

# SLAC effort in the collider design

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*MAP 2014 Spring Meeting (27-31 May, 2014), FermiLab USA*

# Outline

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- Introduction
- Choosing of IP beta
- Linear optics
- Chromatic correction
- Beam dynamics properties
- Summary

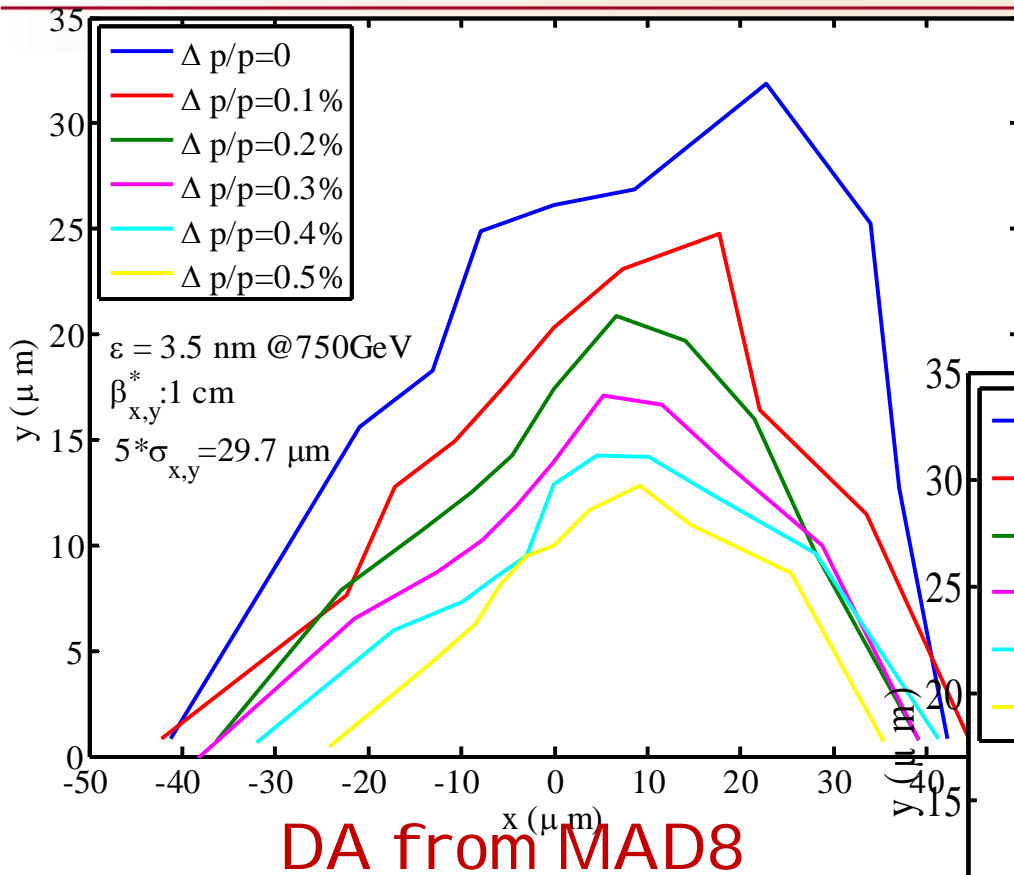
# Introduction

- CMS energy 3 TeV
- High luminosity
- Low  $\beta^*$
- Small circumference
- Sufficient momentum acceptance ( $\sim 1\%$ )
- Sufficient dynamic aperture for a beam with normalized emittance of  $\sim 25 \mu\text{mrad}$
- Absence of long straight to avoid hot spot of neutrino radiation

# Benchmark of 1.5 TeV Muon Collider design

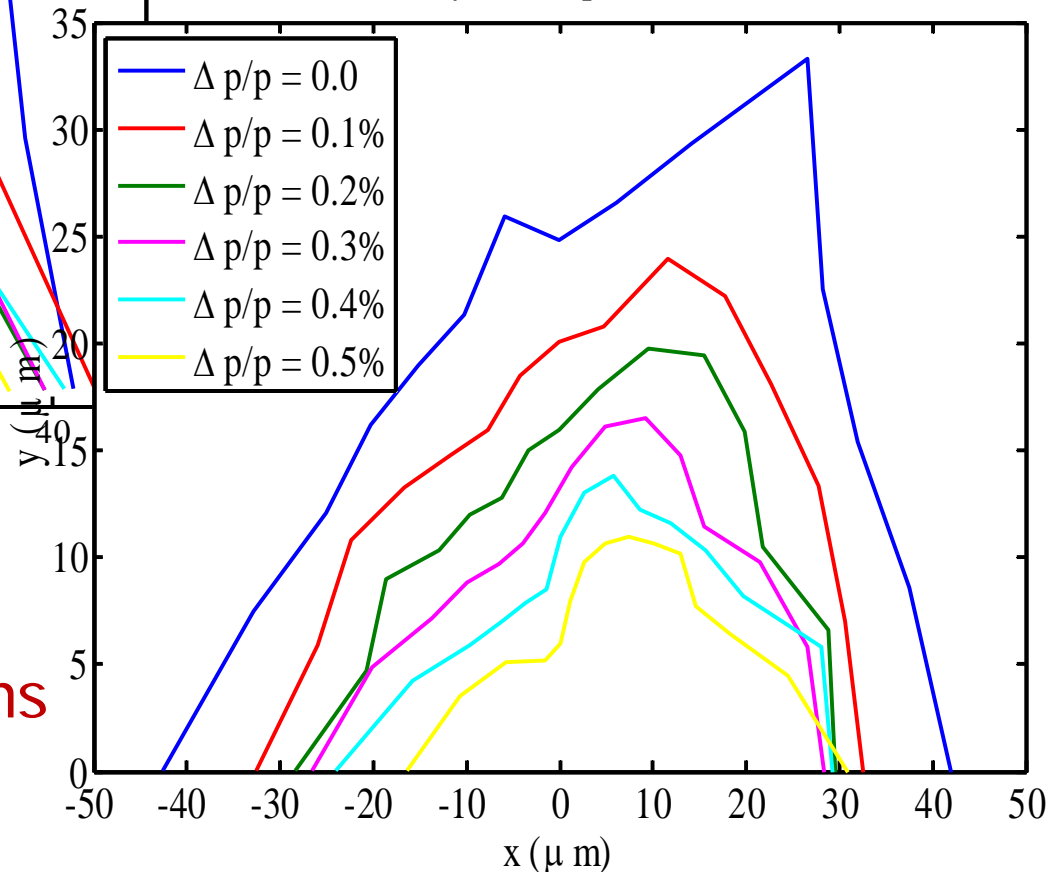
(by Y. Alexahin et al)

SLAC



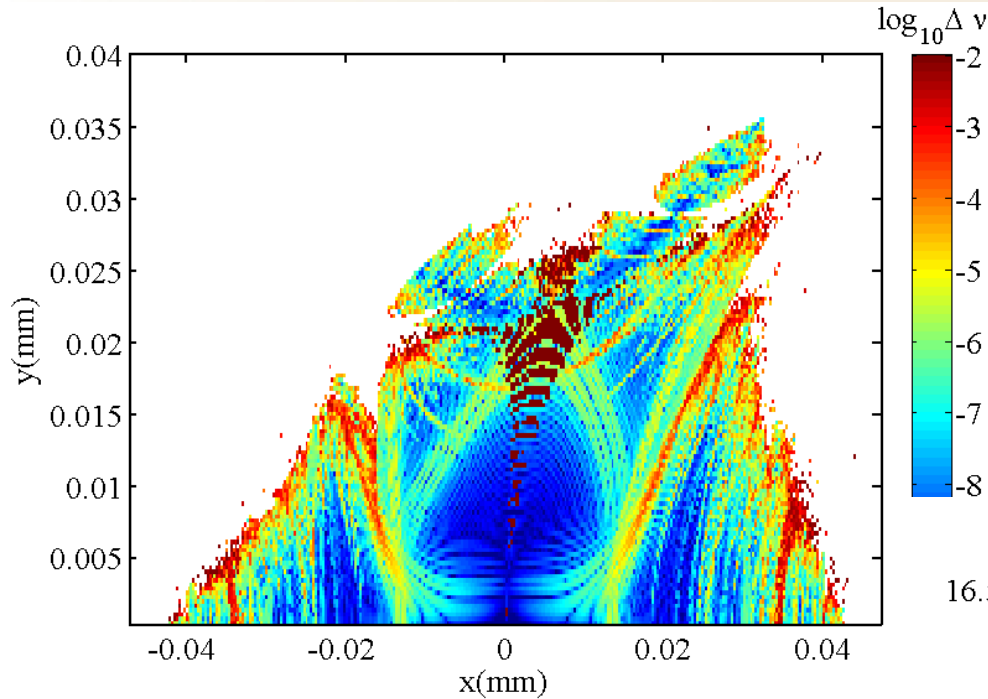
DA from LEGO

Dynamic aperture

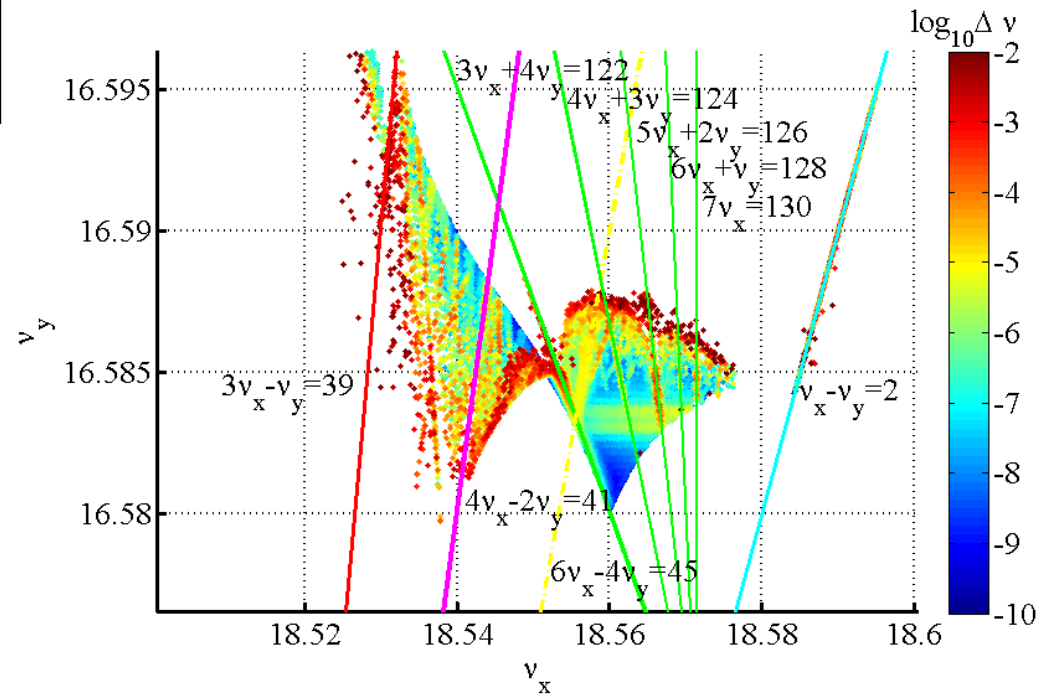


$5\sigma$  in  $X$ ,  $Y$  and  $\delta p$  dimensions

# Frequency Map for the 1.5 TeV design



## Tune footprint



7th order sum resonances

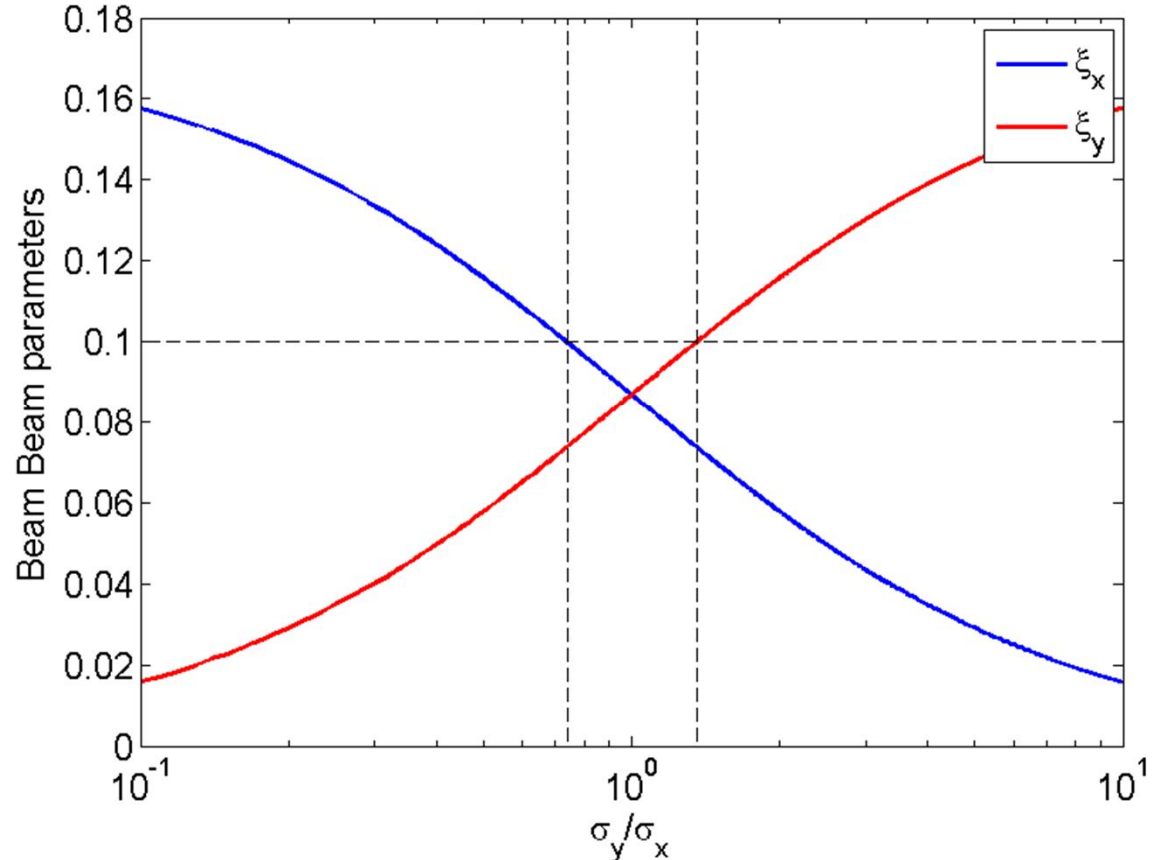
$3\nu_x + 4\nu_y$ ,  $4\nu_x + 3\nu_y$ ,  $5\nu_x + 2\nu_y$ ,  
 $6\nu_x + \nu_y$ , and  $7\nu_x$

Difference resonances

$\nu_x - \nu_y$ ,  $3\nu_x - \nu_y$ ,  $4\nu_x - 2\nu_y$ ,  $6\nu_x - 4\nu_y$

# Beam-Beam parameter versus x&y beam size

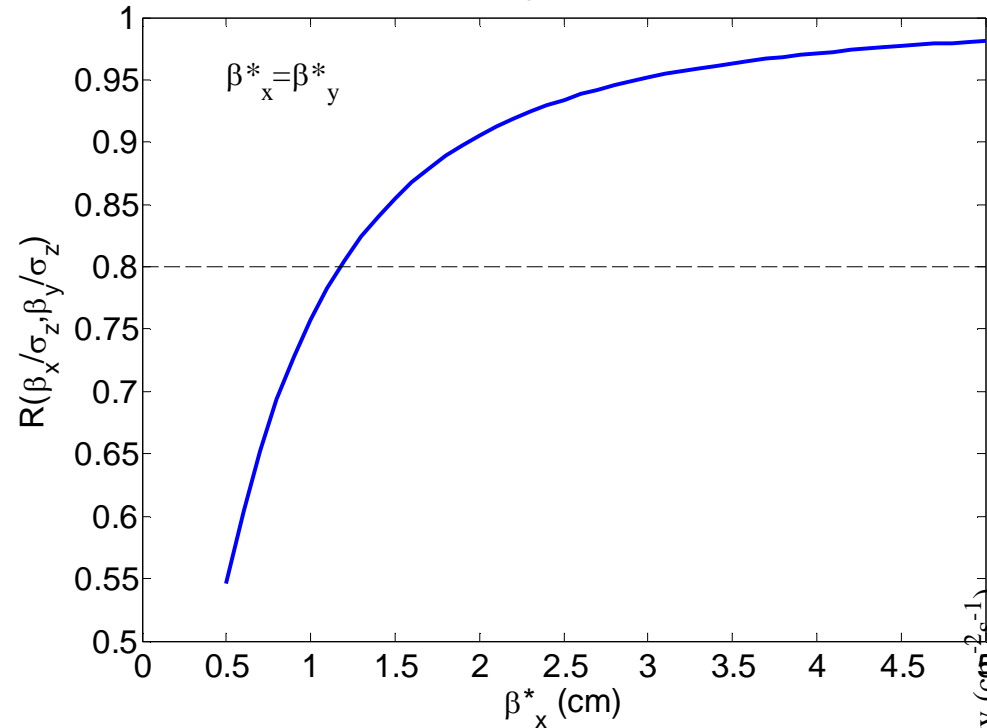
- Muon energy 1.5 TeV
- Normalized rms x & y emittance 25  $\mu\text{m}\cdot\text{rad}$
- Bunch length 1 cm
- Particles per bunch 2e12
- Limit beam-beam parameter at IP to  $\leq 0.1 \rightarrow \sigma_x \approx \sigma_y$



$$\xi_x = r_{muon} N_b / (2\pi \epsilon_{nx} (1 + \frac{\sigma_y}{\sigma_x}))$$
$$\xi_y = \frac{\sigma_y}{\sigma_x} \frac{\epsilon_y}{\epsilon_x} \xi_x$$

# Choosing of IP beta

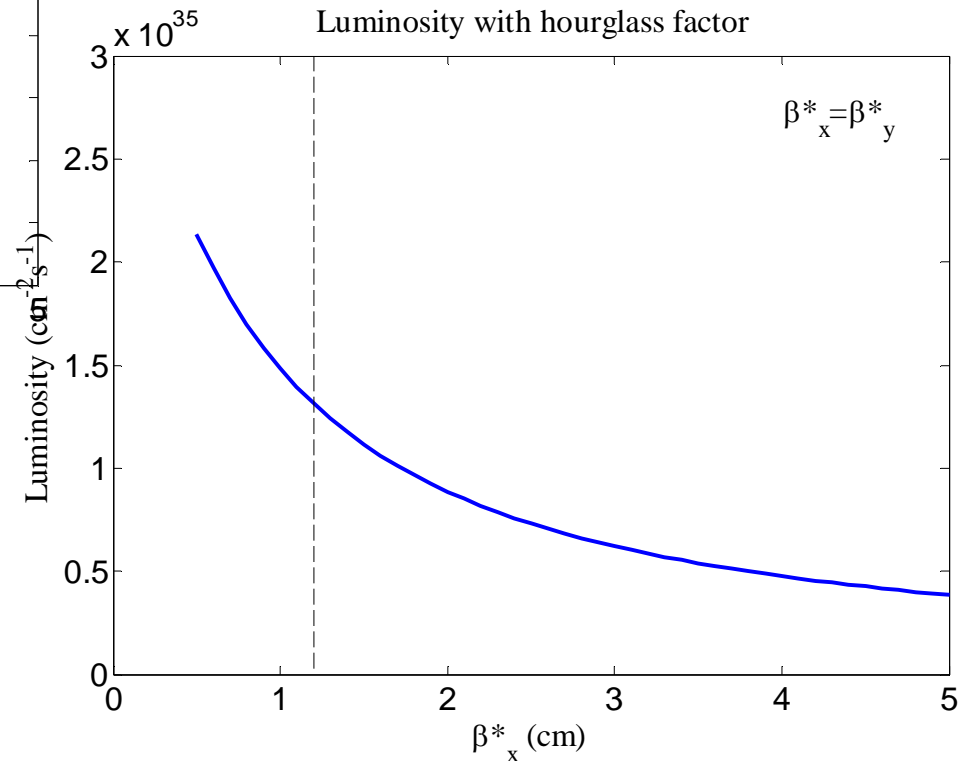
Hourglass factor



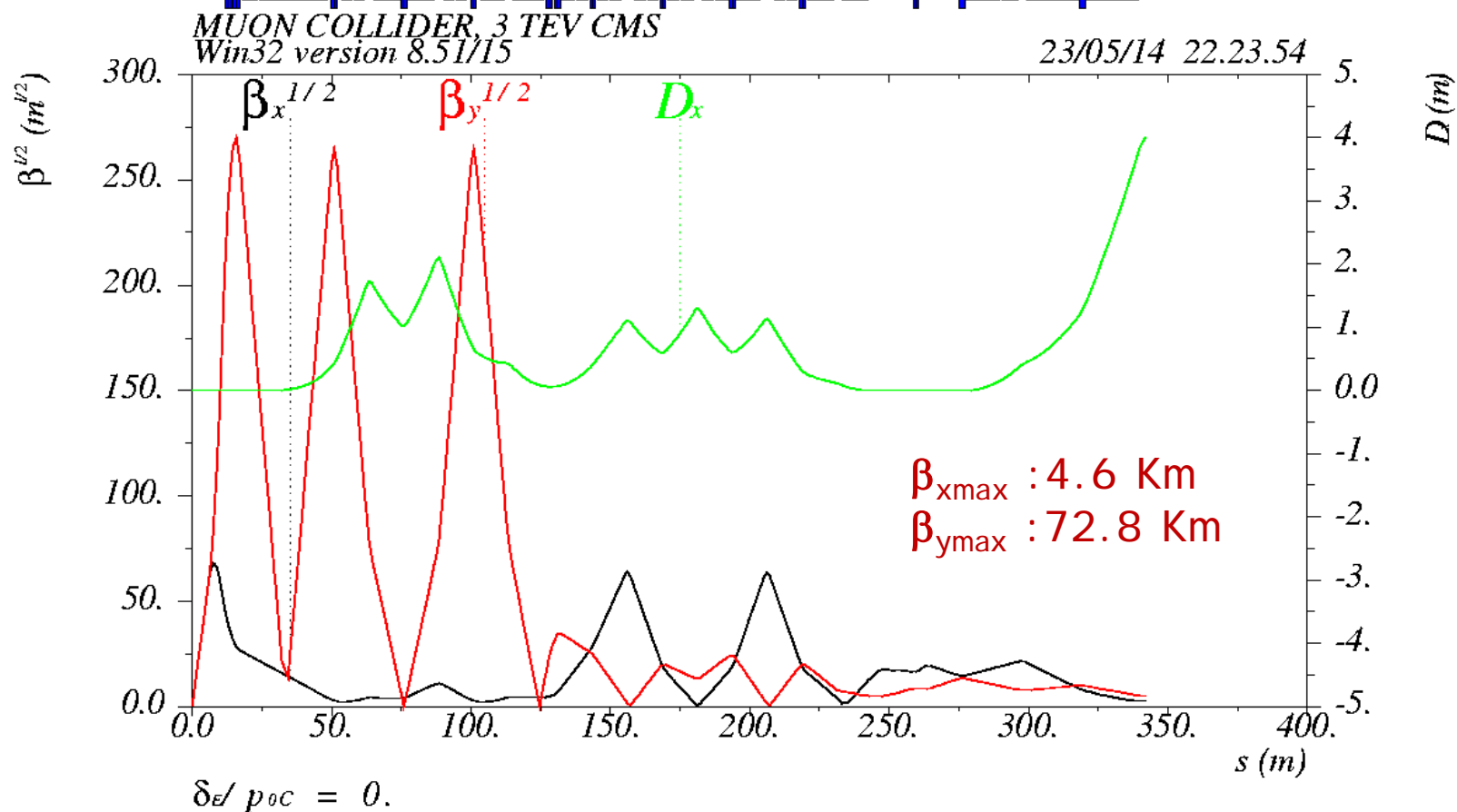
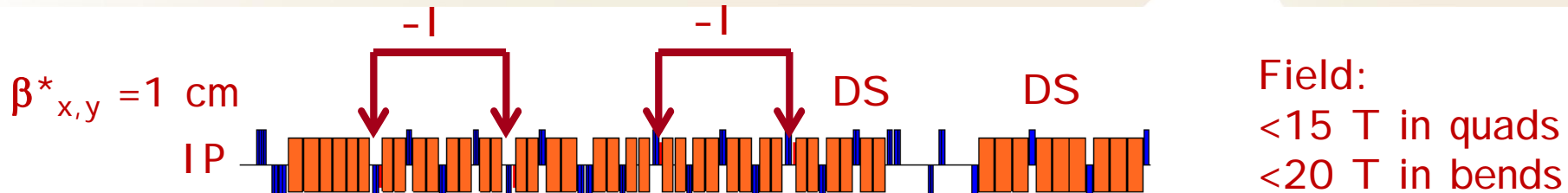
Assume a reasonable  
hourglass factor of  $\geq 0.8$

Choose  $\beta^* = 1 \text{ cm}$   
 $\rightarrow L_{\text{peak}} = 1.5 \cdot 10^{35} \text{ cm}^{-2}\text{s}^{-1}$

Luminosity with hourglass factor

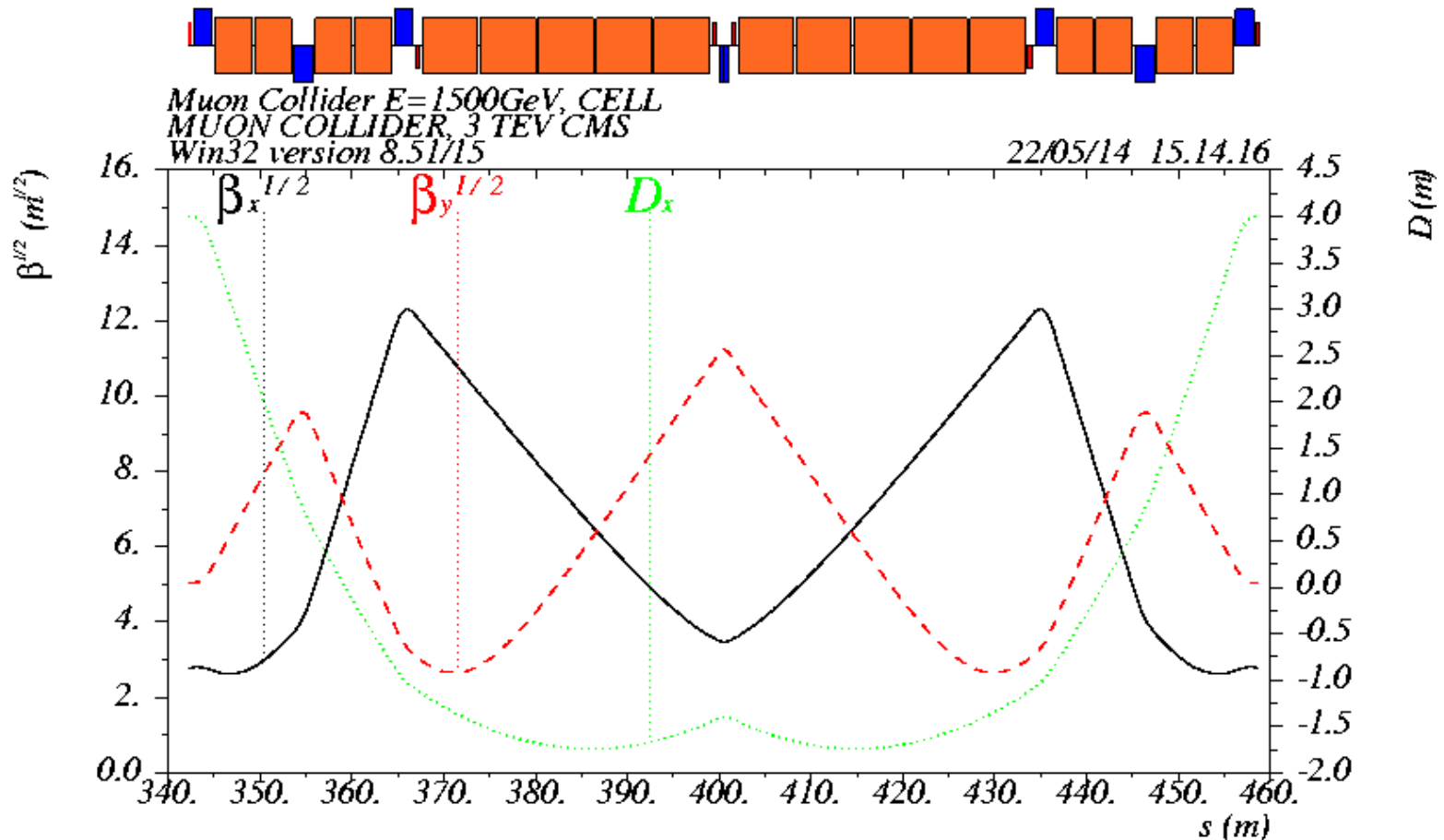


# IR linear optics for 3 TeV design





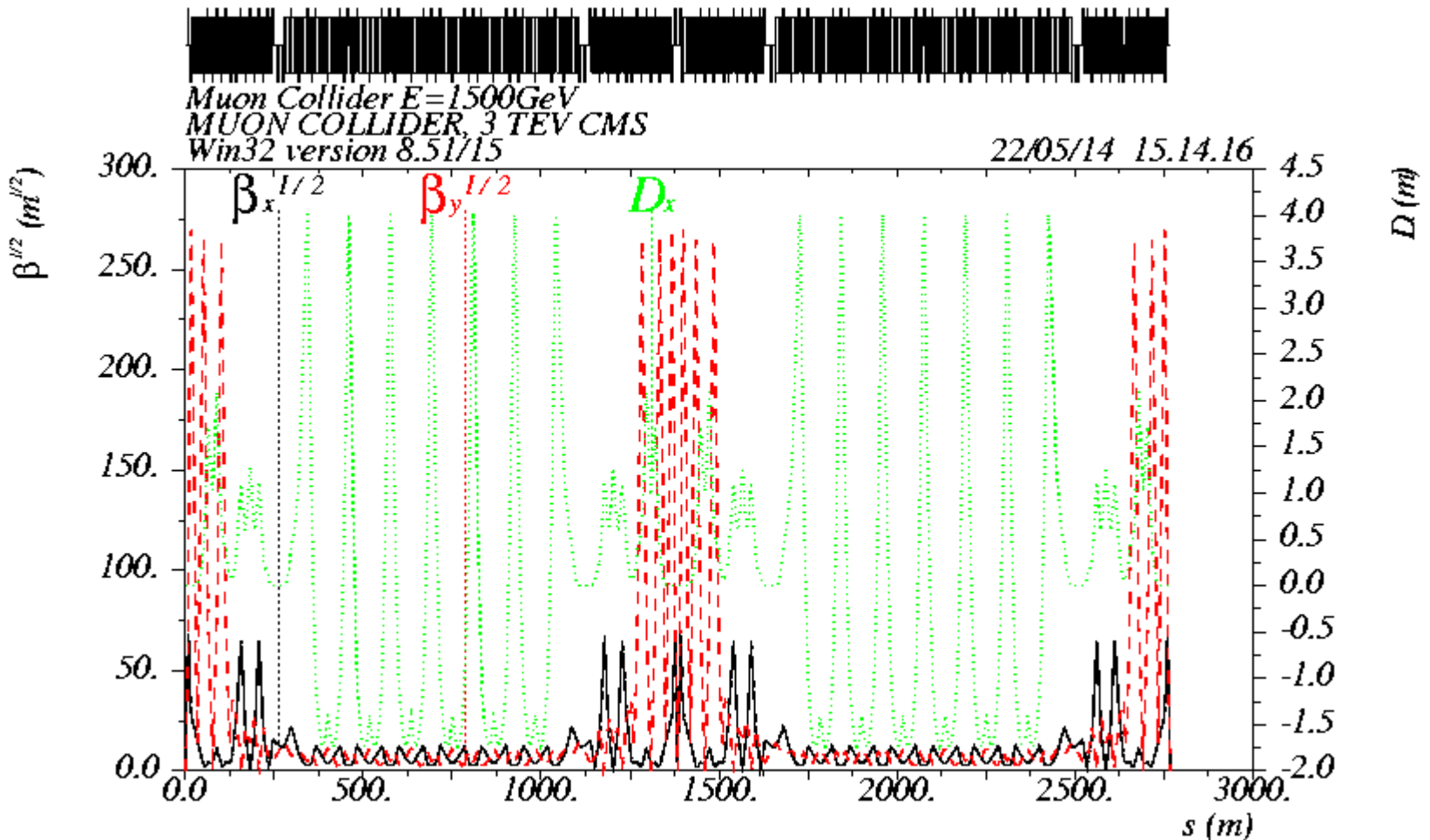
# Arc cell linear optics for 3 TeV



$$\mu_x/\mu_y = 0.833/0.833$$

Based on 1.5 TeV design by Y. Alexahin et al  
Field increased with energy: < 15T in quads, < 20T in bends

# 3 TeV Collider Ring linear optics



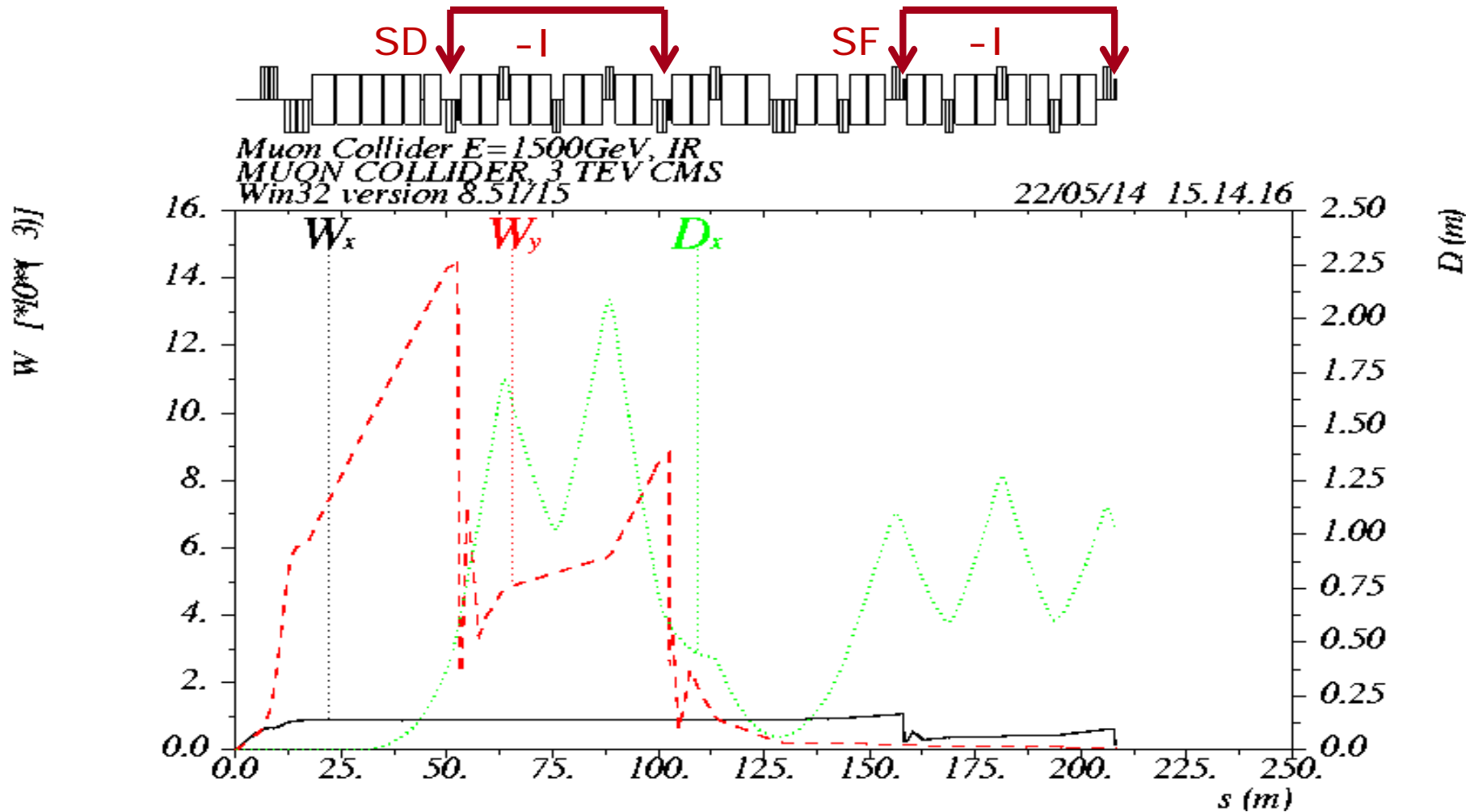
Two IPs twofold symmetry

Circumference: 2.77km;  $v_x/v_y = 20.13/22.22$

# Chromatic correction

- Local correction of chromatic beta beat and higher order chromatic tune shift created by the final focus quads
- Two pairs of  $-1$  x and y correction sextupoles placed  $n\pi$  in x or y phase from the final focus quads
  - large x/y or y/x beta ratio at the IR sextupoles for orthogonal correction
  - cancellation of IR sextupole geometric aberrations
  - no other sextupoles within each IR sextupole pair to minimize octupole-like tune shift with amplitude
- Arc cell design and the arc sextupole correction scheme at this moment are based on 1.5 TeV design (by Y. Alexahin et al)

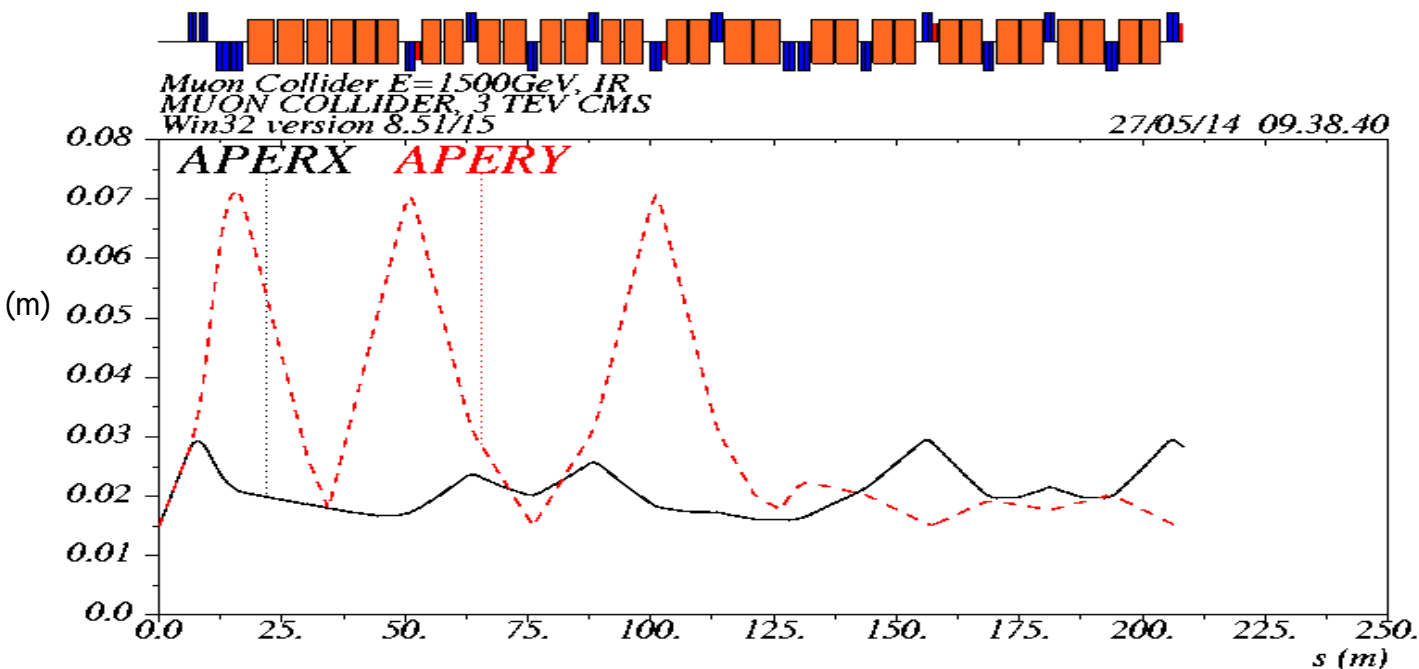
# IR chromatic W-function



IR sextupoles cancel W-function at the IP  
Arc sextupoles correct the tune linear chromaticity

# IR Magnets

magnet	Half-aperture (mm)	Pole tip field (T)	Length (m)
QI R01A	30	14.94	1.6
QI R01B	45	14.94	1.6
QI R02A	75	-14.92	2.45
QI R02B	75	-14.92	2.45
QI R#	50	< 15	2
Dipole	50(66)	< 20	4/4.5/5.5



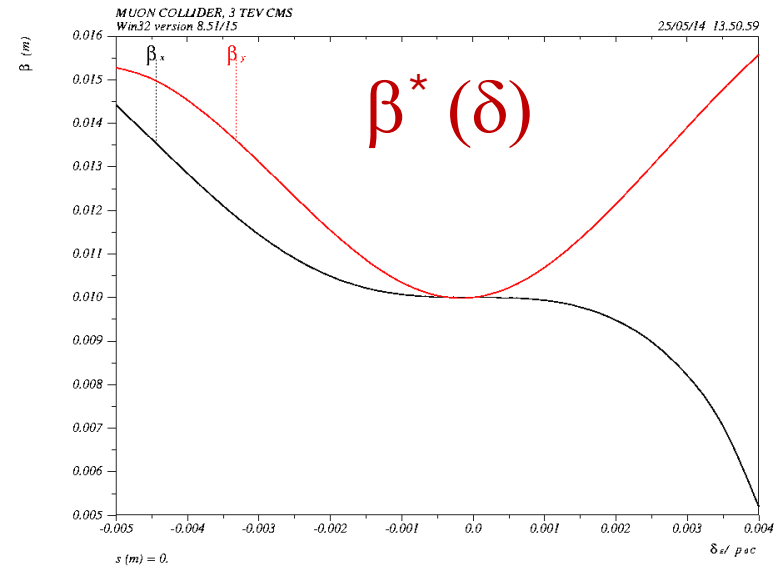
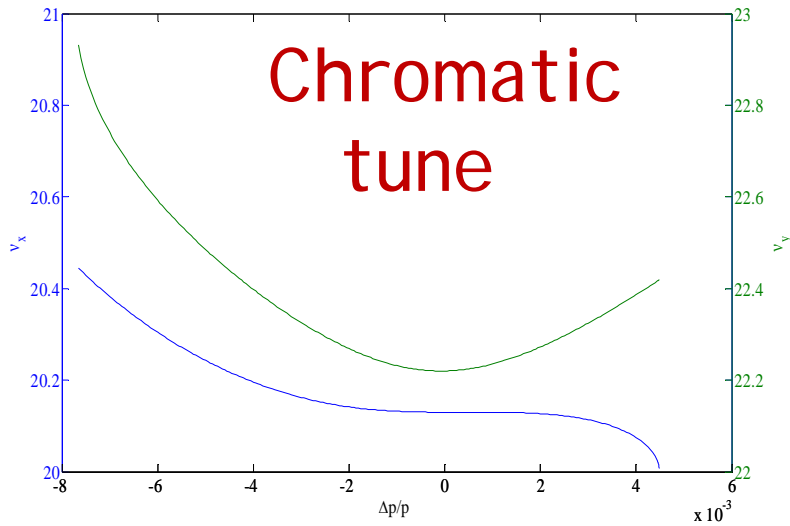
The half aperture calculation in IR is based on the 1.5 TeV design definition:  
 $5\sigma + 15 \text{ mm}$

# Main parameters

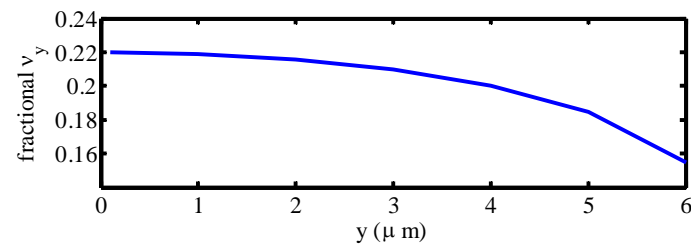
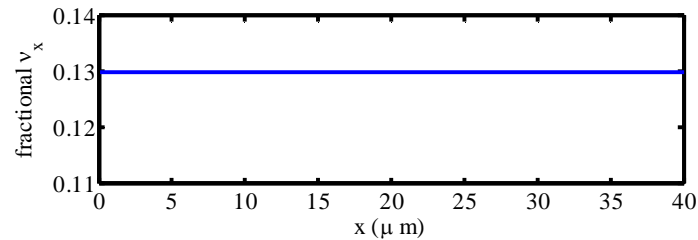
Parameter	Unit	1.5 TeV design	3 TeV design
Beam energy	TeV	0.75	1.5
Number of IPs		2	2
Circumference	m	2730	2767
$\beta^*$	cm	1	1
Tune x/y		18.56/16.58	20.13/22.22 (temporary)
Momentum compaction		-1.30E-05	-2.88E-04
Normalized emittance	( $\pi$ )mm·mrad	25	25
Momentum spread	%	0.1	0.1
Bunch length	cm	1	1
Muons/bunch	$10^{12}$	2	2
Repetition rate	Hz	15	15
Average luminosity	$10^{34}$ cm <sup>-2</sup> s <sup>-1</sup>	1.1	4.5

The average luminosity presented here does not take into account of BB or hourglass factor. The change of luminosity is due to muon beam energy.

# Lattice non-linear properties



## Tune versus amplitude



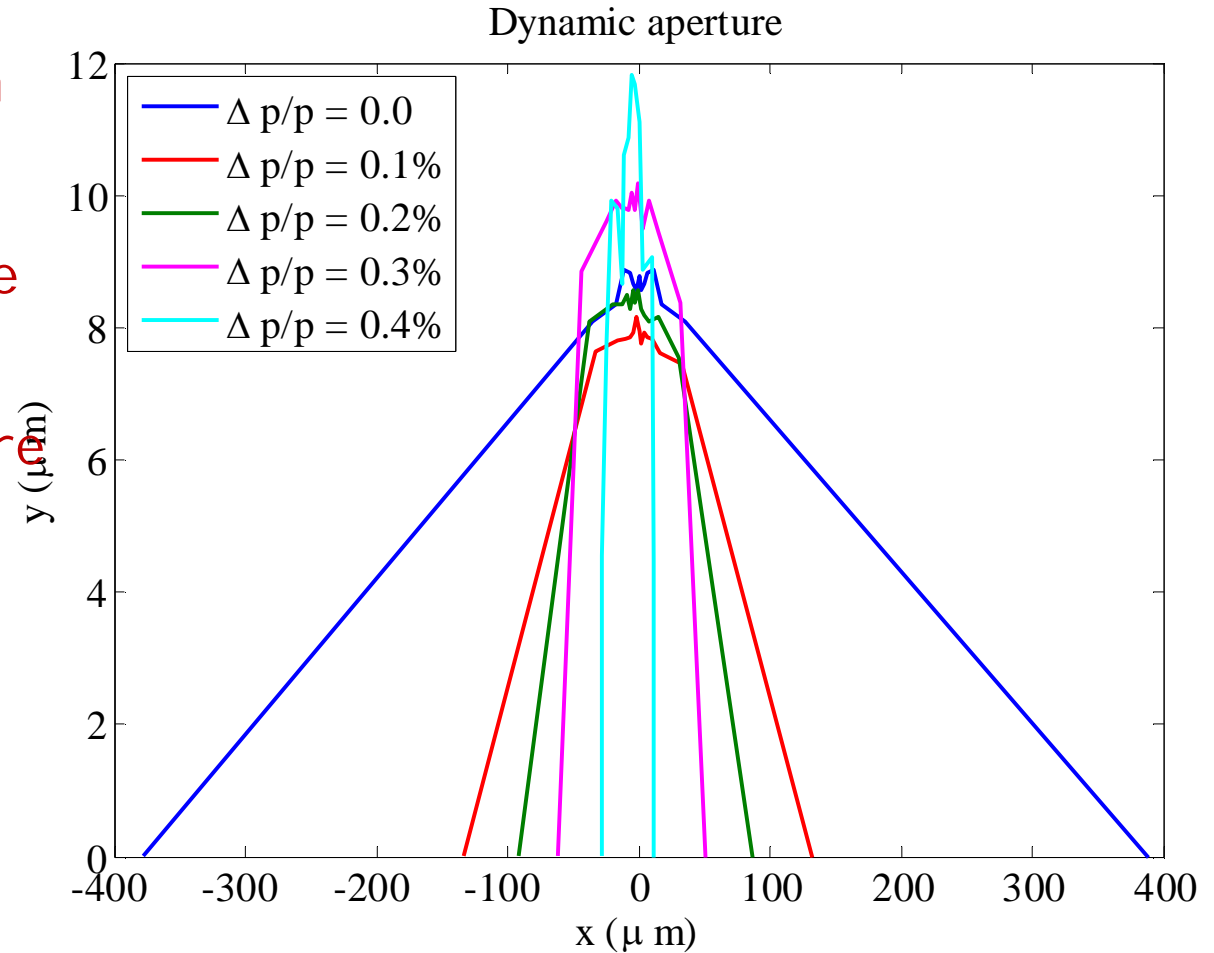
# Dynamic aperture w/o errors

Dynamic aperture from  
LEGO

The on-energy aperture  
is  $\sim 90\sigma_x$  and  $2\sigma_y$

The off-energy aperture  
at 0.4% is  $5\sigma_x$  and  $2\sigma_y$

→ Vertical aperture  
needs to be improved





- A preliminary design of 2.77 km 3TeV CM energy muon collider ring is presented
- The IR chromatic correction scheme uses -1 non-interleaved pairs of sextupoles
- On-energy dynamic aperture currently is 90 sigma in x-plane and 2 sigma in y-plane
- Several improvements are being considered:
  - Improve IR nonlinear chromatic correction scheme
  - Investigate a new design of the arc cell
  - Adjust betatron tune to a more reasonable value above half integer

# Reference

- Y. I. Alexahin et al., “Muon collider interaction region design”, PRST-AB 14, 061001 (2011).
- Y. I. Alexahin et al., “A 3-TeV muon collider lattice design”.
- A.V. Zlobin, et al., “Magnet designs for muon collider ring and interactions regions”, proceedings of IPAC'10, Kyoto, Japan.