Implementation and Improvement of Bead-pull Technique on Cavity Cells



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Goals and Contents

- Tune the screwed-up cavity cells
- Look for local reflection coefficient to tune the cells
- Enhance LabVIEW's calculation ability with Mathcad
- I. Theory II. Implementation III. Improvement IV. Progress Updates



I. Theory: 1st assumption

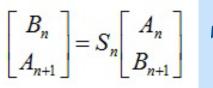
• Each cell is a 2-port network

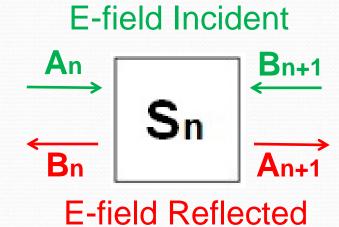
Sn is 2X2 matrix

Fact:

 \rightarrow Scattering matrix *Sn* can be defined

Formula sheet:







I. Theory: 2nd & 3rd assumptions

- Fact:
- Sn is 2X2 matrix
- Sn is unitary Sn is symmetric
- Formula sheet:

$$\begin{bmatrix} B_n \\ A_{n+1} \end{bmatrix} = S_n \begin{bmatrix} A_n \\ B_{n+1} \end{bmatrix}$$

No energy dissipation

→ Energy entering = Energy exiting → $|B_n|^2 + |A_{n+1}|^2 = |A_n|^2 + |B_{n+1}|^2$ → $\left|S_n \begin{bmatrix} A_n \\ B_{n+1} \end{bmatrix}^2 = \begin{bmatrix} A_n \\ B_{n+1} \end{bmatrix}^2$

 $\begin{bmatrix} A_{n+1} \end{bmatrix} \begin{bmatrix} B_{n+1} \end{bmatrix}$ • Cavity cells are identical $S_n = \begin{bmatrix} \Gamma_n & \sqrt{1 - |\Gamma_n|^2} e^{-j\varphi} \\ \sqrt{1 - |\Gamma_n|^2} e^{-j\varphi} & \Gamma_n \end{bmatrix}$ • Power losses the same regardless of propagation direction (reciprocal)



I. Theory: Find the reflection formula

Fact: Sn is 2X2 matrix Sn is unitary Sn is symmetric

Formula sheet:

 $\begin{vmatrix} B_n \\ A_n \end{vmatrix} = S_n \begin{vmatrix} A_n \\ B_n \end{vmatrix}$

 Γ_n =local reflection coefficient at cell #n •φ =phase difference

 $|\Gamma_n| \ll 1, \quad \sqrt{1-|\Gamma_n|} \approx 1$ $S_{n} = \begin{vmatrix} \Gamma_{n} & \sqrt{1 - \left|\Gamma_{n}\right|^{2}} e^{-j\varphi} \\ \sqrt{1 - \left|\Gamma_{n}\right|^{2}} e^{-j\varphi} & \Gamma_{n} \end{vmatrix}$ $I_n = A_n + B_n$ $\Gamma_n = \frac{-I_{n-1} + 2I_n \cos \varphi - I_{n+1}}{I_{n-1} - I_n \exp(-j\varphi)}$ Argo

I. Theory: Bead-pull Technique

Steele's equation:

$$2P_i(S_{11p} - S_{11u}) = -j\omega kI$$

I = In

 $\frac{-I_{n-1}+2I_n\cos\varphi-I_{n+1}}{I_{n-1}-I_n\exp(-j\varphi)}$

Reflection formula:

 S_{11p} and S_{11u}

• Satisfies Steele's equation

- P_i = input power,
- S_{11p} = global reflection with object,
- S_{11u} = global reflection without object
- ω = angular frequency of the field
- *k* = constant depending on geometry of the object
- *I* = E-field at the object's position before the object perturbs the field

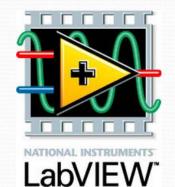


II. Implementation

 S_{11p} and $S_{11u} \leftarrow$ Steele's equation: $2P_i(S_{11p} - S_{11u}) = -j\omega kI^2$ I = In**Reflection formula:** $\Gamma_{n} = \frac{-I_{n-1} + 2I_{n}\cos\varphi - I_{n+1}}{I_{n-1} - I_{n}\exp(-j\varphi)}$



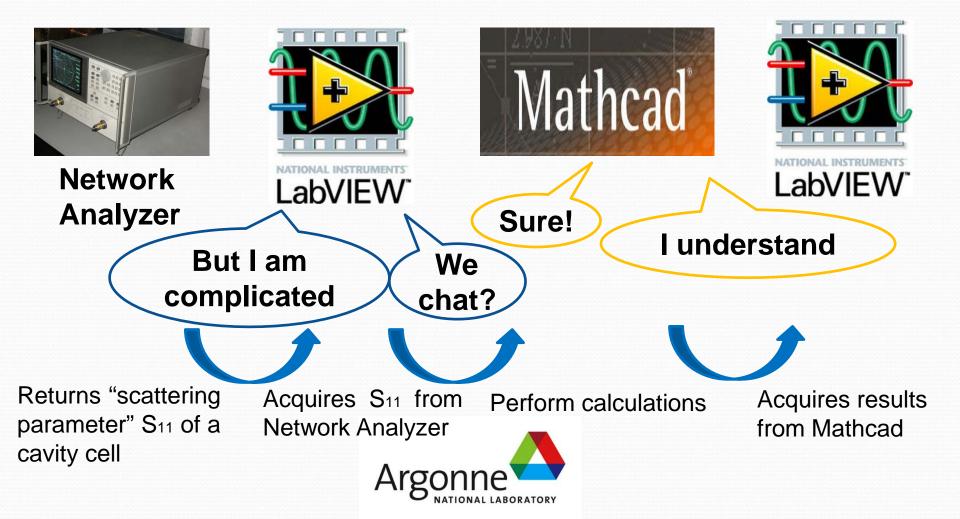
Network Analyzer





III. Improvement

Enhancing LabVIEW's calculation ability with Mathcad



IV. Progress Updates

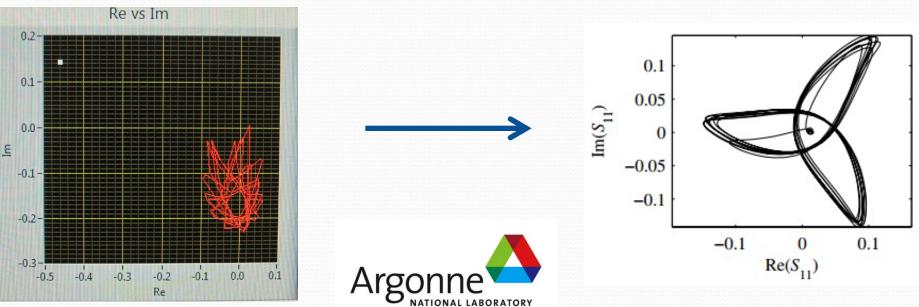
Currently:

LabVIEW codes to get data with bead-pull technique

•LabVIEW-Mathcad interface for enhanced computation

In progress:

Tune the cavity to obtain reasonable plots





[1] D. Alesini et al. "Tuning procedure for traveling wave structures and its application to the C-Band cavities for SPARC photo injector energy upgrade." *Journal of Instrument*, vol. 8, Oct. 2013.

[2] J. Shi et al. "Tuning of Clic accelerating structure prototypes at CERN." *Proc. LINAC*, 2010.



