

# Dielectric sample testing for high-pressured RF cavity

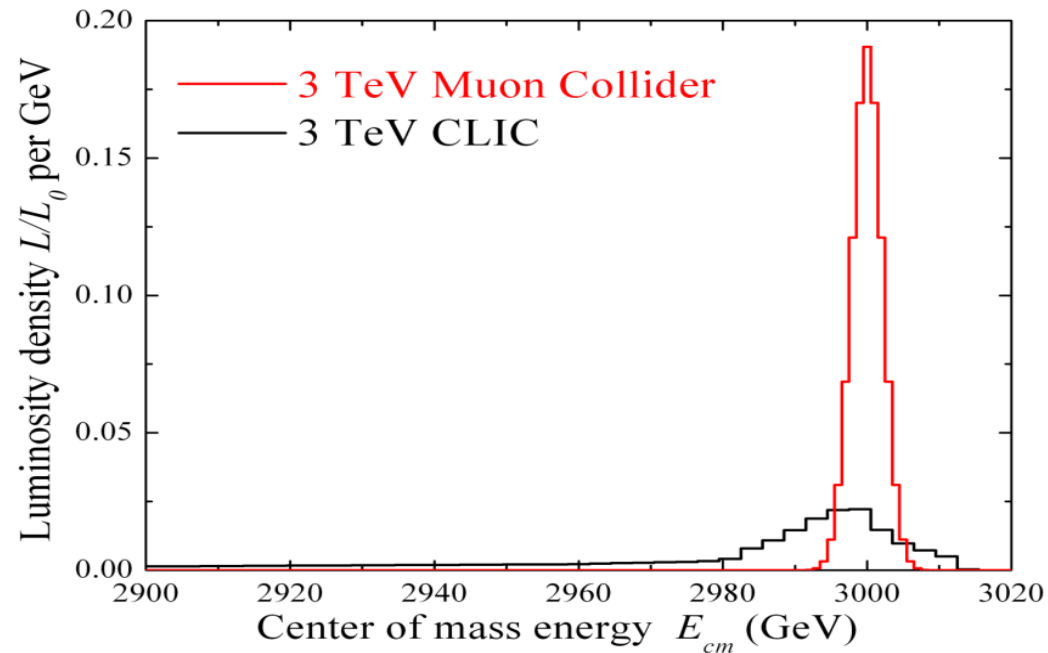
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# Muon collider

## ► Why?

- Cleaner collision
- Much less synchrotron radiation
- Small energy spread at interaction region
- Potential Higgs Factory



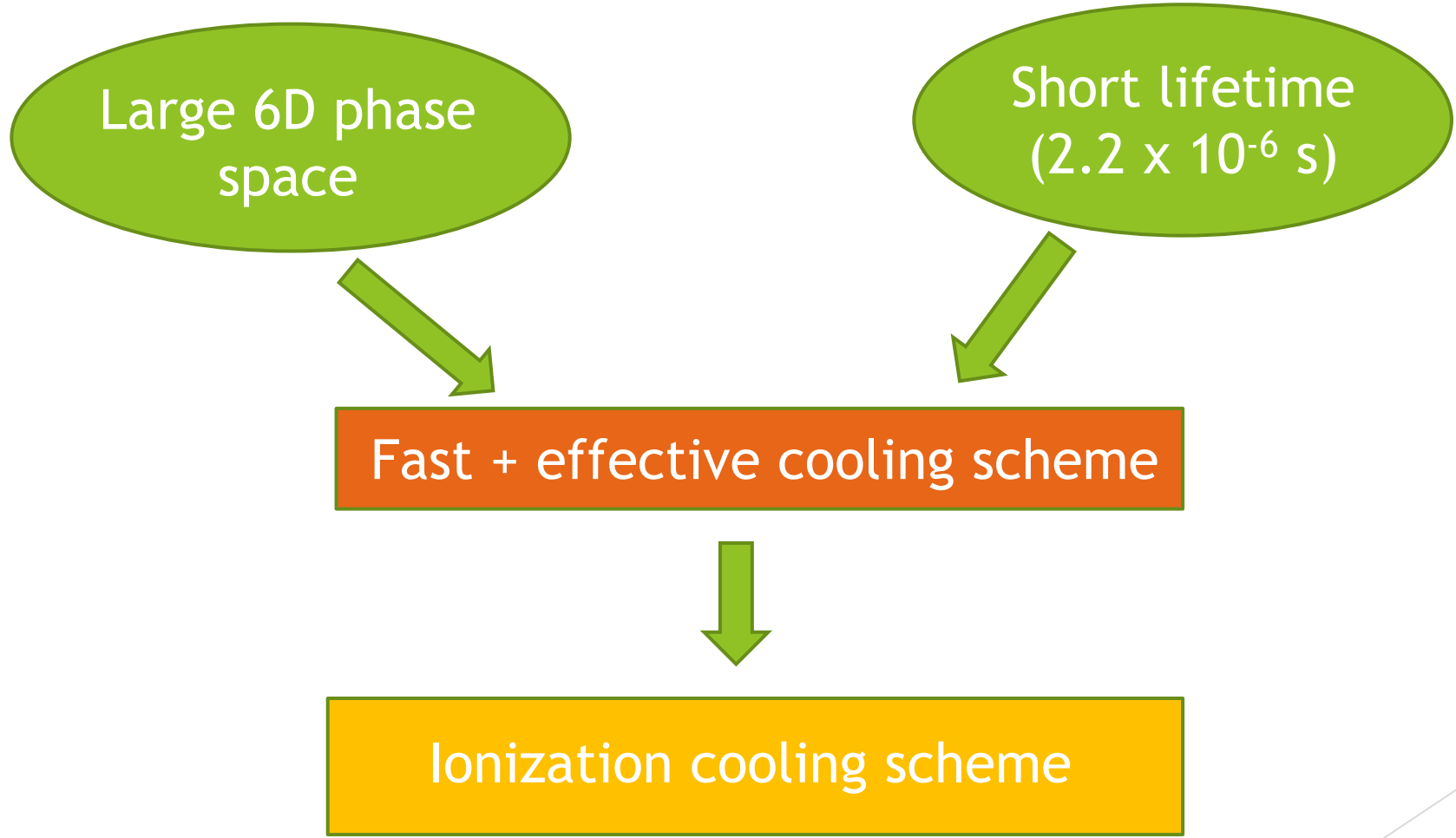
## ► Challenges

Large 6D phase space

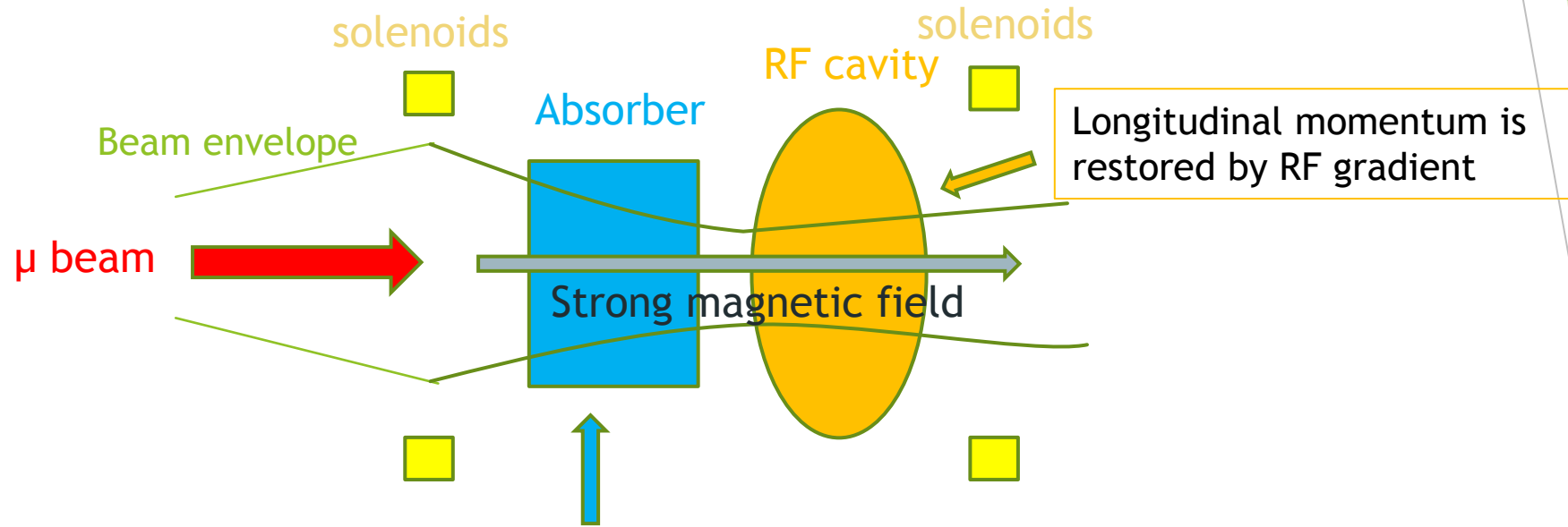
Short lifetime  
( $2.2 \times 10^{-6}$  s)

Fast + effective cooling scheme

Ionization cooling scheme



# Ionization cooling channel



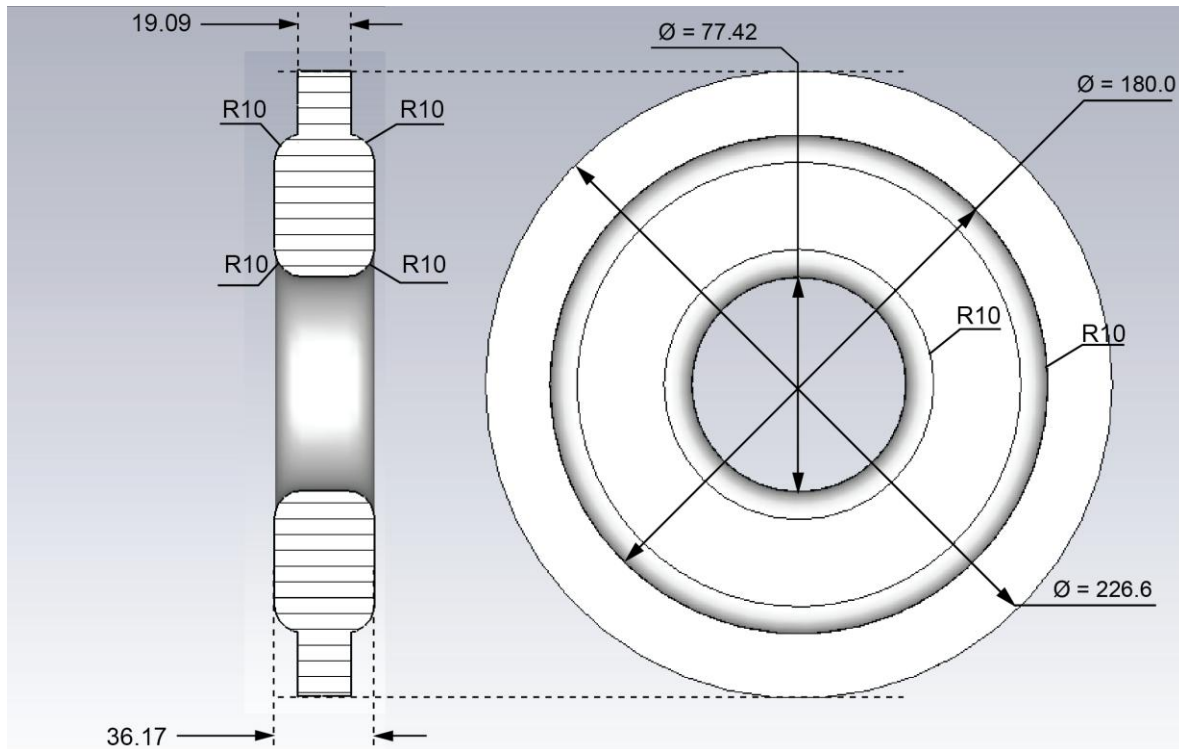
Longitudinal momentum is restored by RF gradient

Transverse and longitudinal momentum both decrease as the beam ionizes low-Z absorber



Necessity in reducing RF cavity's radial size to fit inside solenoids

# Dielectric insert ring



$$f \propto \frac{1}{R\sqrt{\mu\epsilon}}$$

- f**: resonant frequency(Hz)
- R**: radius of cavity (m)
- ε**: relative dielectric constant
- μ**: permeability (H.m<sup>-1</sup>)

By loading the cavity with dielectric structure, smaller radius is enough to attain same resonant frequency

# Important parameters of dielectrics

- ▶ Dielectric constant (permittivity): material properties that determines how electric field affects, or is affected by some medium.

$$\epsilon = \epsilon' - j\epsilon''$$

- ▶ Loss tangent: ratio between the lossy reaction to electric field and lossless reaction to electric field

$$\tan \delta = \frac{\epsilon''}{\epsilon'}$$

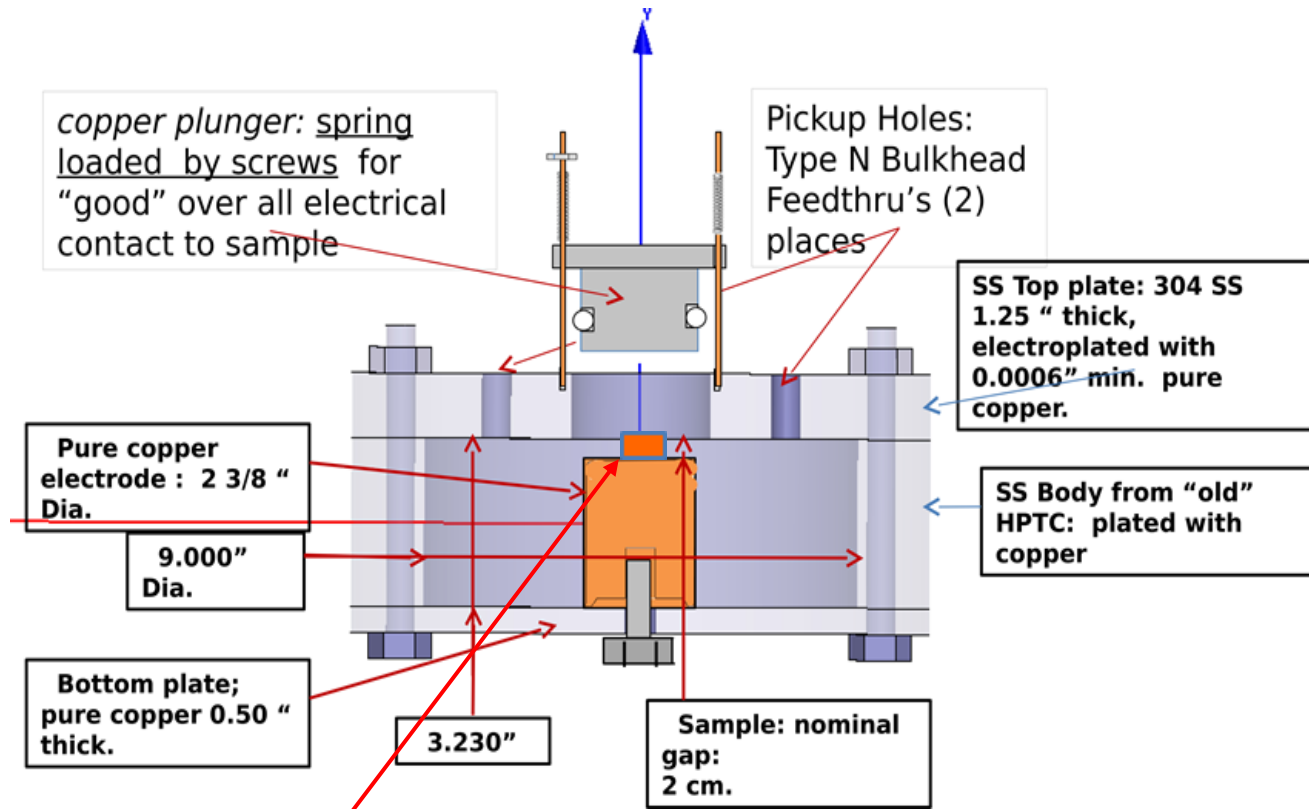
- ▶ Loss tangent quantifies how much electric field energy will be dissipated into heating the dielectric
- ▶ Dielectric material reduces quality factor of cavity => **choose material that gives small loss but can still achieve desired cavity radius**

# Dielectric sample test

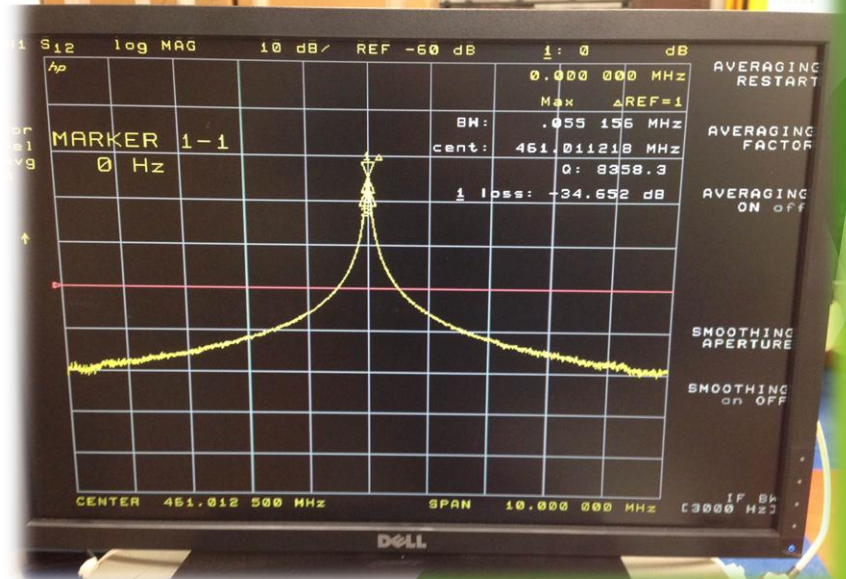
- ▶ Goal:
  - ▶ Determine dielectric constant and loss tangent of various materials
  - ▶ Analyze experimental results to find optimal material for the insert ring
- ▶ Sample tested:
  - ▶ Alumina ( $\text{Al}_2\text{O}_3$ ) with various purity
  - ▶ Magnesium Calcium Titanate (MCT)
  - ▶ Corderite ( $(\text{Mg,Fe})_2\text{Al}_4\text{Si}_5\text{O}_{18}$ )
  - ▶ Aluminum Nitride (AlN)



# Experimental setup

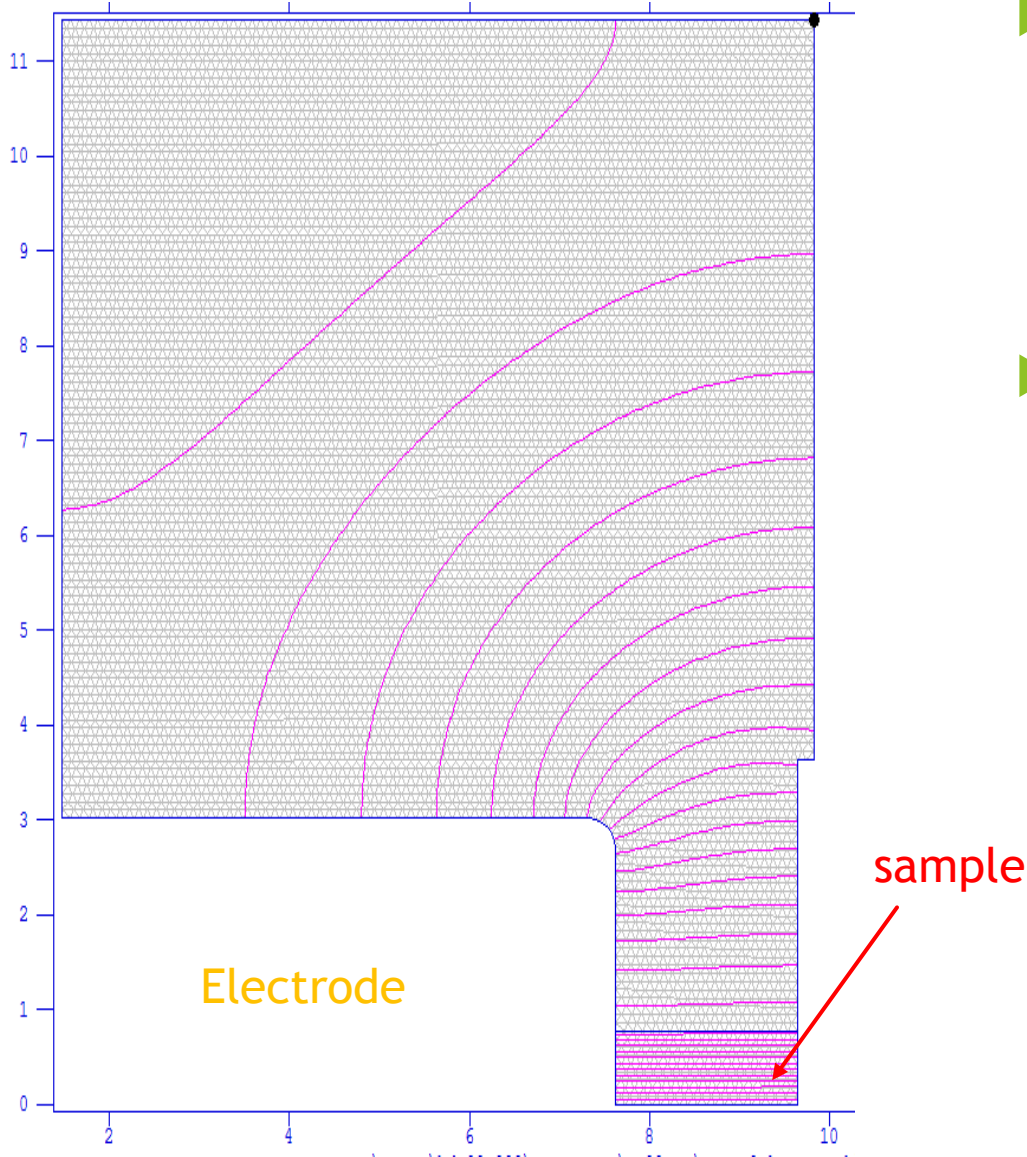


Dielectric sample  
(cylindrical rod or tube)





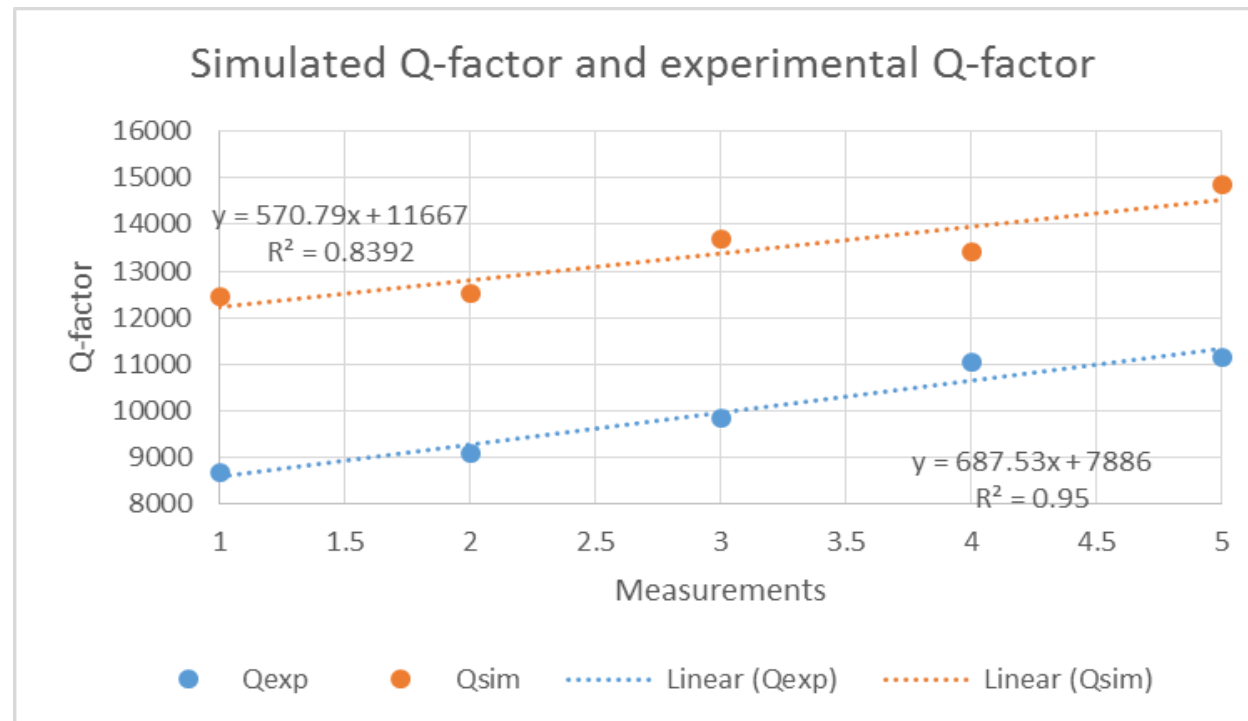
# Method



- ▶ Measure quality factor and resonant frequency of cavity with dielectric sample inside
- ▶ Compare with **quality factor vs loss tangent plot** and **resonant frequency vs dielectric constant plot** obtained from POISSON/SUPERFISH simulation to determine sample's properties

# Calibration

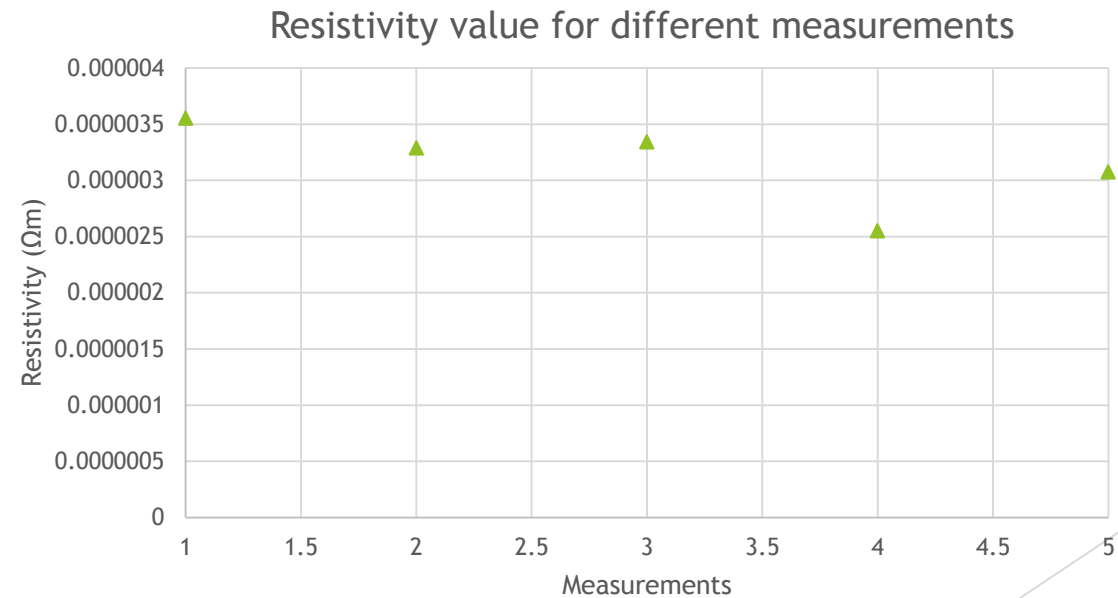
- ▶ SUPERFISH assumes ideal resistivity for copper wall => need to find actual wall resistivity
- ▶ Simulate empty cavity and compare with actual empty cavity with no sample



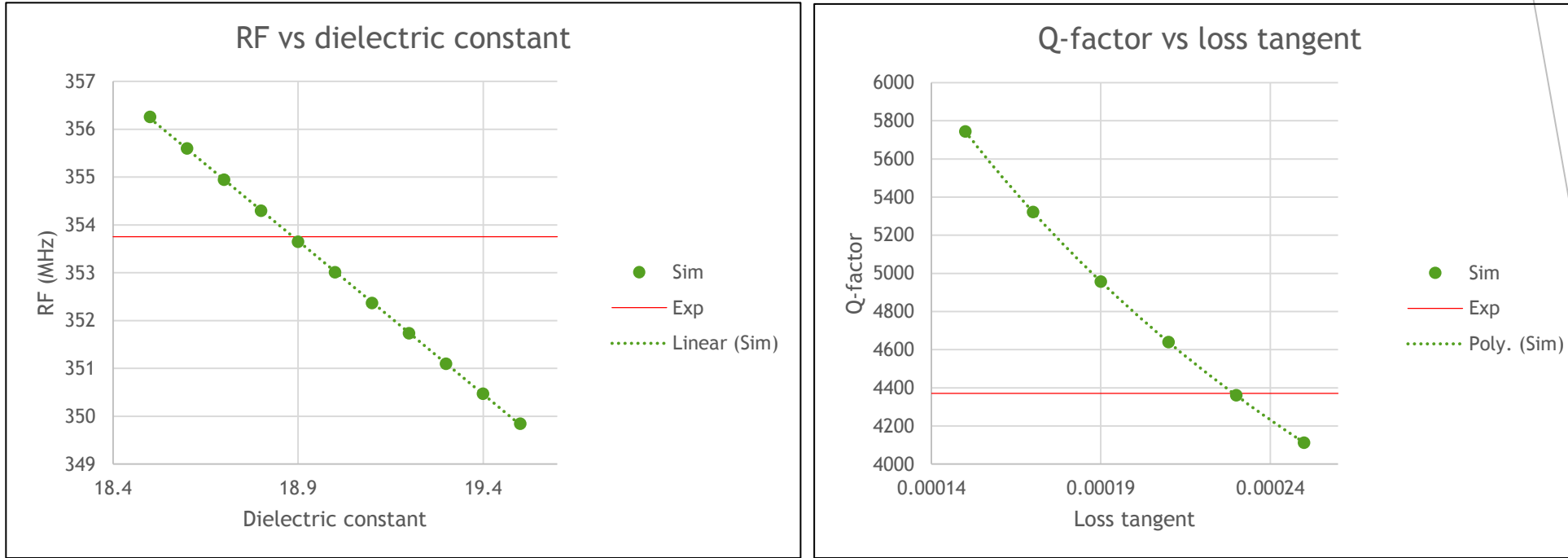
► Relationship between wall resistivity and quality factor:

$$\rho_{wall} = \left( \frac{Q_{simulation}}{Q_{experimental}} \right)^2 \rho_{ideal}$$

►  $\rho_{wall} = 3.16 \times 10^{-6} (\Omega.m)$



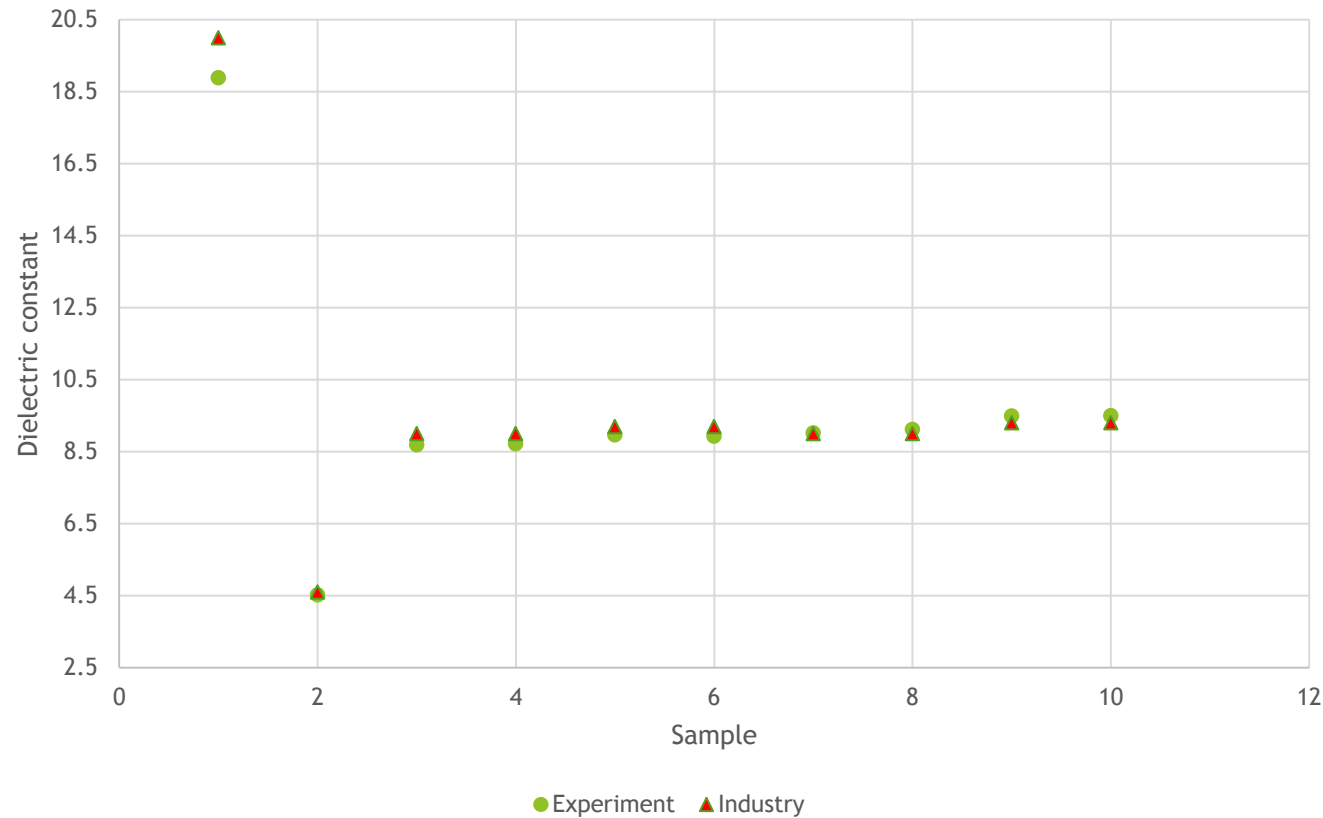
# Results



Sample data of MCT

Dielectric constant and loss tangent => **intersection between simulated relationship and measured values**

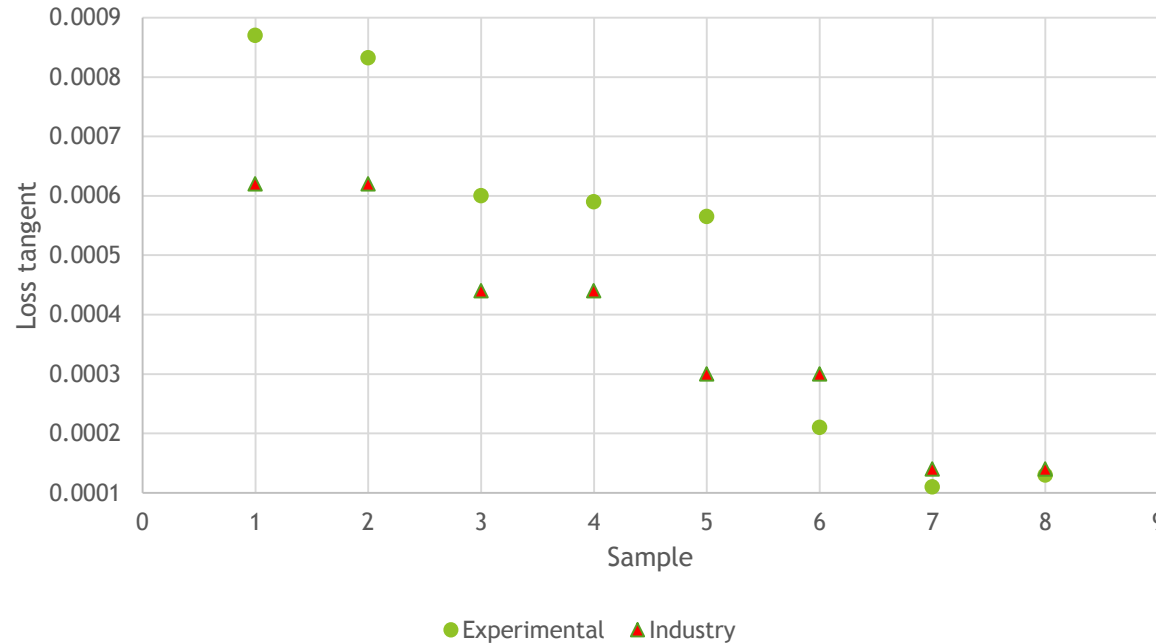
Comparison with industry value for dielectric constant



- 1/ MCT
- 2/ Corderite
- 3/ Alumina 94%
- 4/ Alumina 94%
- 5/ Alumina 96%
- 6/ Alumina 96%
- 7/ Alumina 97.6%
- 8/ Alumina 97.6%
- 9/ Alumina 99.5%
- 10/ Alumina 99.5%

- Dielectric constant error all falls within 6%
- Closely match industry-given value for dielectric constant

Comparison with industry value (loss tangent)



1/ Alumina 94%  
2/ Alumina 94%  
3/ Alumina 96%  
4/ Alumina 96%  
5/ Alumina 97.6%  
6/ Alumina 97.6%  
7/ Alumina 99.5%  
8/ Alumina 99.5

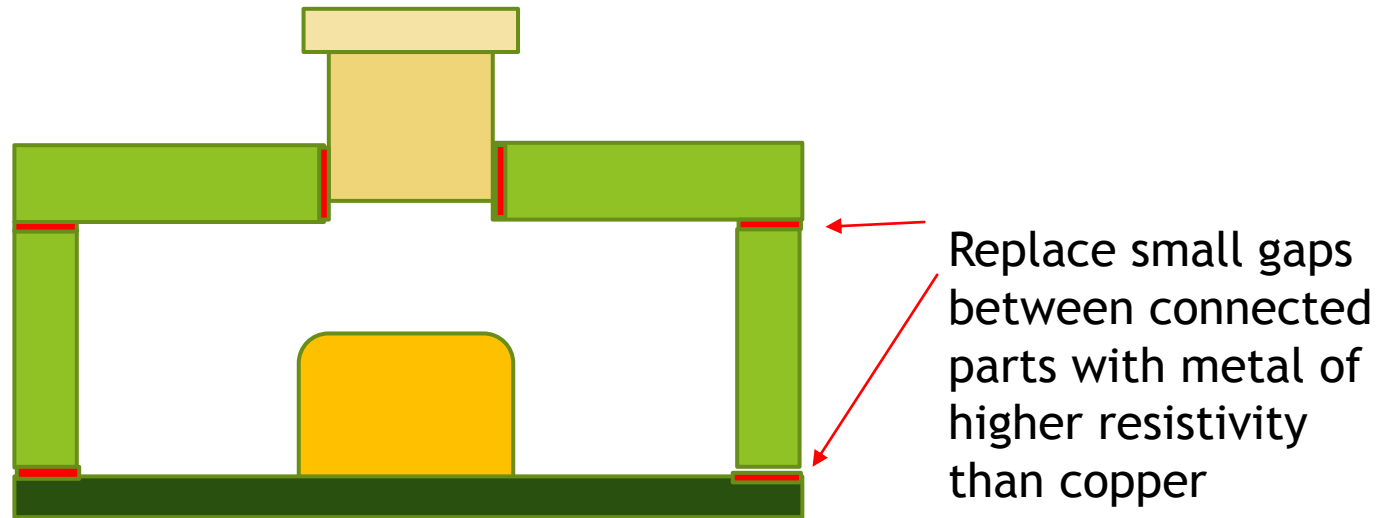
- Comparison used only alumina samples since there is no given loss tangent for others.
- Calculated loss tangent experiences increasing discrepancy with decreasing alumina purity.
- Either the vendors calculate it wrong or there is systematic error in the simulation
- Possible source of systematic error: resistivity at connected joint between cavity's components

# Conclusion

- ▶ Calculated dielectric constants follow consistently with vendor-provided values
- ▶ Discrepancy between calculated loss tangent and vendor-provided values might be because of connection's resistivity.
- ▶ Overall, alumina 99.5% gives the most desirable values for dielectric constant (~9.5) and loss tangent (0.00013)

# Future step

- ▶ Proposed new model to describe better wall resistivity of test cavity:



- ▶ Apply same test for the actual ring in high-powered beam test.



# Acknowledgement

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