

# Higgs Physics at Future $e^+e^-$ Colliders

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BSM Higgs Workshop @ LPC, Fermilab  
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# Overview of Future $e^+e^-$ Facilities

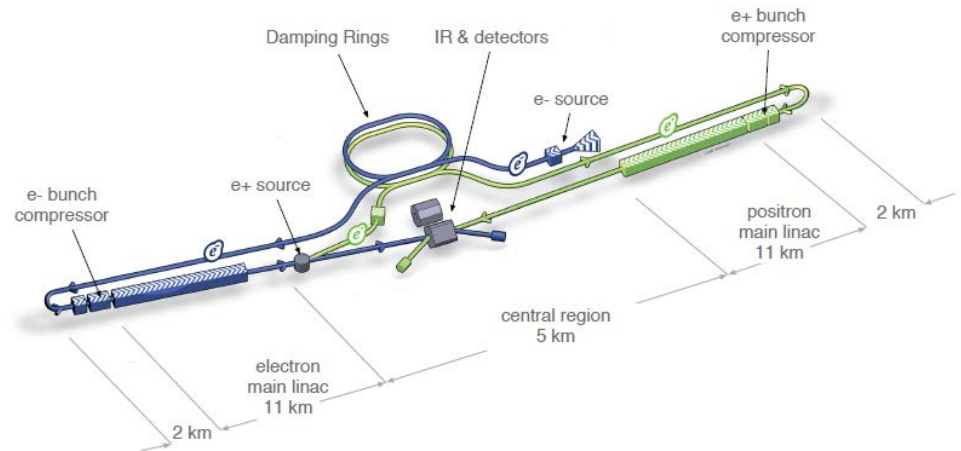
## ILC International Linear Collider

$e^+e^-$  linear collider with SCRF linac

$$250 \leq \sqrt{s} \leq 1000 \text{ GeV}$$

31 km length ( $\sqrt{s} \leq 500 \text{ GeV}$ )

49 km length ( $\sqrt{s} = 1000 \text{ GeV}$ )



## CLIC Compact Linear Collider

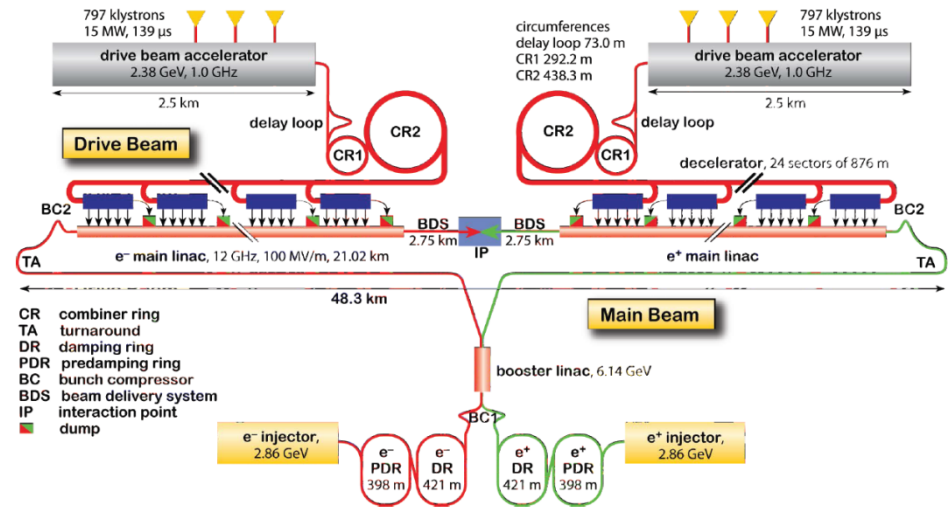
$e^+e^-$  linear collider with X-Band linac

RF powered by a 2nd drive beam

$$350 \leq \sqrt{s} \leq 3000 \text{ GeV}$$

13 km length ( $\sqrt{s} = 500 \text{ GeV}$ )

48 km length ( $\sqrt{s} = 3000 \text{ GeV}$ )



## FCC Future Circular Collider at CERN, 80 -- 100 km circumference tunnel

**FCC-ee** Future Circular Collider,  $e^+e^-$  mode  
(Formerly known as **TLEP**)

$$91 \leq \sqrt{s} \leq 350 \text{ GeV}$$

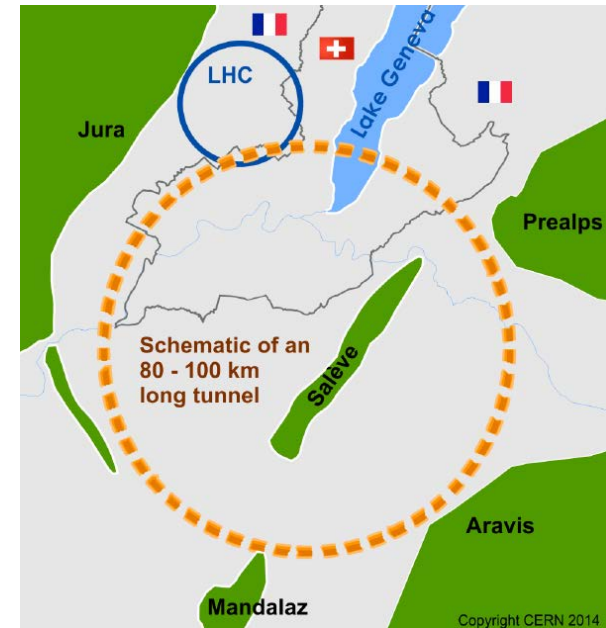
**FCC-he** Future Circular Collider,  $pe^-$  mode

$$3.5 \leq \sqrt{s} \leq 4.9 \text{ TeV}$$

**FCC-hh** Future Circular Collider,  $pp$  mode

Known generically as **VLHC**

$$\sqrt{s} = 100 \text{ TeV}$$



## Circular collider study in China with 50 km circumference tunnel:

**CEPC** Circular Electron Positron Collider

$$\sqrt{s} = 240 \text{ GeV}$$

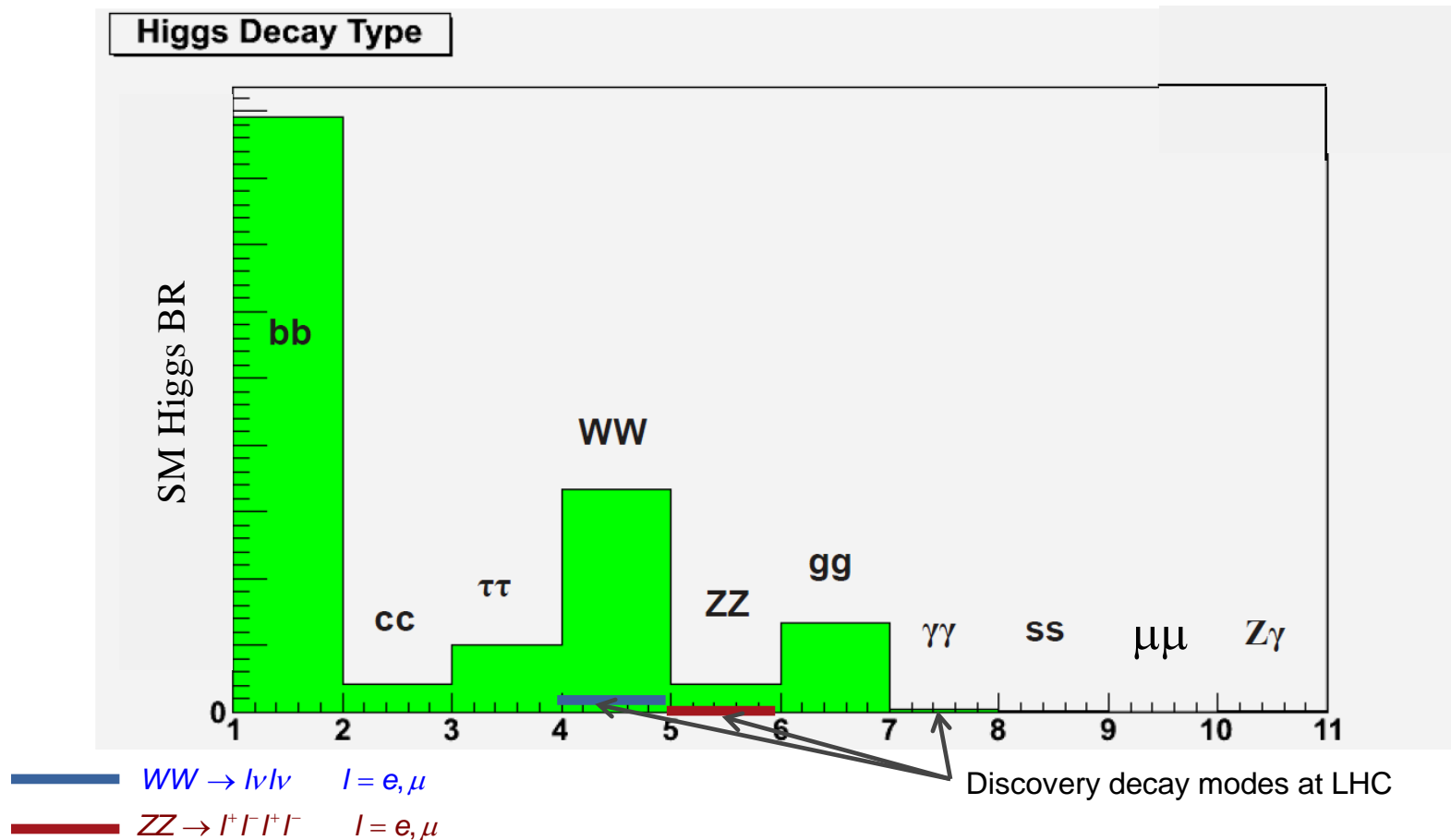
**SppC** Super proton proton Collider

$$50 \text{ TeV} \leq \sqrt{s} \leq 70 \text{ TeV}$$



# Higgs Coupling Measurements at $e^+e^-$ Colliders - Generalities

- All background is electroweak.
- Roughly, the detection efficiency is independent of decay mode  $\Rightarrow \Delta(\sigma \cdot BR) / \sigma \cdot BR \propto 1/\sqrt{BR}$
- The Higgs recoil measurement of  $\sigma(e^+e^- \rightarrow ZH)$  provides model independent measurements of the Higgs BR's and  $\Gamma_{tot}$



Model independent global coupling fit using 32  $\sigma \cdot BR$

measurements  $Y_i$  and  $\sigma_{ZH}$  measurement  $Y_{33}$

$$\chi^2 = \sum_{i=1}^{i=33} \left( \frac{Y_i - Y_i'}{\Delta Y_i} \right)^2,$$

$$Y_i' = F_i \cdot \frac{g_{HZZ}^2 g_{Hb\bar{b}}^2}{\Gamma_0}, \text{ or } Y_i' = F_i \cdot \frac{g_{HWW}^2 g_{Hb\bar{b}}^2}{\Gamma_0}, \text{ or } Y_i' = F_i \cdot \frac{g_{Htt}^2 g_{Hb\bar{b}}^2}{\Gamma_0}$$

$$F_i = S_i G_i \quad \text{where } S_i = \left( \frac{\sigma_{ZH}}{g_Z^2} \right), \left( \frac{\sigma_{\nu\bar{\nu}H}}{g_W^2} \right), \text{ or } \left( \frac{\sigma_{t\bar{t}H}}{g_t^2} \right), \text{ and } G_i = \left( \frac{\Gamma_i}{g_i^2} \right).$$

The cross section calculations  $S_i$  do not involve QCD ISR.

The partial width calculations  $G_i$  do not require quark masses as input.

We believe that the total theory errors for  $S_i$  and  $G_i$  will be at the 0.1% level in 10-15 years.

# Overview of Higgs Physics at $e^+e^-$ Colliders for

$$\sqrt{s} = 250 \text{ GeV} \quad (\text{ILC, FCC-ee, CEPC})$$

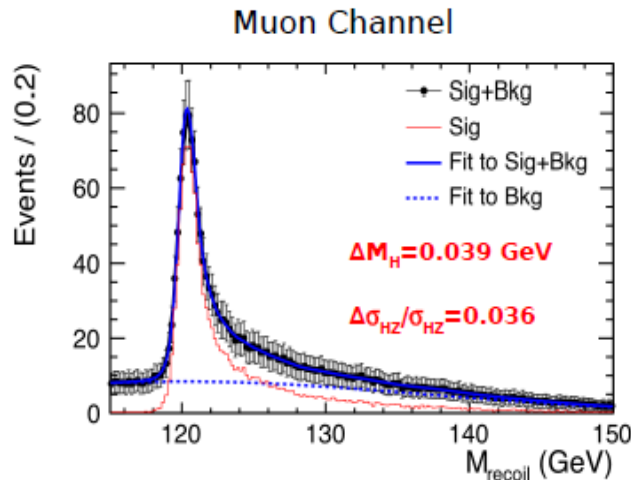
$$\sqrt{s} = 350 \text{ GeV} \quad (\text{ILC, CLIC, FCC-ee})$$

$$\sqrt{s} = 500 \text{ GeV} \quad (\text{ILC, CLIC})$$

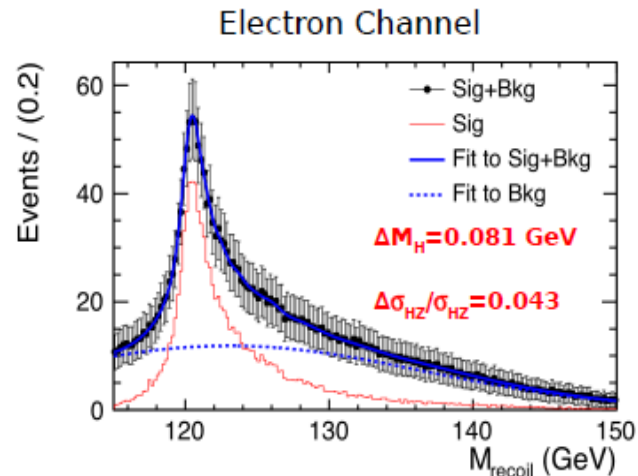
$$\sqrt{s} = 1000 \text{ GeV} \quad (\text{ILC, CLIC})$$

$$\sigma(e^+e^- \rightarrow ZH) \quad \sqrt{s} = 250 \text{ GeV}$$

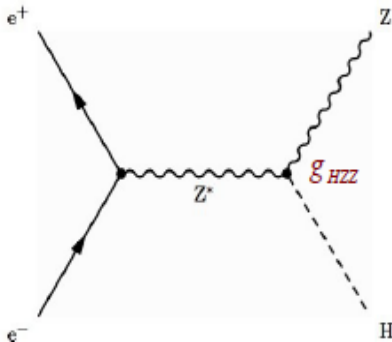
## Higgs Recoil Measurement of Higgs Mass and Higgsstrahlung Cross Section



**Very Precise Measurement**  
**S/B = 8 in Peak Region**



**Less Precise**  
**Bremsstrahlung in detector material**



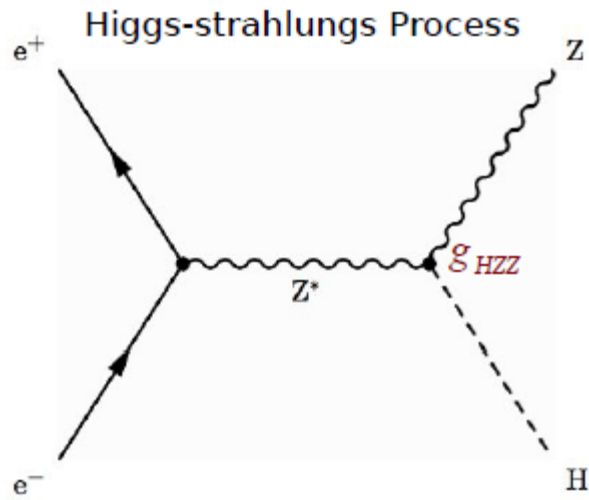
ILC:  $\Delta M_H = .032 \text{ GeV}$ ,  $\Delta \sigma_{HZ} / \sigma_{HZ} = 2.5\%$  for  $L = 250 \text{ fb}^{-1}$

$\Delta M_H = .015 \text{ GeV}$ ,  $\Delta \sigma_{HZ} / \sigma_{HZ} = 1.2\%$  for  $L = 1150 \text{ fb}^{-1}$

$$\sigma_{HZ} \sim g_{HZZ}^2$$

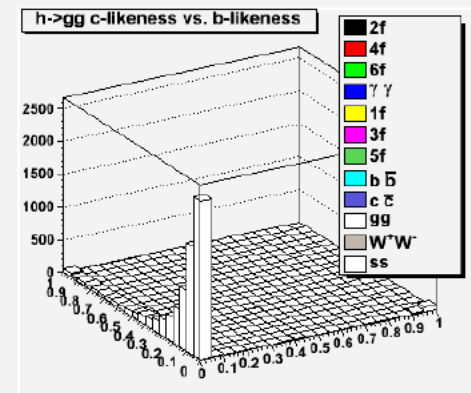
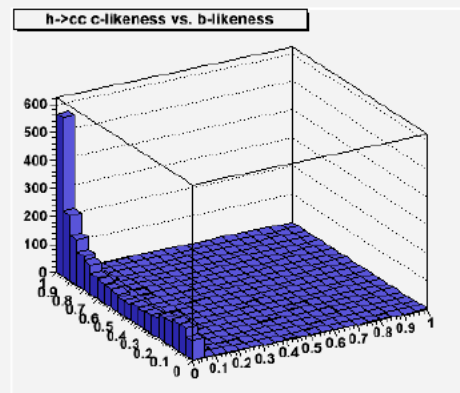
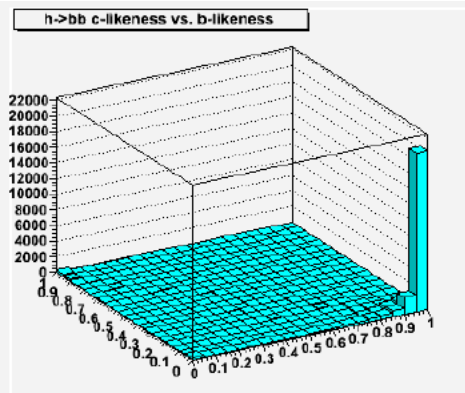
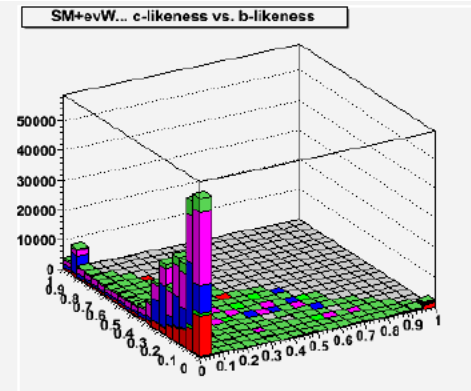
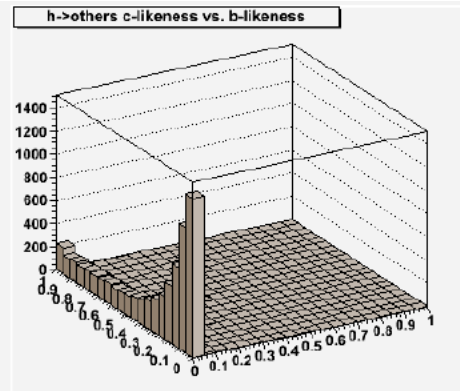
$$\Rightarrow \Delta g_{HZZ} / g_{HZZ} = 1.3\% \text{ (0.6\%)} \text{ for } L = 250 \text{ (1150)} \text{ fb}^{-1}$$

# $\sigma \times \text{BR}$ measurements using $e^+e^- \rightarrow ZH$      $\sqrt{s} = 250 \text{ GeV}$



All Z decays are used for measurement of  $\sigma \times \text{BR}$ . These include  $Z \rightarrow qq$  and  $Z \rightarrow \nu\nu$ .

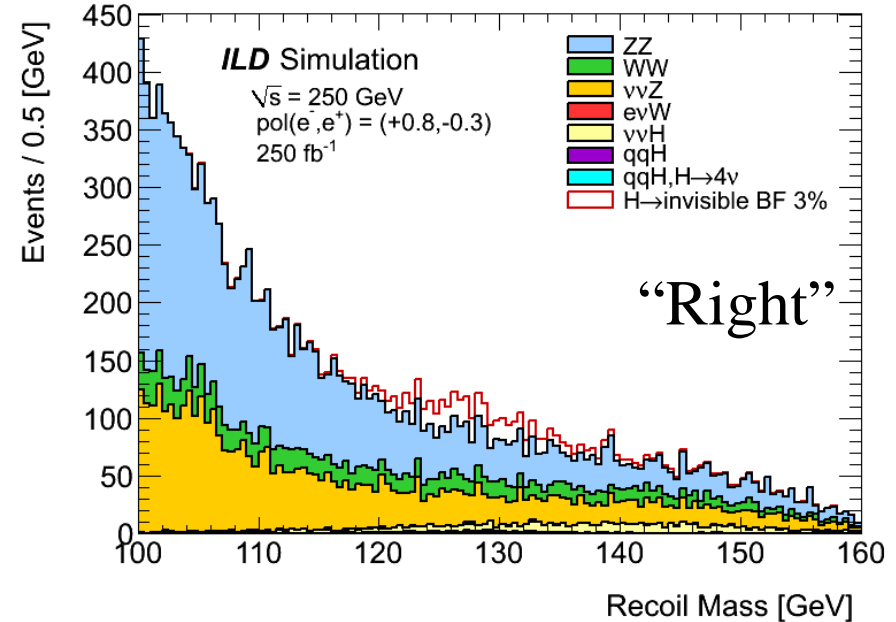
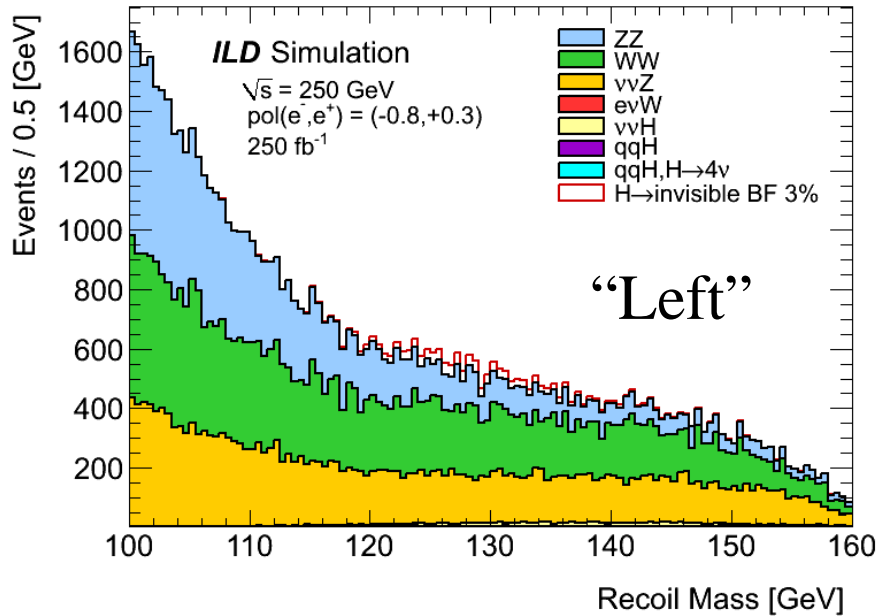
Flavor tagging very important for distinguishing different decay modes



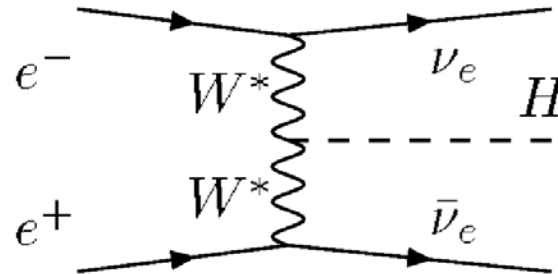
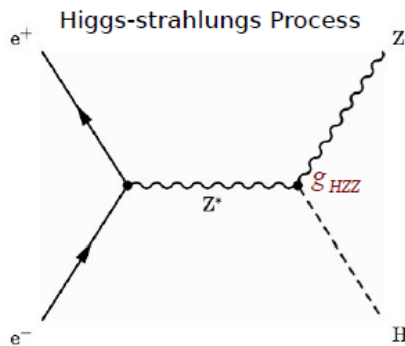


$$e^+e^- \rightarrow ZH, \quad Z \rightarrow qq, \quad H \rightarrow \text{invisible} \quad \sqrt{s} = 250 \text{ GeV}$$

- ▶ If  $\text{BF}(H \rightarrow \text{invisible}) = 3\%$ 
  - Signal is clearly seen for “Right” polarization



$$e^+ e^- \rightarrow ZH, \nu\nu H \quad \sqrt{s} = 350 \text{ GeV}$$

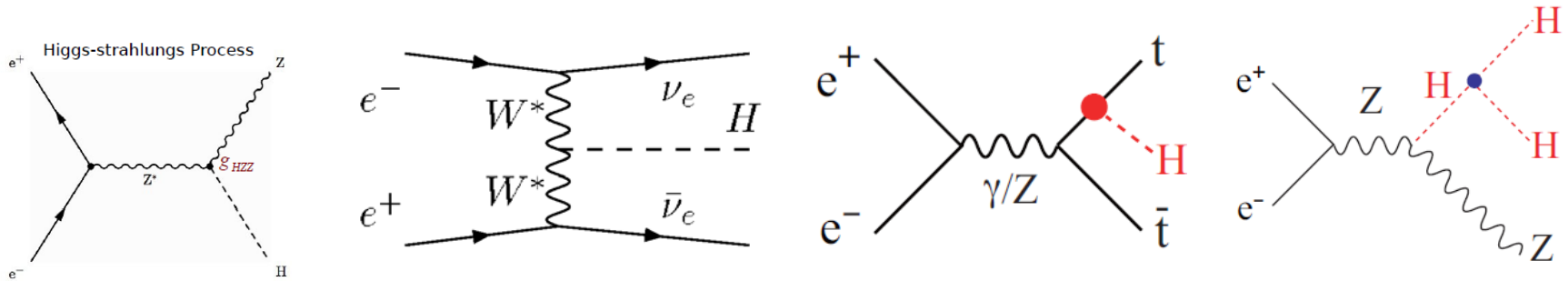


All of the Higgstrahlung studies that were done at  $\sqrt{s} = 250 \text{ GeV}$  can also be done at  $\sqrt{s} = 350 \text{ GeV}$ . Precisions for  $\sigma \cdot BR$  are comparable, as is the precision for  $\sigma(ZH)$  once  $Z \rightarrow q\bar{q}$  decays are included.

$WW$  fusion production of the Higgs at  $\sqrt{s} = 350 \text{ GeV}$  provides a much better measurement of  $g_{HWW}$  compared to  $\sqrt{s} = 250 \text{ GeV}$ . This gives a much improved estimate of the total Higgs width  $\Gamma_H$  which in turn significantly improves the coupling errors obtained from  $\sigma \cdot BR$  measurements made at  $\sqrt{s} = 250 \text{ GeV}$ .

The recoil Higgs mass measurement is significantly worse at  $\sqrt{s} = 350 \text{ GeV}$  with respect to  $\sqrt{s} = 250 \text{ GeV}$ . However, there is hope that direct calorimeter Higgs mass measurements using  $e^+ e^- \rightarrow \nu\nu H$  will recover the precision.

$$e^+ e^- \rightarrow ZH, \nu\nu H, t\bar{t}H, ZHH \quad \sqrt{s} = 500 \text{ GeV}$$



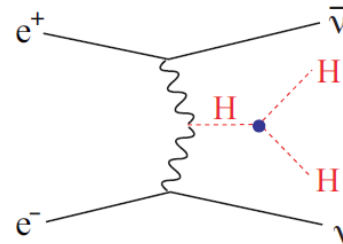
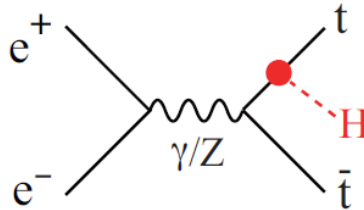
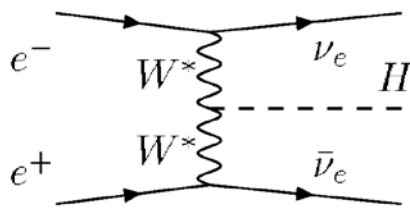
The  $g_{HWW}$  coupling can also be measured well at  $\sqrt{s} = 500 \text{ GeV}$  through  $WW$  fusion production of the Higgs.

Cross section for  $e^+e^- \rightarrow t\bar{t}H$  significantly enhanced near threshold due to  $t\bar{t}$  bound state effects. This leads to a measurement of the top Yukawa coupling  $\Delta y_t / y_t = 14\%$  with  $500 \text{ fb}^{-1}$  at  $\sqrt{s} = 500 \text{ GeV}$ .

The  $ZHH$  channel is open at  $\sqrt{s} = 500 \text{ GeV}$  providing some sensitivity to the Higgs self coupling.

Search for additional Higgs bosons that might have been missed at LHC

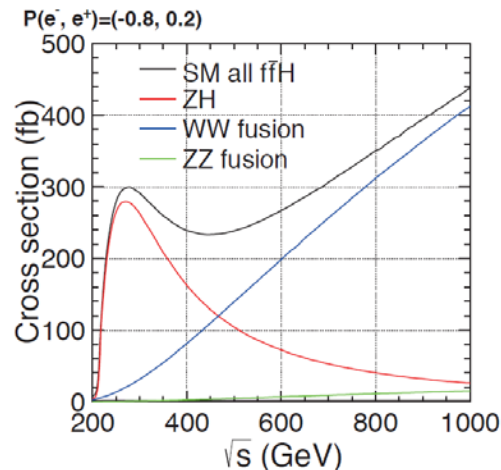
$$e^+e^- \rightarrow \nu\nu H, \quad ttH, \quad \nu\nu HH \quad \sqrt{s} \geq 1 \text{ TeV}$$



At  $\sqrt{s} \geq 1 \text{ TeV}$  an  $e^+e^-$  collider provides better measurements of the top Yukawa coupling and Higgs self coupling.

Search for additional Higgs bosons that might have been missed at LHC.

In addition, an  $e^+e^-$  collider becomes a Higgs factory again since the total Higgs cross section is larger than the total cross sections at 250 GeV, specially if polarized beams are used:



# ILC Energy/Lumi Scenarios

- ▶ Each scenario corresponds to accumulated luminosity at a certain point in time.
- ▶ Assumption: run for  $3 \times 10^7$  s at baseline lumi at each of  $E_{cm}=250, 500, 1000$  GeV, in that order. Then go back and run for  $3 \times 10^7$  s at upgrade lumi at each of  $E_{cm}=250, 500, 1000$  GeV.

Nickname	Ecm(1) (GeV)	Lumi(1) (fb <sup>-1</sup> )	+	Ecm(2) (GeV)	Lumi(2) (fb <sup>-1</sup> )	+	Ecm(3) (GeV)	Lumi(3) (fb <sup>-1</sup> )	Runtime (yr)	Wallplug E (MW-yr)
ILC(250)	250	250							1.1	130
ILC(500)	250	250		500	500				2.0	270
ILC(1000)	250	250		500	500		1000	1000	2.9	540
ILC(LumUp)	250	1150		500	1600		1000	2500	5.8	1220
ILC500(LumUp)	250	1150		500	1600				3.9	660

# ILC Measurement Summary

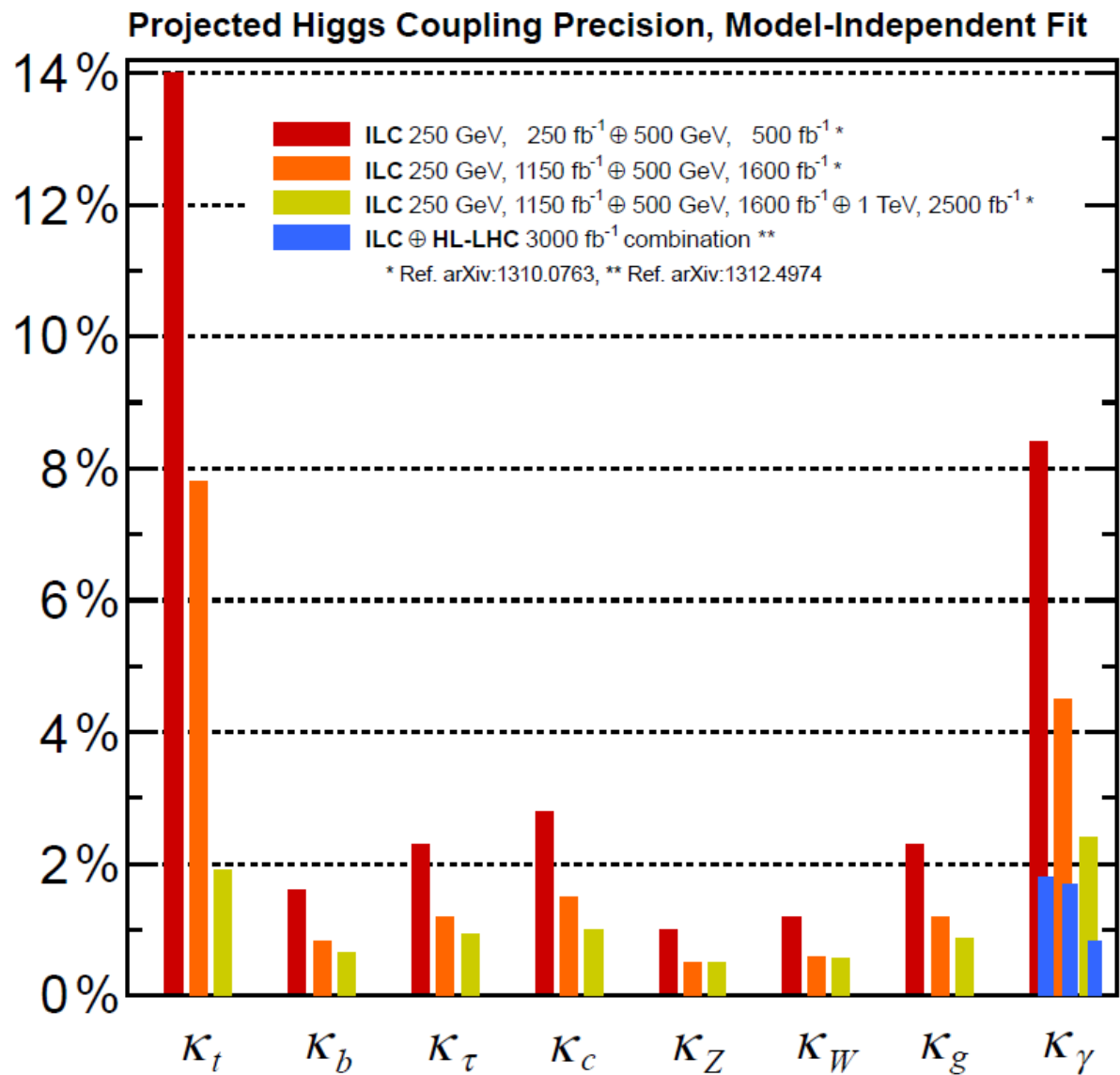
**Table 5.1.** Expected accuracies for cross section and cross section times branching ratio measurements for the 125 GeV  $h$  boson assuming you run  $3 \times 10^7$  s at the baseline differential luminosity for each center of mass energy. For invisible decays of the Higgs, the number quoted is the 95% confidence upper limit on the branching ratio.

$\sqrt{s}$ and $\mathcal{L}$ ( $P_{e-}, P_{e+}$ )	250 fb $^{-1}$ at 250 GeV (-0.8,+0.3)		500 fb $^{-1}$ at 500 GeV (-0.8,+0.3)				1 ab $^{-1}$ at 1 TeV (-0.8,+0.2)		
	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$Zhh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}hh$
$\Delta\sigma/\sigma$	2.6%	-	3.0	-		42.7%			26.3%
BR(invis.)	< 0.9 %	-	-	-	-				
mode	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$								
$h \rightarrow b\bar{b}$	1.2%	10.5%	1.8%	0.7%	28%		0.5%	6.0%	
$h \rightarrow c\bar{c}$	8.3%	-	13%	6.2%			3.1%		
$h \rightarrow gg$	7.0%	-	11%	4.1%			2.3%		
$h \rightarrow WW^*$	6.4%	-	9.2%	2.4%			1.6%		
$h \rightarrow \tau^+\tau^-$	4.2%	-	5.4%	9.0%			3.1%		
$h \rightarrow ZZ^*$	19%	-	25%	8.2%			4.1%		
$h \rightarrow \gamma\gamma$	34%	-	34%	23%			8.5%		
$h \rightarrow \mu^+\mu^-$	100%	-	-	-			31%		

**Table 5.2.** Expected accuracies for cross section and cross section times branching ratio measurements for the 125 GeV  $h$  boson assuming you run  $3 \times 10^7$  s at the sum of the baseline and upgrade differential luminosities for each center of mass energy. For invisible decays of the Higgs, the number quoted is the 95% confidence upper limit on the branching ratio.

$\sqrt{s}$ and $\mathcal{L}$ ( $P_{e-}, P_{e+}$ )	1150 fb $^{-1}$ at 250 GeV (-0.8,+0.3)		1600 fb $^{-1}$ at 500 GeV (-0.8,+0.3)				2.5 ab $^{-1}$ at 1 TeV (-0.8,+0.2)		
	$Zh$	$\nu\bar{\nu}h$	$Zh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$Zhh$	$\nu\bar{\nu}h$	$t\bar{t}h$	$\nu\bar{\nu}hh$
$\Delta\sigma/\sigma$	1.2%	-	1.7	-		23.7%			16.7%
BR(invis.)	< 0.4 %	-	-	-			-		
mode	$\Delta(\sigma \cdot BR)/(\sigma \cdot BR)$								
$h \rightarrow b\bar{b}$	0.6%	4.9%	1.0%	0.4%	16%		0.3%	3.8%	
$h \rightarrow c\bar{c}$	3.9%	-	7.2%	3.5%			2.0%		
$h \rightarrow gg$	3.3%	-	6.0%	2.3%			1.4%		
$h \rightarrow WW^*$	3.0%	-	5.1%	1.3%			1.0%		
$h \rightarrow \tau^+\tau^-$	2.0%	-	3.0%	5.0%			2.0%		
$h \rightarrow ZZ^*$	8.8%	-	14%	4.6%			2.6%		
$h \rightarrow \gamma\gamma$	16%	-	19%	13%			5.4%		
$h \rightarrow \mu^+\mu^-$	46.6%	-	-	-			20%		

# ILC Model Independent Higgs Coupling



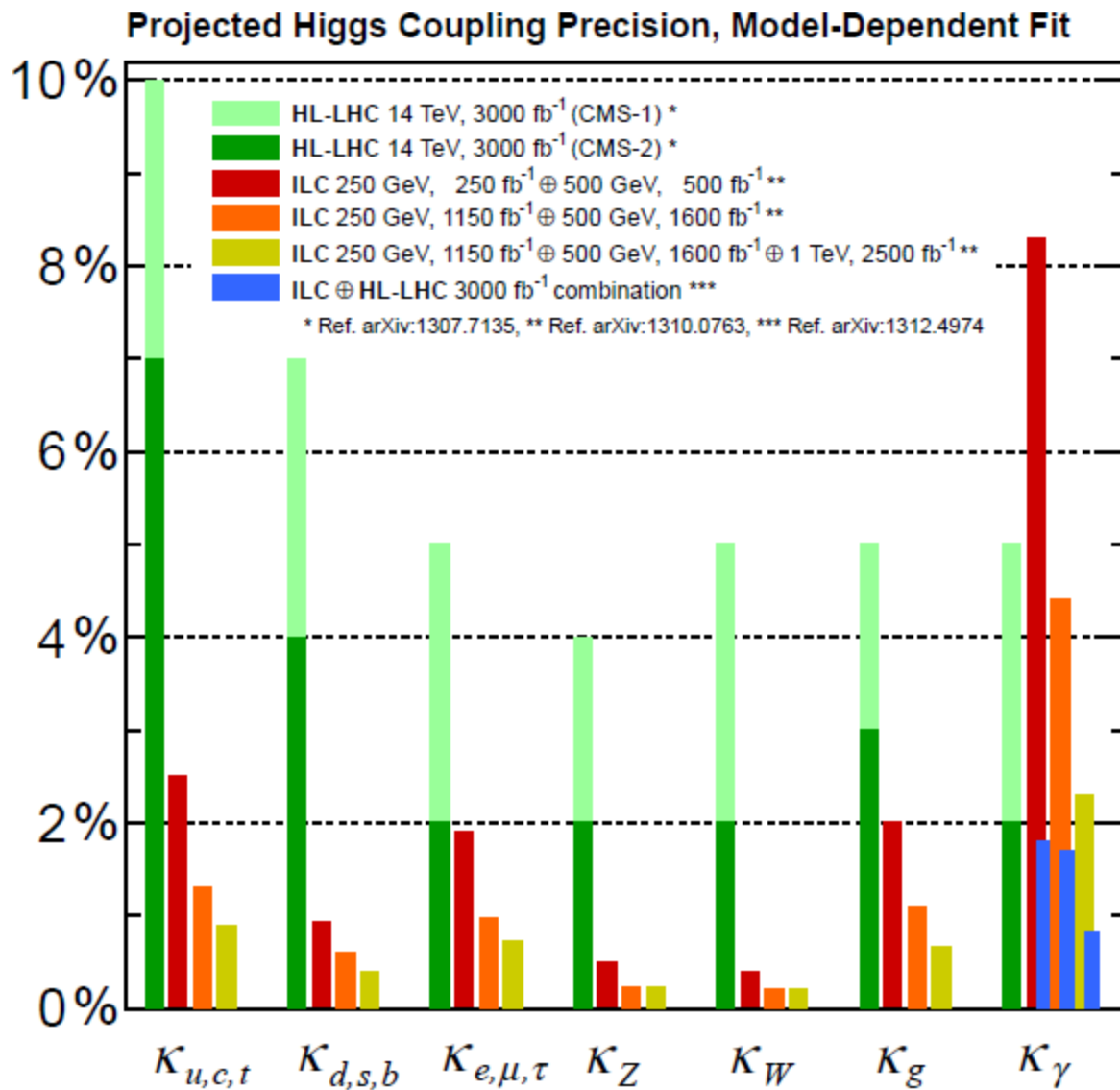
$$\Delta\Gamma_{\text{tot}} = 4.9\%$$

$$2.5\%$$

$$2.3\%$$

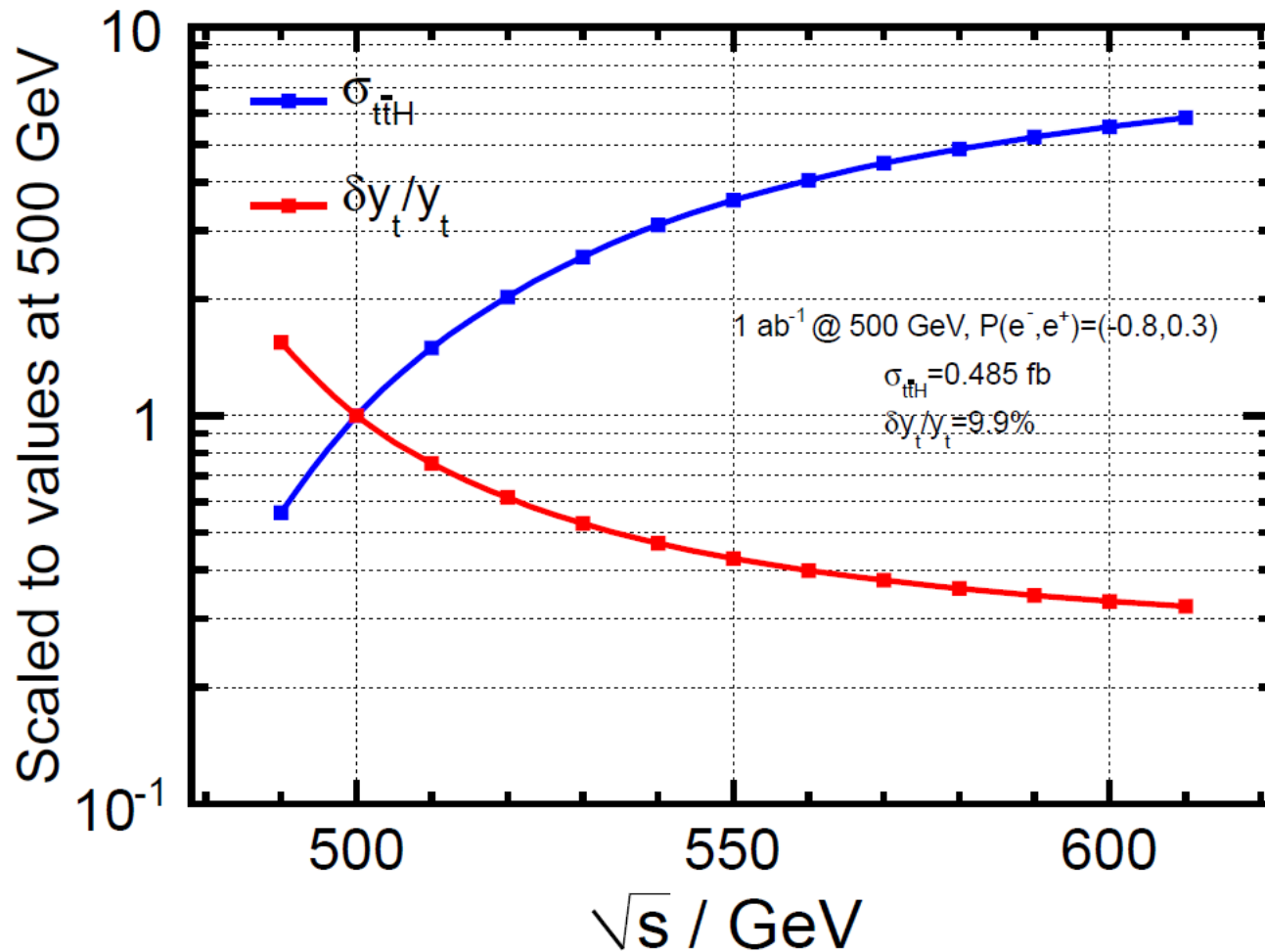
# Higgs Coupling Comparison Between LHC and ILC

## 7 Parameter HXSWG Benchmark





# Top Yukawa Coupling Versus $\sqrt{s}$



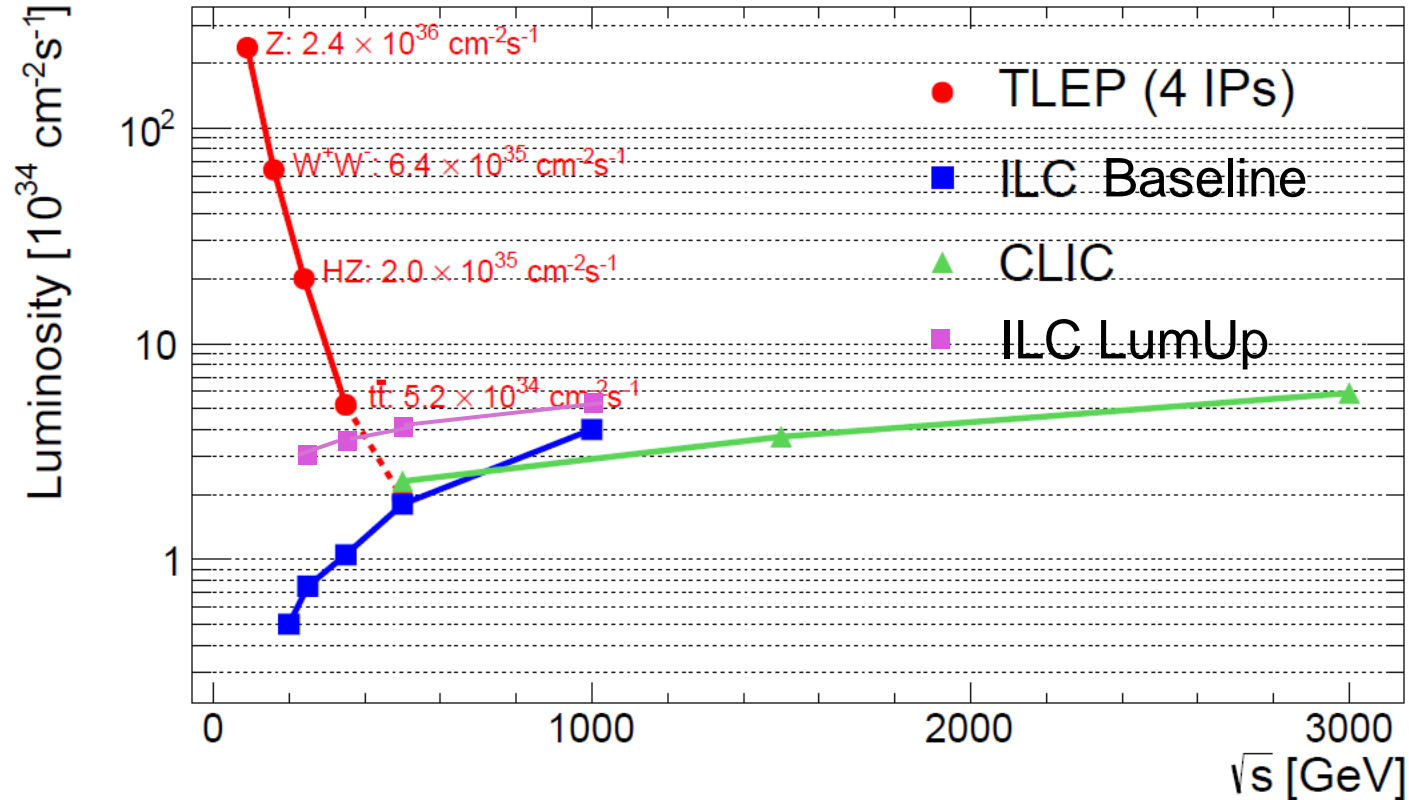
Precision improves by more than a factor of 3  
going from 500 to 550 GeV

# Higgs Self Coupling Summary

	HL-LHC	HE-LHC	VLHC
$\sqrt{s}$ (TeV)	14	33	100
$\int \mathcal{L} dt$ (fb <sup>-1</sup> )	3000	3000	3000
$\sigma \cdot \text{BR}(pp \rightarrow HH \rightarrow bb\gamma\gamma)$ (fb)	0.089	0.545	3.73
$S/\sqrt{B}$	2.3	6.2	15.0
$\lambda$ (stat)	50%	20%	8%

	ILC500	ILC500-up	ILC1000	ILC1000-up	CLIC1400	CLIC3000
$\sqrt{s}$ (GeV)	500	500	500/1000	500/1000	1400	3000
$\int \mathcal{L} dt$ (fb <sup>-1</sup> )	500	1600 <sup>‡</sup>	500+1000	1600+2500 <sup>‡</sup>	1500	+2000
$P(e^-, e^+)$	(-0.8, 0.3)	(-0.8, 0.3)	(-0.8, 0.3/0.2)	(-0.8, 0.3/0.2)	(0, 0)/(-0.8, 0)	(0, 0)/(-0.8, 0)
$\sigma(ZHH)$	42.7%		42.7%	23.7%	–	–
$\sigma(\nu\bar{\nu}HH)$	–	–	26.3%	16.7%		
$\lambda$	83%	46%	21%	13%	28/21%	16/10%

# FCC-ee



2 Big Luminosity Advantages of FCC-ee over ILC:

- 4 IP's
- Luminosity of FCC-ee grows as  $\sqrt{s}$  is lowered below 250, while ILC luminosity drops off

## Model Dependent Fits (7 Parameter HXSWG Benchmark)

Numbers from "First Look at Physics  
Case for TLEP", JHEP 01,164(2014)  
TLEP = 4 exp. @ 240 +350 GeV

Numbers from ILC Higgs  
White Paper, arXiv:1310.0763,

Coupling	TLEP	ILC500(LumUp)*
$g_{HZZ}$	0.05%	0.3%
$g_{HWW}$	0.09%	0.3%
$g_{Hbb}$	0.19%	0.6%
$g_{Hcc}$	0.68%	1.4%
$g_{Hgg}$	0.79%	1.1%
$g_{H\tau\tau}$	0.49%	1.0%
$g_{H\mu\mu}$	6.2%	42%
$g_{H\gamma\gamma}$	1.4%	4.4%

\* Includes several 0.1% systematic errors including 0.1% theory error

## Model Independent fits

Numbers from "First Look at Physics  
Case for TLEP", JHEP 01,164(2014)  
TLEP = 4 exp. @ 240 +350 GeV

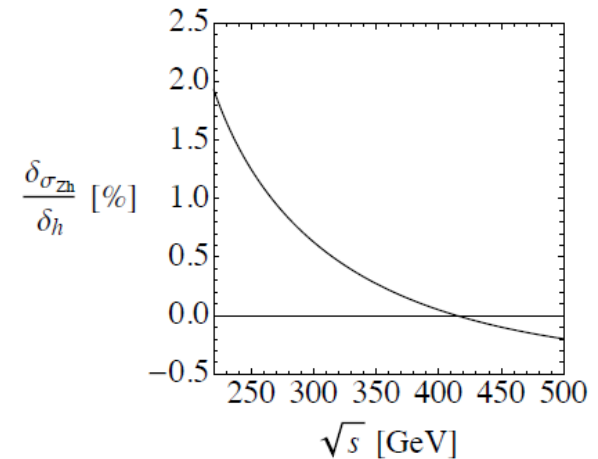
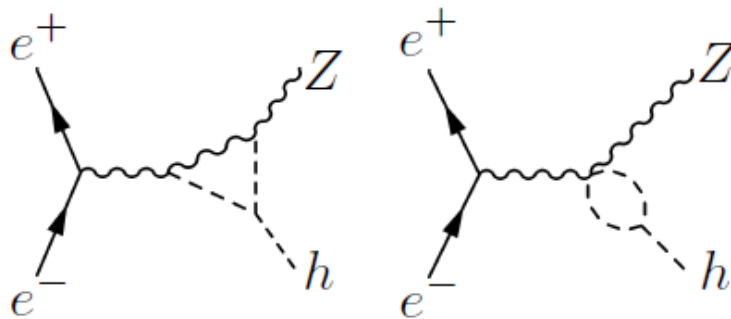
Numbers from ILC Higgs  
White Paper, arXiv:1310.0763,

Coupling	TLEP-240	TLEP	ILC500(LumUp)
$g_{HZZ}$	0.16%	<b>0.15%</b>	0.5%
$g_{HWW}$	0.85%	<b>0.19%</b>	0.6%
$g_{Hbb}$	0.88%	<b>0.42%</b>	0.8%
$g_{Hcc}$	1.0%	<b>0.71%</b>	1.5%
$g_{Hgg}$	1.1%	<b>0.80%</b>	1.2%
$g_{H\tau\tau}$	0.94%	<b>0.54%</b>	1.2%
$g_{H\mu\mu}$	6.4%	<b>6.2%</b>	42%
$g_{H\gamma\gamma}$	1.7%	<b>1.5%</b>	4.5%

## Higgs Self Coupling Measurement at FCC-ee Using NLO

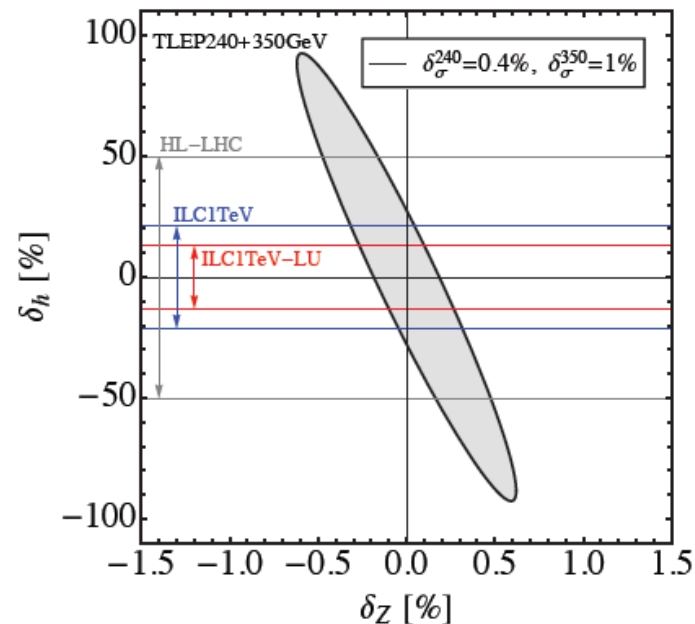
### Contribution to $e^+e^- \rightarrow ZH$ at $\sqrt{s} = 240$ & 350 GeV

M. McCullough, arXiv:1312.3322



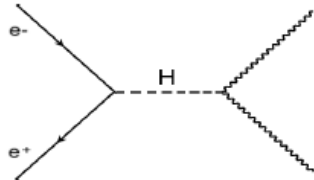
$$\delta_{\sigma}^{240} = 100 (2\delta_Z + 0.014\delta_h) \%$$

Assuming  $\delta_Z = 0$  Higgs self coupling can be constrained to  $|\delta_h| < 28\%$  by FCC-ee at  $\sqrt{s} = 240$  GeV



## Measurement of Electron Yukawa Coupling @ $\sqrt{s} = 125$ GeV?

- Resonant s-channel Higgs production at FCC-ee ( $\sqrt{s} = 125$  GeV):



$$\sigma(e^+e^- \rightarrow H)_{B-W} \sim 1.64 \text{ fb}$$

$$\sigma(e^+e^- \rightarrow H)_{\text{visible}} \sim 280 \text{ ab (ISR + } E_{\text{beam-spread}} \sim \Gamma_H = 4.2 \text{ MeV)}$$

- Signal + backgrounds study for 7 decay channels:

$WW^*(2j, l\nu)$  ( $\sigma = 28 \text{ ab}$ ),  $WW^*(2l2\nu)$  ( $\sigma = 6.7 \text{ ab}$ ),

$WW^*(4j)$  ( $\sigma = 29.5 \text{ ab}$ ),  $ZZ^*(2j2\nu)$  ( $\sigma = 2.3 \text{ ab}$ ),  $ZZ^*(2l2j)$  ( $\sigma = 1.14 \text{ ab}$ ),

$bb(2j)$  ( $\sigma = 156 \text{ ab}$ ),  $gg(2j)$  ( $\sigma = 24 \text{ ab}$ )

- Preliminary analysis:

$$L_{\text{int}} = 10 \text{ ab}^{-1}, S=0.65: \text{BR}(H\text{ee}) < 4.63 \times \text{BR}_{\text{SM}} (3\sigma), g_{\text{hee}} < 2.15 \times g_{\text{Hee,SM}} (3\sigma)$$

Evidence (observation?) will require further improvements in large-BR (huge background) jet channels:  $H \rightarrow bb$ ,  $H \rightarrow WW \rightarrow 4j$

- Challenging accelerator conditions: mono-chromaticity, huge lumi

# Summary

- ▶ Due to the unique experimental environment of  $e^+e^-$  machines, ILC, CLIC and FCC-ee can improve on the excellent Higgs measurements expected from LHC and HL-LHC. They provide a means to bring Higgs coupling precisions from the few percent level to the sub-percent level
- ▶ The ILC – the most mature of the future  $e^+e^-$  designs – provides significant improvement over HL-LHC over a wide range of Higgs couplings.
- ▶ CLIC and FCC-ee can take the Higgs coupling measurements even further, with significant enhancements in energy and luminosity, respectively, relative to the ILC.