

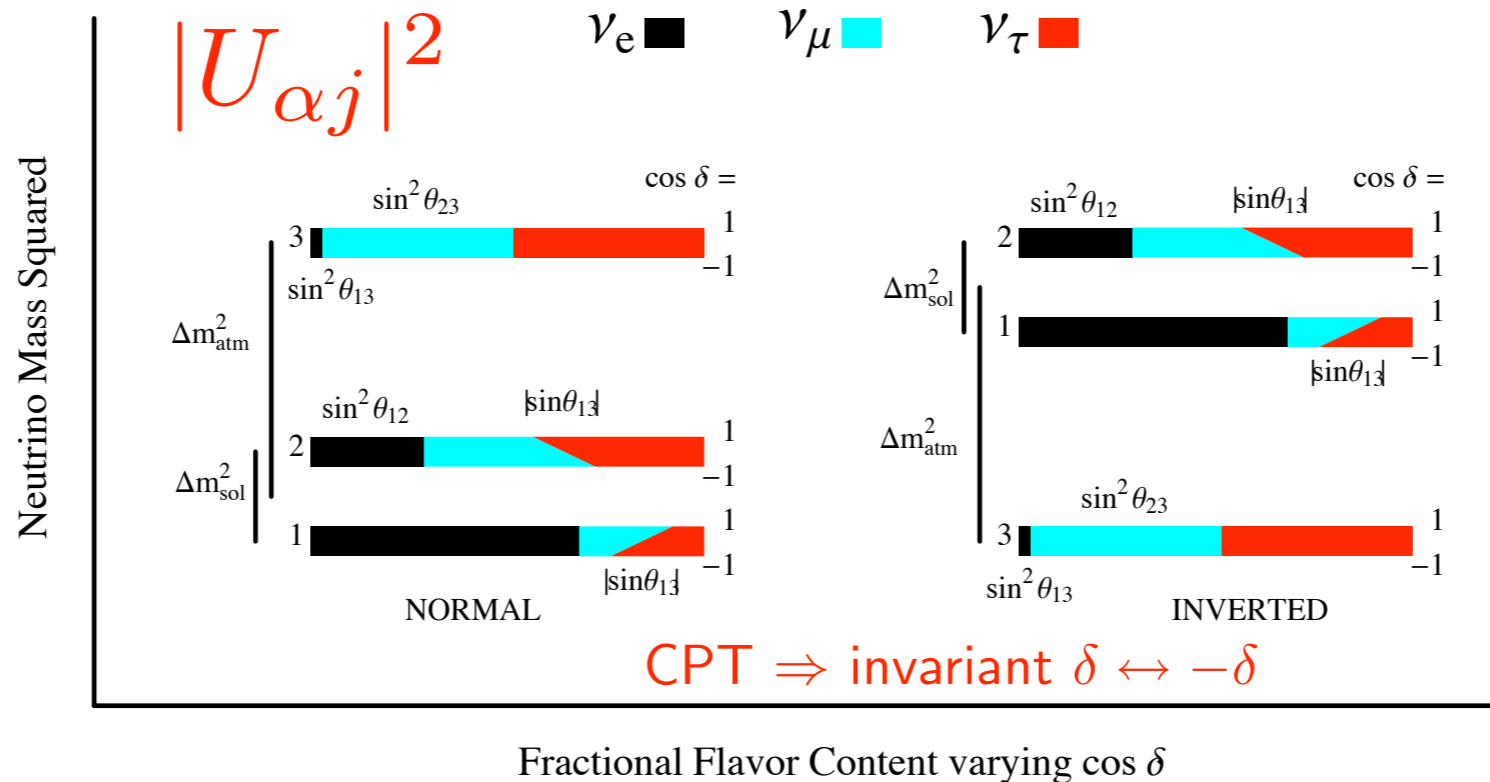
Physics case for long-baseline oscillation measurements:

Stephen Parke
Fermilab



Nu Standard Model:

$$\sqrt{\delta m_{atm}^2} = 0.05 \text{ eV} < \sum m_{\nu_i} < 0.5 \text{ eV} = 10^{-6} * m_e$$



$$\delta m_{sol}^2 = +7.6 \times 10^{-5} \text{ eV}^2$$

$$\sin^2 \theta_{12} \sim \frac{1}{3}$$

$$|\delta m_{atm}^2| = 2.4 \times 10^{-3} \text{ eV}^2$$

$$0 \leq \delta < 2\pi$$

$$\sin^2 \theta_{23} \sim \frac{1}{2}$$

$$|\delta m_{sol}^2| / |\delta m_{atm}^2| \approx 0.03$$


$$\sin^2 \theta_{13} \sim 0.02$$

Except: LSND, miniBooNE, reactor anomaly, gallium anomaly.



Neutrino Mixing Matrix: PMNS

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

 smaller ν_e
content
 $|U_{e1}|^2 > |U_{e2}|^2 > |U_{e3}|^2$



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SNO CC
 KamLAND
 $|U_{e2}|^2$

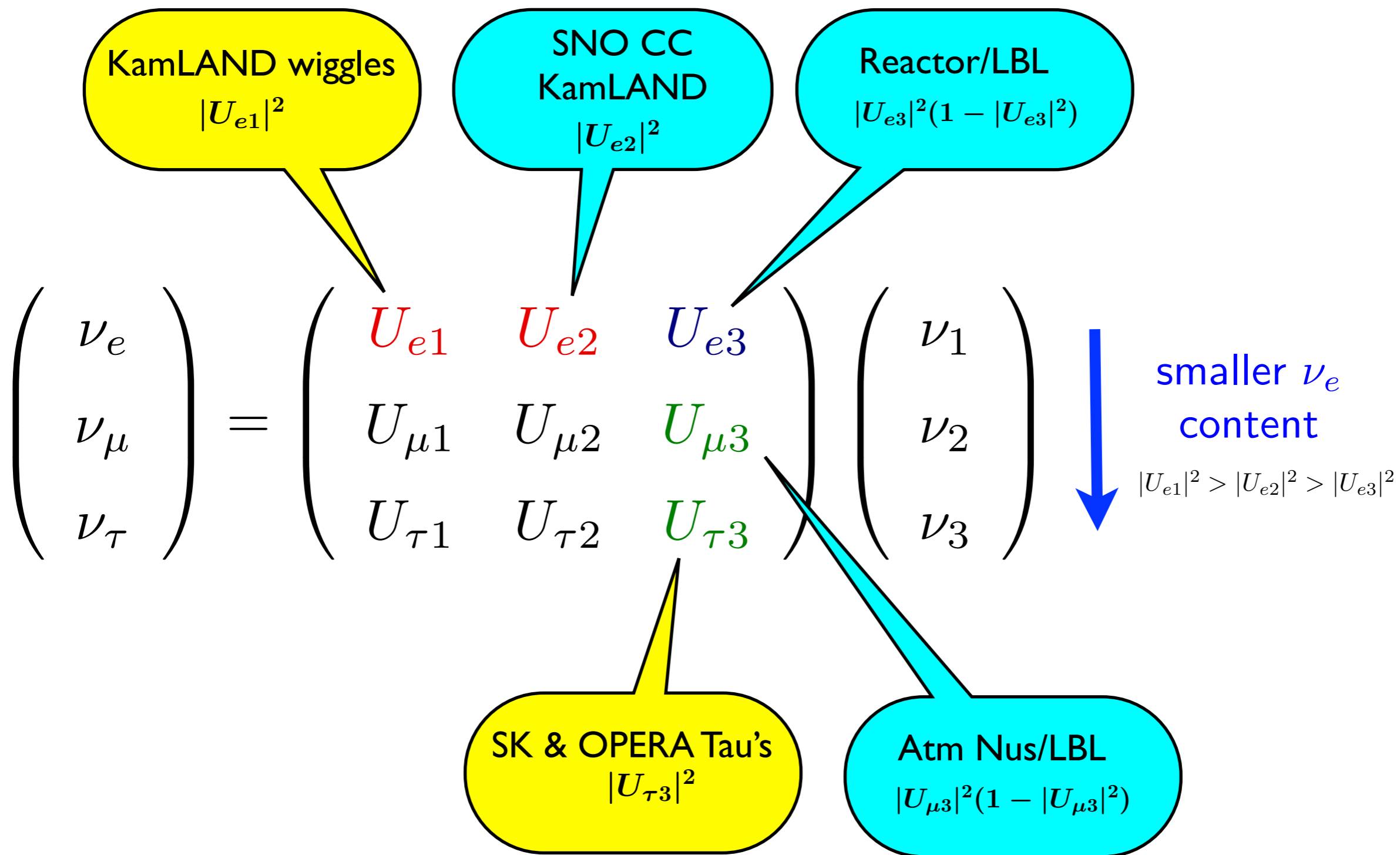
Reactor/LBL
 $|U_{e3}|^2(1 - |U_{e3}|^2)$

smaller ν_e
 content
 $|U_{e1}|^2 > |U_{e2}|^2 > |U_{e3}|^2$

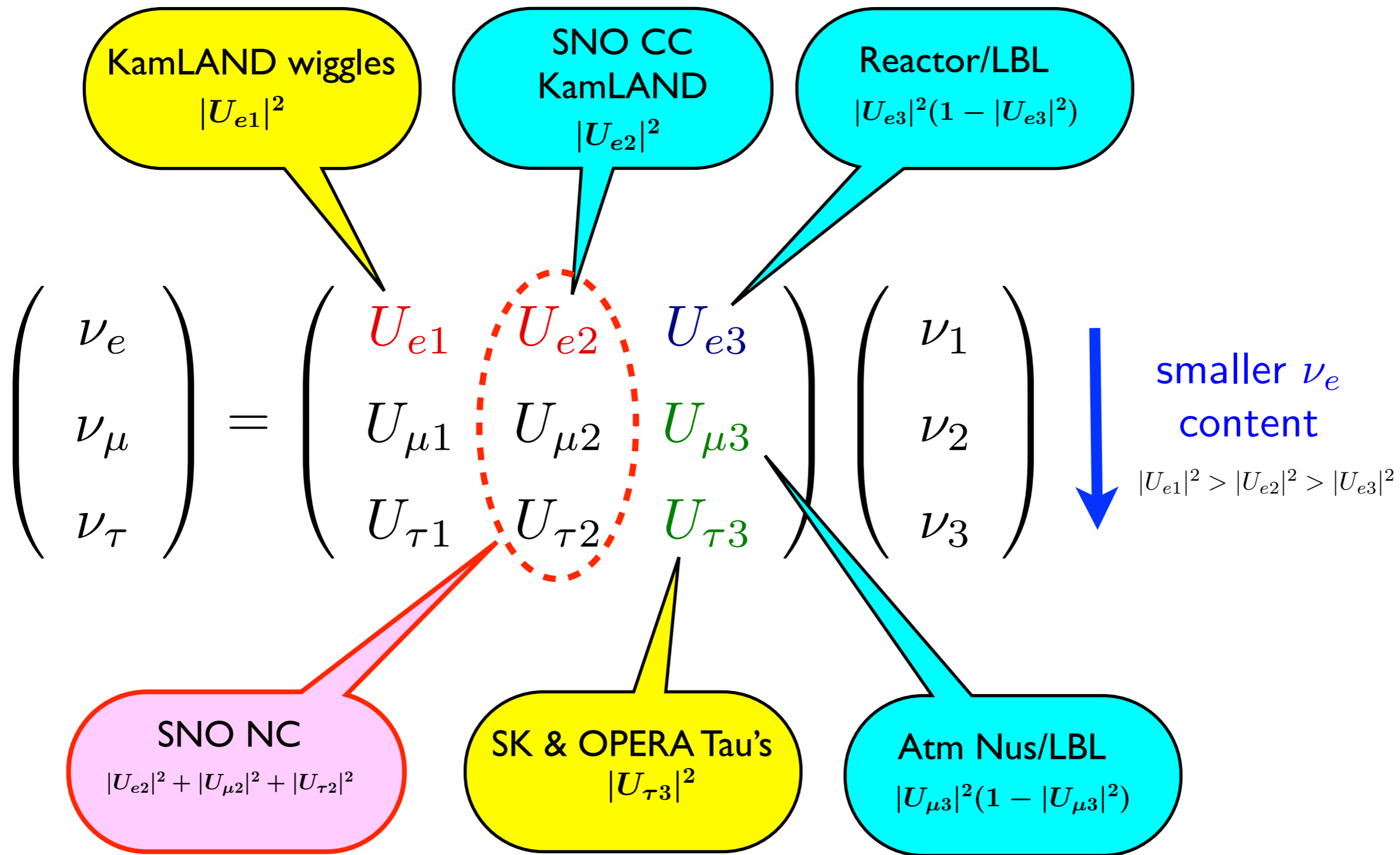
Atm Nus/LBL
 $|U_{\mu3}|^2(1 - |U_{\mu3}|^2)$



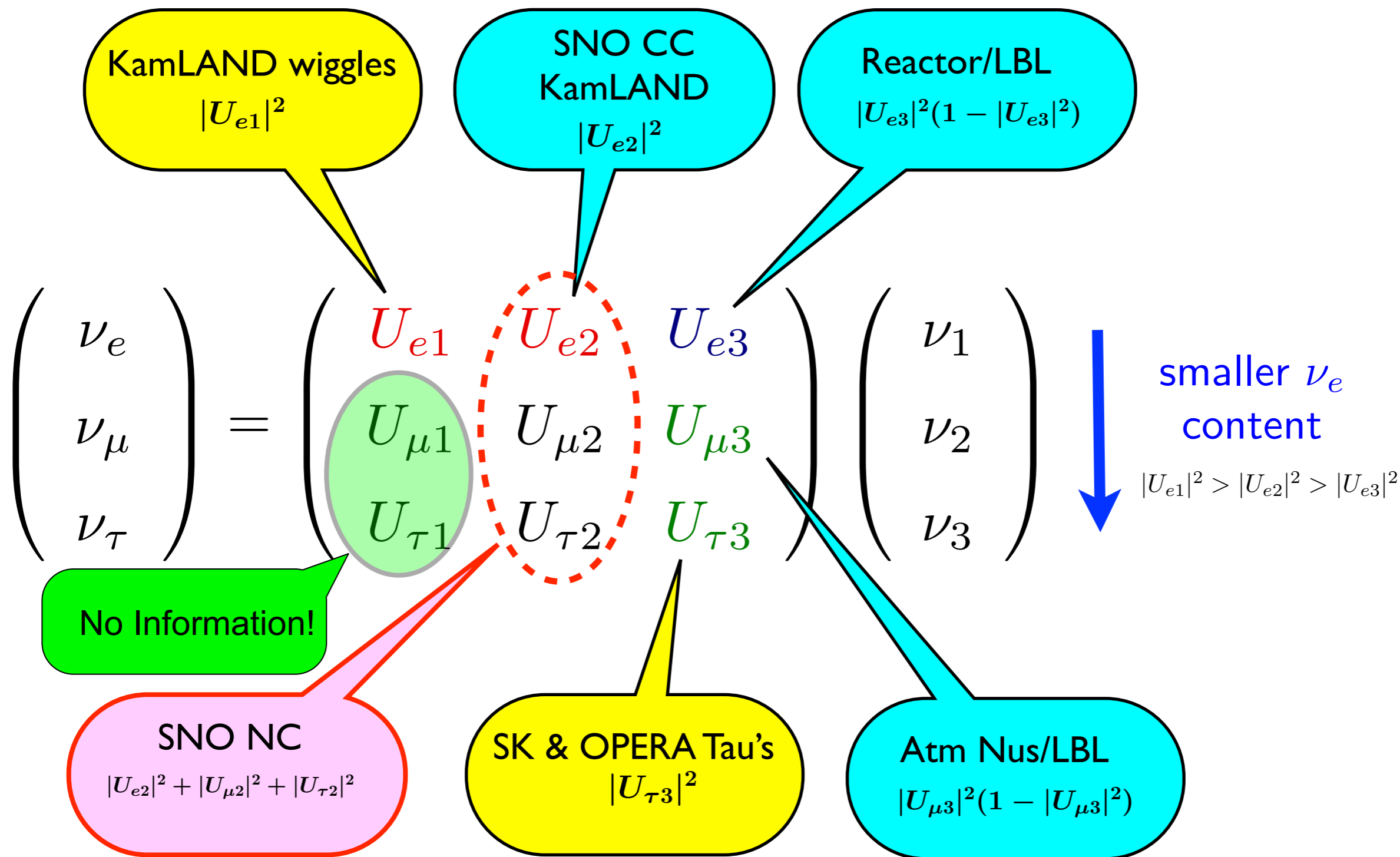
Neutrino Mixing Matrix: PMNS



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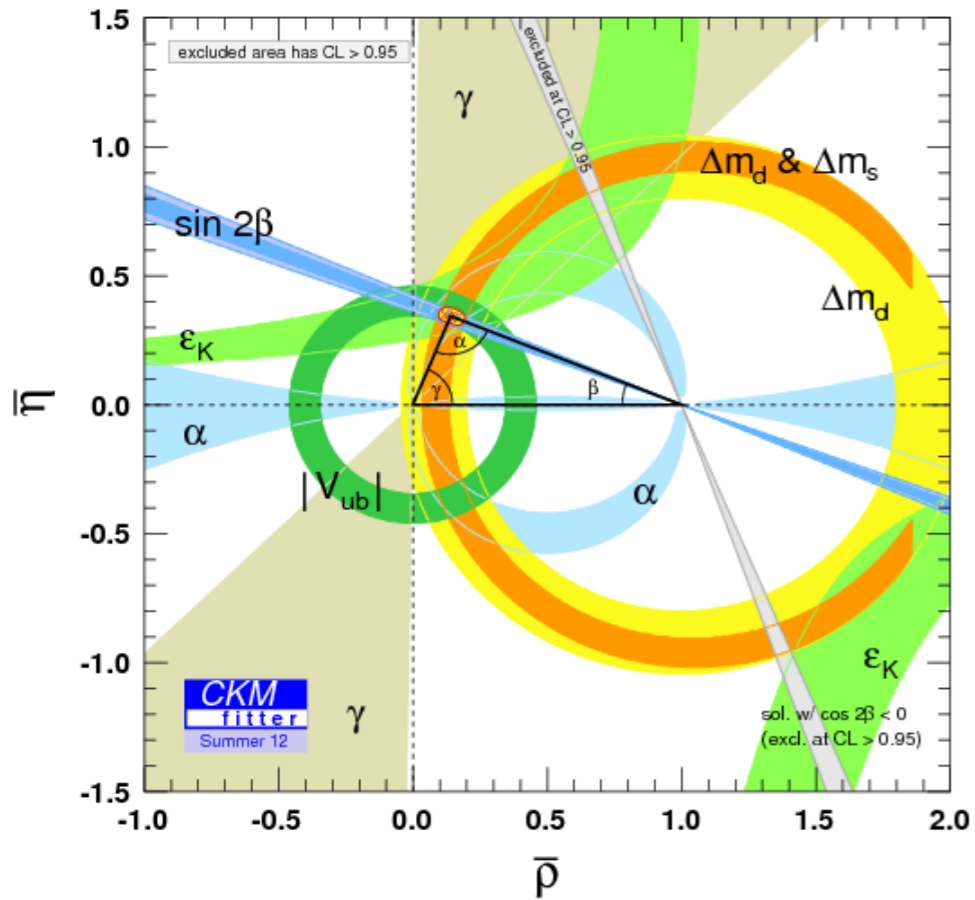


Neutrino Mixing Matrix: PMNS



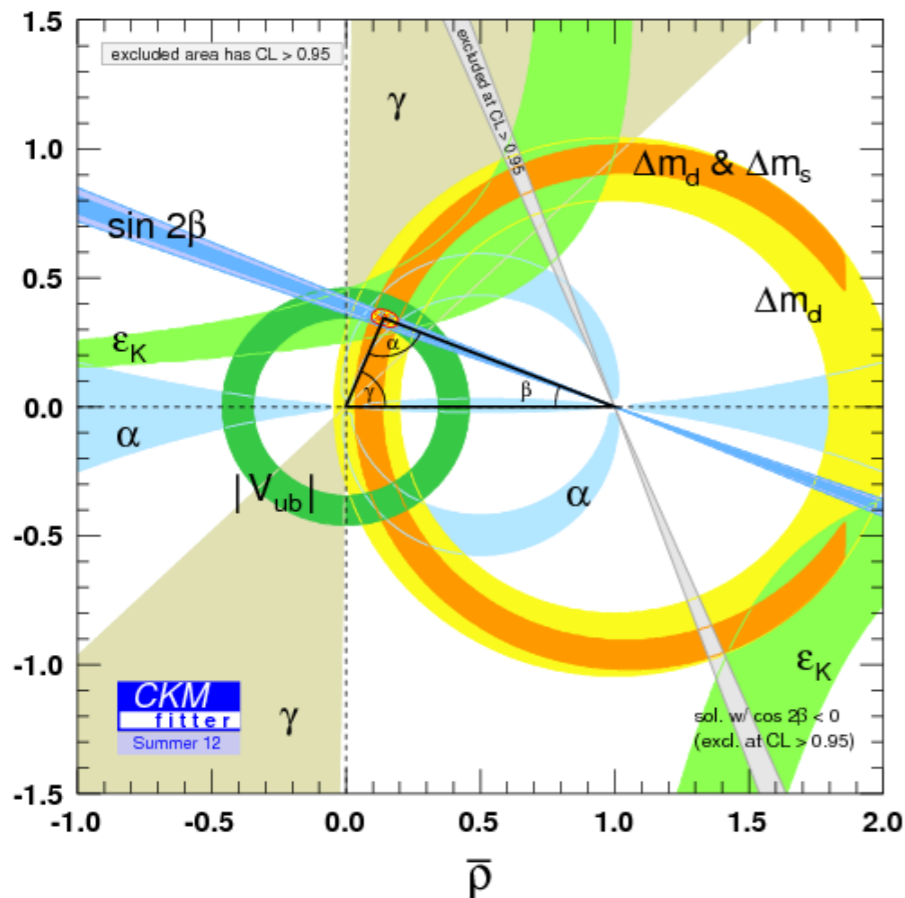
Quark & lepton Unitarity Triangles:

Quark Triangle:



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Quark Triangle:

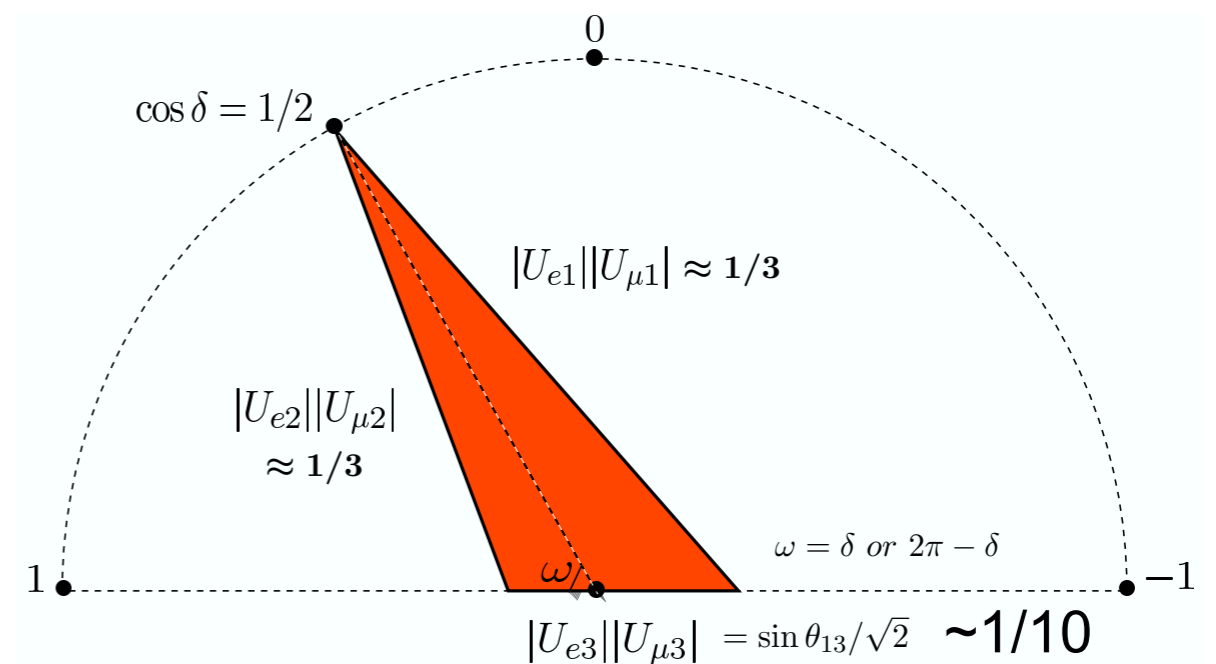


Neutrino Triangle:

$$U_{\mu 1}^* U_{e 1} + U_{\mu 2}^* U_{e 2} + U_{\mu 3}^* U_{e 3} = 0$$

only Unitarity triangle that doesn't involve ν_τ !

$$|J| = 2 \times Area$$

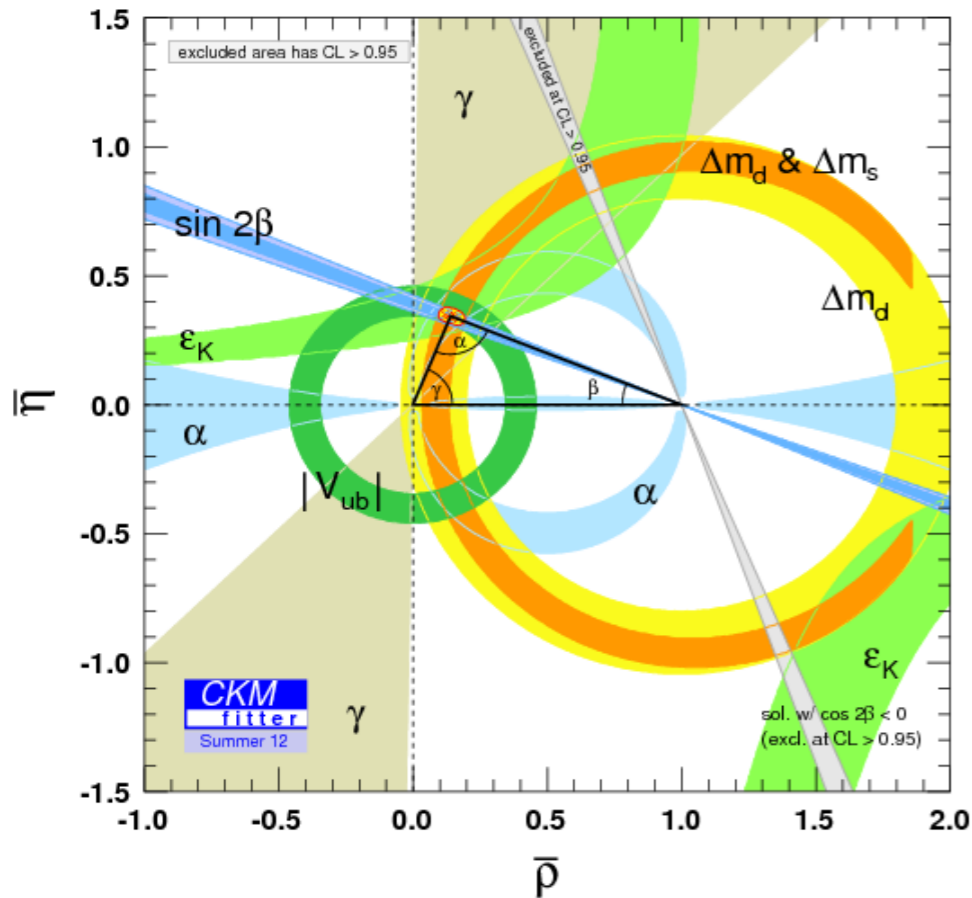


$$|U_{e1}||U_{\mu 1}| = 0.0 - 0.5; |U_{e2}||U_{\mu 2}| = 0.2 - 0.4; |U_{e3}||U_{\mu 3}| = 0.1(1 \pm 0.2)$$



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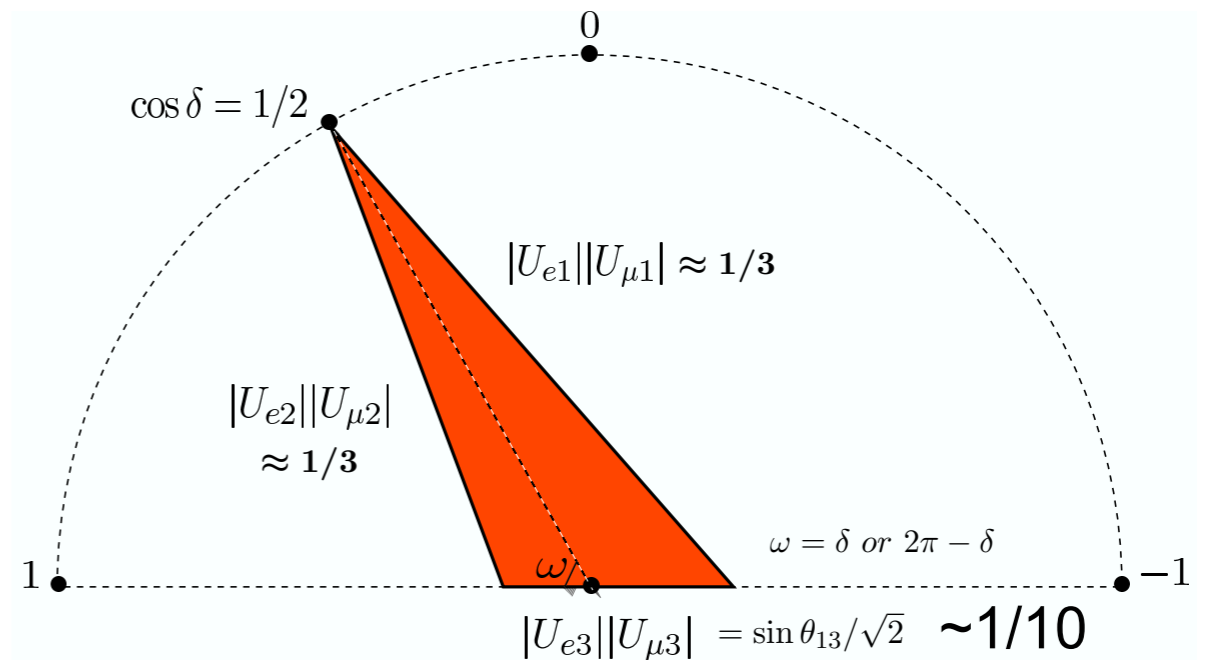


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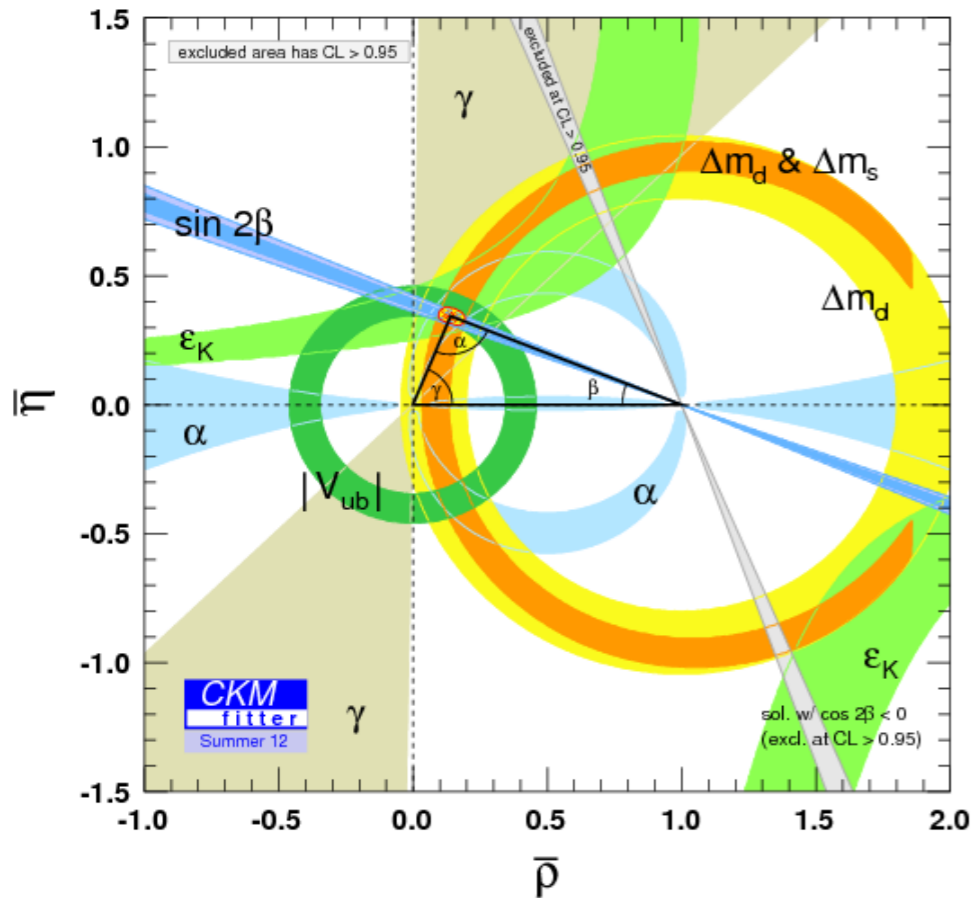
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How to measure $|U_{\mu 1}|^2$ and $|U_{\mu 2}|^2$ separately ? ? ?



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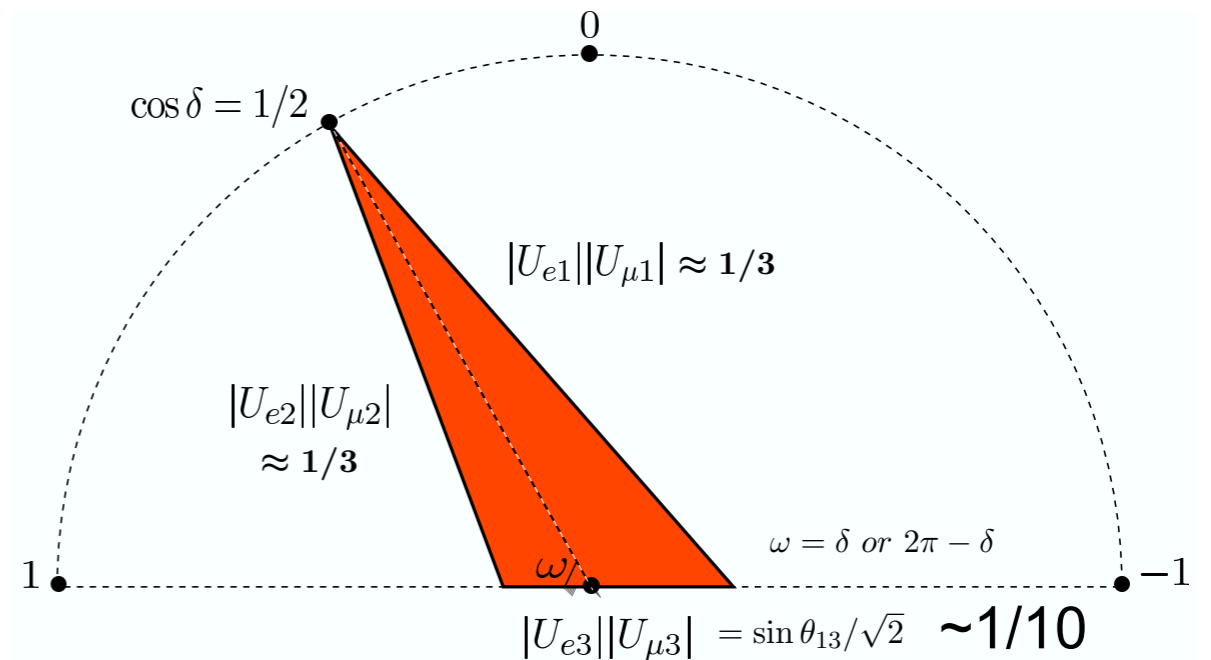


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Neutrino Factory to detector in geo-synchronous orbit ! ! !



Unanswered Questions !

ν Standard Model

- Nature of Neutrino: Majorana (2 comp) or Dirac (4 comp) fermion?
- CPV in Neutrino Sector: determination Dirac phase δ ?
- Ordering of mass eigenstates: Atmos. mass hierarchy, sign of δm_{31}^2 ?
- Is ν_3 more ν_μ or more ν_τ : $|U_{\mu 3}|^2 >$ or $< |U_{\tau 3}|^2$ or $\theta_{23} >$ or $< \pi/4$
- Majorana Phases: 2 additional phases
- Absolute Neutrino Mass: m_{lite}

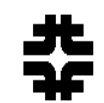


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Beyond ν Standard Model

- What is the mass of the Sterile Neutrinos: light? or Superheavy?
- What is the size of Non-Standard Interactions?
- Where are the True Surprises?



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Leptons v Quarks:

$$V_{MNS} \sim \begin{pmatrix} 0.8 & 0.5 & 0.2 \\ 0.4 & 0.6 & 0.7 \\ 0.4 & 0.6 & 0.7 \end{pmatrix}$$

$$V_{CKM} \sim \begin{pmatrix} 1 & 0.2 & 0.001 \\ 0.2 & 1 & 0.01 \\ 0.001 & 0.01 & 1 \end{pmatrix}$$

Very Different !!!



Flavors & quark-lepton unification

Quarks CKM matrix = $\mathbf{1}$ + (Cabibbo) effects

Leptons' MNSP matrix = \mathbf{X} + (Cabibbo?) effects

↖ contains two large angles

Cabibbo effects as deviation from \mathbf{X}

example: $\theta_{13} \approx \theta_c / \sqrt{2}$ deviation from zero?

speculate: $\theta_{\text{atm}} \approx \pi/4 + O(\theta_c)$ deviation from $\pi/4$?



Masses & Mixings (conti.)

□ Quark-Lepton Complementarity $\theta_{12} + \theta_C = 45^\circ$

□ Solar sum rules **Bimaximal** $\theta_{12} = 45^\circ + \theta_{13} \cos \delta$

Tri-bimaximal $\theta_{12} = 35^\circ + \theta_{13} \cos \delta$

Golden Ratio $\theta_{12} = 32^\circ + \theta_{13} \cos \delta$

Plus HO corrections...

□ Atm. sum rules **Tri-bimaximal-cabibbo** $\theta_{12} = 35^\circ$ $\theta_{23} = 45^\circ$
 $\theta_{13} = \theta_C / \sqrt{2} = 9.2^\circ$

Trimaximal1 $\theta_{23} = 45^\circ + \sqrt{2}\theta_{13} \cos \delta$

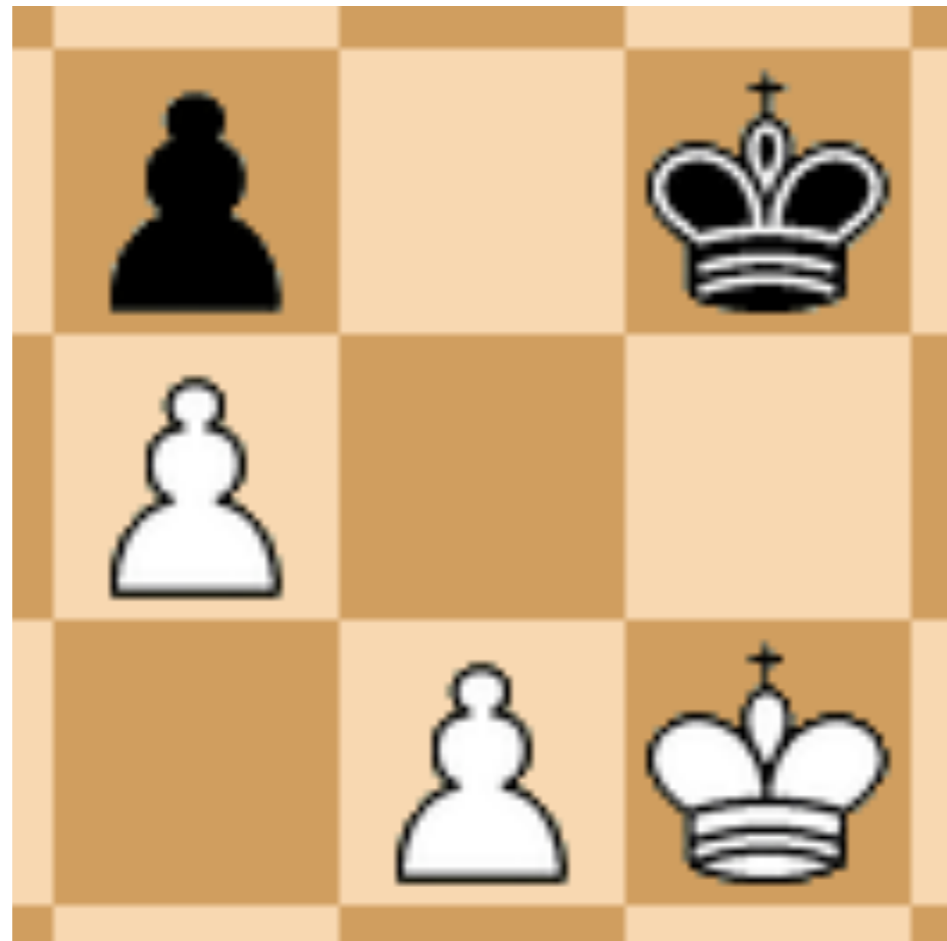
Trimaximal2 $\theta_{23} = 45^\circ - \frac{\theta_{13}}{\sqrt{2}} \cos \delta$

Now that θ_{13} is measured these predict $\cos \delta$

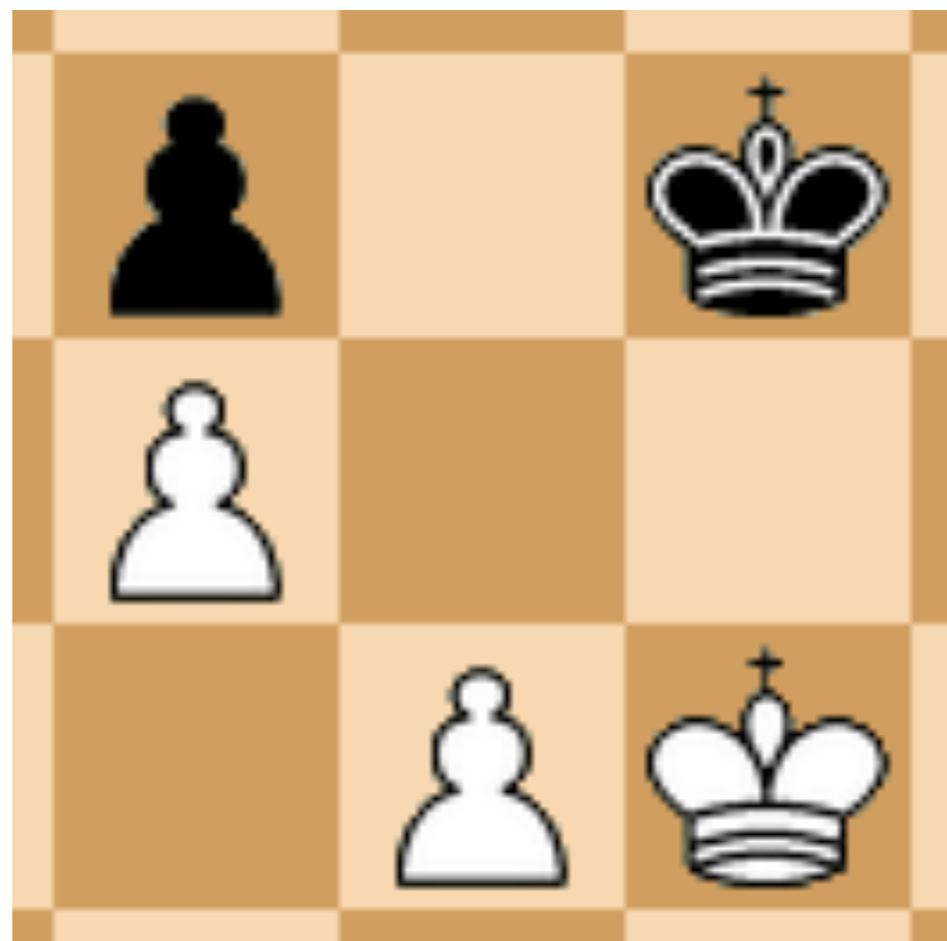
Plus charged Lepton Corrections...



Given this end game:

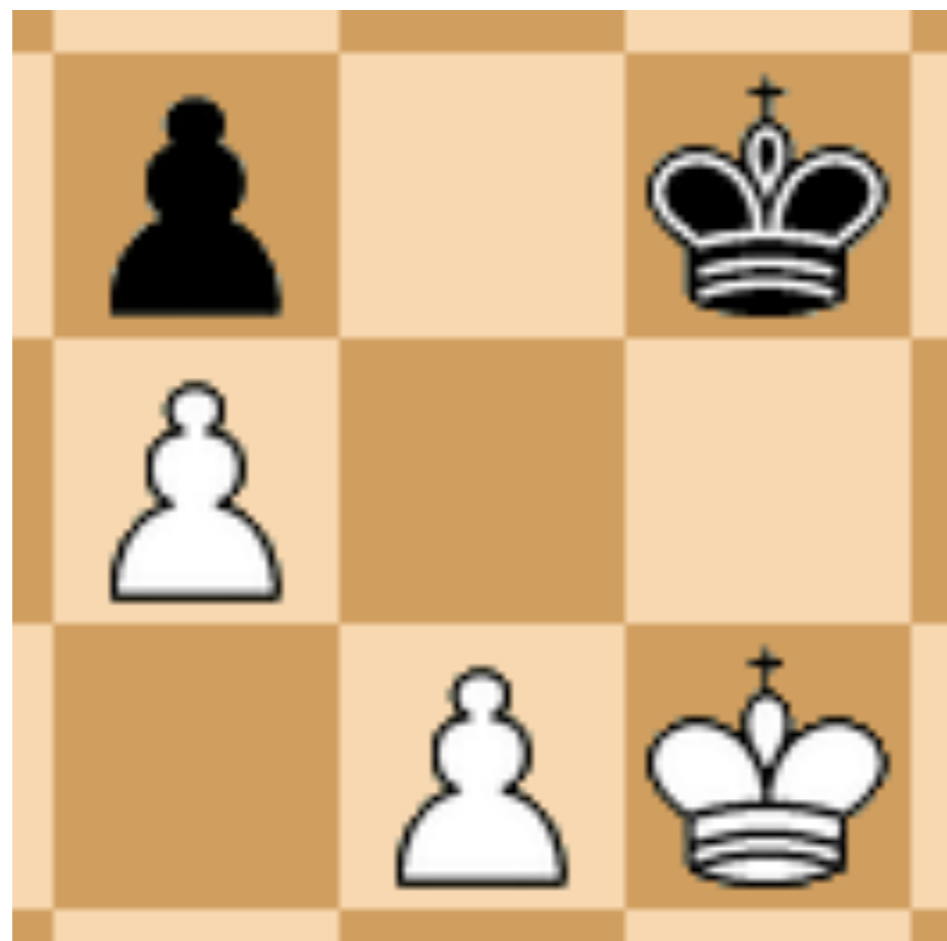


Given this end game:



Deduce the rules of chess!!!

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Deduce the rules of chess!!!

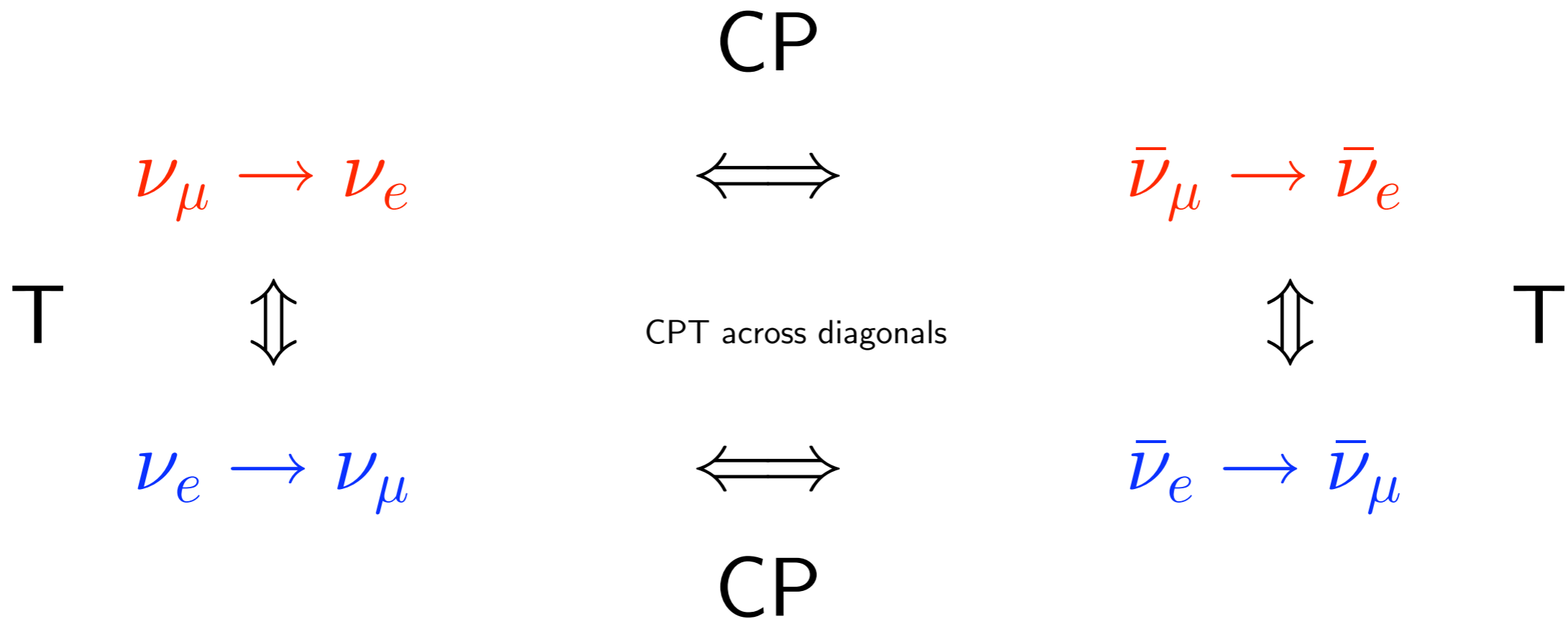
theorists need more hints !



Precision Measurements:



Appearance Experiments:



- First Row: Superbeams where ν_e contamination $\sim 1\%$
- Second Row: ν -Factory or β -Beams, no beam contamination

ν_τ at Neutrino Factory



Vacuum
LBL

$$\nu_{\mu} \rightarrow \nu_e$$

$$P_{\mu \rightarrow e} \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} \right|^2$$

$$\Delta_{ij} = \delta m_{ij}^2 L / 4E$$

CP violation !!!

where $\sqrt{P_{atm}} = \sin \theta_{23} \sin 2\theta_{13} \sin \Delta_{31}$

and $\sqrt{P_{sol}} = \cos \theta_{23} \sin 2\theta_{12} \sin \Delta_{21}$

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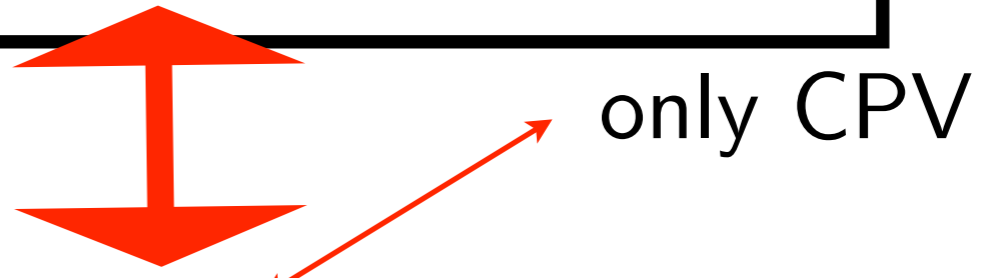
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$$P_{\mu \rightarrow e} \approx P_{atm} + 2\sqrt{P_{atm}P_{sol}} \cos(\Delta_{32} \pm \delta) + P_{sol}$$



only CPV

$$\cos(\Delta_{32} \pm \delta) = \cos \Delta_{32} \cos \delta \mp \sin \Delta_{32} \sin \delta$$

$$\Delta P_{cp} = 2 \sin \delta \sin 2\theta_{13} \sin 2\theta_{23} \sin 2\theta_{12} \cos \theta_{13} \sin \Delta_{21} \sin \Delta_{31} \sin \Delta_{32}$$

$$\nu_\mu \rightarrow \nu_e$$

In Matter:

$$P_{\mu \rightarrow e} \approx \left| \sqrt{P_{atm}} e^{-i(\Delta_{32} \pm \delta)} + \sqrt{P_{sol}} \right|^2$$

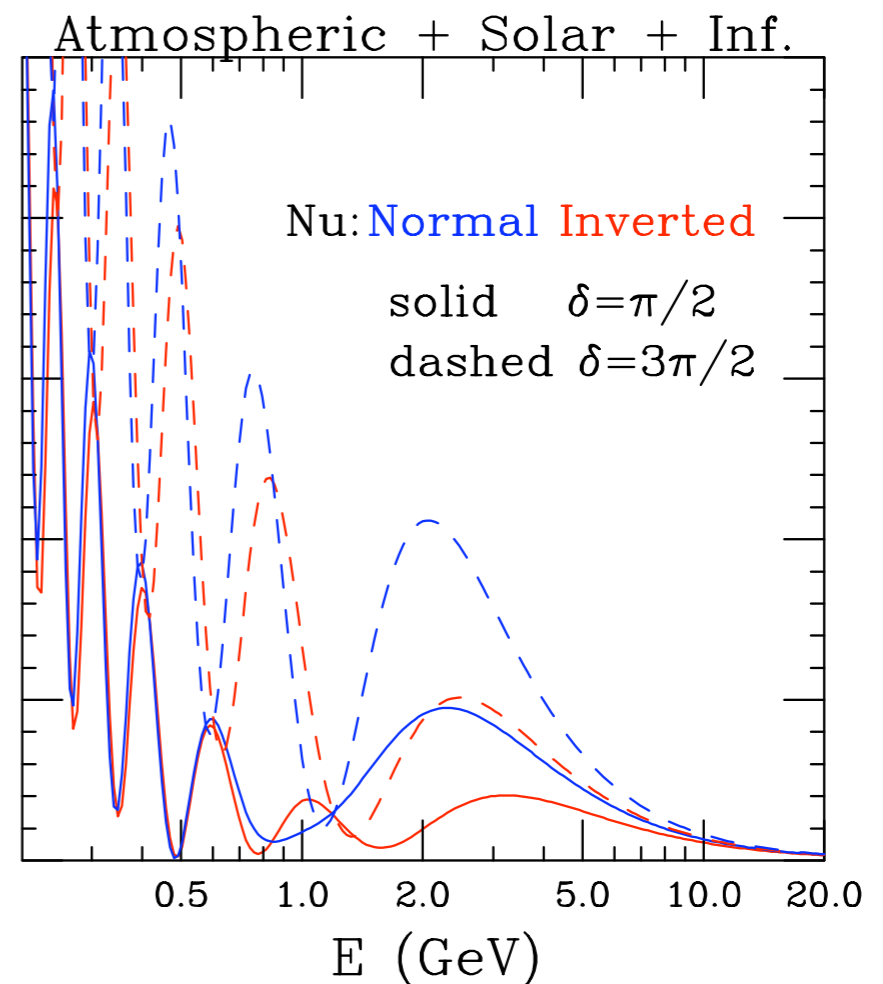
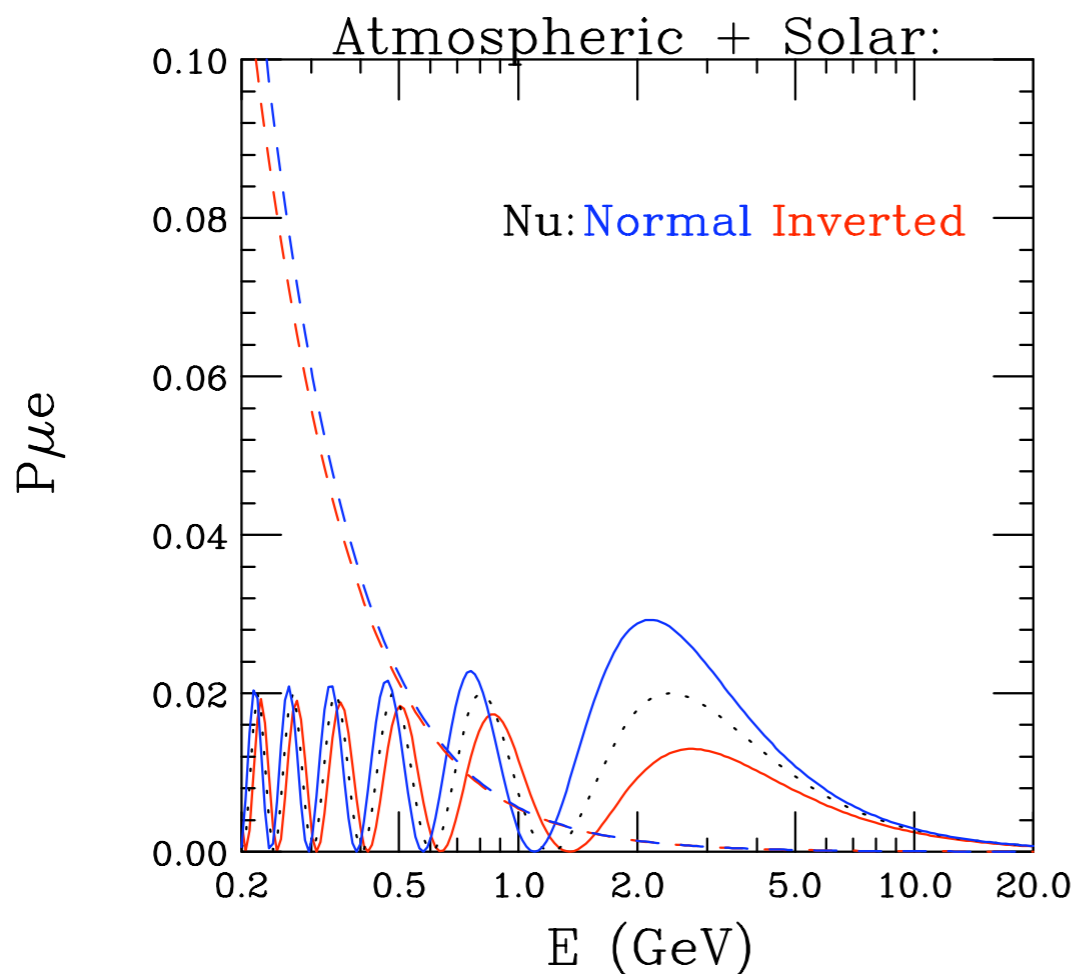
where $\sqrt{P_{atm}} = \sin \theta_{23} \sin 2\theta_{13} \frac{\sin(\Delta_{31} \mp aL)}{(\Delta_{31} \mp aL)} \Delta_{31}$

and $\sqrt{P_{sol}} = \cos \theta_{23} \sin 2\theta_{12} \frac{\sin(aL)}{(aL)} \Delta_{21}$

For $L = 1200 \text{ km}$
and $\sin^2 2\theta_{13} = 0.04$

$$a = G_F N_e / \sqrt{2} = (4000 \text{ km})^{-1},$$

Anti-Nu: Normal Inverted
dashes $\delta = \pi/2$
solid $\delta = 3\pi/2$



1st Oscillation Maximum

At 1st Oscillation Maximum: $\Delta_{31} = \pi/2$:

In vacuum,

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e) \pm P(\nu_\mu \rightarrow \nu_e) = \begin{cases} 2 \sin^2 \theta_{23} \sin^2 2\theta_{13} & \Rightarrow \theta_{23} \text{ “octant”} \\ \frac{\pi}{30} \sin \delta J_r & CPV \end{cases}$$

Reactor:

where $J_r = \sin 2\theta_{13} \cos \theta_{13} \sin 2\theta_{23} \sin 2\theta_{12} \approx 0.3$



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In Matter:

- **sum**, corrections are small – matter*CPV !!!
- **difference** can give Mass Hierarchy,
if matter effects large enough and/or δ favourable



Current Experiments:

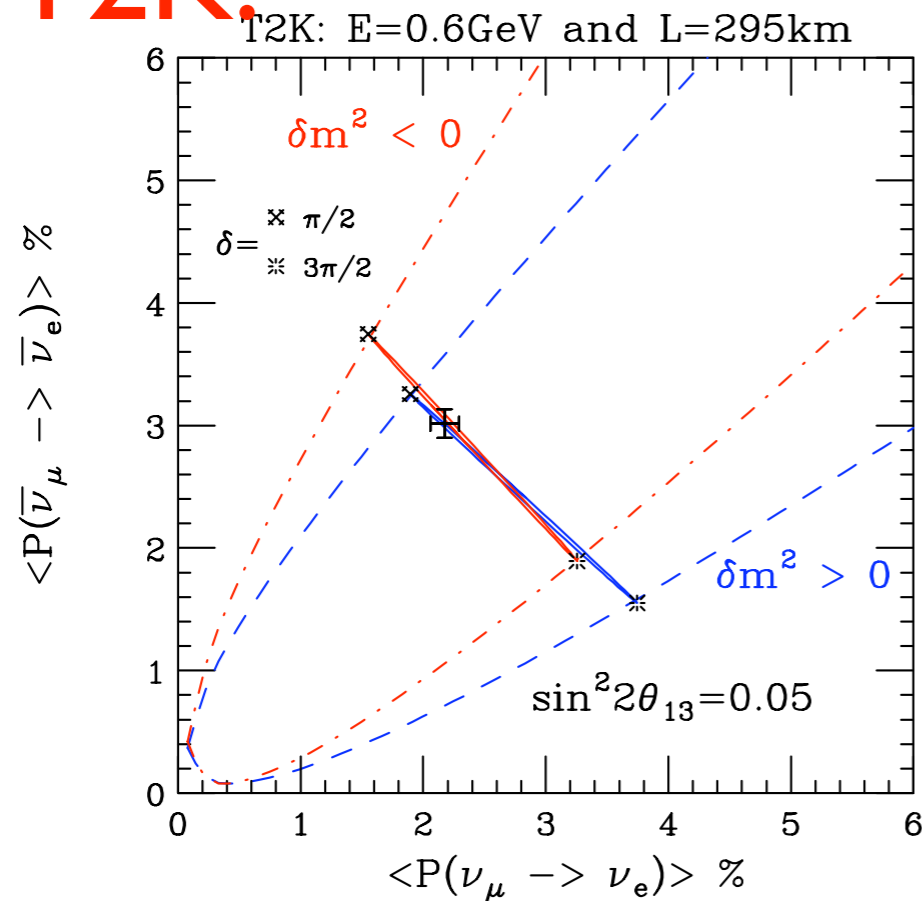
- Near 1st Oscillation Maximum: $L/E = 500 \text{ km/GeV}$

Off Axis beams:

T2K $L=295\text{km}$, $\langle E \rangle = 0.65 \text{ GeV}$, 2.5°

NO ν A: $L=810\text{km}$, $\langle E \rangle = 2.0 \text{ GeV}$, 14 mrad

T2K:



Current Experiments:

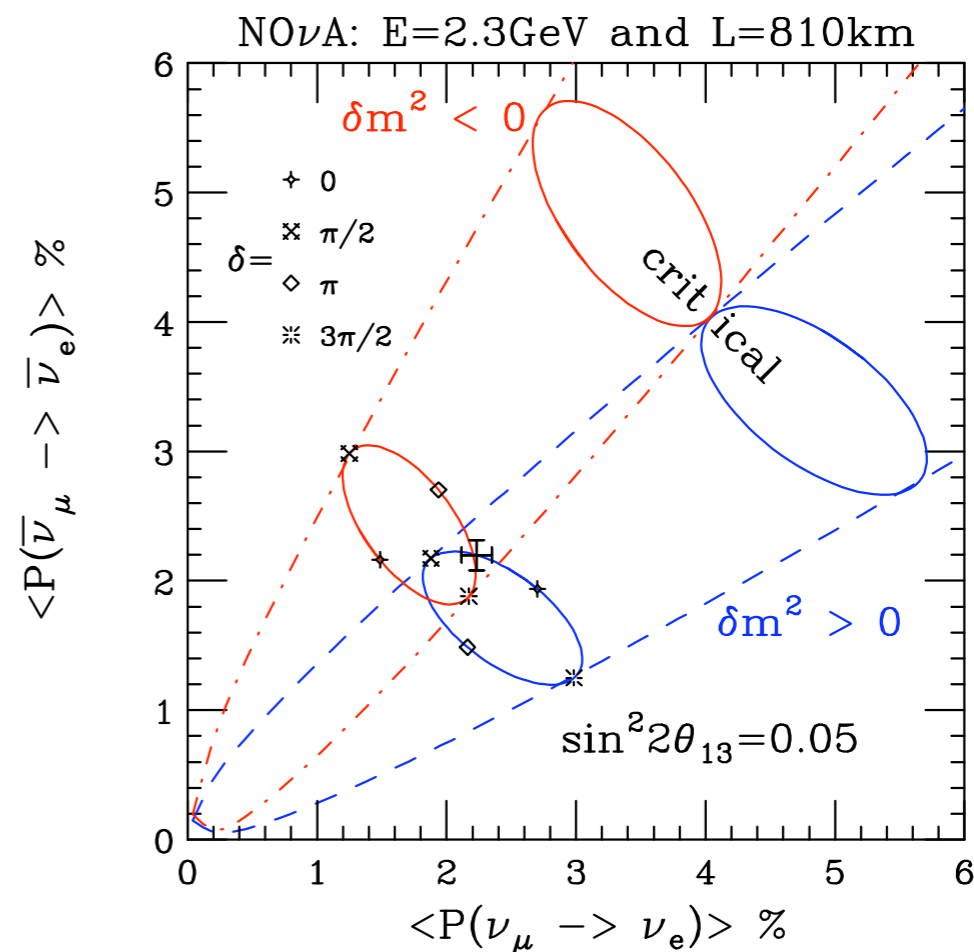
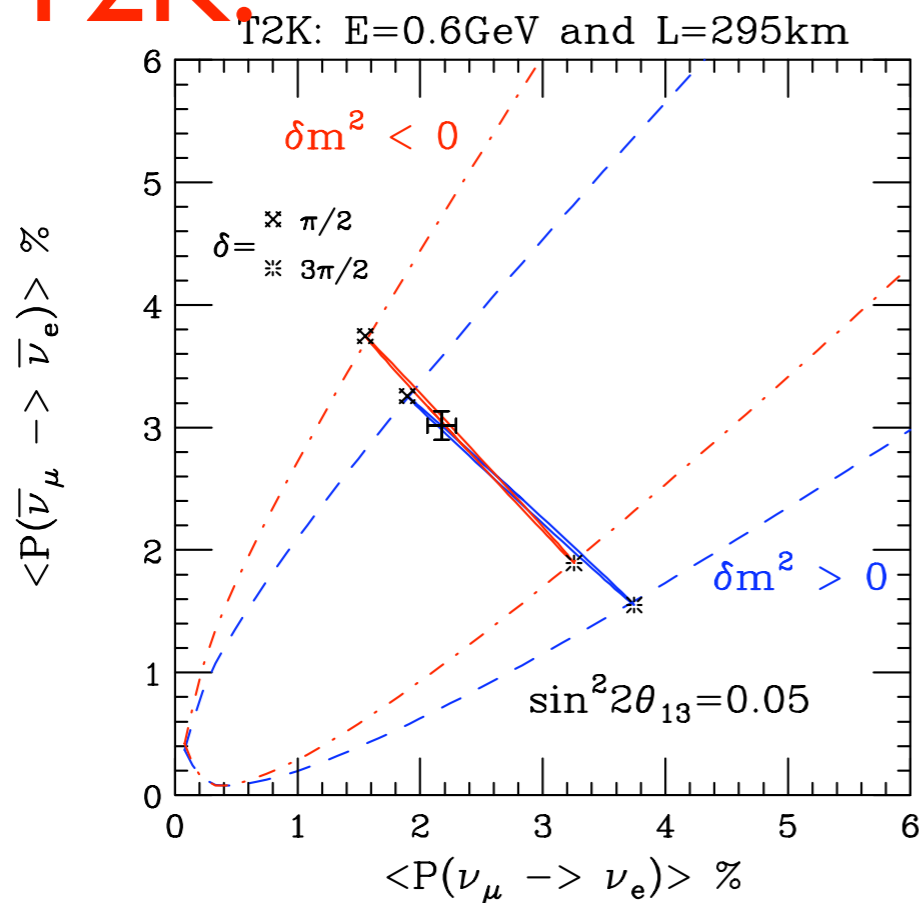
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T2K:



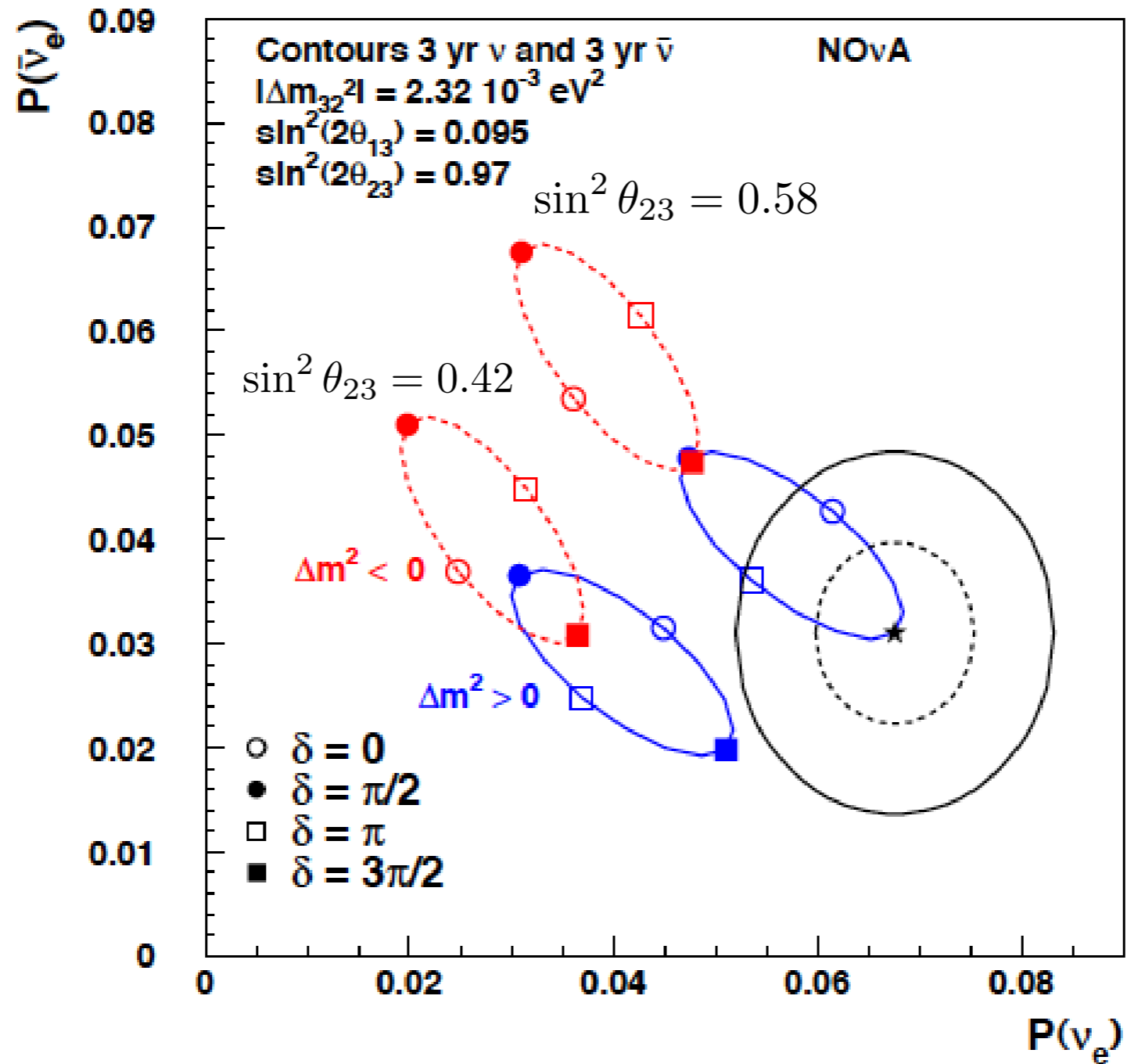
$$\theta_{crit} \approx \frac{\pi^2}{8} \frac{\sin 2\theta_{12}}{\tan \theta_{23}} \frac{\delta m_{21}^2}{\delta m_{31}^2} \left(\frac{4\Delta_{31}^2/\pi^2}{1 - \Delta_{31} \cot \Delta_{31}} \right) / (aL)$$



NOvA

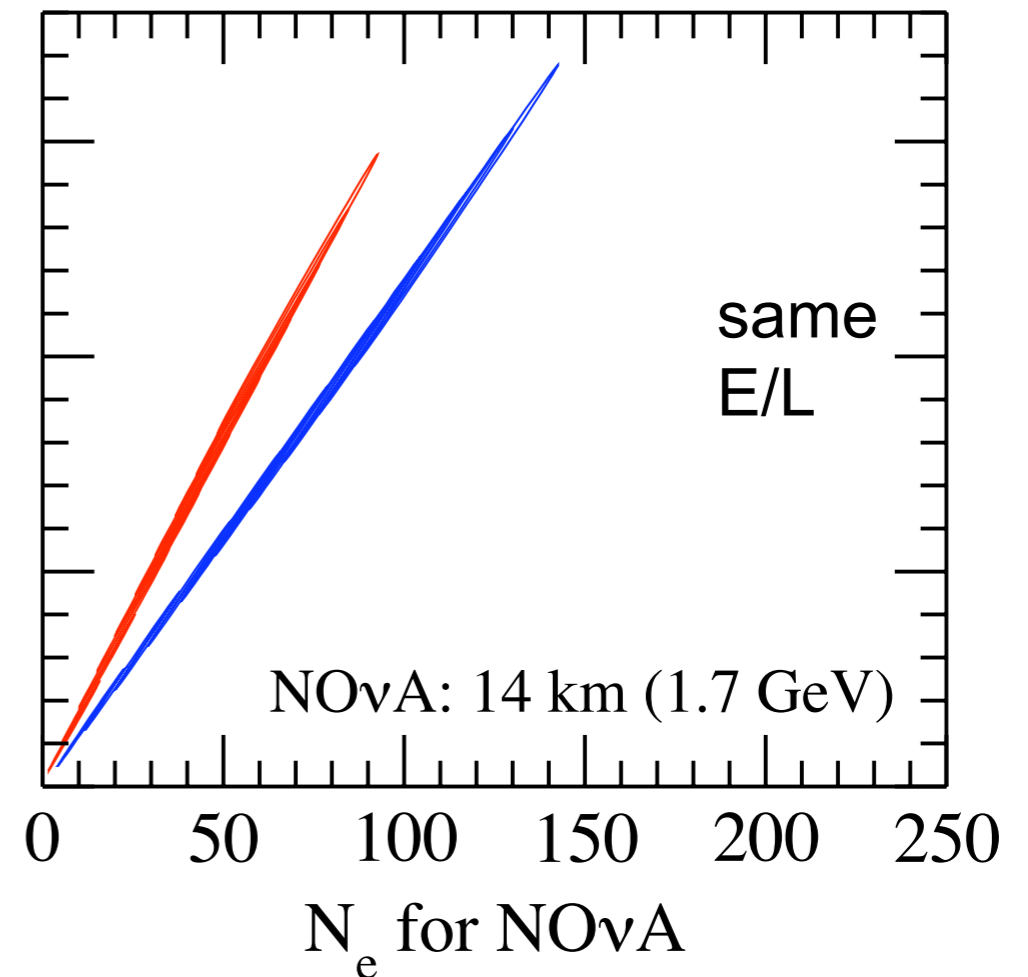
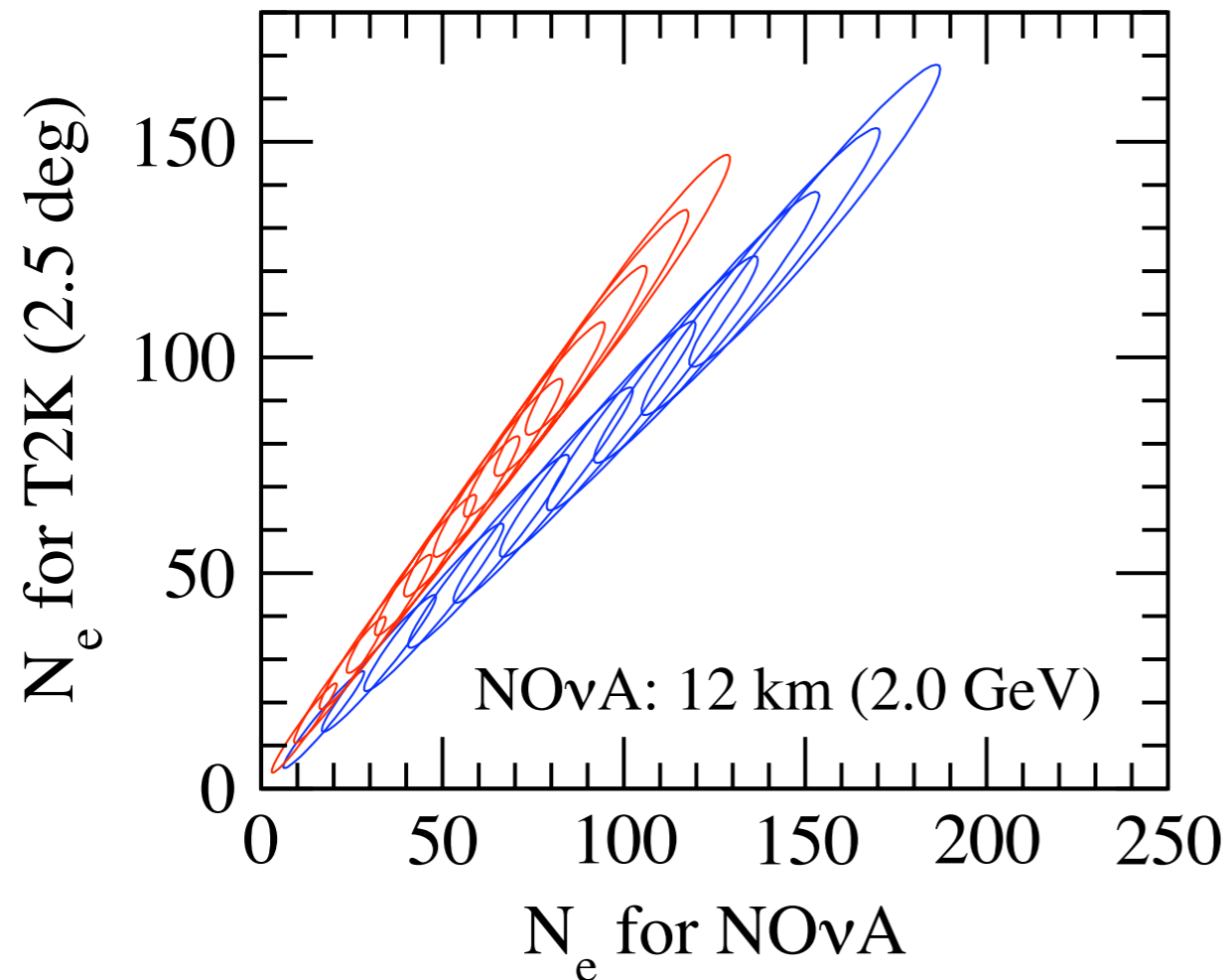


1 and 2 σ Contours for Starred Point



What about combining T2K and NOvA?

Neutrinos Only



Mena, Nunokawa + SP: [hep-ph/0609011](https://arxiv.org/abs/hep-ph/0609011)



Future Experiments:

- Near 1st Oscillation Maximum: $L/E = 500 \text{ km/GeV}$

T2HK $L=295\text{km}$, $\langle E \rangle = 0.65 \text{ GeV}$, off axis 2.5°

LBNE: $L=1300\text{km}$, $E = 1 \text{ to } 5 \text{ GeV}$, broad band beam

LENF $L=1300\text{km}$ $\langle E \rangle = 2.5 \text{ GeV}$

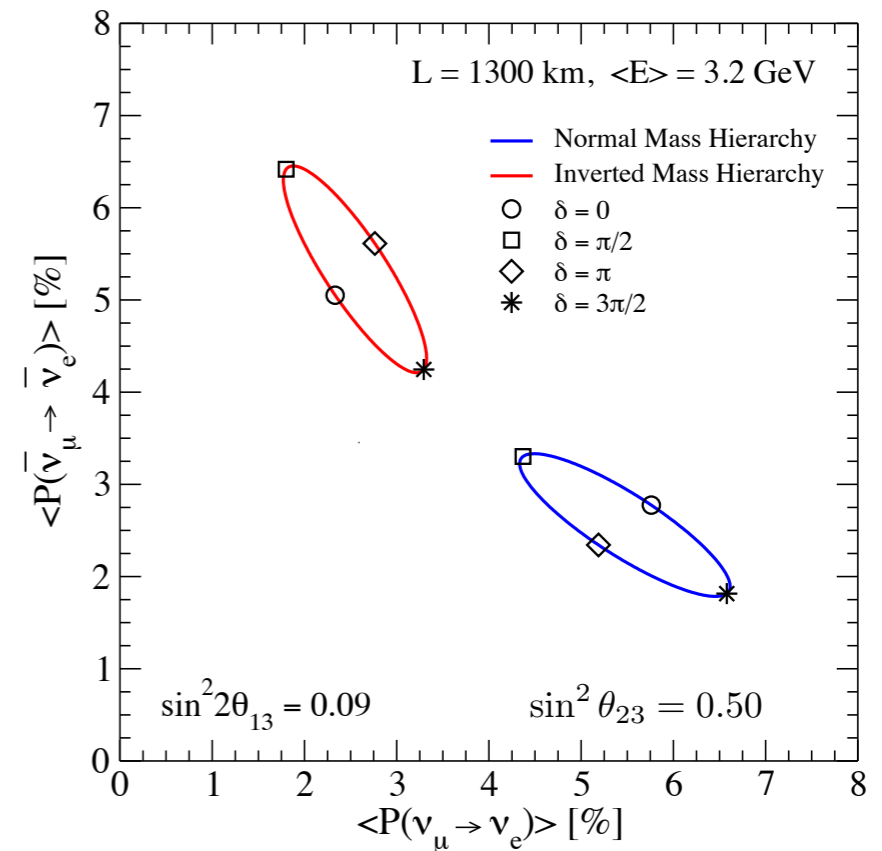
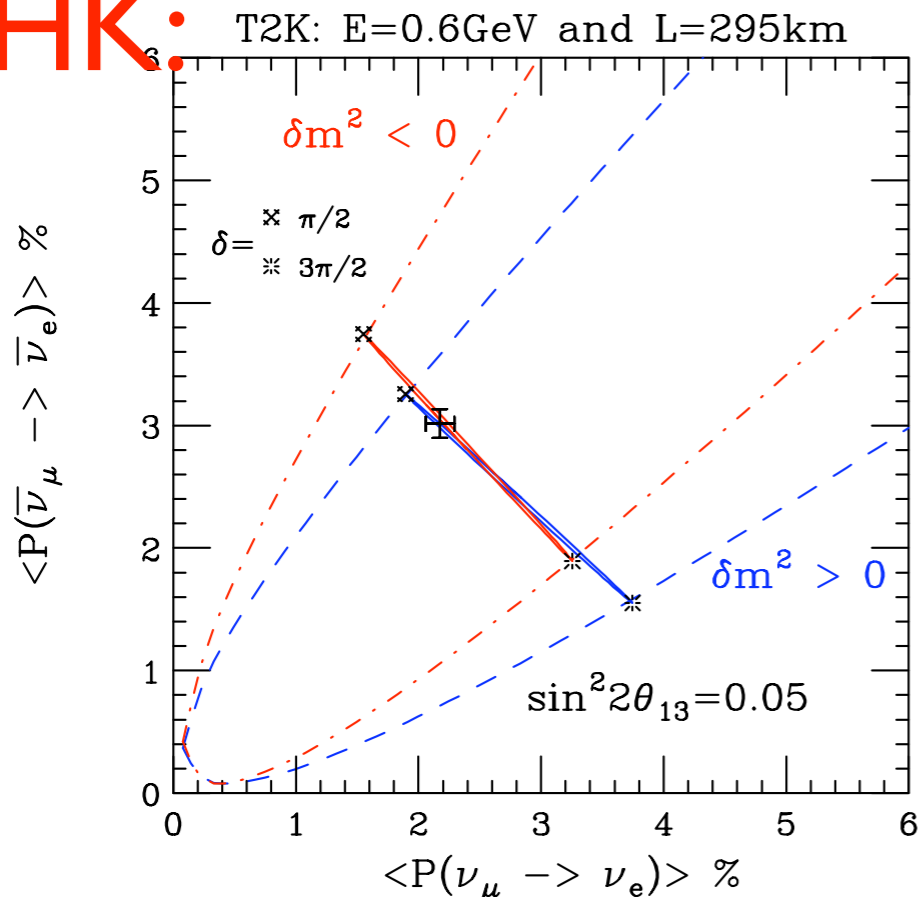
- Near the 2nd Oscillation Maximum: $L/E = 1500 \text{ km/GeV}$

ESS to Garpenberg (540km) $E = 200 \text{ to } 400 \text{ MeV}$, broad band beam

LBNE:

@ same L/E as NOvA

T2HK:

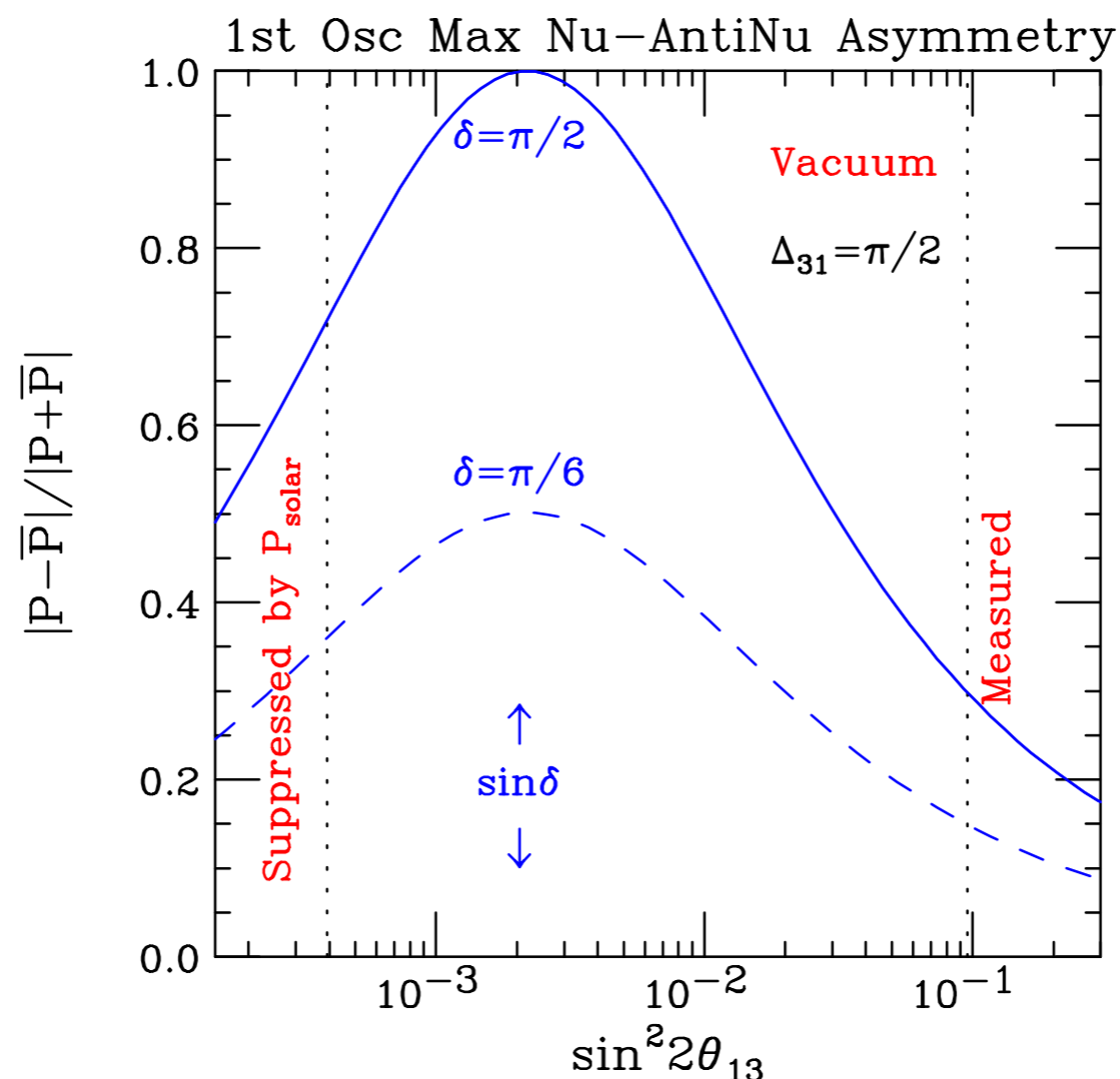


CPV & Neutrino Anti-Neutrino Asymmetry:

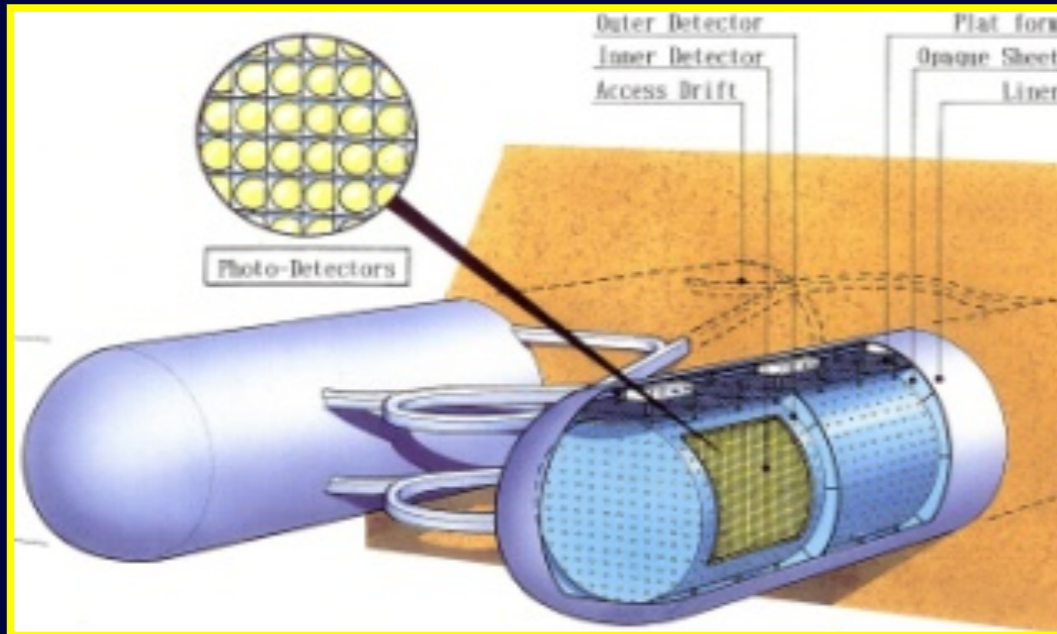
In Vacuum, at 1st Oscillation Maximum:

$$A_{vac} \equiv \frac{|P-\bar{P}|}{|P+\bar{P}|} \approx \frac{1}{11} \frac{\sin 2\theta_{13} \sin \delta}{(\sin^2 2\theta_{13} + 0.002)} = 0.3 \sin \delta$$

$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$ ranges is between $\frac{1}{2}$ and 2 times $P(\nu_\mu \rightarrow \nu_e)$!!!

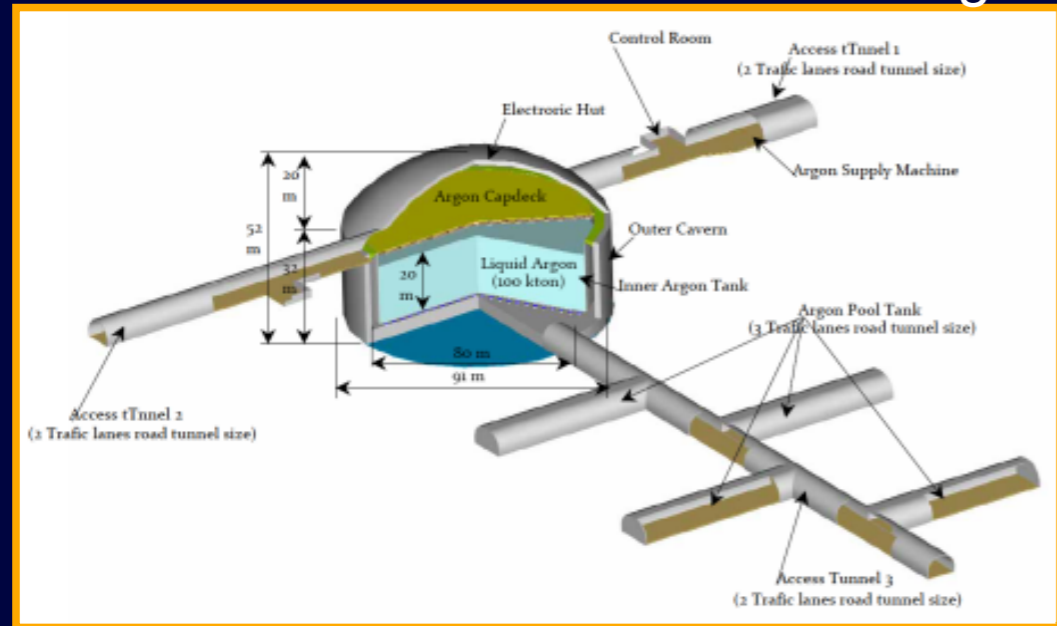


J-PARC+HK @ Kamioka
 $L=295\text{km}$ $OA=2.5\text{deg}$



LoI: The Hyper-Kamiokande Experiment
 arXiv:1109.3262v1

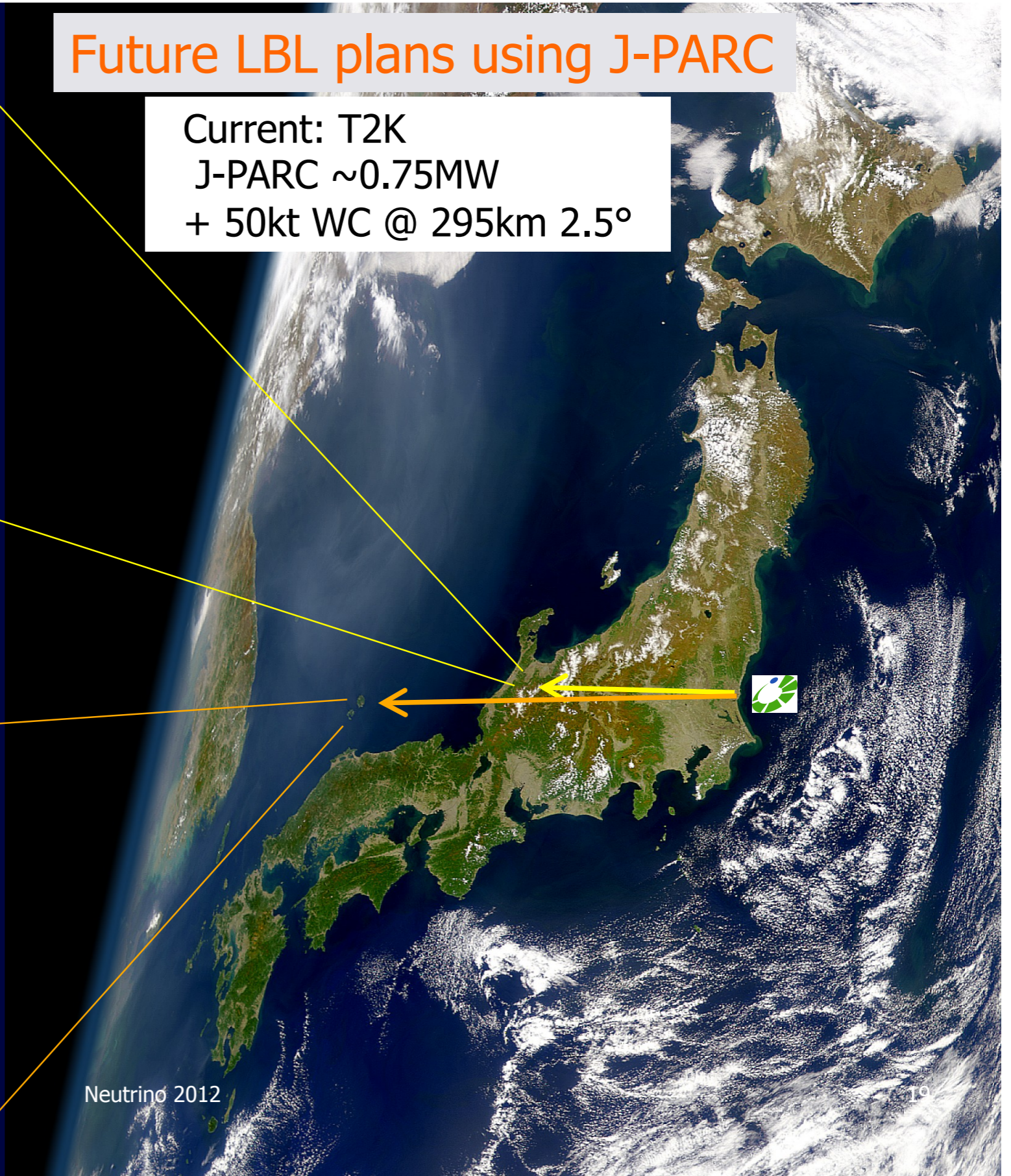
J-PARC+LAr @ Okinoshima
 $L=658\text{km}$ $OA=0.78\text{deg}$



J-PARC P32 (LAr TPC R&D), arXiv:0804.2111

Future LBL plans using J-PARC

Current: T2K
 J-PARC $\sim 0.75\text{MW}$
 + 50kt WC @ 295km 2.5°



Neutrino 2012

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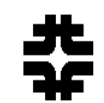
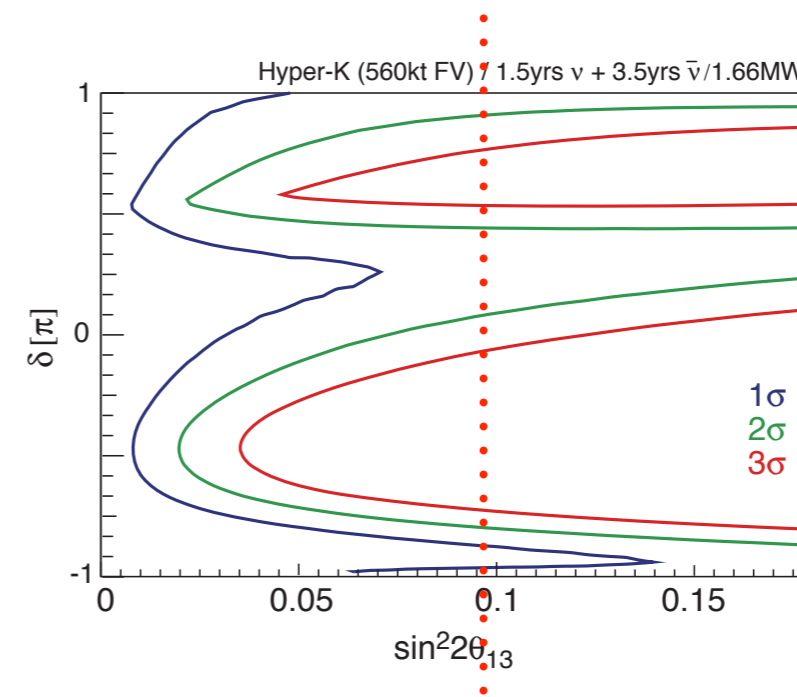


TABLE I. Detector parameters of the baseline design.

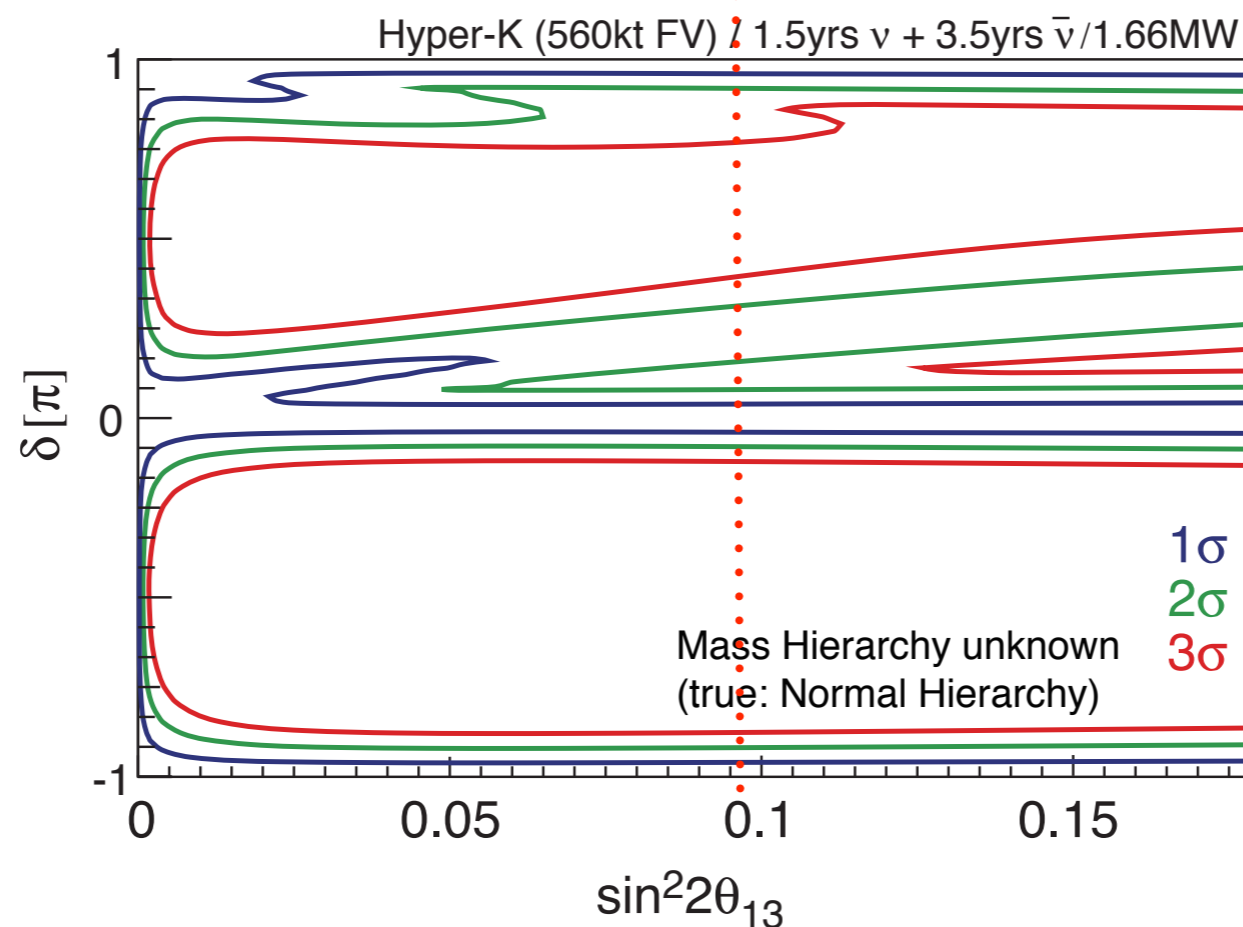
Detector type		Ring-imaging water Cherenkov detector
Candidate site	Address	Tochibora mine Kamioka town, Gifu, JAPAN
	Lat.	36°21'08.928"N
	Long.	137°18'49.688"E
	Alt.	508 m
	Overburden	648 m rock (1,750 m water equivalent)
	Cosmic Ray Muon flux	$1.0 \sim 2.3 \times 10^{-6} \text{ sec}^{-1} \text{ cm}^{-2}$
	Off-axis angle for the J-PARC ν	2.5° (same as Super-Kamiokande)
	Distance from the J-PARC	295 km (same as Super-Kamiokande)
Detector geometry	Total Volume	0.99 Megaton
	Inner Volume (Fiducial Volume)	0.74 (0.56) Megaton
	Outer Volume	0.2 Megaton
Photo-multiplier Tubes	Inner detector	99,000 20-inch ϕ PMTs 20% photo-coverage
	Outer detector	25,000 8-inch ϕ PMTs
Water quality	light attenuation length	> 100 m @ 400 nm
	Rn concentration	< 1 mBq/m ³

Mass Hierarchy:



For $\sin^2 2\theta_{13} = 0.1$, the mass hierarchy can be determined with more than 3σ significance for 46% of the δ parameter space.

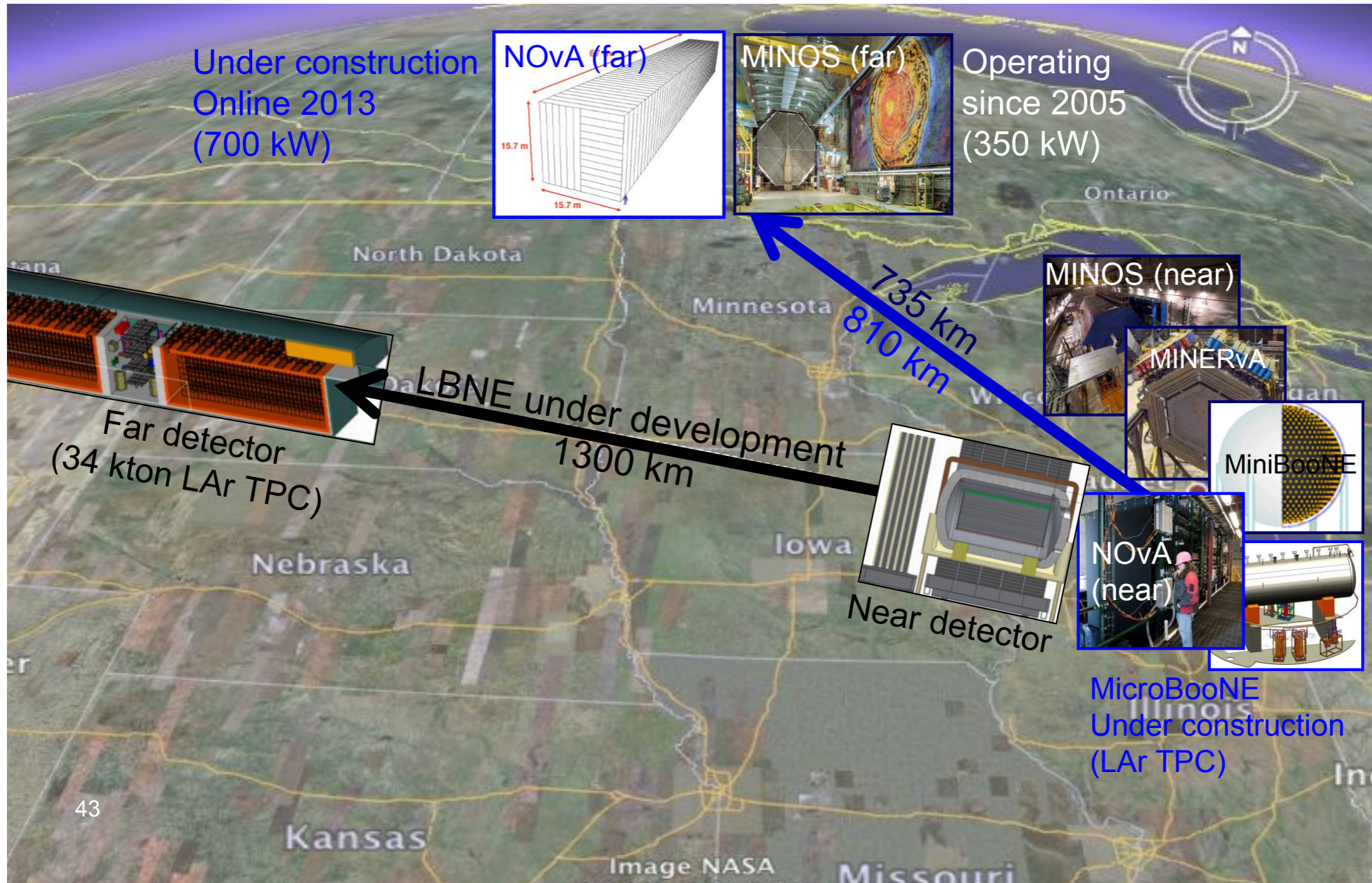
CPV:



MH from Atm Nus:

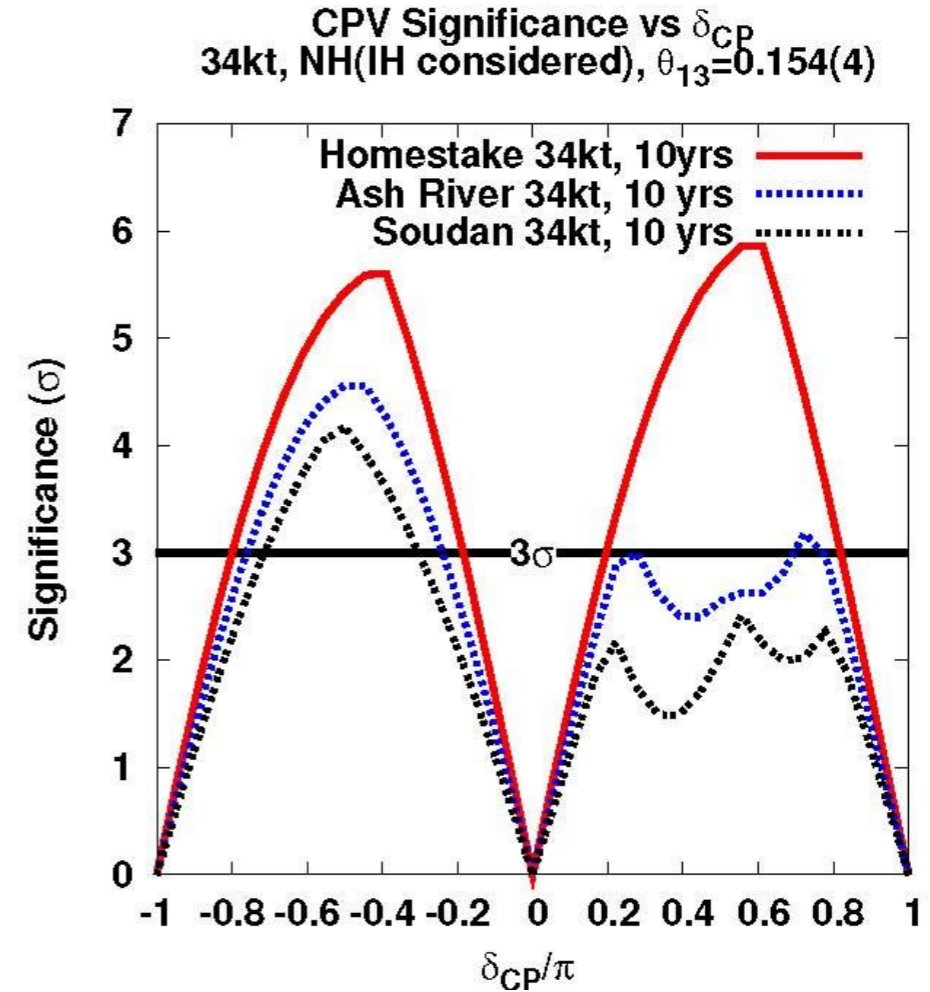
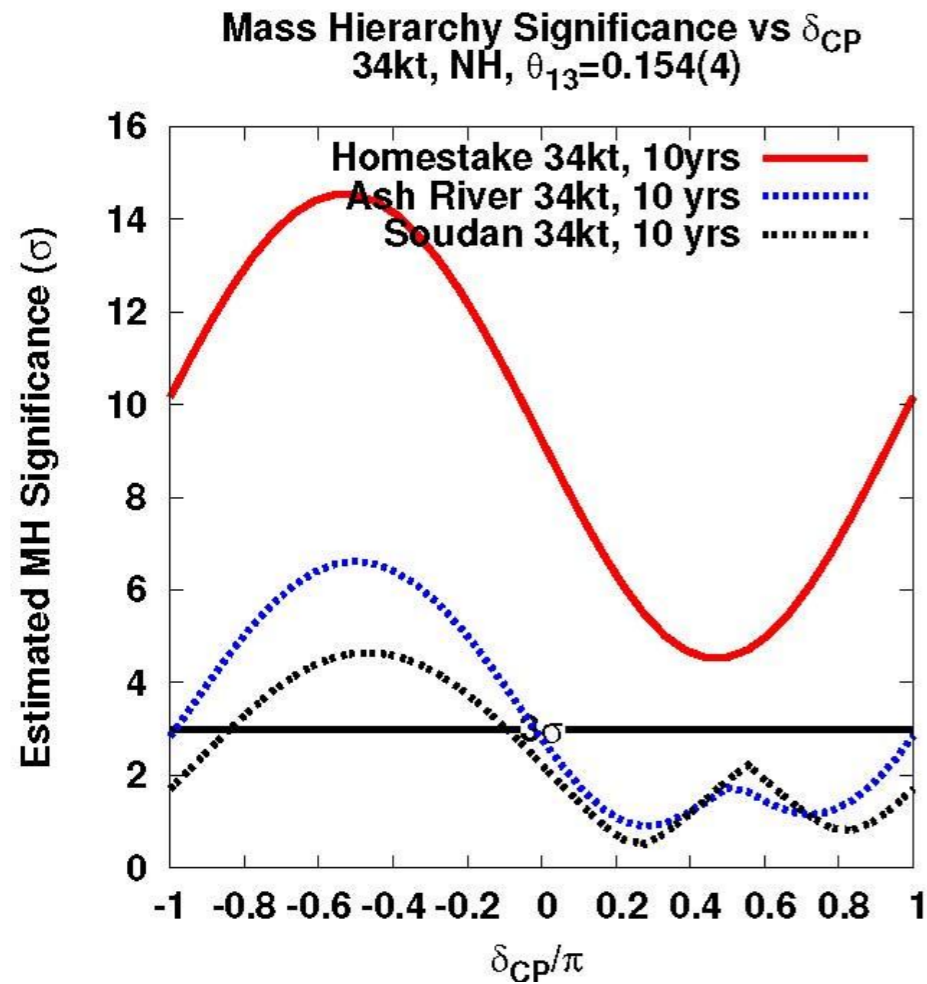
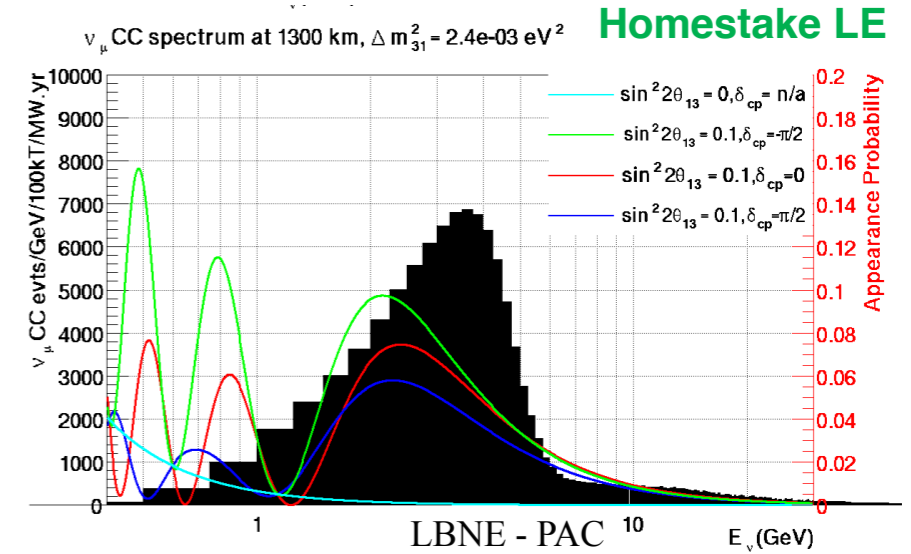


LBNE



LBNE original

- LBNE:
 - Beamline @ Fermilab: 1-5 GeV, 700 kW ----> 2.1 MW
 - Baseline: 1300 km on-axis, Fermilab to Homestake
 - Detector: 34 ktons LAr @ 4300 mwe in Homestake



Staging??? LBNO+LBNE=LBNU



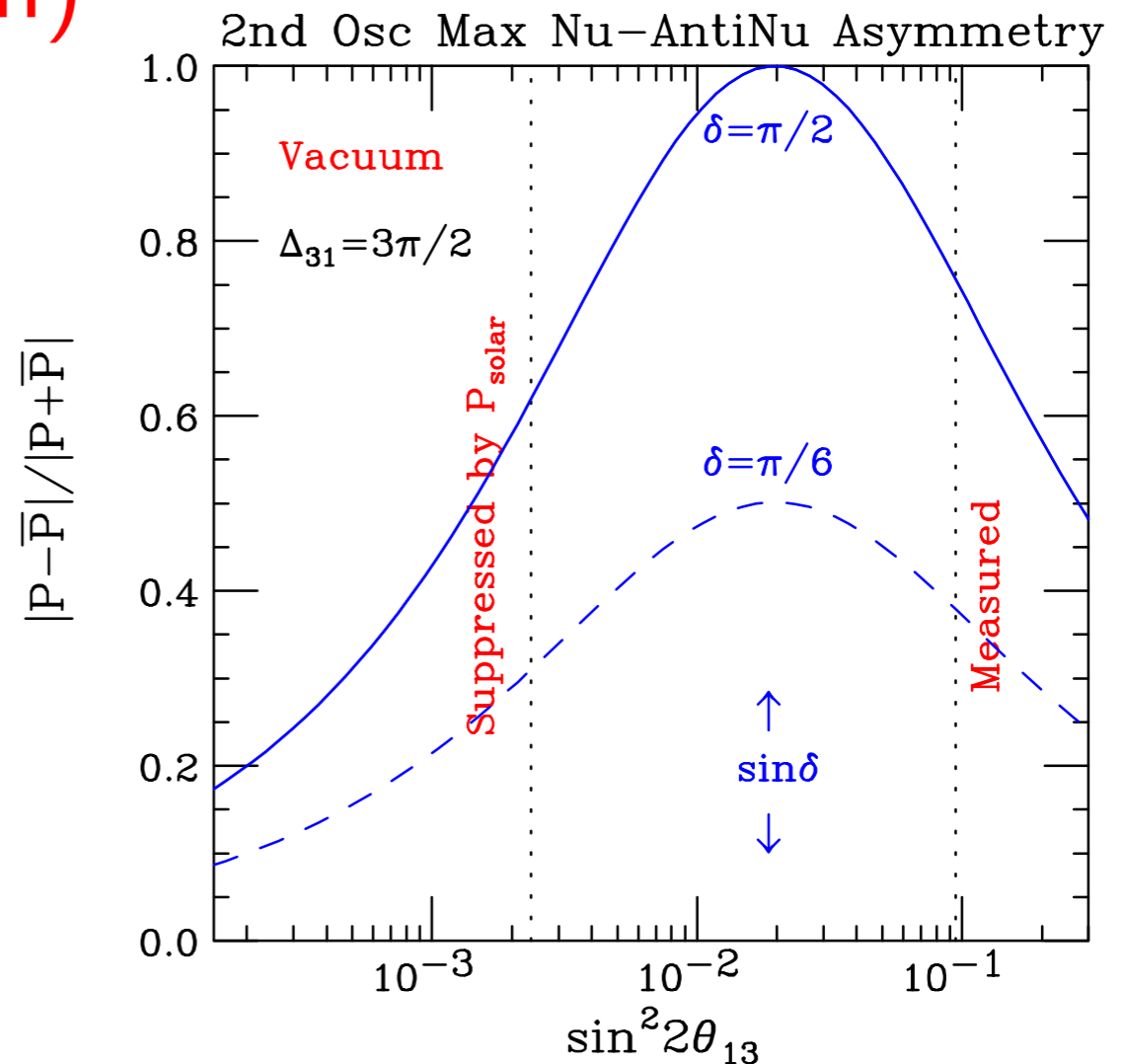
2nd Oscillation Max:

ESS to Garpenburg (540km)

$$A_{vac} \approx 0.75 \sin \delta$$

$$A_{vac}(2^{nd} \text{ OM}) \approx 2.5 A_{vac}(1^{st} \text{ OM})$$

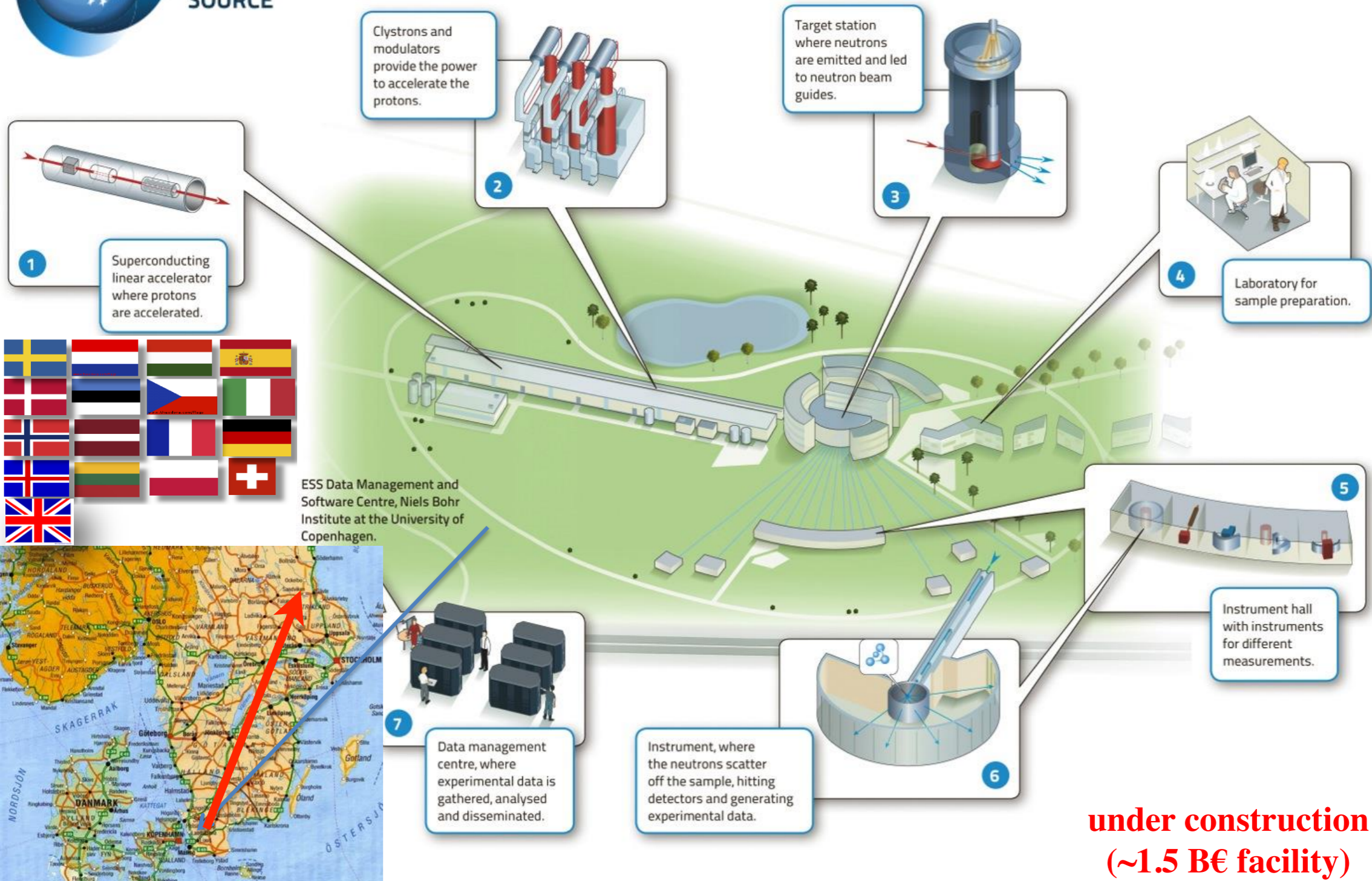
(9/11 of 3)



$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$ ranges is between $\frac{1}{7}$ and $7 P(\nu_\mu \rightarrow \nu_e)$

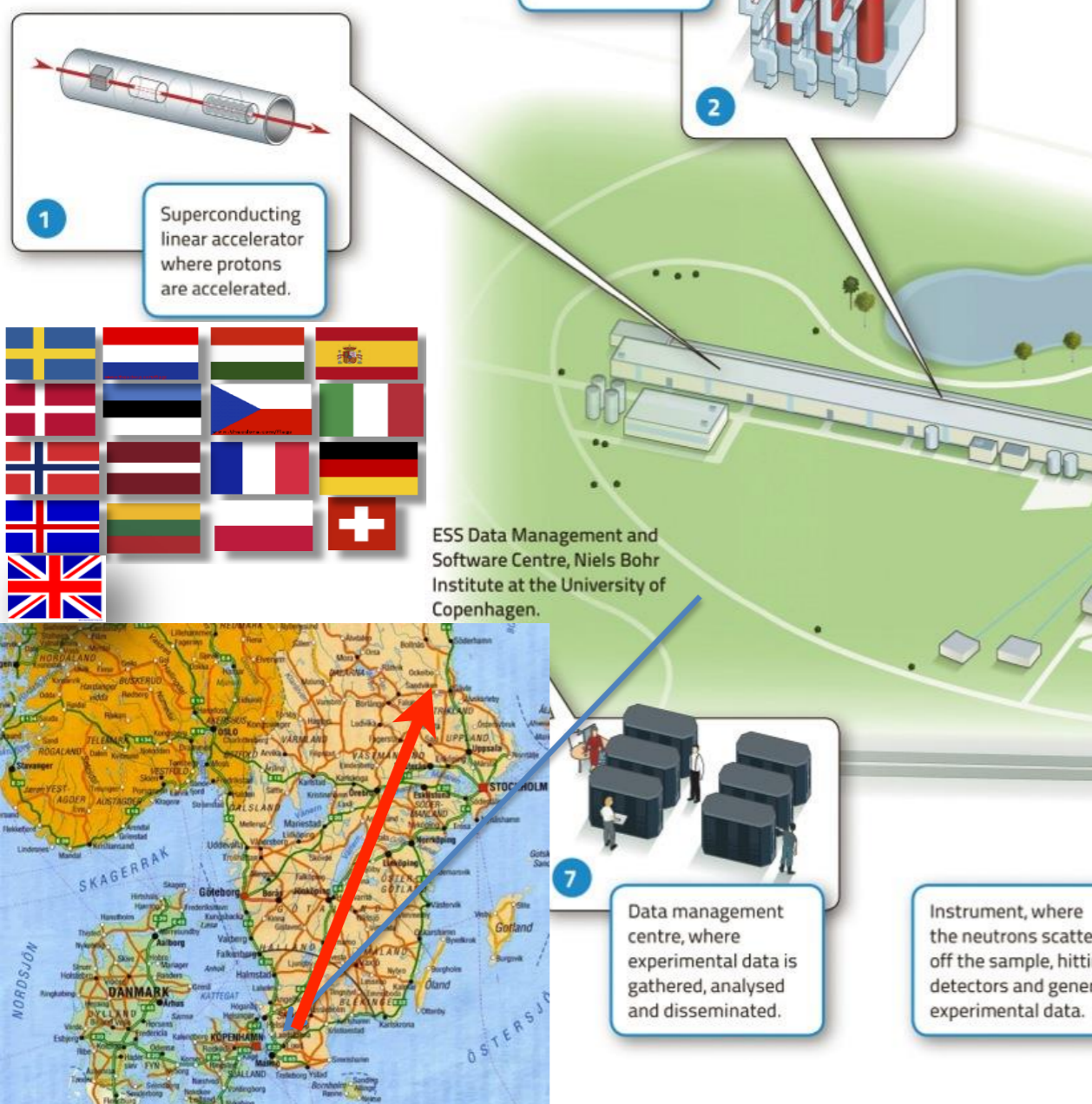
Appearance Probabilities more dynamic near 2nd Osc. Max. than 1st. OM





**under construction
(~1.5 B€ facility)**

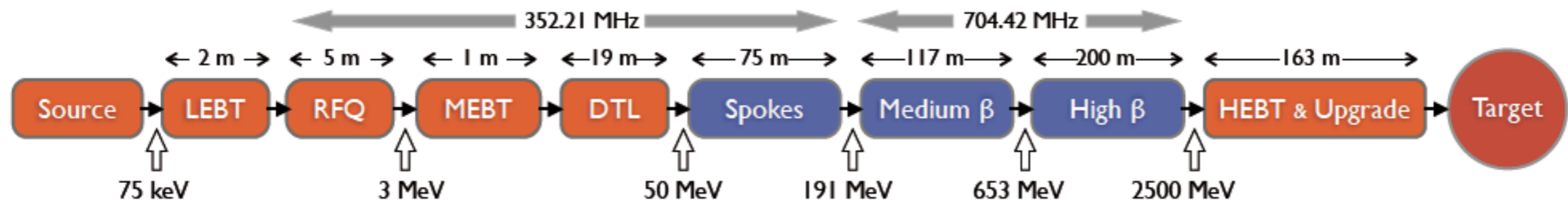
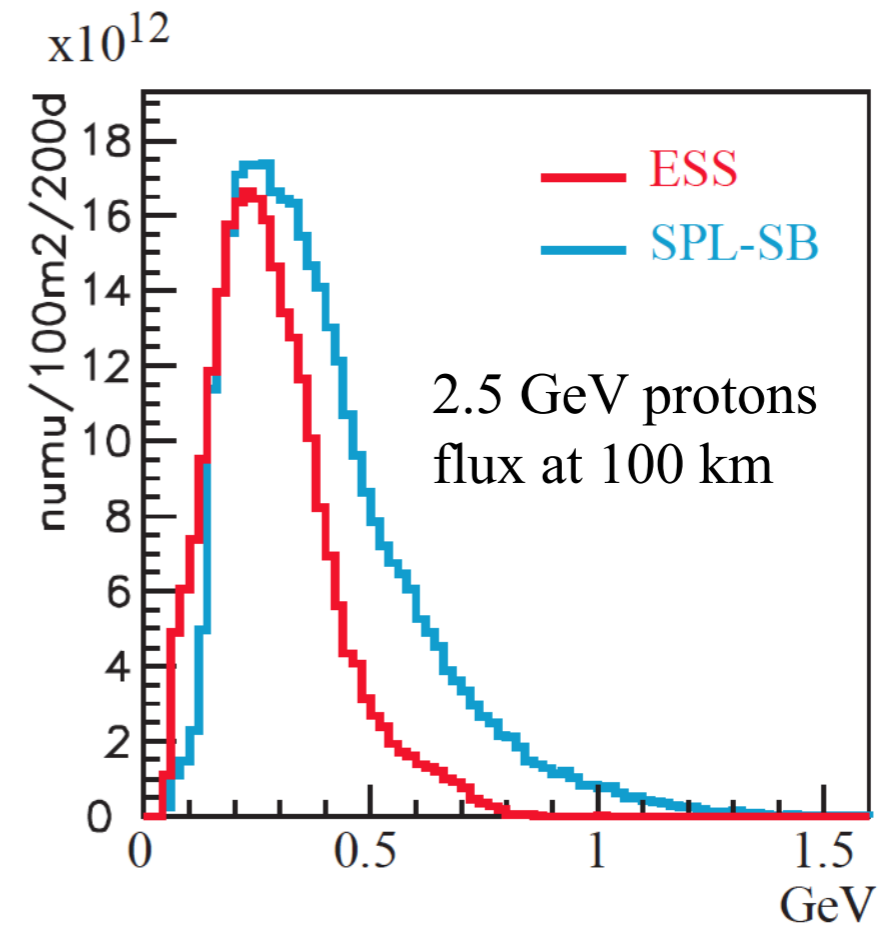
Detector: 500kt WC, MEMPHYS



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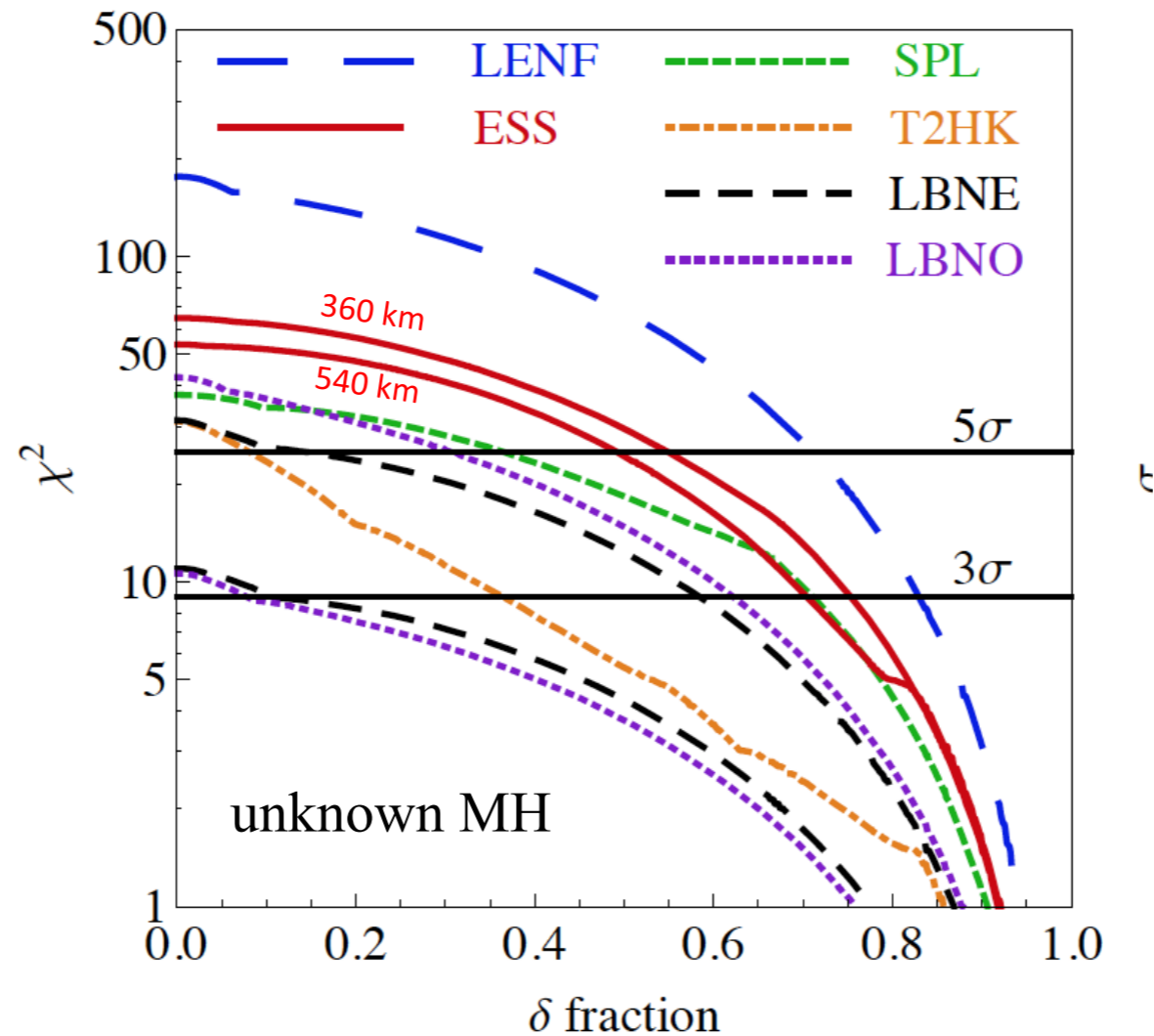
How to add a neutrino facility?

- 2 GeV protons: ~ 300 MeV neutrinos
- No perturbation of the neutron facility
- Close technical collaboration at early stage
- Acceptable cost
- **Linac modifications:**
 - double the rate (14 Hz \rightarrow 28 Hz), one pulse for neutrinos and one pulse for neutrons (5 MW each)
 - additional RF power to drive the two beams (for neutrons and neutrinos)
 - install upgradable power sources
 - or double the power sources (free space has to be foreseen since now)



- *For a fraction of the cost we can get a 5MW proton driver for Neutrino Physics*

CPV



- LBNE: 5+5 years, 0.7 MW, 10/35 kt LAr
- T2HK: 3+7 years, 0.75 MW, 500 kt WC (5%/10% syst. errors)
- SPL: 2+8 years, 4 MW, 500 kt WC (130 km, 5%/10% syst. errors)
- ESS: 2+8 years, 5 MW, 500 kt WC (2 GeV, 360/540 km, 5%/10% syst. errors)
- C2Py: 20/100 kt LAr, 0.8 MW, 2300 km

another possibility: Daedalus



nu_mu Disappearance:

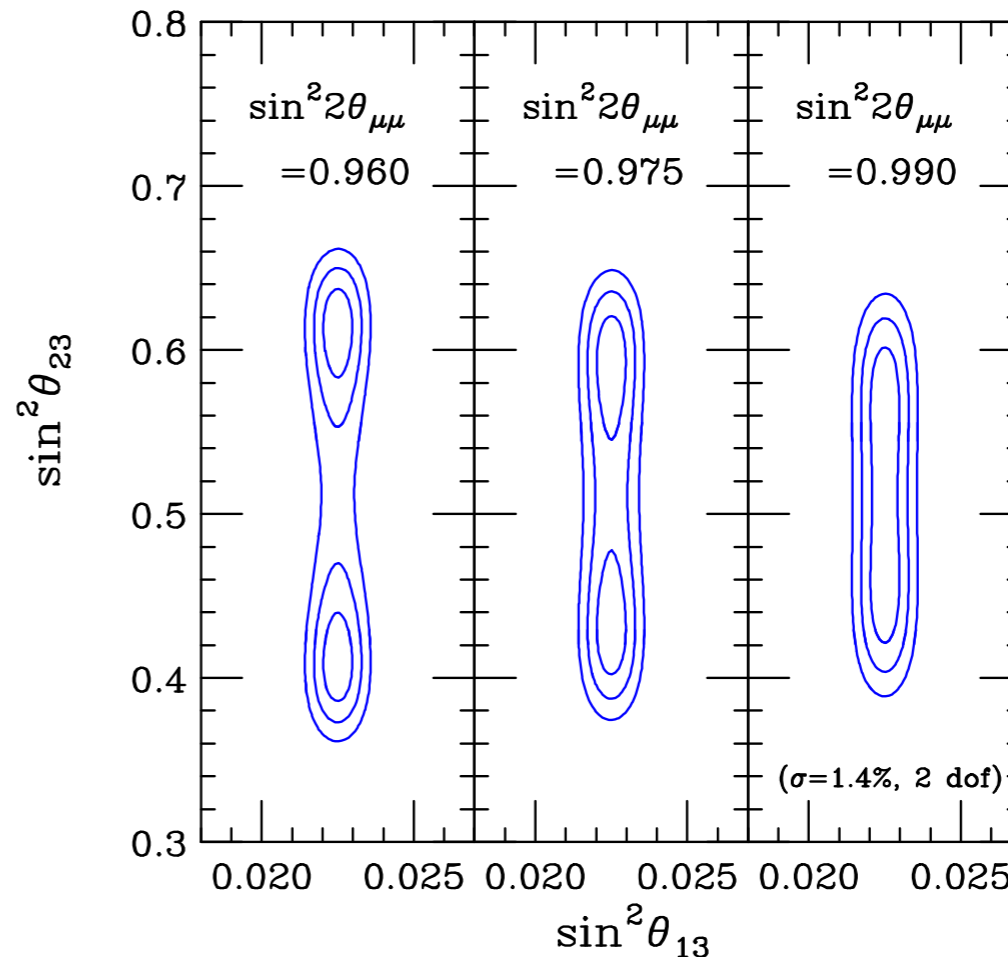
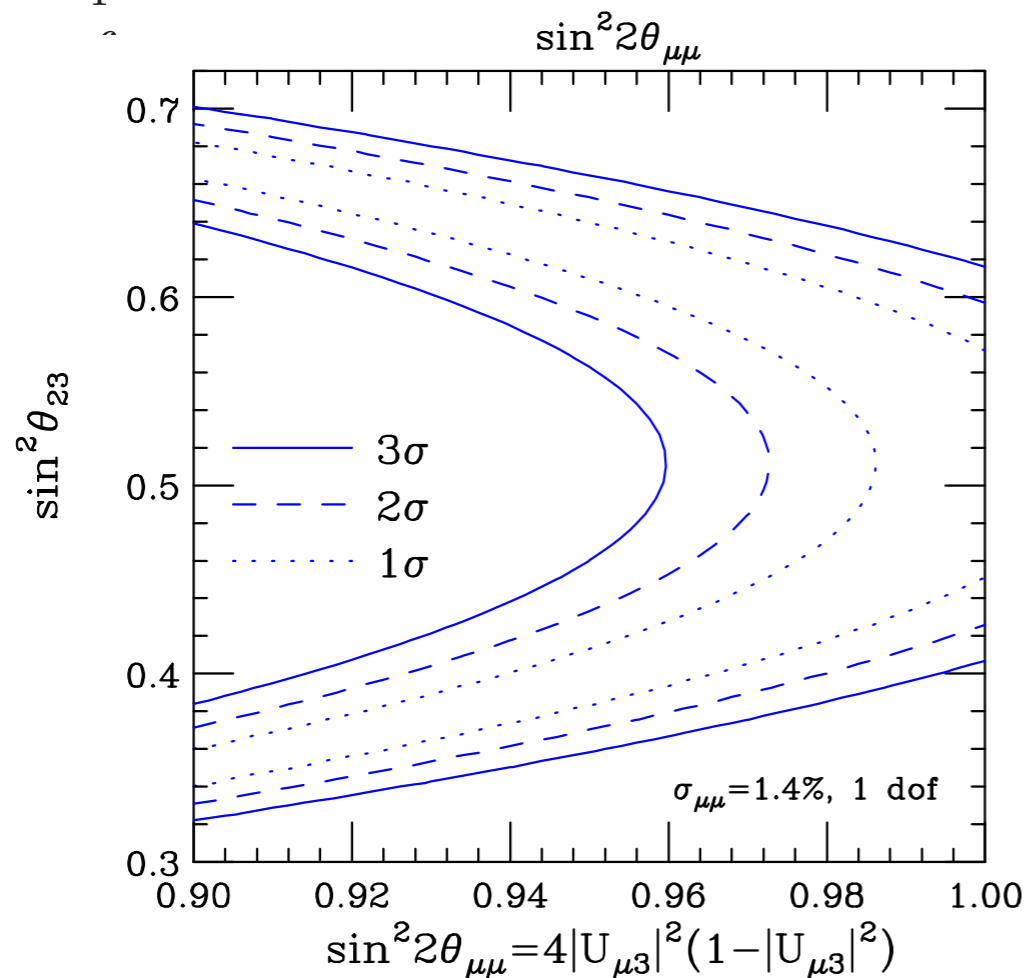
$$\sin^2 2\theta_{\mu\mu} \equiv 4|U_{\mu 3}|^2(1 - |U_{\mu 3}|^2)$$

$$\sin^2 \theta_{23}^{(1)} = \sin^2 \theta_{\mu\mu} / \cos^2 \theta_{13} \approx \sin^2 \theta_{\mu\mu} (1 + \sin^2 \theta_{13}),$$

$$\sin^2 \theta_{23}^{(2)} = \cos^2 \theta_{\mu\mu} / \cos^2 \theta_{13} \approx \cos^2 \theta_{\mu\mu} (1 + \sin^2 \theta_{13}),$$

$$\theta_{\mu\mu} \leq \frac{\pi}{4}$$

23 - Modified Octant Degeneracy:



$$\sin^2 2\theta_{\mu\mu} \equiv 4|U_{\mu 3}|^2(1 - |U_{\mu 3}|^2) = 0.975$$

$$\sigma_{\mu\mu} = 1.4\%$$

Coloma, Minakata and Parke
arXiv:2014.????

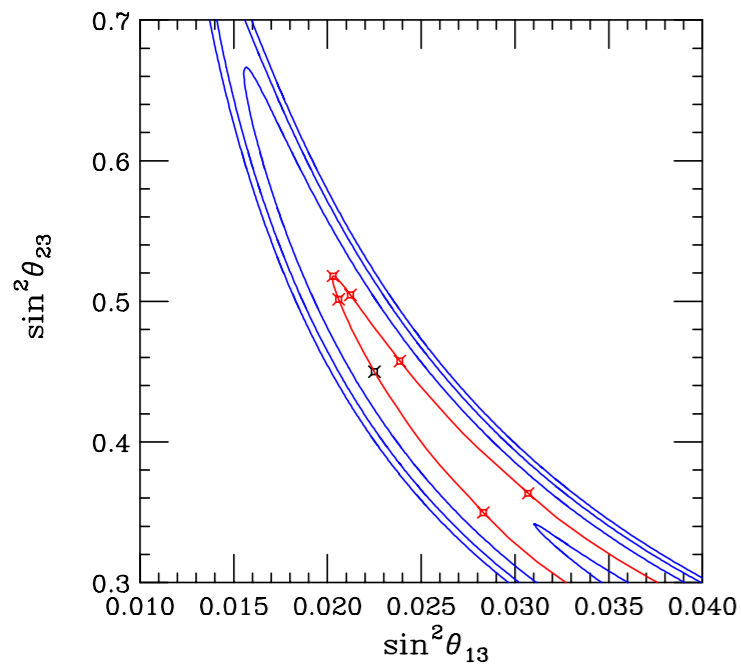


Generalized Intrinsic Degeneracy: (Coloma, Minakata and SP)

Assume θ_{13}, θ_{23} and δ unknown:

ν_e -Appearance

$P(\nu_\mu \rightarrow \nu_e)$ and $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$



$\delta = 60, 70, 80, 90, 100, 110, 120$ degrees

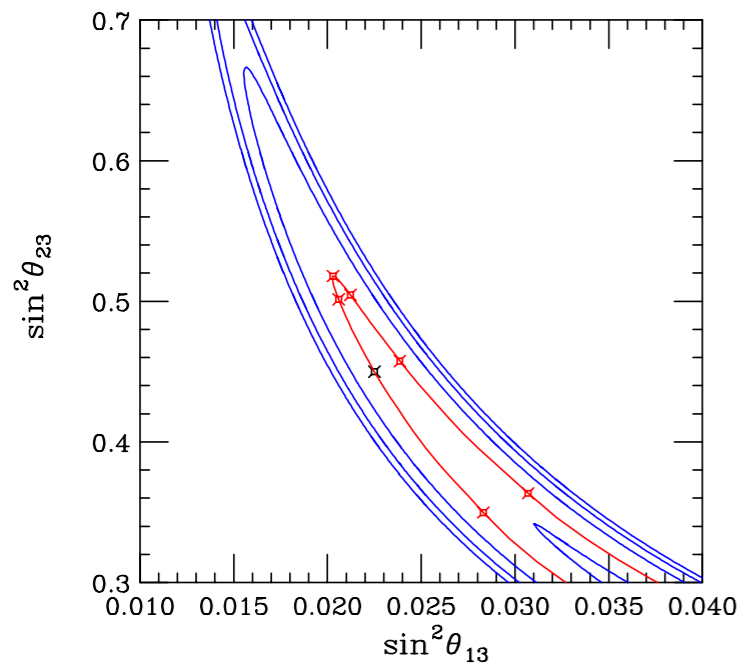


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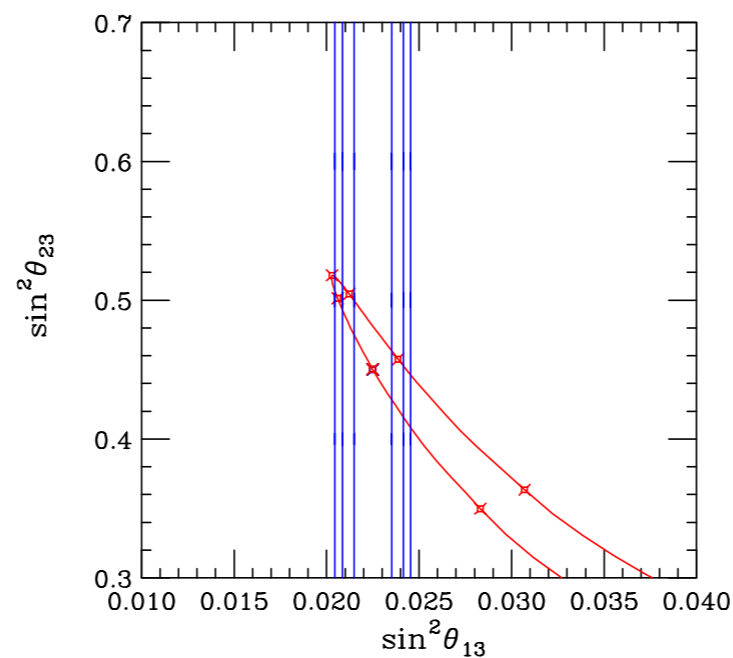
ν_e -Appearance

$P(\nu_\mu \rightarrow \nu_e)$ and $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$



ν_e -Disappearance

$P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$



$\delta = 60, 70, 80, 90, 100, 110, 120$ degrees

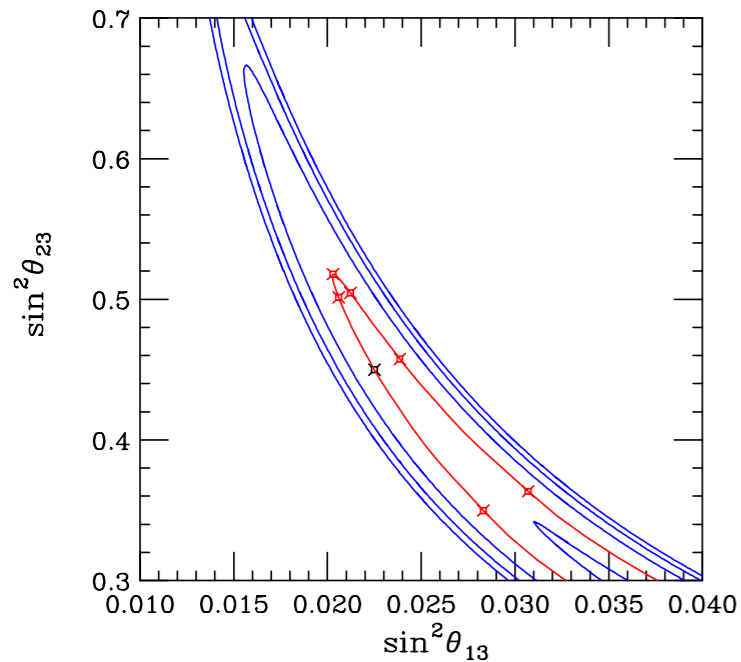


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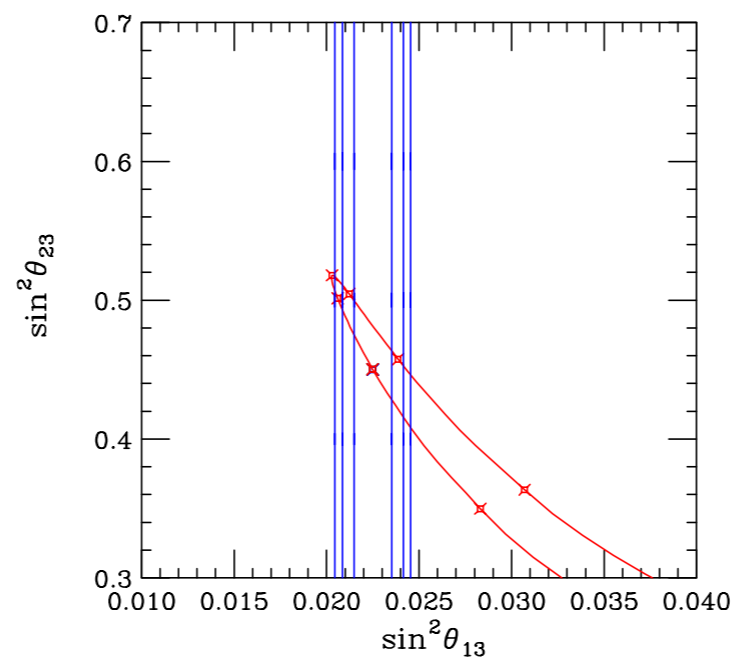
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$P(\nu_\mu \rightarrow \nu_e)$ and $P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)$



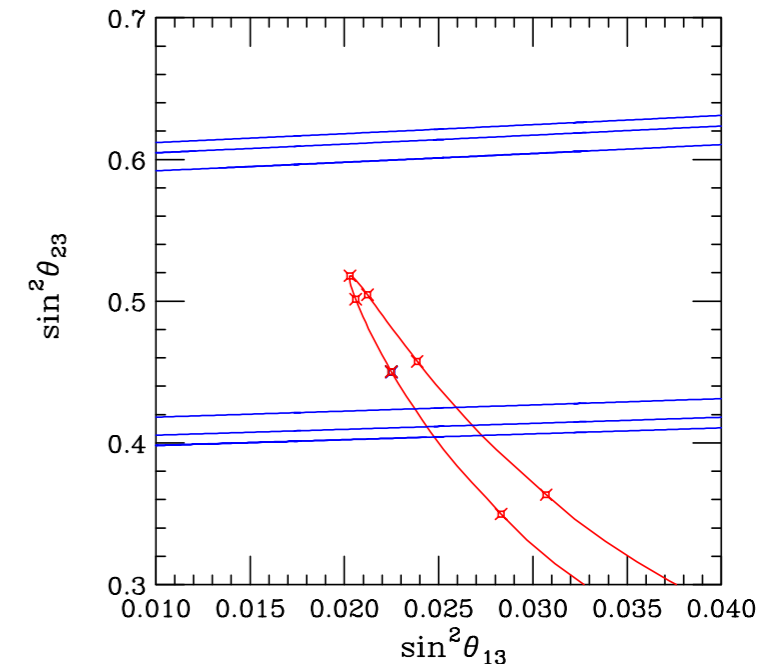
ν_e -Disappearance

$P(\bar{\nu}_e \rightarrow \bar{\nu}_e)$



ν_μ -Disappearance

$P(\nu_\mu \rightarrow \nu_\mu)$

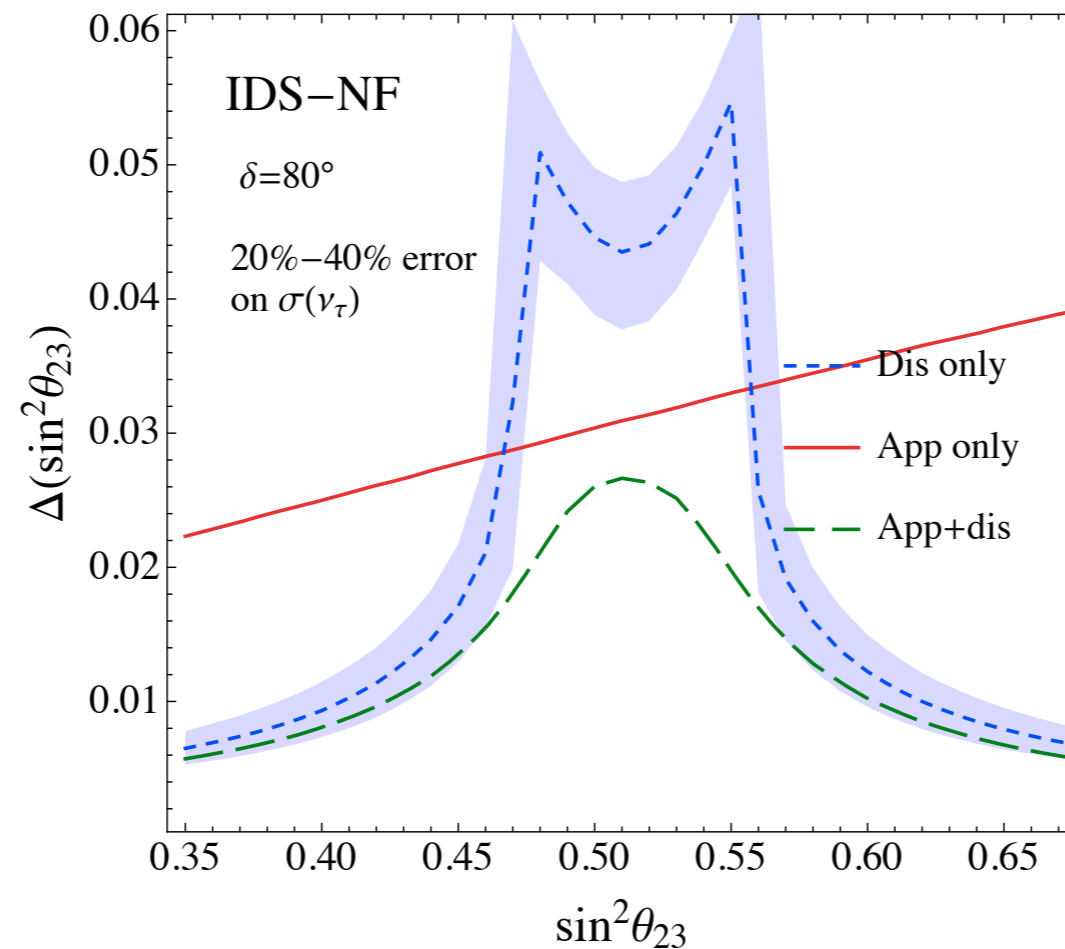


$\delta = 60, 70, 80, 90, 100, 110, 120$ degrees

Spectral information can help break this degeneracy



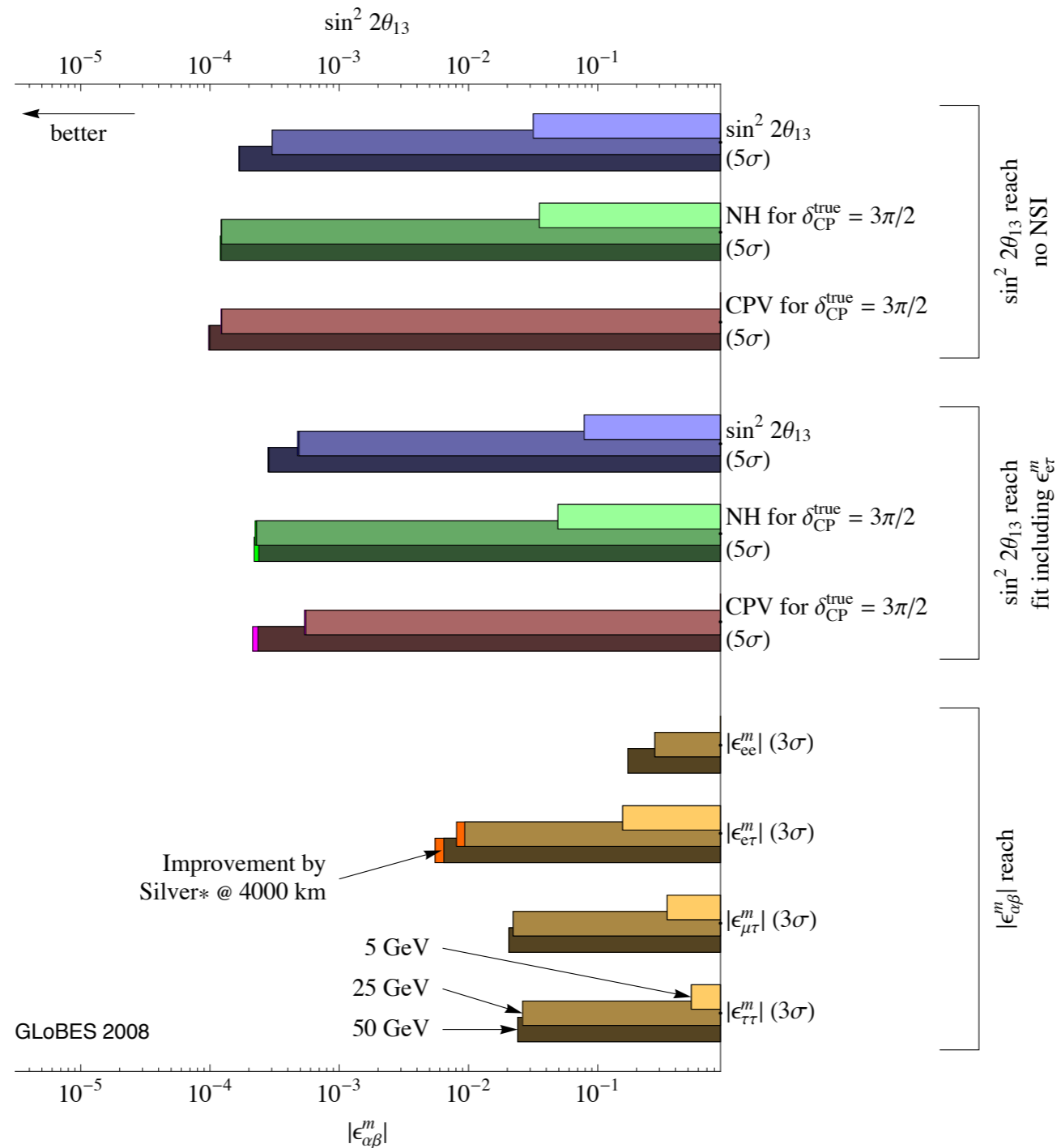
Uncertainty on Theta23 for NF:



Coloma, Minakata and Parke
arXiv:2014.????



Non-Standard Interactions:



Conclusions:

- To Be Majorana or Not To Be Majorana?
- We know $(|U_{e2}|^2, |U_{e3}|^2, |U_{\mu3}|^2)$ with precision of (5,10,15)% but have little information on the other 6 elements of the PMNS matrix without assuming Unitarity. Stringent tests of the ν SM Paradigm needed.
- Determining the Mass Hierarchy & measuring CPV are the next steps. Tau's?
- m_{lite} , if $\ll \delta m_{21}^2$, a new scale to explain !



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 - We know $(|U_{e2}|^2, |U_{e3}|^2, |U_{\mu3}|^2)$ with precision of (5,10,15)% but have little information on the other 6 elements of the PMNS matrix without assuming Unitarity. Stringent tests of the ν SM Paradigm needed.
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 - m_{lite} , if $\ll \delta m_{21}^2$, a new scale to explain !
 - Are there lite Sterile neutrinos?
- Can we exclude $|U_{e4}|^2$ and $|U_{\mu4}|^2 > 0.01$, say, for $\delta m^2 \sim 1eV^2$
- Solving the Neutrino Masses and Mixing pattern is difficult challenge for Theory! Need hints.
 - Where are there further “SURPRISES” in the Neutrino Sector?



We haven't got the money,

so we'll have to think!

E. Rutherford

