^2 M_{B_s}^3}{64\pi\Gamma_{B_s}} \left(\frac{M_{B_s}}{m_b}\right)^2 \left(1 - \frac{2m_\mu^2}{M_{B_s}^2}\right) \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} \times \left( \left| \sum_i \frac{\lambda_{i22}^* \lambda'_{i32}}{M_{\tilde{\nu}_i}^2} \right|^2 + \left| \sum_i \frac{\lambda_{i22} \lambda_{i23}^*}{M_{\tilde{\nu}_i}^2} \right|^2 \right).$

$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(\mathcal{R})} = k \frac{f_{B_s}^2 M_{B_s}^3}{64\pi\Gamma_{B_s}} \left(\frac{\lambda_{i22}\lambda'_{i32}}{M_{\tilde{\nu}_i}^2}\right)^2 \left(\frac{M_{B_s}}{m_b}\right)^2 \left(1 - \frac{2m_\mu^2}{M_{B_s}^2}\right) \times \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}},$

...assume that a single sneutrino dominates, neglect possible CP-violation...



$$\mathcal{B}_{B_s \rightarrow \mu^+ \mu^-}^{(\mathcal{R})} = \frac{3}{20\pi} \frac{M_{B_s}^2}{F(C_3, B_3)} \left(\frac{M_{B_s}}{m_b}\right)^2 \left(1 - \frac{2m_\mu^2}{M_{B_s}^2}\right) \times \sqrt{1 - \frac{4m_\mu^2}{M_{B_s}^2}} x_{B_s}^{(\mathcal{R})} \frac{\lambda_{k22}^2}{M_{\tilde{\nu}_i}^2}.$$

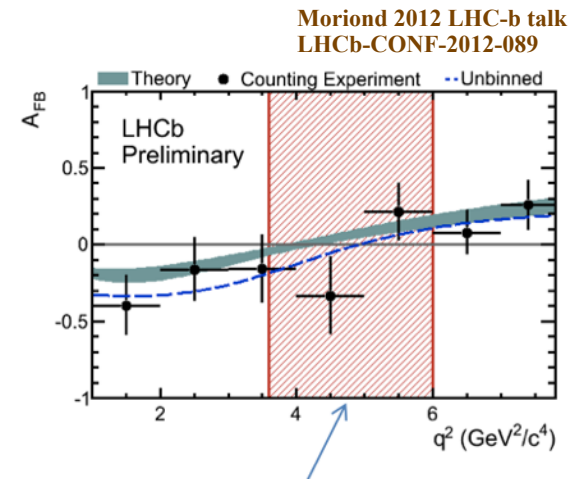
E. Golowich, J. Hewett, S. Pakvasa, A.A.P. and G. Yeghiyan PRD83, 114017 (2011)

# Other electroweak decays

## ► Important for studies of New Physics

- ★ the same current that generates  $B_s \rightarrow \mu^+ \mu^-$  decays also generates  $B \rightarrow K^{(*)} \mu^+ \mu^-$

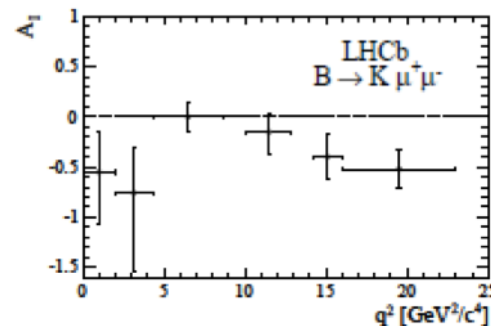
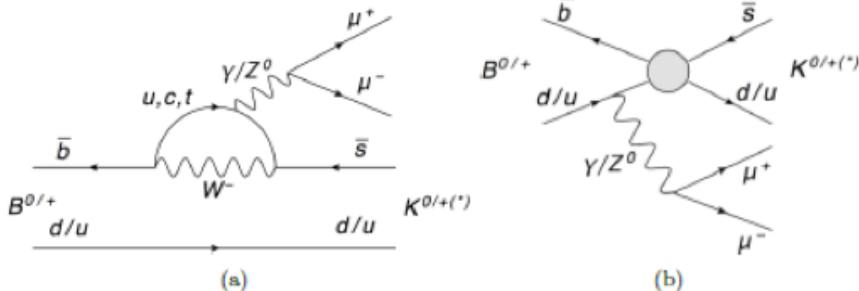
- decay has three particles in the final state: more observables: FB-, isospin, CP-asymmetries
- zero "crossing point" in  $A_{FB}$  is a probe of NP:  
SM predicts  $q_0^2 = 4 - 4.3 \text{ GeV}^2$  (Bobeth et al)  
LHCb measures:  $q_0^2 = 4.9^{+1.1}_{-1.3} \text{ GeV}^2$   
(some SUSY models predict no crossing at all!)



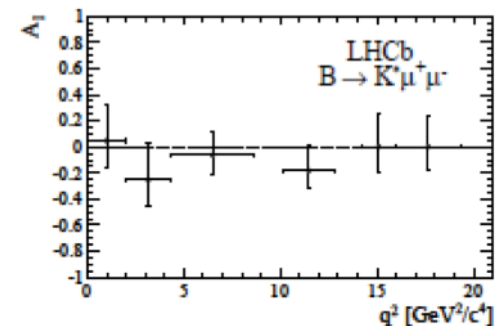
68% confidence interval in  
Zero crossing point from data.

## ★ Isospin asymmetries in $B \rightarrow K^{(*)} \mu^+ \mu^-$

- probes New Physics
- SM predicts (almost) zero
- LHCb measurement is consistent



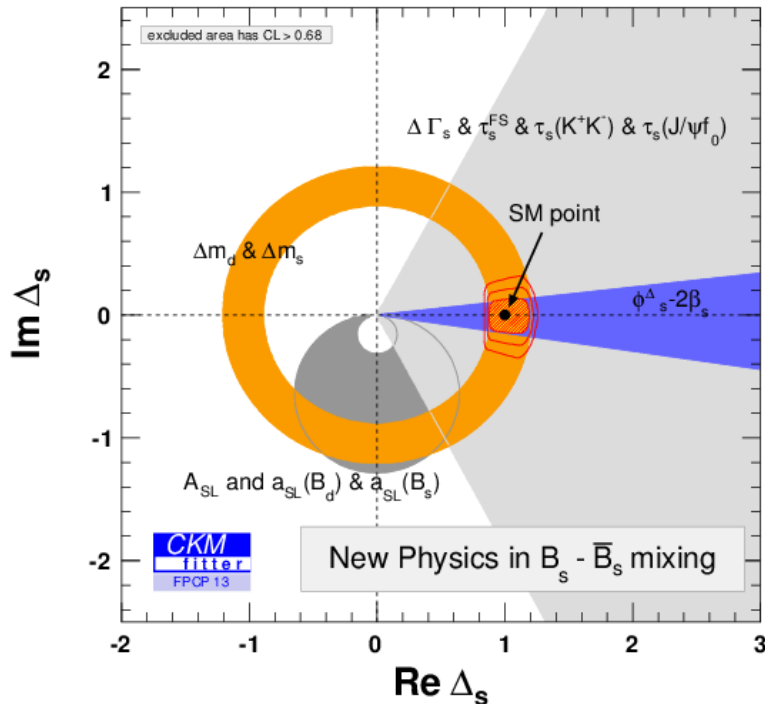
Negative with  $3.0\sigma$   
significance in  $16 < q^2 < 23$



consistent with zero

# B. Mixing in heavy hadrons

Mixing parameters are sensitive probes of new physics



Theoretical predictions?

★ Time development of  $B_s$  system

$$i \frac{d}{dt} \begin{pmatrix} B_q(t) \\ \bar{B}_q(t) \end{pmatrix} = \left[ M - \frac{i}{2} \Gamma \right]_{ij} \begin{pmatrix} B_q(t) \\ \bar{B}_q(t) \end{pmatrix}$$

★ Mixing parameters (concentrate on  $B_s$ )

$$\Delta M_{B_s} = 2 |M_{12}|, \quad \Delta \Gamma_{B_s} = \frac{4 \text{Re}(M_{12} \Gamma_{12}^*)}{\Delta M_{B_s}}$$

♦ NP in phase of  $\Delta M_{B_s}$ :

$$\Delta \Gamma_{B_s} = 2 |\Gamma_{12}| \cos 2\phi_s$$

♦ "direct" NP in  $\Delta \Gamma_{B_s}$ :

$$\Delta \Gamma_{B_s} = \Delta \Gamma_{B_s}^{SM} + \Delta \Gamma_{B_s}^{NP} \cos 2\phi'_s$$

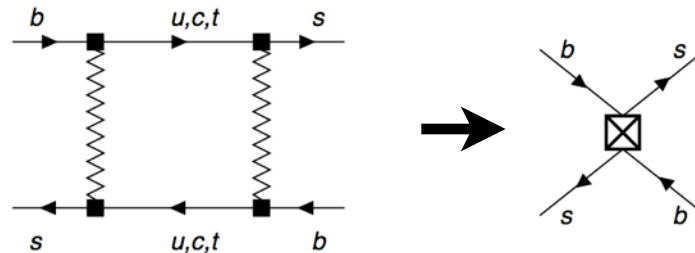
$\uparrow$   $\arg(M_{12})$   
 $\uparrow$   $\arg(\Gamma_{12})$



# Standard Model contributions

Both  $\Delta M_{B_s}$  and  $\Delta \Gamma_{B_s}$  can be computed in the limit  $m_b \rightarrow \infty$ :

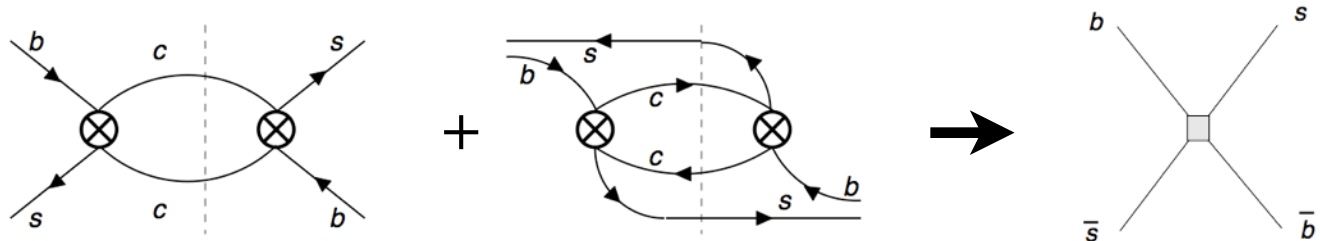
$\Delta M_{B_s}$ :



A. Buras, M. Jamin, P. Weisz

$$M_{12}(B_s) = \frac{G_F^2 M_{B_s}}{12\pi^2} M_W^2 (V_{tb} V_{ts}^*)^2 \hat{\eta}_B S_0(x_t) f_{B_s}^2 B$$

$\Delta \Gamma_{B_s}$ :



A. Lenz, U. Nierste

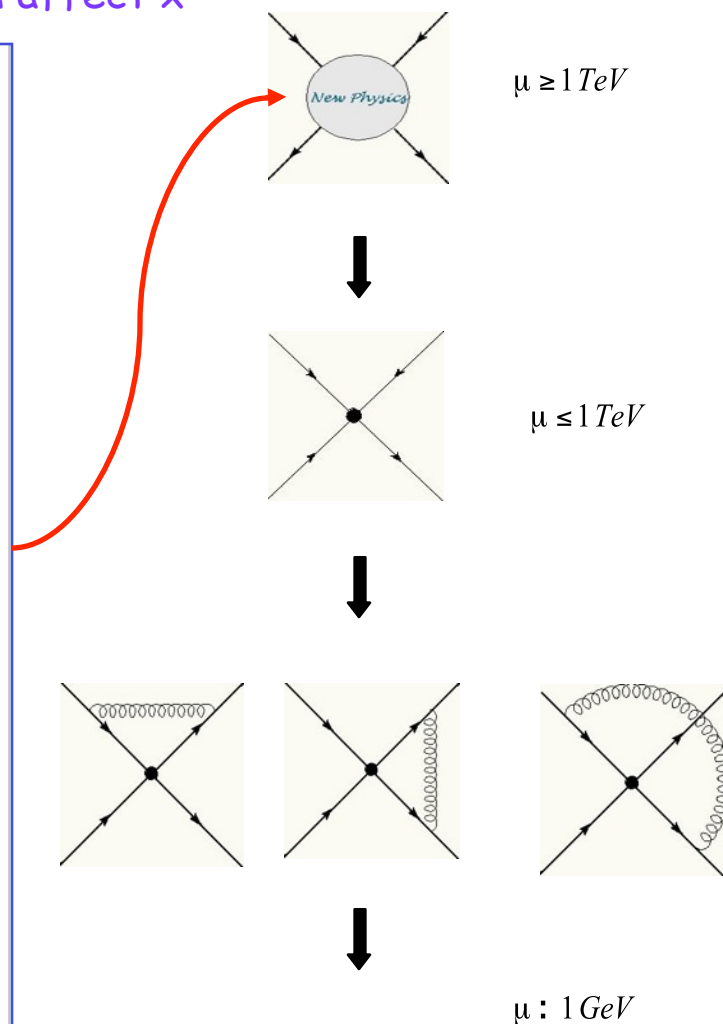
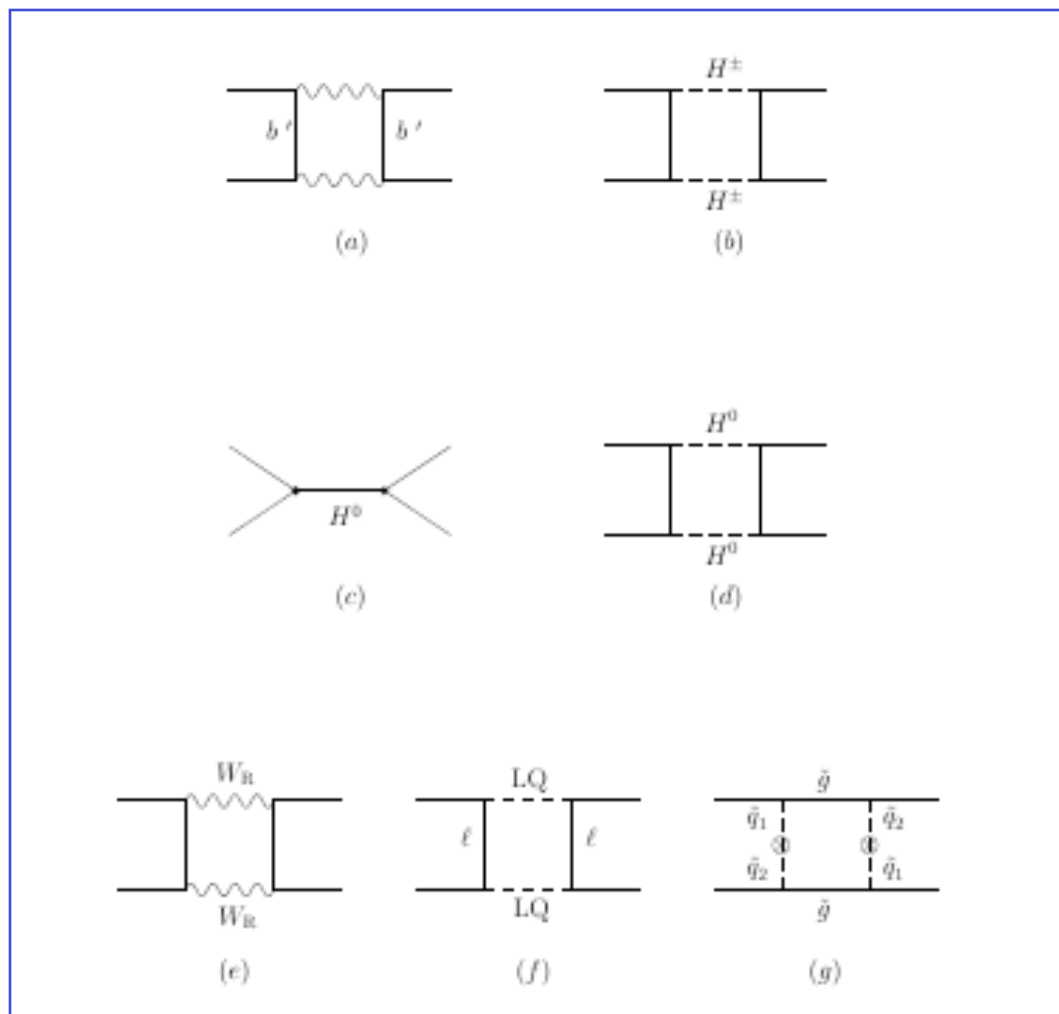
$$\Gamma_{21}(B_s) = \sum_i \frac{C_k(\mu)}{m_h^k} \langle B_s | \mathcal{O}_k^{\Delta B=2}(\mu) | \bar{B}_s \rangle.$$

$$\frac{\Delta \Gamma_s}{\Gamma_s} \approx 0.137 \pm 0.027$$

Lattice estimates for matrix elements?

# Constraints on NP from B(D)-mixing?

★ Multitude of various models of New Physics can affect  $x$



# Generic restrictions on NP from $D\bar{D}$ -mixing

★ Comparing to experimental value of  $x$ , obtain constraints on NP models

- assume  $x$  is dominated by the New Physics model
- assume no accidental strong cancellations b/w SM and NP

$$\mathcal{H}_{NP}^{\Delta C=2} = \frac{1}{\Lambda_{NP}^2} \sum_{i=1}^8 z_i(\mu) Q'_i$$

$$\begin{aligned} Q_1^{cu} &= \bar{u}_L^\alpha \gamma_\mu c_L^\alpha \bar{u}_L^\beta \gamma^\mu c_L^\beta, \\ Q_2^{cu} &= \bar{u}_R^\alpha c_L^\alpha \bar{u}_R^\beta c_L^\beta, \\ Q_3^{cu} &= \bar{u}_R^\alpha c_L^\beta \bar{u}_R^\beta c_L^\alpha, \end{aligned} + \left\{ \begin{array}{c} L \\ \updownarrow \\ R \end{array} \right\} + \begin{aligned} Q_4^{cu} &= \bar{u}_R^\alpha c_L^\alpha \bar{u}_L^\beta c_R^\beta, \\ Q_5^{cu} &= \bar{u}_R^\alpha c_L^\beta \bar{u}_L^\beta c_R^\alpha, \end{aligned}$$

★ ... which are

$$\begin{aligned} |z_1| &\lesssim 5.7 \times 10^{-7} \left( \frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_2| &\lesssim 1.6 \times 10^{-7} \left( \frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_3| &\lesssim 5.8 \times 10^{-7} \left( \frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_4| &\lesssim 5.6 \times 10^{-8} \left( \frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2, \\ |z_5| &\lesssim 1.6 \times 10^{-7} \left( \frac{\Lambda_{NP}}{1 \text{ TeV}} \right)^2. \end{aligned}$$

New Physics is either at a very high scales

tree level:  $\Lambda_{NP} \geq (4 - 10) \times 10^3 \text{ TeV}$

loop level:  $\Lambda_{NP} \geq (1 - 3) \times 10^2 \text{ TeV}$

or have highly suppressed couplings to charm!

Gedalia, Grossman, Nir, Perez  
Phys.Rev.D80, 055024, 2009

E.Golowich, J. Hewett, S. Pakvasa and A.A.P.  
Phys. Rev. D76:095009, 2007

★ Constraints on particular NP models available

# Summary: New Physics in mixing

Model	Approximate Constraint
Fourth Generation (Fig. 2)	$ V_{ub}V_{cb}  \cdot m_b < 0.5 \text{ (GeV)}$
$Q = -1/3$ Singlet Quark (Fig. 4)	$s_2 \cdot m_S < 0.27 \text{ (GeV)}$
$Q = +2/3$ Singlet Quark (Fig. 6)	$ \lambda_{uc}  < 2.4 \cdot 10^{-4}$
Little Higgs	Tree: See entry for $Q = -1/3$ Singlet Quark Box: Region of parameter space can reach observed $x_D$
Generic $Z'$ (Fig. 7)	$M_{Z'}/C > 2.2 \cdot 10^3 \text{ TeV}$
Family Symmetries (Fig. 8)	$m_1/f > 1.2 \cdot 10^3 \text{ TeV}$ (with $m_1/m_2 = 0.5$ )
Left-Right Symmetric (Fig. 9)	No constraint
Alternate Left-Right Symmetric (Fig. 10)	$M_R > 1.2 \text{ TeV}$ ( $m_{D_1} = 0.5 \text{ TeV}$ ) $(\Delta m/m_{D_1})/M_R > 0.4 \text{ TeV}^{-1}$
Vector Leptoquark Bosons (Fig. 11)	$M_{VLQ} > 55(\lambda_{PP}/0.1) \text{ TeV}$
Flavor Conserving Two-Higgs-Doublet (Fig. 13)	No constraint
Flavor Changing Neutral Higgs (Fig. 15)	$m_H/C > 2.4 \cdot 10^3 \text{ TeV}$
FC Neutral Higgs (Cheng-Sher ansatz) (Fig. 16)	$m_H/ \Delta_{uc}  > 600 \text{ GeV}$
Scalar Leptoquark Bosons	See entry for RPV SUSY
Higgsless (Fig. 17)	$M > 100 \text{ TeV}$
Universal Extra Dimensions	No constraint
Split Fermion (Fig. 19)	$M/ \Delta y  > (6 \cdot 10^2 \text{ GeV})$
Warped Geometries (Fig. 21)	$M_1 > 3.5 \text{ TeV}$
Minimal Supersymmetric Standard (Fig. 23)	$ (\delta_{12}^u)_{LR,RL}  < 3.5 \cdot 10^{-2}$ for $\tilde{m} \sim 1 \text{ TeV}$ $ (\delta_{12}^u)_{LL,RR}  < .25$ for $\tilde{m} \sim 1 \text{ TeV}$
Supersymmetric Alignment	$\tilde{m} > 2 \text{ TeV}$
Supersymmetry with RPV (Fig. 27)	$\lambda'_{12k}\lambda'_{11k}/m_{\tilde{d}_{R,k}} < 1.8 \cdot 10^{-3}/100 \text{ GeV}$
Split Supersymmetry	No constraint

★ What about particular models?

- ✓ Considered 21 well-established models
- ✓ Only 4 models yielded no useful constraints

E.Golowich, J. Hewett, S. Pakvasa and A.A.P.  
Phys. Rev. D76:095009, 2007

Gedalia, Grossman, Nir, Perez  
arXiv:0906.1879 [hep-ph]

Bigi, Blanke, Buras, Recksiegel,  
JHEP 0907:097, 2009



## C. CP-violation in charmed mesons

★ Possible sources of CP violation in charm transitions:

★ CPV in  $\Delta c = 1$  decay amplitudes (“direct” CPV)

$$\Gamma(D \rightarrow f) \neq \Gamma(CP[D] \rightarrow CP[f])$$

★ CPV in  $D^0 - \bar{D}^0$  mixing matrix ( $\Delta c = 2$ ):

$$|D_{1,2}\rangle = p|D^0\rangle \pm q|\bar{D}^0\rangle \Rightarrow |D_{CP\pm}\rangle = \frac{1}{\sqrt{2}}(|D^0\rangle \pm |\bar{D}^0\rangle)$$

$$R_m^2 = |q/p|^2 = \left| \frac{2M_{12}^* - i\Gamma_{12}^*}{\Delta m - (i/2)\Delta\Gamma} \right|^2 = 1 + A_m \neq 1$$

★ CPV in the interference of decays with and without mixing

$$\lambda_f = \frac{q}{p} \frac{\overline{A_f}}{A_f} = R_m e^{i(\phi+\delta)} \left| \frac{\overline{A_f}}{A_f} \right|$$

★ One can separate various sources of CPV by customizing observables

# CP-violation I: indirect

★ Indirect CP-violation manifests itself in  $\overline{D}D$ -oscillations

- see time development of a D-system:

$$i \frac{d}{dt} |D(t)\rangle = \left( M - \frac{i}{2} \Gamma \right) |D(t)\rangle$$

$$\langle D^0 | \mathcal{H} | \overline{D}^0 \rangle = M_{12} - \frac{i}{2} \Gamma_{12} \quad \langle \overline{D}^0 | \mathcal{H} | D^0 \rangle = M_{12}^* - \frac{i}{2} \Gamma_{12}^*$$

★ Define mixing parameters

$$y_{12} \equiv |\Gamma_{12}|/\Gamma, \quad x_{12} \equiv 2|M_{12}|/\Gamma, \quad \phi_{12} \equiv \arg(M_{12}/\Gamma_{12})$$

Note: can be calculated in a given model

★ Assume that direct CP-violation is absent ( $\text{Im}(\Gamma_{12}^* \bar{A}_f/A_f) = 0$ ,  $|\bar{A}_f/A_f| = 1$ )

- can relate  $x, y, \phi, |q/p|$  to  $x_{12}, y_{12}$  and  $\phi_{12}$

$$xy = x_{12}y_{12} \cos \phi_{12}, \quad x^2 - y^2 = x_{12}^2 - y_{12}^2,$$

$$(x^2 + y^2)|q/p|^2 = x_{12}^2 + y_{12}^2 + 2x_{12}y_{12} \sin \phi_{12},$$

$$x^2 \cos^2 \phi - y^2 \sin^2 \phi = x_{12}^2 \cos^2 \phi_{12}.$$

★ Four “experimental” parameters related to three “theoretical” ones

- a “constraint” equation is possible

# CP-violation I: indirect

★ Relation; data from HFAG's compilation

$$\frac{x}{y} = \frac{1 - |q/p|}{\tan \phi} = -\frac{1}{2} \frac{A_m}{\tan \phi}$$

- $y/x \approx 0.8 \pm 0.3 \Rightarrow A_m \sim \tan \phi$
- CPV in mixing is comparable to CPV in the interference of decays with and w/out mixing

- aside: if  $|M_{12}| < |\Gamma_{12}|$ :

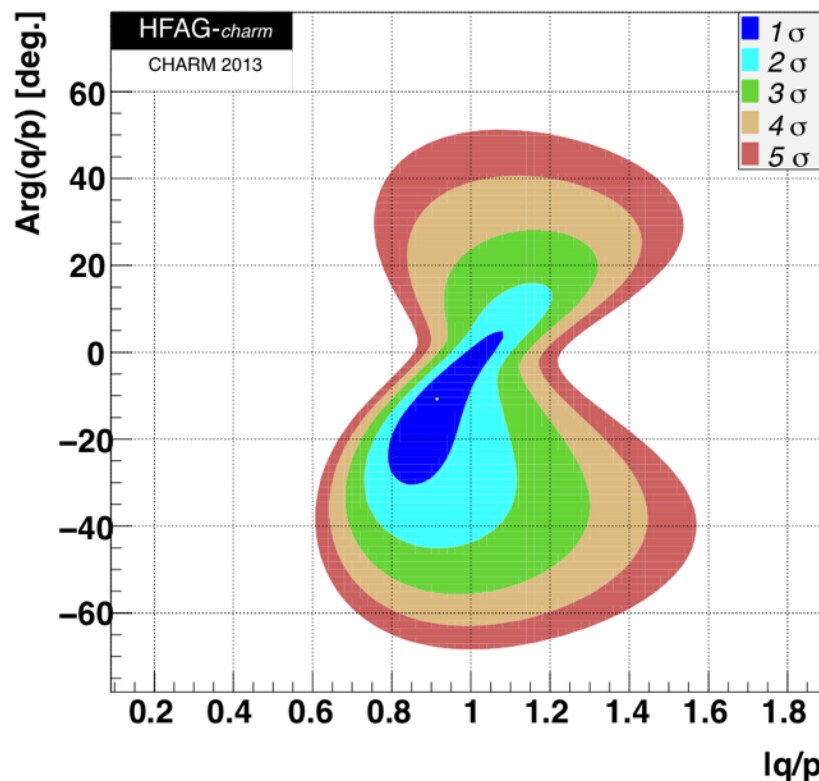
$$x/y = 2 |M_{12}/\Gamma_{12}| \cos \phi_{12},$$

$$A_m = 4 |M_{12}/\Gamma_{12}| \sin \phi_{12},$$

$$\phi = -2 |M_{12}/\Gamma_{12}|^2 \sin 2\phi_{12}.$$

**Note:** CPV is suppressed even if  $M_{12}$  is all NP!!!

Bergmann, Grossman, Ligeti, Nir, AAP  
PL B486 (2000) 418



★ With available experimental constraints on  $x$ ,  $y$ , and  $q/p$ , one can bound WCs of a generic NP Lagrangian -- bound any high-scale model of NP

# CP-violation I: indirect

- ★ Assume that **direct CP-violation is absent** ( $\text{Im}(\Gamma_{12}^* \bar{A}_f/A_f) = 0$ ,  $|\bar{A}_f/A_f| = 1$ )
  - experimental constraints on  $x, y, \varphi, |q/p|$  exist
  - can obtain generic constraints on Im parts of Wilson coefficients

$$\mathcal{H}_{NP}^{\Delta C=2} = \frac{1}{\Lambda_{NP}^2} \sum_{i=1}^8 z_i(\mu) Q'_i$$

- ★ In particular, from  $x_{12}^{\text{NP}} \sin \phi_{12}^{\text{NP}} \lesssim 0.0022$

$$\text{Im}(z_1) \lesssim 1.1 \times 10^{-7} \left( \frac{\Lambda_{\text{NP}}}{1 \text{ TeV}} \right)^2,$$

$$\text{Im}(z_2) \lesssim 2.9 \times 10^{-8} \left( \frac{\Lambda_{\text{NP}}}{1 \text{ TeV}} \right)^2,$$

$$\text{Im}(z_3) \lesssim 1.1 \times 10^{-7} \left( \frac{\Lambda_{\text{NP}}}{1 \text{ TeV}} \right)^2,$$

$$\text{Im}(z_4) \lesssim 1.1 \times 10^{-8} \left( \frac{\Lambda_{\text{NP}}}{1 \text{ TeV}} \right)^2,$$

$$\text{Im}(z_5) \lesssim 3.0 \times 10^{-8} \left( \frac{\Lambda_{\text{NP}}}{1 \text{ TeV}} \right)^2.$$

New Physics is either at a very high scales

tree level:  $\Lambda_{NP} \geq (4 - 10) \times 10^3 \text{ TeV}$

loop level:  $\Lambda_{NP} \geq (1 - 3) \times 10^2 \text{ TeV}$

or have highly suppressed couplings to charm!

- ★ Constraints on particular NP models possible as well

Gedalia, Grossman, Nir, Perez  
Phys.Rev.D80, 055024, 2009

Bigi, Blanke, Buras, Recksiegel,  
JHEP 0907:097, 2009



# CP-violation II: direct (charged D's)

- ★ At least two components of the transition amplitude are required

Look at charged D's (SCS):  $A(D^+ \rightarrow f) \equiv A_f = |A_1| e^{i\delta_1} e^{i\phi_1} + |A_2| e^{i\delta_2} e^{i\phi_2}$

Then, a charge asymmetry will provide a CP-violating observable

$$a_f = \frac{\Gamma(D^+ \rightarrow f) - \Gamma(D^- \rightarrow \bar{f})}{\Gamma(D^+ \rightarrow f) + \Gamma(D^- \rightarrow \bar{f})} = \frac{2 \operatorname{Im} A_1 A_2^* \sin(\delta_1 - \delta_2)}{|A_1|^2 + |A_2|^2 + 2 \operatorname{Re} A_1 A_2^* \cos(\delta_1 - \delta_2)}$$

...or, introducing  $r_f = |A_2/A_1|$ :  $a_f = 2r_f \sin\phi \sin\delta$

Prediction sensitive to  
details of hadronic  
model ( $\delta = \delta_1 - \delta_2$ )

- ★ Same formalism applies if one of the amplitudes is generated by New Physics



- need  $r_f \sim 1\%$  for O(1%) charge asymmetry **assuming** that  $\sin\delta \sim 1$
- need to efficiently detect neutrals (not good for LHCb)

# CP-violation II: direct

★ **IDEA:** consider the DIFFERENCE of decay rate asymmetries:  $D \rightarrow \pi\pi$  vs  $D \rightarrow KK$ !

For each final state the asymmetry

$D^0$ : no neutrals in the final state!

$$a_f = \frac{\Gamma(D \rightarrow f) - \Gamma(\bar{D} \rightarrow \bar{f})}{\Gamma(D \rightarrow f) + \Gamma(\bar{D} \rightarrow \bar{f})} \rightarrow a_f = a_f^d + a_f^m + a_f^i$$

direct
mixing
interference

★ A reason:  $a_{KK}^m = a_{\pi\pi}^m$  and  $a_{KK}^i = a_{\pi\pi}^i$  (for CP-eigenstate final states), so, ideally, mixing asymmetries cancel!

$$a_f^d = 2r_f \sin\phi_f \sin\delta_f$$

★ ... and the resulting DCPV asymmetry is  $\Delta a_{CP} = a_{KK}^d - a_{\pi\pi}^d \approx 2a_{KK}^d$  (double!)

$$A_{KK} = \frac{G_F}{\sqrt{2}} \lambda [(T + E + P_{sd}) + a\lambda^4 e^{-i\gamma} P_{bd}]$$

$$A_{\pi\pi} = \frac{G_F}{\sqrt{2}} \lambda [-(T + E) + P_{sd}) + a\lambda^4 e^{-i\gamma} P_{bd}]$$

★ ... so it is doubled in the limit of  $SU(3)_F$  symmetry

**$SU(3)$  is badly broken in D-decays**  
**e.g.  $\text{Br}(D \rightarrow KK) \sim 3 \text{ Br}(D \rightarrow \pi\pi)$**

# Experiment?

★ Experiment: the difference of CP-asymmetries:  $\Delta a_{CP} = a_{CP, KK} - a_{CP, \pi\pi}$

★ Earlier results (before 2013):

Experiment	$\Delta A_{CP}$
LHCb	$(-0.82 \pm 0.21 \pm 0.11)\%$
CDF	$(-0.62 \pm 0.21 \pm 0.10)\%$
Belle	$(-0.87 \pm 0.41 \pm 0.06)\%$
BaBar	$(+0.24 \pm 0.62 \pm 0.26)\%$

**Looks like CP is broken in  
charm transitions!  
Now what?**

★ Recent results (after 2013):

$D^{*+}$  tag (this analysis):  $\Delta A_{CP} = (-0.34 \pm 0.15 \text{ (stat.)} \pm 0.10 \text{ (syst.)}) \%$   
Semileptonic analysis:  $\Delta A_{CP} = (+0.49 \pm 0.30 \text{ (stat.)} \pm 0.14 \text{ (syst.)}) \%$   
Combination:  $\Delta A_{CP} = (-0.15 \pm 0.16) \%$

LHCb-CONF-2013-003

**Not so sure anymore...**

# Is it Standard Model or New Physics??

★ Is it Standard Model or New Physics? Theorists used to say...

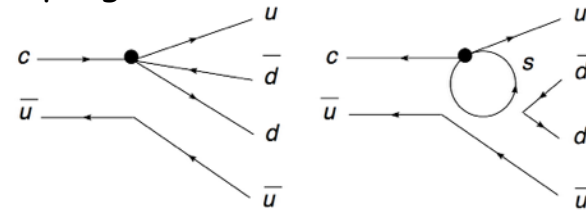
Naively, any CP-violating signal in the SM will be small, at most  $O(V_{ub} V_{cb}^* / V_{us} V_{cs}^*) \sim 10^{-3}$   
 Thus,  $O(1\%)$  CP-violating signal can provide a “smoking gun” signature of New Physics

...what do you say now?

★ assuming SU(3) symmetry,  $a_{CP}(\pi\pi) \sim a_{CP}(KK) \sim 0.15\%$ . Looks more or less 0.1%...

★ let us try Standard Model

- need to estimate size of penguin/penguin contractions vs. tree



- unknown penguin enhancement (similar to  $\Delta I = 1/2$ )

- SU(3) analysis: some ME are enhanced

Golden & Grinstein PLB 222 (1989) 501; Pirtshalava & Uttayarat 1112.5451

- unusually large  $1/m_c$  corrections

Isidori et al PLB 711 (2012) 46; Brod et al 1111.5000

- no assumptions, flavor-flow diagrams

Brod et al 1203.6659; Bhattacharya et al PRD 85 (2012) 054014;  
 Cheng & Chiang 1205.0580

# New Physics: operator analysis

★ Factorizing decay amplitudes, e.g.

$$\mathcal{H}_{|\Delta c|=1}^{\text{eff-NP}} = \frac{G_F}{\sqrt{2}} \sum_{i=1,2,5,6} \sum_q (C_i^q Q_i^q + C_i^{q'} Q_i^{q'}) + \frac{G_F}{\sqrt{2}} \sum_{i=7,8} (C_i Q_i + C_i' Q_i') + \text{H.c.}$$

$$Q_1^q = (\bar{u}q)_{V-A} (\bar{q}c)_{V-A}$$

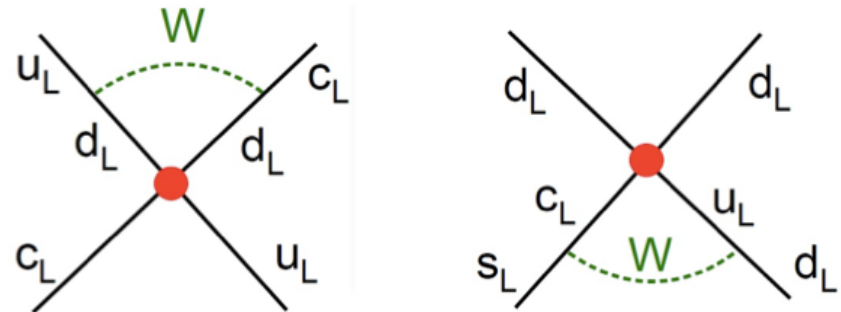
$$Q_2^q = (\bar{u}_\alpha q_\beta)_{V-A} (\bar{q}_\beta c_\alpha)_{V-A}$$

$$Q_5^q = (\bar{u}c)_{V-A} (\bar{q}q)_{V+A}$$

$$Q_6^q = (\bar{u}_\alpha c_\beta)_{V-A} (\bar{q}_\beta q_\alpha)_{V+A}$$

$$Q_7 = -\frac{e}{8\pi^2} m_c \bar{u} \sigma_{\mu\nu} (1 + \gamma_5) F^{\mu\nu} c$$

$$Q_8 = -\frac{g_s}{8\pi^2} m_c \bar{u} \sigma_{\mu\nu} (1 + \gamma_5) T^a G_a^{\mu\nu} c$$



Z. Ligeti, CHARM-2012

★ one can fit to  $\varepsilon'/\varepsilon$  and mass difference in D-anti-D-mixing

Gedalia, et al, arXiv:1202.5038

- LL are ruled out
- LR are borderline
- RR and dipoles are possible

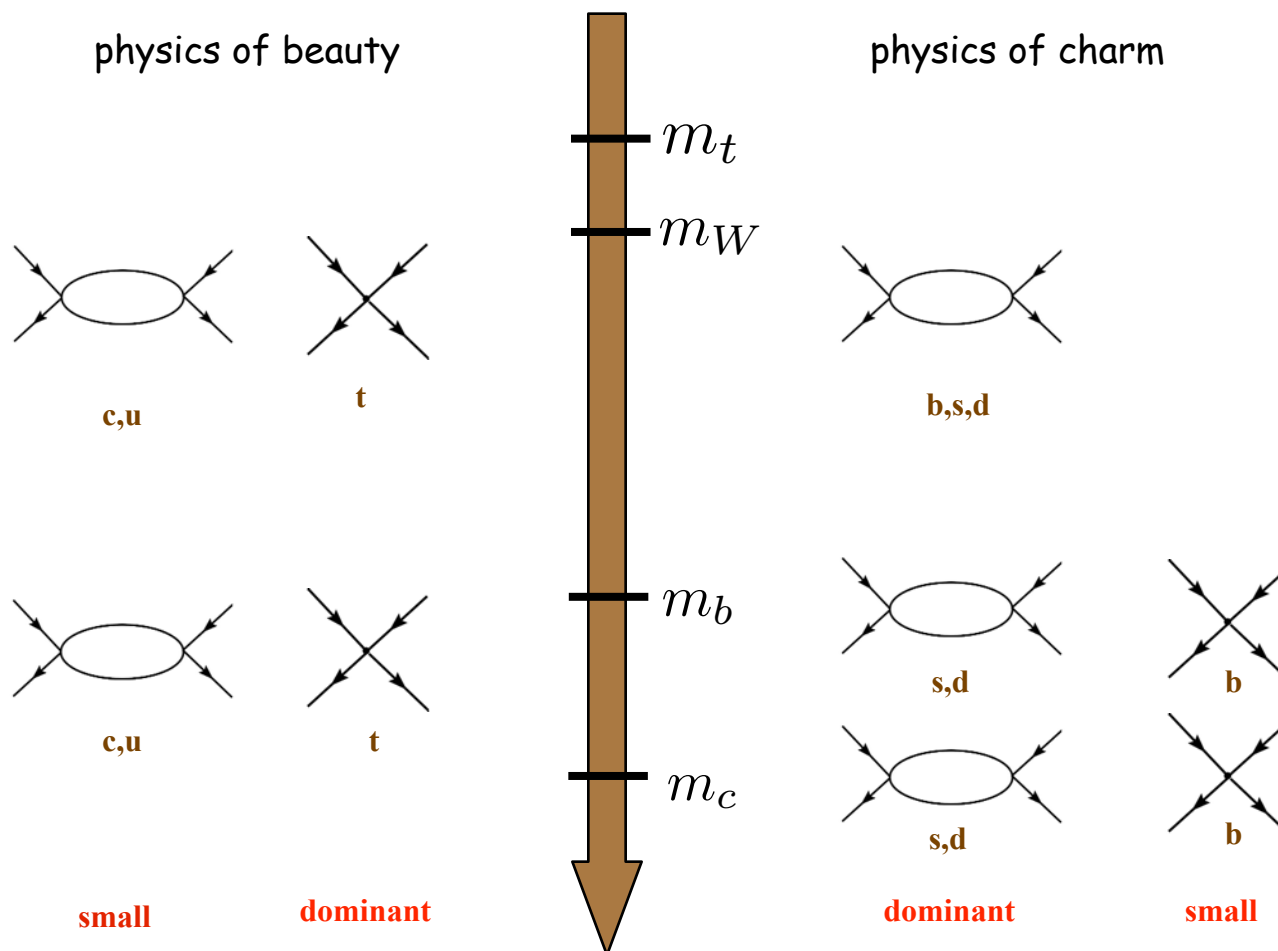
Allowed	Ajar	Disfavored
$Q_{7,8}, Q'_{7,8},$ $\forall f Q_{1,2}^{f'}, Q_{5,6}^{(c-u,b,0)'}$	$Q_{1,2}^{(c-u,8d,b,0)},$ $Q_{5,6}^{(0)}, Q_{5,6}^{(8d)'}$	$Q_{1,2}^{s-d}, Q_{5,6}^{(s-d)'},$ $Q_{5,6}^{s-d,c-u,8d,b}$

Constraints from particular models also available

## 4. Testing QCD tools for flavor physics

★ Modern approach to flavor physics calculations: effective field theories

★ It is important to understand relevant energy scales for the problem at hand



# Testing QCD tools for flavor physics

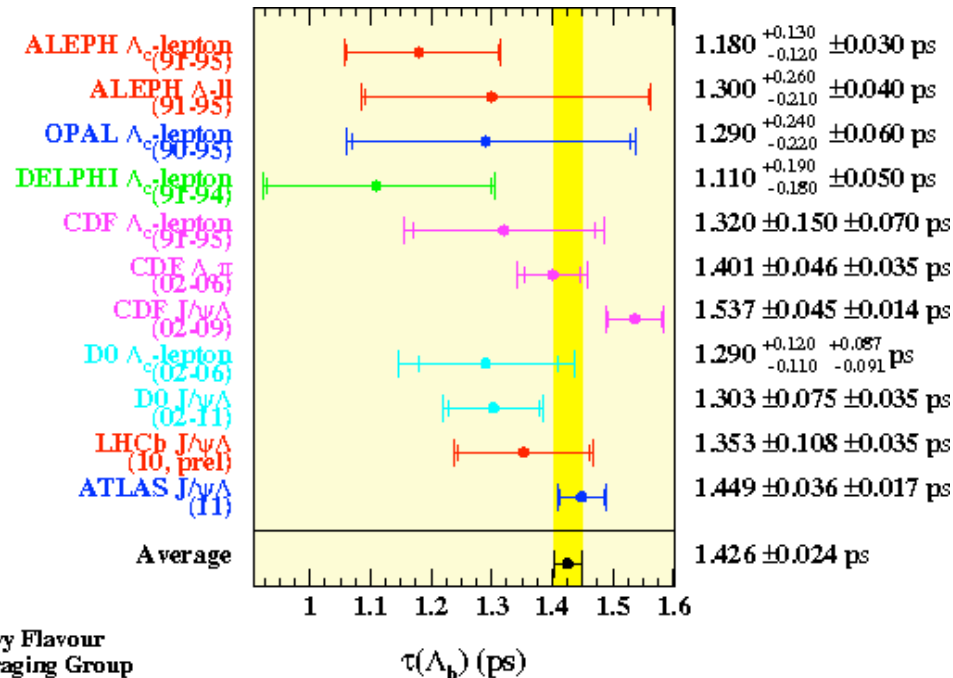
★ Calculations of SM observables can help with testing the tools

1. Nice test of our understanding of non-perturbative effects in QCD
2. One of the few unambiguous theoretical predictions that are easy to test experimentally
3. Theoretical uncertainty can be estimated: precision studies

$$\Gamma(H_b) = \frac{G_F^2 m_Q^5}{192\pi^3} \left[ A_0 + \frac{A_2}{m_Q^2} + \frac{A_2}{m_Q^3} + \dots \right]$$

Heavy Flavour  
Averaging Group

How good are theoretical predictions?



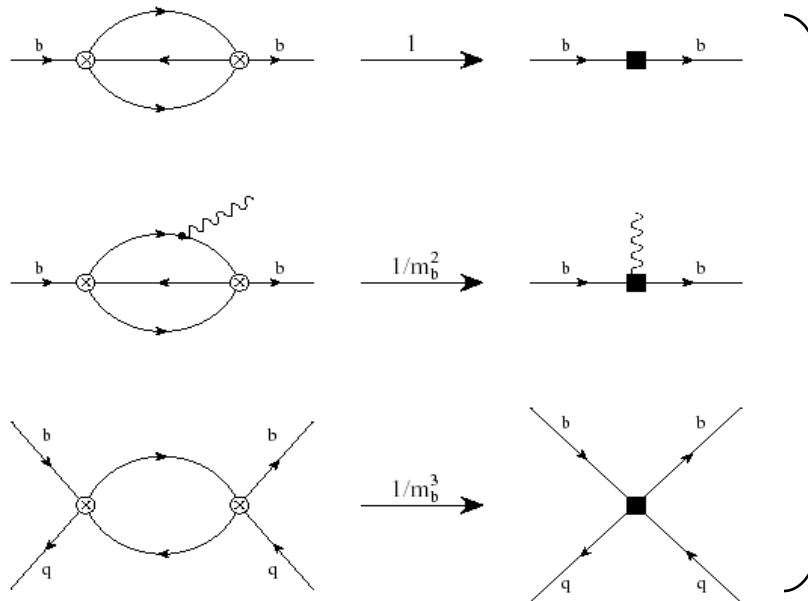


# Theoretical expectations

- Assume quark-hadron duality: relate width to forward matrix element

$$\Gamma(H_b) = \frac{1}{2M_b} \langle H_b | T | H_b \rangle = \frac{1}{2M_b} \langle H_b | \text{Im} i \int d^4x T \{ H_{eff}^{\Delta B=1}(x) H_{eff}^{\Delta B=1}(0) \} | H_b \rangle$$

- This correlator can be expanded using OPE



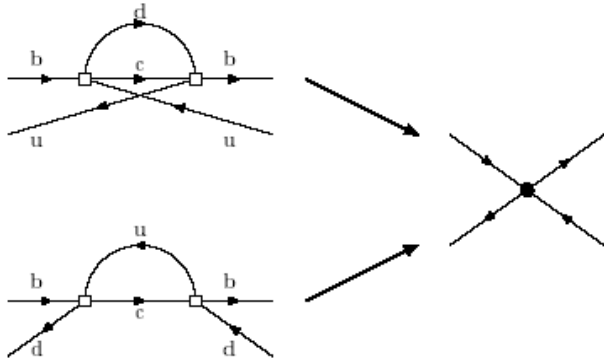
**I. Bigi, M. Shifman, A. Vainshtein, M. Voloshin,  
N. Uraltsev, A. Falk, A. Manohar, M. Wise, M.  
Neubert, C. Sachrajda, P. Colangelo, F. de Fazio,  
...**

$$\Gamma(H_b) = \sum_k \frac{C_k(\mu)}{m_b^k} \langle H_b | O_k^{\Delta B=0}(\mu) | H_b \rangle$$

What are the results?

# Theoretical expectations

➤ Subset of  $1/m_b^3$  corrections:  $\Gamma(H_b) = \sum_k \frac{C_k(\mu)}{m_b^3} \langle H_b | O_k^{\Delta B=0}(\mu) | H_b \rangle$



$$O^q = \bar{b}_L \gamma_\mu q_L \bar{q}_L \gamma^\mu b_L, \quad O_S^q = \bar{b}_R q_L \bar{q}_R b_L,$$

$$T^q = \bar{b}_L \gamma_\mu t^a q_L \bar{q}_L \gamma^\mu t^a b_L, \quad T_S^q = \bar{b}_R t^a q_L \bar{q}_R t^a b_L$$

Two intermediate quarks:  $16\pi^2$  enhanced

For the mesons:

$$\frac{1}{2m_{B_q}} \langle B_q | Q^q | B_q \rangle = \frac{f_{B_q}^2 m_{B_q}}{8} B_1, \quad \frac{1}{2m_{B_q}} \langle B_q | Q_S^q | B_q \rangle = \frac{f_{B_q}^2 m_{B_q}}{8} B_2$$

$$\frac{1}{2m_{B_q}} \langle B_q | T^q | B_q \rangle = \frac{f_{B_q}^2 m_{B_q}}{8} \varepsilon_1, \quad \frac{1}{2m_{B_q}} \langle B_q | T_S^q | B_q \rangle = \frac{f_{B_q}^2 m_{B_q}}{8} \varepsilon_2$$

For the baryons:

$$\langle \Lambda_b | O_1^q | \Lambda_b \rangle = -\tilde{B} \langle \Lambda_b | \tilde{O}_1^q | \Lambda_b \rangle = \frac{\tilde{B}}{6} f_{B_q}^2 m_{B_q} m_{\Lambda_b} r,$$

As a result:

$$\frac{\tau(\Lambda_b)}{\tau(B^0)} \approx 0.98 - (d_1 + d_2 \bar{B})r - (d_3 \varepsilon_1 + d_4 \varepsilon_2) - (d_5 B_1 + d_6 B_2)$$

Lattice: the ONLY study of  $r$ : DiPierro, et al., 1999!

# Lifetime predictions

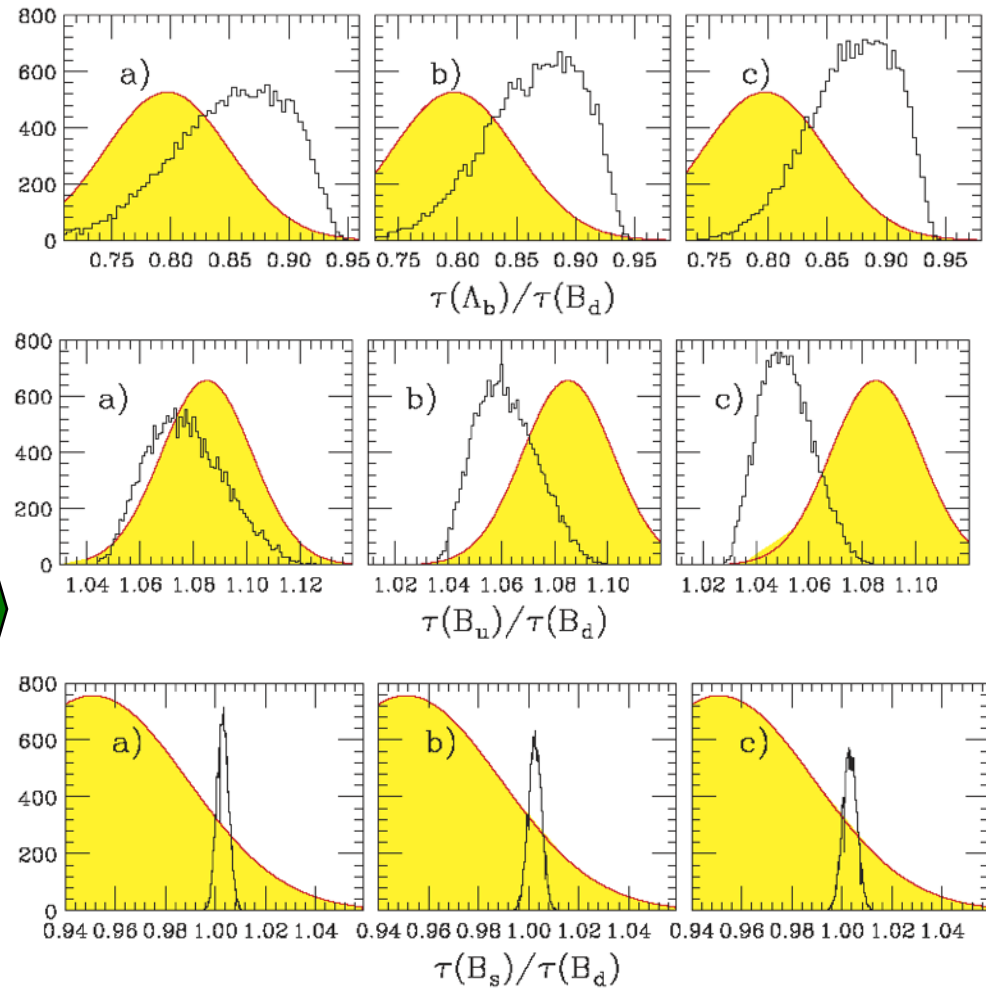
- The expansion appears well convergent for a b-quark
- Conservatively:

$$\tau(\Lambda_b)/\tau(B^0) = 0.87 \pm 0.05$$

$$\tau(B^+)/\tau(B^0) = 1.06 \pm 0.02$$

$$\tau(B_s)/\tau(B^0) = 1.00 \pm 0.01$$

Year	Exp	Ratio
2013	HFAG	$0.941 \pm 0.016$
2013	LHCb	$0.976 \pm 0.012$
2013	CMS	$0.989 \pm 0.040$
2012	Atlas	$0.954 \pm 0.026$
2003	HFAG	$0.789 \pm 0.034$



F. Gabbiani, A. Onishchenko, A.A.P. Phys. Rev. D70, 094031 (2004)

## 5. Things to take home

- Indirect probes for new physics compete well with direct searches
  - for some observables sensitive to scales way above LHC
- Computational techniques for heavy flavors are well-established
  - but don't always work well: "heavy-quark-expansion" techniques for charm often miss threshold effects
  - "hadronic" techniques that sum over large number of intermediate states can be used, BUT one cannot use current experimental data on D-decays
- Calculations of New Physics contributions to mixing are in better shape
  - contributions of NP in  $\Delta b=2$  operators are local and well-behaved
- Can correlate mixing and rare decays with New Physics models
  - signals in B/D-mixing vs B/D rare decays help differentiate among models
- Direct CP-violation in charm decays?
  - evidence for CPV in the up-quark sector looks SM-like



Rembrandt "Old Man in Military Costume",  
BNL/DESY X-ray study

**Accurate analysis of flavor data might reveal hidden  
layers of something previously unknown.**