

GEANT4 Hadronic Cross Section Optimizations

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RESEARCH \ ENGAGEMENT \ INNOVATION

Background CrossSection Calculation

- Hadronic CrossSections

*51 real events simulated in ~2 hours
(provided by Soon)

- ~10% of total wall clock time*
- Deep call chain with no hot spots
 - Reduce call chain length
 - Reduce time spent in calculation

| Scope | WALLCLOCK (us)[0,0] (E) | WALLCLOCK (us)[0,0] (I) |
|--|-------------------------|-------------------------|
| Experiment Aggregate Metrics | 1.29e+09 100 % | 1.29e+09 100 % |
| main | 1.29e+09 100 % | 1.29e+09 100 % |
| ↳ 131: G4UImanager::ApplyCommand(char const*) | | 1.28e+09 99.3% |
| ↳ 422: G4Uicommand::DoIt(G4String) | | 1.28e+09 99.3% |
| ↳ 210: G4UicontrolMessenger::SetNewValue(G4Uicommand*, G4String) | | 1.28e+09 99.3% |
| ↳ 277: G4UImanager::ExecuteMacroFile(char const*) | | 1.28e+09 99.3% |
| ↳ 234: G4Uibatch::SessionStart() | | 1.28e+09 99.3% |
| ↳ 215: G4Uibatch::ExecCommand(G4String const&) | | 1.28e+09 99.3% |
| ↳ 170: G4UImanager::ApplyCommand(char const*) | | 1.28e+09 99.3% |
| ↳ 422: G4Uicommand::DoIt(G4String) | | 1.28e+09 99.3% |
| ↳ 210: G4RunMessenger::SetNewValue(G4Uicommand*, G4String) | | 1.28e+09 99.3% |
| ↳ 287: G4RunManager::BeamOn(int, char const*, int) | | 1.28e+09 99.3% |
| ↳ 155: G4RunManager::DoEventLoop(int, char const*, int) | | 1.26e+09 97.1% |
| ↳ 237: G4RunManager::ProcessOneEvent(int) | | 1.26e+09 97.1% |
| ↳ 264: G4EventManager::DoProcessing(G4Event*) | 9.34e+05 0.1% | 1.26e+09 97.1% |
| ↳ 185: G4TrackingManager::ProcessOneTrack(G4Track*) | 2.98e+06 0.2% | 1.25e+09 96.6% |
| ↳ 125: G4SteppingManager::Stepping() | 5.61e+06 0.4% | 1.17e+09 90.8% |
| ↳ 180: G4VProcess::AlongStepG4PIL(G4Track const&, double, double, double&, G4GPILSelection*) | 2.27e+05 0.0% | 5.64e+08 43.6% |
| ↳ 458: G4Transportation::AlongStepGetPhysicalInteractionLength(G4Track const&, double, double, double&, G4GPILSelection*) | 9.47e+06 0.7% | 5.20e+08 40.2% |
| ↳ 321: G4PropagatorInField::ComputeStep(G4FieldTrack&, double, double&, G4VPhysicalVolume*) | 1.00e+07 0.8% | 3.45e+08 26.7% |
| ↳ 286: G4ChordFinder::AdvanceChordLimited(G4FieldTrack&, double, double, CLHEP::Hep3Vector, double) | 2.51e+06 0.2% | 2.29e+08 17.7% |
| ↳ 202: G4MagInt_Driver::AccurateAdvance(G4FieldTrack&, double, double, double) | 2.40e+06 0.2% | 1.17e+08 9.1% |
| ↳ 185: G4ChordFinder::FindNextChord(G4FieldTrack const&, double, G4FieldTrack&, double&, double, double, CLHEP::Hep3Vector const&) | 4.28e+06 0.3% | 9.35e+07 7.2% |
| ↳ 323: G4MultiLevelLocator::EstimateIntersectionPoint(G4FieldTrack const&, G4FieldTrack const&, CLHEP::Hep3Vector const&) | 2.29e+06 0.2% | 1.02e+08 7.9% |
| ↳ 210: G4ChordFinder::ApproxCurvePointV(G4FieldTrack const&, G4FieldTrack const&, CLHEP::Hep3Vector const&, double) | 1.02e+06 0.1% | 6.01e+07 4.6% |
| ↳ 298: G4VIntersectionLocator::IntersectChord(CLHEP::Hep3Vector const&, CLHEP::Hep3Vector const&, double&, double) | 8.82e+05 0.1% | 1.52e+07 1.2% |

Cross Section Usage

- Cross section calculation is used to:
 - Determine (probabilistically) whether an interaction occurs in traversing a particular geometric volume.
 - Then determine reaction and outcomes.
- CrossSectionDataStore instances created for 65 different processes.
 - Each of these uses different models for different energy domains, particles, materials.
 - Data is (usually) represented in sub-classes of G4PhysicsVector.
- We have been working on increasing the performance of the CrossSection calculations.

Two strategies

- Improved caching of CrossSection results
 - 1 cache entry per *triple* (process/particle/material)
 - Completed (In the pipeline toward production code)
- Surrogate model for CrossSection calculations
 - Prototype completed
 - Initial results are promising

Caching CrossSection Results

- Currently, there is a 1-entry cache per process for XC calculations.
- Observation
 - There is an interleaving of recent calls to GetCrossSection with the same sets of particle, material, process, and energy.
 - Results in same cross section value
 - True even though energy is a double! (The physics is causing this.)
- Optimization
 - Expanded cache recent the most recent cross section for particle, material, process triple.
- Measurements
 - 17% of calls would benefit from this cache
 - 29% of GetCrossSection cycles are from these calls.
 - ~18k triples total
 - ~3k triples would benefit

Caching CrossSection Results

- Implementation
 - Hashtable per process (i.e. per CrossSectionDataStore)
 - `std::unordered_map`
 - One cache entry for each particle/material pair
 - Key
 - material
 - particle definition
 - Value
 - particle energy
 - cross section (including `xsecelm`)

Modified CrossSection Calculation

```
G4double G4CrossSectionDataStore::GetCrossSection(part,mat){
    ...
    entry = process_cache_map[(part,mat)];
    if(entry->energy == part->GetKineticEnergy()){
        xsecelm = entry->xsecelm;
        crossSection = entry->crossSection;
    } else
        //Calculate CrossSection the regular way (including xsecelm)
        ...
        entry->xsecelm = xsecelm;
        entry->crossSection = crossSection;
    }
    return crossSection;
}
```

Caching CrossSection Results

- Performance increase
 - 1.8% reduction in wall clock time (51 real events simulated over 2+ hours)
- Presented at Hadronic working group
 - What is the state of this being put in the production code?

Surrogate Model: XS Usage

In the Hadronic section of the code:

- Particle/Material/Process Triples
 - 50% of cycles in ~10 triples
 - 90% of cycles in ~85 triples
 - Total ~18k triples
- Implementing for tens of triples can utilize fast path for nearly all of the calls.

Surrogate Model

- The cross section of an interaction between a particle and a complex material is (re-computed) on each call.
 - Look up each isotope. Use element and isotope abundance tables to weight the result.
- Typical materials
 - Air, Stainless steel, PbZrO_4 , Cu, Teflon, Circuit boards, ...
- Stainless = { ^{12}C , ^{13}C , (^{14}C), ^{54}Fe , (^{55}Fe), ^{57}Fe , ^{58}Fe , ^{60}Fe , (^{50}Cr), ^{52}Cr , ^{53}Cr , ^{54}Cr , ^{55}Mn , ^{58}Ni , ^{60}Ni , ^{61}Ni , ^{62}Ni , ^{64}Ni , ^{28}Si , ^{29}Si , ^{30}Si }
- Previous versions of G4 used “pseudoelements” based on natural abundances. This was judged inadequate for the “what happened” calculations.

Building the Surrogate Model

- Create fast path for CrossSection calculations (offline or in initialization).
 - Identify common (particle, material, process) triples.
 - The number chosen depends on how much extra storage can be used.
 - Create Surrogate Model
 - Over sample using existing physics model.
 - Down sample to a simpler model with bounded error.
 - Evenly spaced sample points in E , $\ln(E)$, or $\log(E)$
 - Or piecewise linear with adaptively placed nodes (Douglas-Peucker method).
 - Solve a linear system to adjust Y values to remove bias from the sign of the errors in each interval.
 - Represent the reduced model using existing G4PhysicsVector sub-classes.
- For triples where the fast path exists, use it for the mean free path (interaction length) calculations.
 - Single query of a G4PhysicsVector
- When an interaction occurs (rare)
 - Perform original physics calculations

Building the Surrogate Model

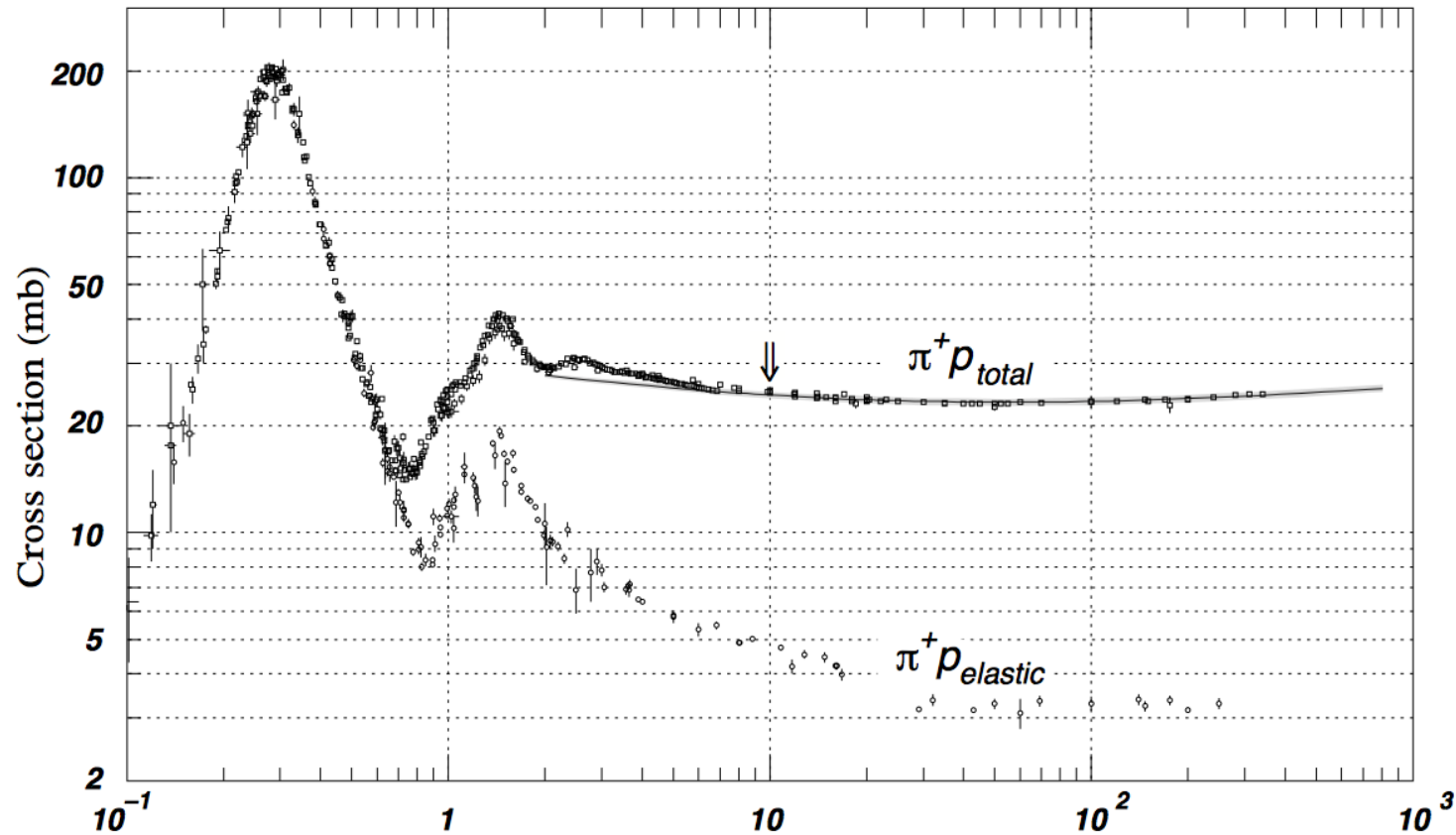
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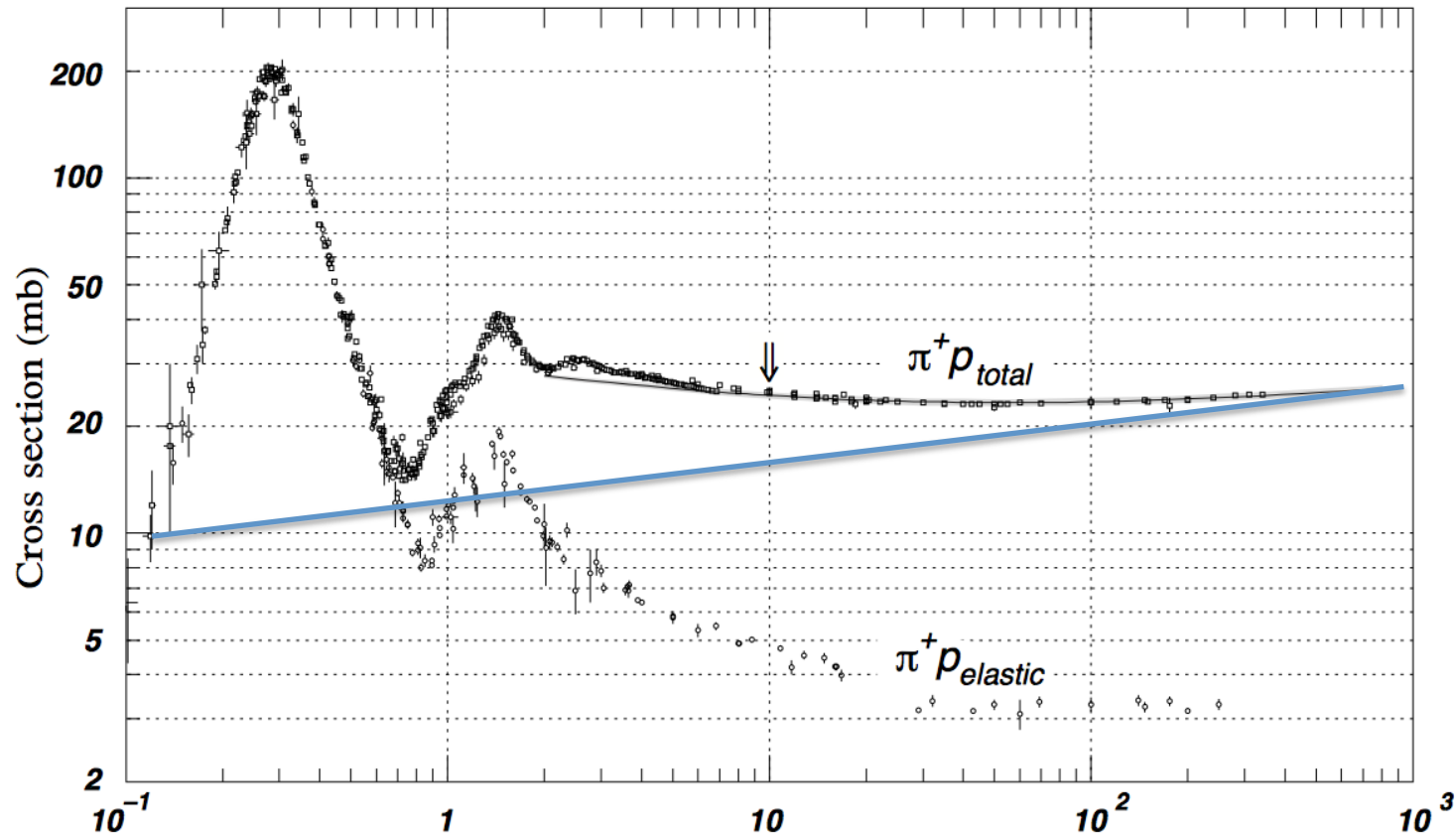
Building the Surrogate Model

Over sample the existing code.



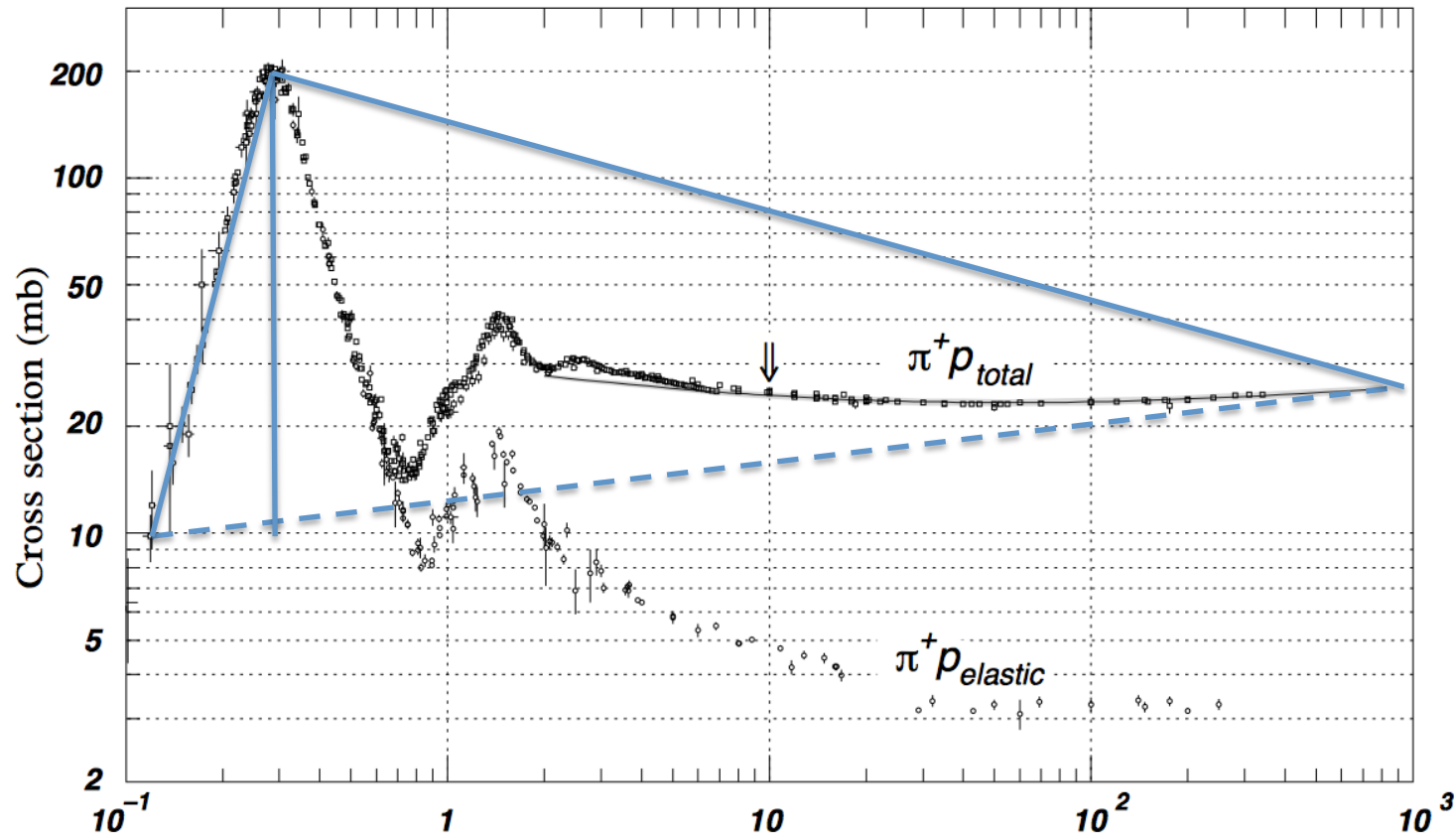
Douglas-Peucker Approximation.

Start with a piecewise-linear approximation.
In each segment, Add the point at the largest error.
Until total error is within the required bound.



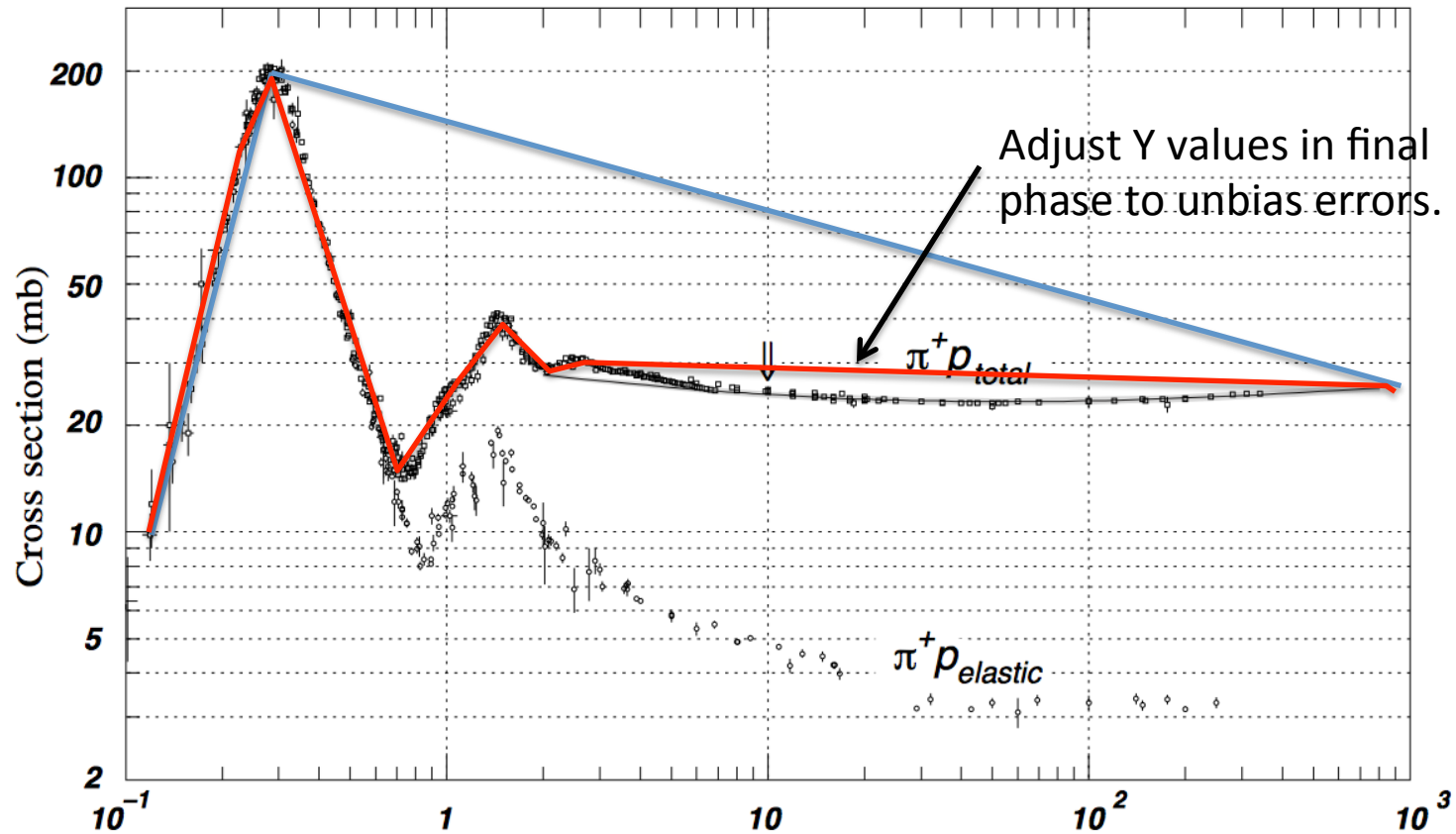
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Existing CrossSection Calculation

```
G4double G4CrossSectionDataStore::GetCrossSection(part,mat){
    ...
    if(mat == currentMaterial && part->GetDefinition() == matParticle
        && part->GetKineticEnergy() == matKinEnergy)
    { return matCrossSection; }

    //Calculate CrossSection the regular way (including xsecelm)
    ...
}

G4double G4CrossSectionDataStore::SampleZandA(part,mat){
    ...
    G4double cross = GetCrossSection(part, mat);
    ...
}
```

Modified CrossSection Calculation

```
G4double G4CrossSectionDataStore::GetCrossSection(part,mat,requireSlowPath){
    ...
    if(!requireSlowPath){
        fast_entry = (*fastPathMap)[searchkey];
    }
    if (!requireSlowPath && fast_entry != NULL){
        matCrossSection=GetCrossSectonFastPath(fast_entry,part);
    } else {
        //Calculate CrossSection the regular way (including xsecelm)
    }
    ...
}

G4double G4CrossSectionDataStore::SampleZandA(part,mat){
    ...
    G4double cross = GetCrossSection(part, mat, true);
    ...
}
```

Fast Path Usage: Runtime

| Triples | Samples | Tolerance | Time | Percent Diff |
|----------------|---------|-----------|-------|--------------|
| 90% | 250K | 1E-05 | 82:36 | 8.0% |
| 90% | 10K | 1E-06 | 85:26 | 6.1% |
| 90% | 500K | 1E-05 | 87:07 | 5.1% |
| 90% | 200K | 1E-06 | 89:03 | 3.8% |
| Slow Path Only | N/A | N/A | 94:57 | 0.0% |
| 90% | 2M | 1E-06 | 99:18 | -2.8% |

Fast Path Usage: Cycles

| Samples | Tol | Cyc/Op (fast) | Cyc/Op (slow) | Cyc/Op (avg) | Init Cycles | Cyc/Op (avg) w/ init | Total Calls |
|---------|------|---------------|---------------|--------------|-------------|----------------------|---------------|
| 2M | 1E-6 | 274 | 3982 | 839 | 2.77E+12 | 2731 | 1,468,837,903 |
| 1M | 1E-6 | 252 | 3936 | 811 | 1.24E+12 | 1651 | 1,475,681,237 |
| 500K | 1E-5 | 240 | 3873 | 786 | 2.58E+11 | 962 | 1,467,516,422 |
| 250K | 1E-5 | 230 | 3981 | 801 | 1.23E+11 | 884 | 1,486,080,112 |
| 10K | 1E-6 | 242 | 3882 | 820 | 6.17E+9 | 824 | 1,520,218,543 |

Questions?