

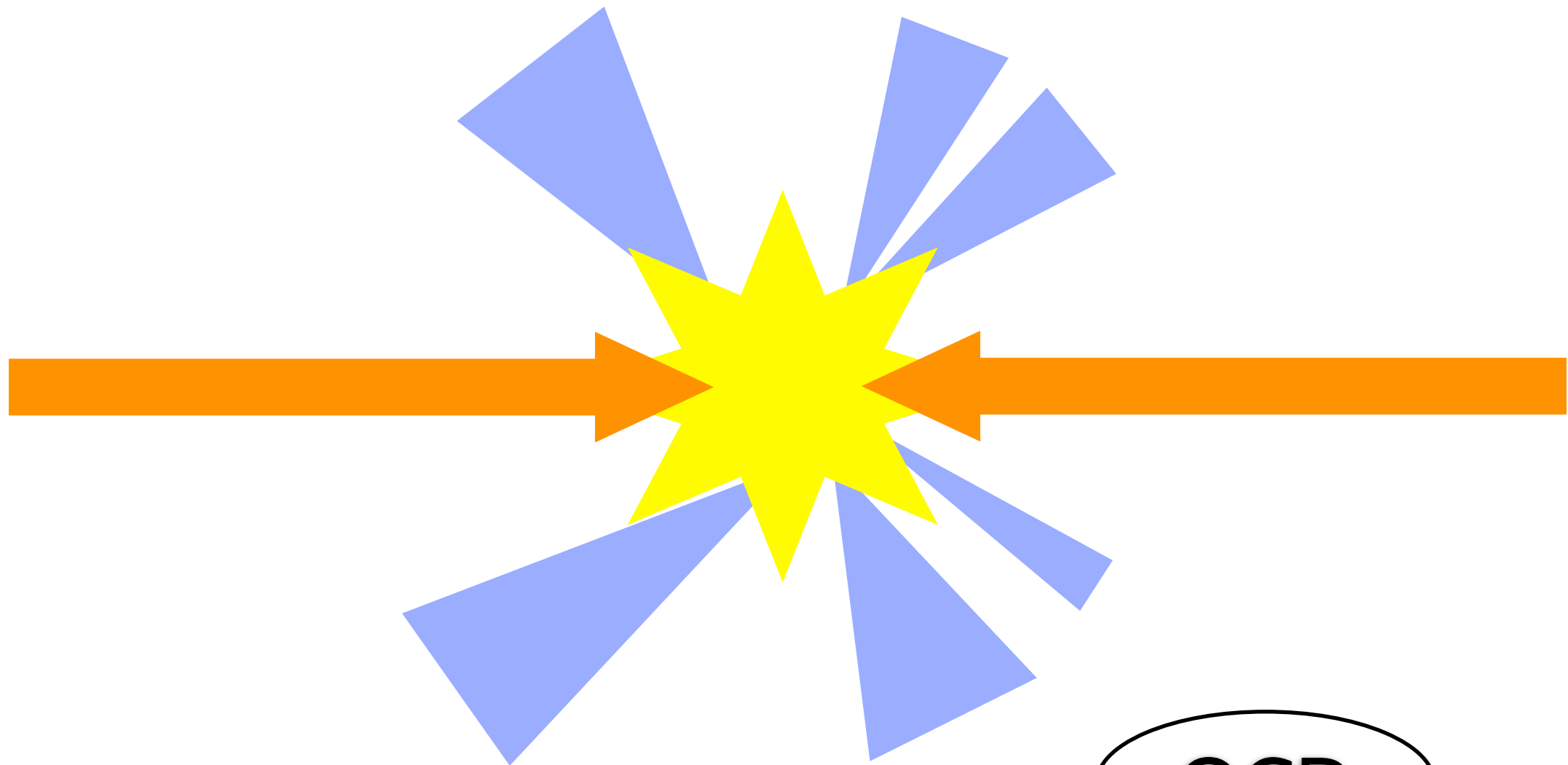


# Evolution variable dependence on jet substructure

**Yasuhito Sakaki**  
KEK, SOKENDAI

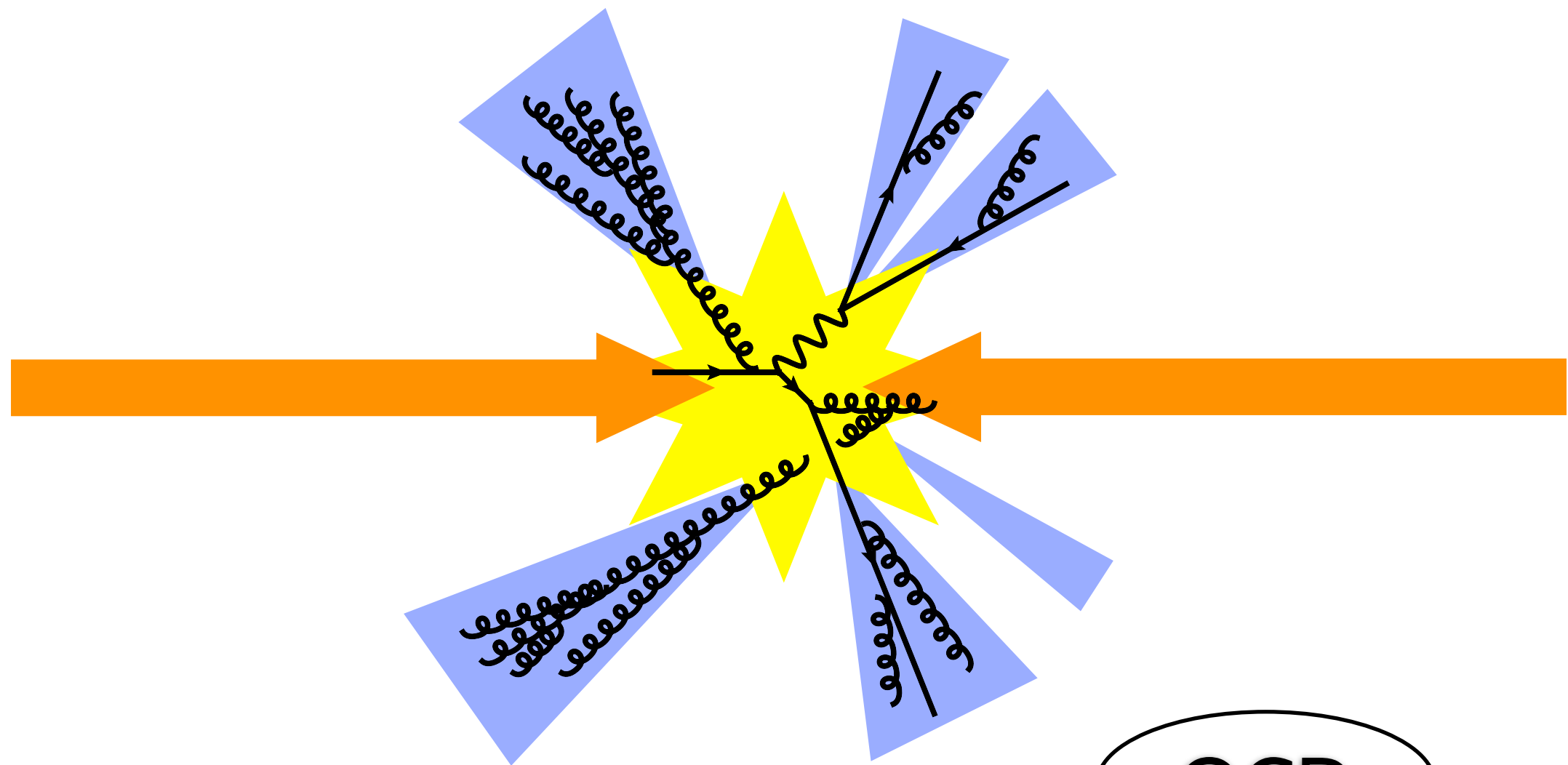
MC4BSM, May 20, 2015 @Fermilab

MC tools predict very well jet properties  
(jet number, momenta, shape...)



How about internal structure of the jets?

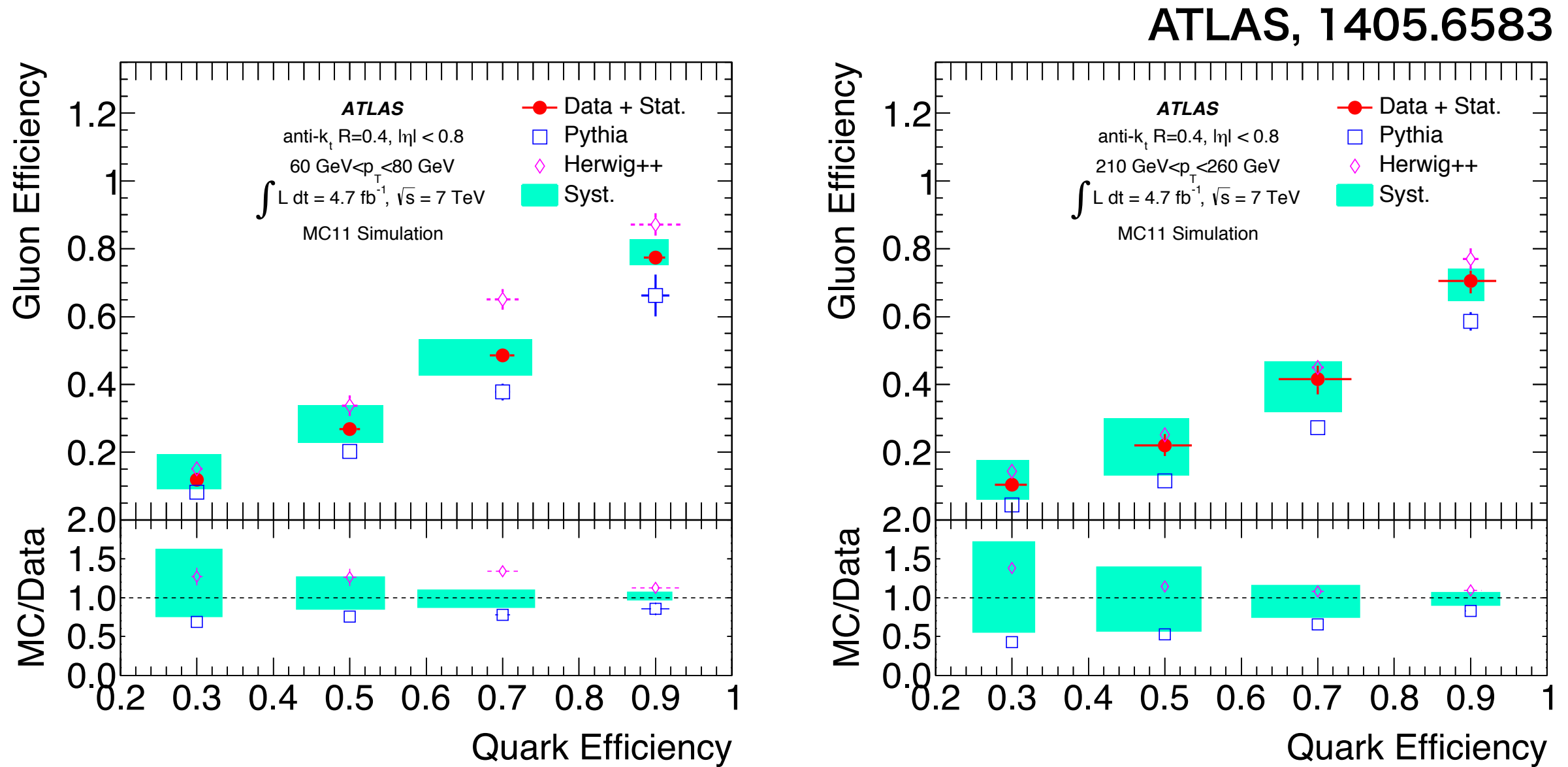
MC tools predict very well jet properties  
(jet number, momenta, shape...)



QCD

How about internal structure of the jets?

# MC dependence on QCD jet substructure



Data lies between **Pythia** and **Herwig**



# Why different?

- It's difficult to answer easily due to many sources of difference among generators...
- Jet substructure is basically formed by QCD radiations (**parton shower**)
- **Evolution variable** is core in parton shower
- Equivalent choices are possible

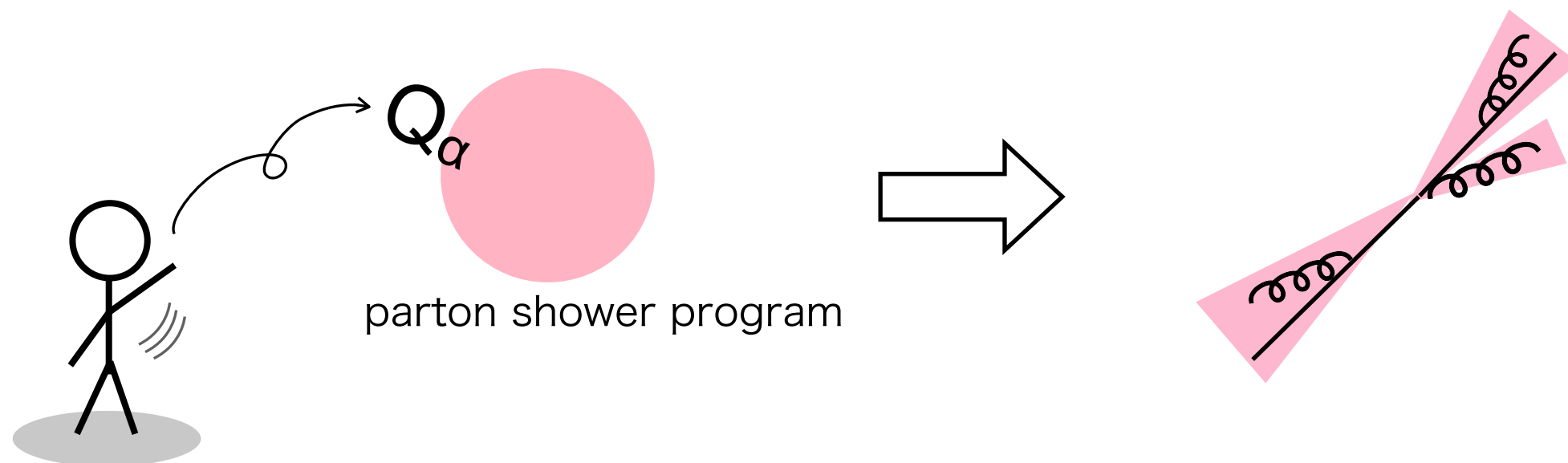
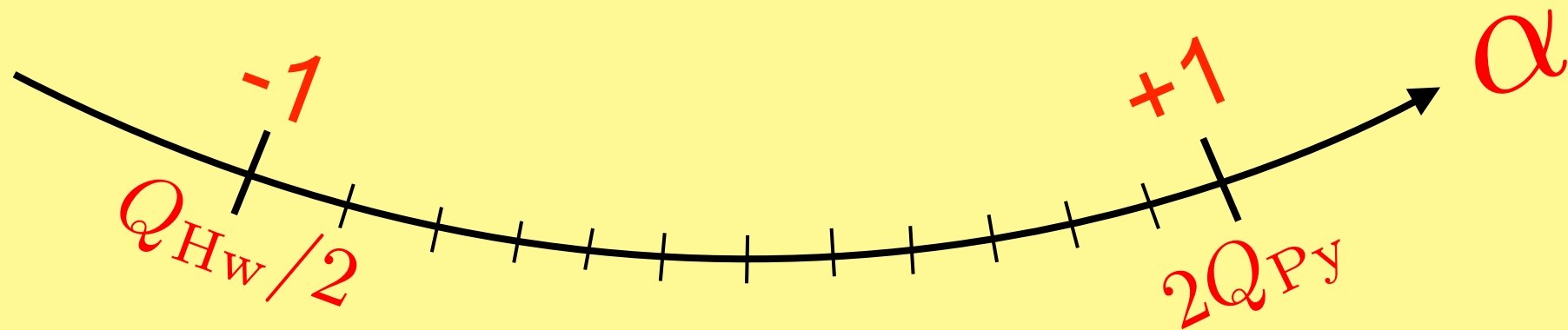
$$\frac{dq^2}{q^2} dz = \frac{dQ_{Py}^2}{Q_{Py}^2} dz = \frac{dQ_{Hw}^2}{Q_{Hw}^2} dz = \dots$$

- Radiation pattern depends on the evolution variable
  - ➡ **Evolution variable dependence on jet substructure**

# Study of evolution variable dependence

in the same modeling of the parton shower

$$Q_\alpha^2 = [4z(1-z)]^\alpha q^2, \quad \frac{dq^2}{q^2} dz = \frac{dQ_\alpha^2}{Q_\alpha^2} dz$$



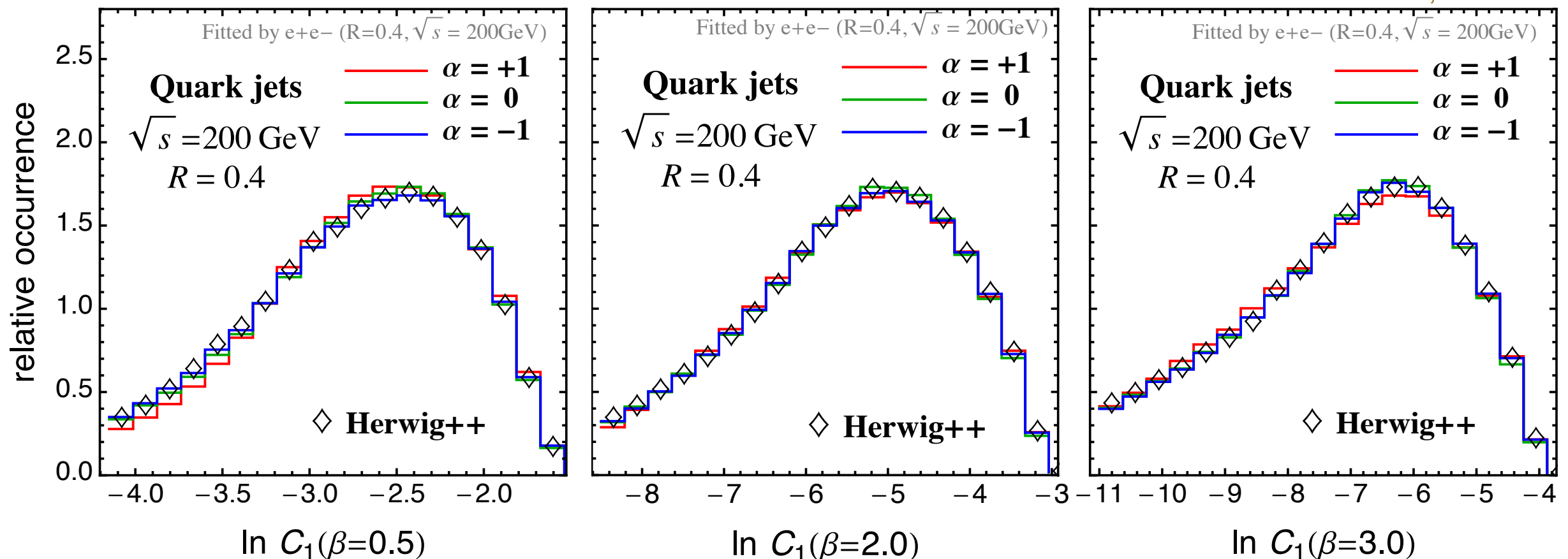
# Tuning

- **Three tunable parameters**
- LEP data is often used to tune parameters  
 ➡ need hadronization
- We use  $e^+e^- \rightarrow q\bar{q}$  events **generated by Herwig++** with hadronization off as “data” alternatively.
- **Three  $C_1(\beta)$  distributions** for fitting ( $R=0.4, \sqrt{s}=200\text{GeV}$ )  
 ➡  $C_1(\beta=2) \Leftrightarrow$  jet mass,  $C_1(\beta=1) \Leftrightarrow$  jet width/girth, ...

A. Larkoski, G. Salam, J. Thaler, 1305.0007

YS, 1505.xxxx

	$\alpha$	$\alpha_S(m_Z)$	$m_{qg}[\text{GeV}]$	$r_{\text{cut}}$
(PY)	+1.0	0.132	0.94	1.00
	+0.5	0.126	0.90	1.00
	$\pm 0.0$	0.121	0.84	1.05
	-0.5	0.119	0.83	1.16
(HW)	-1.0	0.119	0.85	1.25



# Tuning

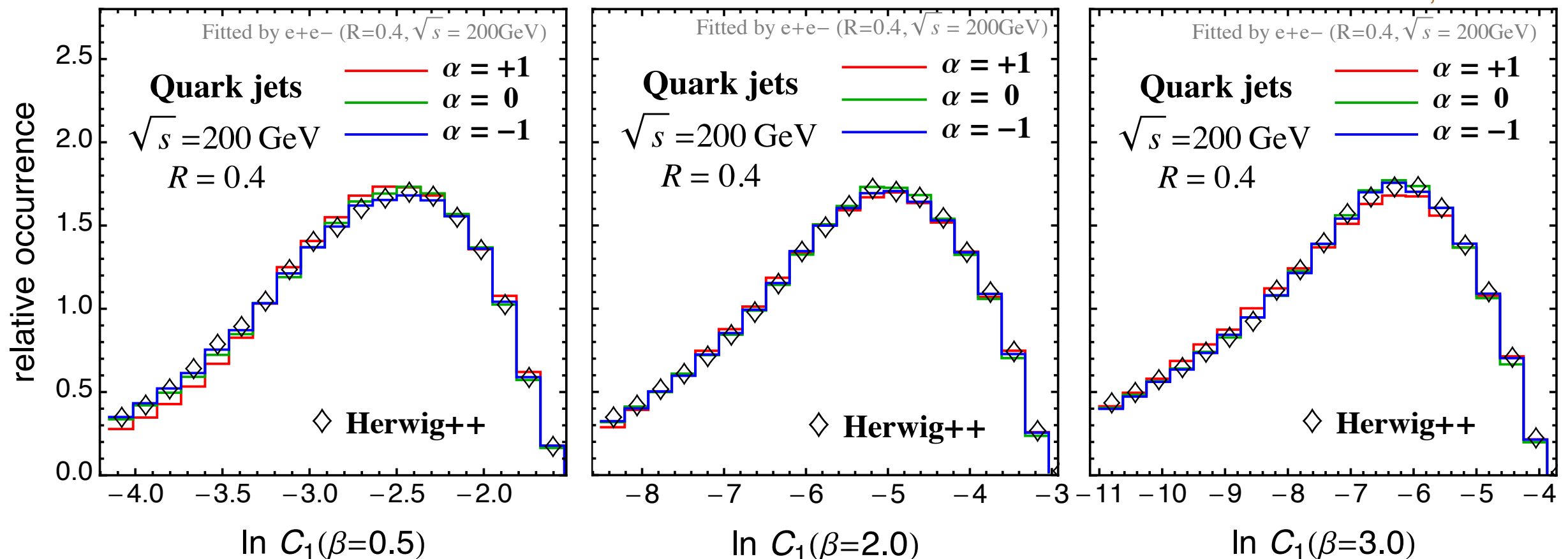
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Pythia-like case ( $\alpha=1$ )  
 choose larger value compare to  
 Herwig-like case ( $\alpha=-1$ )

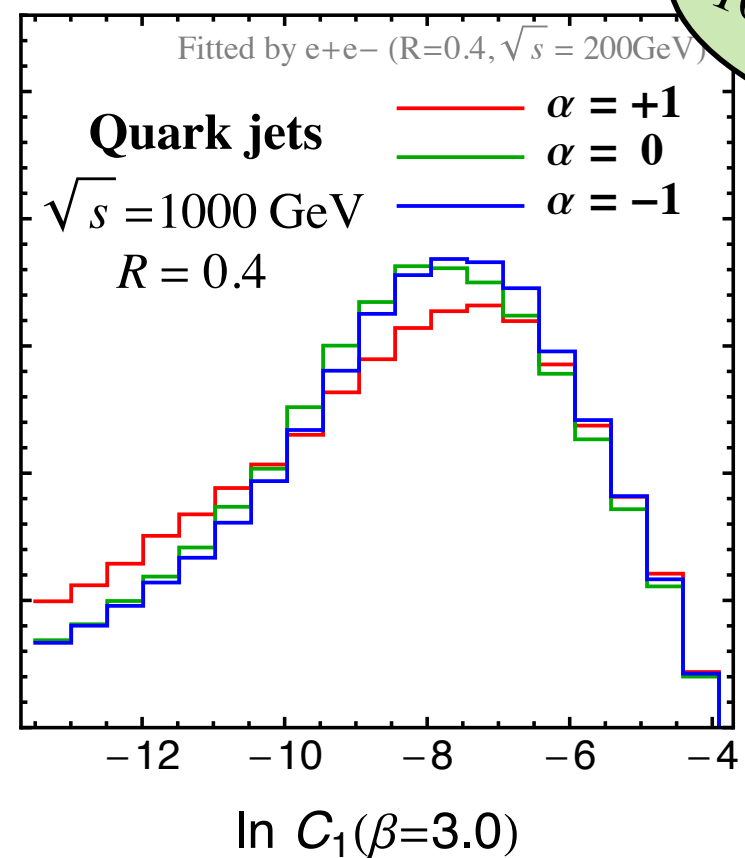
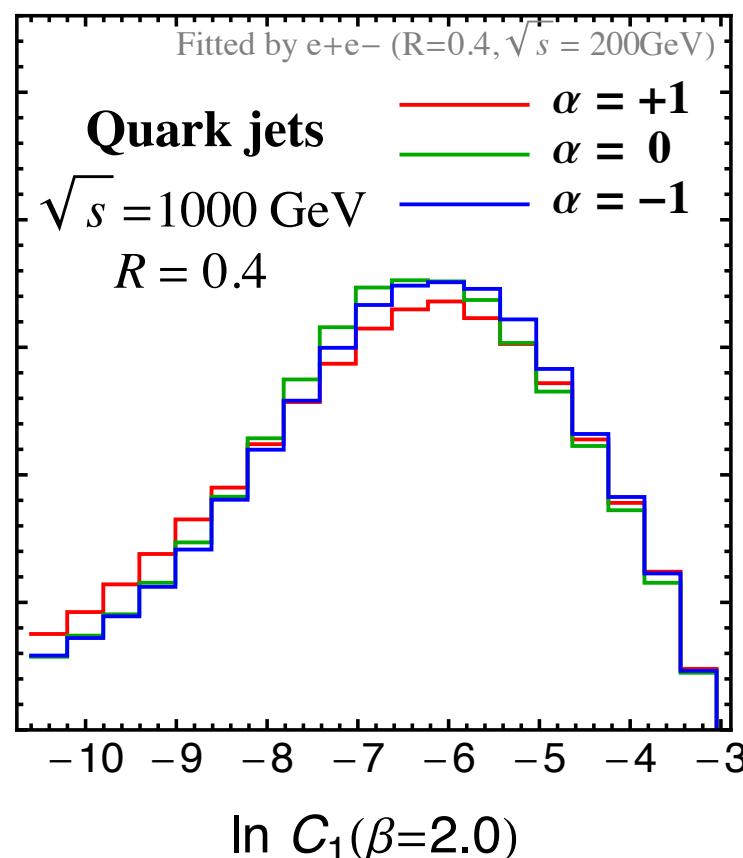
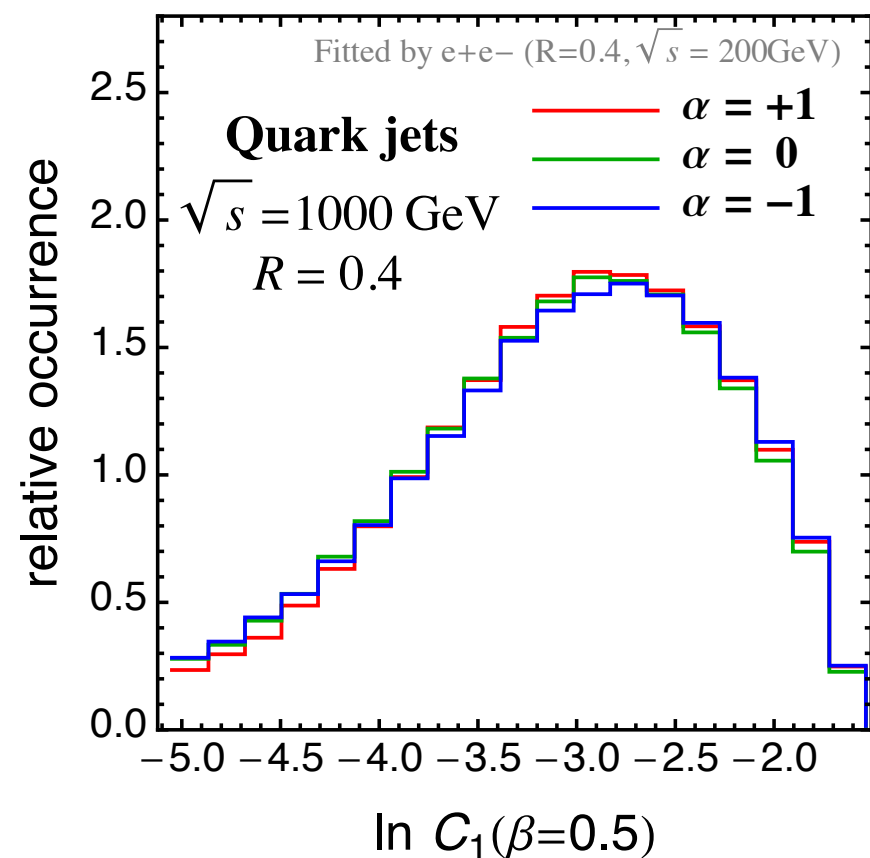
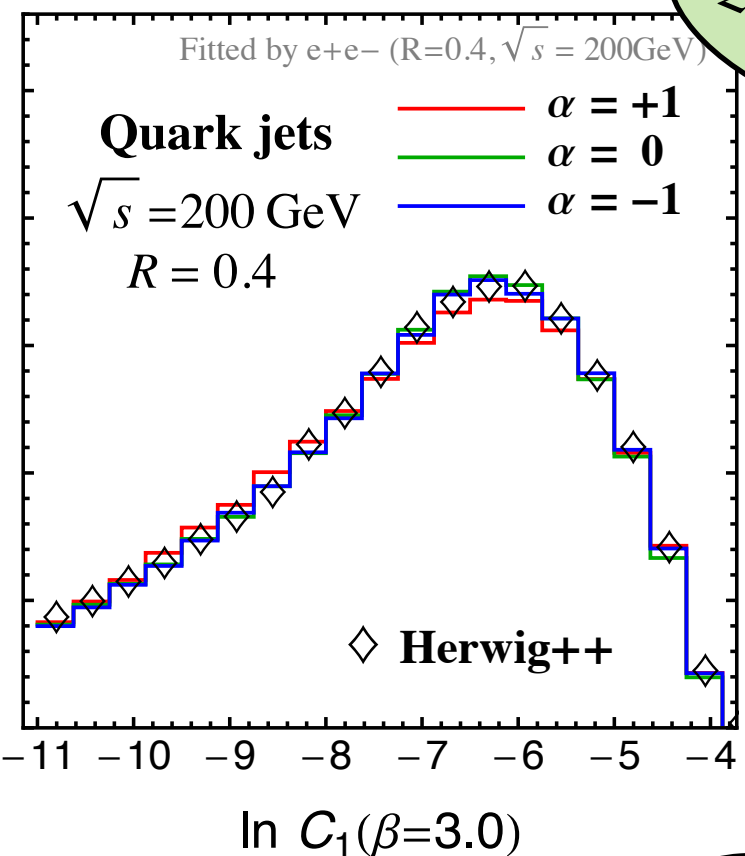
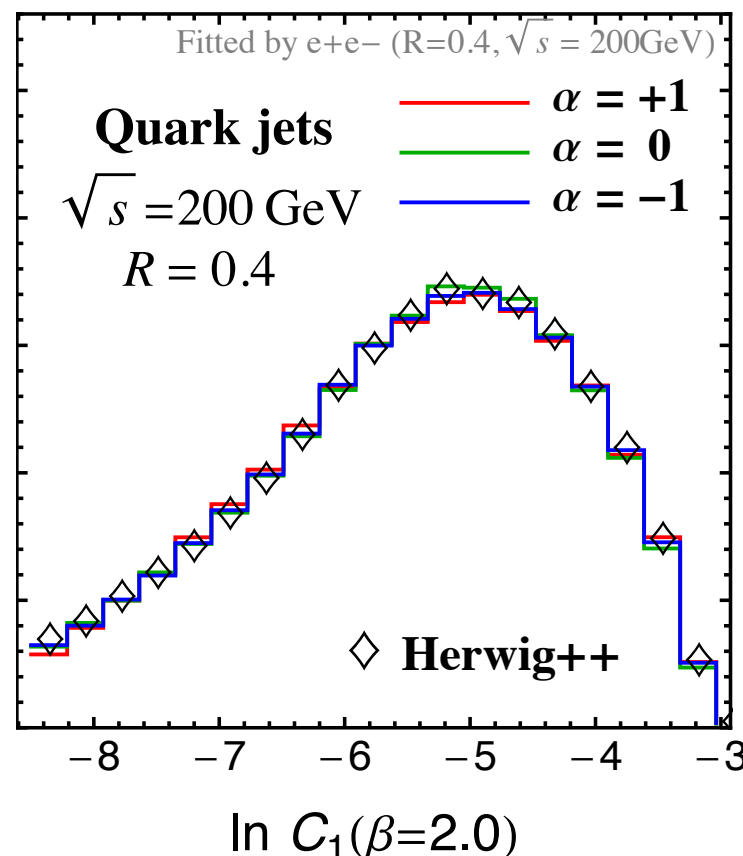
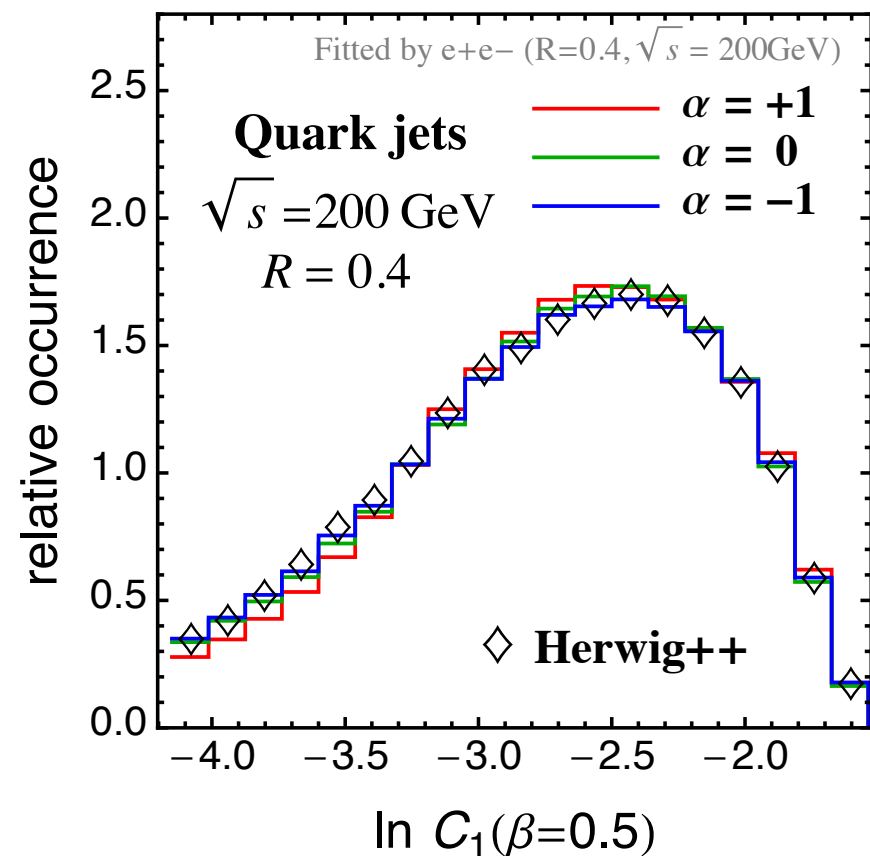
YS, 1505.xxxx



# Fitted results

## Quark jets

YS, 1505.xxxx



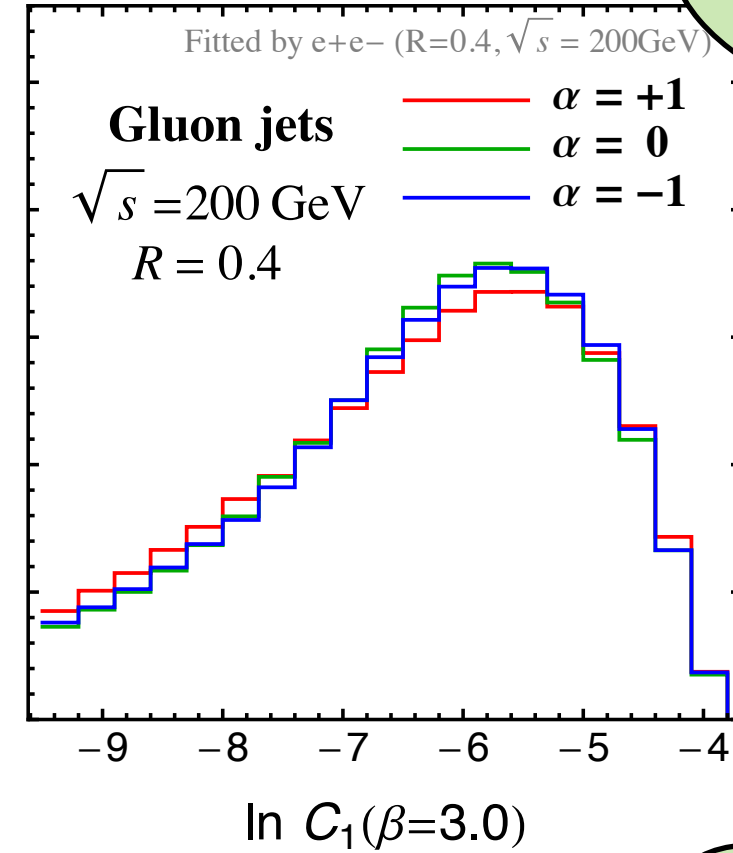
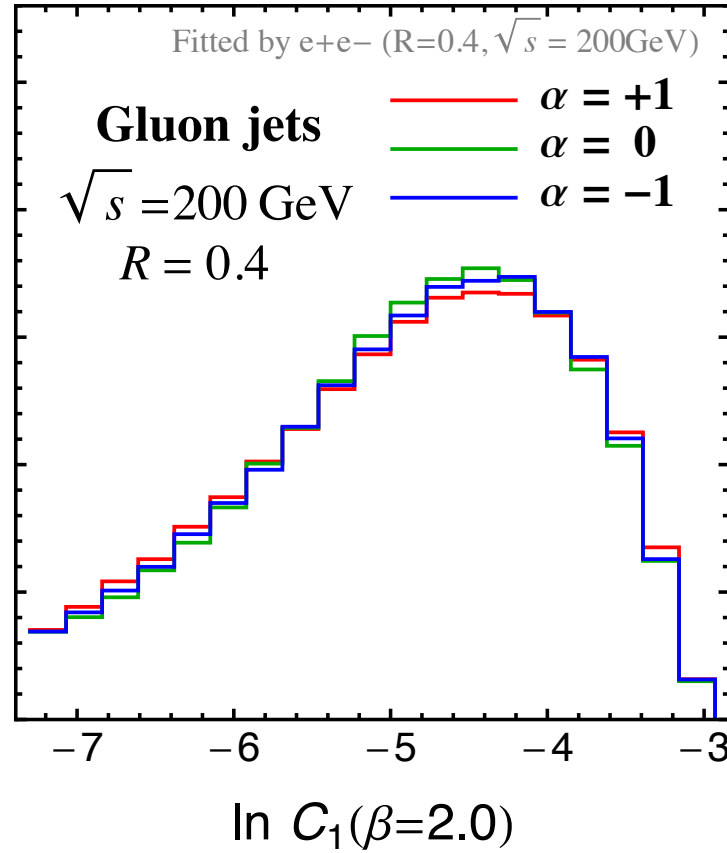
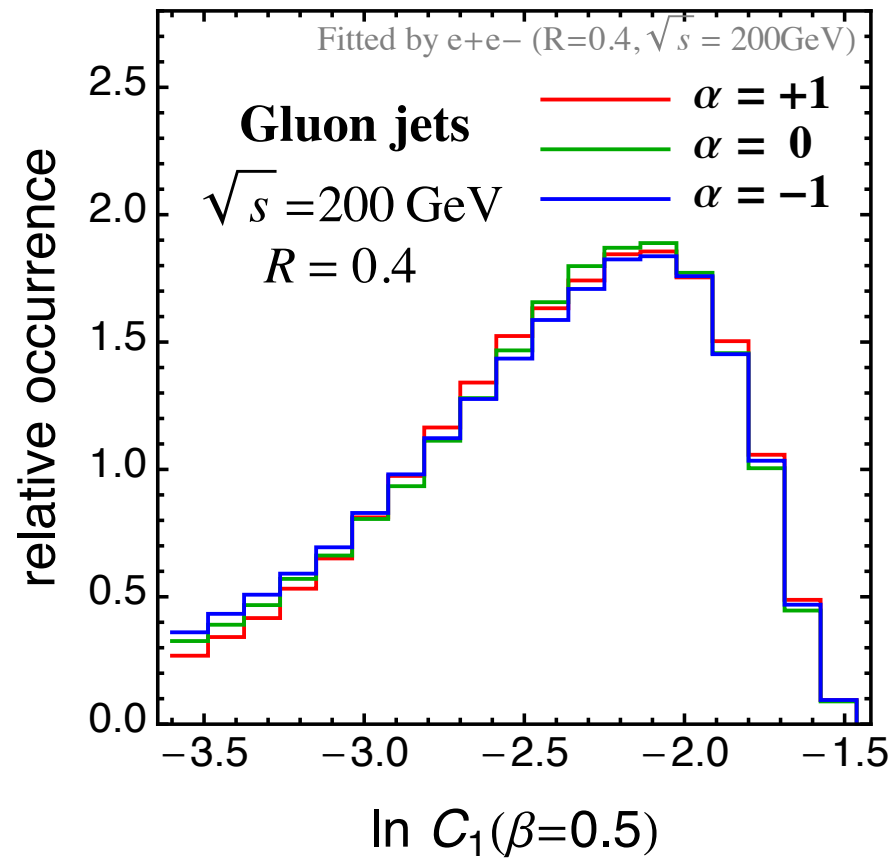
200GeV

1000GeV

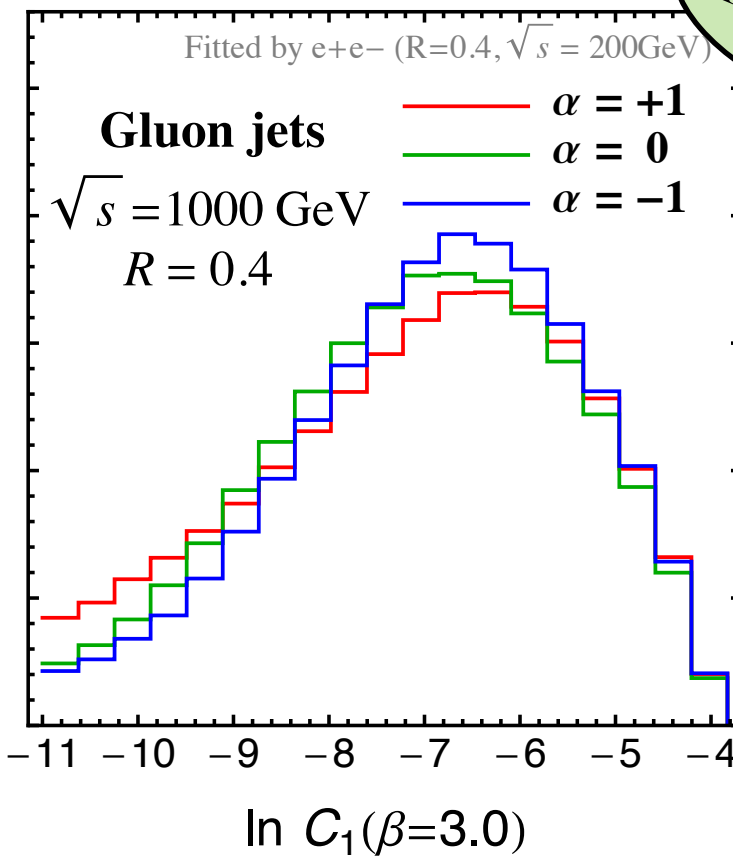
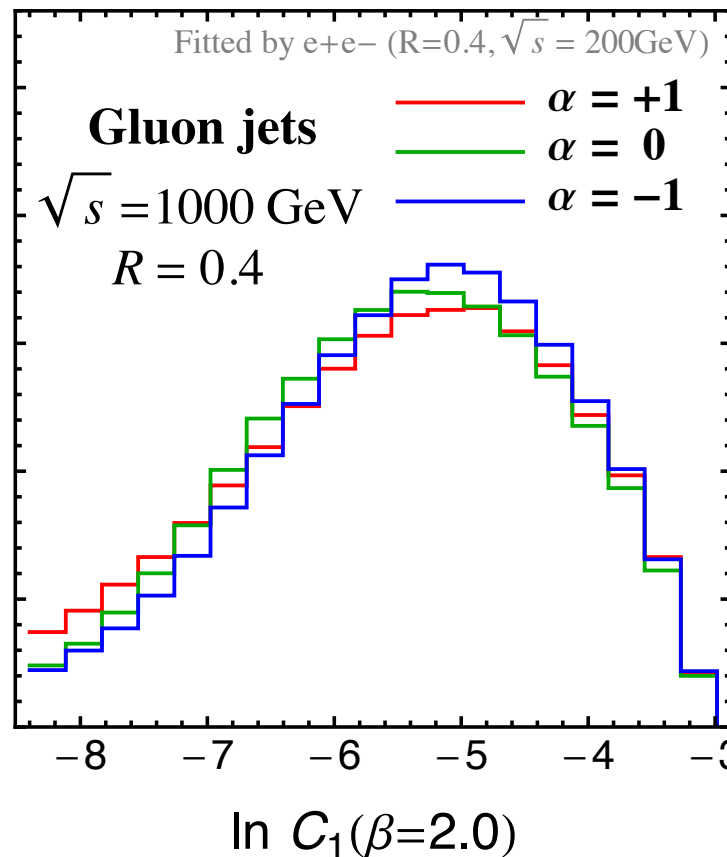
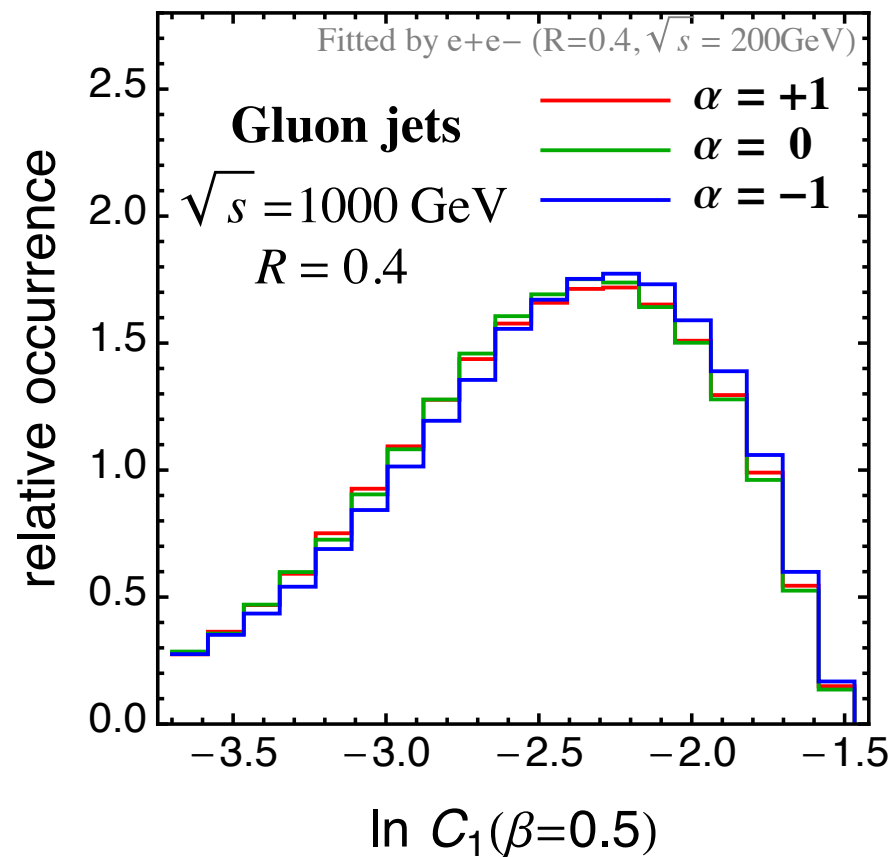
# Fitted results

YS, 1505.xxxx

## Gluon jets

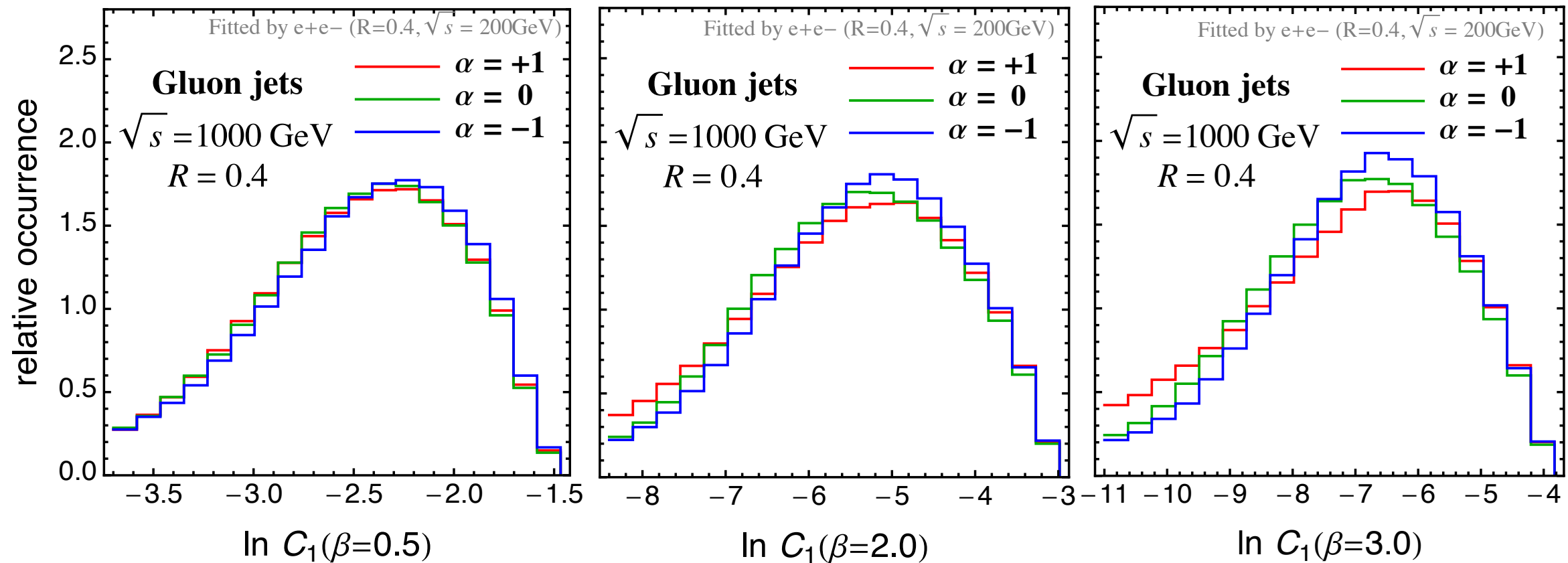


200GeV



1000GeV

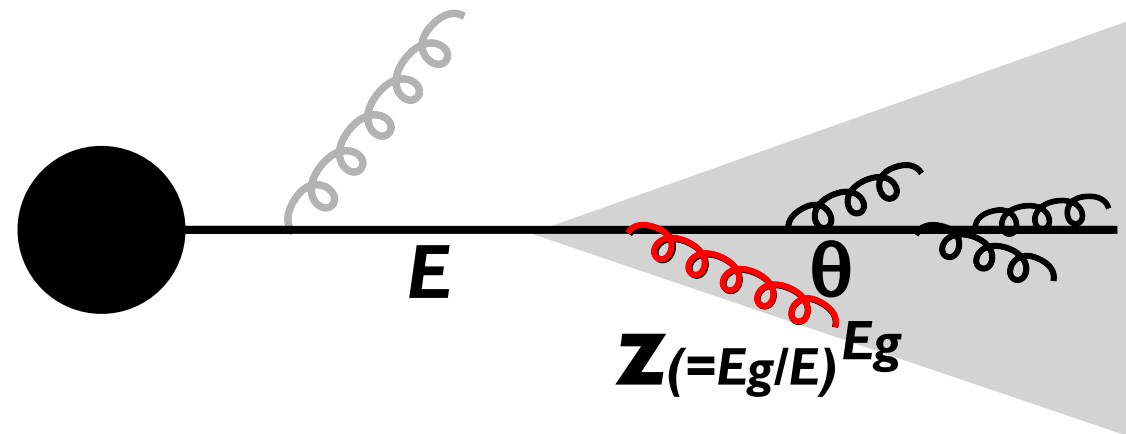
# Wideness of emissions in jet



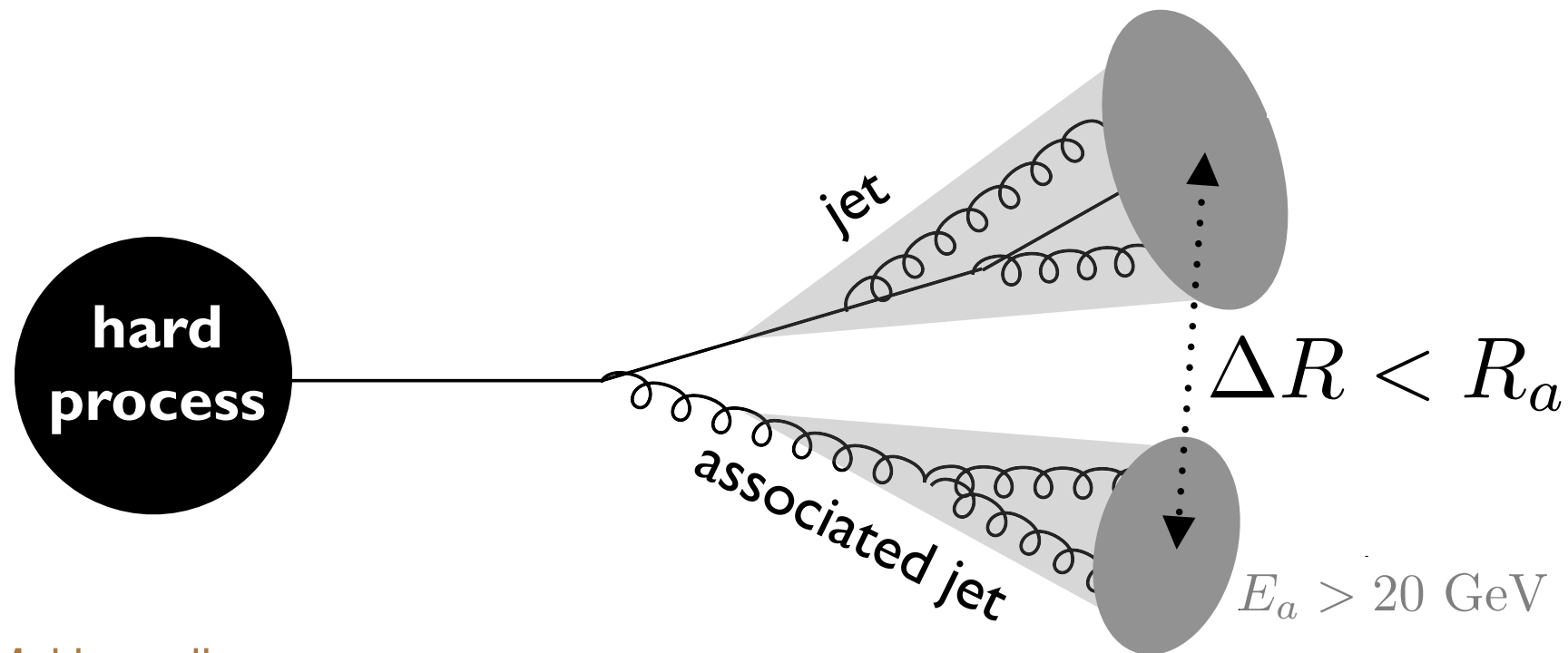
The larger  $\beta$  is, the larger the  $\alpha$ -dependence on  $C_1$  become

**Wideness** of emissions in jet is different

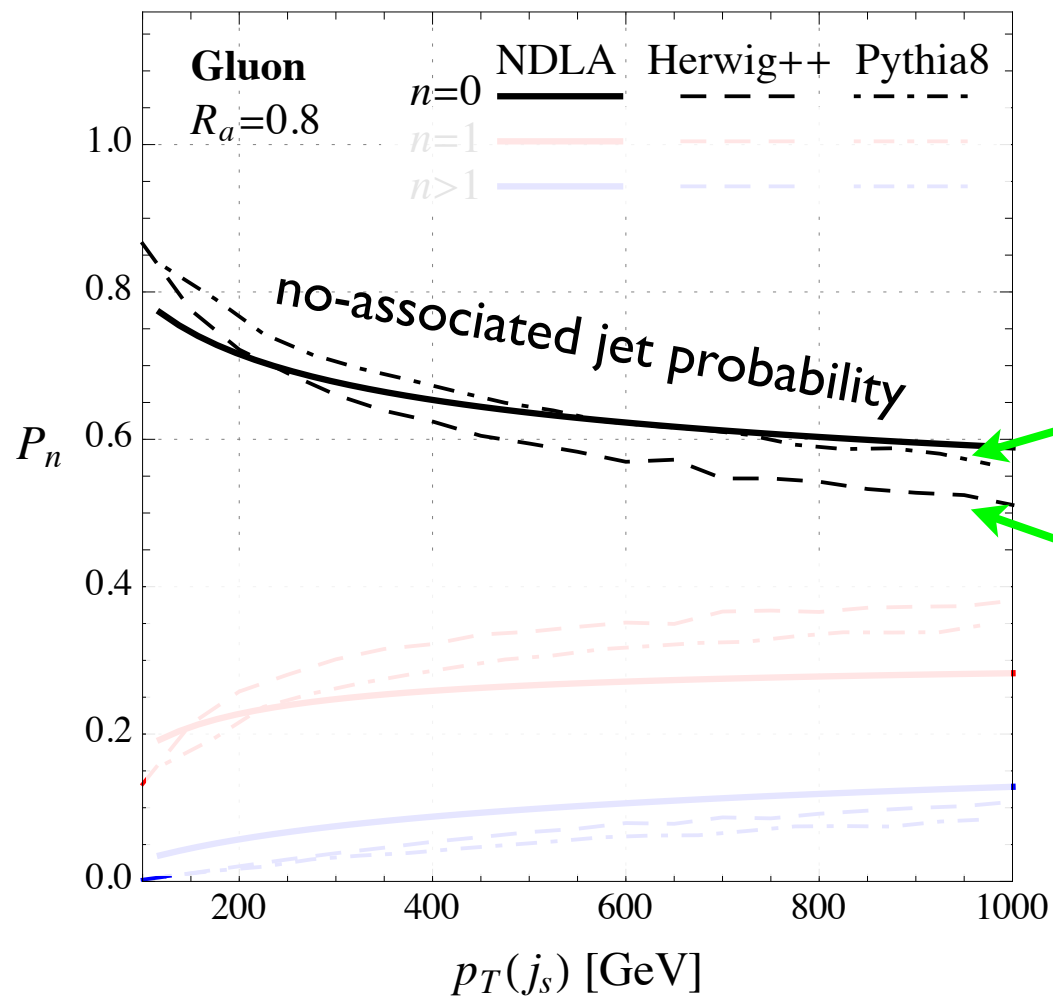
$$\ln C_1^{(\beta)} \sim \ln z + \underline{\underline{\beta \ln \theta}}$$



# Associated jet



B. Bhattacharjee, S. Mukhopadhyay,  
M. M. Nojiri, YS, B. R. Webber, 1501.04794



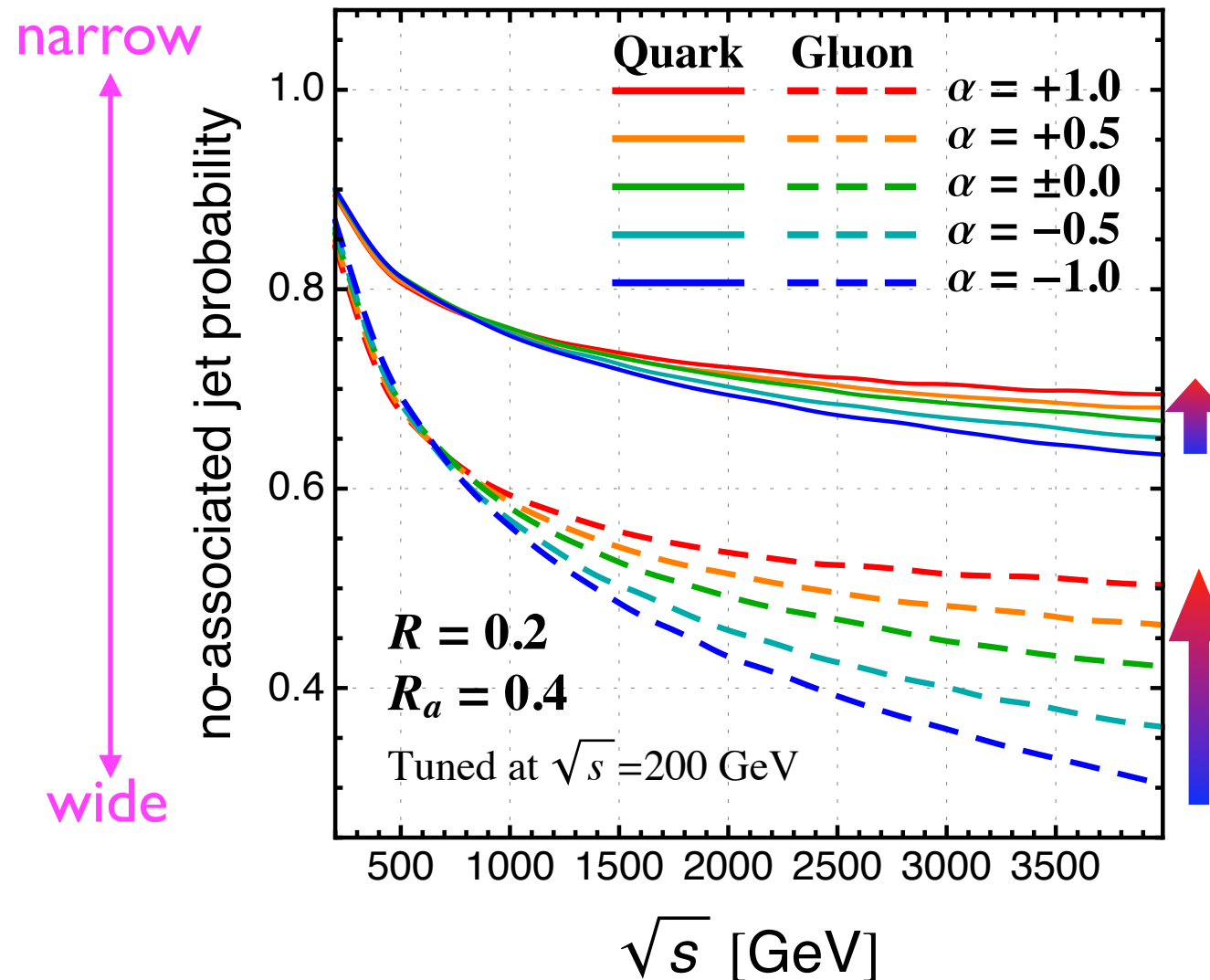
Low no-associated jet probability  
= Wide emissions

Pythia

Herwig

- Herwig predicts wide jets, while Pythia predicts narrower jets.





- The larger  $\alpha$  is, the larger the no-associated jet probabilities become
- Angular ordered shower ( $\alpha = -1$ ) predicts most wide jets, while  $p_{\perp}$  ordered shower ( $\alpha = +1$ ) predicts narrower jets
- This is other qualitative coincidences between Pythia and Herwig
- Wideness is tunable by  $\alpha$

# Summary

- **MC dependence** on QCD jet substructure exist
- Study of **evolutoin variable dependence** on the jet substructure in the same modeling of parton shower
  - ➡  $Q_\alpha = [4z(1-z)]^\alpha q^2$
- The  **$\alpha$ -dependence** on jet shape variables (class of  $C_1$ ) and no-associated jet probability exist
- Two qualitative coincidences of the difference between **Pythia** and **Herwig** just by changing  $\alpha$ 
  - ➡ Value of tuned  $\alpha_s(m_Z)$
  - ➡ Wideness of emissions in/around leading jets
    - ▶ The widenness is tunable by  $\alpha$

*B*ack up  
*Belle II*

# Quick explanation to formalizm

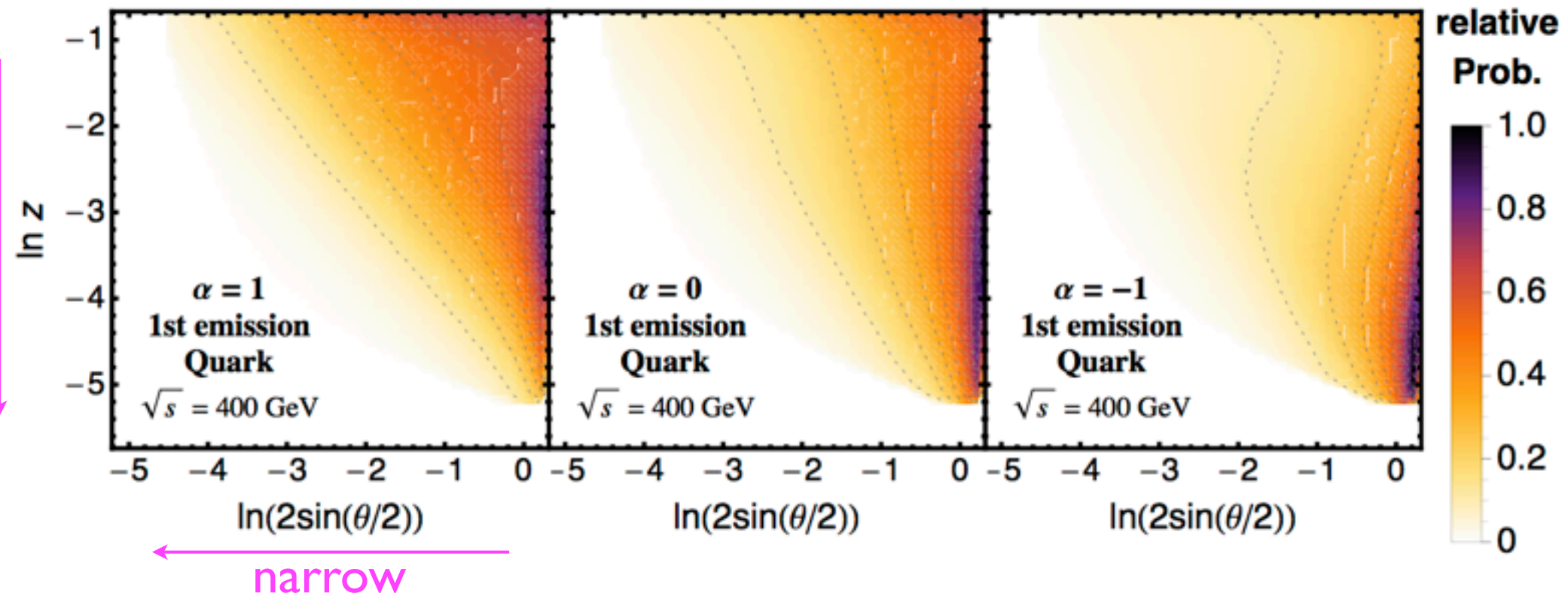
- Using kinematics on Herwig++
- Traditional  $1 \rightarrow 2$  branching
- 1-loop running constant
- Imposing angular ordering by vetoing (excepting  $\alpha = -1$ )
- No hadronization
- Three tunable parameters
  - $\alpha_s(m_Z)$
  - $m_{qg}$  : effective mass for massless partons (to avoid soft collinear singularity).  $k_T$  cut off.
  - $r_{cut} : (Q_{cut} / Q_{min}) = (Q_{cut} / 2m_{qg})$

# Radiation pattern (Quark)

YS, 1505.xxxx

1st

soft

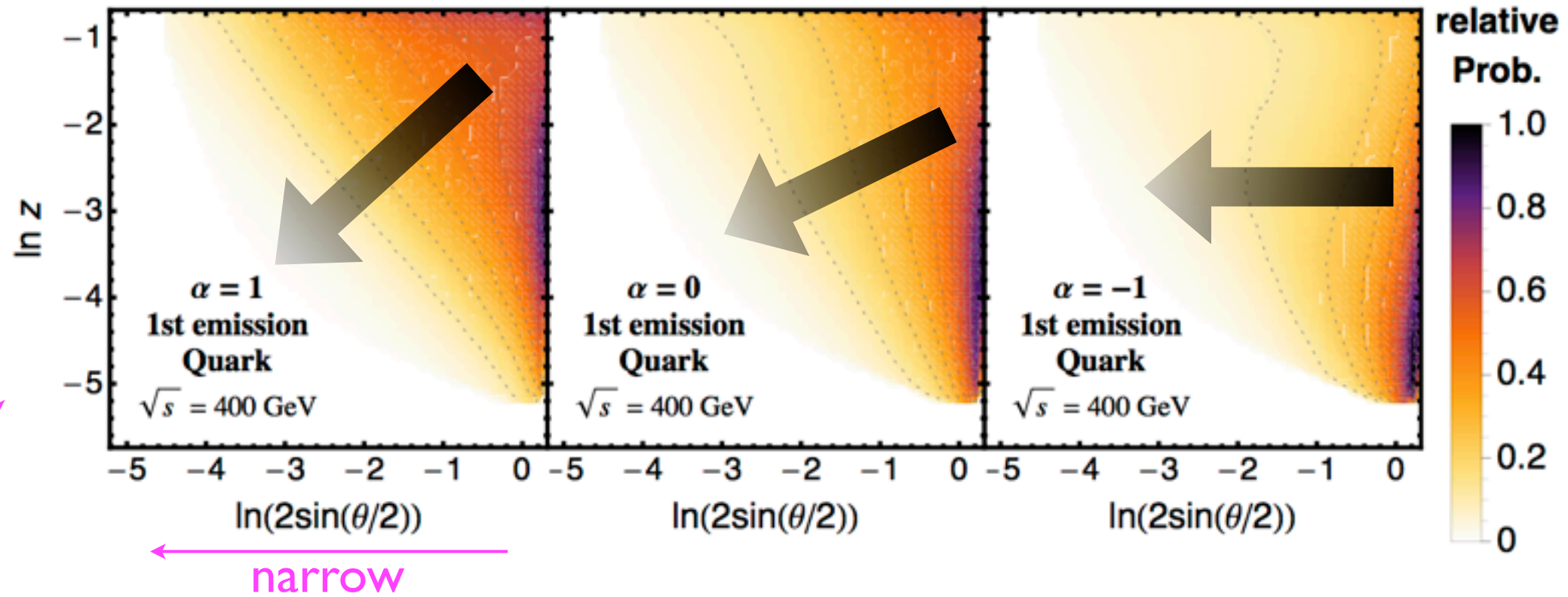


# Radiation pattern (Quark)

YS, 1505.xxxx

1st

soft



$p_\perp$ -ordering

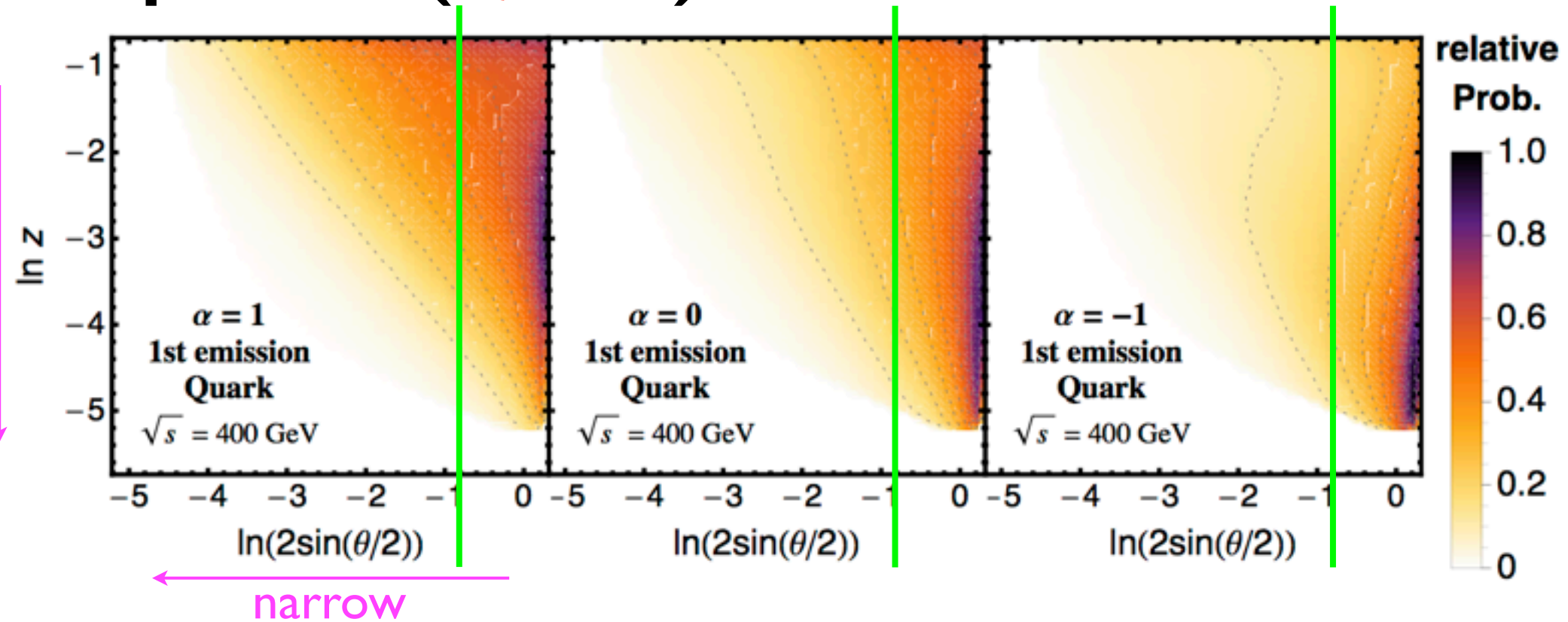
angular-ordering

# Radiation pattern (Quark)

$\theta=0.4$  YS, 1505.xxxx

1st

soft



- The 1st emissions are wide and soft for small  $\alpha$ .
- The emissions are neglected (or often vetoed in matching)



# Radiation pattern (Quark)

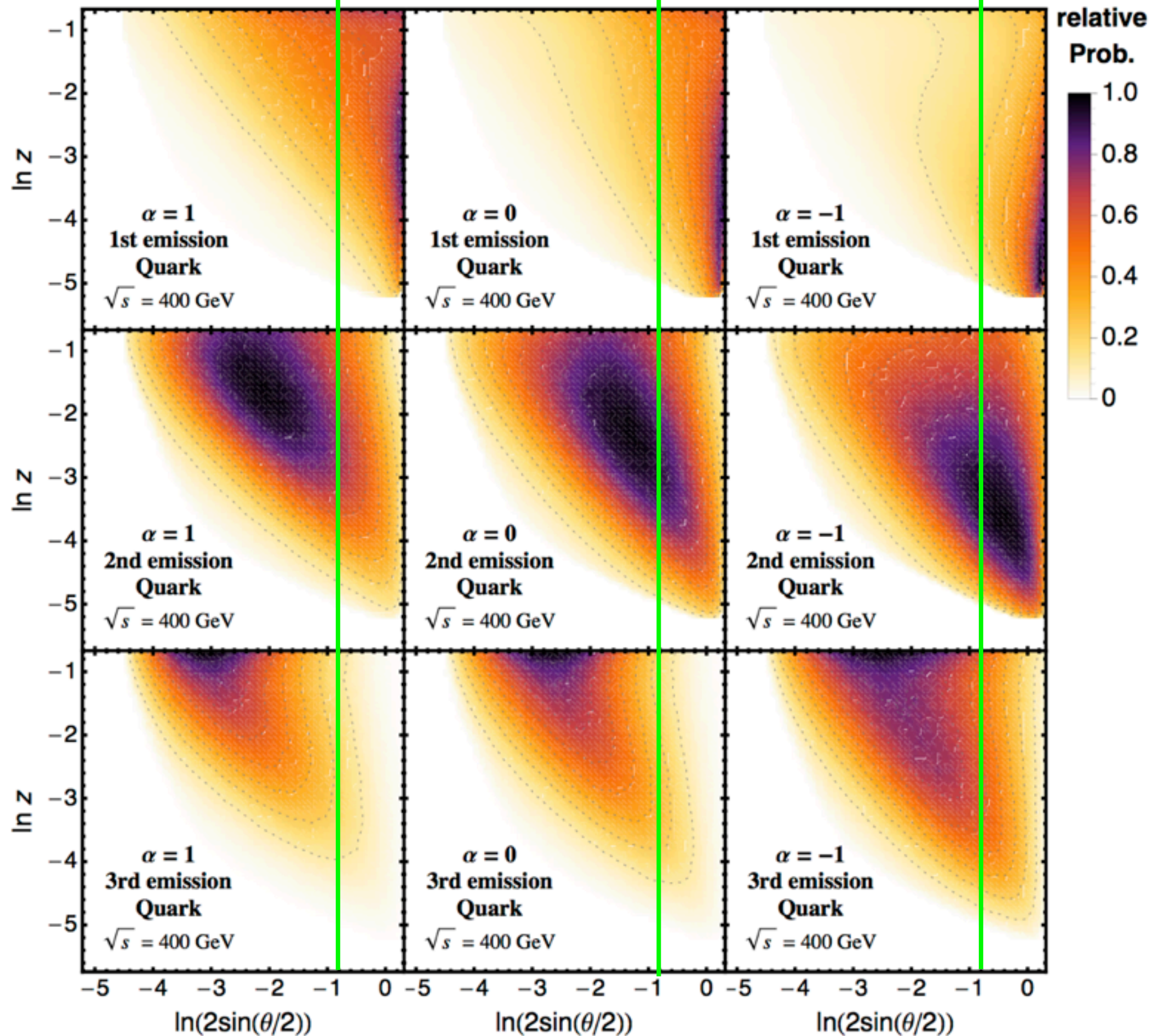
$\theta=0.4$

YS, 1505.xxxx

1st

2nd

3rd





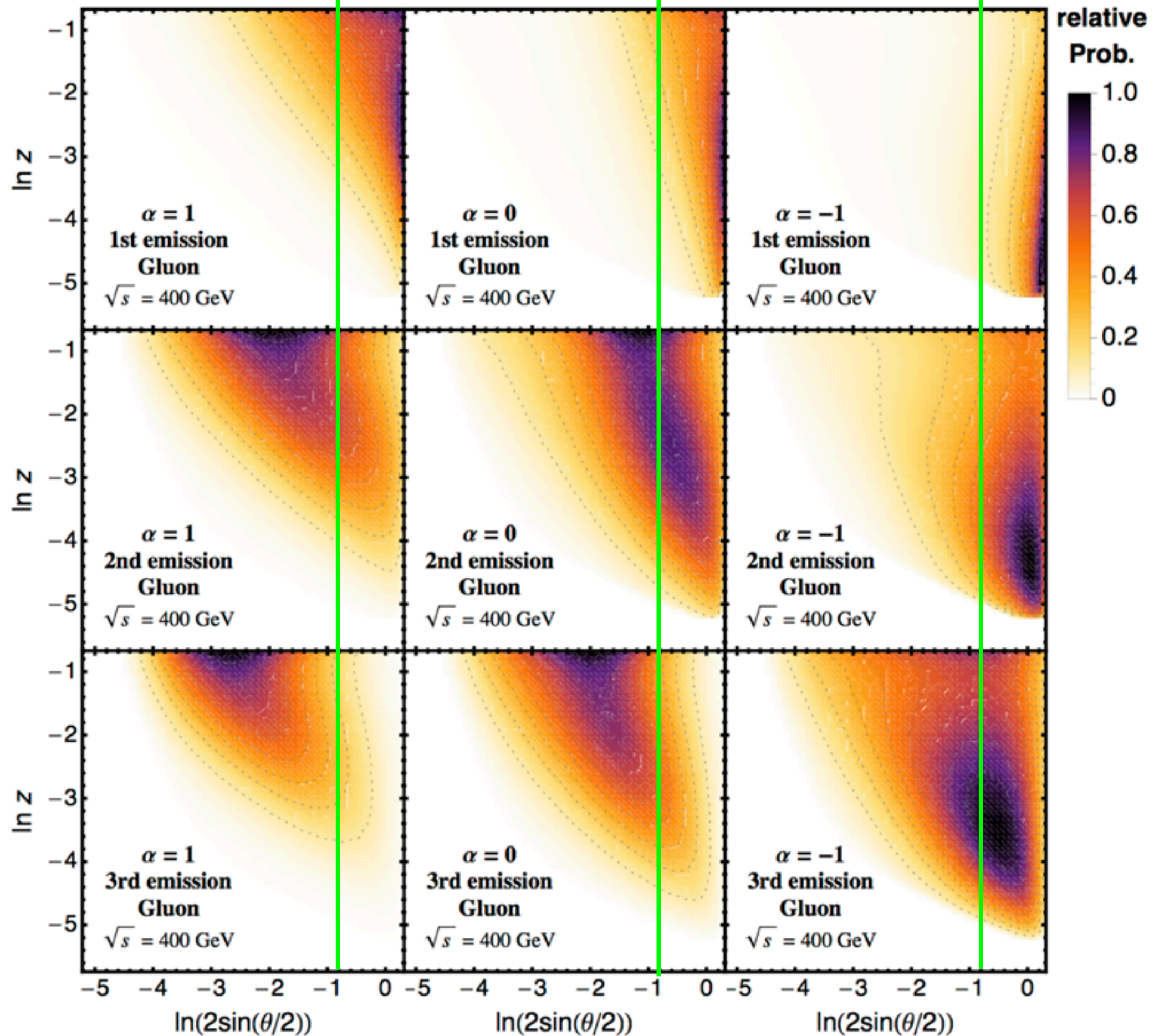
# Radiation pattern (Gluon)

$\theta=0.4$  YS, 1505.xxxx

1st

2nd

3rd



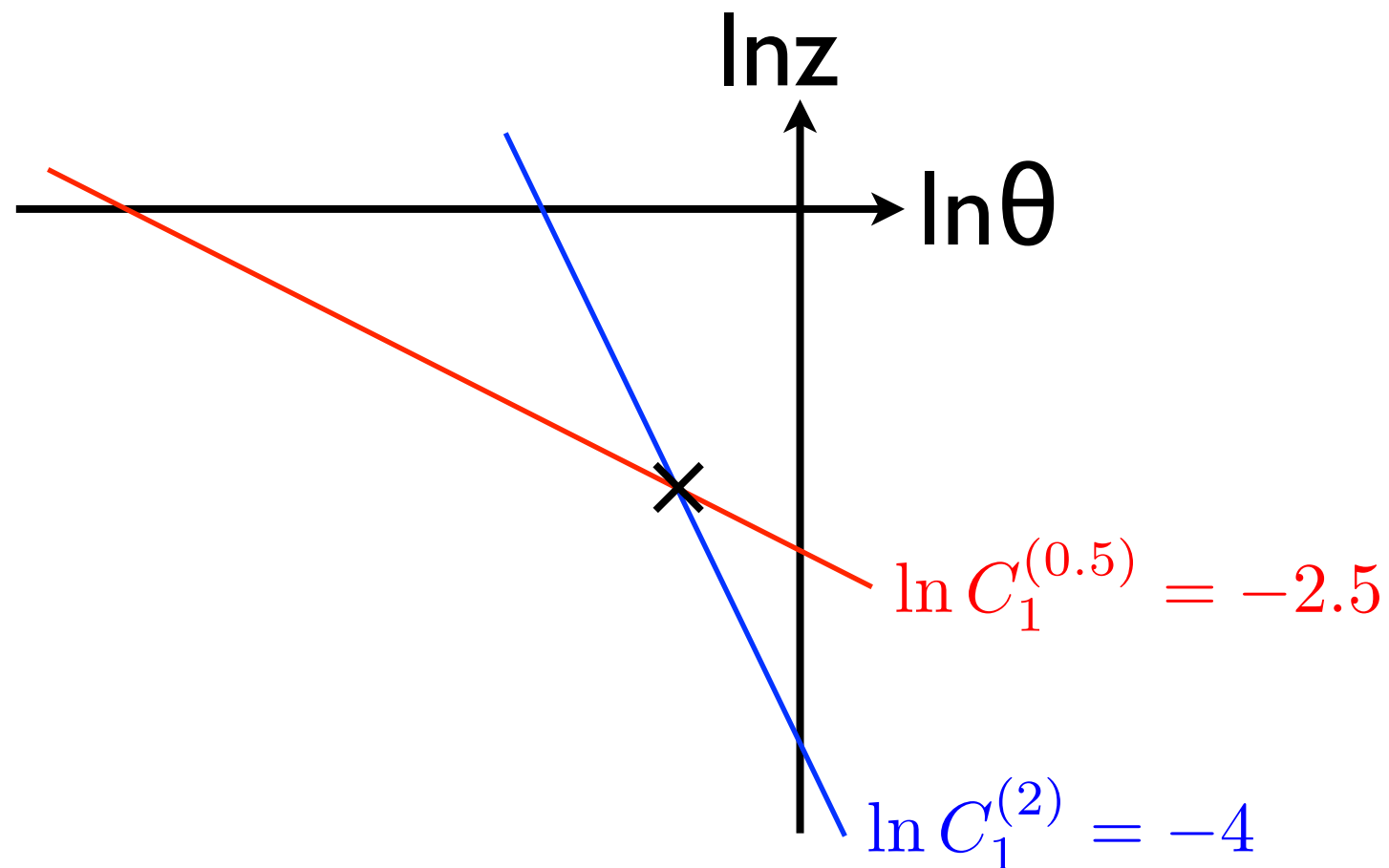
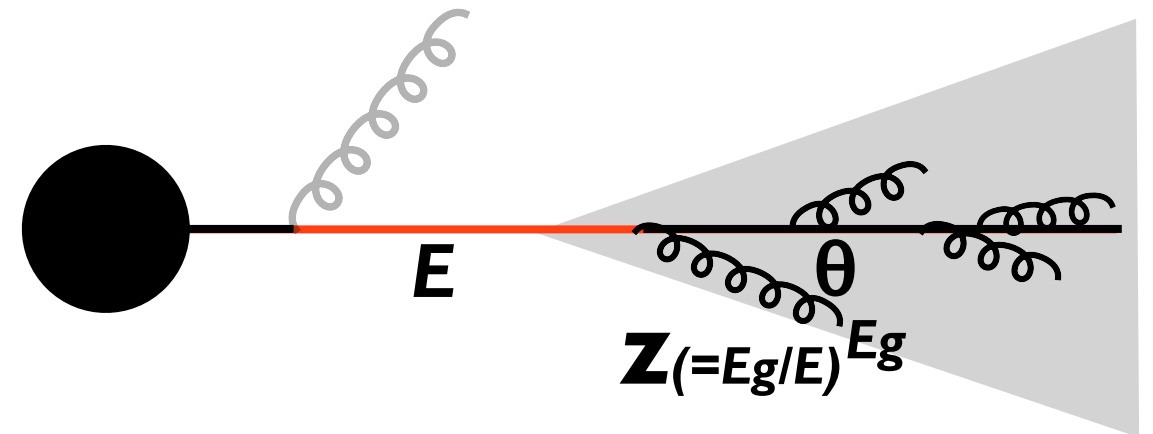
- One of well-studied jet shape variables

$$C_1^{(\beta)} = \sum_{i < j \in \text{jet}} \frac{E_i}{E_{\text{jet}}} \frac{E_j}{E_{\text{jet}}} \left( 2 \sin \frac{\theta_{ij}}{2} \right)^\beta$$

$$\sim z(1-z)\theta^\beta$$

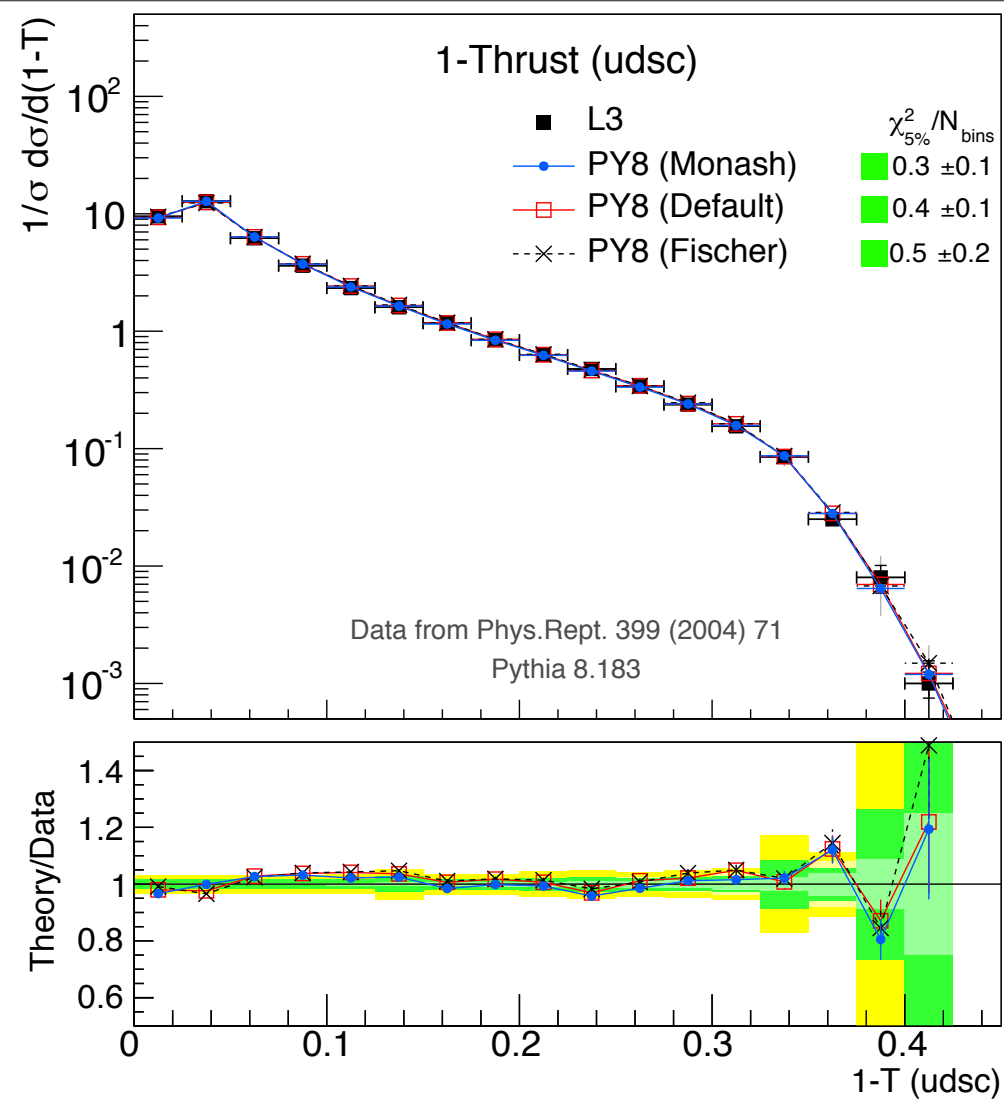
$$\sim z\theta^\beta$$

$$\ln C_1^{(\beta)} \sim \ln z + \beta \ln \theta$$



# Tuning

P.Skands, S.Carrazza2,J.Rojo, 1404.5630



- LEP data is often used to tune parameters  
 ➡ need hadronization
- We use  $e^+e^- \rightarrow q\bar{q}$  events generated by Herwig++ with hadronization off as “data” alternatively.
- Three  $C_1$  distributions for tuning ( $R=0.4, \sqrt{s}=200\text{GeV}$ )



$$C_1^{(\beta)} = \sum_{i < j \in \text{jet}(R)} \frac{E_i}{E_{\text{jet}}} \frac{E_j}{E_{\text{jet}}} \left( 2 \sin \frac{\theta_{ij}}{2} \right)^\beta$$

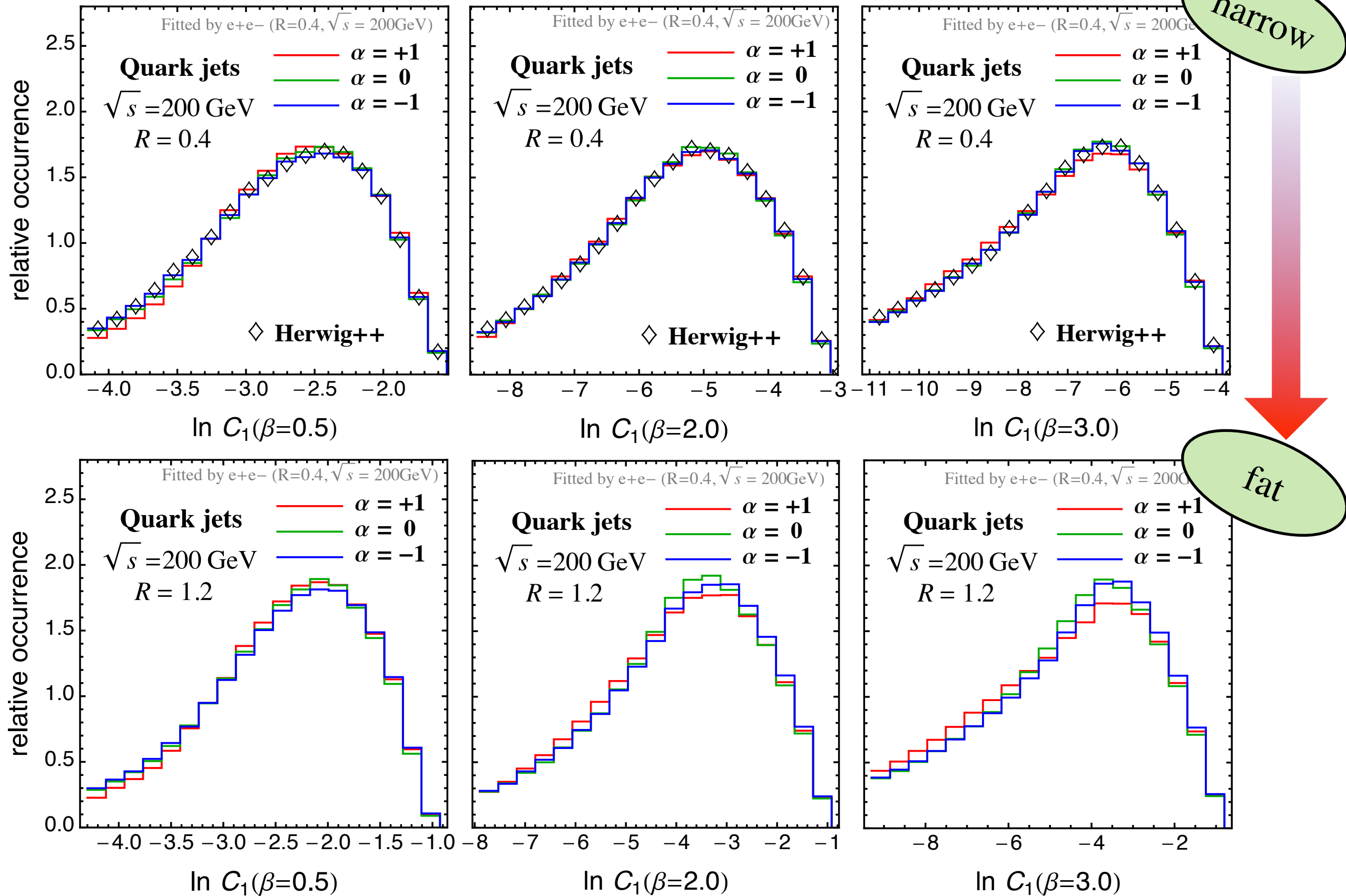
A. Larkoski, G. Salam, J. Thaler, JHEP06(2013)108

A. Larkoski, D. Neill, J. Thaler, JHEP04(2014)017

# Fitted results

**Quark @  $\sqrt{s} = 200$  GeV**

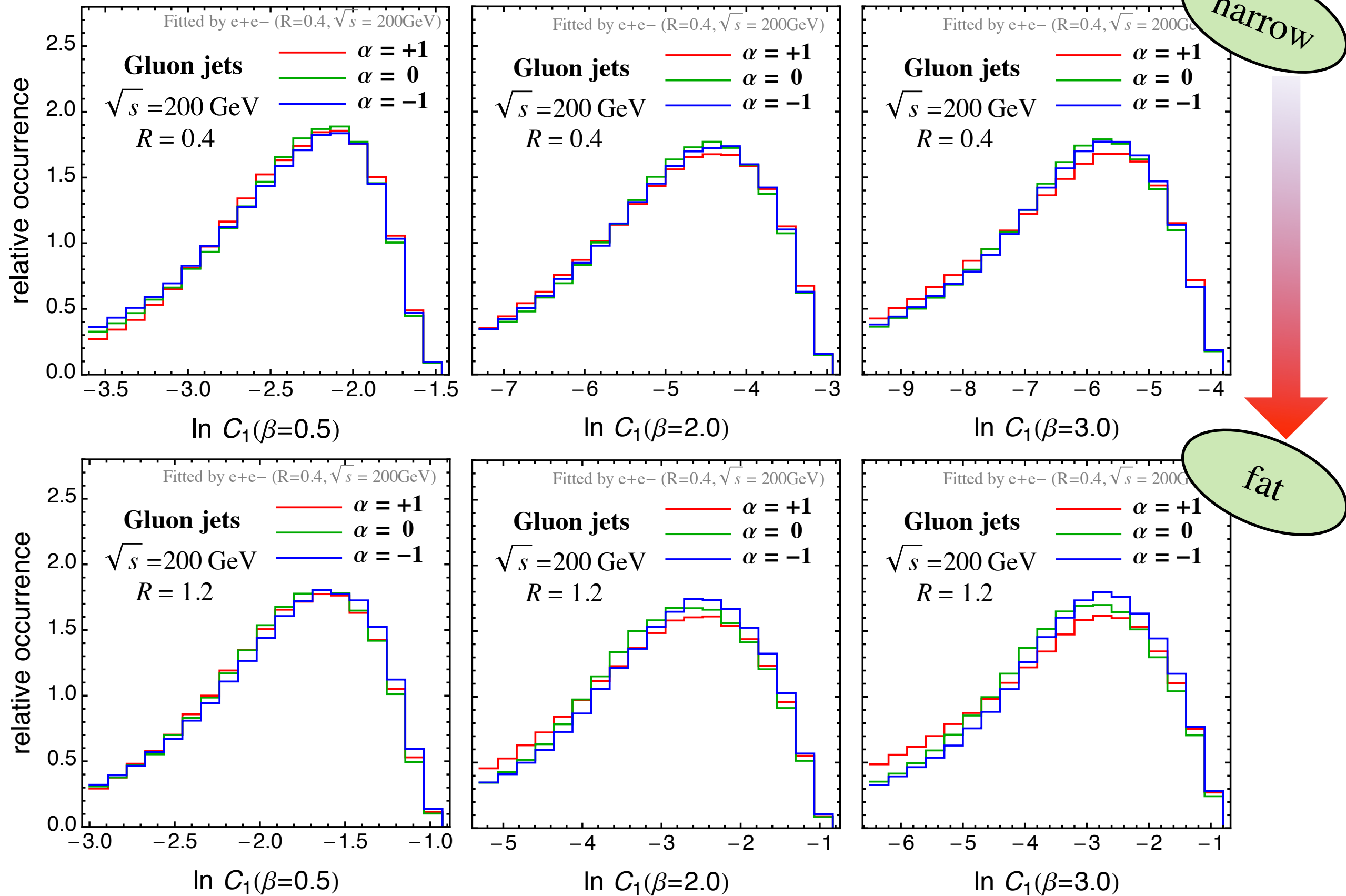
YS, 1505.xxxx



# Fitted results

**Gluon @  $\sqrt{s} = 200$  GeV**

YS, 1505.xxxx

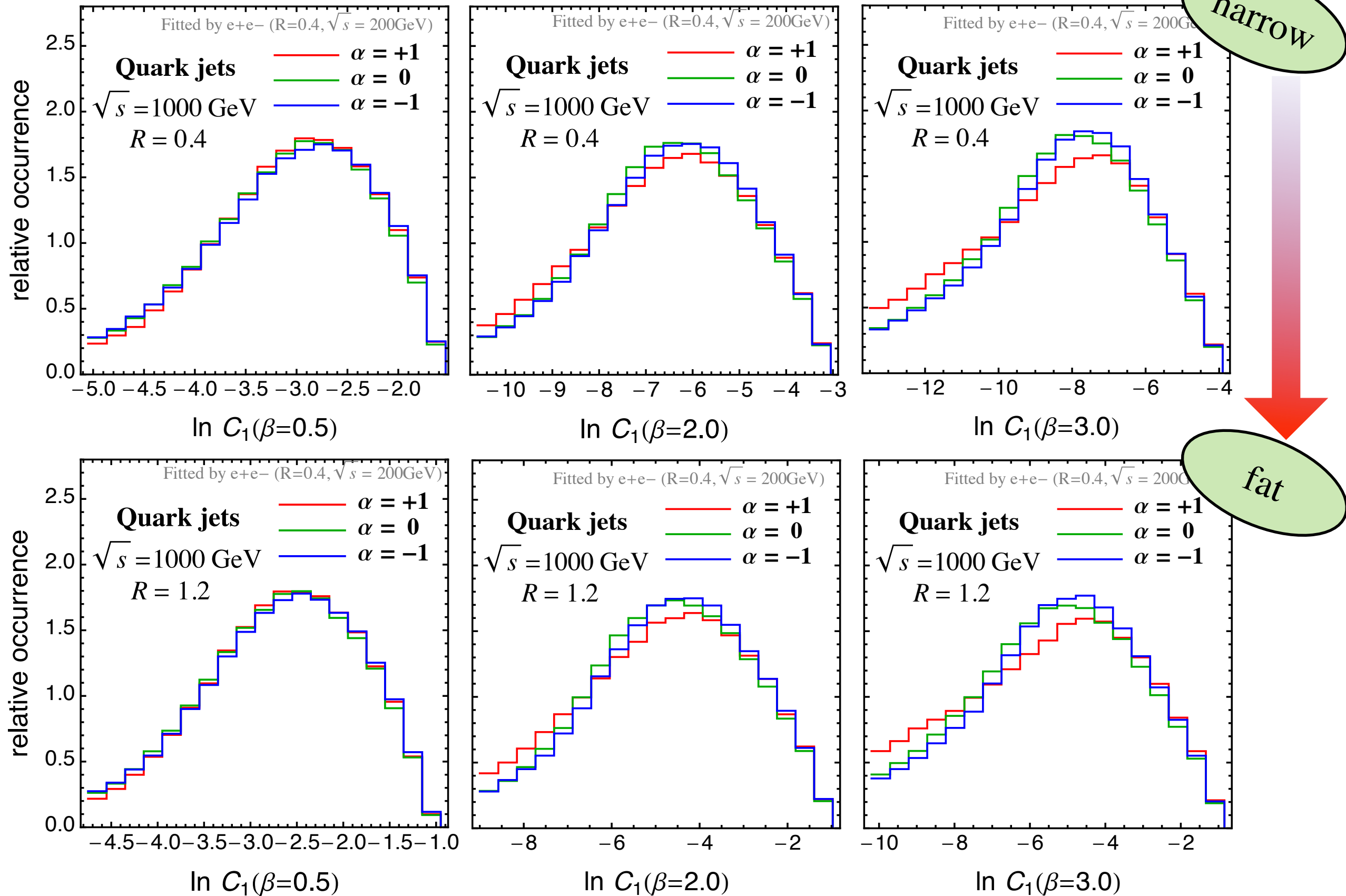




# Fitted results

**Quark @  $\sqrt{s} = 1000$  GeV**

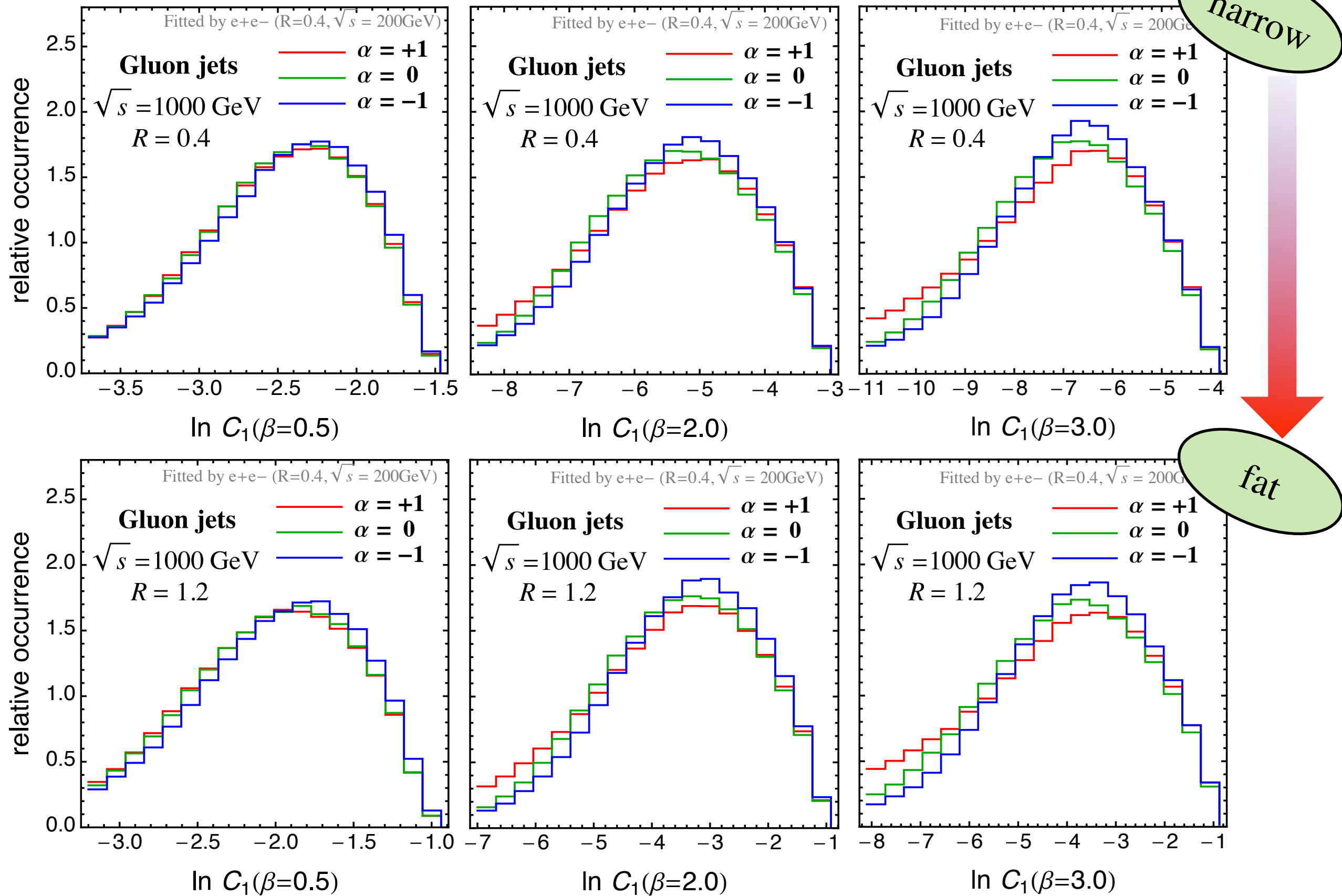
YS, 1505.xxxx

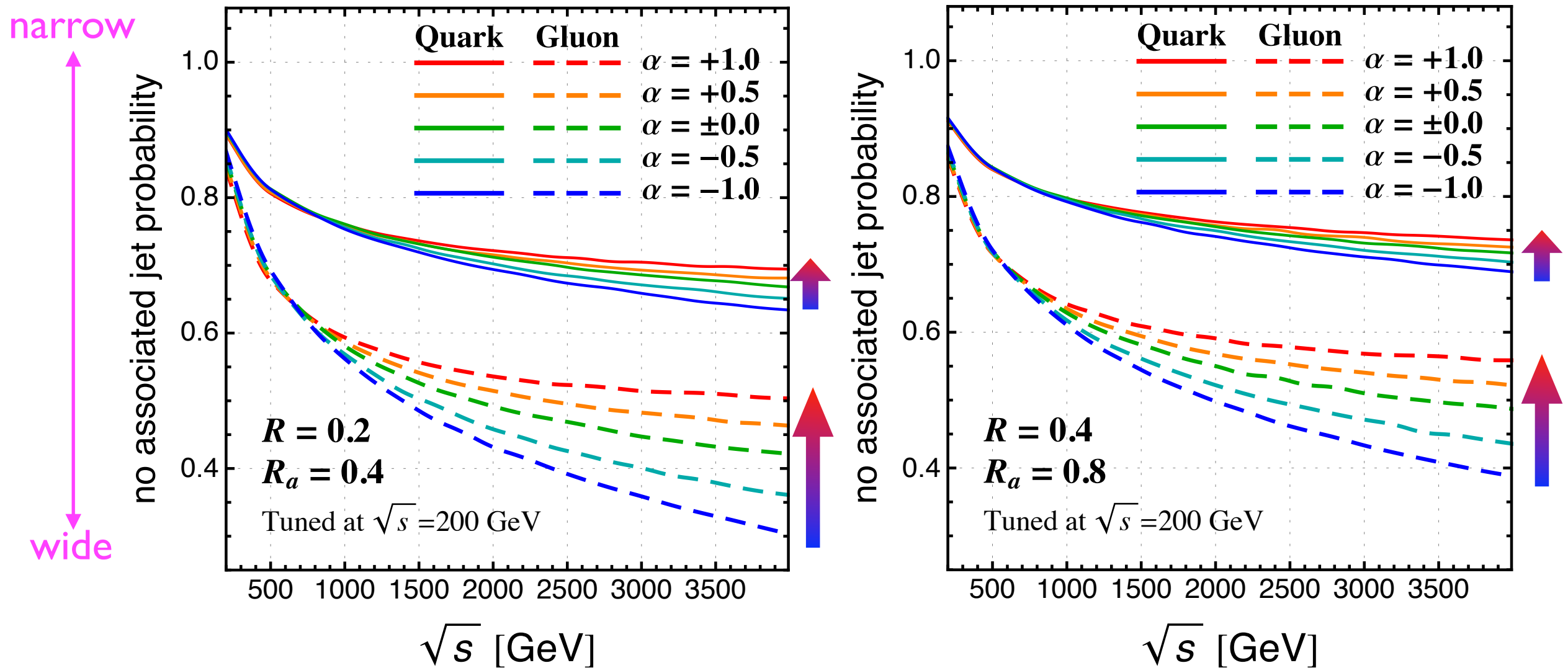


# Fitted results

**Gluon @  $\sqrt{s} = 1000$  GeV**

YS, 1505.xxxx

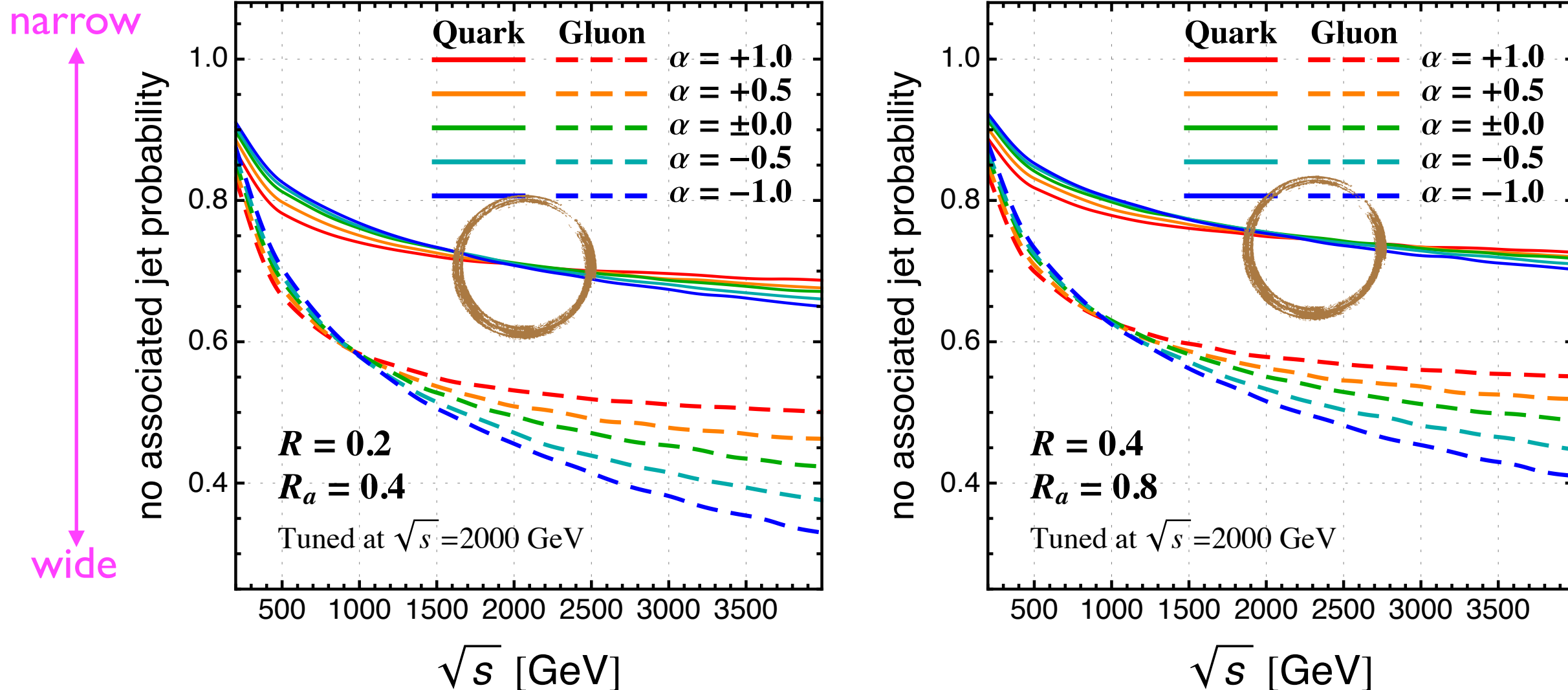




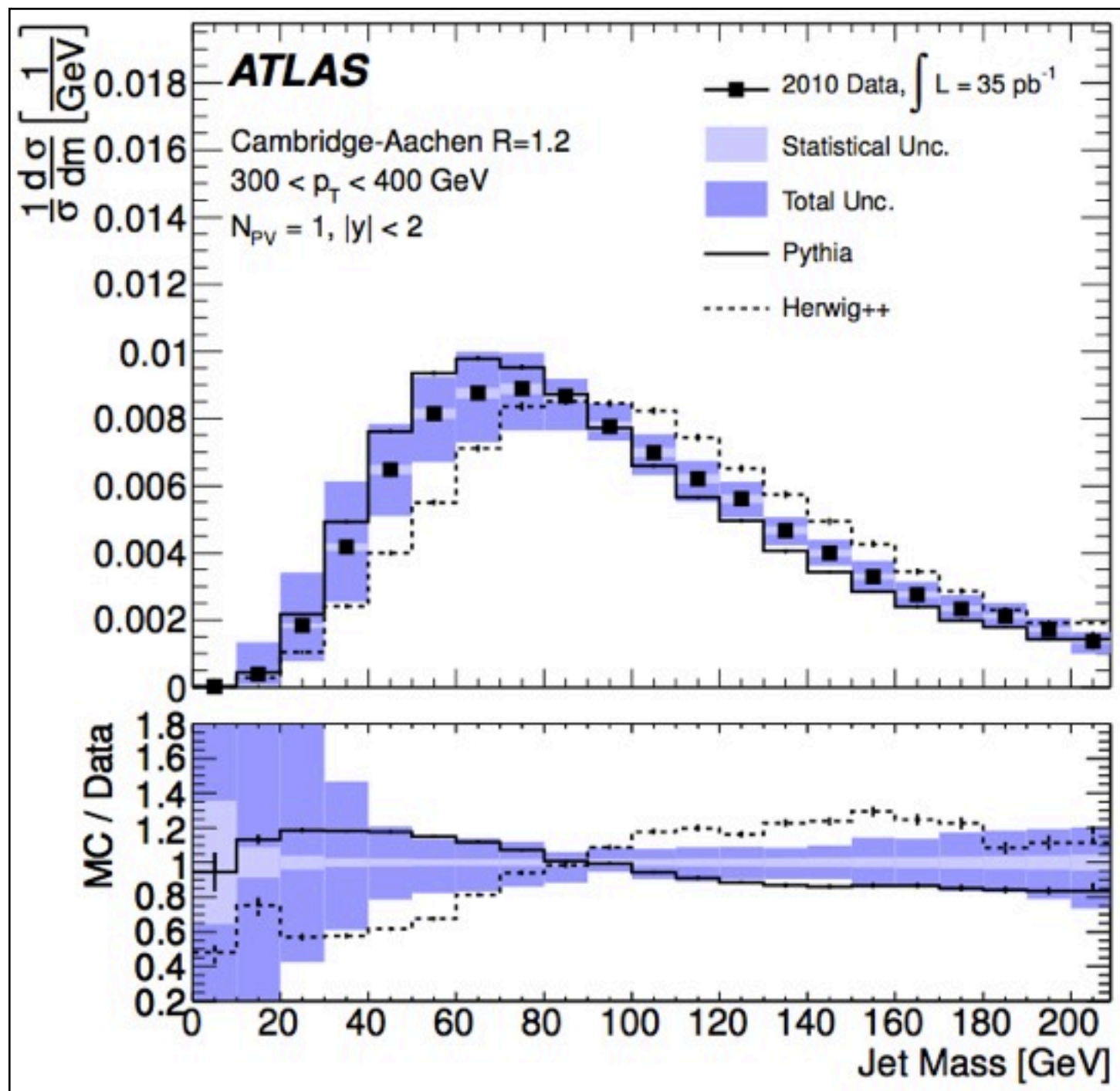
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- Angular ordered shower ( $\alpha = -1$ ) predicts most wide jets, while  $p_{\perp}$  ordered shower ( $\alpha = +1$ ) predicts narrower jets
- This is other qualitative coincidences between Pythia and Herwig
- Wideness is tunable by  $\alpha$



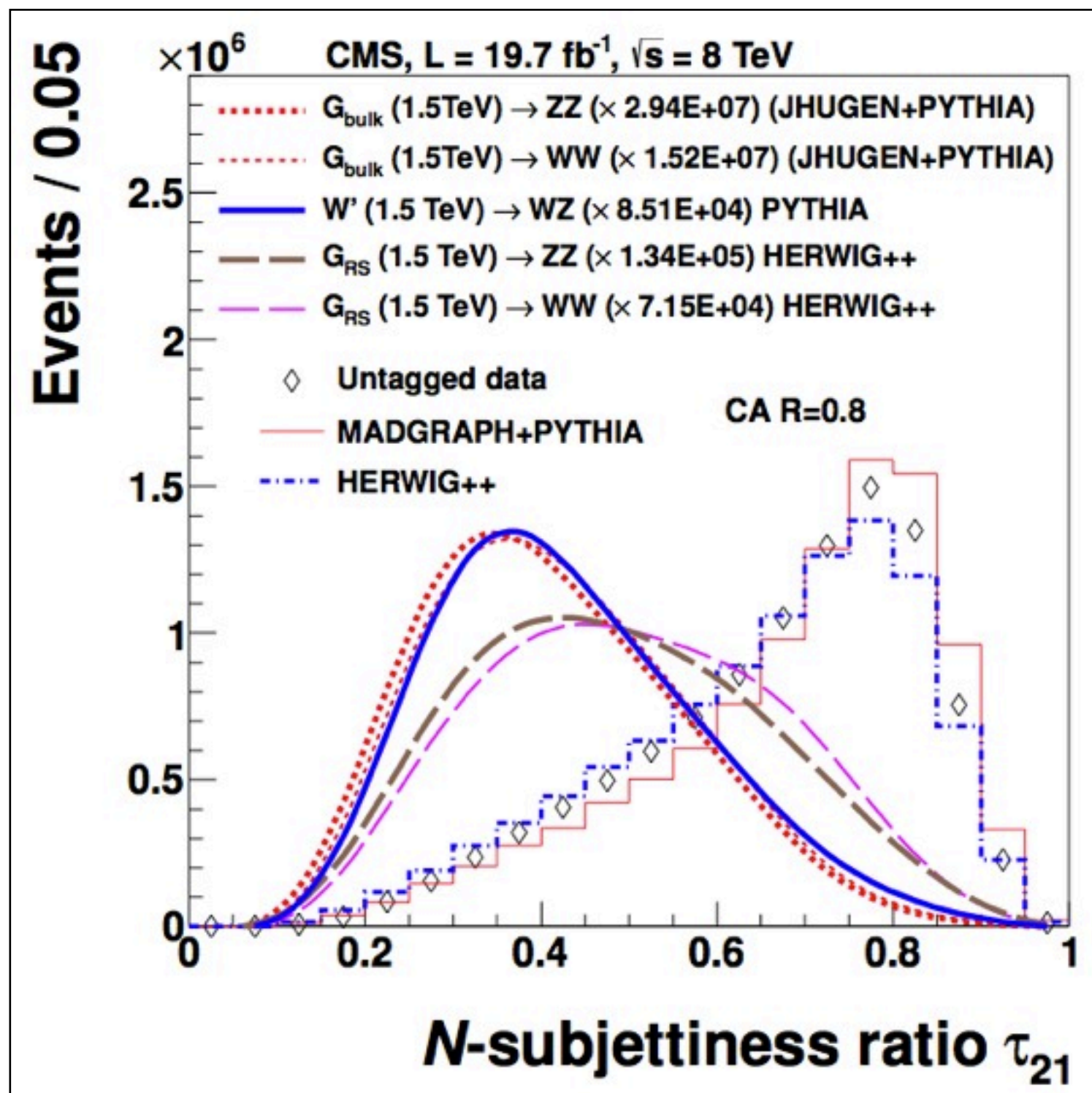
Tuned @  $\sqrt{s} = 2000$  GeV



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- Wideness is tunable by  $\alpha$



- Nature live between Pythia and Herwig



- Nature live between Pythia and Herwig