



Dalitz Plot Analysis of $B \rightarrow D\bar{D}K$ decays

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for the BaBar collaboration

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Introduction

- Results recently published by BaBar (March 2015)
- Analysis chiefly done by Vincent Poireau (LAPP, Annecy)

PHYSICAL REVIEW D **91**, 052002 (2015)

Dalitz plot analyses of $B^0 \rightarrow D^- D^0 K^+$ and $B^+ \rightarrow \bar{D}^0 D^0 K^+$ decays

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Dalitz plot analyses of $B^0 \rightarrow D^- D^0 K^+$ and $B^+ \rightarrow \bar{D}^0 D^0 K^+$ decays[illegible]

(BABAR Collaboration)

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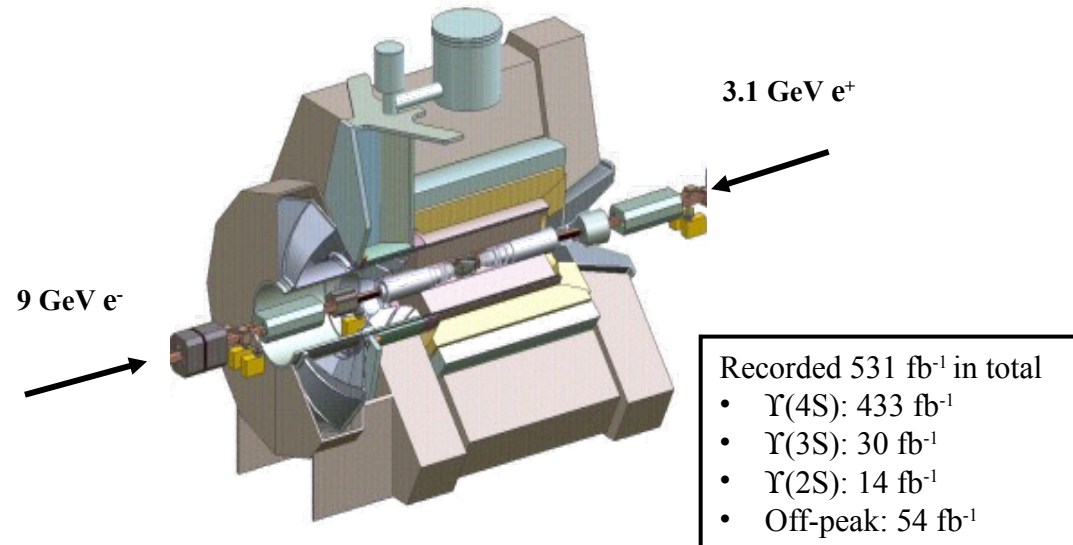
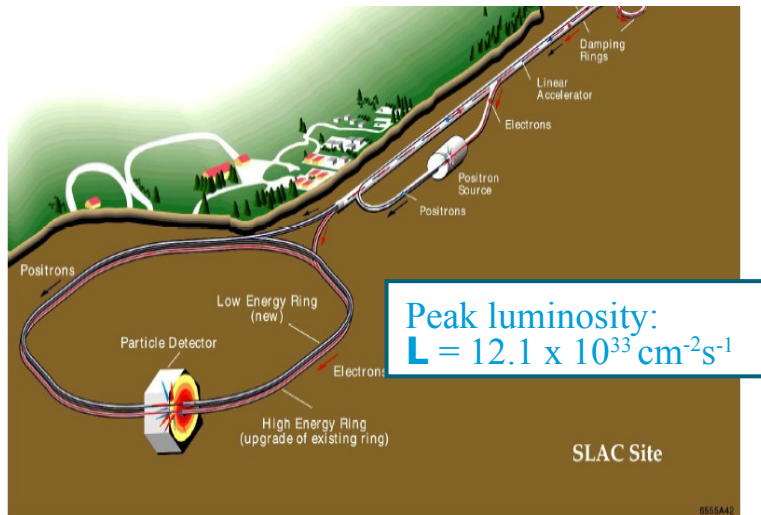
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Introduction, continued

Center of mass: 10.58 GeV
 $e^+ e^- \rightarrow \Upsilon(4S) (b\bar{b}) \rightarrow B\bar{B}$



- The *BABAR* experiment switched off in 2008, but still produces many interesting results!

- 549 papers in total
- 26 in 2013
- 15 in 2014
- ~15 expected in 2015

Introduction, continued

- Studying $B \rightarrow D^{(*)}D^{(*)}K$ decays

- **22 modes**

- These modes have been the topics of **three previous BaBar papers**

- Time-dependent **CP asymmetry** in $B \rightarrow D^{*-}D^{*+}K^0_S$ Phys. Rev. D74, 091101, 2006
- Study of the **resonances** $\psi(3770)$, $D_{s1}(2536)$, and $X(3872)$ Phys. Rev. D77, 011102, 2008
- Measurement of 22 **branching fractions** Phys. Rev. D83, 032004, 2011

- These decays contain **resonances**
in $D^{(*)}D^{(*)}K$ ($c\bar{s}$) or
 $D^{(*)}D^{(*)}K$ ($c\bar{c}$)

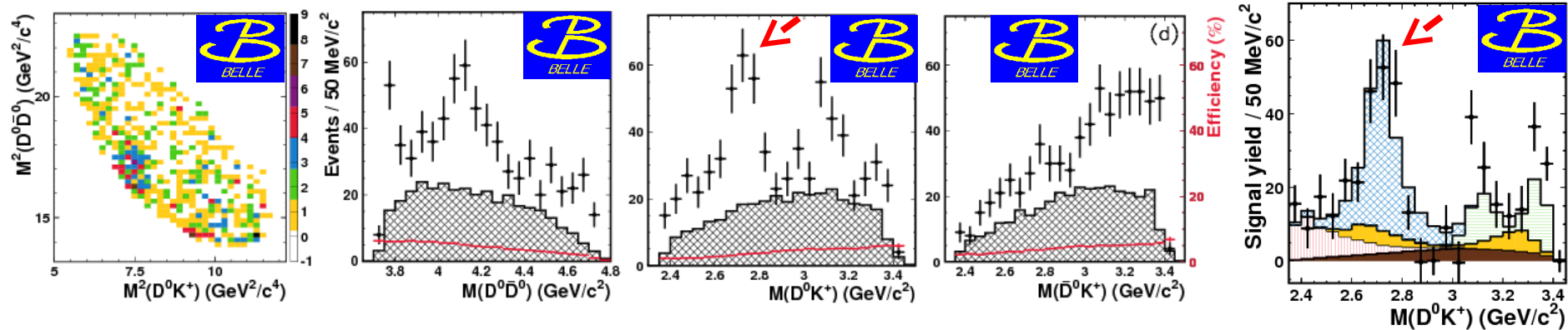
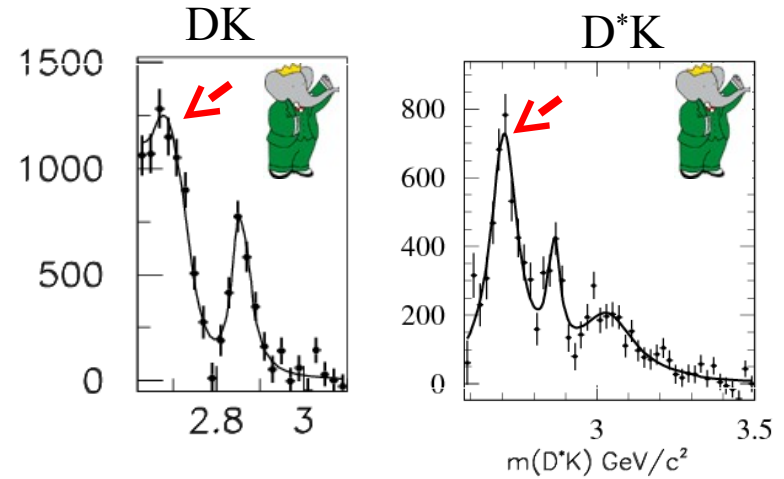
- Here we report on properties of
the $D_{s1}(2700)$

Neutral B mode	Charged B mode
$B^0 \rightarrow D^- D^0 K^+$	$B^+ \rightarrow \bar{D}^0 D^+ K^0$
$B^0 \rightarrow D^- D^{*0} K^+$	$B^+ \rightarrow \bar{D}^0 D^{*+} K^0$
$B^0 \rightarrow D^{*-} D^0 K^+$	$B^+ \rightarrow \bar{D}^{*0} D^+ K^0$
$B^0 \rightarrow D^{*-} D^{*0} K^+$	$B^+ \rightarrow \bar{D}^{*0} D^{*+} K^0$
$B^0 \rightarrow D^- D^+ K^0$	$B^+ \rightarrow \bar{D}^0 D^0 K^+$
$B^0 \rightarrow D^- D^{*+} K^0 + D^{*-} D^+ K^0$	$B^+ \rightarrow \bar{D}^0 D^{*0} K^+$
	$B^+ \rightarrow \bar{D}^{*0} D^0 K^+$
$B^0 \rightarrow D^{*-} D^{*+} K^0$	$B^+ \rightarrow \bar{D}^{*0} D^{*0} K^+$
$B^0 \rightarrow \bar{D}^0 D^0 K^0$	$B^+ \rightarrow D^- D^+ K^+$
$B^0 \rightarrow \bar{D}^0 D^{*0} K^0 + \bar{D}^{*0} D^0 K^0$	$B^+ \rightarrow D^- D^{*+} K^+$
	$B^+ \rightarrow D^{*-} D^+ K^+$
$B^0 \rightarrow \bar{D}^{*0} D^{*0} K^0$	$B^+ \rightarrow D^{*-} D^{*+} K^+$

The $D_{s1}(2700)$

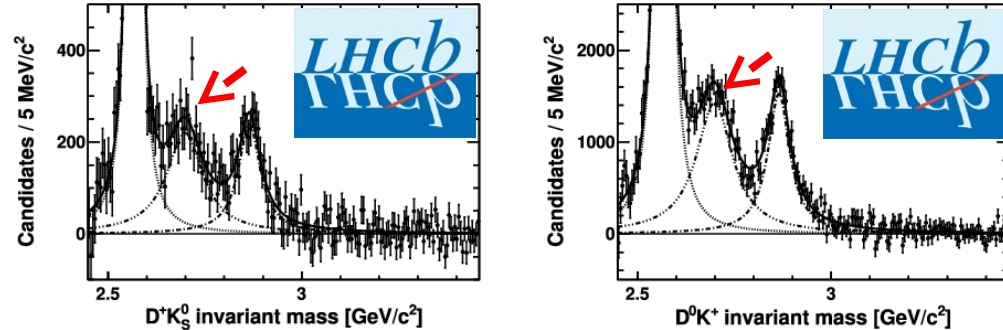
- The $D_{s1}(2700)$ was **discovered** by BaBar in inclusive e^+e^- interactions
 - Decaying to DK
 - Observed later also in D^*K
 - Discovered as well $D_{sJ}(2860)$ and $D_{sJ}(3040)$

This discovery was **confirmed by Belle** in $B^+ \rightarrow \bar{D}^0(D^0K^+)$



The $D_{s1}(2700)$, continued

- LHCb also studied this state with 1.0 fb^{-1} R. Aaij *et al.*, JHEP 1210 (2012) 151



- Found properties:

Name	J^P	Mass (MeV/c^2)	Width (MeV)
$D_{s1}^*(2700)$ (PDG)	1^-	2709 ± 4	117 ± 13

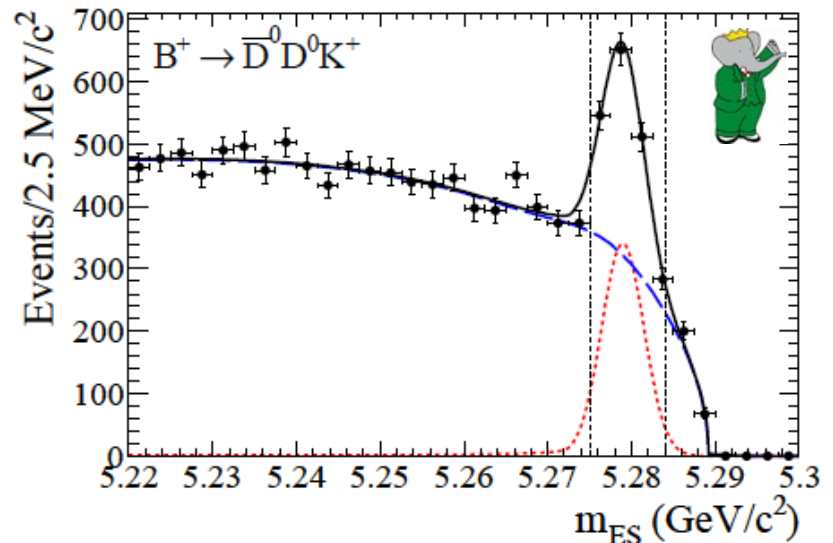
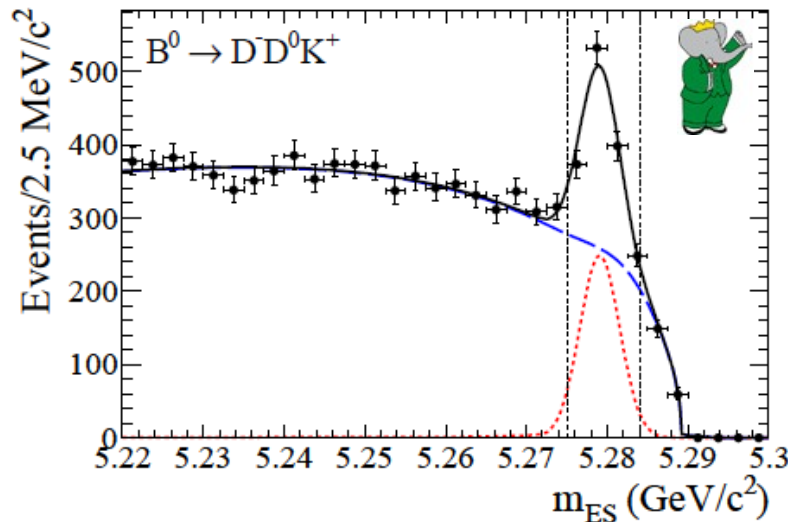
- Our goal here is to study the $D_{s1}(2700)$ *using a full Dalitz analysis*
- We use both $B^0 \rightarrow D^- D^0 K^+$ and $B^+ \rightarrow \bar{D}^0 D^0 K^+$ channels
 - We do not attempt to study channels containing D^* mesons (vector)

The Data Sample

- Run1-Run6, 429 fb⁻¹: $N_{\text{BB}}^- = (470.9 \pm 0.1 \pm 2.8) \times 10^6$
- Exclusive reconstruction
 - $D^0 \rightarrow K^- \pi^+$, $D^0 \rightarrow K^- \pi^+ \pi^0$, $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$
 - $D^+ \rightarrow K^- \pi^+ \pi^+$
 - For $\bar{D}^0 D^0 K^+$, at least one of the D^0 's is required to decay to $K^- \pi^+$
- Use the exact same selection as the analysis on the measurement of 22 branching fractions
 - Based on track quality, Particle ID
 - Invariant D mass
 - Topological variables
 - ΔE cut

The Data Sample, continued

- m_{ES} distribution after the complete selection



- To obtain the Dalitz plot, a cut on m_{ES} is also imposed
- $B^0 \rightarrow D^- D^0 K^+$: 1470 events with a purity of $(38.6 \pm 2.8 \pm 2.1)\%$
- $B^+ \rightarrow \bar{D}^0 D^0 K^+$: 1894 events with a purity of $(41.6 \pm 2.5 \pm 3.1)\%$

Dalitz Plot Analysis

- **Isobar formalism** $\mathcal{M} = \sum_i c_i A_i$
 - c_i : complex coefficients representing the **modulus** and **phase**
 - A_i : complex amplitudes representing the **dynamical function** describing the **intermediate resonance**

- **Likelihood**

$$\mathcal{L} = p \times \varepsilon(m_1^2, m_2^2) \times \frac{|\mathcal{M}|^2}{\int |\mathcal{M}|^2 \varepsilon(m_1^2, m_2^2) dm_1^2 dm_2^2} + (1 - p) \times \frac{B(m_1^2, m_2^2)}{\int B(m_1^2, m_2^2) dm_1^2 dm_2^2}$$

- p : **purity** from m_{ES} fits
- ε is the **efficiency** and B the **background** in the Dalitz plane

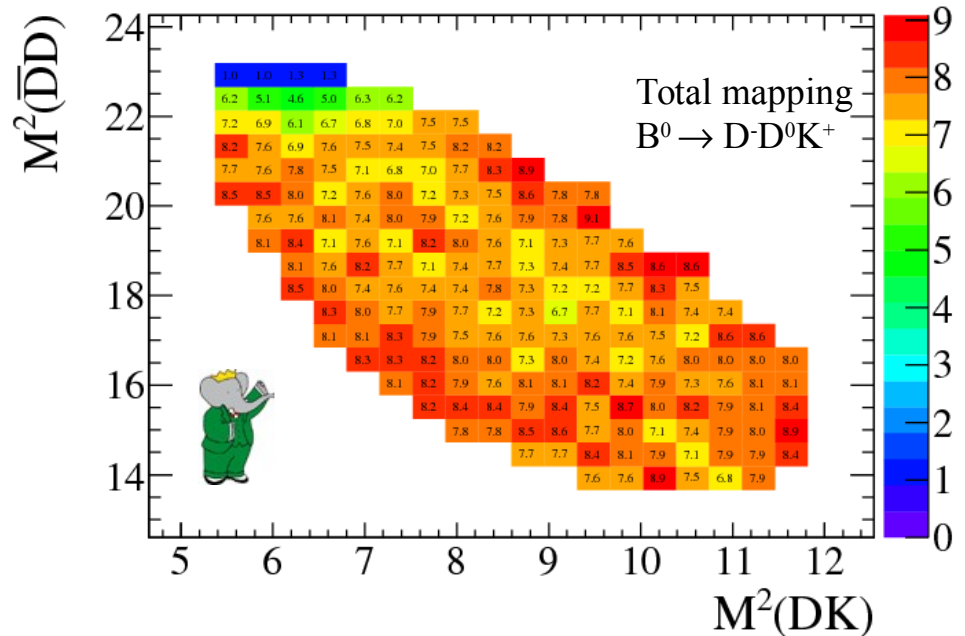
- **Minimizing** $\mathcal{F} = \sum_i -2 \times \log(\mathcal{L}_i)$

- To compare fits we use

$$\Delta\mathcal{F} = \mathcal{F} - \mathcal{F}_{\text{nominal}}$$

Efficiency across the Plot

- Efficiency determined from flat-distribution simulated Dalitz in each D submode
 - 22×22 bins
- Overall efficiency obtained by weighting all D submodes by their Branching Fractions (Bfs)
- Bins are combined if <10 events in the bin
- 2D-Interpolation of the binned efficiencies gives efficiency at any point
- At edge of plot do not use interpolation



Background Term in the Fits

- From generic MC with the same selections as the data
 - We checked using the m_{ES} sideband that the MC correctly reproduces the data
- Histogram the background Dalitz plot (30x30 bins)
 - Non-uniform distribution: no fit done (not expected to fit well)
- Use a 2D-interpolation of the distribution, just as for efficiency

Dalitz Plots

- **Expected** contributions

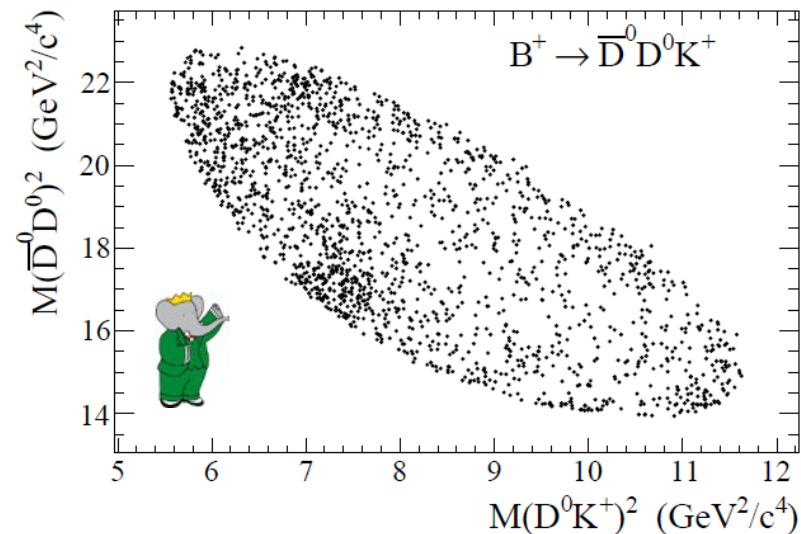
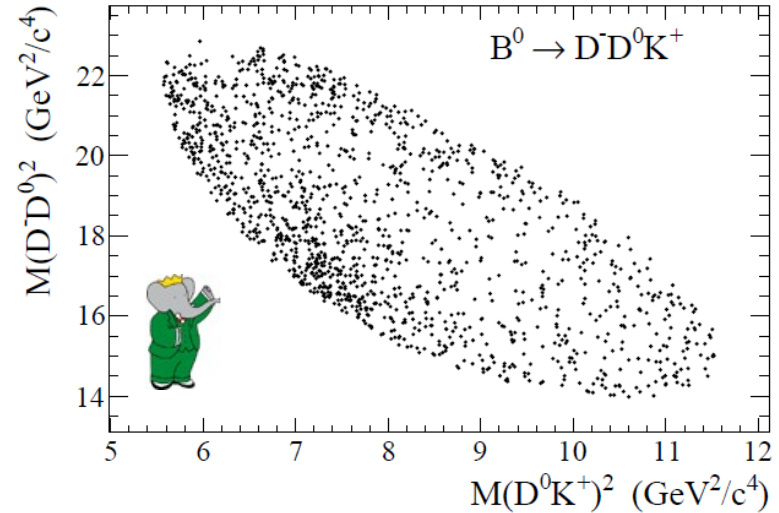
- Nonresonant events
- $D_{s1}(2700) \rightarrow D^0 K^+$
- $D_{s2}^*(2573) \rightarrow D^0 K^+$
 - Has never been observed in DDK
- $D_{sJ}^*(2860) \rightarrow D^0 K^+$
 - Not included in the nominal fit

- **Additional** contributions for $\bar{D}^0 D^0 K^+$

- $\psi(3700) \rightarrow \bar{D}^0 D^0$
- $\psi(4160) \rightarrow \bar{D}^0 D^0$
- $\chi_{c2}(2P)$, $\psi(4040)$, $\psi(4415)$ also possible, not included in the nominal fit

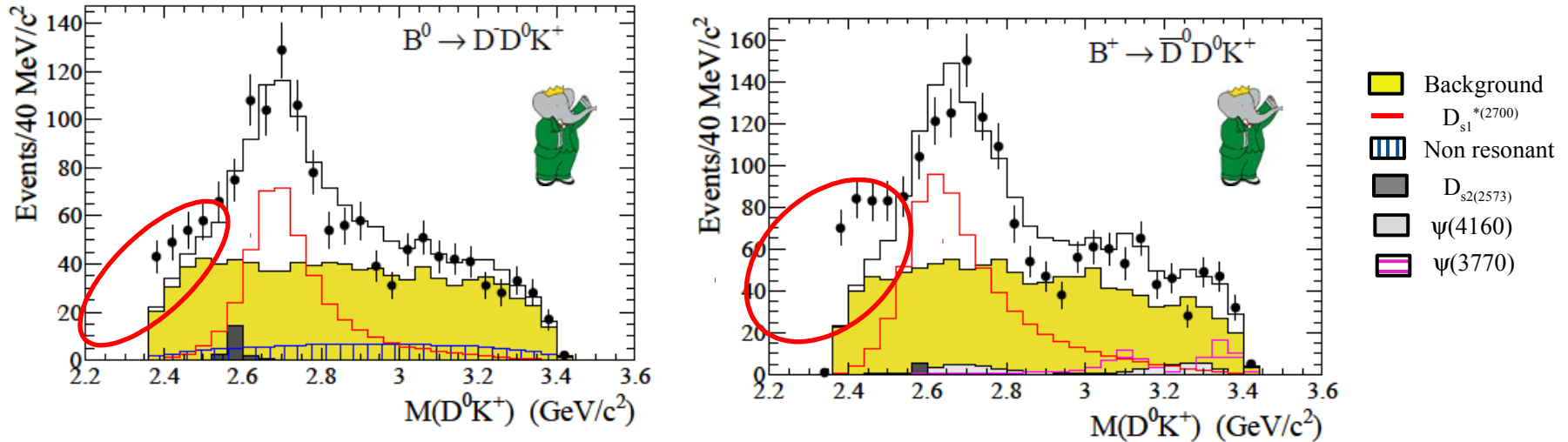
- All resonance parameters **fixed to PDG**, except $D_{s1}(2700)$ parameters

- $D_{s1}(2700)$ is the reference amplitude in the Dalitz fit



Fits with known amplitudes

- Fits with known amplitudes



- Fits are not satisfactory

- $B^0 \rightarrow D D^0 K^+$: $\chi^2/\text{ndof} = 82/48$, $\Delta F = 36$

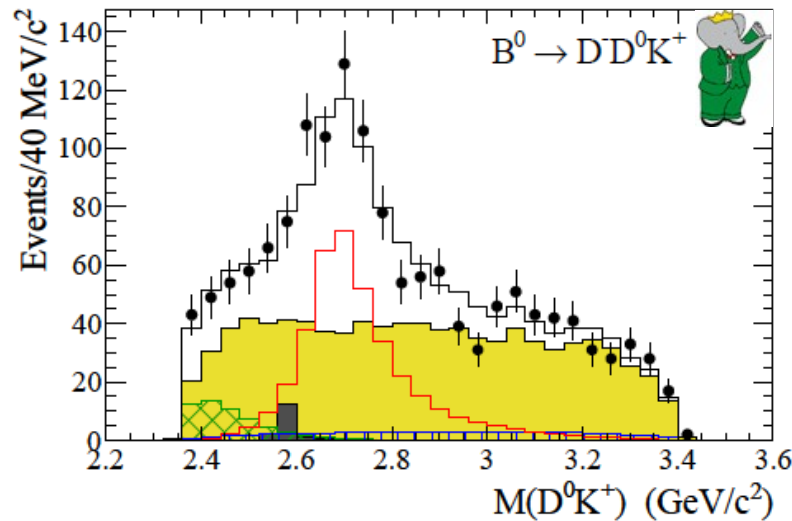
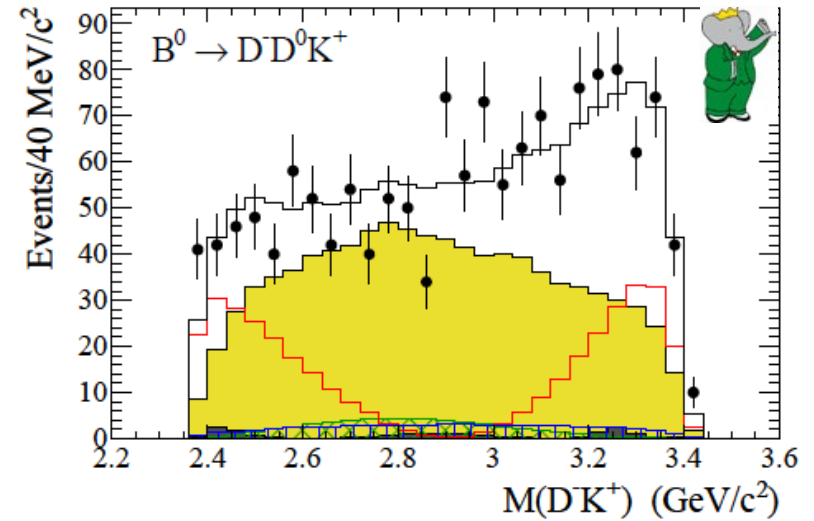
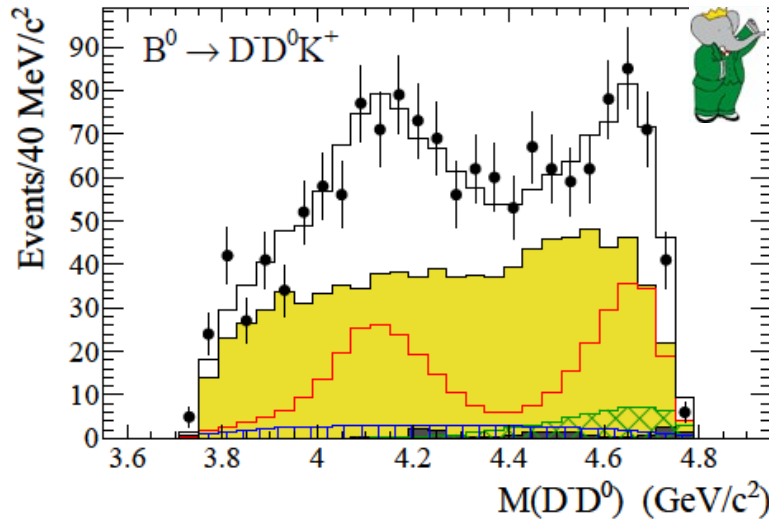
- $B^+ \rightarrow \bar{D}^0 D^0 K^+$: $\chi^2/\text{ndof} = 265/51$, $\Delta F = 223$

- Regions at low $D^0 K^+$ mass not well described

The Low Mass Effect

- Belle also observes this effect in $B^+ \rightarrow \bar{D}^0 D^0 K^+$
- We checked that this contribution is from $B \rightarrow DDK$ signal events and is not background
 - m_{ES} binwise fits: fit m_{ES} in bins of $m(D^0 K^+)$
 - sPlot
- We checked that this is not the reflection of a known resonance in another cross-feed mode
 - No contribution from $D_{s1}(2536) \rightarrow D^* K$
 - No contribution from $D_{s1}(2700) \rightarrow D(^*) K$
- Fits performed adding a scalar amplitude at low mass
 - Quality of fits improves
 - $B^0 \rightarrow D^- D^0 K^+$: $M_{\text{scalar}} = 2412 \pm 16 \text{ MeV}$, $\Gamma_{\text{scalar}} = 163 \pm 64 \text{ MeV}$
 - $B^+ \rightarrow \bar{D}^0 D^0 K^+$: $M_{\text{scalar}} = 2453 \pm 20 \text{ MeV}$, $\Gamma_{\text{scalar}} = 283 \pm 45 \text{ MeV}$
 - We reject this solution
 - Only $\sim 1.5\sigma$ different
 - Such a wide resonance at this mass would be speculative
- It is not possible to conclude that a resonance contributes here
 - We use an arbitrary function to describe it
 - Exponential function $A_{\text{ExpO}} = e^{-\alpha(m_2^2 - m_{2\text{thr}}^2)}$
 - (Some authors integrate this term into the nonresonant one)

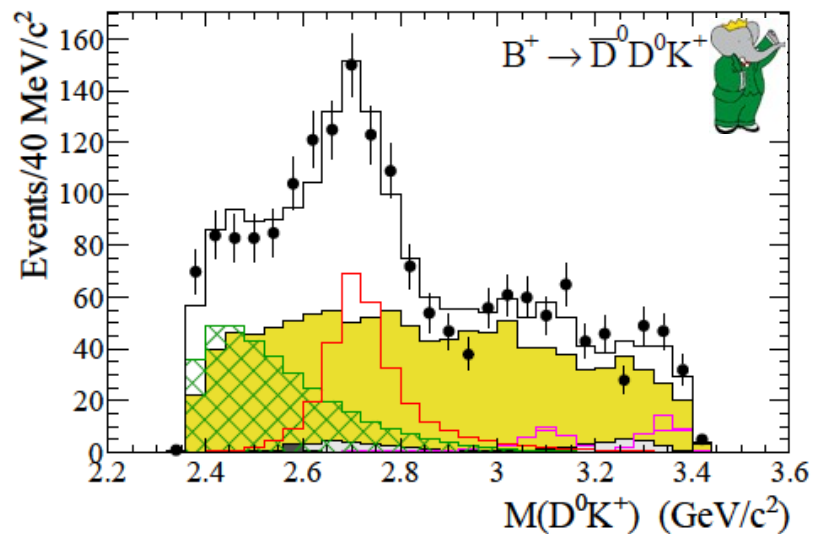
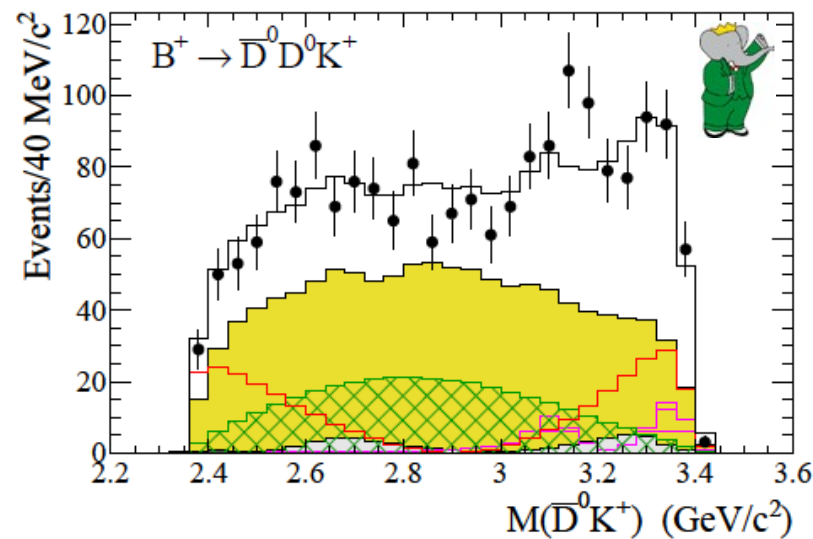
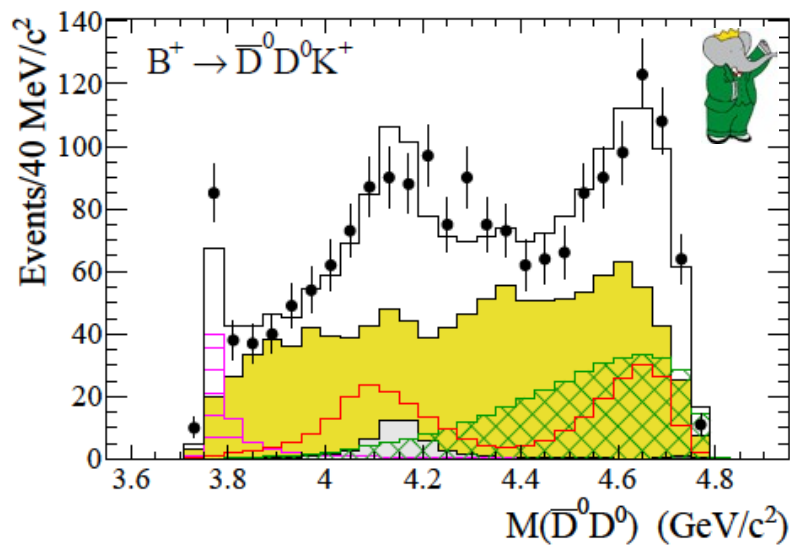
The Nominal Fit: B^0



- Background
- $D_{s1}^*(2700)$
- Nonresonant
- $D_{s2}(2573)$
- Exponential

$$\chi^2/\text{ndof} = 56/45$$

The Nominal Fit: B^+



- Background
- $D_{s1}^*(2700)$
- $D_{s2}(2573)$
- $\psi(4160)$
- $\psi(3770)$
- Exponential

$$\chi^2/\text{ndof} = 86/48$$

Nominal Fits, continued

- Each fit result is in fact the **best fit** among 250; these use **randomized** initial parameters [within their bounds].
 - Choose the **smallest negative log likelihood**
 - Avoids **local minima** (as opposed to the global minimum)
- We reject **nonconverging fits** + fits with fit fraction sum $> 250\%$
 - Due to the **unusually large interference** between the exponential and the non-resonant components for $B^0 \rightarrow D^- D^0 K^+$
- We include in the **systematics** the small differences in the resonance parameters for the fits **close to the minimum**
- The presence of several close minima is confirmed **by toy MC**

Systematic Effects

- Fit bias

- Generate **toy MC samples** using the fit parameters and fit these toys to extract the fit bias

- Efficiency

- **Raw efficiency** instead of interpolation
- **Statistical fluctuation** taken into account by randomizing (within stat. uncertainty) the efficiency in each bin

- Background description

- **Signal purity** varied according to its total uncertainty

- Fit model

- **Blatt-Weisskopf** factor varied from 0 to 5 GeV^{-1} (nominal 1.5 GeV^{-1})
- **Low-mass effect**: use a scalar fit or an alternative arbitrary function
- **$\psi(3770)$** : using KEDR exp. results instead of PDG values
- **$D_{s2}(2573)$** : fit repeated without this (small) contribution

- Local minima

- Use the **other** minima (close enough to the global one)

Estimates of Systematic errors

Units are MeV/c² (for M), MeV (for Γ)

- Breakdown of systematic errors on the $D_{s1}(2700)$ parameters

$$B^0 \rightarrow D \bar{D}^0 K^+$$

Parameter	Value	Bias	Eff.	Eff. II	Bkg	BW	Low mass	D_{s2}^*	Min.	Total
$M(D_{s1}^*(2700)^+)$	2694	± 2	0	± 1	0	$^{+13}_{-2}$	$^{+0}_{-1}$	0	$^{+3}_{-0}$	$^{+13}_{-3}$
$\Gamma(D_{s1}^*(2700)^+)$	145	± 8	± 1	± 3	$^{+4}_{-3}$	$^{+17}_{-9}$	$^{+5}_{-0}$	-6	$^{+11}_{-4}$	$^{+22}_{-14}$

$$B^+ \rightarrow \bar{D}^0 D^0 K^+$$

Parameter	Value	Bias	Eff.	Eff. II	Bkg	BW	Low mass	D_{s2}^*	ψ	Min.	Total
$M(D_{s1}^*(2700)^+)$	2707	± 4	0	± 1	± 3	$^{+7}_{-4}$	$^{+0}_{-4}$	+1	0	$^{+0}_{-5}$	± 8
$\Gamma(D_{s1}^*(2700)^+)$	113	± 5	± 1	± 3	$^{+9}_{-7}$	$^{+17}_{-0}$	$^{+0}_{-9}$	-5	+2	$^{+0}_{-7}$	$^{+20}_{-16}$

Results

- $D_{s1}(2700)$ observed for the first time in $B^0 \rightarrow D D^0 K^+$ decays
- Low-mass effect has an important contribution
- $D_{s2}(2573)$ observed with a 3.4σ significance (including systematics) in $B^0 \rightarrow D D^0 K^+$
- $\psi(4160)$ observed with a 3.3σ significance (including systematics) in $B^+ \rightarrow D^0 D^0 K^+$
- No need for $D_{sJ}^*(2860)$, $D_{sJ}(3040)$, $\chi_{c2}(2P)$, $\psi(4040)$, $\psi(4415)$

$$B^0 \rightarrow D D^0 K^+$$

Contribution	Modulus	Phase (°)	Fraction (%)
$D_{s1}^*(2700)^+$	1.00	0	$66.7 \pm 7.8^{+3.5}_{-3.8}$
$D_{s2}^*(2573)^+$	$0.031 \pm 0.008 \pm 0.002$	$277 \pm 17^{+6}_{-9}$	$3.2 \pm 1.6^{+0.3}_{-0.4}$
Nonresonant	$1.33 \pm 0.63^{+0.46}_{-0.35}$	$287 \pm 21^{+10}_{-15}$	$10.9 \pm 6.6^{+7.0}_{-4.3}$
Exponential	$6.94 \pm 1.83^{+0.82}_{-0.43}$	$269 \pm 33^{+17}_{-15}$	$9.9 \pm 2.9^{+3.0}_{-3.3}$
Sum			$90.6 \pm 10.7^{+8.4}_{-6.7}$

$$B^+ \rightarrow \bar{D}^0 D^0 K^+$$

Contribution	Modulus	Phase (°)	Fraction (%)
$D_{s1}^*(2700)^+$	1.00	0	$38.3 \pm 5.0^{+0.8}_{-6.2}$
$D_{s2}^*(2573)^+$	$0.021 \pm 0.010^{+0.009}_{-0.003}$	$267 \pm 30^{+17}_{-13}$	$0.6 \pm 1.1^{+0.4}_{-0.2}$
$\psi(3770)$	$1.40 \pm 0.21^{+0.20}_{-0.24}$	$284 \pm 22^{+26}_{-30}$	$9.0 \pm 3.1^{+0.4}_{-0.8}$
$\psi(4160)$	$0.78 \pm 0.20^{+0.18}_{-0.14}$	$188 \pm 13^{+14}_{-17}$	$6.4 \pm 3.1^{+1.9}_{-2.4}$
Exponential	$16.15 \pm 2.26^{+1.09}_{-1.74}$	$308 \pm 8^{+6}_{-5}$	$44.5 \pm 6.2^{+1.3}_{-2.1}$
Sum			$98.9 \pm 9.2^{+2.5}_{-7.0}$

Branching Fractions

- We measure the partial branching fractions of the resonances
- We use f_{res} , the fit fraction of the resonance and B_{tot} , the total branching fraction of the mode measured in our previous publication

$$\mathcal{B}_{\text{res}} = f_{\text{res}} \times \mathcal{B}_{\text{tot}}$$

Mode	$\mathcal{B} (10^{-4})$
$B^0 \rightarrow D^- D_{s1}^* (2700)^+ [D^0 K^+]$	$7.14 \pm 0.96 \pm 0.69$
$B^+ \rightarrow \bar{D}^0 D_{s1}^* (2700)^+ [D^0 K^+]$	$5.02 \pm 0.71 \pm 0.93$
$B^0 \rightarrow D^- D_{s2}^* (2573)^+ [D^0 K^+]$	$0.34 \pm 0.17 \pm 0.05$
$B^+ \rightarrow \bar{D}^0 D_{s2}^* (2573)^+ [D^0 K^+]$	$0.08 \pm 0.14 \pm 0.05$
$B^+ \rightarrow \psi(3770) K^+ [\bar{D}^0 D^0]$	$1.18 \pm 0.41 \pm 0.15$
$B^+ \rightarrow \psi(4160) K^+ [\bar{D}^0 D^0]$	$0.84 \pm 0.41 \pm 0.33$

$D_{s1}(2700)$ results

- Mass and width of the $D_{s1}(2700)$ for the two modes

Mode	Mass (MeV/ c^2)	Width (MeV)
$B^0 \rightarrow D^- D^0 K^+$	$2694 \pm 8^{+13}_{-3}$	$145 \pm 24^{+22}_{-14}$
$B^+ \rightarrow \bar{D}^0 D^0 K^+$	$2707 \pm 8 \pm 8$	$113 \pm 21^{+20}_{-16}$

- The two modes are **in agreement** within their uncertainties
- The two measurements are combined by computing a **weighted mean** taking into account the asymmetric uncertainties; this works well for all **uncorrelated** uncertainties. The Blatt-Weisskopf factor uncertainties are *correlated*, so these are removed from the combination, and taken accounted for later in a conservative fashion.

$D_{s1}(2700)$ results, continued

- Mass and width after **combining modes** (with total uncertainties)

$$M(D_{s1}^*(2700)^+) = 2699_{-7}^{+14} \text{ MeV}/c^2,$$

$$\Gamma(D_{s1}^*(2700)^+) = 127_{-19}^{+24} \text{ MeV},$$



- Compatible** with the world average

$$M(D_{s1}^*(2700)^+) = 2709 \pm 4 \text{ MeV}/c^2$$

$$\Gamma(D_{s1}^*(2700)^+) = 117 \pm 13 \text{ MeV}$$

- Spin** of $D_{s1}(2700)$

- Analysis performed with $J = 1$
- Fits repeated with **$J = 0$ and $J = 2$**

Mode	$J = 0$		$J = 1$		$J = 2$	
	$\Delta\mathcal{F}$	χ^2/n_{dof}	χ^2/n_{dof}	$\Delta\mathcal{F}$	χ^2/n_{dof}	χ^2/n_{dof}
$B^0 \rightarrow D^- D^0 K^+$	131	131/45	56/45	108	125/45	
$B^+ \rightarrow \bar{D}^0 D^0 K^+$	63	137/48	86/48	99	145/48	

- Assuming parity conservation,
we deduce $D_{s1}(2700)$ is a 1^- state

Conclusions

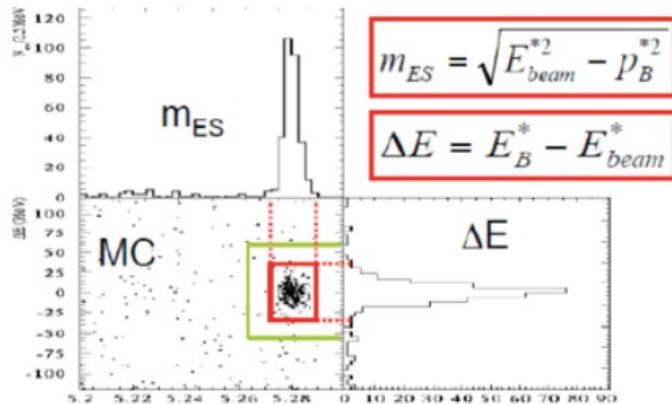


- We performed a Dalitz analysis of the modes $B^0 \rightarrow D^- D^0 K^+$ and $B^+ \rightarrow \bar{D}^0 D^0 K^+$
 - We extract moduli and phases for all contributions
- We observe the $D_{s1}(2700)$ meson in both final states
 - We measure precisely its **mass and width**
- We observe an **enhancement** between 2350 and 2500 MeV in the $D^0 K^+$ invariant mass
 - We are **not able** to interpret this effect
 - It is described in the fit by an **ad-hoc function**
 - Could be a **new D_s** excited state?
 - A specific form of a **nonresonant amplitude**?
 - More information will be brought by **LHCb** and **Belle II**
- We do not observe the $D_{sJ}(2860)$ and $D_{sJ}(3040)$ in these final states

ADDITIONAL SLIDES

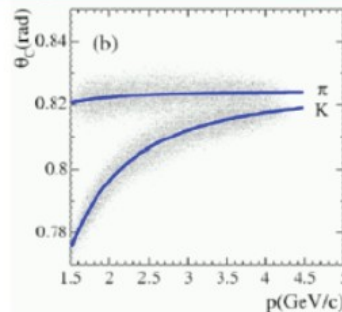
Common analysis techniques

Kinematics of fully reconstructed B



K/ π separation

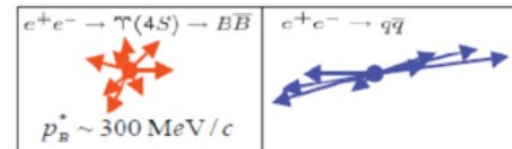
Very good
particle ID
between 1.5
and 4 GeV/c



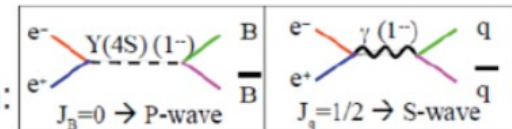
Background discrimination

Suppression by **multi-variable classifiers** based on **event-shape variables**:
Fisher discriminant, Boosted Decision Trees (BTD)...

Topology:



Angular distribution:



- Strongly discriminate continuum events ($e^+e^- \rightarrow q\bar{q}$ ($q = u, d, s, c$))
- Background from B decays

Variables are often combined to a **likelihood function**, used in a **maximum likelihood fit** for signal/background separation and to measure parameters of interest

EVENT SELECTION

Selection for the primary charged K	Selection for the primary neutral K
1 - GoodTrackLoose + KLHNotAPion 2 - KLHTight	1 - $ M(K_s^0) - M(K_s^0)_{PDG} < 9.5 \text{ MeV}/c^2$ + $p(\chi^2) > 0.1\%$ + Length of flight $> 2 \text{ mm}$
Selection for $D^0 \rightarrow K^- \pi^+$	Selection for $D^0 \rightarrow K^- \pi^+ \pi^0$
1 - $ M(D^0) - M(D^0)_{Meas.} < 2.5\sigma$ + K KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - K KLHTight	1 - $ M(D^0) - M(D^0)_{Meas.} < 2.5\sigma$ + K KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - K KLHTight 3 - Dalitz weight > 10
Selection for $D^0 \rightarrow K^- \pi^+ \pi^- \pi^+$	Selection for $D^+ \rightarrow K^- \pi^+ \pi^+$
1 - $ M(D^0) - M(D^0)_{Meas.} < 2.5\sigma$ + K KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - K KLHTight	1 - $ M(D^+) - M(D^+)_{Meas.} < 2.5\sigma$ + K KLHNotAPion + $p(\chi^2) > 0.1\%$ 2 - K KLHTight
Selection for $D^{*+} \rightarrow D^0 \pi^+, D^+ \pi^0$	Selection for $D^{*0} \rightarrow D^0 \pi^0, D^0 \gamma$
1 - $ \Delta M - \Delta M_{PDG} < 3 \text{ MeV}/c^2$ where $\Delta M = M(D^{*+}) - M(D^0/D^+)$ + $p^*(\pi) < 450 \text{ MeV}/c$ + D^0/D^+ selection steps described above	1 - $\Delta M \in [138, 146] (D^0 \pi^0), [130, 150] (D^0 \gamma) \text{ MeV}/c^2$ where $\Delta M = M(D^{*0}) - M(D^0)$ + $p^*(\pi^0) < 450 \text{ MeV}/c + E(\gamma) > 100 \text{ MeV}$ + D^0 selection steps described above
Selection for B	Final step
1 - $D^{(*)}$ and K at least satisfying the level of selection 1 described above + $R_2 < 0.3$ + $ \cos(\theta_B) < 0.9$	1 - Best ΔE candidate + ΔE cut (see Table 5 of BAD 2141) + m_{ES} cut (see text)