

Dark Gauge $U(1)$ Symmetry for an Alternative Left-Right Model

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The 26th International Workshop on Weak Interactions and
Neutrinos (WIN2017) June 23, 2017

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- Restore symmetry between Left-Right sectors
- Generate naturally small neutrino masses
- Accomodate dark matter

Minimal Left-Right Model

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- Simple extension of the SM gauge group
- Spontaneous/Explicit breaking of P ($SU(2)_L \longleftrightarrow SU(2)_R$) (also CP)
- Generation of naturally light neutrino masses (Seesaw I/III)

$$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

$$Q_L = \begin{pmatrix} u_L \\ d_L \end{pmatrix} \equiv [3, 2, 1, \frac{1}{3}] \quad Q_R = \begin{pmatrix} u_R \\ d_R \end{pmatrix} \equiv [3, 1, 2, \frac{1}{3}]$$

$$\ell_L = \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \equiv [1, 2, 1, -1] \quad \ell_R = \begin{pmatrix} \nu_R \\ e_R \end{pmatrix} \equiv [1, 1, 2, -1]. *$$

- $\eta \sim (1, 2, 2, 0)$, $\Delta_L \sim (1, 3, 1, -1)$, $\Delta_R \sim (1, 1, 3, -1)$
- Seesaw I/II
- $\eta \sim (1, 2, 2, 0)$, $\phi_L \sim (1, 2, 1, 1/2)$, $\phi_R \sim (1, 1, 2, 1/2)$
- Double seesaw through Weinberg dim-5 operator
- Flavour changing neutral currents

*N.G. Deshpande et al., Phys. Rev. D 44, 837 (1991).

Alternative Left-Right Model

$$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)_{B-L}$$

$$(u, d)_L : (3, 2, 1, \frac{1}{6}) \quad (h^c, u^c)_L : (\bar{3}, 1, 2, -\frac{1}{6})$$

$$(\nu_E, E)_L : (1, 2, 1, -\frac{1}{2}) \quad (e^c, n)_L : (1, 1, 2, \frac{1}{2})$$

$$h_L : (3, 1, 1, -\frac{1}{3}) \quad d_L^c : (\bar{3}, 1, 1, \frac{1}{3})$$

$$\begin{pmatrix} \nu_e & E^c \\ e & N_E^c \end{pmatrix}_L : (1, 2, 2, 0) \quad N_L^c : (1, 1, 1, 0), \quad \dagger$$

- ALRM is motivated by superstring-inspired E_6 model
- Flavour changing neutral currents are naturally absent tree level
- W_R^\pm has lepton number ± 1 and odd parity so they do not mix with W_L^\pm
- $SU(2)_R$ breaking scale can be below as TeV, W_R^\pm and Z' are reachable at LHC

† E. Ma, Phys. Rev. D 36, 274 (1987); K. S. Babu, X.-G. He, and E. Ma, Phys. Rev. D 36, 878 (1987); J. L. Hewett and T. G. Rizzo, [hep-ph/9302009](#)

Dark Alternative Left-Right Models with Global Symmetries

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Fermion	$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)$	S	Scalar	$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)$	S
$\psi_L = (\nu, e)_L$	(1, 2, 1, -1/2)	1	Φ	(1, 2, 2, 0)	1/2
$\psi_R = (n, e)_R$	(1, 1, 2, -1/2)	1/2	$\tilde{\Phi} = \sigma_2 \Phi^* \sigma_2$	(1, 2, 2, 0)	-1/2
$Q_L = (u, d)_L$	(3, 2, 1, 1/6)	0	Φ_L	(1, 2, 1, 1/2)	0
$Q_R = (u, h)_R$	(3, 1, 2, 1/6)	1/2	Φ_R	(1, 1, 2, 1/2)	-1/2
d_R	(3, 1, 1, -1/3)	0	Δ_L	(1, 3, 1, 1)	-2
h_L	(3, 1, 1, -1/3)	1	Δ_R	(1, 1, 3, 1)	-1 ‡

- No tree level FCNC
- Neutrino masses ($m_\nu \sim \langle \Delta_L^0 \rangle \implies L \rightarrow (-1)^L$, R parity)
- Fermionic Dark Matter (Scotinos) ($m_n \sim \langle \Delta_R^0 \rangle$)
- Lepton number given by $L=S-T_{3R}$
- $\langle \phi_1^0 \rangle = 0$ by $S-T_{3R}$
- h, W_R^\pm has $L=1, \mp 1$
- SM particles are even, n, h, W_R^\pm , and Δ_R^\pm are odd under parity

‡S. Khalil, H.-S. Lee, E. Ma, Phys. Rev. D 79, 041701(R) (2009)

Dark Alternative Left-Right Models II

with Global Symmetries

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Fermion	$SU(3)_C \times SU(2)_L \times SU(2)_R \times U(1)$	S			
$\psi_L = (\nu, e)_L$	(1, 2, 1, -1/2)	1			
$\psi_R = (n, e)_R$	(1, 1, 2, -1/2)	3/2			
ν_R	(1, 1, 1, 0)	1			
n_L	(1, 1, 1, 0)	2			
$Q_L = (u, d)_L$	(3, 2, 1, 1/6)	0	Φ	(1, 2, 2, 0)	-1/2
$Q_R = (u, h)_R$	(3, 1, 2, 1/6)	-1/2	$\tilde{\Phi} = \sigma_2 \Phi^* \sigma_2$	(1, 2, 2, 0)	1/2
d_R	(3, 1, 1, -1/3)	0	Φ_L	(1, 2, 1, 1/2)	0
h_L	(3, 1, 1, -1/3)	-1	Φ_R	(1, 1, 2, 1/2)	1/2 §

- No tree level FCNC
- Dirac neutrino masses ($m_\nu \sim \langle \phi_L^0 \rangle$)
- Dirac Fermionic Dark Matter (Scotinos) ($m_n \sim \langle \phi_R^0 \rangle$)
- Lepton number given by $L=S+T_{3R}$ and is conserved
- $\langle \phi_1^0 \rangle = 0$ by $S+T_{3R}$
- $\nu_R \nu_R$ breaks L and generates Majorana neutrino mass through canonical seesaw
- n remains Dirac fermion protected by residual global $U(1)$ ($n, W_R^+ \sim 1, h, \phi_1^{0,-} \sim -1$)

§ S. Khalil, H.-S. Lee, E. Ma, Phys. Rev. D 81, 051702(R) (2010)

Particle Content of the $U(1)_D$ ALRM

particles	$SU(3)_C$	$SU(2)_L$	$SU(2)_R$	$U(1)_X$	$U(1)_S$
$(u, d)_L$	3	2	1	1/6	0
$(u, h)_R$	3	1	2	1/6	-1/2
d_R	3	1	1	-1/3	0
h_L	3	1	1	-1/3	-1
$(\nu, l)_L$	1	2	1	-1/2	0
$(n, l)_R$	1	1	2	-1/2	1/2
ν_R	1	1	1	0	0
n_L	1	1	1	0	1
(ϕ_L^+, ϕ_L^0)	1	2	1	1/2	0
(ϕ_R^+, ϕ_R^0)	1	1	2	1/2	1/2
η	1	2	2	0	-1/2
ζ	1	1	1	0	1
$(\psi_1^0, \psi_1^-)_R$	1	1	2	-1/2	2
$(\psi_2^+, \psi_2^0)_R$	1	1	2	1/2	1
χ_R^+	1	1	1	1	-3/2
χ_R^-	1	1	1	-1	-3/2
χ_{1R}^0	1	1	1	0	-1/2
χ_{2R}^0	1	1	1	0	-5/2
σ	1	1	1	0	3

Symmetry breaking, Mass Generation, and Flavour Changing Neutral Currents

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- $\langle \phi_R^0 \rangle = 0$, $\langle \eta_2^0 \rangle = 0$ and conserve $S+T_{3R}$
- All exotic fermions have half integer charges under $S+T_{3R}$
- Particle content and charge assignments result in additional unbroken Z_2 symmetry, under which exotic fermions are odd and others are even
- $S+T_{3R}$ is broken to S' by $\langle \sigma \rangle \neq 0$ and gives masses to exotic fermions
- S' charges for exotic fermions are different from $S+T_{3R}$ charges
- Presence of ζ induces $\zeta^3 \sigma^*$ and $\chi_{1R}^0 \chi_{1R}^0 \zeta$ breaks S' further to Z_3

Particle content of proposed model under $(T_{3R} + S) \times Z_2$

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particles	gauge $T_{3R} + S$	global S'	Z_3	Z_2
u, d, ν, l	0	0	1	+
$(\phi_L^+, \phi_L^0), (\eta_2^+, \eta_2^0), \phi_R^0$	0	0	1	+
n, ϕ_R^+, ζ	1	1	ω	+
$h, (\eta_1^0, \eta_1^-)$	-1	-1	ω^2	+
ψ_{2R}^+, χ_R^+	$3/2, -3/2$	0	1	-
ψ_{1R}^-, χ_R^-	$3/2, -3/2$	0	1	-
ψ_{1R}^0, ψ_{2R}^0	$5/2, 1/2$	1, -1	ω, ω^2	-
χ_{1R}^0, χ_{2R}^0	$-1/2, -5/2$	1, -1	ω, ω^2	-
σ	3	0	1	+

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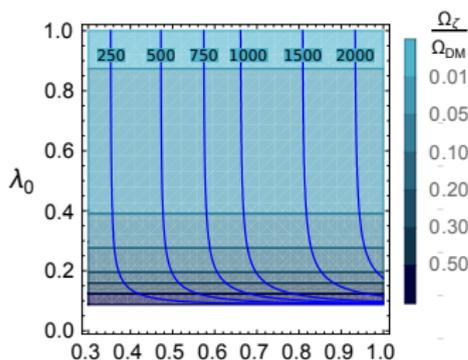
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- $M(Z') > 4\text{TeV}$
- DM candidates: Fermionic DM (χ_0) ($\chi_0\bar{\chi}_0 \Rightarrow \zeta\zeta^*$),
Scalar DM (ζ) ($\zeta\zeta^* \Rightarrow HH$)
- $\langle \sigma \times v_{rel} \rangle_{\chi} = \frac{f_0^4}{4\pi m_{\chi_0}} \frac{(m_{\chi_0}^2 - m_{\zeta}^2)^{3/2}}{(2m_{\chi_0}^2 - m_{\zeta}^2)^2} (f_0 \zeta \chi_{0R} \chi_{0R})$
- $\langle \sigma \times v_{rel} \rangle_{\zeta} = \frac{\lambda_0^2}{16\pi} \frac{(m_{\zeta}^2 - m_H^2)^{1/2}}{m_{\zeta}^3} (\lambda_0 \zeta \zeta^* HH)$
- $\nu_R > 35\text{TeV} \Rightarrow M_{Z'} > 18\text{TeV}, M_{W_R} > 16\text{TeV}$



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- (Alternative, Dark)Left-Right Models have no tree level FCNC
- Generate naturally small neutrino masses (Seesaw I/II/III/Double)
- Rich phenomenology accessible at LHC
- Different variations are possible
- Natural Dark Matter candidates due to residual symmetry
- 2 layers of DM stabilized by Z_3 and Z_2 in case of Gauged DLRM

Particle Content of the Model

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Particle	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	L	copies	Z_2
$Q_i = (u, d)_i$	3	2	1/6	0	3	+
u^c	3^*	1	-2/3	0	3	+
d^c	3^*	1	1/3	0	3	+
$L_i = (\nu, e)_i$	1	2	-1/2	1	3	+
e^c	1	1	1	-1	3	+
$(E^0, E^-)_{L,R}$	1	2	-1/2	1	1	-
$N_{L,R}$	1	1	0	1	1	-
$\Phi = (\phi^+, \phi^0)$	1	2	1/2	0	1	+
s_i^0	1	1	0	0	3	-

New \mathcal{L} agrangian

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$$\mathcal{L}_{new} \supset \begin{aligned} & \overline{N}_L (E_R^0 \phi^0 - E_R^- \phi^+) \\ & \left(\overline{E}_R^0 E_L^0 + E_R^+ E_L^- \right) \\ & \left(\overline{\nu}_{Li} E_R^0 + \overline{e}_{Li}^- E_R^- \right) s_j \\ & N_L N_L \\ & m_i^2 s_i^2 \end{aligned}$$

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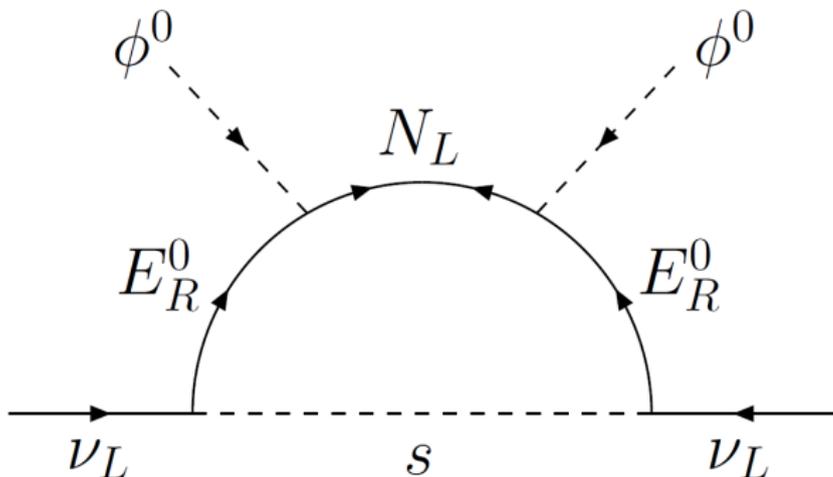
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$$\mathcal{M}_{E,N} = \begin{pmatrix} 0 & m_E & m_D \\ m_E & 0 & 0 \\ m_D & 0 & m_N \end{pmatrix}$$

$$m_1 = \frac{m_E^2 m_N}{m_E^2 + m_D^2}$$

$$m_{2,3} = \pm \sqrt{m_E^2 + m_D^2} + \frac{m_D^2 m_N}{2(m_E^2 + m_D^2)}$$

$$m_N \ll m_E, m_D$$

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$$m_\nu = f^2 \frac{m_D^2 m_N}{m_E^2 + m_D^2} F(x)$$
$$F(x) = \frac{1}{1-x} \left(1 + \frac{x \ln x}{1-x} \right)$$
$$x = \frac{m_s^2}{(m_E^2 + m_D^2)}$$

$f_{e,\mu,\tau}$	0.1
x	≈ 0
m_N	10 MeV
m_D	10 GeV
m_E	1 TeV
m_ν	0.1 eV

Z₃ symmetry and Neutrino Mixing

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$$(\nu_i, l_i) \sim \underline{1}, \underline{1}', \underline{1}'', \quad s_1 \sim \underline{1}, \quad (s_2 \pm is_3)/\sqrt{2} \sim \underline{1}', \underline{1}'', \quad l_{iR} \sim \underline{1}, \underline{1}', \underline{1}''$$

$$m_s^2 s^2 + m_s'^2 (s_2^2 + s_3^2)$$

$$\mathcal{M}_\nu = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1/\sqrt{2} & i/\sqrt{2} \\ 0 & 1/\sqrt{2} & -i/\sqrt{2} \end{pmatrix} O^T \begin{pmatrix} I(m_{s_1}^2) & 0 & 0 \\ 0 & I(m_{s_2}^2) & 0 \\ 0 & 0 & I(m_{s_3}^2) \end{pmatrix} O \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1/\sqrt{2} & 1/\sqrt{2} \\ 0 & i/\sqrt{2} & -i/\sqrt{2} \end{pmatrix}$$

$$\mathcal{M}_\nu|_{f_\mu=f_\tau} = \begin{pmatrix} A & C & C^* \\ C & D^* & B \\ C^* & B & D \end{pmatrix}$$

$$\text{Cobimaximal Mixing:} \quad \theta_{23} = \pi/4, \quad \exp(-i\delta) = \pm i, \quad \theta_{13} \neq 0$$

$f_\mu \neq f_\tau$ case

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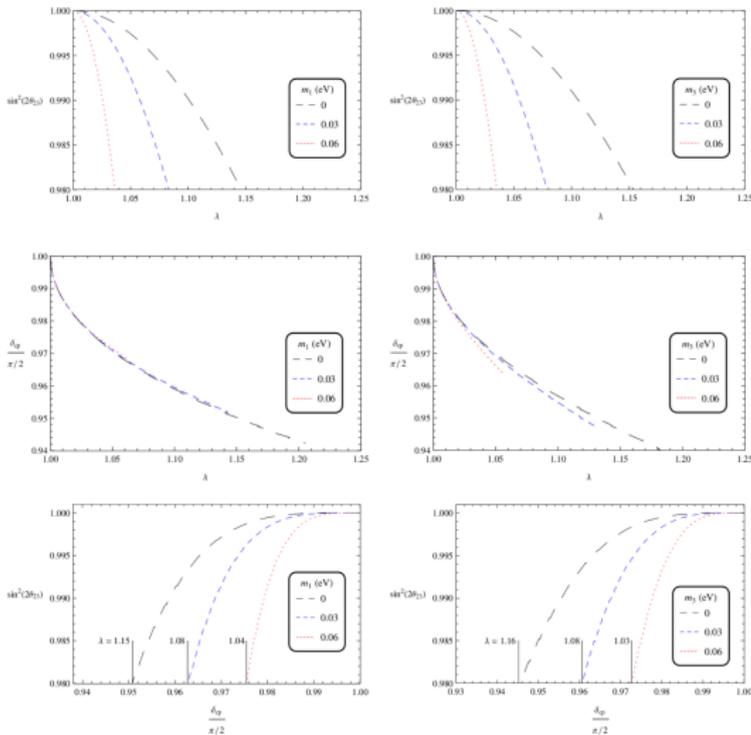
$$M_\nu = E_\alpha U E_\beta M_d E_\beta U^T E_\alpha$$
$$M_\nu M_\nu^\dagger = E_\alpha U M_d^2 U^\dagger E_\alpha^\dagger$$
$$M_\nu^\lambda M_\nu^{\lambda\dagger} = E_\alpha U \underbrace{[1 + \Delta] M_{\lambda d}^2 [1 + \Delta^\dagger]}_{OM_{new}^2 O^T} U^\dagger E_\alpha^\dagger$$

$$\Delta = U^\dagger \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & \lambda - 1 \end{pmatrix} U, \quad M_{\lambda d}^2 = \begin{pmatrix} m_1^2 & 0 & 0 \\ 0 & m_2^2 & 0 \\ 0 & 0 & \lambda^2 m_3^2 \end{pmatrix}$$

$$\lambda = \frac{f_\mu}{f_\tau}$$

$f_\mu \neq f_\tau$ case

⇒ Normal ordering (left) and Inverted ordering (right).



Muon Anomalous Magnetic Moment

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$$\Delta a_\mu = \frac{(g-2)_\mu}{2} = \frac{f_\mu^2 m_\mu^2}{16\pi^2 m_E^2} \sum_i |U_{\mu i}|^2 G(x_i)^\S$$

$$G(x) = \frac{1 - 6x + 3x^2 + 2x^3 - 6x^2 \ln x}{6(1-x)^4}, \quad x_i = m_{S_i}^2 / m_E^2$$

$$U = O \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1/\sqrt{2} & 1/\sqrt{2} \\ 0 & i/\sqrt{2} & -i/\sqrt{2} \end{pmatrix}$$

$$\left. \begin{array}{l} x_i \ll 1 \\ m_E \sim 1 \text{ TeV} \end{array} \right\} \Delta a = \frac{f_\mu^2 m_\mu^2}{96\pi^2 m_E^2} \approx 10^{-11} f_\mu^2$$

[§]S. Kanemitsu and K. Tobe, Phys. Rev. D86, 095025 (2012).

$$\mu \rightarrow e\gamma$$

Gauge $U(1)_D$
Symmetry for
ALRM

Oleg Popov

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$$A_{\mu e} = \frac{ef_\mu f_e m_\mu}{32\pi^2 m_E^2} \sum_i U_{ei}^* U_{\mu i} G(x_i)$$
$$Br(\mu \rightarrow e\gamma) = \frac{12\pi^2 |A_{\mu e}|^2}{m_\mu^2 G_F^2} < 5.7 \times 10^{-13} \ddagger$$
$$f_\mu f_e < 0.03$$

\ddagger MEG Collaboration, J. Adams et al., Phys. Rev. Lett. 110, 201801 (2013).

Dark Matter

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Dark Matter Candidates: N_L, S

$$-\mathcal{L}_{int} = \frac{\lambda_{hS}}{2} \nu h S^2 + \frac{\lambda_{hS}}{4} h^2 S^2$$

$$m_S \lesssim m_h/2 \text{ or } m_S > 150 \text{ GeV}$$

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- Inverse Seesaw Neutrino Mass
- Z_3 Flavor Symmetry \implies Cobimaximal Mixing
- Deviation from Cobimaximal Mixing
- $g-2$ and $\mu \rightarrow e\gamma$