

# Future High Energy Colliders

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## Outline:

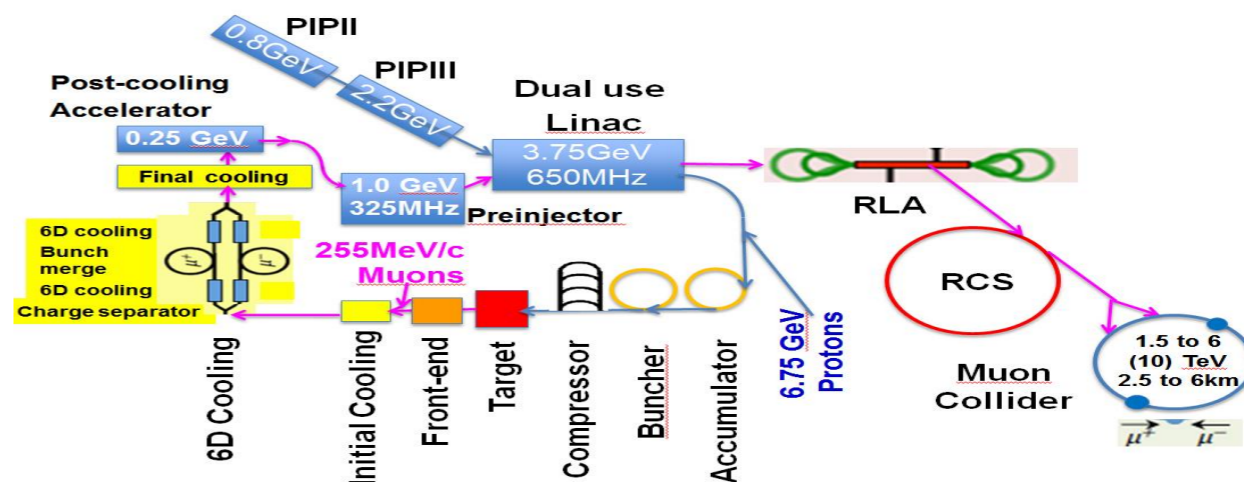
- A Higgs boson — Now what?
- Basics of Future High Energy Colliders
- Higgs Studies and More Scalars
- Supersymmetry
- Other BSM physics: Dynamics, Dilatons, ...
- Summary and Outlook

(parallel talks Friday)

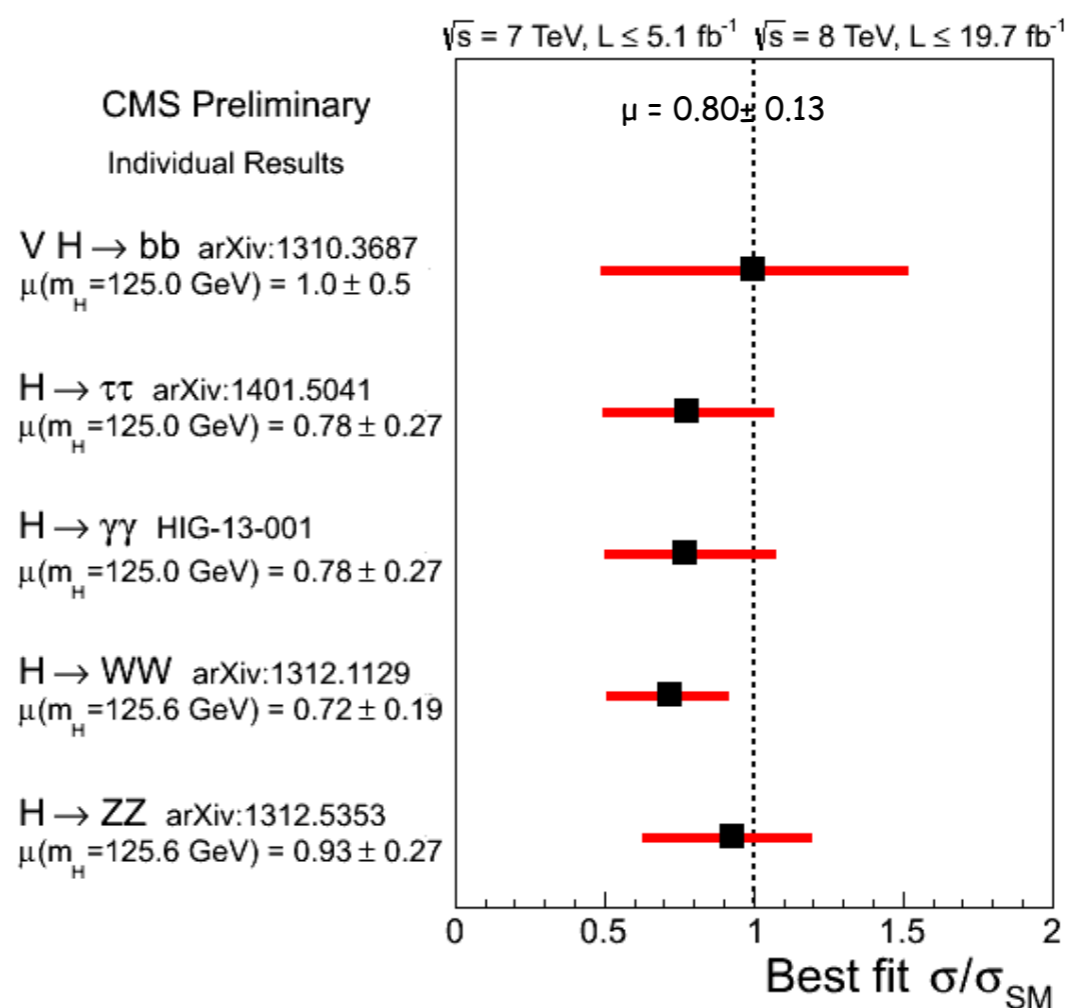
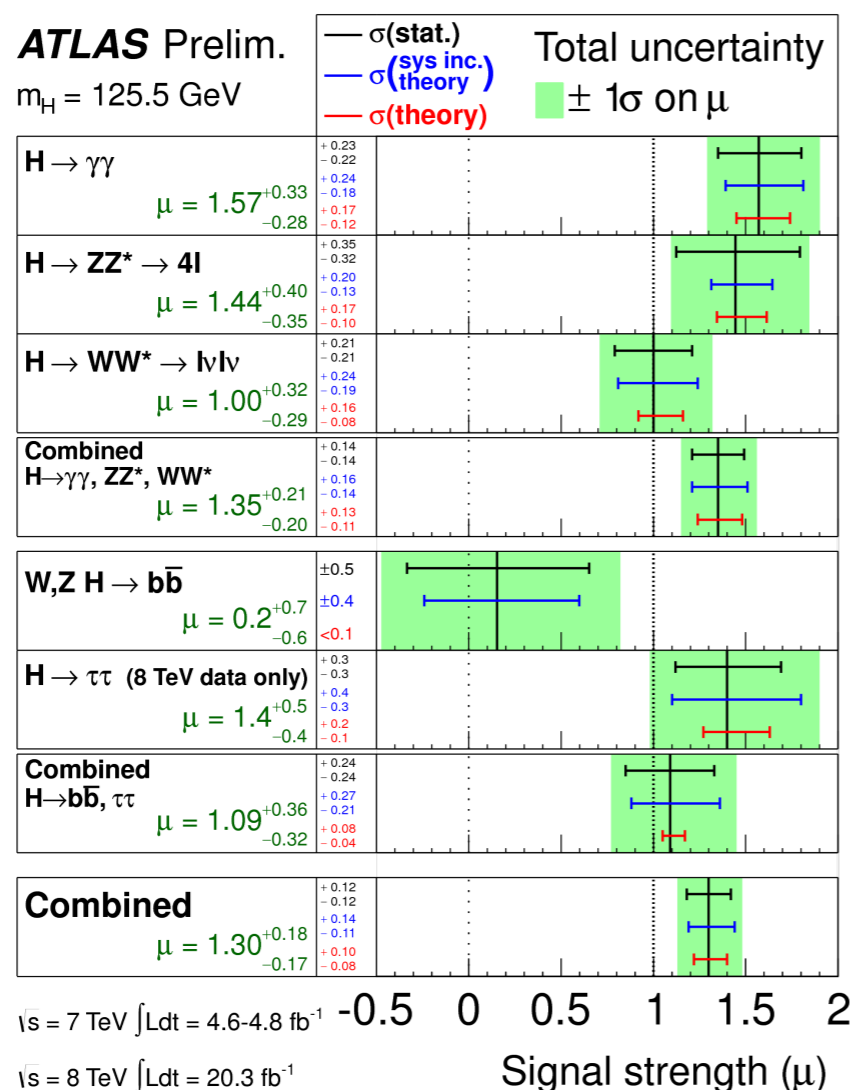
(Zhen Liu)

(Adam Martin)

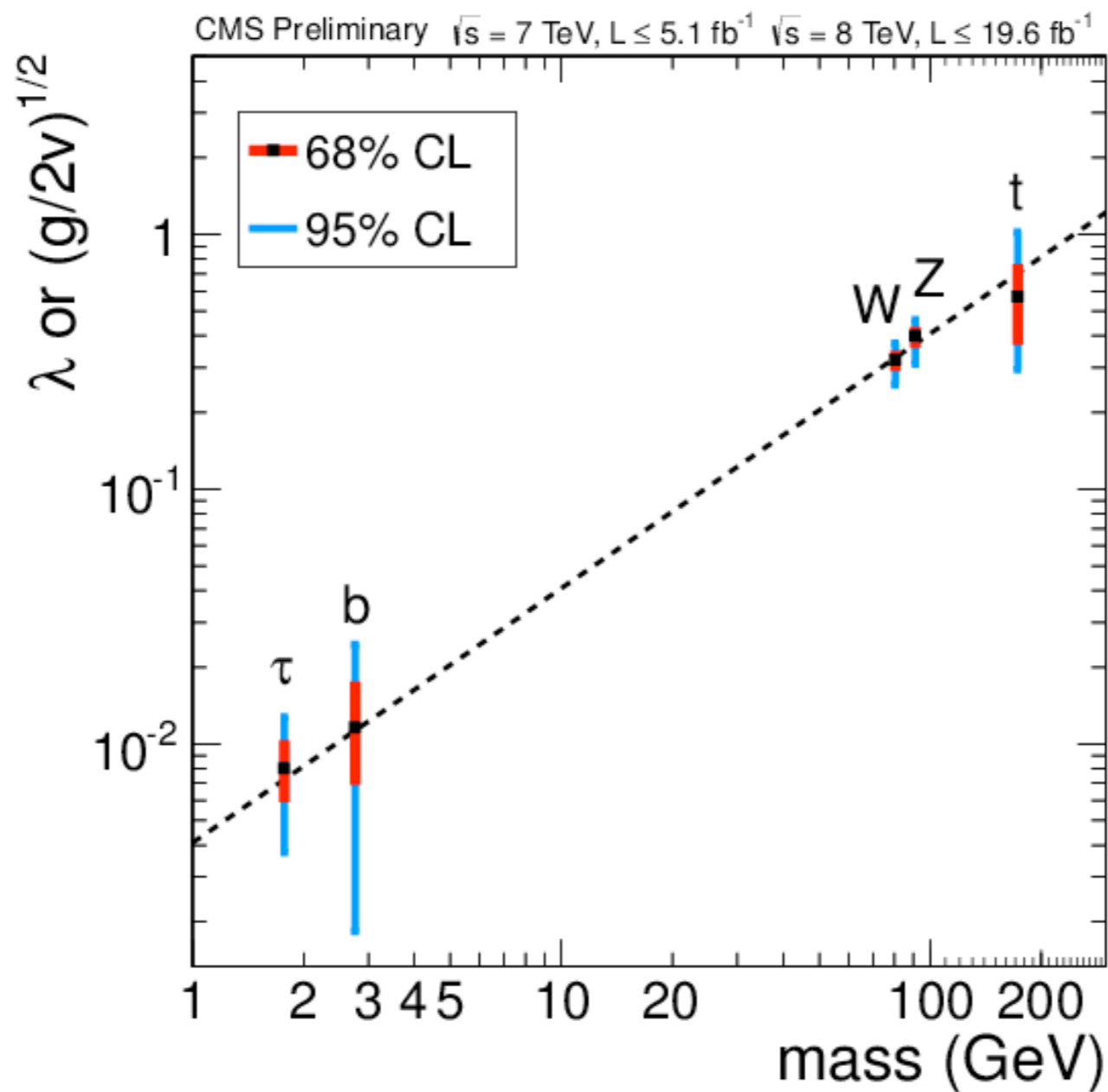
Muon Accelerator Program  
Spring Meeting  
Fermilab, May 27-31, 2014



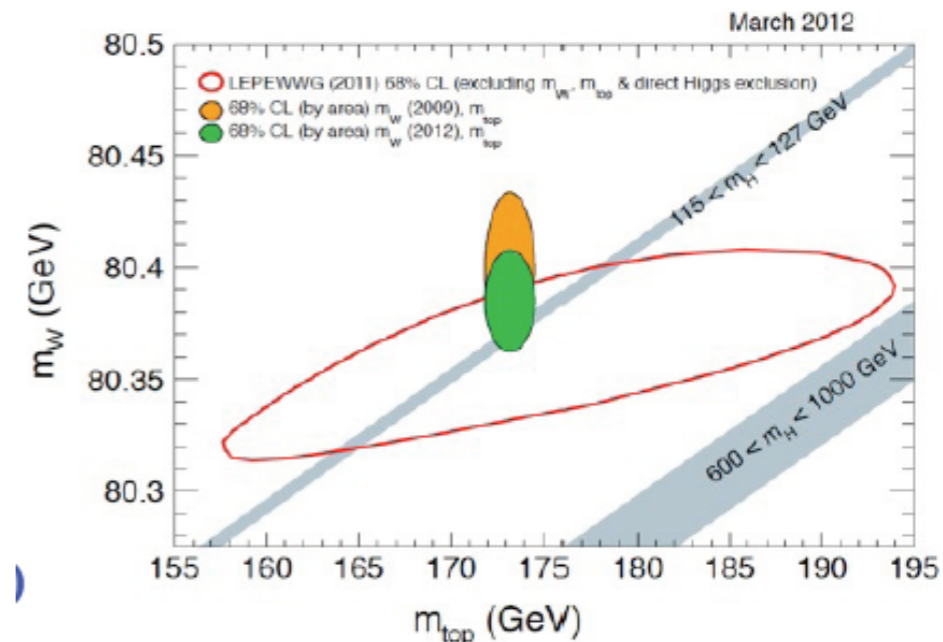
- A Higgs Boson - Observed in 2012 by Atlas and CMS experiments at the LHC
  - Completes the spectrum of the SM (Except for the origin of neutrino masses)
  - Spin and Parity consistent with  $0^+$  ( $2^+$  and  $0^-$  ruled out  $> 3\sigma$ )
  - Couplings consistent with SM expectations (Within present errors)



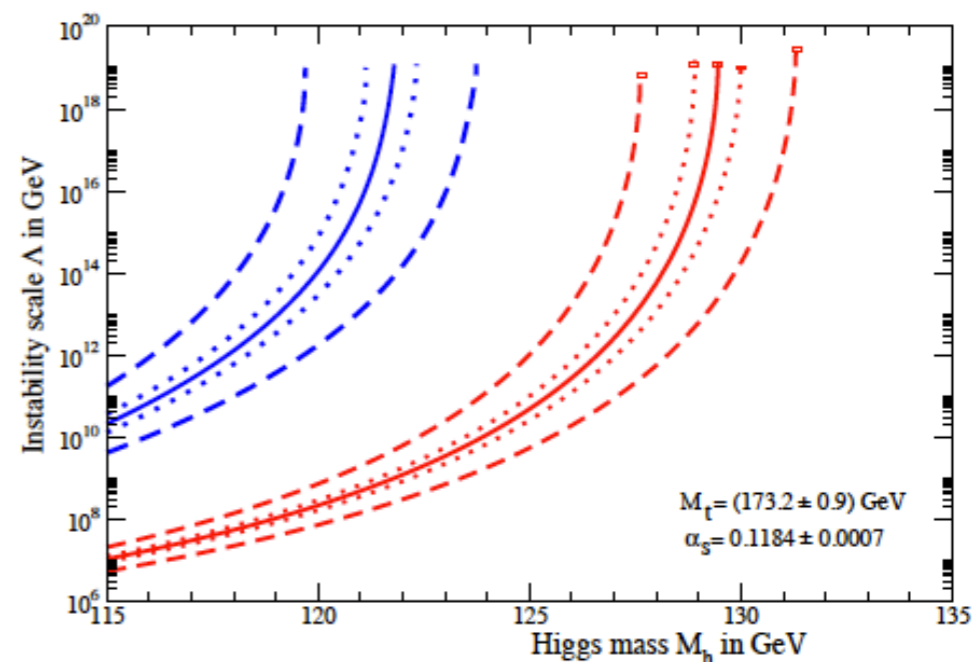
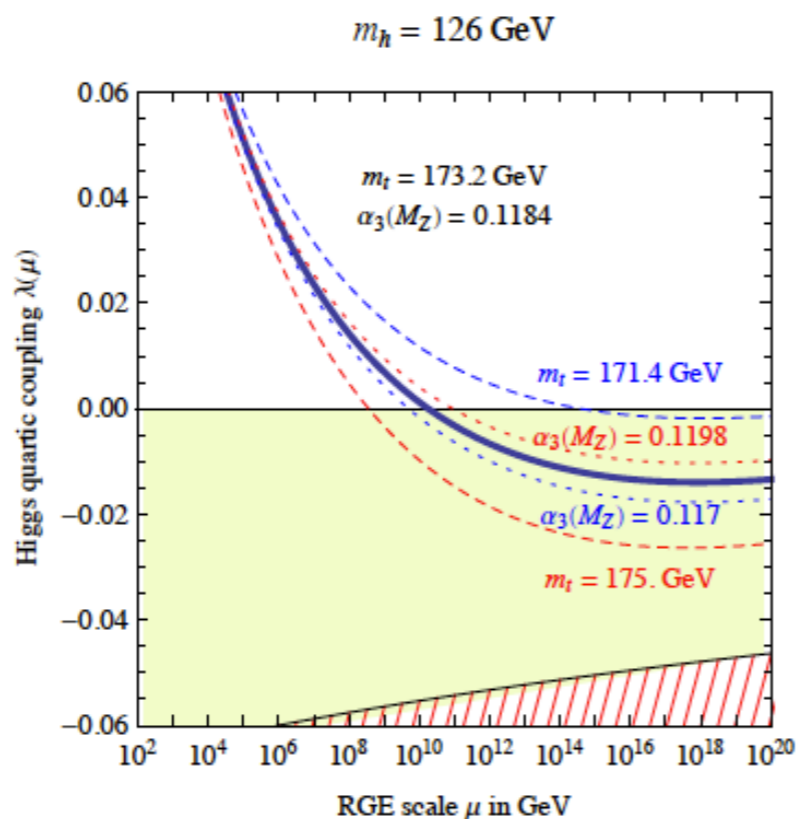
- Higgs coupling proportional to mass



- Indirect measurements are all consistent with a 125.5 GeV Higgs
- For a 125.5 GeV Higgs the SM is consistent to the Planck scale; but the vacuum is only metastable above  $10^{10}$  GeV.



Jean Elias-Miro et. al.  
[arXiv:1112.3022]



- Theorists are intrigued by this edge of stability. ★

- The SM Higgs:
  - All properties are determined for given mass.
  - Any deviations signal new physics.
  - SM theoretical uncertainties can be greatly reduced:

Lepage, Mackenzie, Peskin  
[arXiv:1404.0319]

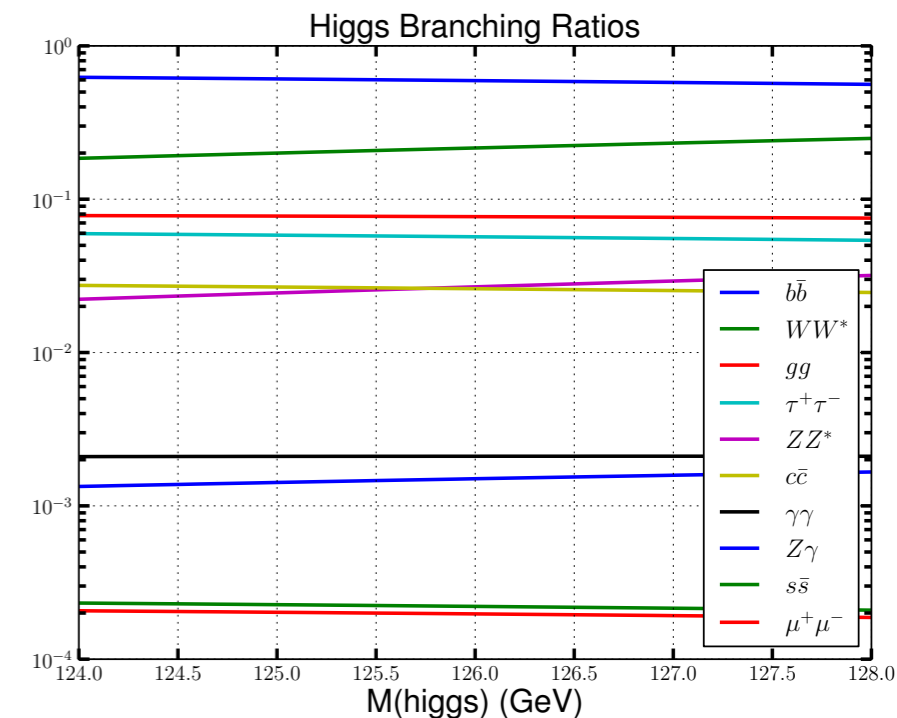
PT -> 4th order QCD

LS ->  $\alpha=0.03\text{fm}$

LS<sup>2</sup> ->  $\alpha=0.023\text{fm}$

ST ->  $\times 100$

	$\delta m_b(10)$	$\delta \alpha_s(m_Z)$	$\delta m_c(3)$	$\delta_b$	$\delta_c$	$\delta_g$
current errors [10]	0.70	0.63	0.61	0.77	0.89	0.78
+ PT	0.69	0.40	0.34	0.74	0.57	0.49
+ LS	0.30	0.53	0.53	0.38	0.74	0.65
+ LS <sup>2</sup>	0.14	0.35	0.53	0.20	0.65	0.43
+ PT + LS	0.28	0.17	0.21	0.30	0.27	0.21
+ PT + LS <sup>2</sup>	0.12	0.14	0.20	0.13	0.24	0.17
+ PT + LS <sup>2</sup> + ST	0.09	0.08	0.20	0.10	0.22	0.09
ILC goal				0.30	0.70	0.60



- Theoretical questions:
  - Couplings and width SM?
  - Scalar self-coupling SM?
  - Any non SM or invisible decay modes?
- The Higgs boson will be studied great detail at present and potential future colliders: LHC-14, LHC-HL, ILC, TLEP
- Muon Collider Higgs Factory (Mass and direct width measurements)

- The strong case for a TeV scale hadron collider rested on two arguments:
  1. Unitarity required that a mechanism for EWSB was manifest at or below the TeV scale.
  2. The SM is unnatural ('t Hooft conditions).
    - Concept of naturalness.
      - K. Wilson, G. 't Hooft
      - A theory  $[L(\mu)]$  is natural at scale  $\mu \Leftrightarrow$  for any small dimensionless parameter  $\lambda$  (e.g.  $m/\mu$ ) in  $L(\mu)$ , the limit  $\lambda \rightarrow 0$  enhances the symmetries of  $L(\mu)$
    - The SM Higgs boson is unnatural. ( $m_H^2/\mu^2$ )
      - Maybe no large gap in scales (Extra Dimensions)
    - Two potential solutions:
      - scalars not elementary  $\rightarrow$  New strong dynamics (TC, walking TC, little Higgs, top color, ...)
      - fermion masses are natural  $\rightarrow$  Symmetry coupling fermions and bosons (SUSY)
- Quest for the "natural" theory to replace the SM has preoccupied theorists since the early 80's. (Is there a third way?)

G. 't Hooft in Proceedings of Recent Developments in Gauge Theories, Cargese, France (1980)

NATURALNESS, CHIRAL SYMMETRY, AND SPONTANEOUS CHIRAL SYMMETRY BREAKING

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ABSTRACT

A properly called "naturalness" is imposed on gauge theories. It is an order-of-magnitude restriction that must hold at all energy scales  $\mu$ . To construct models with complete naturalness for elementary particles one needs more types of confining gauge theories besides quantum chromodynamics. We propose a search

- The observed Higgs Boson resolves the unitarity crisis:  $m_H = 125.5 \text{ GeV}$   
(New physics must appear at or below the TeV scale)
- The second argument remains strong, but is now less rigorously tied to the TeV scale and
  - No evidence for new physics beyond the Standard Model (BSM) to date:
    - BSM (SUSY, Strong Dynamics, Extra Dimensions, New fermions or gauge bosons,...)

## - ATLAS limits

### ATLAS Exotics Searches\* - 95% CL Exclusion

Status: April 2014

ATLAS Preliminary  
 $\int \mathcal{L} dt = (1.0 - 20.3) \text{ fb}^{-1}$   $\sqrt{s} = 7, 8 \text{ TeV}$

Model	$\ell, \gamma$	Jets	$E_T^{\text{miss}}$	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Mass limit	Reference
Extra dimensions	ADD $G_{KK} + g/q$	-	1-2 j	Yes	4.7	$M_0$ 4.37 TeV
	ADD non-resonant $\ell\ell\gamma\gamma$	$2\gamma$ or $2e, \mu$	-	-	4.7	$M_s$ 4.18 TeV
	ADD QBH $\rightarrow \ell q$	$1 e, \mu$	1 j	-	20.3	$M_{\text{th}}$ 5.2 TeV
	ADD BH high $N_{\text{th}}$	$2\mu$ (SS)	-	-	20.3	$M_{\text{th}}$ 5.7 TeV
	ADD BH high $\Sigma p_T$	$\geq 1 e, \mu$	$\geq 2 j$	-	20.3	$M_{\text{th}}$ 6.2 TeV
	RS1 $G_{KK} \rightarrow \ell\ell$	$2 e, \mu$	-	-	20.3	$G_{KK} \text{ mass}$ 2.47 TeV
	RS1 $G_{KK} \rightarrow ZZ \rightarrow \ell\ell qq/\ell\ell\ell\ell$	$2$ or $4 e, \mu$	$2 j$ or -	-	1.0	$G_{KK} \text{ mass}$ 845 GeV
	RS1 $G_{KK} \rightarrow WW \rightarrow \ell\nu\ell\nu$	$2 e, \mu$	-	Yes	4.7	$G_{KK} \text{ mass}$ 1.23 TeV
	Bulk RS $G_{KK} \rightarrow HH \rightarrow b\bar{b}b\bar{b}$	-	4 b	-	19.5	$G_{KK} \text{ mass}$ 590-710 GeV
	Bulk RS $G_{KK} \rightarrow t\bar{t}$	$1 e, \mu$	$\geq 1 b, \geq 1 J/2 j$	Yes	14.3	$G_{KK} \text{ mass}$ 0.5-2.0 TeV
$S^1/Z_2$ ED	$2 e, \mu$	-	-	5.0	$M_{KK} \approx R^{-1}$ 4.71 TeV	
UED	$2\gamma$	-	Yes	4.8	Compact scale $R^{-1}$ 1.41 TeV	
Gauge bosons	SSM $Z' \rightarrow \ell\ell$	$2 e, \mu$	-	-	20.3	$Z' \text{ mass}$ 2.86 TeV
	SSM $Z' \rightarrow \tau\tau$	$2\tau$	-	-	19.5	$Z' \text{ mass}$ 1.9 TeV
	SSM $W' \rightarrow \ell\nu$	$1 e, \mu$	-	Yes	20.3	$W' \text{ mass}$ 3.28 TeV
	EGM $W' \rightarrow WZ \rightarrow \ell\nu \ell' \ell'$	$3 e, \mu$	-	Yes	20.3	$W' \text{ mass}$ 1.52 TeV
LRSM $W_R \rightarrow t\bar{b}$	$1 e, \mu$	$2 b, 0-1 j$	Yes	14.3	$W' \text{ mass}$ 1.84 TeV	
CI	CI $qqqq$	-	$2 j$	-	4.8	$\Lambda$ 7.6 TeV
	CI $qq\ell\ell$	$2 e, \mu$	-	-	5.0	$\Lambda$ 13.9 TeV
	CI $uutt$	$2 e, \mu$ (SS) $\geq 1 b, \geq 1 j$	Yes	14.3	$\Lambda$ 3.3 TeV	
DM	EFT D5 operator	-	1-2 j	Yes	10.5	$M_*$ 731 GeV
	EFT D9 operator	-	$1 J, \leq 1 j$	Yes	20.3	$M_*$ 2.4 TeV
LO	Scalar LQ 1 <sup>st</sup> gen	$2 e$	$\geq 2 j$	-	1.0	LQ mass 660 GeV
	Scalar LQ 2 <sup>nd</sup> gen	$2\mu$	$\geq 2 j$	-	1.0	LQ mass 685 GeV
	Scalar LQ 3 <sup>rd</sup> gen	$1 e, \mu, 1\tau$	$1 b, 1 j$	-	4.7	LQ mass 534 GeV
Heavy quarks	Vector-like quark $TT \rightarrow Ht + X$	$1 e, \mu$	$\geq 2 b, \geq 4 j$	Yes	14.3	T mass 790 GeV
	Vector-like quark $TT \rightarrow Wb + X$	$1 e, \mu$	$\geq 1 b, \geq 3 j$	Yes	14.3	T mass 670 GeV
	Vector-like quark $BB \rightarrow Zb + X$	$2 e, \mu$	$\geq 2 b$	-	14.3	B mass 725 GeV
	Vector-like quark $BB \rightarrow Wt + X$	$2 e, \mu$ (SS) $\geq 1 b, \geq 1 j$	Yes	14.3	B mass 720 GeV	
Excited fermions	Excited quark $q^* \rightarrow q\gamma$	$1\gamma$	1 j	-	20.3	$q^* \text{ mass}$ 3.5 TeV
	Excited quark $q^* \rightarrow qg$	-	$2 j$	-	13.0	$q^* \text{ mass}$ 3.84 TeV
	Excited quark $b^* \rightarrow Wt$	$1$ or $2 e, \mu, 1 b, 2 j$ or $1 j$	Yes	4.7	$b^* \text{ mass}$ 870 GeV	
	Excited lepton $\ell^* \rightarrow \ell\gamma$	$2 e, \mu, 1\gamma$	-	-	13.0	$\ell^* \text{ mass}$ 2.2 TeV
Other	LRSM Majorana $\nu$	$2 e, \mu$	$2 j$	-	2.1	$N^0 \text{ mass}$ 1.5 TeV
	Type III Seesaw	$2 e, \mu$	-	-	5.8	$N^0 \text{ mass}$ 245 GeV
	Higgs triplet $H^{\pm\pm} \rightarrow \ell\ell$	$2 e, \mu$ (SS)	-	-	4.7	$H^{\pm\pm} \text{ mass}$ 409 GeV
	Multi-charged particle	-	-	-	4.4	Multi-charged particle mass 490 GeV
Magnetic monopoles	-	-	-	2.0	monopole mass 862 GeV	

$\sqrt{s} = 7 \text{ TeV}$   $\sqrt{s} = 8 \text{ TeV}$

Mass scale [TeV]  $10^{-1}$  1 10

### ATLAS SUSY Searches\* - 95% CL Lower Limits

Status: Moriond 2014

ATLAS Preliminary  
 $\int \mathcal{L} dt = (4.6 - 22.9) \text{ fb}^{-1}$   $\sqrt{s} = 7, 8 \text{ TeV}$

Model	$e, \mu, \tau, \gamma$	Jets	$E_T^{\text{miss}}$	$\int \mathcal{L} dt [\text{fb}^{-1}]$	Mass limit	Reference	
Inclusive Searches	MSUGRA/CMSSM	0	2-6 jets	Yes	20.3	$\tilde{g}, \tilde{g}$ 1.7 TeV	
	MSUGRA/CMSSM	$1 e, \mu$	3-8 jets	Yes	20.3	$\tilde{g}$ 1.2 TeV	
	MSUGRA/CMSSM	0	7-10 jets	Yes	20.3	$\tilde{g}$ 1.1 TeV	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\ell\ell$	0	2-6 jets	Yes	20.3	$\tilde{g}$ 740 GeV	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\ell\ell$	0	2-6 jets	Yes	20.3	$\tilde{g}$ 1.3 TeV	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\ell\ell$	$1 e, \mu$	3-6 jets	Yes	20.3	$\tilde{g}$ 1.18 TeV	
	$\tilde{g}, \tilde{g} \rightarrow q\bar{q}\ell\ell$	$2 e, \mu$	0-3 jets	-	20.3	$\tilde{g}$ 1.12 TeV	
	GMSB ( $\tilde{t}$ NLSP)	$2 e, \mu$	2-4 jets	Yes	4.7	$\tilde{g}$ 1.24 TeV	
	GMSB ( $\tilde{t}$ NLSP)	$1-2\tau$	0-2 jets	Yes	20.7	$\tilde{g}$ 1.4 TeV	
	GGM (bino NLSP)	$2\gamma$	-	Yes	20.3	$\tilde{g}$ 1.28 TeV	
3 <sup>rd</sup> gen. med.	$\tilde{g} \rightarrow b\bar{b}\ell\ell$	0	3 b	Yes	20.1	$\tilde{g}$ 1.2 TeV	
	$\tilde{g} \rightarrow t\bar{t}\ell\ell$	0	7-10 jets	Yes	20.3	$\tilde{g}$ 1.1 TeV	
	$\tilde{g} \rightarrow b\bar{b}\ell\ell$	$0-1 e, \mu$	3 b	Yes	20.1	$\tilde{g}$ 1.34 TeV	
	$\tilde{g} \rightarrow b\bar{b}\ell\ell$	$0-1 e, \mu$	3 b	Yes	20.1	$\tilde{g}$ 1.3 TeV	
	3 <sup>rd</sup> gen. squarks direct production	$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow b\bar{b}\ell\ell$	0	2 b	Yes	20.1	$\tilde{b}_1$ 100-620 GeV
		$\tilde{b}_1\tilde{b}_1, \tilde{b}_1 \rightarrow t\bar{t}\ell\ell$	$2 e, \mu$ (SS)	0-3 b	Yes	20.7	$\tilde{b}_1$ 275-430 GeV
		$\tilde{t}_1\tilde{t}_1$ (light), $\tilde{t}_1 \rightarrow Wb\ell\ell$	$1-2 e, \mu$	1-2 b	Yes	4.7	$\tilde{t}_1$ 110-167 GeV
		$\tilde{t}_1\tilde{t}_1$ (light), $\tilde{t}_1 \rightarrow Wb\ell\ell$	$2 e, \mu$	0-2 jets	Yes	20.3	$\tilde{t}_1$ 130-210 GeV
		$\tilde{t}_1\tilde{t}_1$ (medium), $\tilde{t}_1 \rightarrow b\ell\ell$	$2 e, \mu$	2 jets	Yes	20.3	$\tilde{t}_1$ 215-530 GeV
		$\tilde{t}_1\tilde{t}_1$ (medium), $\tilde{t}_1 \rightarrow b\ell\ell$	0	2 b	Yes	20.1	$\tilde{t}_1$ 150-580 GeV
$\tilde{t}_1\tilde{t}_1$ (heavy), $\tilde{t}_1 \rightarrow t\ell\ell$		$1 e, \mu$	1 b	Yes	20.7	$\tilde{t}_1$ 200-610 GeV	
$\tilde{t}_1\tilde{t}_1$ (heavy), $\tilde{t}_1 \rightarrow t\ell\ell$		0	2 b	Yes	20.5	$\tilde{t}_1$ 320-660 GeV	
$\tilde{t}_1\tilde{t}_1$ (natural GMSB)		0	mono-jet/c-tag	Yes	20.3	$\tilde{t}_1$ 90-200 GeV	
$\tilde{t}_1\tilde{t}_1$ (natural GMSB)		$2 e, \mu$ (Z)	1 b	Yes	20.3	$\tilde{t}_1$ 150-580 GeV	
EW direct	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$2 e, \mu$	0	Yes	20.3	$\tilde{t}_1$ 90-325 GeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$2 e, \mu$	0	Yes	20.3	$\tilde{t}_1$ 140-465 GeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$1-2 e, \mu$	1-2 b	Yes	4.7	$\tilde{t}_1$ 180-330 GeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$2\tau$	-	Yes	20.7	$\tilde{t}_1$ 700 GeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$3 e, \mu$	0	Yes	20.3	$\tilde{t}_1$ 420 GeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$2-3 e, \mu$	0	Yes	20.3	$\tilde{t}_1$ 285 GeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$1 e, \mu$	2 b	Yes	20.3	$\tilde{t}_1$ 270 GeV	
	Stable, stopped $\tilde{g}$ R-hadron	0	1-5 jets	Yes	22.9	$\tilde{g}$ 832 GeV	
	GMSB, stable $\tilde{t}_1, \tilde{t}_1 \rightarrow t\ell\ell$	$1 e, \mu$	-	-	15.9	$\tilde{t}_1$ 475 GeV	
	GMSB, $\tilde{t}_1 \rightarrow \gamma\ell\ell$ , long-lived $\tilde{t}_1$	$2\gamma$	-	Yes	4.7	$\tilde{t}_1$ 230 GeV	
RPV	LFV $pp \rightarrow \nu\tau + X, \nu\tau \rightarrow e + \mu$	$2 e, \mu$	-	-	4.6	$\tilde{g}$ 1.61 TeV	
	LFV $pp \rightarrow \nu\tau + X, \nu\tau \rightarrow e + \mu + \tau$	$1 e, \mu + \tau$	-	-	4.6	$\tilde{g}$ 1.1 TeV	
	Bilinear RPV CMSSM	$1 e, \mu$	7 jets	Yes	4.7	$\tilde{g}$ 1.2 TeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\ell\ell$	$4 e, \mu$	-	Yes	20.7	$\tilde{t}_1$ 760 GeV	
	$\tilde{t}_1\tilde{t}_1, \tilde{t}_1 \rightarrow W\ell\ell$	$3 e, \mu + \tau$	-	Yes	20.7	$\tilde{t}_1$ 350 GeV	
	$\tilde{g} \rightarrow qq\ell\ell$	0	6-7 jets	-	20.3	$\tilde{g}$ 916 GeV	
	$\tilde{g} \rightarrow t\ell\ell$	$2 e, \mu$ (SS)	0-3 b	Yes	20.7	$\tilde{g}$ 880 GeV	
	Scalar gluon pair, sgluon $\rightarrow \tilde{g}\tilde{g}$	0	4 jets	-	4.6	sgluon 100-287 GeV	
	Scalar gluon pair, sgluon $\rightarrow t\bar{t}$	$2 e, \mu$ (SS)	2 b	Yes	14.3	sgluon 350-800 GeV	
	WIMP interaction (D5, Dirac $\chi$ )	0	mono-jet	Yes	10.5	$M^0$ scale 704 GeV	

$\sqrt{s} = 7 \text{ TeV}$  full data  $\sqrt{s} = 8 \text{ TeV}$  partial data  $\sqrt{s} = 8 \text{ TeV}$  full data

Mass scale [TeV]  $10^{-1}$  1 10

\*Only a selection of the available mass limits on new states or phenomena is shown. All limits quoted are observed minus 1 $\sigma$  theoretical signal cross section uncertainty.





- There must be new physics:

- The Standard Model is incomplete:

- dark matter; neutrino masses and mixing -> new fields or interactions;
- baryon asymmetry in the universe -> more CP violation
- gauge unification -> new interactions;
- gravity: strings and extra dimensions

- Experimental hints of new physics:  $(g-2)_\mu$ ,

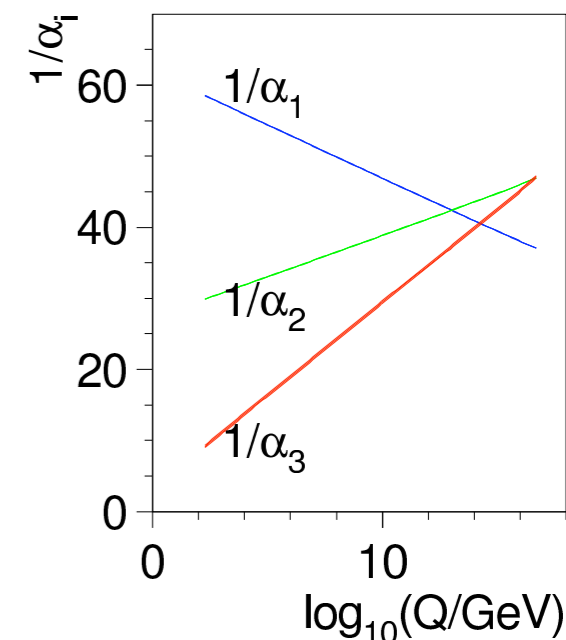
- Scalar sector problematic:

$$\mu^2(\Phi^\dagger\Phi) + \lambda (\Phi^\dagger\Phi)^2 + \Gamma_{ij} \psi_{iL}^\dagger \psi_{jR} \Phi + h.c.$$

$m_H^2/M_{\text{planck}}^2 \approx 10^{-34}$   
Hierarchy problem

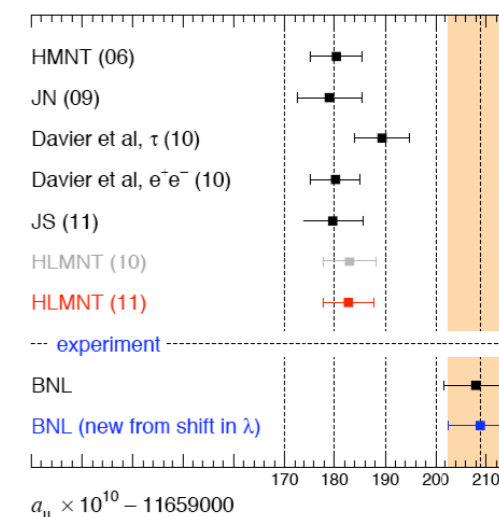
vacuum stability

large range of fermion masses



muon  $(g-2)$

- Davier, Hoecker, Malaescu, Zhang
- Jegerlehner, Szafron
- Hagiwara, Liao, Martin, Nomura, Teubner
- hadronic VP contributions  $(685 \pm 4) \times 10^{-10}$



There remains a persistent discrepancy of 3.3-3.6  $\sigma$

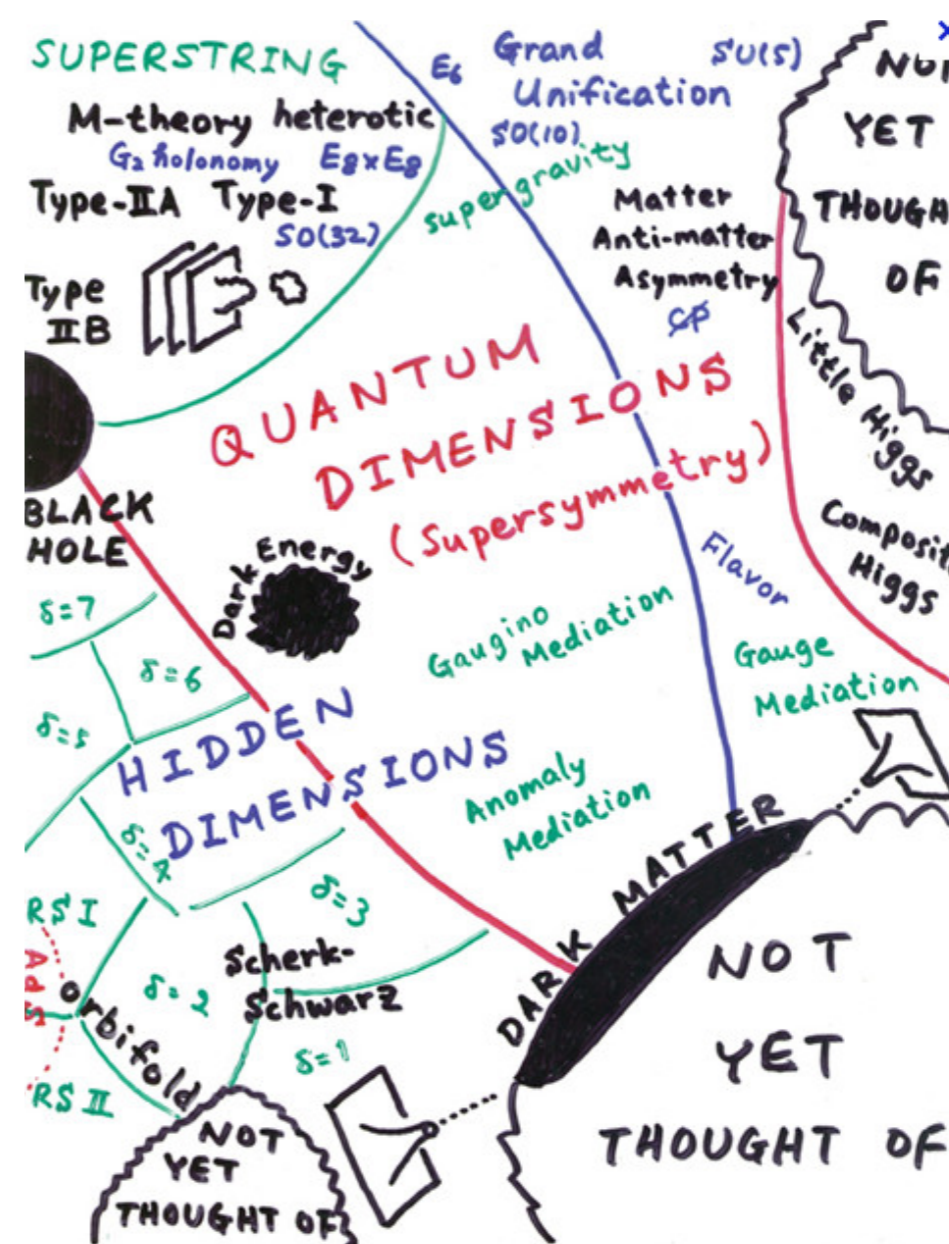
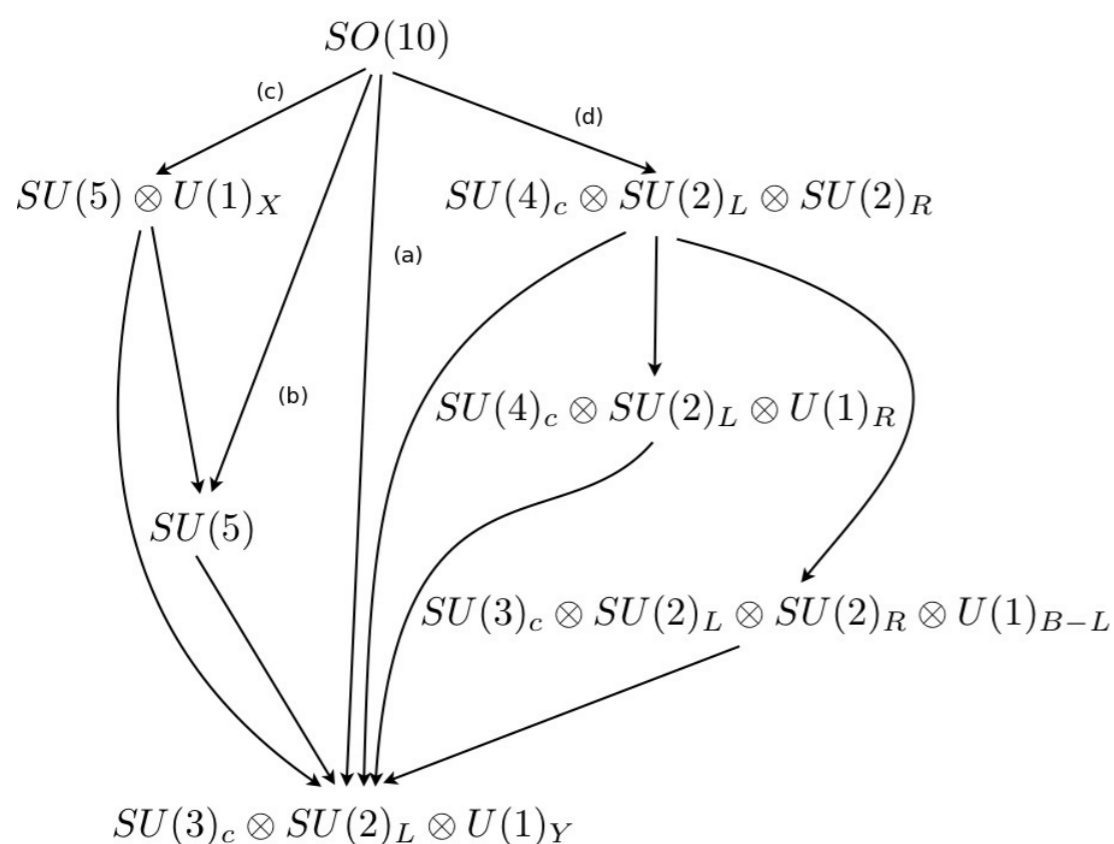
- Scales already probed at the LHC suggest that to study BSM new physics a future energy frontier collider must have  $\sqrt{\hat{s}}$  in the multi-TeV range even for EW processes !!

- But we don't know the scale of new physics. From electroweak scale to Planck scale. Worse case - no nearby scale. Dark matter is axions and right handed neutrinos get mass at high scale. Only an axion would be directly observable. Best case - nearby physics

Desert

or

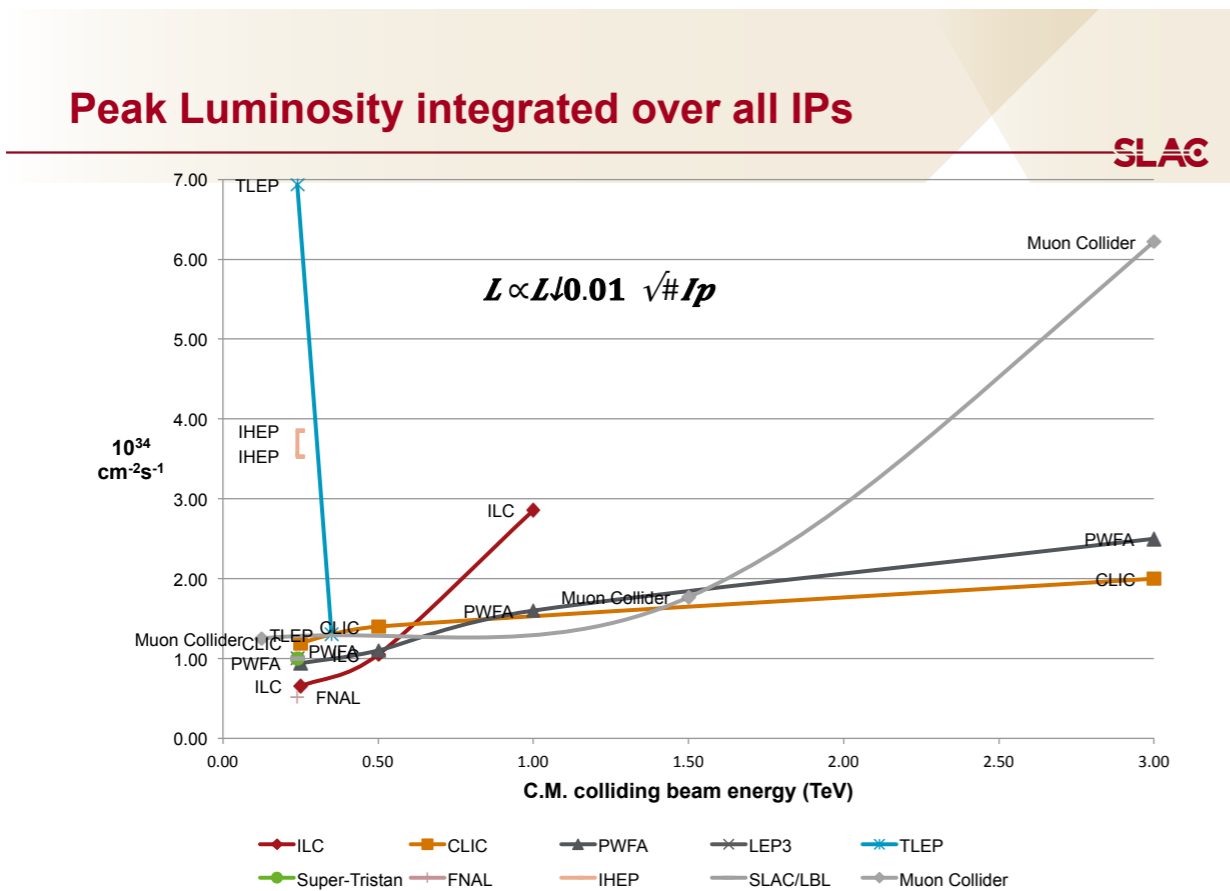
Oasis



- Possible new gauge bosons and fermions.
- Naturalness requires nearby new physics.

H. Murayama

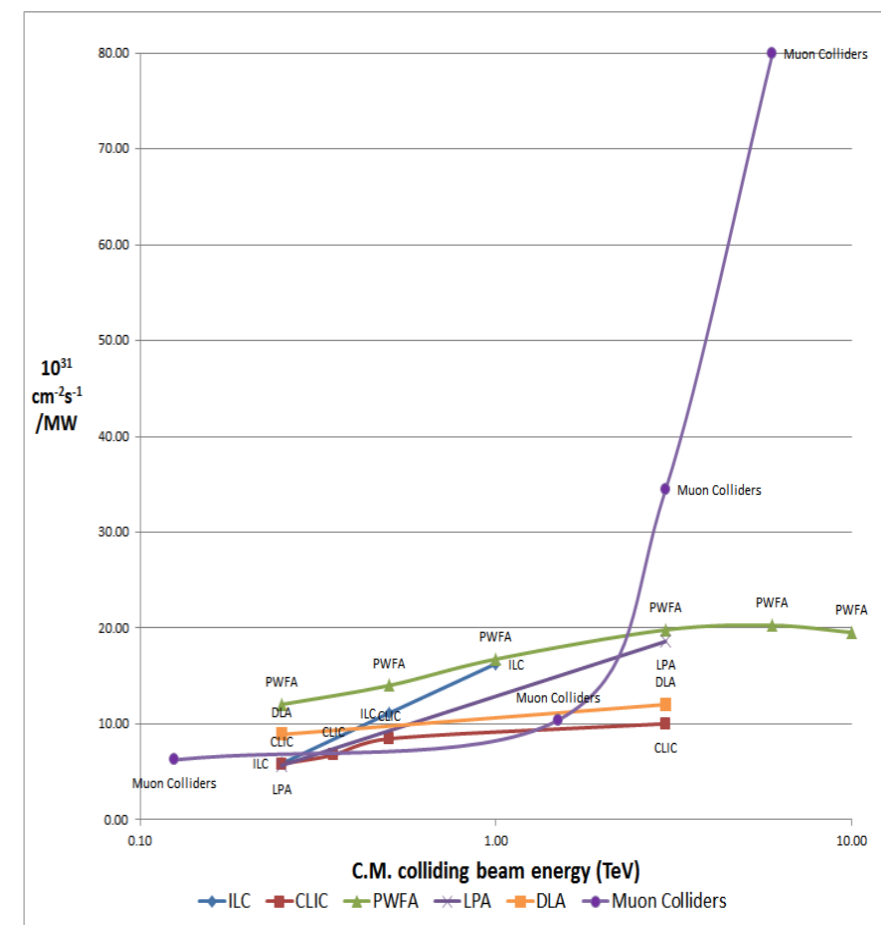
- Hadron colliders - LHC-14, LHC-HL, VLHC  $\leq 100$  TeV pp collider [(CERN), (China), (USA)],...
- Comparison of lepton colliders:



J.P.Delahaye @ UCLA March 21,2013

Review of HIGGS Factory technology options

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J-P. Delahaye, *et al.* [arXiv:1308.0494]

- Increase of luminosity with energy. Needed for new physics.
- Wall power in operation a major concern.
- For  $\sqrt{s}$  above a few TeV only the muon collider remains a potentially viable lepton collider.

## Limitations on energy and luminosity of a muon collider (a theorist's view)

- Production of muons:  $N_\mu = 2 \times 10^{12} (\mu^\pm / \text{beam}) \times 12 (\text{beams}/\text{sec}^{-1}) \rightarrow 7.5 \times 10^{20} (\mu^\pm / \text{year})$

J-P. Delahaye, *et al.* [arXiv:1308.0494]

-  $\int dt \mathcal{L} = 1.32 \text{ ab}^{-1} (E_{\text{cm}}/(3\text{TeV}))^2 (N_\mu/(7.5 \times 10^{20}))^2$

- Neutrino beams far radiation:  $\theta_{\frac{1}{2}} = \frac{mc^2}{E} = 1.057 \frac{10^{-4}}{E_\mu(\text{TeV})}$

Table 1: Radial distance,  $R$ , from the ring center with center-of-mass energy,  $\sqrt{s}$ , and depth,  $d$ , needed to reduce neutrino-induced dose at surface to DOE (100 mrem) and Fermilab (10 mrem) annual off-site limits at  $N_D$  decays/yr.

	$\sqrt{s}$ (TeV)	0.5	1	2	3	4
	$N_D \times 10^{21}$	0.2	0.2	2	2	2
100 mrem	$R$ (km)	0.4	1.1	6.5	12	18
	$d$ (m)	$\leq 1$	$\leq 1$	3.3	11	25
10 mrem	$R$ (km)	1.2	3.2	21	37	57
	$d$ (m)	$\leq 1$	$\leq 1$	34	107	254

N. V. Mokhov and A. VanGinneken

Conf. Proc. C990329, 3074(1999).

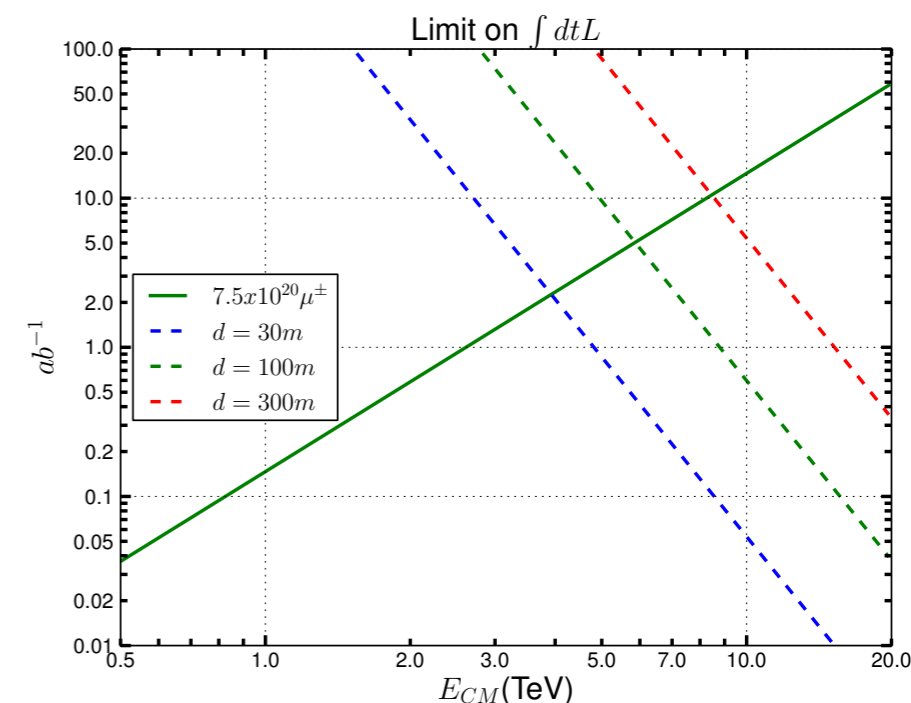
- dose  $\propto N_\mu E_{\text{cm}}^3 R^{-2}$ : If maximum dose = 0.3 mSv/yr = 30 mrem/yr

$$\left( \frac{N_\mu}{7.5 \times 10^{20}} \right) \leq 7.48 \frac{\text{dose}}{(0.3 \text{ mSv})} \left( \frac{3 \text{ TeV}}{E_{\text{cm}}} \right)^3 \frac{d}{(100 \text{ m})}$$

- For  $7.5 \times 10^{20} (\mu^\pm / \text{year})$  and ring depth = 100 m:

- Maximum luminosity  $\sim 4.6 \text{ ab}^{-1}/\text{yr}$  at  $E_{\text{cm}} \sim 6 \text{ TeV}$ .

Muon Collider Parameters								
Parameter	Units	Higgs Factory		Top Threshold Options		Multi-TeV Baselines		Accounts for Site Radiation Mitigation
		Startup Operation	Production Operation	High Resolution	High Luminosity			
CoM Energy	TeV	0.126	0.126	0.35	0.35	1.5	3.0	6.0
Avg. Luminosity	$10^{34} \text{ cm}^{-2} \text{ s}^{-1}$	0.0017	0.008	0.07	0.6	1.25	4.4	12
Beam Energy Spread	%	0.003	0.004	0.01	0.1	0.1	0.1	0.1
Higgs* or Top* Production/ $10^7$ sec		3,500*	13,500*	7,000*	60,000*	37,500*	200,000*	820,000*
Circumference	km	0.3	0.3	0.7	0.7	2.5	4.5	6
No. of IPs		1	1	1	1	2	2	2
Repetition Rate	Hz	30	15	15	15	15	12	6
$\beta^*$	cm	3.3	1.7	1.5	0.5	1 (0.5-2)	0.5 (0.3-3)	2.5
No. muons/bunch	$10^{12}$	2	4	4	3	2	2	2
No. bunches/beam		1	1	1	1	1	1	1
Norm. Trans. Emittance, $\epsilon_{\text{TN}}$	$\pi$ mm-rad	0.4	0.2	0.2	0.05	0.025	0.025	0.025
Norm. Long. Emittance, $\epsilon_{\text{LN}}$	$\pi$ mm-rad	1	1.5	1.5	10	70	70	70
Bunch Length, $\sigma_s$	cm	5.6	6.3	0.9	0.5	1	0.5	2
Proton Driver Power	MW	4 <sup>†</sup>	4	4	4	4	4	1.6



- Variation of total muons per year with the constraints:

- $E_{cm} = 6 \text{ TeV} \rightarrow 7.0 \times 10^{20} (\mu^\pm/\text{year}) \int dt \mathcal{L} = 4.6 \text{ ab}^{-1}/\text{yr}$
- $E_{cm} = 10 \text{ TeV} \rightarrow 1.5 \times 10^{20} (\mu^\pm/\text{year}) \int dt \mathcal{L} = 0.6 \text{ ab}^{-1}/\text{yr}$

- Cross Sections at a Muon Collider:

- For s-channel pair production ( $|\theta| > 10^\circ$ )  
 $R = \sigma/\sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) \sim \text{flat}$

Sweet spot  
~ 6 TeV

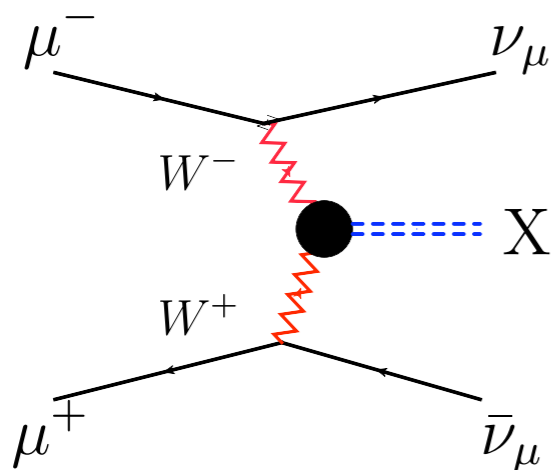
$$\sigma_{\text{QED}}(\mu^+\mu^- \rightarrow e^+e^-) = \frac{4\pi\alpha^2}{3s} = \frac{86.8 \text{ fb}}{s(\text{TeV}^2)}$$

- Resonance production: R large

$$R_{\text{peak}} = (2J + 1)3 \frac{B(\mu^+\mu^-)B(\text{visible})}{\alpha_{\text{EM}}^2}$$

1000 Z'/yr  
@ 11 TeV

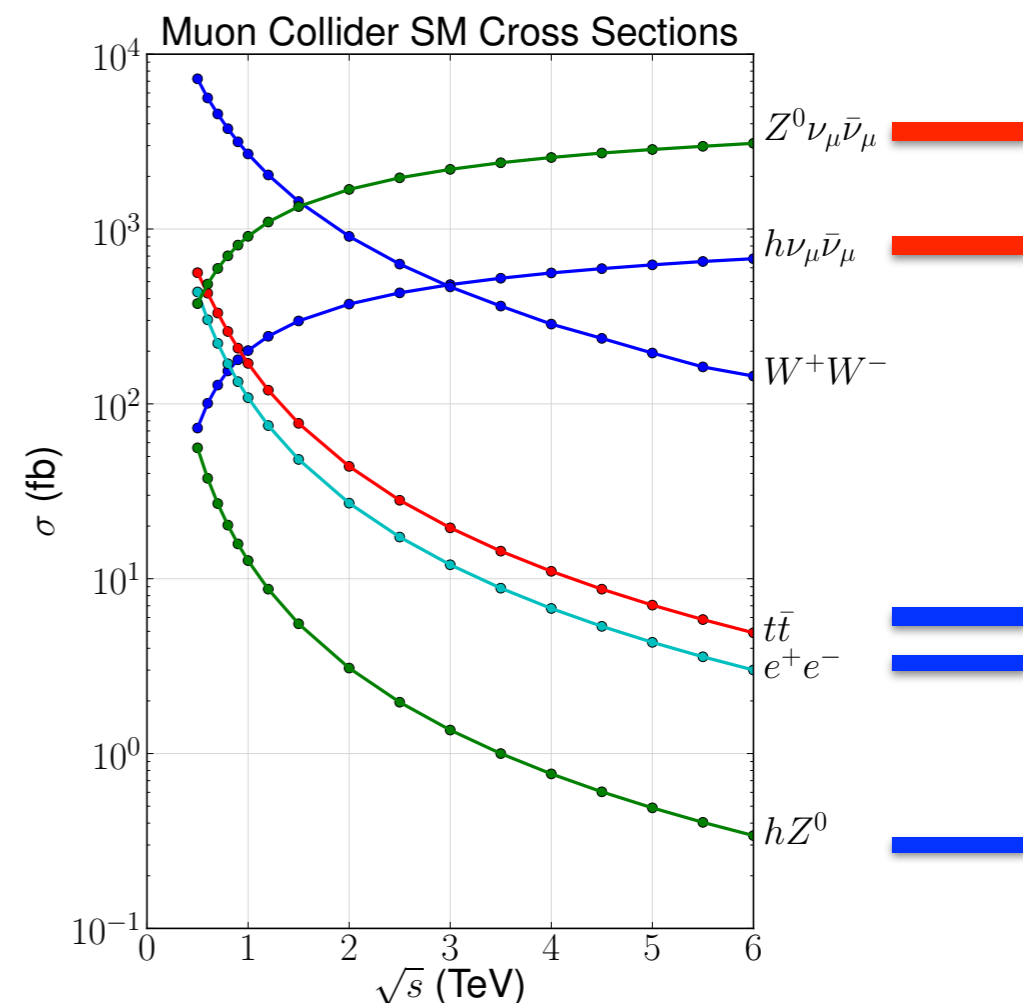
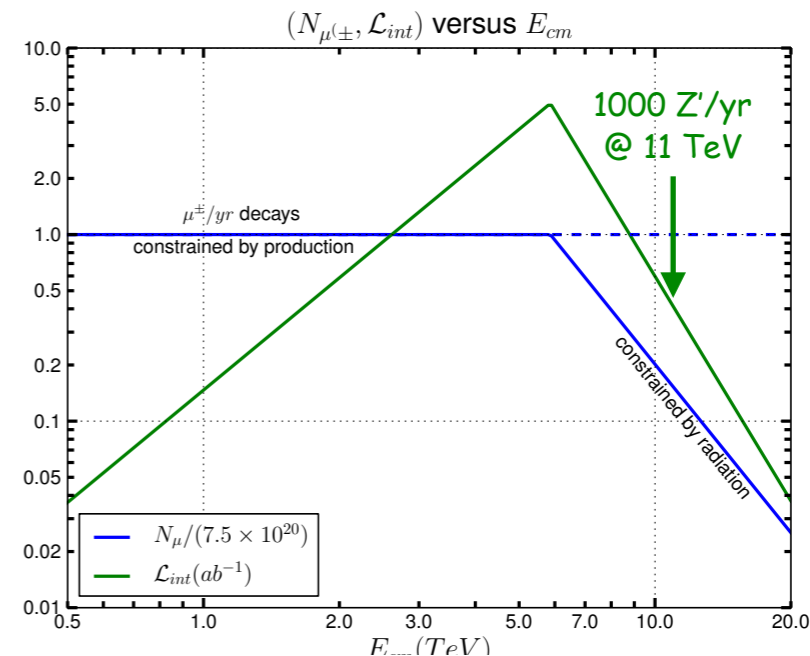
- Fusion Processes: For SM pair production ( $|\theta| > 10^\circ$ )



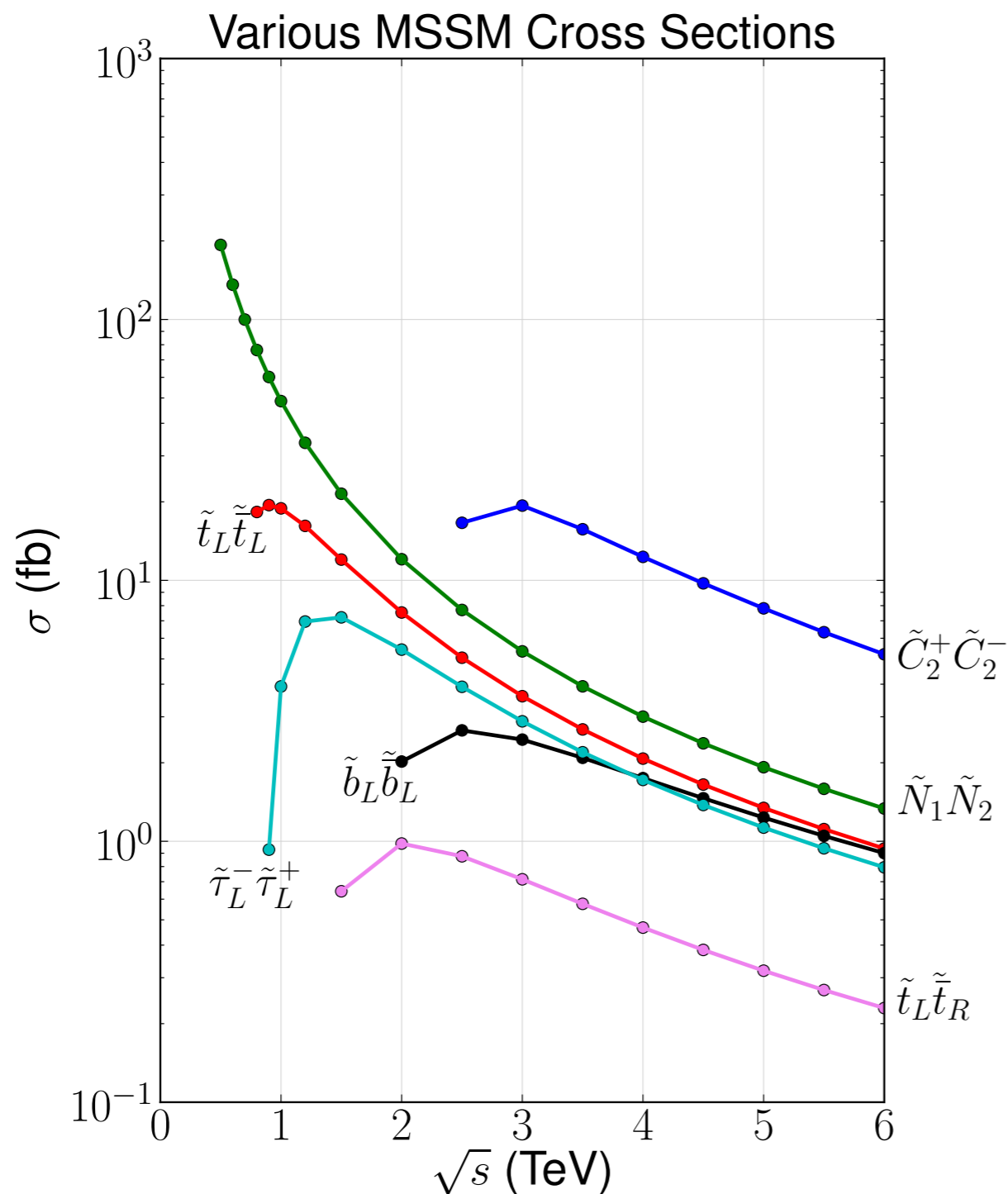
$$\sigma(s) = C \ln\left(\frac{s}{M_X^2}\right) + \dots$$

Cross sections rise with energy

- An EW boson collider !!



— Sample cross sections for Sparticles



At 6 TeV with particle masses below threshold

22,000 chargino  $\chi^{\pm}_2$  pairs/year

5,700 neutralino  $\chi^0_2 \chi^0_1$  pairs/year

3,600 stop pairs/year

- VLHC: up to 100 TeV
  - The physics reach of these colliders is relatively simple to estimate.
  - Since EHLQ (30 yrs ago) there have been great advances in theory and experiment:
    - Background measurements, detector advances, improved PDF's, higher order QCD/EW calculations.
    - Integrated luminosities ( $300 \text{ fb}^{-1}/\text{yr}$ ) - Almost two orders of magnitude greater were assumed for the SSC.

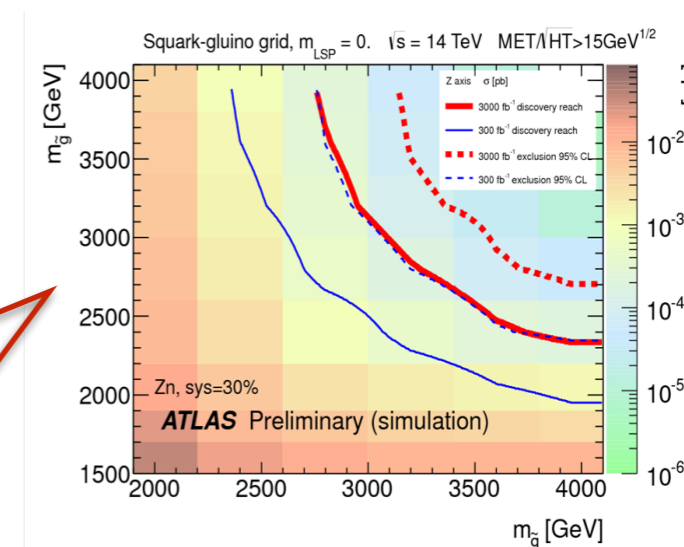
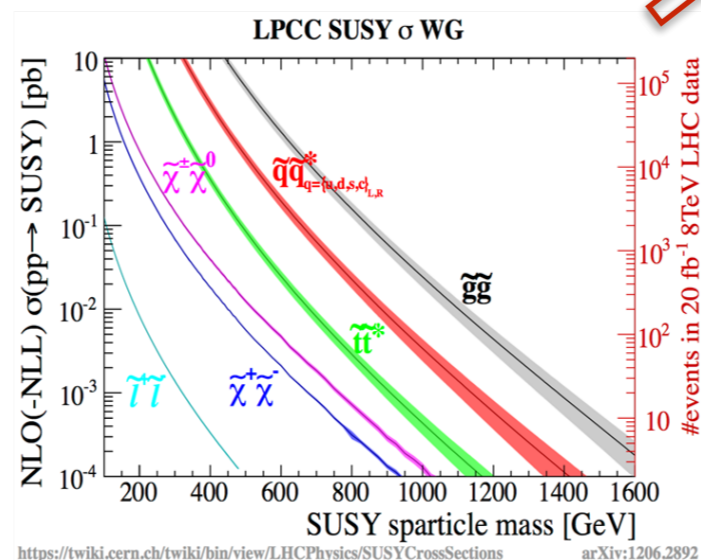
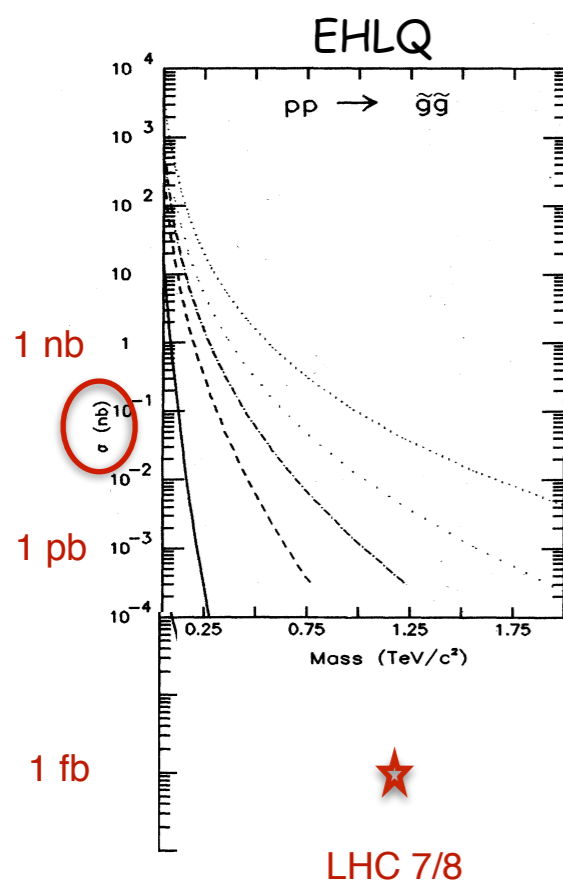
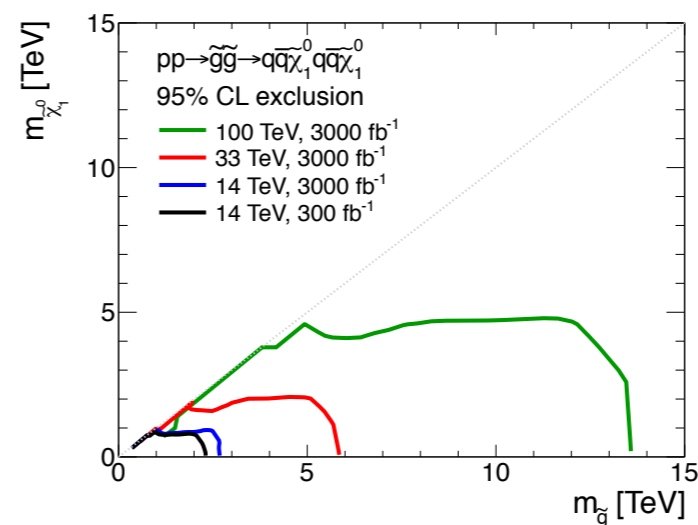


Figure 9: Expected gluino mass limit using 300 /fb and 3000 /fb at 14 TeV in ATLAS [14].

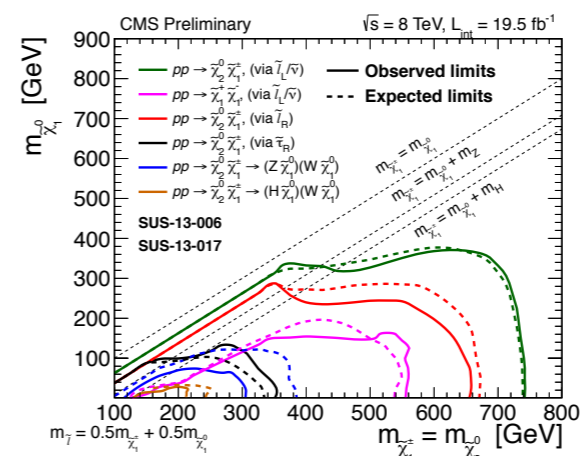
- 5 $\sigma$  discovery/[95% cl limits] at future hadron colliders:
  - squarks and gluinos

Simplified Model	14 TeV 300 fb <sup>-1</sup>	14 TeV 3000 fb <sup>-1</sup>	33 TeV	100 TeV
$\tilde{g} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{\chi}_1^0} \simeq 0$	1.9 TeV [2.3 TeV]	2.2 TeV [2.7 TeV]	5.0 TeV [5.8 TeV]	11 TeV [13.5 TeV]
$\tilde{g} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{g}} \simeq m_{\tilde{\chi}_1^0}$	0.75 TeV [0.9 TeV]	0.9 TeV [1.0 TeV]	1.5 TeV [1.8 TeV]	4.6 TeV [5.5 TeV]
$\tilde{q} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{\chi}_1^0} \simeq 0$	0.80 TeV [1.5 TeV]	0.9 TeV [1.7 TeV]	1.4 TeV [3.4 TeV]	2.4 TeV [8.0 TeV]
$\tilde{q} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{q}} \simeq m_{\tilde{\chi}_1^0}$	0.45 TeV [0.65 TeV]	0.45 TeV [0.70 TeV]	0.80 TeV [1.3 TeV]	3.0 TeV [3.9 TeV]
$\tilde{g} - \tilde{q} - \tilde{\chi}_1^0$ light flavor decays $m_{\tilde{g}} \simeq m_{\tilde{q}}$ and $m_{\tilde{\chi}_1^0} \simeq 0$	2.7 TeV [2.8 TeV]	3.0 TeV [3.2 TeV]	6.6 TeV [6.8 TeV]	15.5 TeV [16 TeV]
$\tilde{g} - \tilde{\chi}_1^0$ heavy flavor decays $m_{\tilde{\chi}_1^0} \simeq 0$	1.6 TeV [1.9 TeV]	2.0 TeV [2.4 TeV]	3.4 TeV [3.9 TeV]	6.3 TeV [8.8 TeV]

[arXiv:1311.6480]



[arXiv:1405.2993]

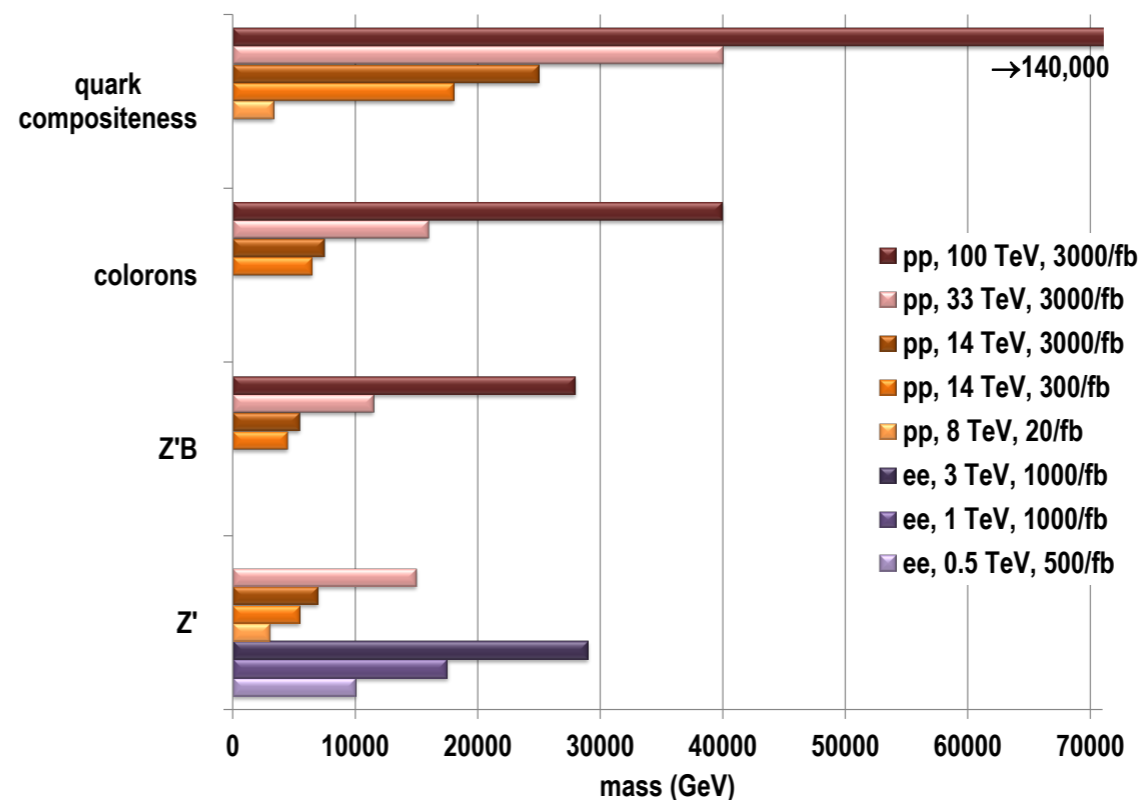
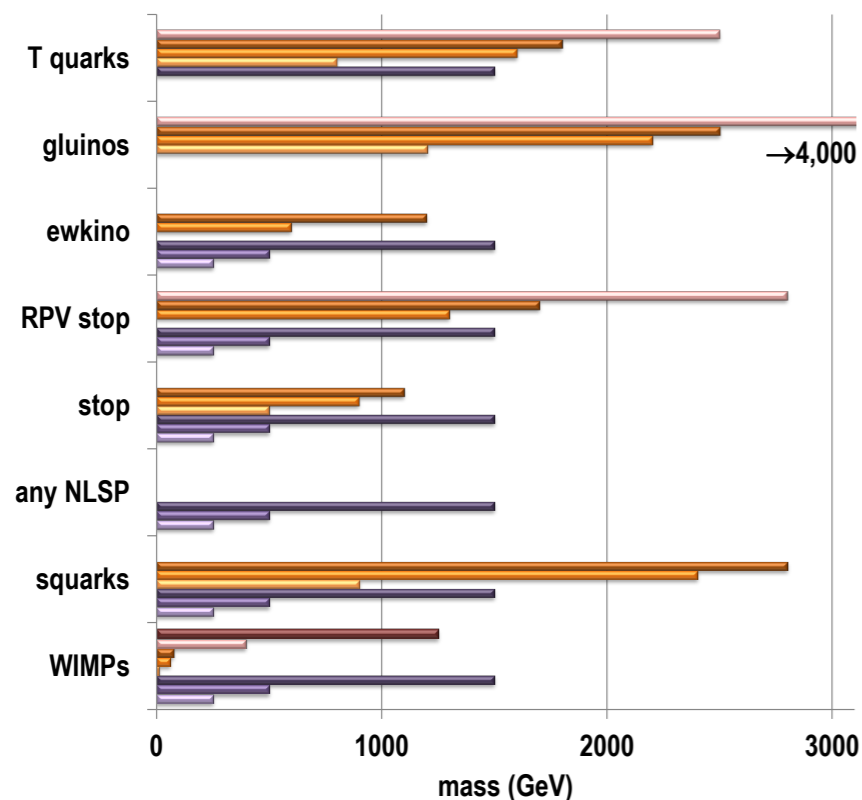


- Limits very dependent on LSP mass and decay modes.



— BSM 95% exclusion limits:

Snowmass Study [arXiv:1311.0299]



— For comparison: a 6 TeV MC will be a factory for:

- T quarks, squarks, stops, sleptons, ewkinos, and NLSP's < 3 TeV
- Compositeness scales > 300 TeV

— For  $m(Z') < 11$  TeV discovered at a hadron collider, the decay modes could be studied in detail at a MC.

— A 3-6 TeV Muon Collider would be complimentary to a 100 TeV hadron collider and would have significant discovery potential of its own.

## P5: Science Questions and Science Drivers

S. Dawson et.al. Snowmass 2013:  
Higgs working group report [arXiv:1310.8361]

### 1. Use the Higgs boson as a new tool for discovery

### 2. ....

- LHC -> HL-LHC (5%-10%) errors on couplings
- Statistics dominate for lepton colliders  
ILC (500), TLEP(350) ultimately 1%

**Table 1-13.** Expected relative precisions on the signal strengths of different Higgs decay final states as well as the 95% CL upper limit on the Higgs branching ratio to the invisible decay from the ZH search estimated by ATLAS and CMS. The ranges are not comparable between ATLAS and CMS. For ATLAS, they correspond to the cases with and without theoretical uncertainties while for CMS they represent two scenarios of systematic uncertainties.

$\int \mathcal{L} dt$ (fb <sup>-1</sup> )	Higgs decay final state							
	$\gamma\gamma$	WW*	ZZ*	$b\bar{b}$	$\tau\tau$	$\mu\mu$	Z $\gamma$	BR <sub>inv</sub>
ATLAS								
300	9 – 14%	8 – 13%	6 – 12%	N/A	16 – 22%	38 – 39%	145 – 147%	< 23 – 32%
3000	4 – 10%	5 – 9%	4 – 10%	N/A	12 – 19%	12 – 15%	54 – 57%	< 8 – 16%
CMS								
300	6 – 12%	6 – 11%	7 – 11%	11 – 14%	8 – 14%	40 – 42%	62 – 62%	< 17 – 28%
3000	4 – 8%	4 – 7%	4 – 7%	5 – 7%	5 – 8%	14 – 20%	20 – 24%	< 6 – 17%

**Table 1-16.** Uncertainties on coupling scaling factors as determined in a completely model-independent fit for different  $e^+e^-$  facilities. Precisions reported in a given column include in the fit all measurements at lower energies at the same facility, and note that the model independence requires the measurement of the recoil HZ process at lower energies. <sup>‡</sup>ILC luminosity upgrade assumes an extended running period on top of the low luminosity program and cannot be directly compared to TLEP and CLIC numbers without accounting for the additional running period. ILC numbers include a 0.5% theory uncertainty. For invisible decays of the Higgs, the number quoted is the 95% confidence upper limit on the branching ratio.

Facility		ILC	ILC(LumiUp)	TLEP (4 IP)	CLIC
$\sqrt{s}$ (GeV)	250	500	1000	240	350
$\int \mathcal{L} dt$ (fb <sup>-1</sup> )	250	+500	+1000	1150+1600+2500 <sup>‡</sup>	10000
$P(e^-, e^+)$	(-0.8, +0.3)	(-0.8, +0.3)	(-0.8, +0.2)	(same)	(0, 0)
$\Gamma_H$	12%	5.0%	4.6%	2.5%	1.9%
$\kappa_\gamma$	18%	8.4%	4.0%	2.4%	1.7%
$\kappa_g$	6.4%	2.3%	1.6%	0.9%	1.1%
$\kappa_W$	4.9%	1.2%	1.2%	0.6%	0.85%
$\kappa_Z$	1.3%	1.0%	1.0%	0.5%	0.16%
$\kappa_\mu$	91%	91%	16%	10%	6.4%
$\kappa_\tau$	5.8%	2.4%	1.8%	1.0%	0.94%
$\kappa_c$	6.8%	2.8%	1.8%	1.1%	1.0%
$\kappa_b$	5.3%	1.7%	1.3%	0.8%	0.88%
$\kappa_t$	–	14%	3.2%	2.0%	–
BR <sub>inv</sub>	0.9%	< 0.9%	< 0.9%	0.4%	0.19%

## - A Role for a future Muon Collider Higgs Factory?

- Only a muon collider can produce the Higgs boson as an s-channel resonance.

-  $\sigma(e^+e^- \rightarrow Zh \rightarrow l^+l^- h) = 19.1 \text{ fb}$  (250 GeV) versus

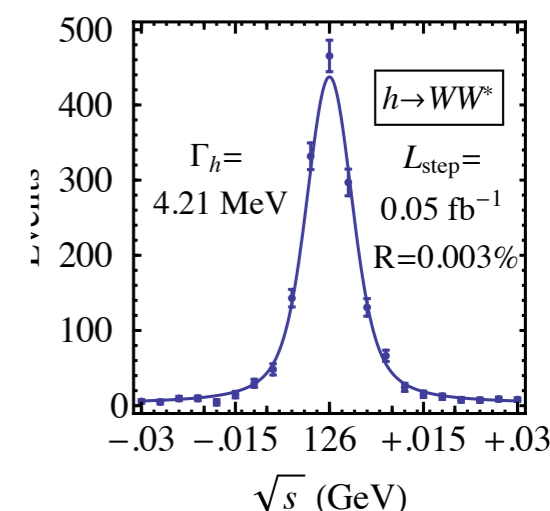
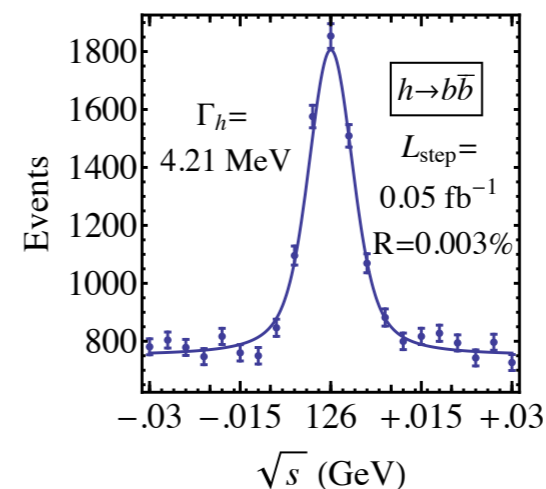
$\sigma(\mu^+\mu^- \rightarrow h) = 26 \text{ pb}$  (for  $\Delta = \Gamma$  and including ISR and a  $15^\circ$  forward cut)

$$\left[\frac{m_\mu}{m_e}\right]^2 = 4.28 \times 10^4$$

$$\sigma_{\text{eff}}(s) = \int d\sqrt{\hat{s}} \frac{dL(\sqrt{s})}{d\sqrt{\hat{s}}} \sigma(\mu^+\mu^- \rightarrow h \rightarrow X)$$

$$\propto \begin{cases} \Gamma_h^2 B / [(s - m_h^2)^2 + \Gamma_h^2 m_h^2] & (\Delta \ll \Gamma_h), \\ B \exp\left[-\frac{(m_h - \sqrt{s})^2}{2\Delta^2}\right] \left(\frac{\Gamma_h}{\Delta}\right) / m_h^2 & (\Delta \gg \Gamma_h). \end{cases}$$

$$\sigma(\mu^+\mu^- \rightarrow h \rightarrow X) = \frac{4\pi\Gamma_h^2 \text{Br}(h \rightarrow \mu^+\mu^-) \text{Br}(h \rightarrow X)}{(s - m_h^2)^2 + \Gamma_h^2 m_h^2}.$$



T. Han and Z. Liu [arXiv:1210.7803]  
also see Zhen Liu's talk on Friday

- Finding the Higgs requires  $\sim 250 \text{ pb}^{-1}$

- Assuming  $\int \mathcal{L} dt = 1 \text{ fb}$   $R = \Delta E/E = 0.003\%$

- Unique results:

1. Higgs mass to 60 keV

2. Direct measurement of Higgs width to 150 keV

3. Measurement  $\delta \kappa_\mu = 1\%$  using the known width and coupling to  $WW^*$

$\Gamma_h = 4.21 \text{ MeV}$	$L_{\text{step}} (\text{fb}^{-1})$	$\delta\Gamma_h (\text{MeV})$	$\delta B$	$\delta m_h (\text{MeV})$
$R = 0.01\%$	0.005	0.73	6.5%	0.25
	<b>0.025</b>	<b>0.35</b>	<b>3.0%</b>	<b>0.12</b>
	0.2	0.17	1.1%	0.06
$R = 0.003\%$	0.01	0.30	4.4%	0.12
	<b>0.05</b>	<b>0.15</b>	<b>2.0%</b>	<b>0.06</b>
	0.2	0.08	1.0%	0.03

## – Higgs Self-Coupling ( $\lambda$ ):

- SM:  $m_H^2 = (8\lambda/g^2) m_W^2 + \text{loop corrs.}$
- LHC; HL-LHC; VLHC: **50%; 20%; 8% (stat only)**
- ILC (500); ILC (1000); CLIC (3000): **83%; 21%; 16%**

Table 1-22. Signal significance for  $pp \rightarrow HH \rightarrow bb\gamma\gamma$  and percentage uncertainty on the Higgs self-coupling at future hadron colliders, from [102].

	HL-LHC	HE-LHC	VLHC
$\sqrt{s}$ (TeV)	14	33	100
$\int \mathcal{L} dt$ ( $\text{fb}^{-1}$ )	3000	3000	3000
$\sigma \cdot \text{BR}(pp \rightarrow HH \rightarrow bb\gamma\gamma)$ (fb)	0.089	0.545	3.73
$S/\sqrt{B}$	2.3	6.2	15.0
$\lambda$ (stat)	50%	20%	8%

- Measurement improves with energy at a lepton collider
- Muon Collider (6 TeV): **8%**

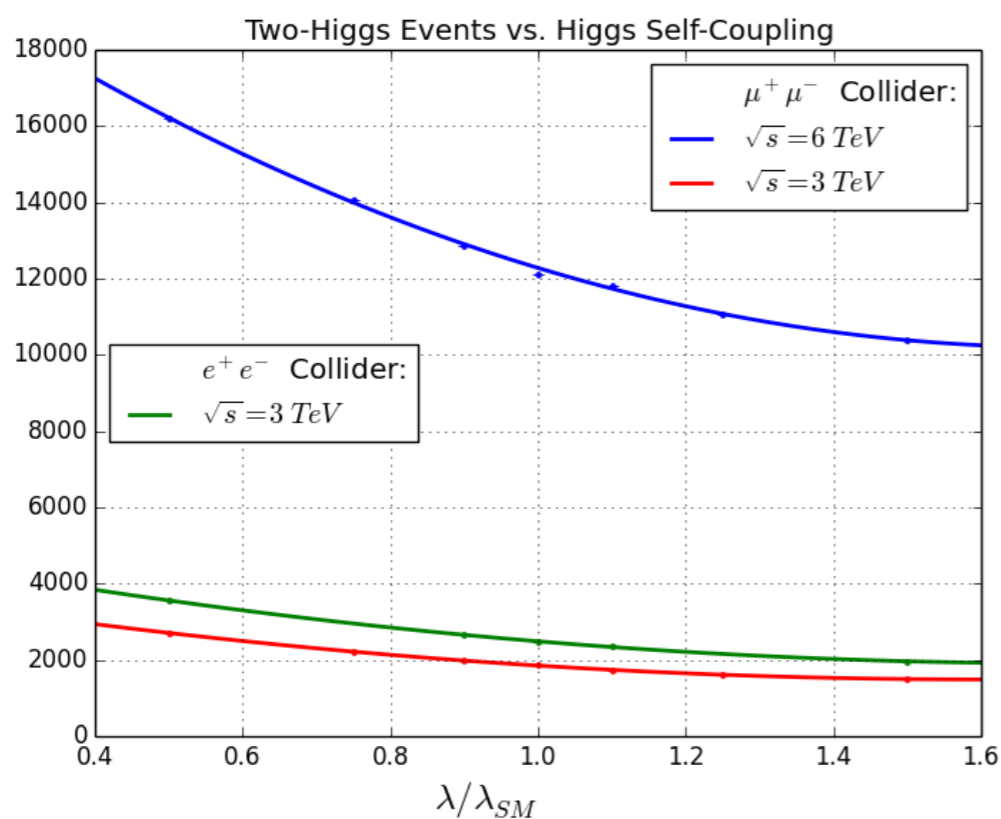
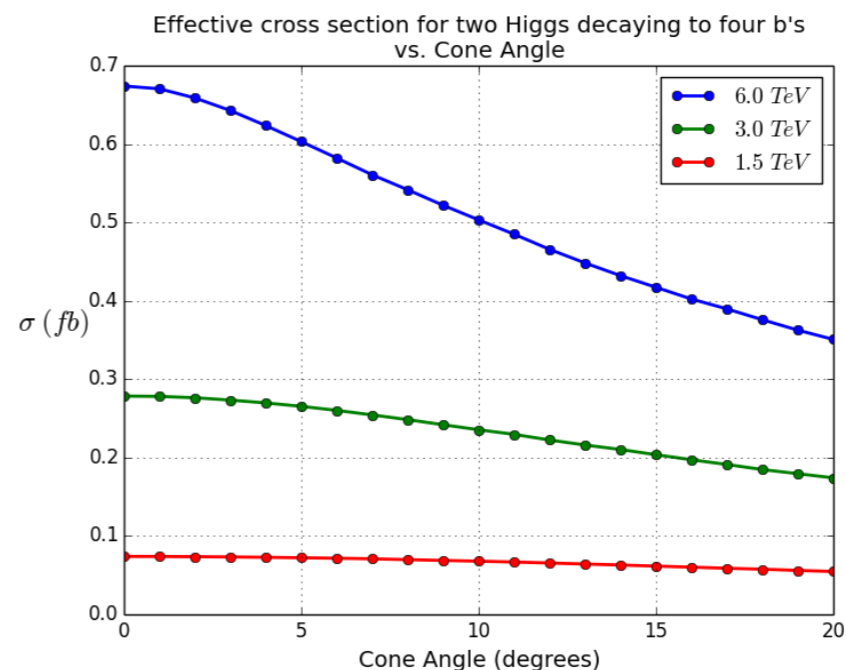


Figure 3: Estimated number of double-Higgs events after five Snowmass years, or  $5 \times 10^7 s$ .

	ILC500	ILC500-up	ILC1000	ILC1000-up	CLIC1400	CLIC3000
$\sqrt{s}$ (GeV)	500	500	500/1000	500/1000	1400	3000
$\int \mathcal{L} dt$ ( $\text{fb}^{-1}$ )	500	1600 <sup>‡</sup>	500+1000	1600+2500 <sup>‡</sup>	1500	+2000
$P(e^-, e^+)$	(-0.8, 0.3)	(-0.8, 0.3)	(-0.8, 0.3/0.2)	(-0.8, 0.3/0.2)	(0, 0)/(-0.8, 0)	(0, 0)/(-0.8, 0)
$\sigma(ZHH)$	42.7%		42.7%	23.7%	–	–
$\sigma(\nu\bar{\nu}HH)$	–	–	26.3%	16.7%		
$\lambda$	83%	46%	21%	13%	28/21%	16/10%



- Given evidence of non-standard Higgs Couplings, what is the BSM origin ?

**Table 1-8.** Generic size of Higgs coupling modifications from the Standard Model values when all new particles are  $M \sim 1$  TeV and mixing angles satisfy precision electroweak fits. The Decoupling MSSM numbers assume  $\tan \beta = 3.2$  and a stop mass of 1 TeV with  $X_t = 0$  for the  $\kappa_\gamma$  prediction.

Model	$\kappa_V$	$\kappa_b$	$\kappa_\gamma$
Singlet Mixing	$\sim 6\%$	$\sim 6\%$	$\sim 6\%$
2HDM	$\sim 1\%$	$\sim 10\%$	$\sim 1\%$
Decoupling MSSM	$\sim -0.0013\%$	$\sim 1.6\%$	$\sim -0.4\%$
Composite	$\sim -3\%$	$\sim -(3 - 9)\%$	$\sim -9\%$
Top Partner	$\sim -2\%$	$\sim -2\%$	$\sim +1\%$

- **Higgs inverse problem**

- Many models might lead to similar deviations.
- Generic dependence:  $(v/M_{\text{bsm}})^2$  [decoupling MSSM  $\kappa_v \sim (v/M_{\text{bsm}})^4$ ]
- ILC (500)  $\kappa_v = 1.0\%$ :  $\kappa_b = 1.7\%$   $\kappa_\gamma = 8.7\%$
- Scales probed:  $0.3 \text{ TeV} < M_{\text{bsm}} < 3 \text{ TeV}$
- Would need a lepton collider with 6 TeV to directly observe the physics suggested by these deviations and disentangle the possibilities.

## Two Higgs Doublet Models (eg. Type II)

$$V = m_{11}^2 \Phi_1^\dagger \Phi_1 + m_{22}^2 \Phi_2^\dagger \Phi_2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + \Phi_2^\dagger \Phi_1) + \frac{1}{2} \lambda_1 (\Phi_1^\dagger \Phi_1)^2 + \frac{1}{2} \lambda_2 (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{1}{2} \lambda_5 [(\Phi_1^\dagger \Phi_2)^2 + (\Phi_2^\dagger \Phi_1)^2]$$

$$\tan \beta = v_2/v_1, \quad \beta - \alpha, \quad m_{12}^2, \quad m_H, \quad m_A, \quad m_{H^\pm}$$

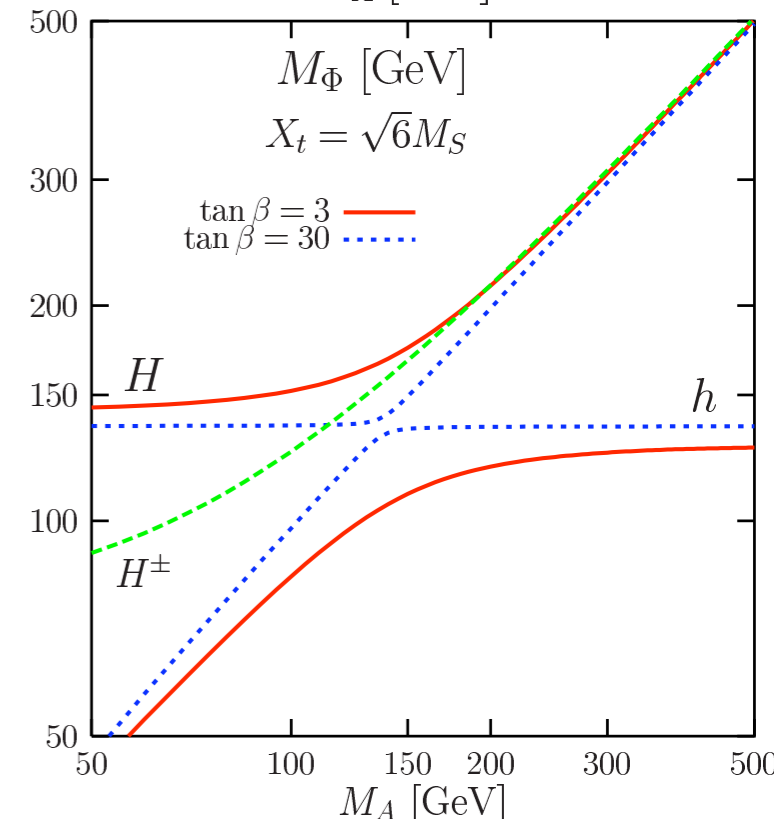
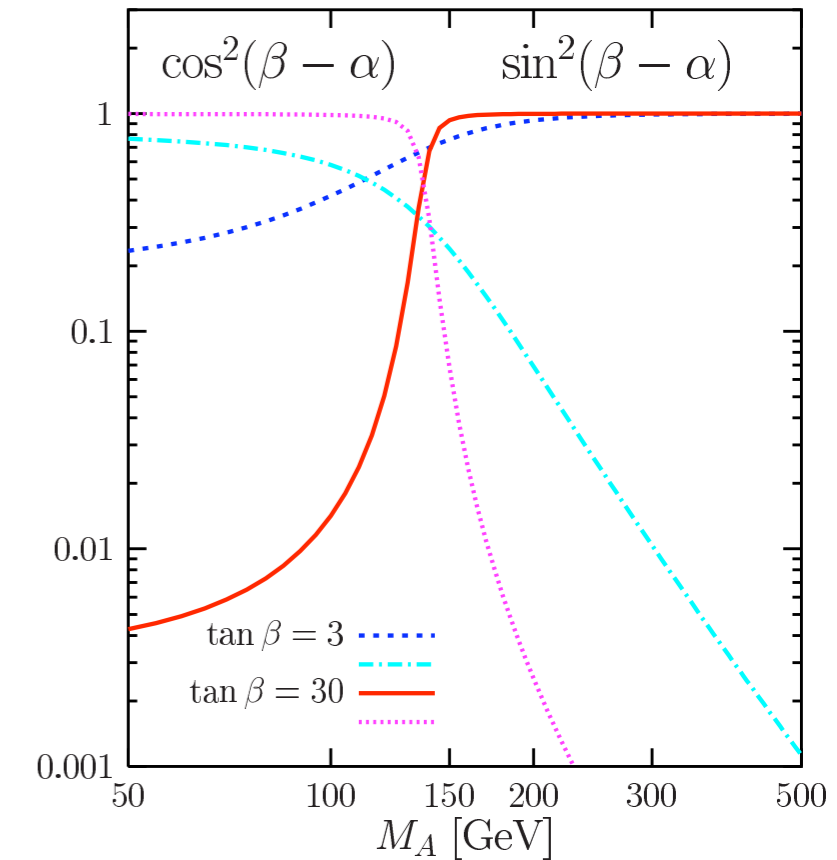
- Five scalar particles:  $h^0, H^0, A^0, H^\pm$
- Decay amplitudes depend on two parameters:  $(\alpha, \beta)$

	$\mu^+ \mu^-, b\bar{b}$	$t\bar{t}$	$ZZ, W^+W^-$	$ZA^0$
$h^0$	$-\sin \alpha / \cos \beta$	$\cos \alpha / \sin \beta$	$\sin(\beta - \alpha)$	$\cos(\beta - \alpha)$
$H^0$	$\cos \alpha / \cos \beta$	$\sin \alpha / \sin \beta$	$\cos(\beta - \alpha)$	$-\sin(\beta - \alpha)$
$A^0$	$-i\gamma_5 \tan \beta$	$-i\gamma_5 / \tan \beta$	0	0

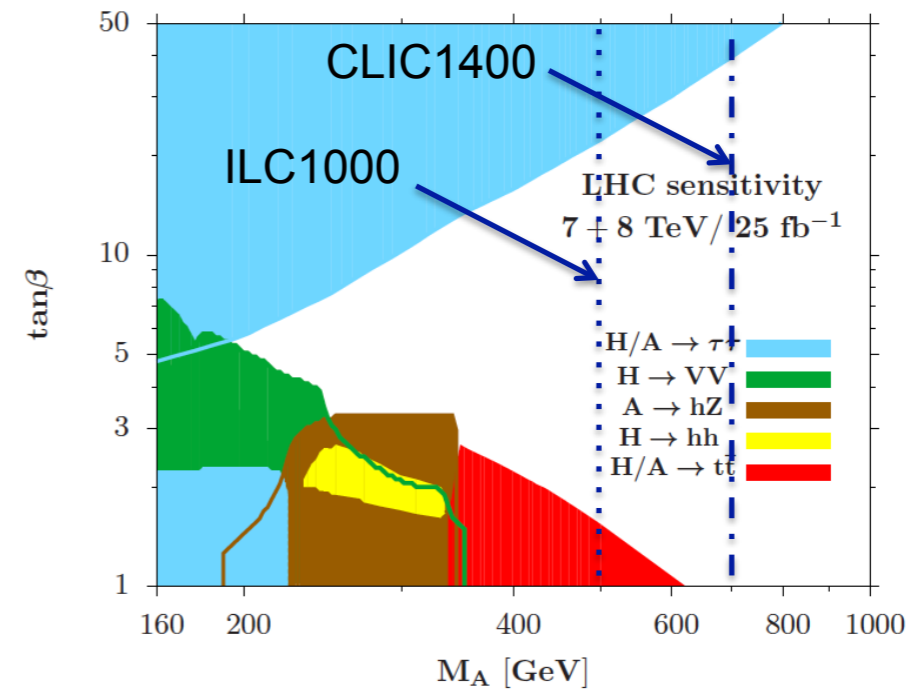
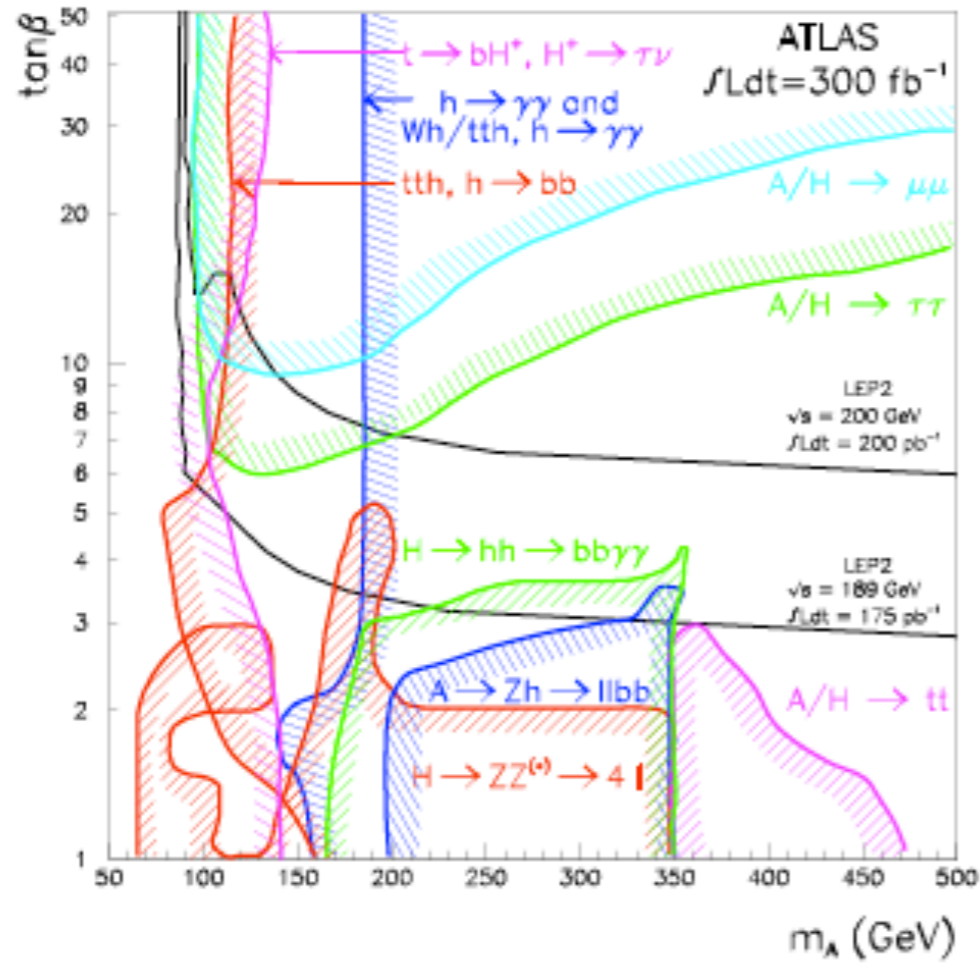
$$\tan 2\alpha = \frac{M_A^2 + M_Z^2}{M_A^2 - M_Z^2} \tan 2\beta.$$

- decoupling limit  $m_{A^0} \gg m_{Z^0}$   $\cos(\beta - \alpha) \rightarrow 0$ :

- »  $h^0$  couplings close to SM values
- »  $H^0, H^\pm$  and  $A^0$  nearly degenerate in mass
- »  $H^0$  small couplings to  $VV$ , large couplings to  $ZA^0$
- » For large  $\tan \beta$ ,  $H^0$  and  $A^0$  couplings to charged leptons and bottom quarks enhanced by  $\tan \beta$ . Couplings to top quarks suppressed by  $1/\tan \beta$  factor.



- The LHC has difficulty observing the H, A especially for masses  $> 500$  GeV. Even at  $\sqrt{s} = 14$  TeV and  $300 \text{ fb}^{-1}$ .



J. Gunion and H. Haber [arXiv:hep-ph/0207010], ...

M. Carena, I. Low, N. R. Shah and C. Wagner [arXiv:1310.2244]

– Loophole - Alignment without decoupling.

- The lightest CP-even Higgs mimics the SM higgs.

$$\begin{pmatrix} s_\beta^2 & -s_\beta c_\beta \\ -s_\beta c_\beta & c_\beta^2 \end{pmatrix} \begin{pmatrix} -s_\alpha \\ c_\alpha \end{pmatrix} = -\frac{v^2}{m_A^2} \begin{pmatrix} L_{11} & L_{12} \\ L_{12} & L_{22} \end{pmatrix} \begin{pmatrix} -s_\alpha \\ c_\alpha \end{pmatrix} + \frac{m_h^2}{m_A^2} \begin{pmatrix} -s_\alpha \\ c_\alpha \end{pmatrix} .$$

Mass and eigenvector eq. for h in THDM

$\alpha$  - mixing angle;  $\tan \beta = v_2/v_1$

$L_{11} = \lambda_1 c_\beta^2 + \lambda_5 s_\beta^2$ ;  $L_{22} = \lambda_2 s_\beta^2 + \lambda_5 c_\beta^2$ ;

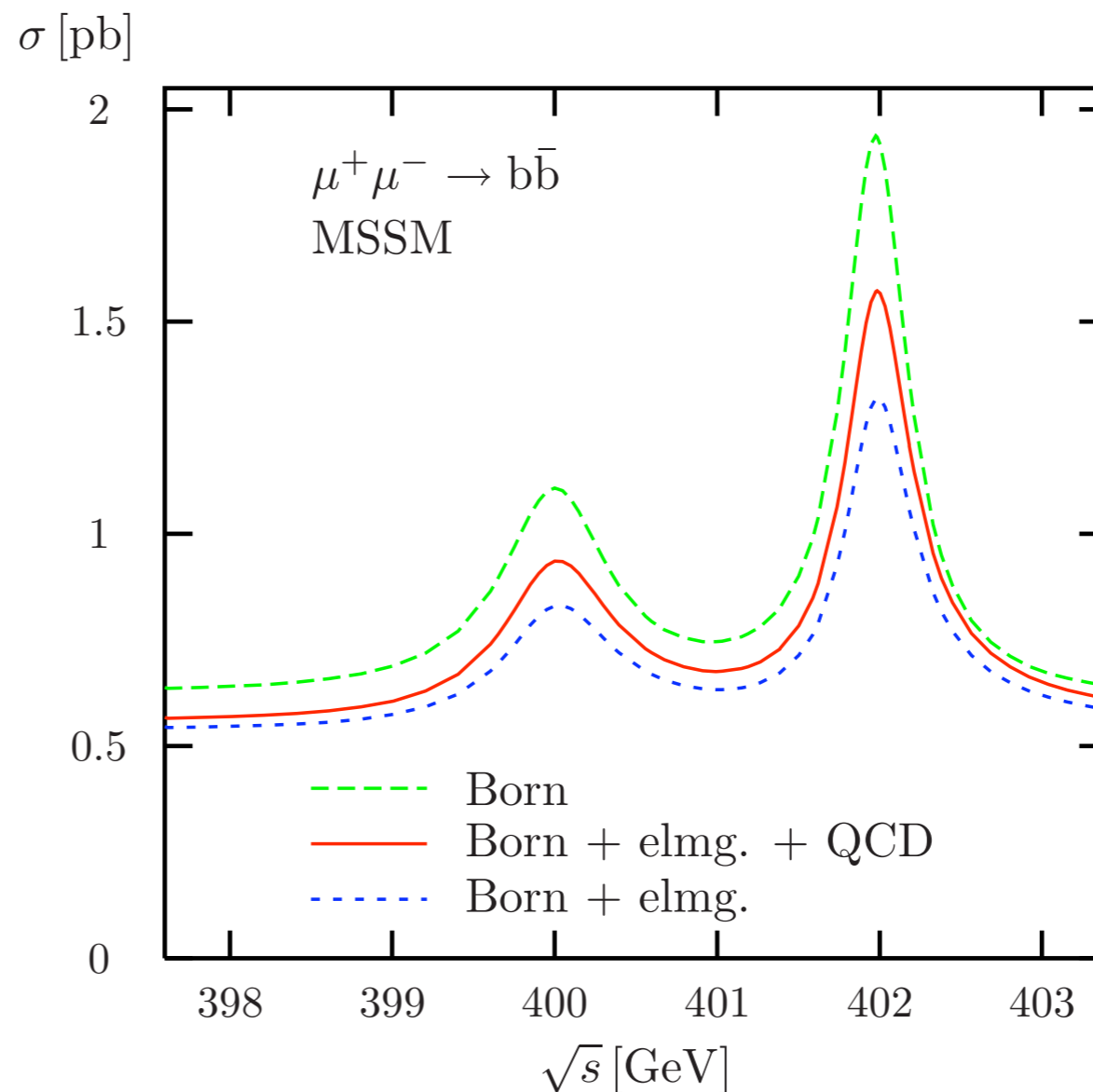
$L_{12} = (\lambda_3 + \lambda_4) s_\beta c_\beta$

- $\cos(\beta - \alpha) = 0 \rightarrow$  h has SM couplings:  $1/m_A \rightarrow 0$  usual decoupling.
  - RHS = 0  $\rightarrow$  alignment: independent of  $m_A$  but requires a specific value of  $\tan \beta$
  - In lowest order H/A,  $H^\pm$  states do not couple to W and Z's.
  - Only the lightest CP even neutral higgs contributes to the EW symmetry breaking.
  - However these states do have Yukawa couplings to fermions.
  - Signals at LHC are different from the usual decoupling THDM signals
- The muon collider can observe these states as s-channel resonances.  
(if the branching ratio to  $\mu^+\mu^-$  is not much smaller than for the SM higgs)

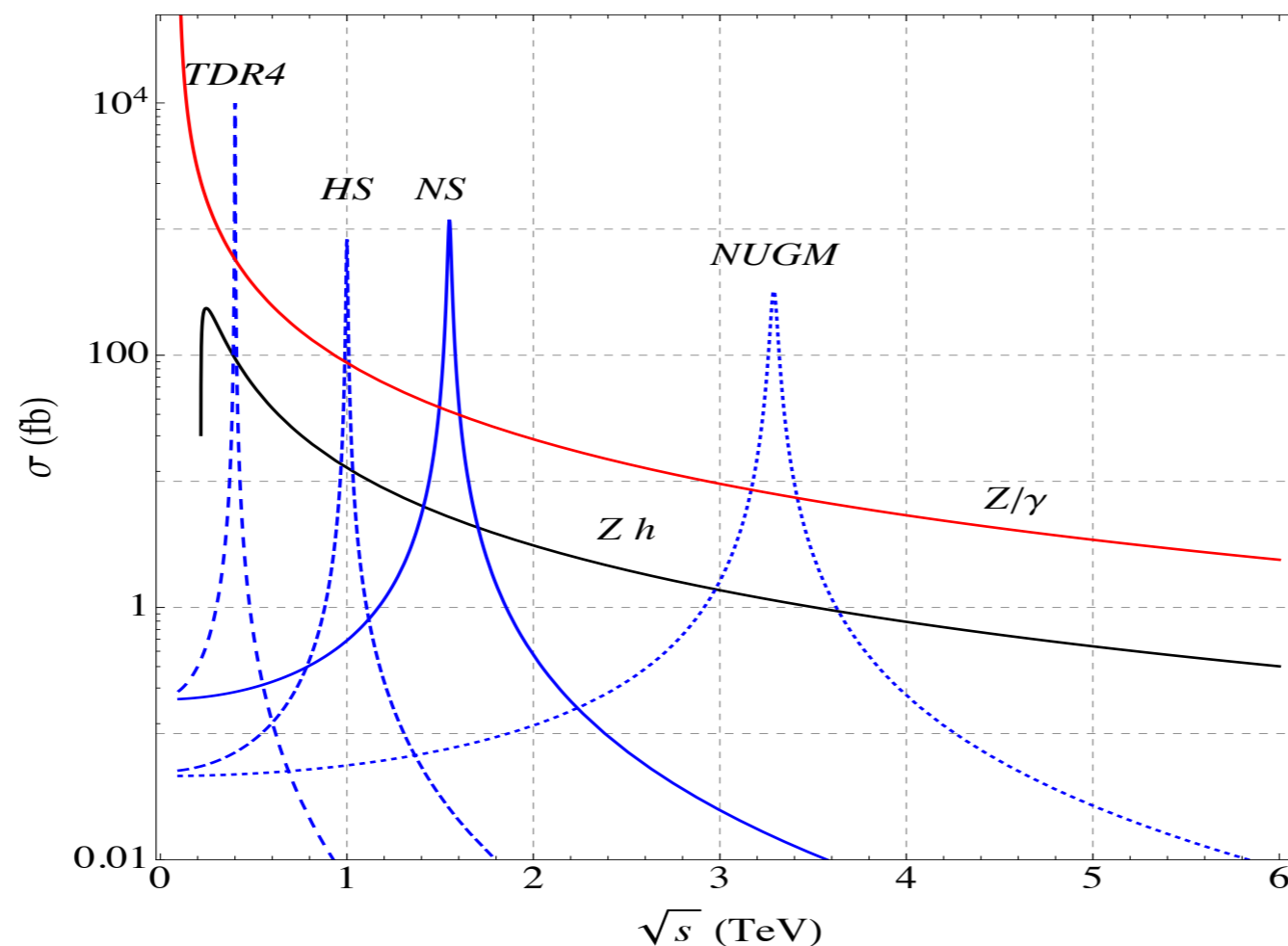


- Early studies have shown the power of a Muon Collider to separate these states.
- Good energy resolution is needed for  $H^0$  and  $A^0$  studies:

Dittmaier and Kaiser  
[hep-ph/0203120]

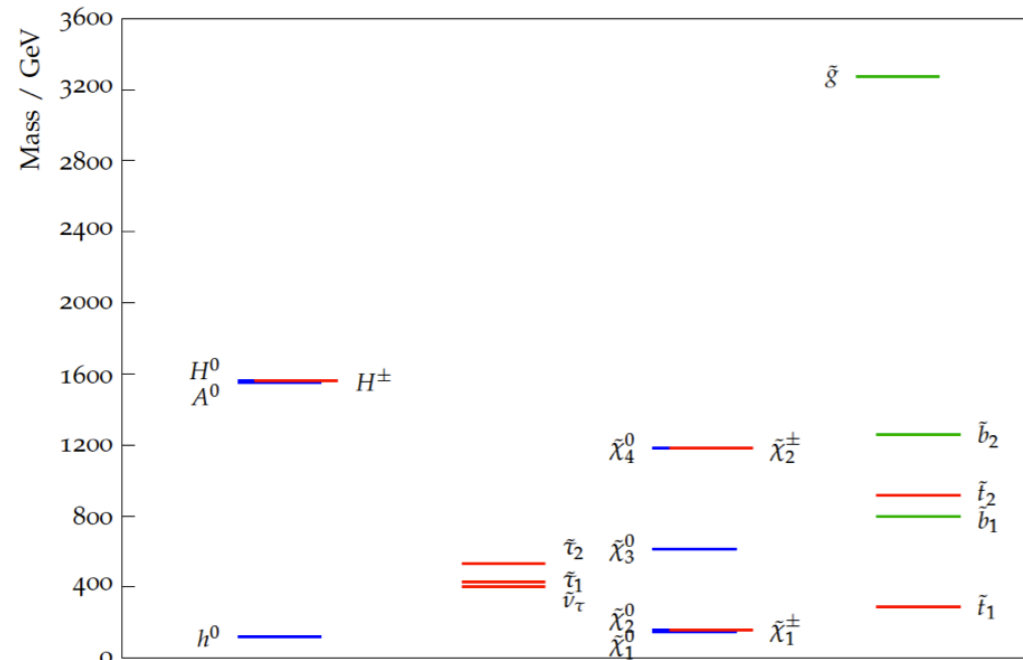


- However generally expect heavy:  $H^\pm$ ,  $H^0$  and  $A^0$ 
  - LHC limits on  $H^\pm$ :  $\sim 350$  (ATLAS) (CMS)
  - SUSY models that evade the all present experimental constraints often have very heavy THDM scalars
- The  $H/A$  are observable as  $s$ -channel resonances at a MC!



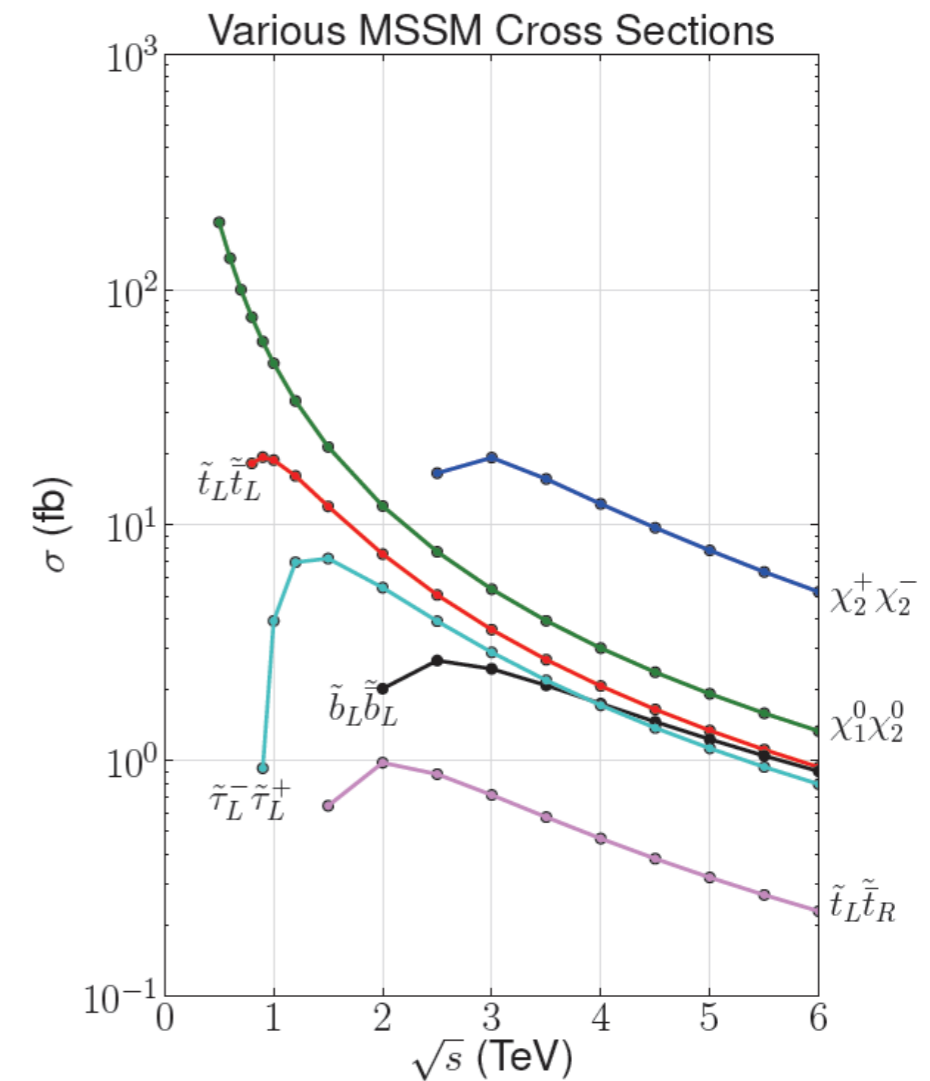
- Example of Natural SUSY

- Low-lying spectrum



- For electroweakinos, sleptons, ...

$A \geq 3\text{TeV}$  muon collider has discovery reach beyond a 100 TeV pp collider !

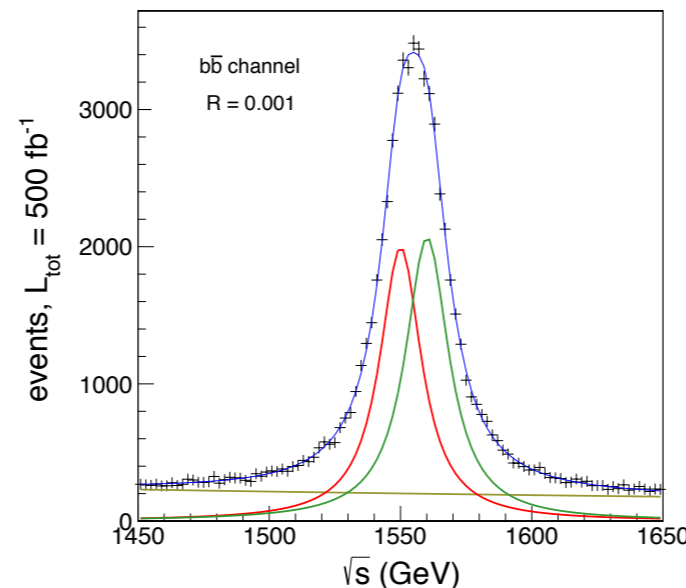
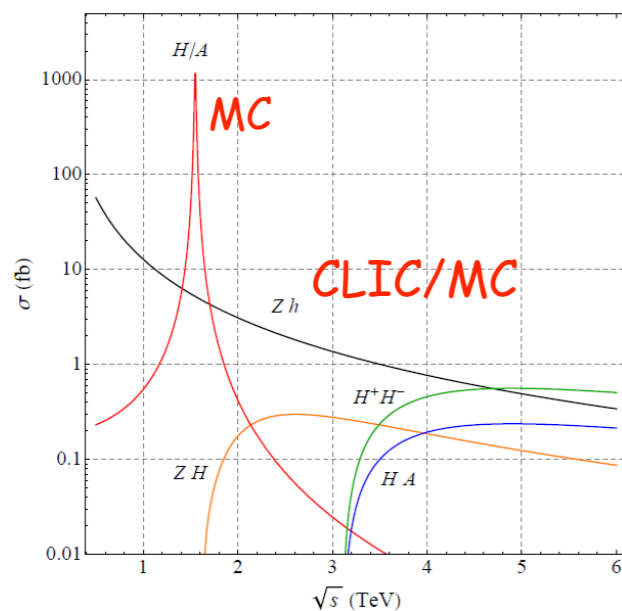


- The  $H/A$  are observable as s-channel resonances at a MC!
  - $M_H = M_A \sim 1.5 \text{ TeV}/c^2$ ,  $\Gamma \sim 19 \text{ GeV}$
  - Large  $\tan\beta \sim 20$
  - Limited spectrum of SUSY particle decays.
  - **Expect  $10^6$   $H/A$  decays per  $1 \text{ ab}^{-1}$**
- From this model we see the power of resonance production:
  - The states  $H/A$  are separable:  $\Delta M \approx 10 \text{ MeV}$ . Widths and branching ratios can be disentangled
  - Tau decays ( $\sim 8\%$ ) may allow  $H/A$  CP determination.
  - Decays to supersymmetric particles ( $\sim 20\%$ ): Self-analysing ewkinos - (Initial state beam polarization not essential)

**E.E and A. Martin [arXiv:1306.2609]**

TABLE I. Properties of the  $H$  and  $A$  states in the Natural Supersymmetry benchmark model [35]. In addition to masses and total widths, the branching ratios for various decay modes are shown.

	$H$		$A$	
Mass	1.560 TeV		1.550 TeV	
Width	19.5 GeV		19.2 GeV	
(Decay)	Br	(Decay)	Br	
$(b\bar{b})$	0.64	$(b\bar{b})$	0.65	
$(\tau^+\tau^-)$	$8.3 \times 10^{-2}$	$(\tau^+\tau^-)$	$8.3 \times 10^{-3}$	
$(s\bar{s})$	$3.9 \times 10^{-4}$	$(s\bar{s})$	$4.0 \times 10^{-3}$	
$(\mu^+\mu^-)$	$2.9 \times 10^{-4}$	$(\mu^+\mu^-)$	$2.9 \times 10^{-4}$	
$(t\bar{t})$	$6.6 \times 10^{-3}$	$(t\bar{t})$	$7.2 \times 10^{-3}$	
$(gg)$	$1.4 \times 10^{-5}$	$(gg)$	$6.1 \times 10^{-5}$	
$(\gamma\gamma)$	$1.1 \times 10^{-7}$	$(\gamma\gamma)$	$3.8 \times 10^{-9}$	
$(Z^0Z^0)$	$2.6 \times 10^{-5}$	$(Z^0\gamma)$	$4.3 \times 10^{-8}$	
$(h^0h^0)$	$4.4 \times 10^{-5}$			
$(W^+W^-)$	$5.3 \times 10^{-5}$			
$(\tilde{\tau}_1^\pm \tilde{\tau}_2^\mp)$	$9.2 \times 10^{-3}$	$(\tilde{\tau}_1^\pm \tilde{\tau}_2^\mp)$	$9.5 \times 10^{-3}$	
$(\tilde{t}_1 \tilde{t}_1^*)$	$3.1 \times 10^{-3}$	$(\tilde{t}_1 \tilde{t}_1^*)$	$1.1 \times 10^{-3}$	
$(\chi_1^0 \chi_1^0)$	$2.6 \times 10^{-3}$	$(\chi_1^0 \chi_1^0)$	$3.2 \times 10^{-3}$	
$(\chi_2^0 \chi_2^0)$	$1.3 \times 10^{-3}$	$(\chi_2^0 \chi_2^0)$	$1.1 \times 10^{-3}$	
$(\chi_1^0 \chi_3^0)$	$2.8 \times 10^{-2}$	$(\chi_1^0 \chi_3^0)$	$3.9 \times 10^{-2}$	
$(\chi_1^0 \chi_4^0)$	$1.7 \times 10^{-2}$	$(\chi_1^0 \chi_4^0)$	$4.0 \times 10^{-2}$	
$(\chi_2^0 \chi_3^0)$	$3.8 \times 10^{-2}$	$(\chi_2^0 \chi_3^0)$	$2.7 \times 10^{-2}$	
$(\chi_2^0 \chi_4^0)$	$4.0 \times 10^{-2}$	$(\chi_2^0 \chi_4^0)$	$1.5 \times 10^{-2}$	
$(\chi_1^\pm \chi_2^\mp)$	$5.7 \times 10^{-2}$	$(\chi_1^\pm \chi_2^\mp)$	$6.0 \times 10^{-2}$	



- **The  $H/A$  resonances are a factory for SUSY studies at a Muon Collider.**

- Supersymmetry

$$Q|boson \rangle = |\text{fermion} \rangle; \quad Q|\text{fermion} \rangle = |boson \rangle$$

- The symmetry is not manifest at presently observable energies.

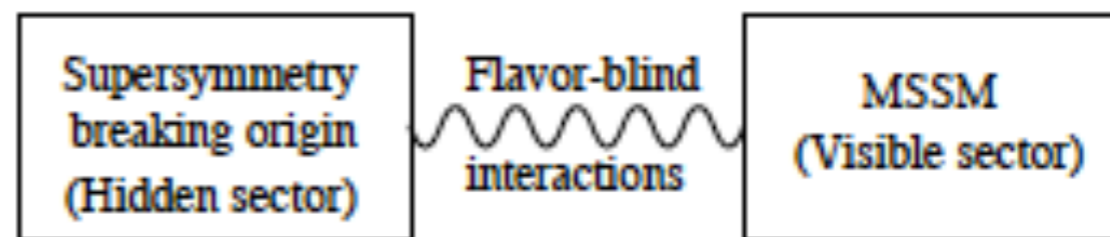
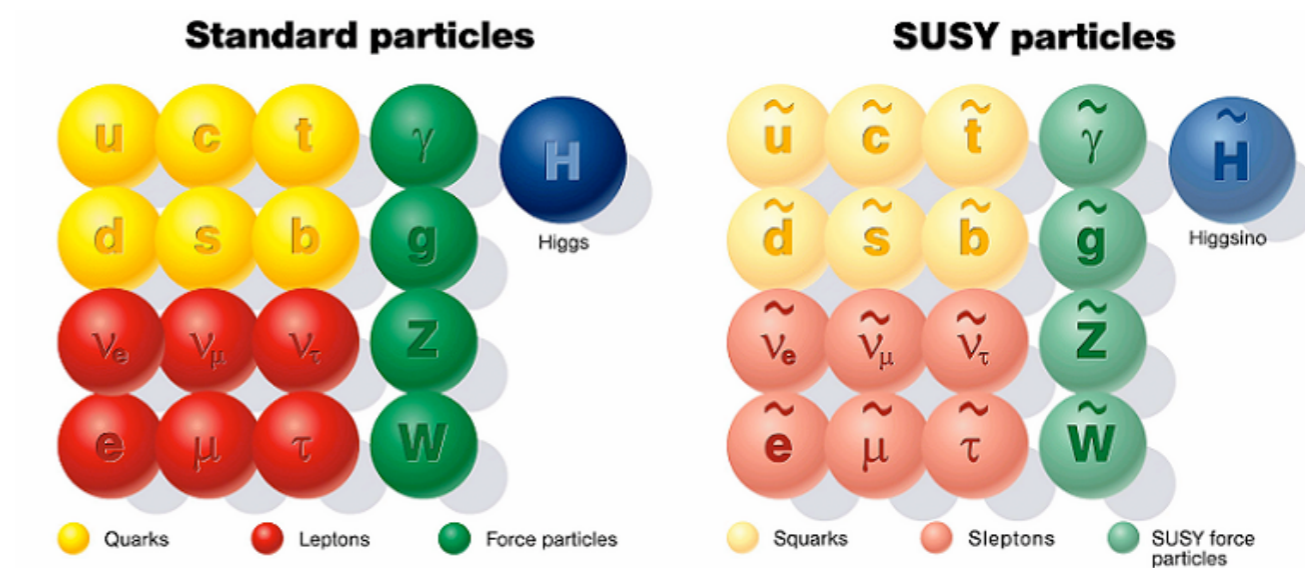
- If the breaking occurs near the EWSB scale, SUSY can be a solution of the naturalness problem of the standard model.

- Questions:

- What breaks the symmetry?

- mSUGRA (gravity)
- GMSB (gauge)
- AMSB (anomalies)

- What is the spectrum of superpartner masses?



- Ten years ago:



- cMSSM - simple model with only 5 parameters ( $m_0, m_{1/2}, \tan\beta, A/m_0, \text{sign}(\mu)$ ); pMSSM (19 parameters), unconstrained (104+)
- LHC limits on SUSY sparticles in various cMSSM scenerios:
  - Gluino and light squark masses limits  $\sim 1.2\text{TeV}$
  - The detailed study of the full SUSY spectrum will require a multiTev lepton collider.
- Bounds on cMSSM from all present data: LHC, B decays, Dark matter limits,  $(g-2)_\mu, \dots$

O. Buchmueller et.al. [arXiv:1312.5250]

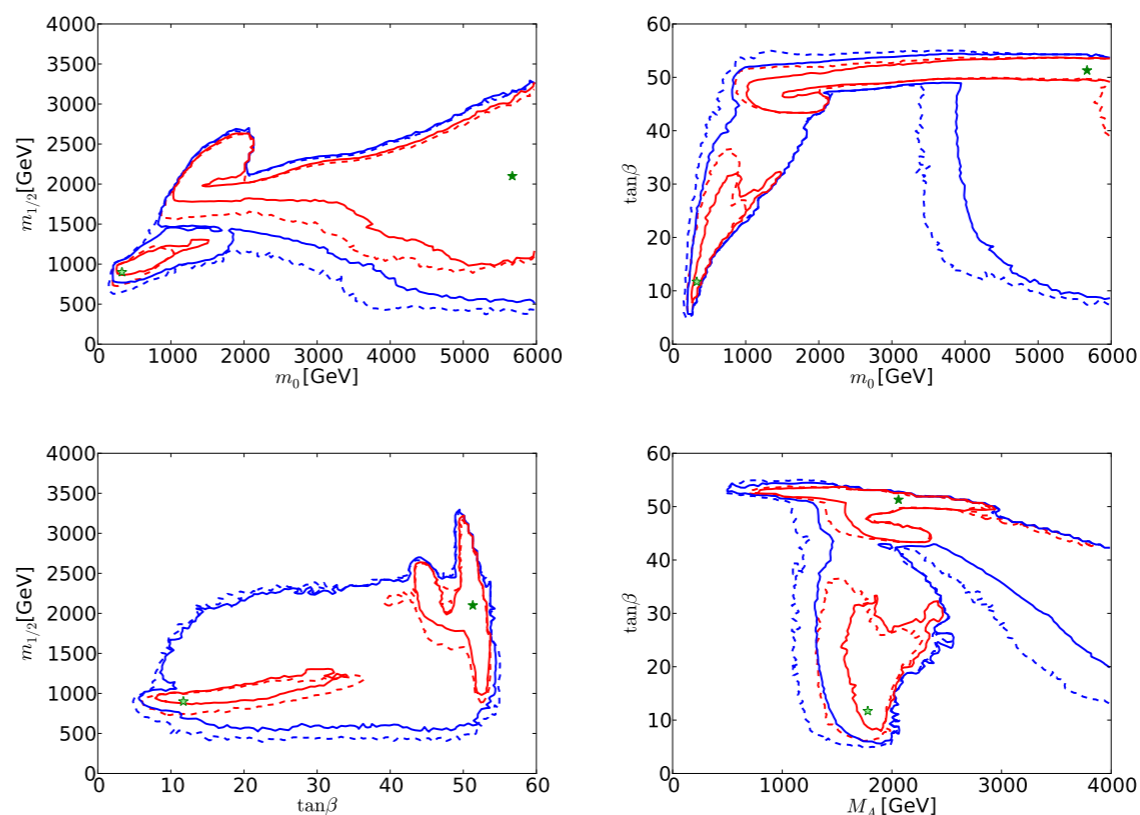
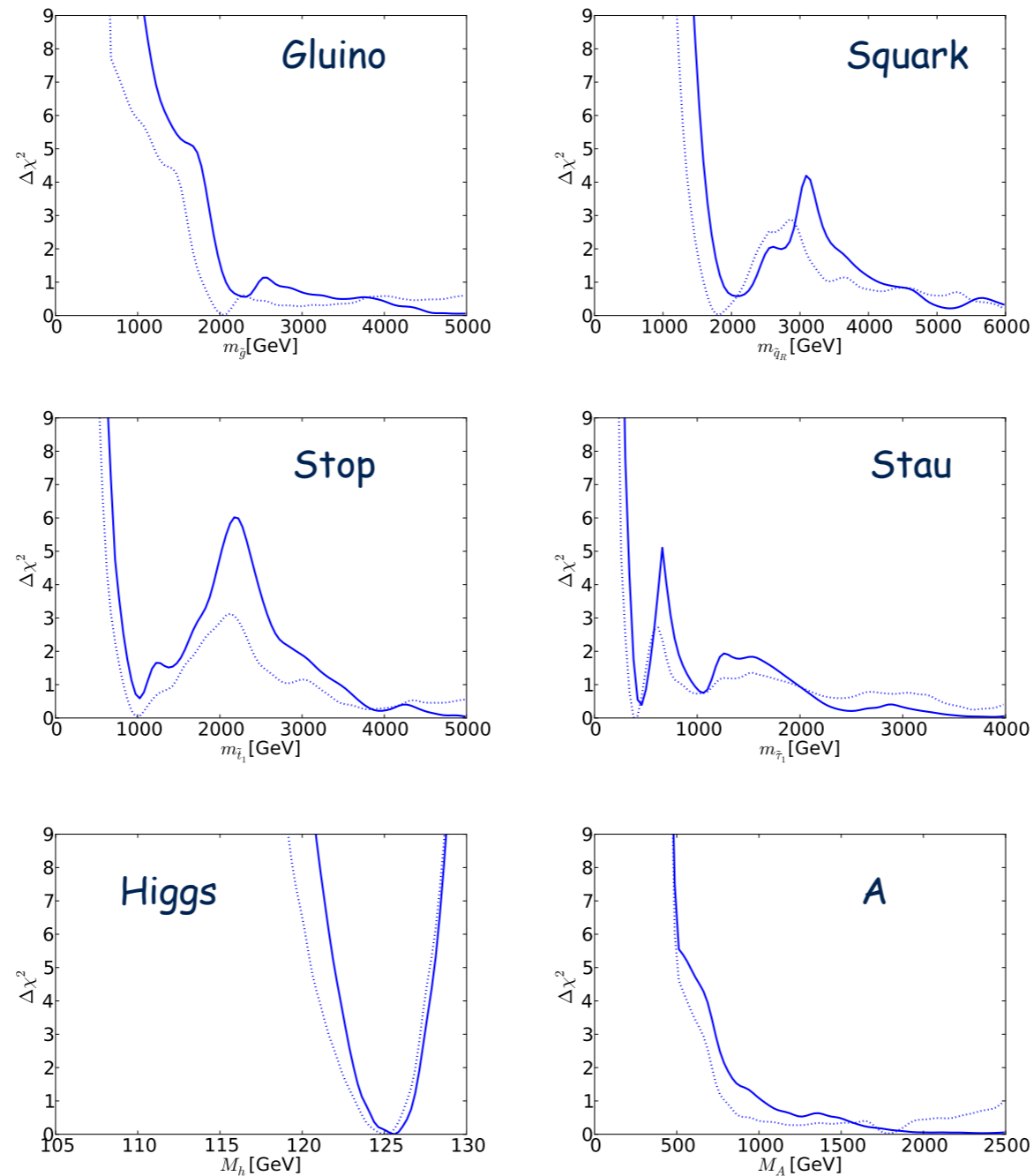


Figure 3. A compilation of parameter planes in the CMSSM for  $\mu > 0$ , including the  $(m_0, m_{1/2})$  plane (upper left), the  $(m_0, \tan\beta)$  plane (upper right), the  $(\tan\beta, m_{1/2})$  plane (lower left), and the  $(M_A, \tan\beta)$  plane (lower right), after implementing the ATLAS 20/fb jets +  $\cancel{E}_T$ ,  $\text{BR}(B_{s,d} \rightarrow \mu^+\mu^-)$ ,  $M_h$ ,  $\Omega_\chi h^2$ , LUX constraints and other constraints as described in the text. The results of the current CMSSM fit are indicated by solid lines and filled stars, and a fit to previous data [21] using the same implementations of the  $M_h$ ,  $\sigma_p^{\text{SI}}$  and other constraints is indicated by dashed lines and open stars. The red lines denote  $\Delta\chi^2 = 2.30$  contours (corresponding approximately to the 68% CL), and the red lines denote  $\Delta\chi^2 = 5.99$  (95% CL) contours.

- Projecting into one dimensional bounds - most likely sparticle masses rise





– Are various constrained models consistent with a Higgs mass of 125.5 GeV?

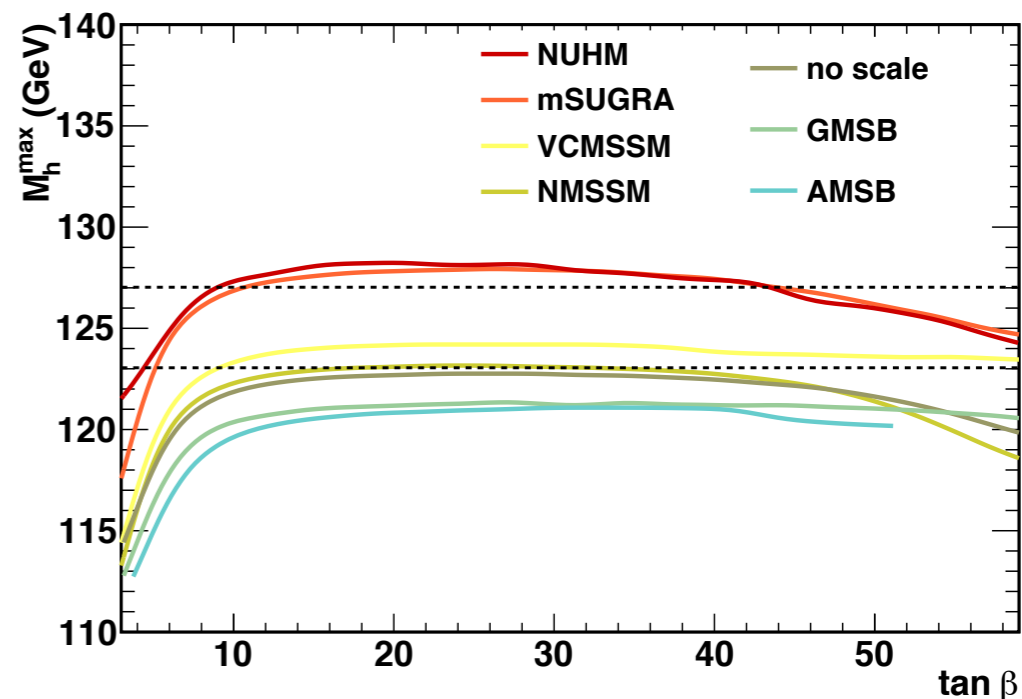
– Parameters varied in wide range.  
Upper bound - mh in top 1%

– GMSB, AMSB ✘

– mSUGRA ✓

- NUHM: non universal  $m_0$
- VCMSSM:  $m_0 \approx -A_0$
- NMSSM:  $m_0 \approx 0$   $A_0 \approx -1/4 m_{1/2}$
- no scale:  $m_0 \approx A_0 \approx 0$

[A. Atbey, et. al.: arXiv:1112.3028]



– As mass scales increase ( $\mu^2$  increases) more fine tuning. The little hierarchy problem.

$$\frac{m_Z^2}{2} = \frac{m_{H_d}^2 + \Sigma_d^d - (m_{H_u}^2 + \Sigma_u^u) \tan^2 \beta}{\tan^2 \beta - 1} - \mu^2$$

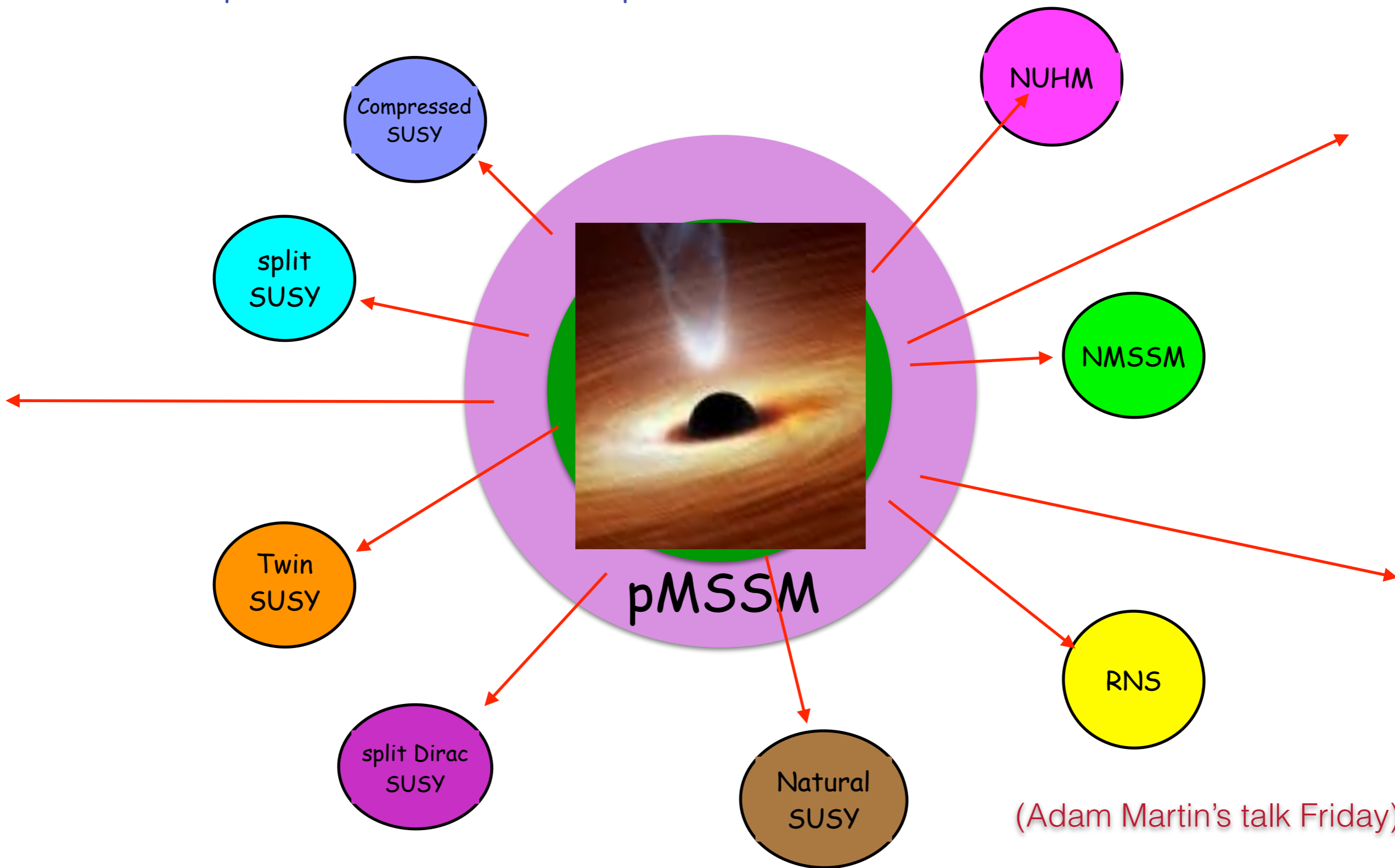
for large masses need big cancellations

[one loop]

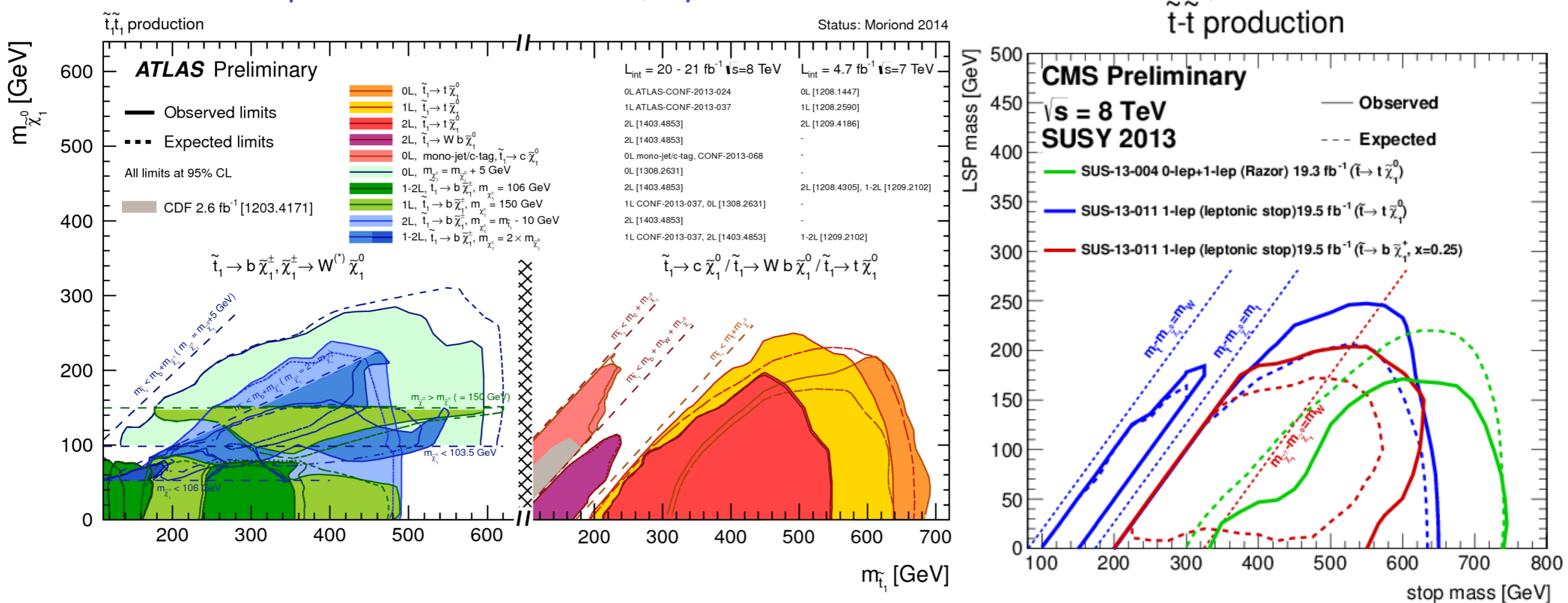
$$\Sigma_t^t = \frac{3g^2}{8\pi^2} \frac{m_t^4}{m_W^4} \left[ \ln \frac{m_t^2}{m_{\tilde{t}}^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right]$$

$$\tilde{X}_t = \frac{2\tilde{A}_t^2}{M_S^2} \left( 1 - \frac{A_t^2}{12M_S^2} \right), \quad \tilde{A}_t = A_t - \mu \cot \beta$$

– 2014: Escape from the Black Hole of Experimental Limits

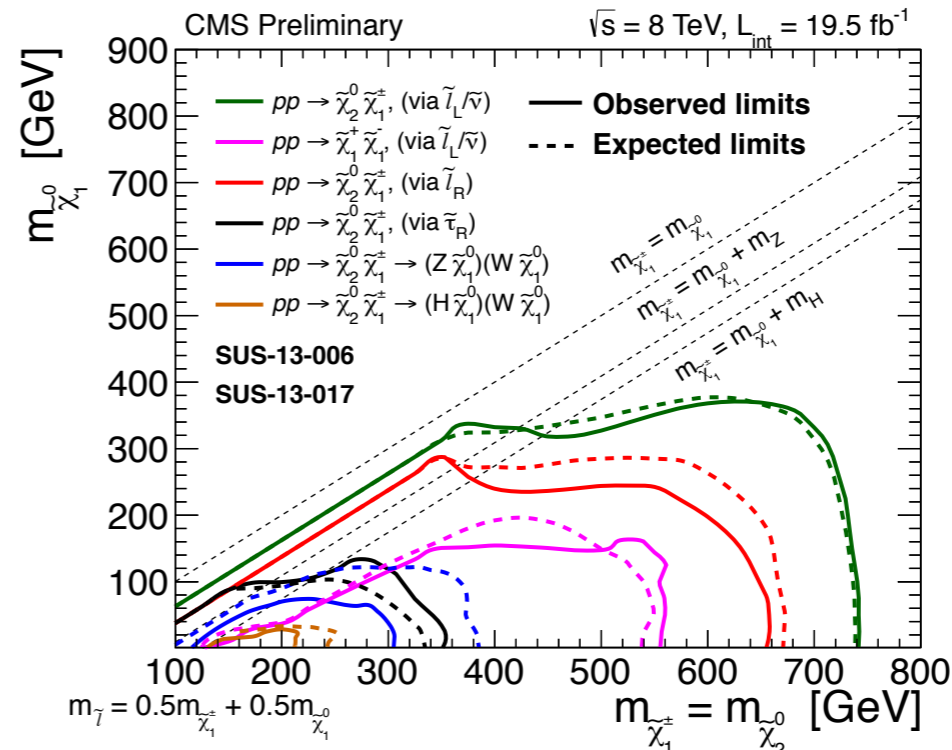
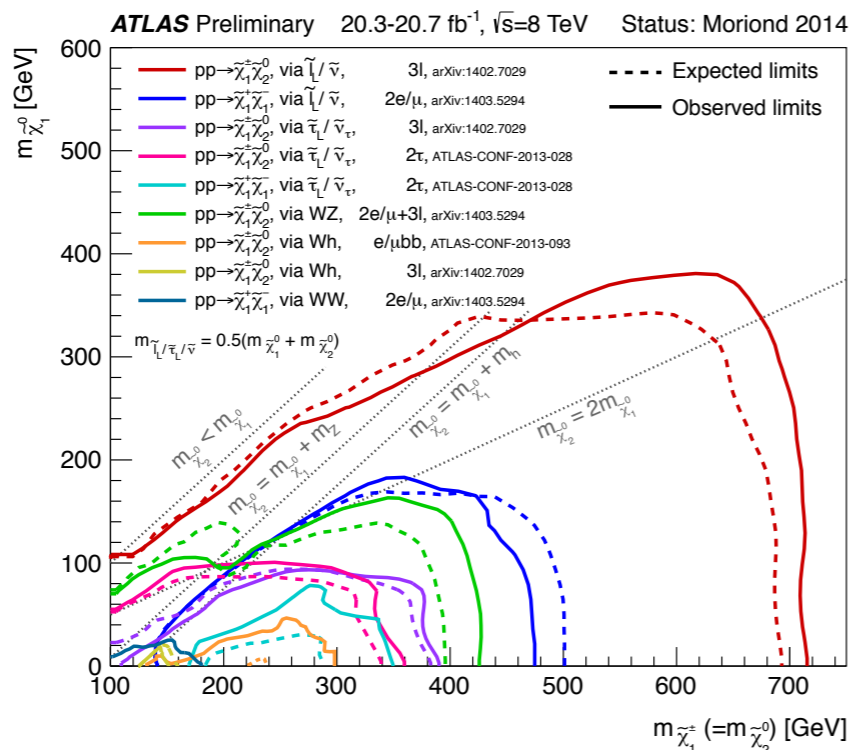


- LHC stop limits pushing theories to stronger nominal fine tuning..
  - Masses up to 700 GeV excluded (beyond the reach of even a 1 TeV ILC)



- But still gaps in the exclusion plots depending on decay mode and decay product masses.
- Look forward to the LHC run 2 at 13+ TeV.

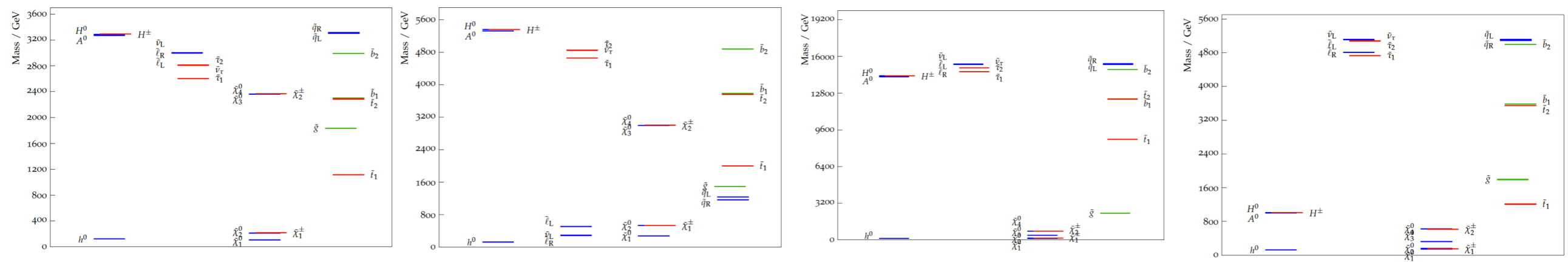
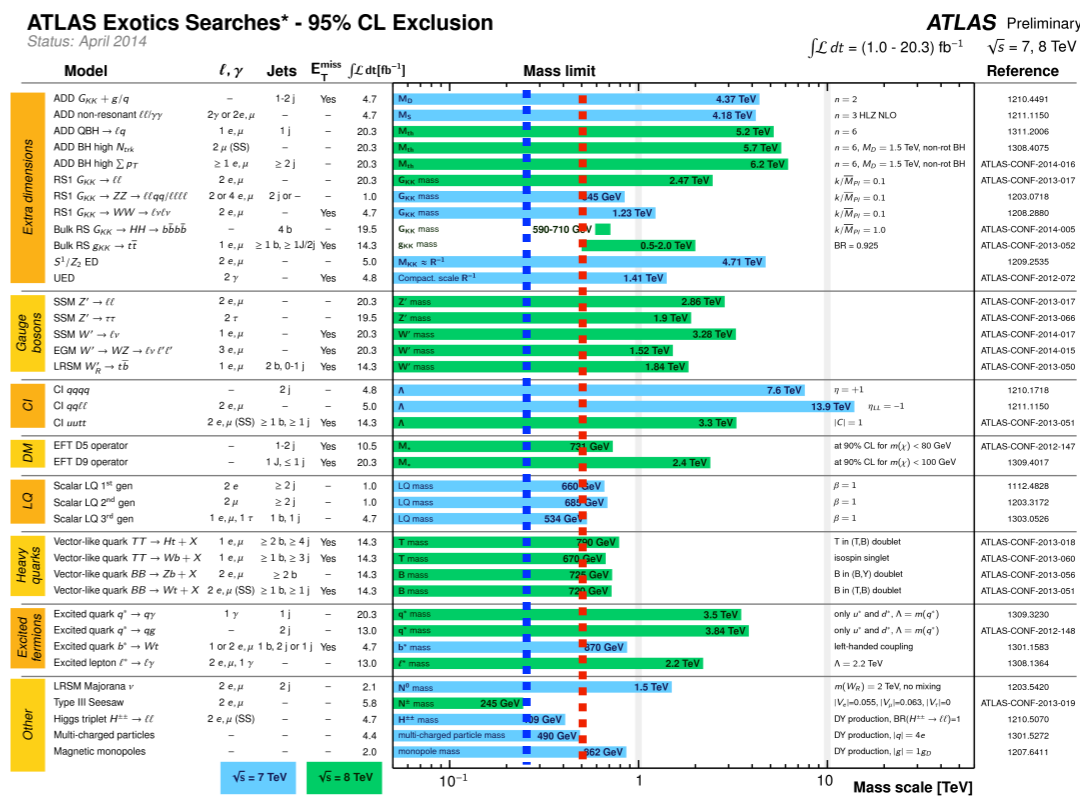
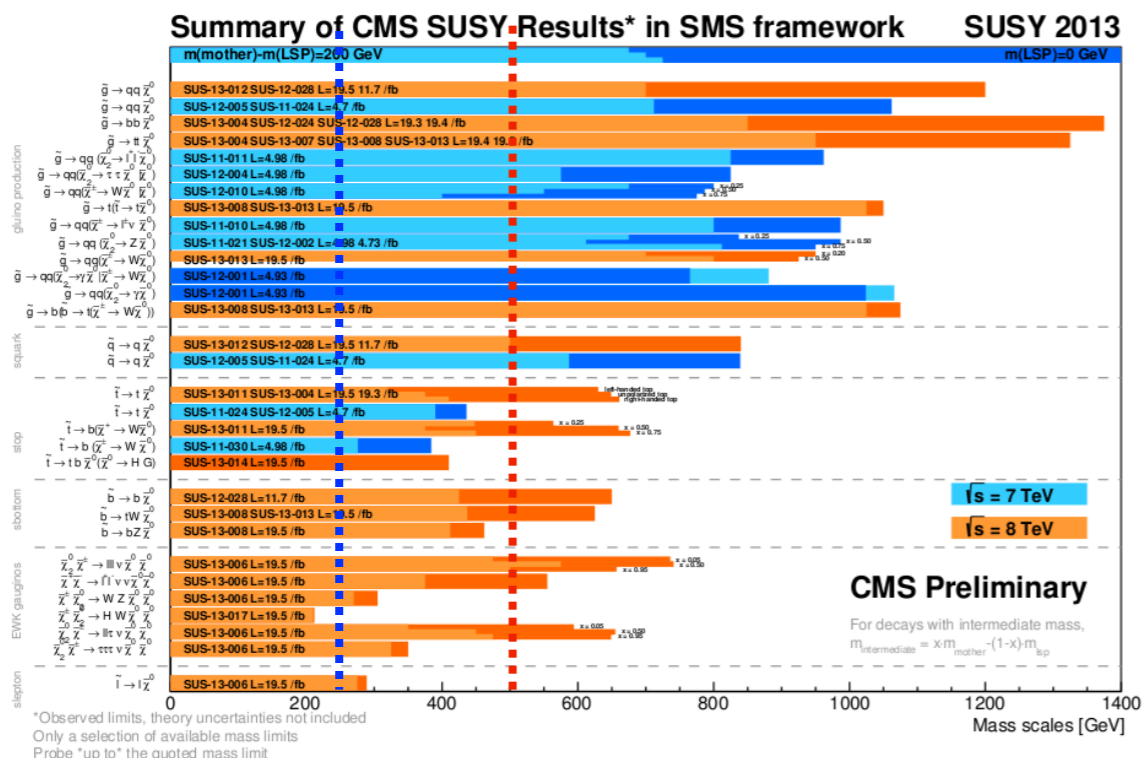
- Need to observe and study all 4 charginos and 2 neutralinos. Limits for  $\chi_1^+$ ,  $\chi_2^0$  already exist from LHC 8/7 TeV run.



- Seems to rule out study of even these lowest at the ILC even upgraded to 1 TeV.
- Focussing on higgs decays of  $\chi_2^0$  A. Bharucha<sup>1†</sup>, S. Heinemeyer<sup>2‡</sup>, F. von der Pahlen studied this issue [arXiv:1404.0365]. Based on existing data they conclude:

Altogether these results show, on the one hand, how important it is to look at a realistic spectrum (i.e. where the decays to a Higgs boson are not neglected), and on the other hand that dedicated searches for the  $Wh + E_T^{\text{miss}}$  channel are beneficial [43]. The results indicate that there is ample room for chargino/neutralino production at the ILC with  $\sqrt{s} \leq 1$  TeV.

- Determining the nature of SUSY dynamics and hence the nature of SUSY breaking will require detailed measurements of almost the full spectrum. This is not possible at the ILC (500) [.....] and by the end of run 2 we will know the fate of an ILC(1000) [.....].



Sample spectra (2012) that try to minimize fine tuning in a 100+ parameter space.

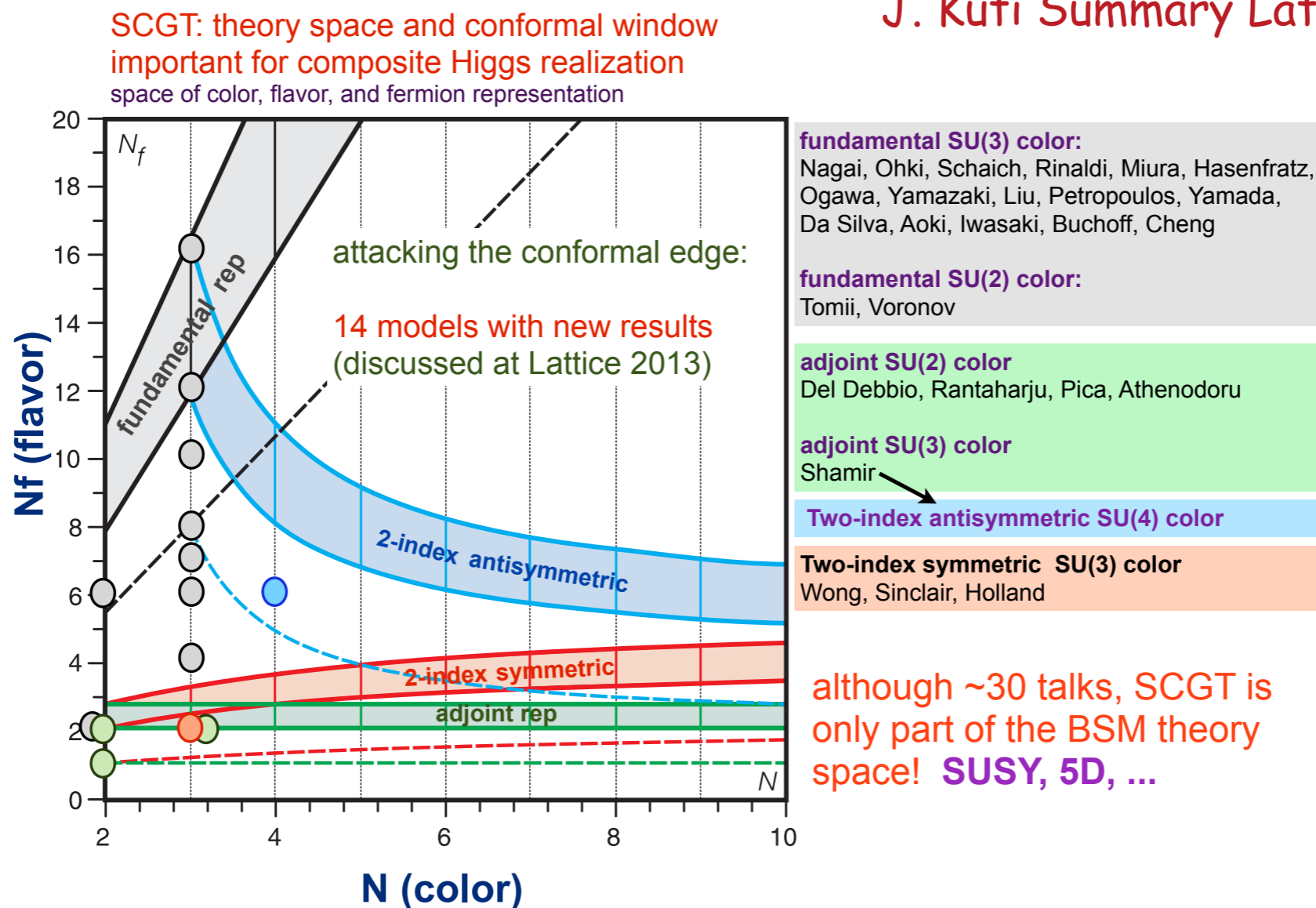
- QCD-like Technicolor is dead but ETC and Walking Technicolor lives
  - QCD-like technicolor failed to give quark and lepton masses -> ETC
  - ETC could produce flavor changing neutral currents too large -> Walking Technicolor
  - Walking requires near conformal strong dynamics. Is this possible?
- Spectrum not QCD like - what does it look like?
  - Can light scalars arise in walking technicolor theories?
  - Can the Higgs be a pseudodilaton?
  - What would rest of spectrum look like?
  - What are low-lying states?
- What is role of ETC and 4 fermion interactions?
  - Not presently in lattice studies
  - EWSB driven by four fermion interactions

R. Sekhar Chivukula, Andrew G. Kenneth Lane [NP B343, 554 (1990):  
W.~A.~Bardeen, C.~T.~Hill and M.~Lindner  
[Phys.Rev. D41,1647(1990)]

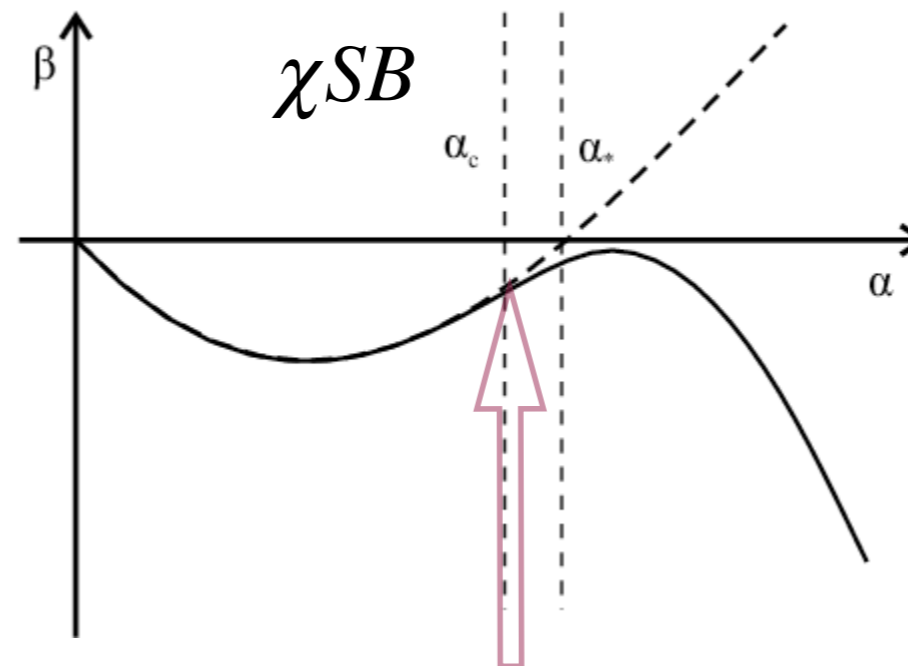
- Lattice Studies

- Look for theories in which walking can be realized.
- Evidence for conformal behaviour:  $SU(2)$  adjoint fermion doublet (U,D)
- $SU(3)$  16 fundamental fermions

## J. Kuti Summary Lattice 2013



– Walking technicolor toy models



when chiral symmetry breaking  
turns conformal FP into walking

- SU(4) 6 antisymmetric rank 2 tensor 1
- SU(3) 2 adjoint fermions (octets)

- Much progress but still much to learn to have the tools to make realistic models of a strong dynamics solution.
- Will likely need more experimental hints. Low-lying spectrum.
- Requires high energy colliders.

T. DeGrand, Y. Shamir and B. Svetitsky [arXiv:1307.2425].



- Electroweak Symmetry Breaking is generated dynamically at nearby scale
  - ~~Technicolor~~, ETC, walking TC, topcolor, Two Scale TC, composite Higgs models, ...
  - New strong interactions nearby:
    - What is the spectrum of low-lying states? What makes the Higgs light?
    - What is the ultraviolet completion? Gauge group? Fermion representations?
    - What is the energy scale of the new dynamics?
    - Any new insight into quark and/or lepton flavor mixing and CP violation?

## - Contact interactions

- e.g. Compositeness, broken flavor symmetries, ...

- Present LHC bounds ( $\sim 10$  TeV)  $\mathcal{L} = \frac{g^2}{\Lambda^2} (\bar{\Psi}\Gamma\Psi)(\bar{\Psi}\Gamma'\Psi)$

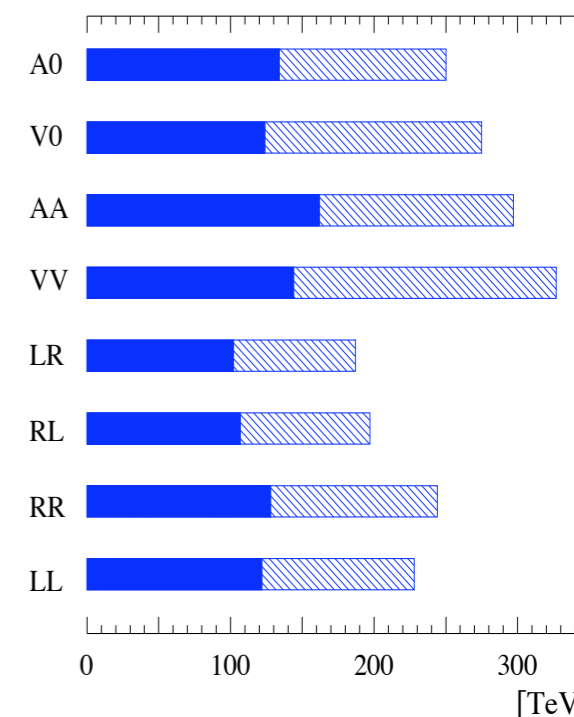
- Muon collider (3 TeV) sensitive to scales  $> 200$  TeV

- Forward cone cut not important
- Polarization useful in determining chiral character of the

$1 \text{ ab}^{-1}$ ,  $P_{\pm}=0.8$ ,  $e^+e^- \rightarrow \mu^+\mu^-$   
 $\Delta P/P=0.5\%$

CLIC(3 TeV):  $P_{\pm}=0.6$ ,  $\Delta_{\text{sys}}=0.5\%$ ,  $\Delta L=0.5\%$

LC (1TeV):  $P_{\pm}=0.6$ ,  $\Delta_{\text{sys}}=0.2\%$ ,  $\Delta L=0.5\%$



- The Higgs discovery has changed the theory landscape. SUSY and strong Dynamics ideas survive present LHC results (but cMSSM and QCD-like Technicolor are dead)
- Naturalness is still a powerful motivation for BSM physics, What is the fate of naturalness? SUSY with some fine tuning? Higgs as a composite state? or another not yet imagined solution?
- The direction of BSM physics is not yet clear. Much will be learned from the 13+ TeV LHC running. Further clues from a ILC/TLEP Higgs Factory, rare processes and dark matter searches may appear.
- However it is already clear that the full exploration of Terascale physics will require new high energy colliders with sensitivity to pair production of multiTeV BSM particles.
  - HL-LHC for new QCD colored particles. (e.g. squarks, gluions,..) -> 100 TeV Collider ?
  - A staged muon collider at  $\sqrt{s}$  up to 6 TeV and integrated luminosity of  $5 \text{ ab}^{-1}$ . Complimentary to a 100 TeV pp collider but also having its own unique discovery and detailed study potential. Particularly strong case for SUSY.
  - Narrow s-channel states played an important role in past lepton colliders. A new element is the possibility of additional scalar higgs-like resonances. If such states exist in the multi-TeV region, they will play a similar role in precision studies for new physics.

– P5 statement on Muon Collider:

- Muon colliders can reach higher energies than  $e^+e^-$  accelerators, but have many technical challenges. Addressing all of the necessary challenges would require a very strong physics motivation based on results from ongoing or future accelerators.

Project/Activity	Scenario A	Scenario B	Senario C	Science Drivers					
				Hi: Higgs	Ne Neutrinos	Da Dark Matter	Co Cosm. Accel.	Th The Unknown	Te: Technique (Frontier)
MAP	N	N	N	✓	✓	✓		✓	E,I

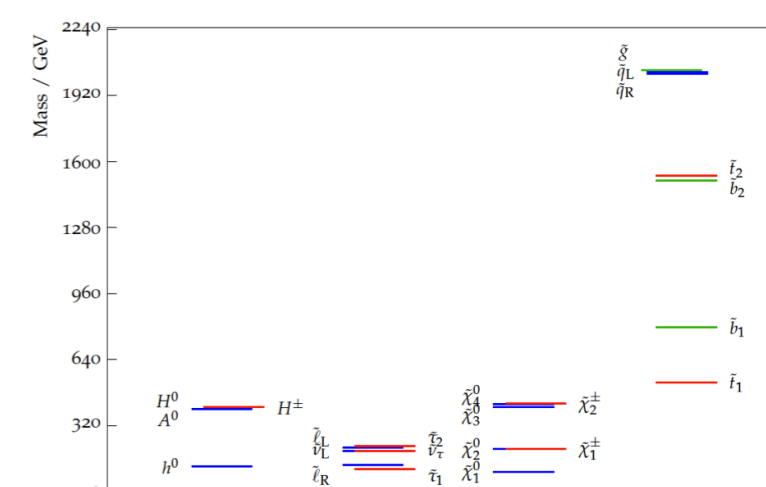
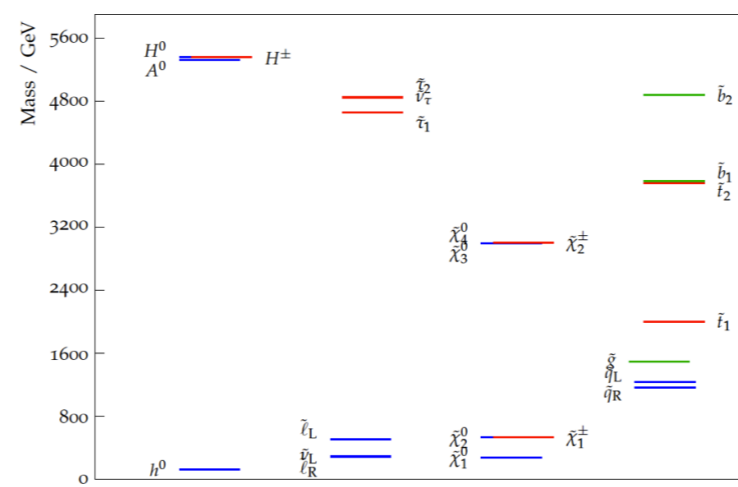
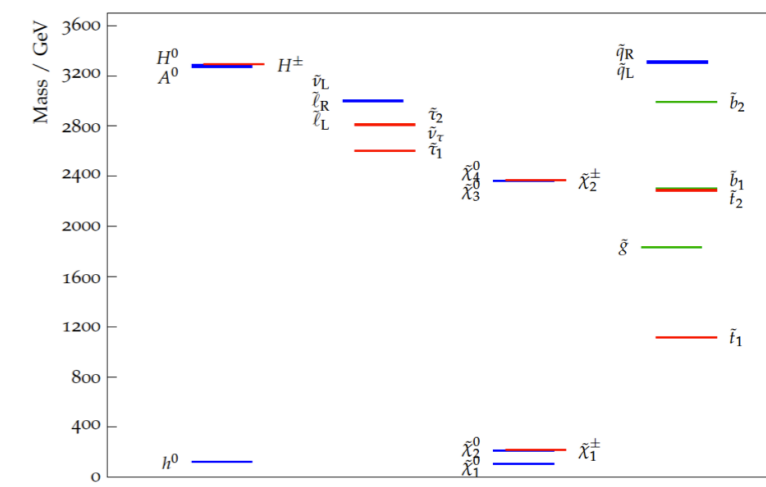
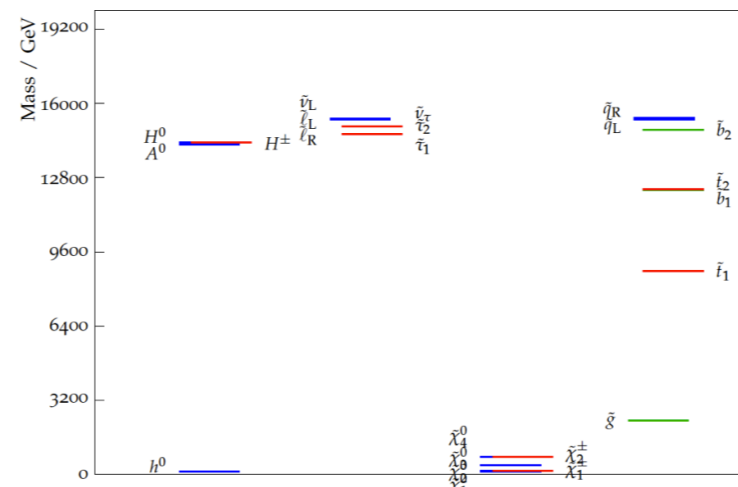
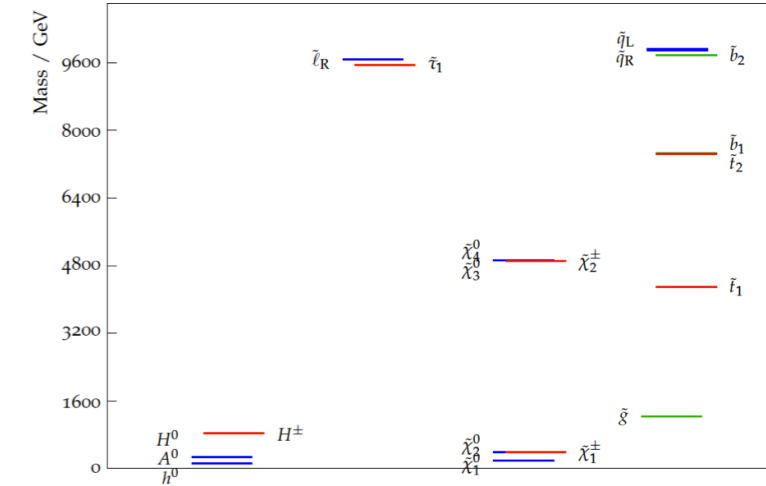
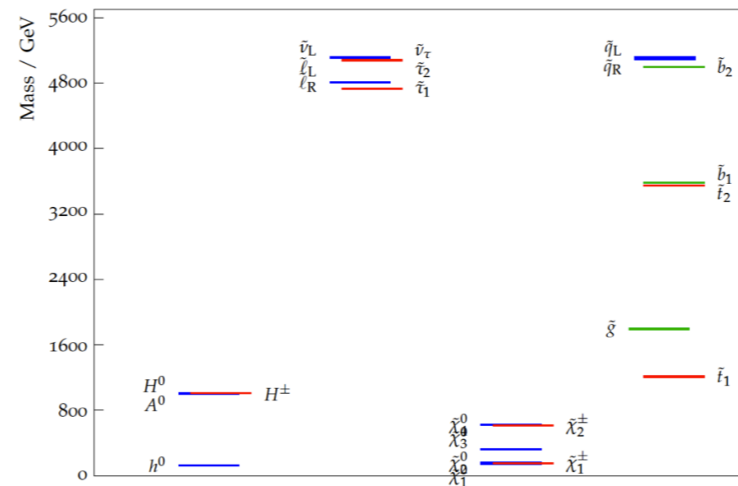
- New physics will provide this clear and compelling case for a Muon Collider with  $E_{cm}$  in the multi-Tev range. This is likely to happen during run 2 of the LHC.
- Many technical challenges need to be met (6D cooling, target design, backgrounds from muon decays, detector design, .. ). We should explore the technology feasibility of a MC and find ways to make it affordable.

BACKUP SLIDES

## Post-LHC7 SUSY Benchmarks for the ILC

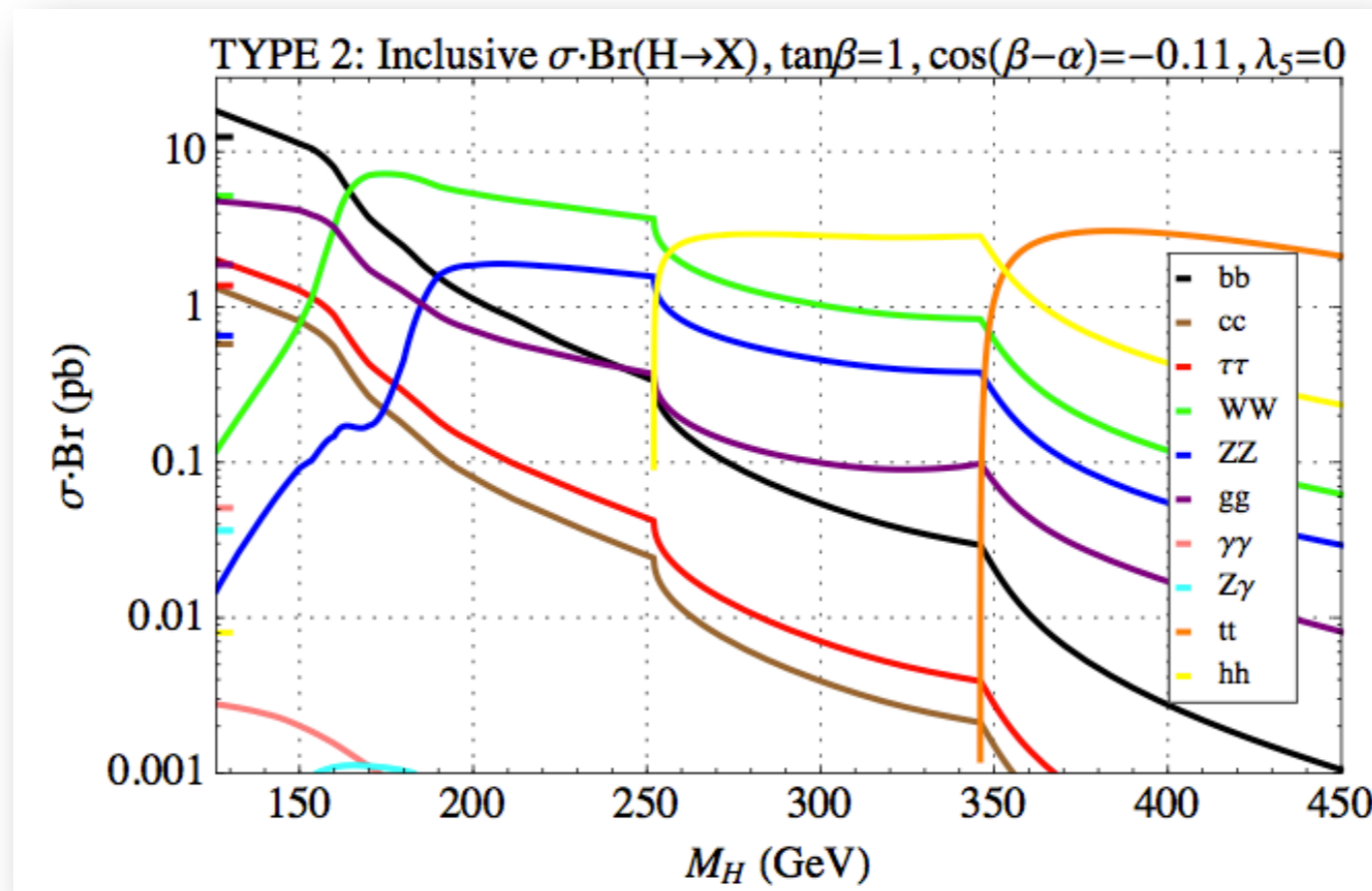
Here we list a couple of interesting SUSY scenarios to study in view of LHC results (status April 2012). See [arxiv:hep-ph/1205.6929](http://arxiv.org/abs/1205.6929) for further information!

- **Natural SUSY:**
  - [SLHA from IsaSugra](#)
  - [IsaSugra native output](#)
  - [full mass spectrum, zoom below 3.6 TeV, zoom below 1 TeV](#)
- **Hidden SUSY:**
  - [SLHA from IsaSugra](#)
  - [IsaSugra native output](#)
  - [full mass spectrum, zoom below 1 TeV](#)
- **Non-universal Higgs Masses (NUHM2):**
  - [SLHA from IsaSugra](#)
  - [IsaSugra native output](#)
  - [full mass spectrum, zoom below 1 TeV](#)
- **mSugra / cMSSM:**
  - [SLHA from IsaSugra](#)
  - [IsaSugra native output](#)
  - [full mass spectrum, zoom below 1 TeV](#)
- **Non-universal Gaugino Masses (NUGM):**
  - [SLHA from IsaSugra](#)
  - [IsaSugra native output](#)
  - [full mass spectrum, zoom below 1 TeV](#)
- **Light Stleptons with stau NLSP, original TDR4 (pMSSM, now excluded by XENON100):**
  - [FeynHiggs 2.8.6 native output](#)
  - [SLHA from SPheno 3.1.4](#)
  - [full mass spectrum, zoom below 1 TeV, zoom below 500 GeV](#)
- **Light Stleptons with stau NLSP, aka TDR4 (pMSSM):**
  - [FeynHiggs 2.8.6 native output](#)
  - [SLHA from SPheno 3.1.4](#)
  - [full mass spectrum, zoom below 1 TeV, zoom below 500 GeV](#)
- **Light Stleptons with stau NLSP, aka TDR5 (pMSSM):**  
 same as TDR4, but with heavier stop1 (about 450 GeV)
  - [FeynHiggs 2.8.6 native output](#)
  - [SLHA from SPheno 3.1.4](#)



Search strategies for the extra scalars in “Alignment without decoupling” could be very different:

Craig, Galloway, Thomas:1305.242



Dominant decay channels are WW, hh and tt, which are very different from the most considered bb and tau tau!

Ian Low's talk at AWLC (5/13/2014)

- The path from the intensity frontier back to the energy frontier has physics at each step.
- A staged Muon Collider can provide a Neutrino Factory to fully disentangle neutrino physics.
- The observation of a new state at 125 GeV by both ATLAS and CMS revitalizes consideration of a Higgs factory as part of a staged multi-Tev muon collider. This is particularly attractive if there is an enlarged scalar sector (eg. THDM, SUSY)
- The unique measurements of the Muon Higgs factory.
  - Most precise measurement of Higgs mass:  $\Delta m_H = 0.06$  MeV; direct Higgs width measurement:  $\Delta \Gamma_H = 0.18$  MeV; measurement of  $BR(\mu^+\mu^-)$   $BR(WW^*)$  to 2% and can separate nearly degenerate scalar resonances.
- A multiTeV lepton collider will be required for full coverage of Terascale physics.
  - The physics potential for a muon collider at  $\sqrt{s}$  up to 6 TeV and integrated luminosity of  $5 \text{ ab}^{-1}$  is outstanding. Particularly strong case for SUSY and new strong dynamics.
  - Narrow s-channel states played an important role in past lepton colliders. The new element now is the possibility of new scalar higgs-like resonances. If such states exist in the multi-TeV region, they will play a similar role in precision studies for new physics.