Monte Carlo review

Stefan Prestel



 $\begin{array}{c} {\rm MC4BSM~2015} \\ {\rm Fermilab,~May~18,~2015} \end{array}$

Outline

- 1) Introduction
- 2) Parton showering, higher-order calculcations and their combination.
- 3) Soft physics: Multiple interactions and hadronisation.

Know what we want to look for...

Know what we're facing...

Assess if there is a realistic chance with our current experiments ...and check before building a new experiment.

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Missing E_T and jets (a.k.a. classical SUSY)?

Compressed masses?

Dark sectors?

New bound states?

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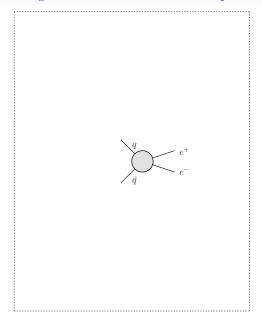
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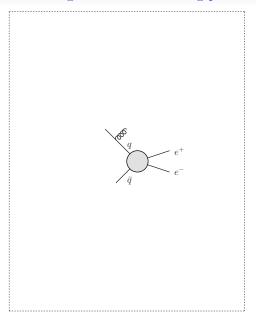
We need an accurate representation of "known" and "unknown" physics that feels like data!



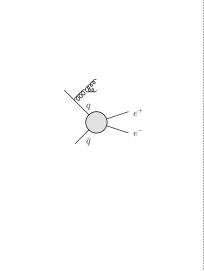
Event generation: Start from hard process



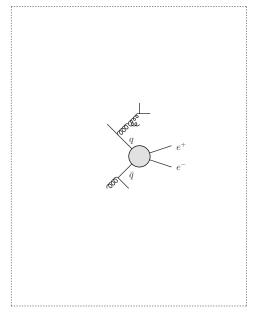
...and emit gluons from incoming partons



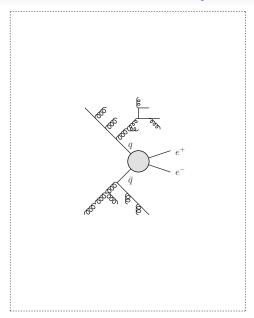
...or outgoing partons



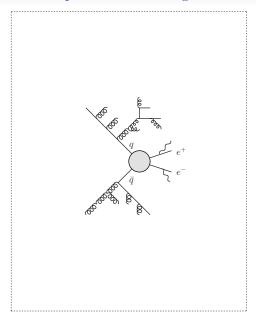
...or split gluons into quarks



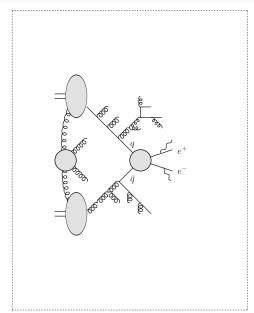
...and how to do this arbitrarily often



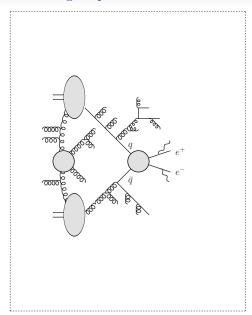
...and emit photons from charged fermions



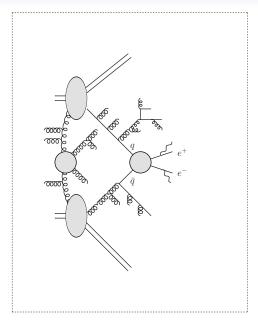
...and include multiple interactions between composite protons



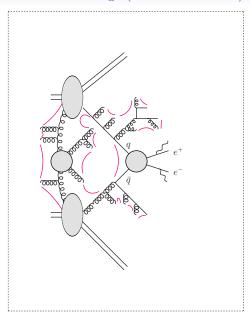
...which again produce more radiation



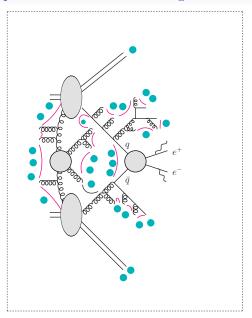
...and add beam remnants to form a colourless state



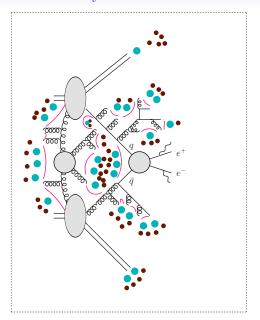
...and form strings (colour flux tubes)



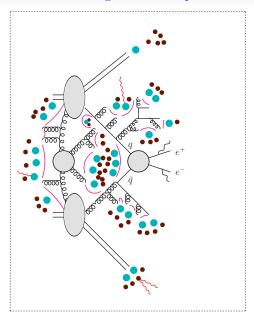
...and produce hadrons from strings and remnants



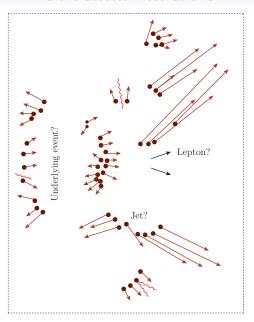
...and decay the excited hadrons



...which can again involve photons



And the detector records this...



Standard event generator frameworks

The three commonly used General Purpose Event Generators are

HERWIG	PYTHIA	SHERPA
Basic ME generator	Basic ME generator	Mature ME generator
Angular ordered \tilde{q} shower and p_{\perp} -ordered CS dipole shower	$p_{\perp} ext{-} ext{ordered}$ dipoles with ME-corrections, VINCIA antenna shower	p_{\perp} -ordered CS dipole shower, ANTS antenna shower
YFS multipole QED MPI afterburner	QED from shower Interleaved MPI	YFS multipole QED MPI afterburner
Cluster hadronisation	String hadronisation	Cluster hadronisation

2) Parton showering, higher-order calculcations and their combination

- a) Factorisation and parton showers
- b) Why we need more...
- c) NLO calculations and matching.
- d) Many-jet calculations, combining many NLO calculations.

Soft/collinear limits and splitting probabilities

Cross sections containing an additional collinear gluon factorise as

$$d\sigma(\mathsf{pp} \to \mathsf{Y} + \mathsf{g} + \mathsf{X}) \approx d\sigma(\mathsf{pp} \to \mathsf{Y} + \mathsf{X}) \int \frac{dp_{\perp}^2}{p_{\perp}^2} \frac{dz}{z} \frac{\alpha_s}{2\pi} \frac{f(\frac{\mathsf{x}_{\mathsf{g}}}{z}, t)}{f_{\mathsf{g}}(x_{\mathsf{g}}, t)} P(z)$$

with the splitting kernels P(z), independent of the process pp \rightarrow Y + X.

Multi-parton cross sections can be approximated by "dressing up" low-multiplicity results with many collinear partons.

The splitting kernels have a probabilistic interpretation:

$$\int_{p_{\perp \min}^2}^{p_{\perp \max}^2} \frac{dp_{\perp}^2}{p_{\perp}^2} \int_{z_{\min}}^{z_{\max}} dz \frac{\alpha_s}{2\pi} P(z) \equiv \begin{array}{c} \text{Probability of emitting a gluon with} \\ \text{momentum fraction } 1-z \in [z_{\min}, z_{\max}] \text{ and} \\ \text{transverse momentum } p_{\perp} \in [p_{\perp \min}, p_{\perp \max}]. \end{array}$$

Note that $\frac{dp_{\perp}^2}{p_{\perp}^2} = \frac{d\theta^2}{\theta^2} = \frac{dQ^2}{Q^2} \implies$ Evolution variable is up for debate.

Parton showering

Use probabilities to dress partons with softer partons ⇒ Jet formation!

The "naive" probability of an emission in the interval $[t, t + \delta t]$ is

$$\delta t \int_0^1 dz P(z)$$

...which gives the probability of no emission between two times

$$1 - \delta t \int dz P(z)$$

...and the probability of no emissions in n intervals of step size $\delta t/n$:

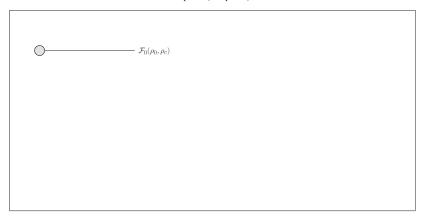
$$\left[1 - \frac{\delta t}{n} \int dz P(z)\right]^n = \exp\left\{-\int_{t}^{t+\delta t} dt \int dz P(z)\right\} = \Pi(t+\delta t,t)$$

Thus, we find

Probability of no emission Probability of an emission at t_1 $\Pi(t_0,t_1)$ P(z)

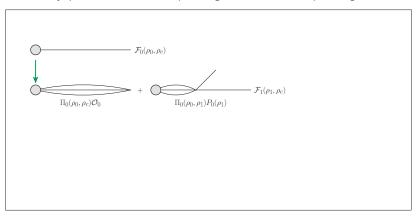
Parton showers

Parton showers start from a (simple) input state:



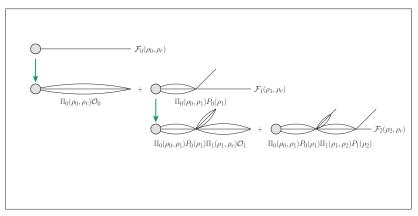
Parton showers

...and may produce no hard splitting, or a hardest splitting



Parton showers

...and then no further splitting, or a second hardest splitting, etc.



The all-order factors Π_i are called Sudakov form factors. They connect to resummation, and make jet cross sections well-behaved.

Parton showers vs. fixed order

Parton showers give an approximate multi-parton (jet) cross section which...

- + is always finite.
- + is good for any number of emissions.
- but is only valid for very small relative p_{\perp} .

Is your signal affected by (many) jets¹?

- ⇒ Need good calculation for partonic jet seeds!
- ⇒ Need something better than plain parton shower.
- ⇒ Combine the strengths of showers and fixed-order calculations!

Parton showers start from lowest-multiplicity tree-level inputs. The next step is next-to-leading order.

 $^{^1}$ Translation: You need to apply n_{jets} , $p_{\perp jet}$, H_T cuts or use "kinematic endpoint variables" like M_{T2} .

Do you need ME+PS for BSM signals?

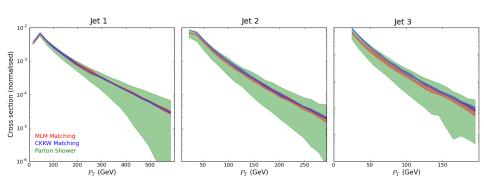


Figure: Jet p_{\perp} s for squarks+jets. PS bands are obtained by varying between "wimpy" and "power shower", merged bands by varying the merging scale from 50-200 GeV (taken from Phys.Rev. D87 (2013) 3, 035006 (Dreiner, Krämer, Tattersall)).

⇒ Improved QCD pins down the transverse momenta.

...and how good is your exclusion?

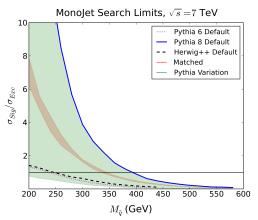
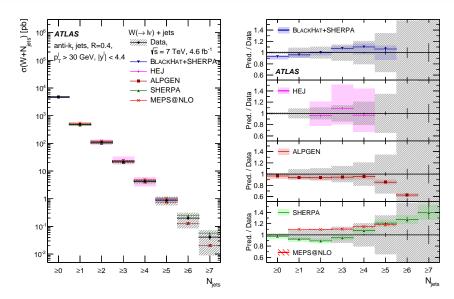


Figure: Exclusion limits for squarks+jets. PS bands are obtained by varying between "wimpy" and "power shower", merged bands by varying the merging scale from 50-200 GeV (taken from Phys.Rev.D87(2013)3,035006 (Dreiner, Krämer, Tattersall)).

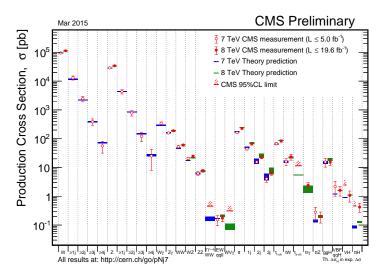
 \Rightarrow Improved QCD pins down jet momenta, reducing MC uncertainties.

Precision backgrounds: Do you worry about multi-jet states?



(Figure taken from EPJC 75 (2015) 2 82)

Precision backgrounds: Do you worry about deviations in cross sections?



 $CMS \ summary \ \left({taken \ from \ https://twiki.cern.ch/twiki/bin/view/CMSPublic/PhysicsResultsCombined} \right)$

Mission statement

Task: Combine multiple fixed-order calculations with each other and with PS into a single *one-does-it-all* prediction.

Keep highest accuracy for inclusive n-jet cross sections.

Keep PS resummation for exclusive quantities.

The current state-of-the-art is NLO merging.

Next-to-leading order calculations

Pen-and-paper: Add Born + Virtual + Real.

$$\langle \mathcal{O} \rangle^{\text{NLO}} \quad = \quad \int B_n \mathcal{O}(\Phi_n) d\Phi_n + \int V_n \mathcal{O}_n(\Phi_n) d\Phi_n + \int B_{n+1} \mathcal{O}(\Phi_n) d\Phi_{n+1}$$

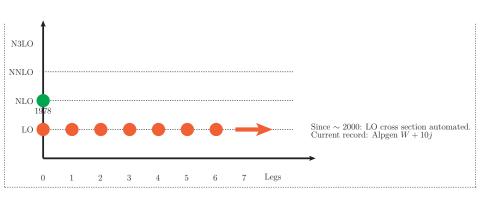
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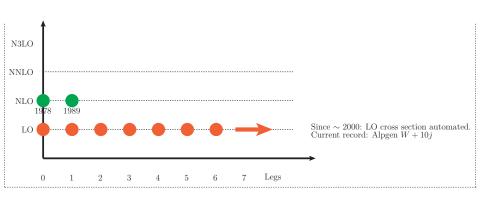
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Reality: Phase space integral separately divergent \Rightarrow Add zero!

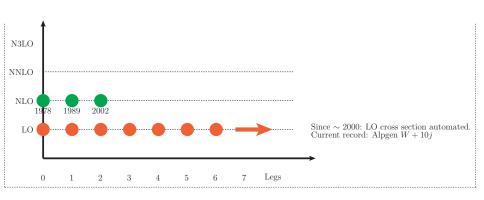
$$\langle \mathcal{O} \rangle^{\mathsf{NLO}} = \int \left[\mathbf{B}_n + \mathbf{V}_n + \int \mathbf{D}_{n+1} \right] \mathcal{O}(\Phi_n) d\Phi_n + \int \left[\mathbf{B}_{n+1} \mathcal{O}(\Phi_{n+1}) - \mathbf{D}_{n+1} \mathcal{O}(\Phi_n') \right] d\Phi_{n+1}$$



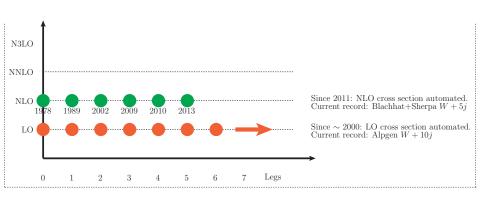
A few years ago, NLO calculation were thanks to dedicated theorists producing dedicated codes (e.g. MCFM)



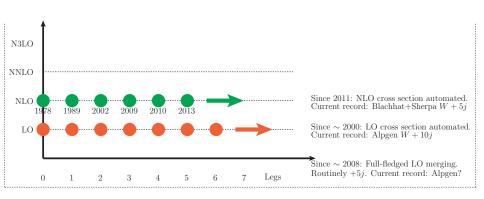
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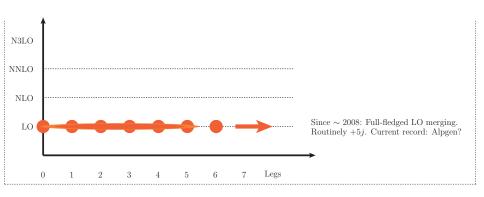


...then new unitarity techniques removed the "virtual matrix element" bottle-neck (BlackHat, HELAC-NLO)



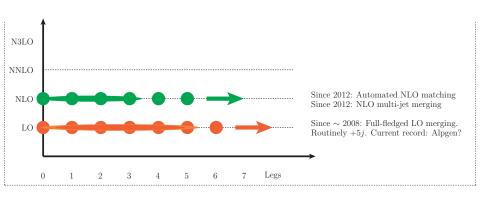
Now, you can execute these calculations yourself with tools like (BlackHat, GOSAM, OpenLoops, NJet) + Sherpa, (GOSAM, MadLoop) + MG5_aMC!

What did that mean for event simuation?



Many LO matrix elements available ⇒ Multi-jet merging.

What did that mean for event simuation?



Many NLO matrix elements available \Rightarrow Automated NLO+PS matching, NLO merging.

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Real reality: States Φ_{n+1} and Φ'_n are correlated. \Rightarrow Problematic, since further manipulations (e.g. hadronisation) can spoil the cancellations

$$\begin{split} \langle \mathcal{O} \rangle^{\mathsf{NLO}} &= \int \left[\mathrm{B}_n + \mathrm{V}_n + \mathrm{I}_n + \int d\Phi_{\mathrm{rad}} \left(\qquad - \mathrm{D}_{n+1} \right) \right] \mathcal{O}(\Phi_n) d\Phi_n \\ &+ \int \left(\mathrm{B}_{n+1} \qquad \right) \mathcal{O}(\Phi_{n+1}) \\ &+ \int \left(\qquad \qquad \right) \end{split}$$

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Real reality: States Φ_{n+1} and Φ'_n are correlated. \Rightarrow Problematic, since further manipulations (e.g. hadronisation) can spoil the cancellations \Rightarrow Add more zeros!

$$\begin{split} \langle \mathcal{O} \rangle^{\text{NLO}} &= \int \left[B_n + V_n + I_n + \int d\Phi_{\mathrm{rad}} \left(B'_{n+1} - D_{n+1} \right) \right] \mathcal{O}(\Phi_n) d\Phi_n \\ &+ \int \left(B_{n+1} \right) \mathcal{O}(\Phi_{n+1}) \\ &+ \int \left(-B'_{n+1} \mathcal{O}(\Phi_n) \right) \end{split}$$

Pen-and-paper: Add Born + Virtual + Real.

⇒ Add more zeros!

$$\langle \mathcal{O} \rangle^{\text{NLO}} \quad = \quad \int B_n \mathcal{O}(\Phi_n) d\Phi_n + \int V_n \mathcal{O}_n(\Phi_n) d\Phi_n + \int B_{n+1} \mathcal{O}(\Phi_n) d\Phi_{n+1}$$

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NLO matching

For NLO matching, we start out with a shower-dependent seed cross section and a shower Sudakov factor

$$egin{array}{lcl} \overline{\mathrm{B}}_n & = & \mathrm{B}_n + \mathrm{V}_n + \mathrm{I}_n + \int d\Phi_{\mathrm{rad}} \left(\mathrm{B}'_{n+1} - \mathrm{D}_{n+1}
ight) \\ \\ \Delta^B(t_0, t_{min}) & = & \exp \left(- \int^{t_0} d\Phi_{\mathrm{rad}} rac{\mathrm{B}'_{n+1}}{\mathrm{B}_n}
ight) \end{array}$$

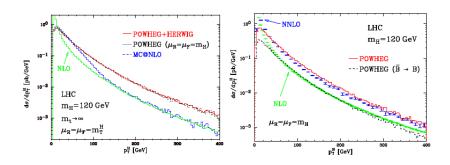
and perform a PS step on $\overline{\mathrm{B}}_{n}^{\ 1}$

$$\begin{split} \overline{B}_{n}\Delta^{B}(t_{0},t_{min})\mathcal{O}_{0}(\Phi_{n}) + \int_{0}^{t_{0}} d\Phi_{\mathrm{rad}} \overline{B}_{n} \frac{B'_{n+1}}{B_{n}} \Delta^{B}(t_{0},t)\mathcal{O}_{1}(\Phi_{n+1}) \\ + \left(B_{n+1} - B'_{n+1}\right)\mathcal{O}_{1}(\Phi_{n+1}) \end{split}$$

At $\mathcal{O}(\alpha_s^{n+1})$, this gives back the NLO cross section. Common schemes are

POWHEG:
$$B'_{n+1} = B_{n+1} \cdot \frac{h'}{h^2 + p_{\perp}^2}$$
, $t_0 = s$
MC@NLO: $B'_{n+1} = D_{n+1} \cdot \Theta(\mu_O - t(S_{+1}))$, $\mu_O = kQ^2$

...a cautionary tale



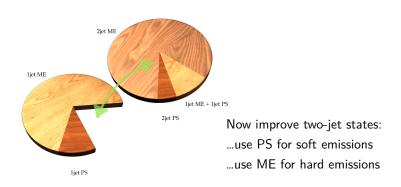
NLO+PS methods usually lead to a smaller differences. There are striking counter-examples where large differences are consistent with higher order effects.

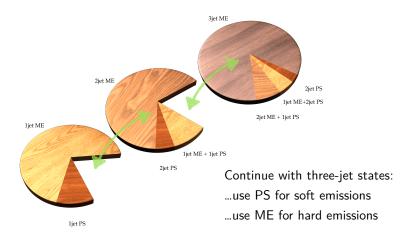
Large differences usually appear in the "LO" part of the prediction

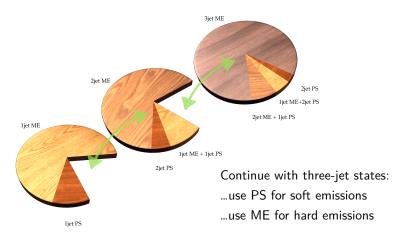
Good news: We can improve on this!



Look at one-jet states:
...use PS for soft emissions
...use ME for hard emissions







The dependence on the hard-soft separation (merging scale) is removed by resummation, i.e. by including Sudakov form factors and a running coupling. (Further tricks are often necessary)

Differences merging/matching

NLO matching is NLO-correct.

⇒ Good uncertainty estimate, limited applicability.

Merging can be used to combine "any number" of LO calculations.

⇒ Questionable uncertainty, broad applicability.

We can be lucky if

- ...NLO matched calculation describes very exclusive data.
- ...merged calculations describe normalisations.

It would be unreasonable to expect Luck in one process = Luck in another process

 \Rightarrow Both strategies are incomplete and need to be combined for a satisfactory result.

NLO matching \otimes merging = NLO merging

Any leading-order method \mathbf{X} contains approximate $\mathcal{O}(\alpha_s)$ -corrections from the expansion of the necessary all-order factors (e.g. Sudakovs).

But we want to use more accurate NLO results whenever possible!

NLO matching \otimes merging = NLO merging

Any leading-order method \mathbf{X} contains approximate $\mathcal{O}(\alpha_s)$ -corrections from the expansion of the necessary all-order factors (e.g. Sudakovs).

But we want to use more accurate NLO results whenever possible!

To do NLO multi-jet merging for your preferred LO scheme **X**, do:

- \diamond Subtract approximate $\mathcal{O}(\alpha_{\rm s})$ -terms from merged calculation **X**, add multiple NLO calculations.
- Ensure that real-emission parts of fixed-order calculations do not overlap.
- Ensure that fixed-order and shower calculations do not overlap ...just as we did at leading order.
- Adjust higher orders to suit your other needs.
- ⇒ X@NLO

LHC Run II+ era theory predictions (H+jets)

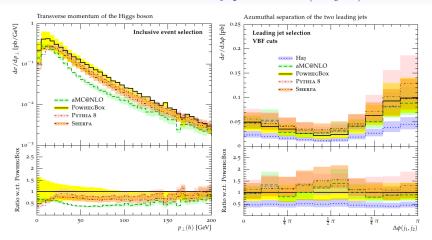
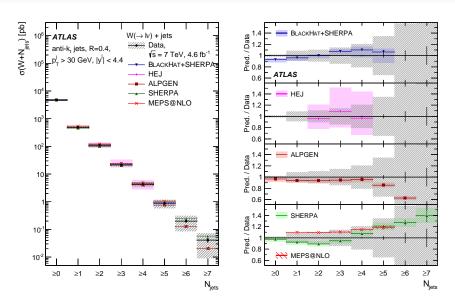


Figure: $p_{\perp,H}$ and $\Delta\phi_{12}$ for gg \rightarrow H after merging (H+0)@NLO, (H+1)@NLO, (H+2)@NLO, (H+3)@LO, compared to other generators.

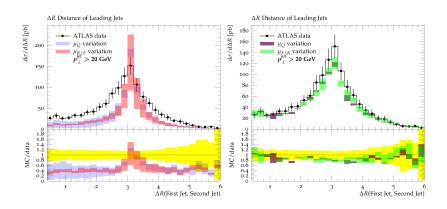
⇒ The generators come closer together if enough fixed-order matrix elements are employed. Uncertainties in exclusive regions can still be large.

NLO merged results: The end of a 10-year journey



...but in general theory uncertainties decrease (from EPJC 75 (2015) 2 82) $_{49/77}$

NLO merged results: The end of a 10-year journey



W(+jets) production at ATLAS (PRD 85 (2012) 092002) in PYTHIA8 UNLOPS.

Back to the big picture

However

```
...showers are still only QCD/QED<sup>1</sup>
```

...and at "low" accuracy.

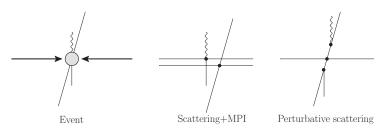
...there's more to a realistic state than $2 \rightarrow n$ scattering.

¹ No longer true! Electroweak effects are also included by now.

3) Soft physics: Multiple interactions and hadronisation.

- a) Multiparton interactions
- b) Hadronisation
- c) Why should I care?

Realistic final states (MPI)



Assume we understand weak showers and matrix element merging. What if a state mixes "soft" MPI and hard perturbative physics?

At LHC, jets from MPI are relatively soft. \Rightarrow Small (?) effects. But the effects are usually directly in the "resummation" region.

- \Rightarrow Competition should be understood.
 - \diamond Can we simply only look at jets with large p_{\perp} , i.e ignore competition?
 - ♦ Can we improve the PS accuracy without worrying about MPI?

Multiple interactions

Multiple interactions between the composite protons are supported by 30 years of evidence:

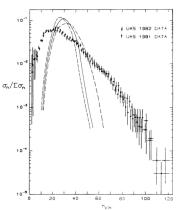


FIG. 3. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs simple models: dashed low p_T only, full including hard scatterings, dash-dotted also including initial- and final-state radiation.

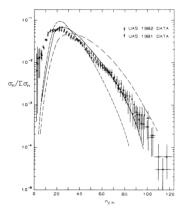


FIG. 5. Charged-multiplicity distribution at 540 GeV, UA5 results (Ref. 32) vs impact-parameter-independent multiple-interaction model: dashed line, p_{Tmin} =2.0 GeV; solid line, p_{Tmin} =1.6 GeV; dashed-dotted line, p_{Tmin} =1.2 GeV.

Multiple interactions

Measurements indicate that the "underlying event" (UE) has a mini-jet structure. This leads to the following model.

- 1. Overlay QCD (QED) 2 ightarrow 2 transitions on top of the hard interaction.
- 2. Introduce (non-perturbative colour-screening) parameter $p_{\perp 0}$ into $2 \to 2$ cross section regularise divergence.
- 3. Order multiple scatterings in descending p_{\perp} sequence, with cut-off $p_{\perp min}$ and scattering probability $\approx \frac{1}{\sigma_{total}} \frac{d\sigma^{reg}(2 \rightarrow 2)}{dp_{\perp}}$
- 4. Ensure that energy, momentum, colour, flavour are conserved.

 \Rightarrow MPI model for the UE of soft jets in hadronic collisions with a handful of parameters. MPI models are tuned to UE measurements.

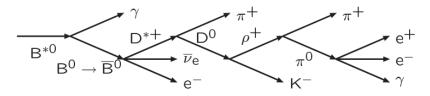
Hadronisation

...our result still contains coloured partons \Rightarrow Needs to be converted to hadrons! Two prescriptions have passed the test of time:

Cluster	String
Form hadrons by decaying "preconfined" colourless clusters of partons.	Colour flux tubes (strings, junctions) between partons break to form hadrons.
Gluons split non-perturbatively to $q ar q$	Gluons are kink on string.
Many-parameter energy-momentum structure.	Few-parameter energy-momentum structure.
Few-parameter flavour chemistry.	Many-parameter flavour chemistry.

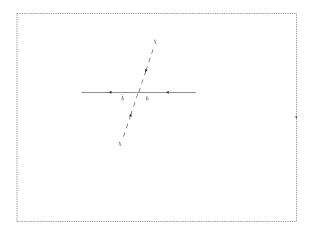
Hadron decays

Fragmentation can produce excited hadrons, which will then decay, e.g.

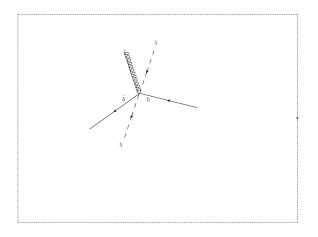


Most particles are produced in this part.

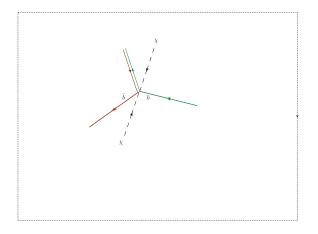
- \Rightarrow Process has to be modelled for the correct jet structure by
- ...Hadronic matrix elements for some (important) decays.
- ...PDG decay tables for others. If tables are incomplete, be creative.



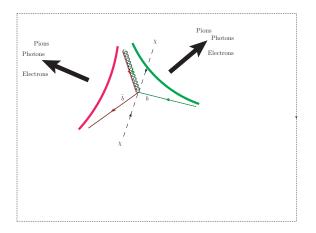
Assume dark matter annihilates into bottom quarks.



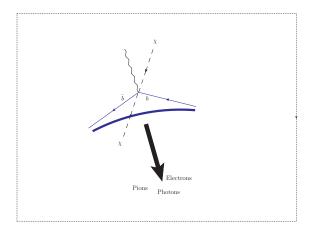
The quarks will radiate.



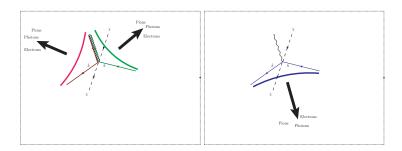
If the quarks radiate a gluon, we find two colour lines



The colour lines form strings, which form hadrons and photons in the region spanned by the string.



If a photon were radiated instead, the string would be spanned between the bottom quarks, and there would be no activity close to the "hard" photon.



This difference is called the string effect. It is model-dependent and may (partially) stem from tunes to data.

If your favorite DM primarily annihilates into quarks, and your primary concern is the photon spectrum, you *might* have to worry about hadronisation¹. So be careful:)

 $^{^{1}}$ The same effect can also be obtained from perturbative physics - it's not obvious if the photons are imprinted by peturbative or non-perturbative effects.

Summary

- Event generation can be divided into subproblems.
- Massive progress in fixed-order calculations, and including accurate (multi-jet) results into parton showers.
- Background estimations rather reliable now
 ...but can (should?) equally well be applied to signal processes.
- Less dramatic progress on the all-order structure of showers although showers do continuously get better.
- Event simulation more than perturbative 2 → n scatterings.
 Multiparton interactions are omnipresent at hadron colliders.
 Hadronisation is a must at colliders and beyond.

Summary

- Event generation can be divided into subproblems.
- Massive progress in fixed-order calculations, and including accurate (multi-jet) results into parton showers.
- Background estimations rather reliable now
 ...but can (should?) equally well be applied to signal processes.
- Less dramatic progress on the all-order structure of showers although showers do continuously get better.
- Event simulation more than perturbative $2 \rightarrow n$ scatterings. Multiparton interactions are omnipresent at hadron colliders. Hadronisation is a must at colliders and beyond.

Most simple signals are excluded. So we can finally have some fun!

Back-up supplement

LO merging

```
MLM available with Alpgen + (Herwig6, Pythia6/8), Madgraph + (Herwig++, Pythia6/8), Whizard + Pythia6 CKKW no longer available (?) in Sherpa, Herwig++ CKKW-L / METS available in Sherpa, (Alpgen, Madgraph,...) + Pythia8 UMEPS available in (Alpgen, Madgraph,...) + (Herwig++, Pythia8) matching
```

NLO matching

NLO merging
NNLO matching
Other improvements

```
LO merging
NLO matching
POWHEG available in Sherpa, Herwig++, POWHEG-BOX + (Herwig6/++, Pythia6/8)
MC@NLO available in Sherpa, Herwig++, aMC@NLO + (Herwig6/++, Pythia6/8)
NLO merging
NNLO matching
Other improvements
```

```
LO merging

NLO matching

NLO merging

MEPS@NLO available in Sherpa

UNLOPS available in Herwig++, (POWHEG-BOX, aMC@NLO) + Pythia8

FXFX available in aMC@NLO + (Herwig++, Pythia8)

NNLO matching

Other improvements
```

LO merging
NLO matching
NLO merging
NNLO matching
UN²LOPS available as plugin to Sherpa
MINLO-NNLOPS available through POWHEG-BOX
Other improvements

NLO merging
NNLO matching
Other improvements

MiNLO available through POWHEG-BOX
Iterated ME corrections available through VINCIA
ME reweighting available in HEJ
KRKC proposed new NLO matching

GENEVA proposed higher-logs + fixed-order (NLO, NNLO) + showers

LO merging
NLO matching

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The book: Collins, Perturbative Quantum Chromodynamics Collins, Soper, Sterman (Nucl.Phys.B250(1985)199)

Peter Skands' TASI lectures (arXiv:1207.2389)

Factorisation: Divide and conquer

Many older lectures of MCNet (montecarlonet.org) and CTEQ schools.

Stefan Höche's TASI lectures (http://slac.stanford.edu/shoeche/tasi14/ws/tasi.pdf)

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                               Herwig++ (Eur.Phys.J. C72 (2012) 2187)
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METS (JHEP 0911 (2009) 038, JHEP 0905 (2009) 053)
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Pythia (JHEP 1302 (2013) 094) Herwig (JHEP 1308 (2013) 114) Sherpa (arXiv:1405.3607)
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                                               Plots taken from arXiv:1401.7971
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                                             arXiv:1405.1067
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                                       arXiv:1407.2940
UN<sup>2</sup>LOPS: arXiv:1405.3607
                            arXiv:1407 3773
GENEVA: JHEP 1309 (2013) 120 JHEP 1406 (2014) 089
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Parton shower basics

Parton showers are unitary all-order operators:

$$\begin{split} \text{PS} \Big[\sigma^{\text{ME}}_{+0} \Big] & = & \sigma^{\text{PS}}_{+0} \, + \, \sigma^{\text{PS}}_{+1} \, + \, \sigma_{+ \, \geq \, 2} \\ & = & \sigma^{\text{ME}}_{+0} \Pi_{\mathbb{S}_{+0}} \left(\rho_{0}, \rho_{\text{min}} \right) & \longleftarrow \text{ 0 emissions in } \left[\rho_{0}, \rho_{\text{min}} \right] \\ & + & \sigma^{\text{ME}}_{+0} \Pi_{\mathbb{S}_{+0}} \left(\rho_{0}, \rho_{1} \right) \alpha_{s} w_{f}^{0} P_{0} \Pi_{\mathbb{S}_{+1}} \left(\rho_{1}, \rho_{\text{min}} \right) \longleftarrow \text{ 1 emission in } \left[\rho_{0}, \rho_{\text{min}} \right] \\ & + & \sigma^{\text{ME}}_{+0} \Pi_{\mathbb{S}_{+0}} \left(\rho_{0}, \rho_{1} \right) \alpha_{s} w_{f}^{0} P_{0} \Pi_{\mathbb{S}_{+1}} \left(\rho_{1}, \rho_{2} \right) \alpha_{s} w_{f}^{1} P_{1} \left[\Pi_{\mathbb{S}_{+2}} \left(\rho_{2}, \rho_{\text{min}} \right) + \ldots \right] \\ & \qquad \qquad \uparrow & \uparrow \\ & \text{ 2 or more emissions in } \left[\rho_{0}, \rho_{\text{min}} \right] \end{split}$$

 $\stackrel{!}{=} \sigma^{\mathsf{ME}}_{+0}$ The no-emission probabilities

$$\Pi_{\delta_{+i}}\left(\rho_{1},\rho_{2}\right)=\exp\left\{-\int_{\rho_{2}}^{\rho_{1}}d\rho\alpha_{s}w_{j}^{i}P_{i}\right\}$$

define exclusive cross sections and remove the overlap between samples!

CKKW(-L)

Aim: Combine multiple tree-level calculations with each other and (PS) resummation. Fill in soft and collinear regions with parton shower.

$$\begin{split} \langle \mathcal{O} \rangle &= B_0 \mathcal{O}(S_{+0j}) \\ &- \int d\rho \ B_0 P_0(\rho) \Theta_>^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho) \mathcal{O}(S_{+0j}) \\ &+ \int B_1 \Theta_>^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho) \mathcal{O}(S_{+1j}) \\ &- \int d\rho \ B_1 P_1(\rho) \Theta_>^{(2)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \Pi_{S_{+1}}(\rho_1, \rho) \mathcal{O}(S_{+1j}) \\ &+ \int B_2 \Theta_>^{(2)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \Pi_{S_{+1}}(\rho_1, \rho) \mathcal{O}(S_{+2j}) \end{split}$$

Changes inclusive cross sections

⇒ Can contain numerically large (sub-leading) logs.

⇒ Needs fixing!

Bug vs. Feature in CKKW(-L)

The ME includes terms that are not compensated by the PS approximate virtual corrections (i.e. Sudakov factors).

These are the improvements that we need to describe multiple hard jets!

If we simply add samples, the "improvements" will degrade the inclusive cross section: σ_{inc} will contain $\ln(t_{\rm MS})$ terms.

THE INCLUSIVE CROSS SECTION DOES NOT CONTAIN LOGS RELATED TO CUTS ON HIGHER MULTIPLICITIES.

Traditional approach: Don't use a too small merging scale.

 \rightarrow Uncancelled terms numerically not important.

Unitary approach¹:

Use a (PS) unitarity inspired approach exactly cancel the dependence of the inclusive cross section on $t_{\rm MS}$.

Unitarised ME+PS

Aim: If you add too much, then subtract what you add!

$$\begin{split} \langle \mathcal{O} \rangle &= B_0 \mathcal{O}(S_{+0j}) \\ &- \int d\rho \ B_1 \Theta_>^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho) \mathcal{O}(S_{+0j}) - \int d\rho \ B_2 \Theta_>^{(2)} \Theta_<^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho) \mathcal{O}(S_{+0j}) \\ &+ \int B_1 \Theta_>^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho) \mathcal{O}(S_{+1j}) \\ &- \int d\rho \ B_2 \Theta_>^{(2)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \Pi_{S_{+1}}(\rho_1, \rho) \mathcal{O}(S_{+1j}) \\ &+ \int B_2 \Theta_>^{(2)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \Pi_{S_{+1}}(\rho_1, \rho) \mathcal{O}(S_{+2j}) + \int B_2 \Theta_>^{(2)} \Theta_<^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \mathcal{O}(S_{+2j}) \end{split}$$

Inclusive cross sections preserved by construction.

Cancellation between different "jet bins".

 \Rightarrow Statistics needs fixing.

NLO matching with MC@NLO

Aim: Achieve NLO for inclusive +0-jet, and LO for inclusive +1-jet observables and attach PS resummation.

To get there, remember that the (regularised) NLO cross section is

$$\begin{split} \mathrm{B}_{\mathrm{NLO}} &= & \left[\mathrm{B}_{n} + \mathrm{V}_{n} + \mathrm{I}_{n} \right] \mathcal{O}_{0} + \int d\Phi_{\mathrm{rad}} \left(\mathrm{B}_{n+1} \mathcal{O}_{1} - \mathrm{D}_{n+1} \mathcal{O}_{0} \right) \\ &= & \left[\mathrm{B}_{n} + \mathrm{V}_{n} + \mathrm{I}_{n} \right] \mathcal{O}_{0} + \int d\Phi_{\mathrm{rad}} \left(\mathrm{S}_{n+1} \mathcal{O}_{0} - \mathrm{D}_{n+1} \mathcal{O}_{0} \right) \\ &+ \int d\Phi_{\mathrm{rad}} \left(\mathrm{S}_{n+1} \mathcal{O}_{1} - \mathrm{S}_{n+1} \mathcal{O}_{0} \right) + \int d\Phi_{\mathrm{rad}} \left(\mathrm{B}_{n+1} \mathcal{O}_{1} - \mathrm{S}_{n+1} \mathcal{O}_{1} \right) \end{split}$$

where S_{n+1} are some additional "transfer functions", e.g. the PS kernels.

Red term is the $\mathcal{O}(\alpha_s)$ part of a shower from B_n . \Rightarrow Discard from $B_{\rm NLO}$.

Thus, we have the seed cross section

$$\widehat{\mathbf{B}}_{\mathrm{NLO}} = \left[\mathbf{B}_{n} + \mathbf{V}_{n} + \mathbf{I}_{n} + \int d\Phi_{\mathrm{rad}} \left(\mathbf{S}_{n+1} - \mathbf{D}_{n+1} \right) \right] \mathcal{O}_{0} + \int d\Phi_{\mathrm{rad}} \left(\mathbf{B}_{n+1} - \mathbf{S}_{n+1} \right) \mathcal{O}_{1}$$

This is not the NLO result...but showering the \mathcal{O}_0 -part will restore this!

UMEPS, MC@NLO-style (Plätzer)

Aim: Combine multiple tree-level calculations with each other and (PS) resummation. Fill in soft and collinear regions with parton shower.

$$\begin{split} \langle \mathcal{O} \rangle &= B_0 \Pi_{S_{+0}}(\rho_0, \rho_{MS}) \mathcal{O}(S_{+0j}) \\ &- \int d\rho \ [B_1 - B_0 P_0(\rho)] \, \Theta_>^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho) \mathcal{O}(S_{+0j}) \\ &+ \int B_1 \Theta_>^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho) \Pi_{S_{+1}}(\rho, \rho_{MS}) \mathcal{O}(S_{+1j}) \\ &- \int d\rho \ [B_2 - B_1 P_1(\rho)] \, \Theta_>^{(2)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \Pi_{S_{+1}}(\rho_1, \rho) \mathcal{O}(S_{+1j}) \\ &+ \int B_2 \Theta_>^{(2)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \Pi_{S_{+1}}(\rho_1, \rho) \mathcal{O}(S_{+2j}) \, + \int B_2 \Theta_>^{(2)} \Theta_<^{(1)} w_f w_{\alpha_s} \Pi_{S_{+0}}(\rho_0, \rho_1) \mathcal{O}(S_{+2j}) \end{split}$$

Inclusive cross sections preserved by construction. Less cancellation between different "jet bins" fixed. \Longrightarrow Statistics okay.

Start with UMEPS:

$$\begin{split} \langle \mathcal{O} \rangle &= \int d\phi_0 \bigg\{ \mathcal{O}(S_{+0j}) \Bigg(\begin{array}{ccc} B_0 + & & & - & \int \widehat{B}_{1 \to 0} & & - & \int \widehat{B}_{2 \to 0} \Bigg) \\ &+ \int \mathcal{O}(S_{+1j}) \Bigg(& & \widehat{B}_1 & & - & \int \widehat{B}_{2 \to 1} & & \bigg) &+ \int \!\! \int \!\! \mathcal{O}(S_{+2j}) \widehat{B}_2 \end{array} \bigg\} \end{split}$$

Remove all unwanted $\mathcal{O}(\alpha_s^n)$ - and $\mathcal{O}(\alpha_s^{n+1})$ -terms:

$$\begin{split} \langle \mathcal{O} \rangle &= \int d\phi_0 \bigg\{ \mathcal{O}(s_{+0j}) \Bigg(& - \Bigg[\int \widehat{B}_{1 \to 0} \Bigg]_{-1,2} & - \int \widehat{B}_{2 \to 0} \Bigg) \\ &+ \int \mathcal{O}(s_{+1j}) \left(& \left[\widehat{B}_1 \right]_{-1,2} - \left[\int \widehat{B}_{2 \to 1} \right]_{-2} \right) & + \int \!\! \int \!\! \mathcal{O}(s_{+2j}) \widehat{B}_2 \ \bigg\} \end{split}$$

Add full NLO results:

$$\begin{split} \langle \mathcal{O} \rangle &= \int d\phi_0 \bigg\{ \mathcal{O}(s_{+0j}) \Bigg(\qquad \widetilde{B}_0 \qquad \qquad - \left[\int \widehat{B}_{1 \to 0} \right]_{-1,2} \qquad - \int \widehat{B}_{2 \to 0} \Bigg) \\ &+ \int \mathcal{O}(s_{+1j}) \left(\widetilde{B}_1 + \left[\widehat{B}_1 \right]_{-1,2} - \left[\int \widehat{B}_{2 \to 1} \right]_{-2} \right) \\ &+ \int \int \mathcal{O}(s_{+2j}) \widehat{B}_2 \ \bigg\} \end{split}$$

Unitarise:

$$\begin{split} \langle \mathcal{O} \rangle &= \int d\phi_0 \bigg\{ \mathcal{O}(s_{+0j}) \Bigg(\qquad \widetilde{B}_0 \, - \int_{s} \widetilde{B}_{1 \to 0} \, + \int_{s} B_{1 \to 0} \, - \Bigg[\int \widehat{B}_{1 \to 0} \Bigg]_{-1,2} \, - \int_{s} B_{2 \to 0}^{\uparrow} \, - \int \widehat{B}_{2 \to 0} \Bigg) \\ &+ \int \mathcal{O}(s_{+1j}) \left(\, \widetilde{B}_1 \, + \, \left[\widehat{B}_1 \right]_{-1,2} \, - \left[\int \widehat{B}_{2 \to 1} \right]_{-2} \right) \, + \int \!\! \int \!\! \mathcal{O}(s_{+2j}) \widehat{B}_2 \, \bigg\} \end{split}$$

Comparison of NLO merging schemes

FxFx: Restricts the range of merging scales. Cross section changes thus numerically small.

Probably fewest counter events.

MEPS@NLO: Improved, colour-correct Sudakov of MC@NLO for the first emission. Larger $t_{\rm MS}$ range. Smaller cross section changes. Improved resummation in process-independent way.

UNLOPS: Inclusive observables strictly NLO correct. Further shower improvements also directly improve the results.

Many counter events if done naively.

MiNLO: applies analytical (N)NLL Sudakov factors, which cancel problematic logs, only merging two multiplicities. Was moulded into an NNLO matching.

The next step(s): Matching @ NNLO

Aim: For important processes – lumi monitors like Drell-Yan, precision studies (ggH, ZH, WBF,...) – reduce uncertainties and remove personal bias. But make sure all other improvements stay intact!

Observation: If an NLO merged calculation leads to a well-defined zero-jet inclusive cross section, it is easy to upgrade this cross section to NNLO.

 \Longrightarrow Fulfilled by MiNLO and UNLOPS

 \Longrightarrow NNLO+PS schemes have been implemented (MiNLO-NNLOPS and UN 2 LOPS)

Deriving an UN²LOPS matching

We basically follow a "merging strategy":

- Pick calculations to combine (two MC@NLOs) with each other and with the PS resummation.
- Remove kinematic overlaps between the two MC@NLOs by dividing the one-jet phase space.
- Reweight one-jet MC@NLO (to make it exclusive \leftrightarrow want to describe hardest jet with this), remove all undesired terms at $\mathcal{O}(\alpha_s^{1+1})$ and make sure that the whole thing is numerically stable. Reweight subtractions with $\Pi_{S_{+0}}$ to be able to group them with virtuals.
- Add and subtract reweighted one-jet MC@NLO, (→ unitarise) to ensure inclusive zero-jet cross section is unchanged w.r.t. NLO.
- Remove all terms up to $\mathcal{O}(\alpha_s^2)$ in the zero-jet contribution, replace by NNLO jet-vetoed cross section.

Aim: Combine just two NLO calculations, then upgrade to NNLO directly.

Start over again, now combining MC@NLO's because those are resonably stable. Thus:

- \diamond Use 0-jet matched (MC@NLO $_0)$ and 1-jet matched calculation (MC@NLO $_1).$
- \diamond Remove hard $(q_T > \rho_{\rm MS})$ reals in MC@NLO $_0$.
- \diamond Reweight B_1 of MC@NLO $_1$ with "zero-jet Sudakov" factor $\Pi_{S_{+0}}/\alpha_{S}$ running.
- \diamond Reweight NLO part \widetilde{B}_1^R of MC@NLO $_1$ with "zero-jet Sudakov" factor.
- \diamond Subtract erroneous $\mathcal{O}(\alpha_s^{+1})$ terms multiplying B_1 .
- \diamond Reweight subtractions with $\Pi_{S_{+0}}$ to be able to group them with $\widetilde{B}_{1}^{R}.$
- \diamond Put $\rho_{\rm MS} \rightarrow \rho_{\rm c} < 1 {\rm GeV.} \; (\rightarrow$ MC@NLO $_{\rm 0}$ becomes exclusive NLO)
- \diamond Unitarise by subtracting the processed MC@NLO $_1^\prime$ from the "zero-q_T bin".
- \diamond Remove all terms up to α_s^2 from the "zero- q_T bin" and add the q_T -vetoed NNLO cross section.
- $\Rightarrow \sigma_{inclusive}$ @ NNLO, resummation as accurate as Sudakov, stats fine. NNLO logarithmic parts from q_T -vetoed TMDs (EFT calculation), hard coefficients from q_T -subtraction (i.e. DYNNLO, HNNLO), power corrections from MC@NLO $_1$.

$$\begin{split} \mathcal{O}^{(\mathrm{UN^2LOPS})} &= \int \!\! d\Phi_0 \, \bar{\bar{B}}_0^{q_{T,\mathrm{cut}}}(\Phi_0) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \, \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \Big] \, B_1(\Phi_1) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Pi_0(t_1,\mu_Q^2) \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \, B_1(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, \tilde{B}_1^R(\Phi_1) \, \mathcal{O}(\Phi_0) + \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \Pi_0(t_1,\mu_Q^2) \, \tilde{B}_1^R(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_2 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, H_1^R(\Phi_2) \, \mathcal{O}(\Phi_0) + \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_2 \, \Pi_0(t_1,\mu_Q^2) \, H_1^R(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \\ &+ \int_{\mathcal{O}} \!\! d\Phi_2 \, H_1^E(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \end{split}$$

$$\begin{split} \mathcal{O}^{(\mathrm{UN^2LOPS})} &= \int \!\! d\Phi_0 \, \bar{\bar{\mathrm{B}}}_0^{q_{\mathrm{T,cut}}}(\Phi_0) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{\mathrm{T,cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1, \mu_Q^2) \, \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1, \mu_Q^2) \Big) \Big] \, \mathrm{B}_1(\Phi_1) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{\mathrm{T,cut}}} \!\! d\Phi_1 \, \Pi_0(t_1, \mu_Q^2) \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1, \mu_Q^2) \Big) \, \mathrm{B}_1(\Phi_1) \, \bar{\mathcal{F}}_1(t_1, \mathcal{O}) \\ &+ \int_{q_{\mathrm{T,cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1, \mu_Q^2) \Big] \, \tilde{\mathrm{B}}_1^{\mathrm{R}}(\Phi_1) \, \mathcal{O}(\Phi_0) + \int_{q_{\mathrm{T,cut}}} \!\! d\Phi_1 \, \Pi_0(t_1, \mu_Q^2) \, \tilde{\mathrm{B}}_1^{\mathrm{R}}(\Phi_1) \, \bar{\mathcal{F}}_1(t_1, \mathcal{O}) \\ &+ \int_{q_{\mathrm{T,cut}}} \!\! d\Phi_2 \, \Big[1 - \Pi_0(t_1, \mu_Q^2) \Big] \, \mathrm{H}_1^{\mathrm{R}}(\Phi_2) \, \mathcal{O}(\Phi_0) + \int_{q_{\mathrm{T,cut}}} \!\! d\Phi_2 \, \Pi_0(t_1, \mu_Q^2) \, \mathrm{H}_1^{\mathrm{R}}(\Phi_2) \, \mathcal{F}_2(t_2, \mathcal{O}) \\ &+ \int_{q_{\mathrm{T,cut}}} \!\! d\Phi_2 \, \, \mathrm{H}_1^{\mathrm{E}}(\Phi_2) \, \mathcal{F}_2(t_2, \mathcal{O}) \end{split}$$

Note that this is just an extention of the old Sudakov veto algorithm:

Run trial shower on the reconstructed zero-jet state,

If trial shower produces an emission, keep zero-jet kinematics and stop; else start PS off one-jet state.

$$\begin{split} \mathcal{O}^{(\mathrm{UN^2LOPS})} &= \int \!\! d\Phi_0 \, \bar{\bar{B}}_0^{q_{7,\mathrm{cut}}}(\Phi_0) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{7,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \, \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \Big] \, B_1(\Phi_1) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{7,\mathrm{cut}}} \!\! d\Phi_1 \, \Pi_0(t_1,\mu_Q^2) \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \, B_1(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{7,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, \tilde{B}_1^R(\Phi_1) \, \mathcal{O}(\Phi_0) + \int_{q_{7,\mathrm{cut}}} \!\! d\Phi_1 \Pi_0(t_1,\mu_Q^2) \, \tilde{B}_1^R(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{7,\mathrm{cut}}} \!\! d\Phi_2 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, H_1^R(\Phi_2) \, \mathcal{O}(\Phi_0) + \int_{q_{7,\mathrm{cut}}} \!\! d\Phi_2 \, \Pi_0(t_1,\mu_Q^2) \, H_1^R(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \\ &+ \int_{q_{7,\mathrm{cut}}} \!\! d\Phi_2 \, H_1^E(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \end{split}$$

Note: $\left[1 - \Pi_0(t_1, \mu_Q^2)\right] \tilde{B}_1^R$ etc. comes from using q_T -vetoed cross sections.

$$\begin{split} \mathcal{O}^{(\mathrm{UN}^2\mathrm{LOPS})} &= \int \!\! d\Phi_0 \, \bar{\bar{B}}_0^{q_{T,\mathrm{cut}}}(\Phi_0) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \, \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \Big] \, B_1(\Phi_1) \, \mathcal{O}(\Phi_0) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Pi_0(t_1,\mu_Q^2) \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \, B_1(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, \bar{B}_1^R(\Phi_1) \, \mathcal{O}(\Phi_0) + \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \Pi_0(t_1,\mu_Q^2) \, \bar{B}_1^R(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_2 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, H_1^R(\Phi_2) \, \mathcal{O}(\Phi_0) + \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_2 \, \Pi_0(t_1,\mu_Q^2) \, H_1^R(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \\ &+ \int_{\mathcal{O}} \!\! d\Phi_2 \, H_1^E(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \end{split}$$

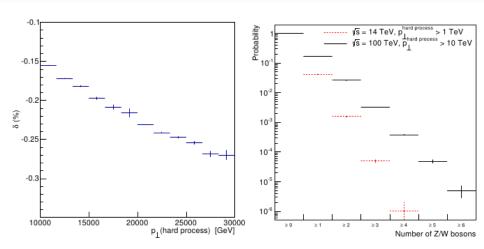
$$\tilde{B}_0^{q_{T,\text{cut}}} + \tilde{B}_1^R + H_1^R + H_1^E = B_{\text{NNLO}}$$

Other terms drop out in inclusive observables.

$$\begin{split} \mathcal{O}^{(\mathrm{UN^2LOPS})} &= \int \!\! d\Phi_0 \, \bar{\bar{B}}_0^{q_{T,\mathrm{cut}}}(\Phi_0) \, \mathit{O}(\Phi_0) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \, \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \Big] \, B_1(\Phi_1) \, \mathit{O}(\Phi_0) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Pi_0(t_1,\mu_Q^2) \Big(w_1(\Phi_1) + w_1^{(1)}(\Phi_1) + \Pi_0^{(1)}(t_1,\mu_Q^2) \Big) \, B_1(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, \tilde{B}_1^R(\Phi_1) \, \mathit{O}(\Phi_0) + \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_1 \, \Pi_0(t_1,\mu_Q^2) \, \tilde{B}_1^R(\Phi_1) \, \bar{\mathcal{F}}_1(t_1,\mathcal{O}) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_2 \, \Big[1 - \Pi_0(t_1,\mu_Q^2) \Big] \, H_1^R(\Phi_2) \, \mathit{O}(\Phi_0) + \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_2 \, \Pi_0(t_1,\mu_Q^2) \, H_1^R(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \\ &+ \int_{q_{T,\mathrm{cut}}} \!\! d\Phi_2 \, H_1^E(\Phi_2) \, \mathcal{F}_2(t_2,\mathcal{O}) \end{split}$$

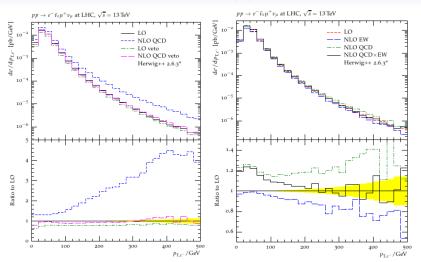
Orange terms do not contain any universal α_s corrections present in the PS. H_1 do not contribute in the soft/collinear limit. \Longrightarrow PS accuracy is preserved.

Weak reals in PYTHIA 8 arXiv:1401.6364



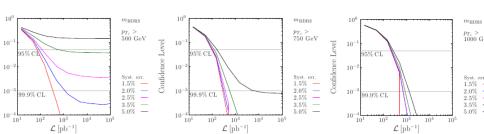
- Splitting kernels $\frac{|\mathcal{M}_{2\to3}|d\Phi_{rad}}{|\mathcal{M}_{2\to3}|}$. Ordering variable $p_{\perp}^2+kM_B^2$.
- Small effect at LHC, larger at FCC.
- Effect mostly from the first (few) weak bosons.

Weak virtuals in HERWIG++ arXiv:1401.3964



- Multiply (full!) electro-weak virtual corrections as phase-space dependent K-factor $K(\hat{s}, \hat{t})$. No real emissions included.
- Effect on ("QCD-cleaned") vetoed observables large.

Weak reals in SHERPA arXiv:1403.4788



- Splitting kernels: Massive CS dipoles (CDST). Ordered in p_{\perp} .
- Boosted techniques at LHC can discriminate between pure QCD and jets containing hadronically decaying W's.