

# DESIGN AND SIMULATION OF A HIGH FIELD COOLING CHANNEL

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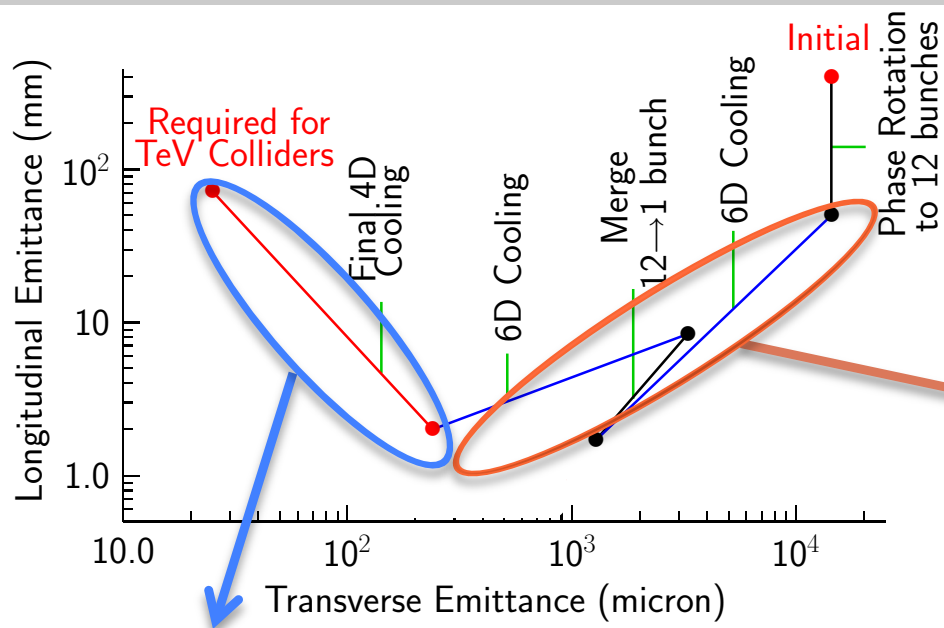
**BROOKHAVEN NATIONAL LABORATORY**



# LAYOUT & INTRODUCTION

- Muon Collider cooling concept
- Final cooling starting point and goals
- High field cooling channel concept
- High field cooling channel design
- Simulation results for 40 – 30 – 25 T cooling channels
- Conclusion + to do list

# MUON COLLIDER COOLING CONCEPT



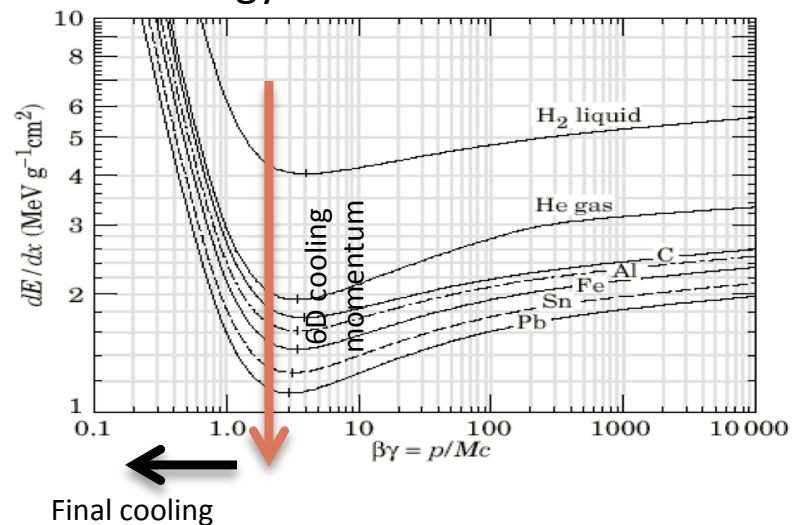
- Muon production
- Muon Capture
- Bunching into 12 microbunches
- Energy phase rotation of microbunches to a common central energy

**6D cooling Channels:**  
Target :  $\epsilon_T = 300 \mu\text{m}$   $\epsilon_L = 1.5 \text{ mm}$

- **High field cooling Channel (40 T solenoids)**
- Target :  $\epsilon_T = 25 \mu\text{m}$   $\epsilon_L = 72 \text{ mm}$

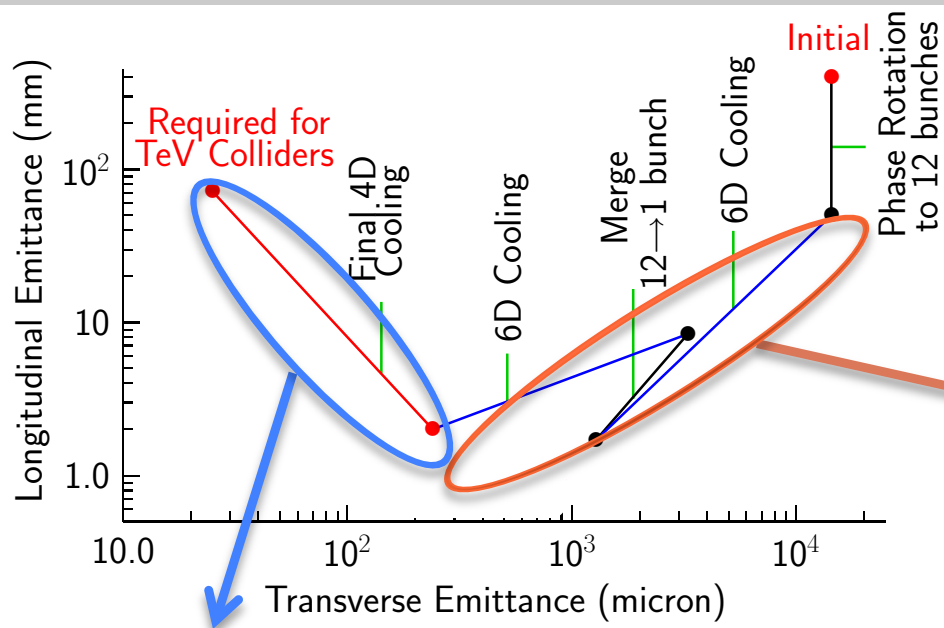
**New regim:**  
High field + Low energy

Energy loss in low z material



$$\epsilon_{equ,N} = \frac{\beta_{\perp} E_s^2}{2\beta mc^2 L_R (dE/ds)}$$

# MUON COLLIDER COOLING CONCEPT



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Reduction of  $\epsilon_T < 300 \mu\text{m}$

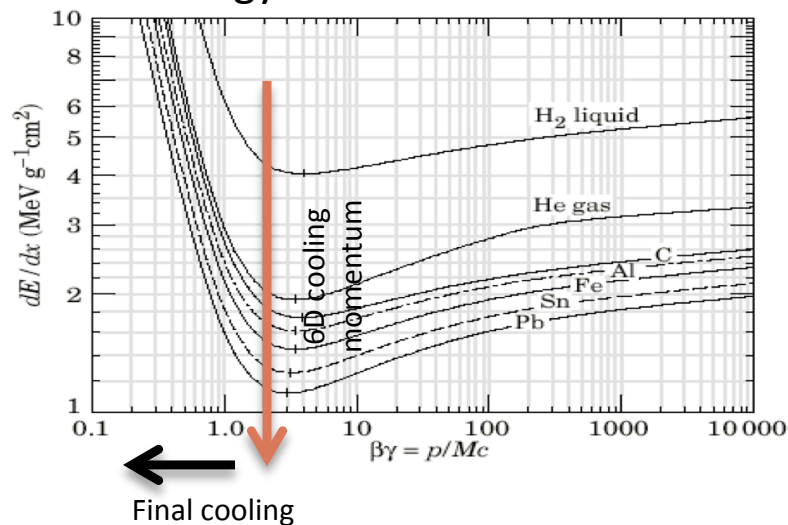
→  $P < 135 \text{ MeV}/c$  + strong focusing 50-25 T

$P < 135 \text{ MeV}/c$  → Positive slope of  $dE/dx$

→ requires small initial  $\epsilon_L$  to

limit the expansion of  $\sigma_E$  &  $\sigma_t$

Energy loss in low z material



$$\epsilon_{equ,N} = \frac{\beta_{\perp} E_s^2}{2\beta mc^2 L_R (dE/ds)}$$

# HIGH FIELD IONIZATION COOLING CONCEPT

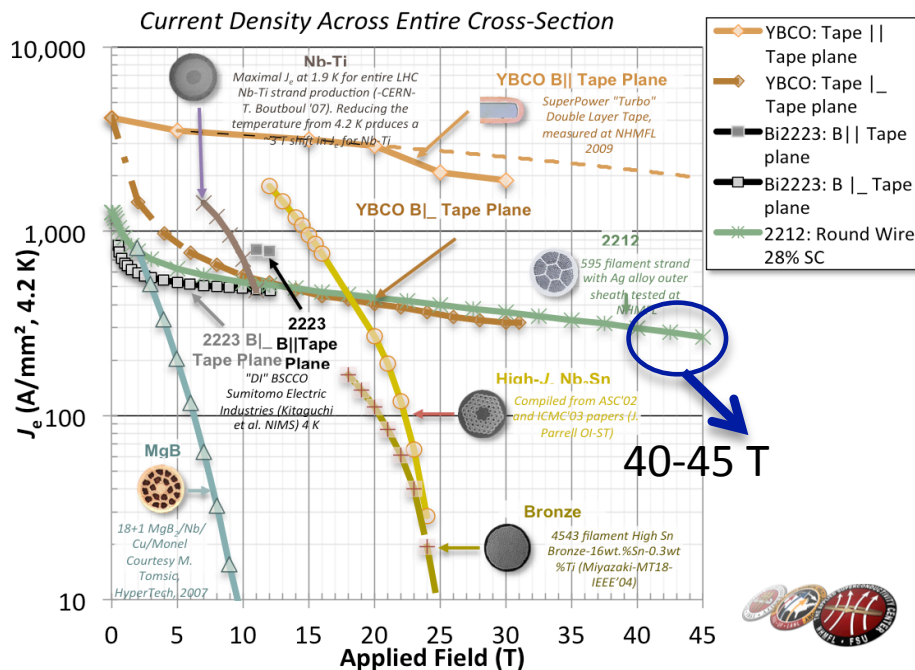
Minimum emittance achievable in a long solenoid field

$$\epsilon_{\perp}(\min) \propto \frac{E}{BL_R(dE/ds)}$$

B magnetic field at absorber location

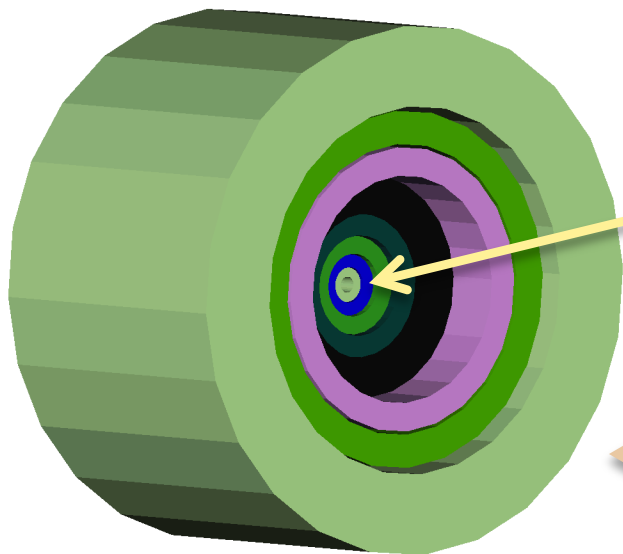
$L_R$  Material radiation length

$dE/ds$  Energy loss in material



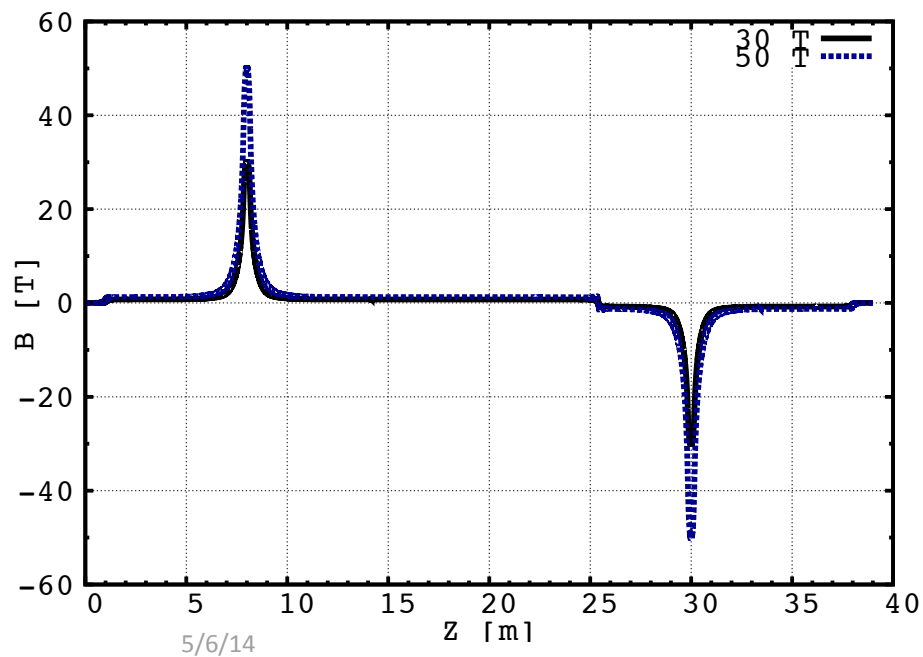
Experimental data from High Magnetic Field Laboratory show the possibility of 40 T fields.

# HIGH FILED 50 T MAGNET



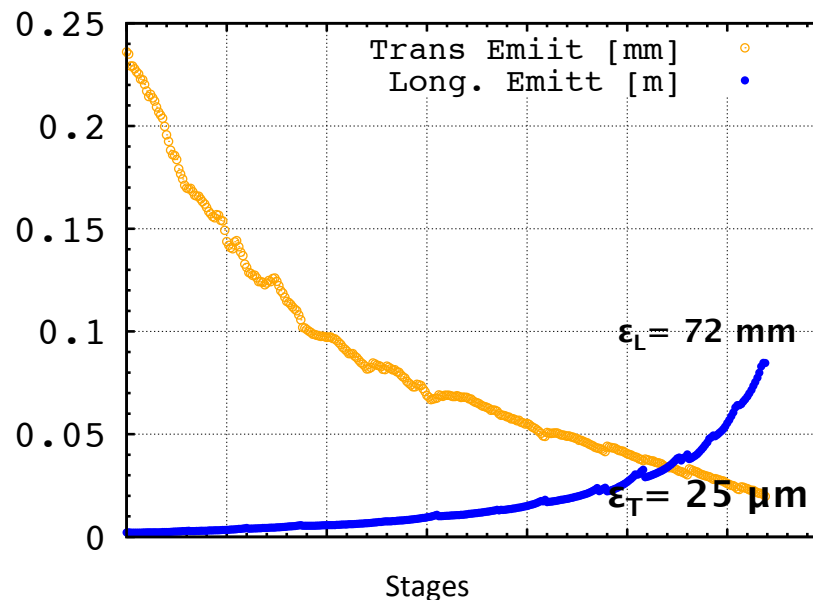
Length [m]	Inner radius [m]	Thickness [m]	I/A [A/mm <sup>2</sup> ]
0.317	0.025	0.029	164.26
0.337	0.055	0.041	142.43
0.375	0.098	0.056	125.88
0.433	0.157	0.067	119.07
0.503	0.228	0.120	85.99
0.869	0.355	0.089	39.60
0.868	0.454	0.104	44.30
0.992	0.575	0.252	38.60

*R. Palmer – B. Weggel*



# HIGH FIELD IONIZATION COOLING CHANNEL DESIGN

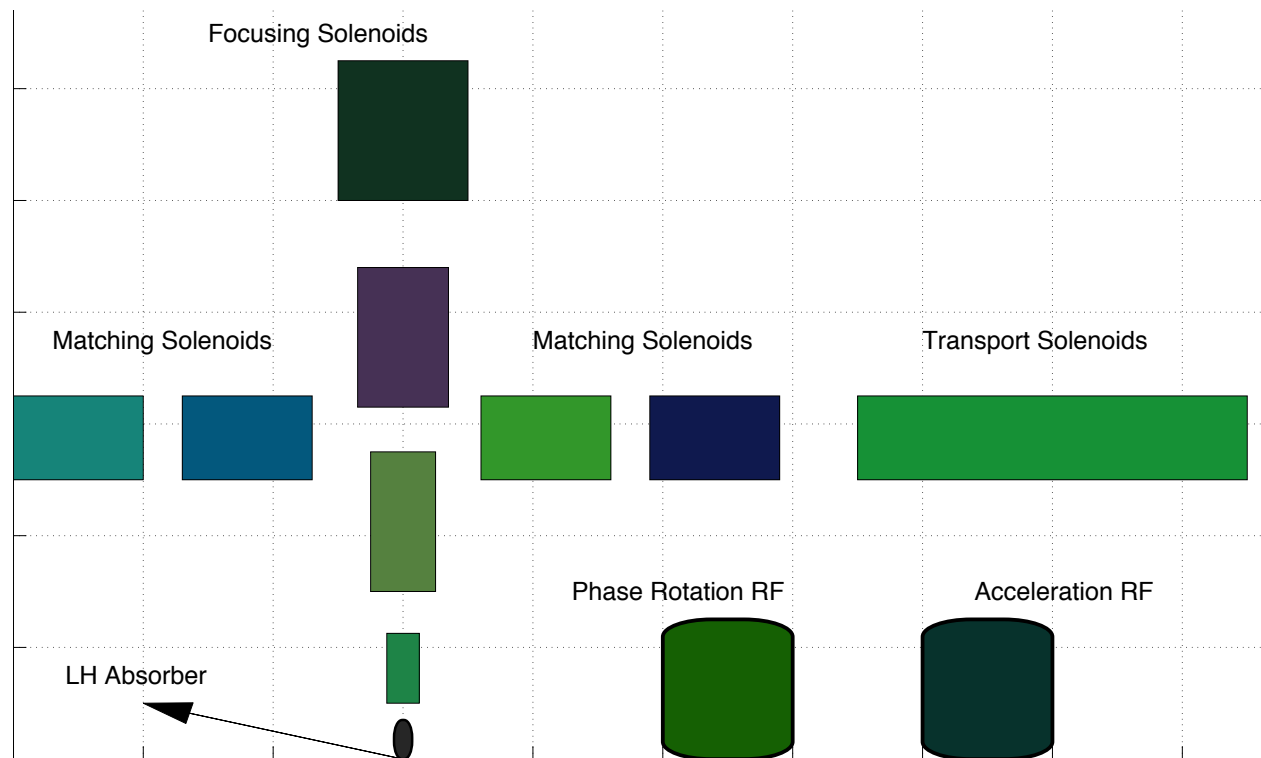
- Cool in the transverse dimensions while the longitudinal emittance grows
- Reduce energy gradually as we progress in the stages
- Reduce absorber length gradually
- Maintain energy spread within acceptable limits



Emittance reduction in absorbers excluding matching and acceleration

# HIGH FIELD IONIZATION COOLING CHANNEL DESIGN

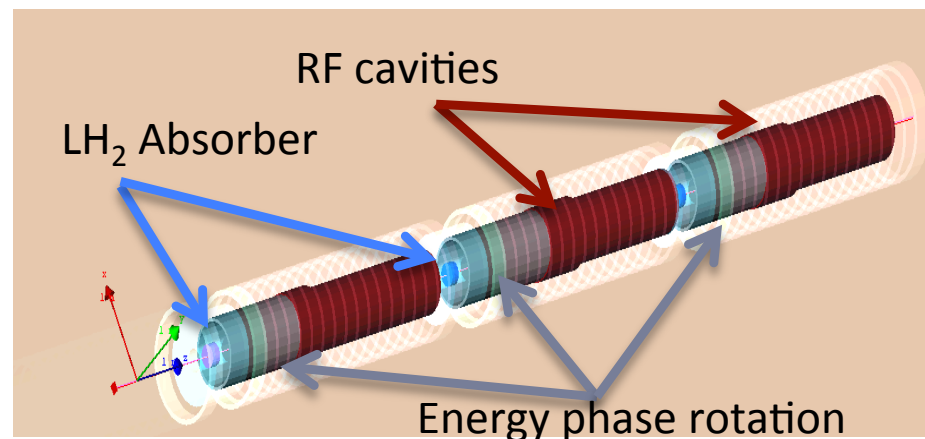
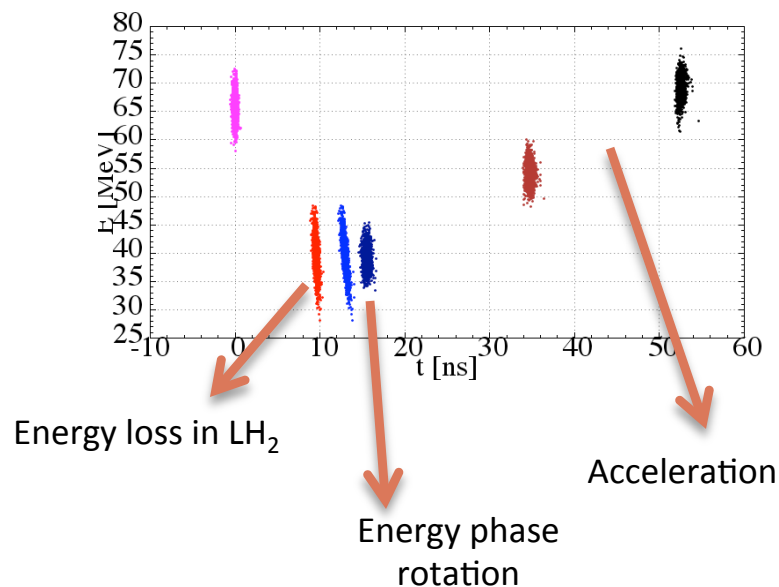
- Cool in the transverse dimensions while the longitudinal emittance grows
- Reduce energy gradually as we progress in the stages
- Anti-symmetric transverse match to and out of the high field solenoids
- Energy phase rotation to maintain low energy spread
  - Increases bunch length
  - Reduce the RF frequencies gradually





# HIGH FIELD COOLING CHANNEL SIMULATIONS

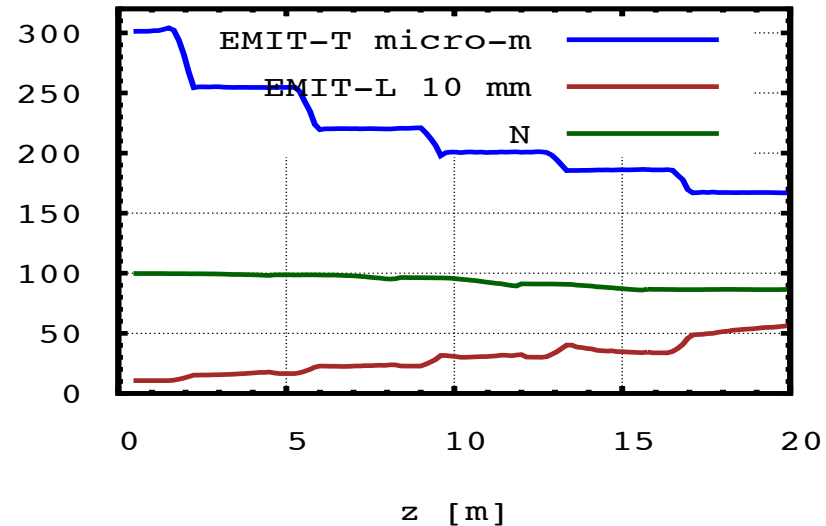
- Muon beam energy falls gradually 70 to 6 MeV
- LH<sub>2</sub> absorber length falls gradually from 65 cm to 12 cm
- Energy phase rotation to maintain the energy spread of the beam
- Bunch rms length rises from 5 cm to 300 cm
- RF cavities frequencies fall from 325 MHz to 4 MHz



# HIGH FIELD COOLING CHANNEL SIMULATIONS

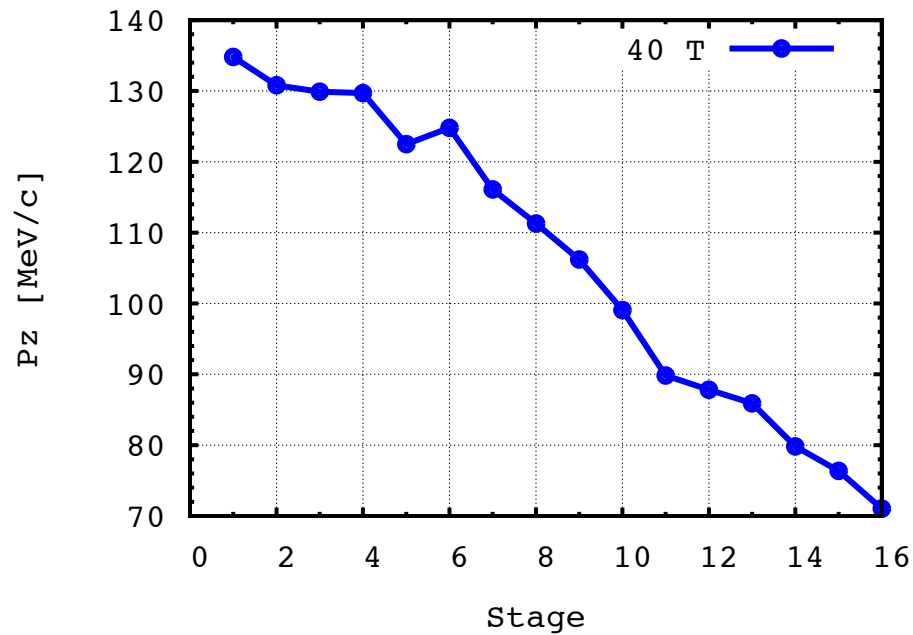
- Muon beam energy falls gradually 70 to 6 MeV
- LH<sub>2</sub> absorber length falls from 65 cm to 1 cm
- Energy phase rotation to maintain the energy spread of the beam
- Bunch rms length rises from 5 cm to 300 cm
- RF cavities frequencies fall from 325 MHz to 10 MHz

- Transverse emittance reduction in 40 T field
- Transverse matching
- Energy phase rotation
- RF acceleration



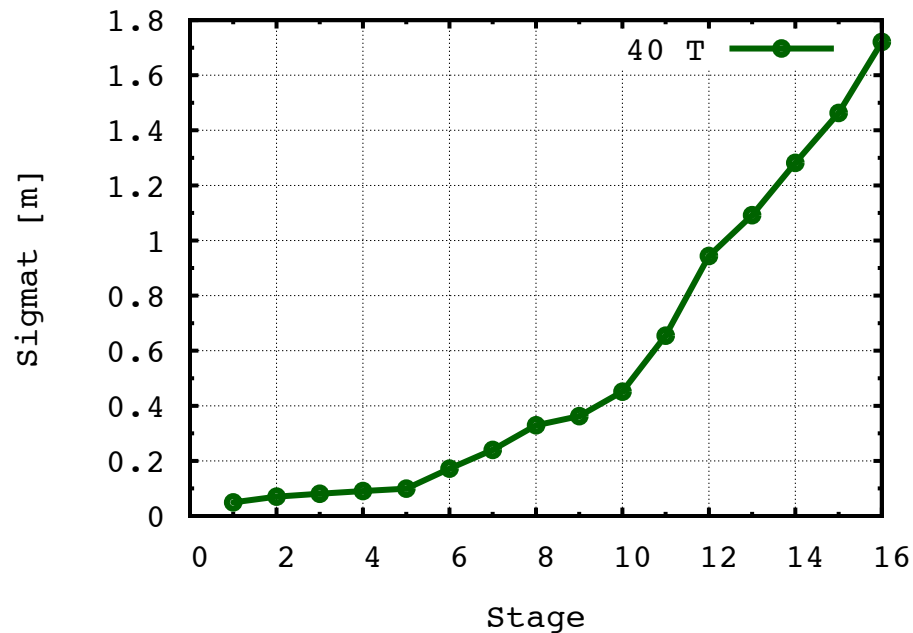
# HIGH FIELD COOLING CONCEPT

- Complete channel using 40 T focusing coils
- 3.0 T transport field between stages
- Drop momentum gradually

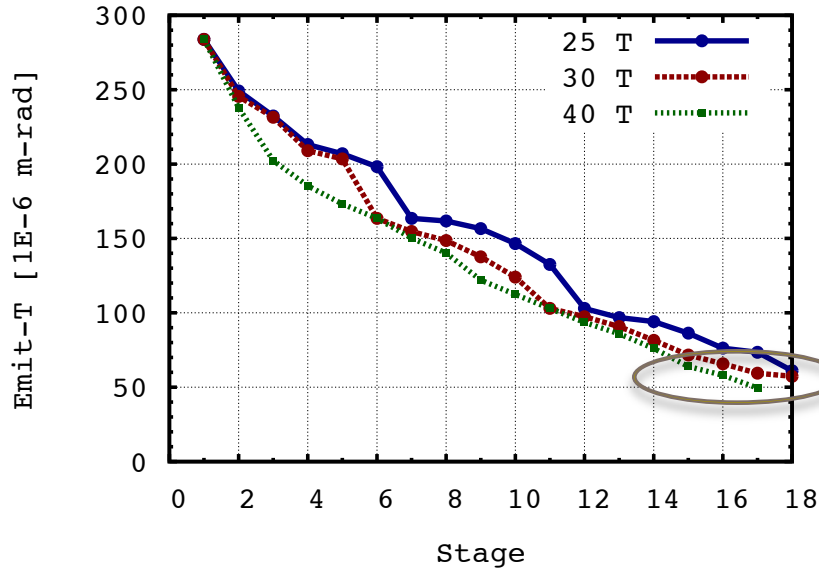


# HIGH FIELD COOLING CONCEPT

- Complete channel using 40 T focusing coils
- 3.0 T transport field between stages
- Bunch length increases after energy phase rotation



# 25 - 30 - 40 T CHANNELS

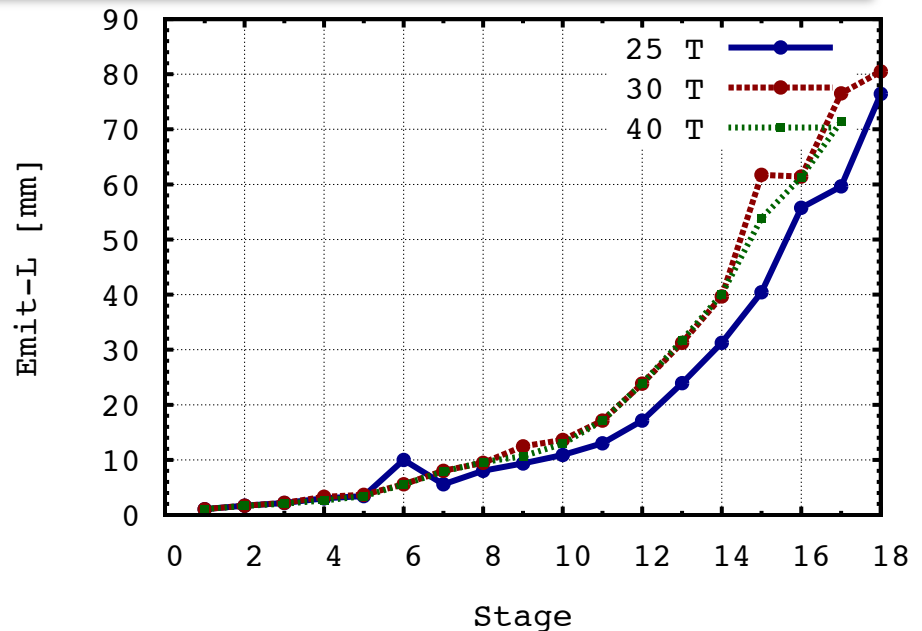


Transverse emittance [ $\mu\text{m}$ ]

B = 25 T can achieve  $60 \mu\text{m}$  without re-optimization  
Equi. Emittance may limit further cooling

Longitudinal emittance [mm]

Transmission is  $\sim 40\%$  in all channels



## CONCLUSION & SUMMARY

- Explore the concept of low energy - high field cooling channel with transverse and longitudinal matching
- A first pass of a complete design and simulation of a high field cooling channel

$$- \rightarrow \varepsilon_T = 50 \mu\text{m} \quad \varepsilon_L \sim > 72 \text{ mm}$$

- To do list
- Optimize the 30-25 T channels – find the lowest achievable emittance ?!
- Optimize the 40 T to achieve the required 25  $\mu\text{m}$
- Improve transmission
- Replace the current sheets with the SC high field magnet