

# keV sterile neutrinos and new tests for non-thermal DM candidates

WIN 2017

based on work with many collaborators:

(1704.07838, ApJ 836 (2017)61, JCAP 1611(038), JCAP  
1604(003), JCAP 1506(011))

Maximilian Totzauer

June 20, 2017

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- 6 New Approaches to assess Structure Formation
- 7 Conclusion and Outlook

# Brief introduction into Sterile Neutrinos

# What is a sterile neutrino?

	I	II	III	
mass →	2.4 MeV	1.27 GeV	171.2 GeV	
charge →	$\frac{2}{3}$	$\frac{2}{3}$	$\frac{2}{3}$	0
name →	u up	c charm	t top	g gluon
	Left Right	Left Right	Left Right	0
				$\gamma$ photon
Quarks	4.8 MeV $-\frac{1}{3}$ d down	104 MeV $-\frac{1}{3}$ s strange	4.2 GeV $-\frac{1}{3}$ b bottom	0
	Left Right	Left Right	Left Right	$Z^0$ weak force
	0 eV 0 $\nu_e$ electron neutrino	0 eV 0 $\nu_\mu$ muon neutrino	0 eV 0 $\nu_\tau$ tau neutrino	$H$ Higgs boson
	Left Right	Left Right	Left Right	spin 0
Leptons	0.511 MeV -1 e electron	105.7 MeV -1 $\mu$ muon	1.777 GeV -1 $\tau$ tau	80.4 GeV $\pm 1$ $W^\pm$ weak force
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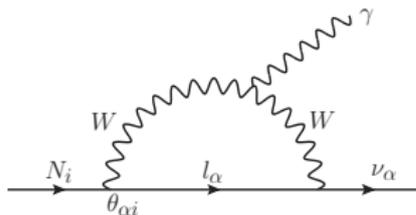
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- Can be (a part of) the **cosmic DM**.
- If so: would have a rather clear signal for  $\sin^2(2\theta) \neq 0$ :



Decay  $N \rightarrow \nu \gamma$  gives photons with  $E_\gamma = m_N/2$ .

Claim for a signal @  $E_\gamma = 3.55$  keV in 2014, highly disputed & still unresolved issue.

# Production Templates for Dark Matter

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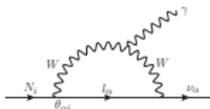
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- **Decay of parent particles:** Highly non-thermal process, parent  $P$  itself can freeze in or out or be a decay product itself.  
 $\Omega_{\text{DM}} = \Omega_{\text{DM}}(\sigma_{P \leftrightarrow \text{SM}}, \Gamma_P)$

# Production Mechanisms for Sterile Neutrino Dark Matter

# How to fill the templates with physical models for SN?

The popular production mechanisms are:

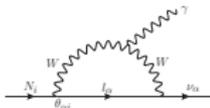
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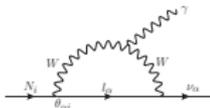
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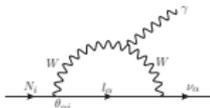


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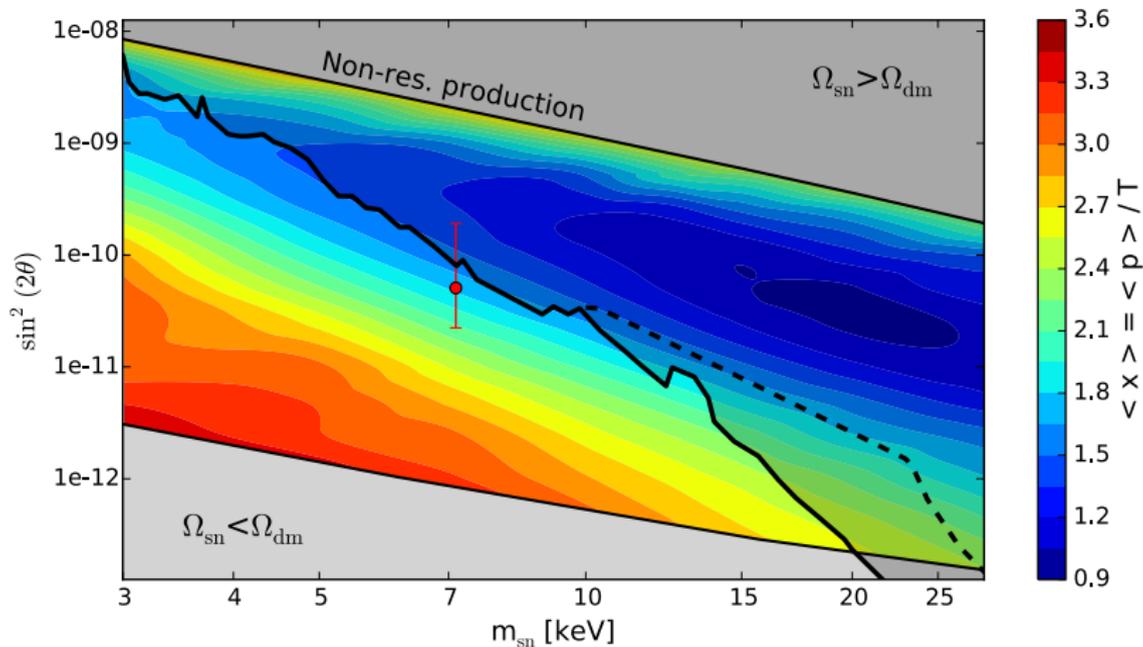
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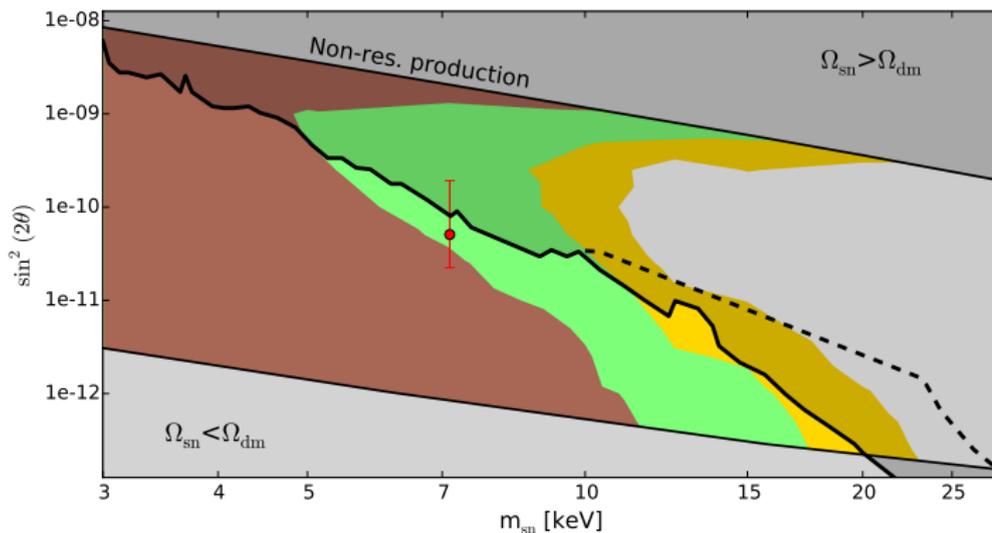
## DW / SF and structure formation

“Temperature map” of SF (taken from 1601.07553 by A. Schneider)

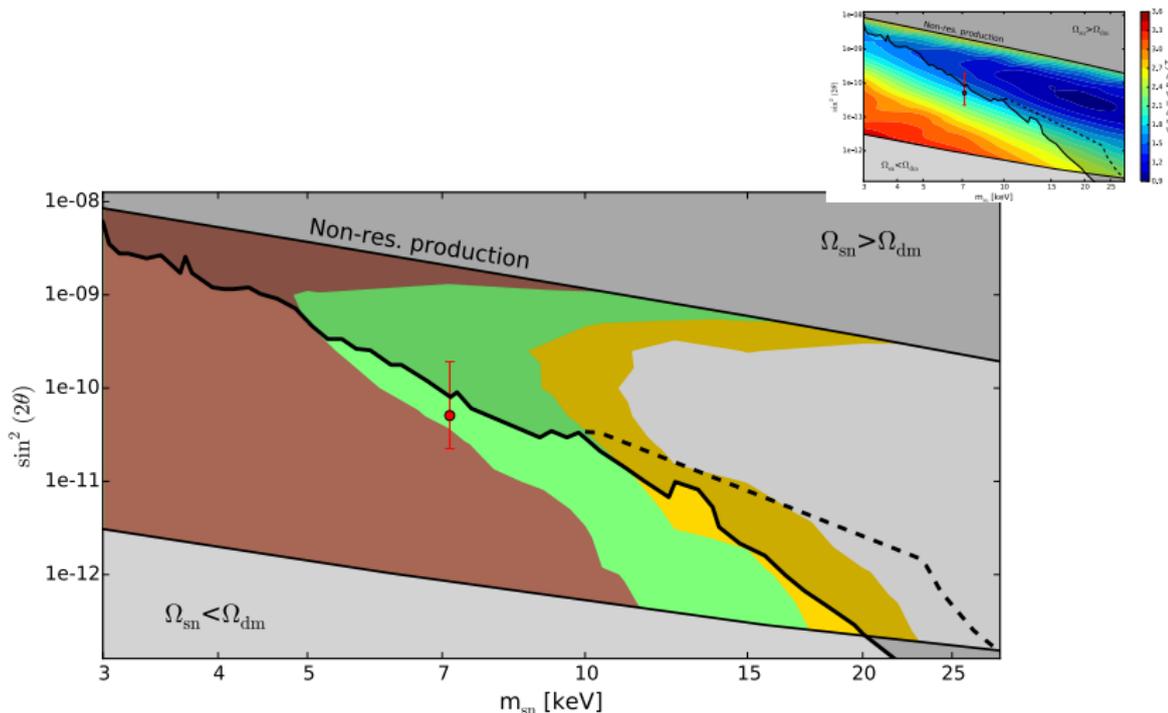


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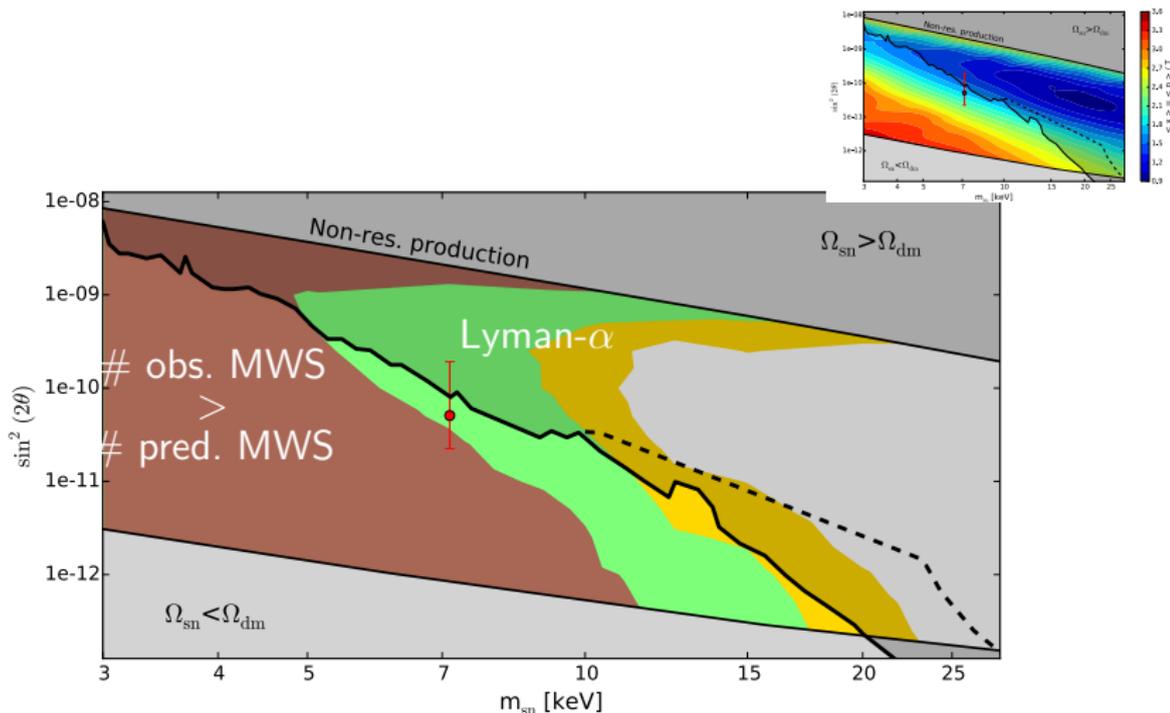
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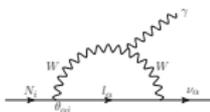
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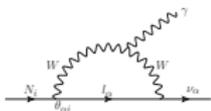


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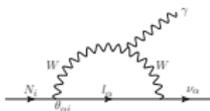


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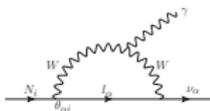


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- ~~DW/SF + late thermalisation in dark sector~~  $\rightarrow$  Talk by R. S. L. Hansen.
- ~~Decay production~~ via some parent particle, e.g. real scalar singlet  $S$  coupled to Higgs sector.

# The Scalar Decay Model for keV Steriles

## A simple model for scalar decay – Lagrangian

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where

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- Mixing  **$\sin^2 \theta$  switched off** in this model (good approx., cf. 1512.05369 (Merle, Schneider, MT))  $\Rightarrow$  Can however be **arbitrarily small, not needed to produce  $\nu_S$** .

## A simple model for scalar decay – production channels

Production of scalar  $S$  from SM d.o.f. depending on whether  
 $T > T_{\text{EW}}$  (I) //  $T < T_{\text{EW}}$  &  $m_S > m_h/2$  (II) //  $T < T_{\text{EW}}$  &  $m_S < m_h/2$  (III).

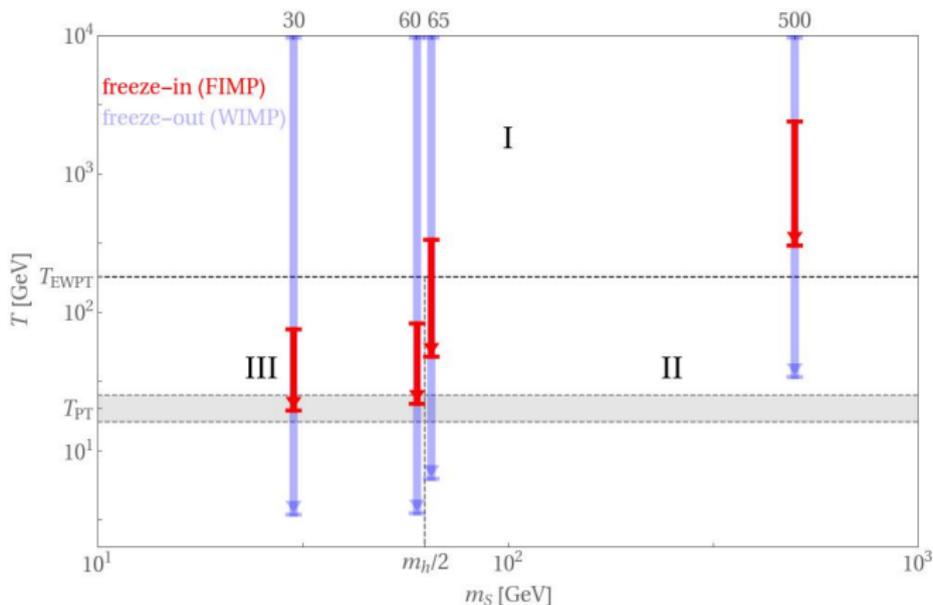
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regime	production channels
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II	
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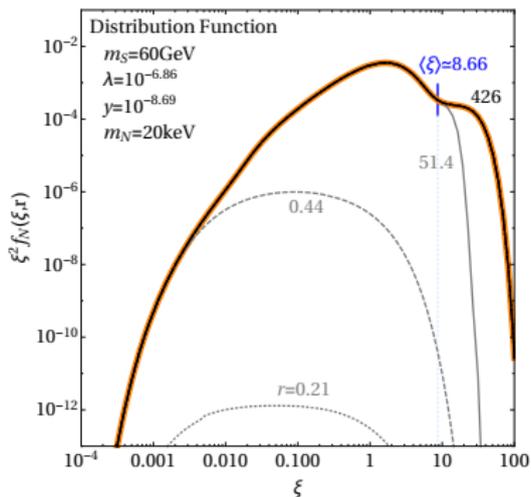
# A simple model for scalar decay – different $m_S$

Depending on  $\lambda$  and  $m_S$ , different production regimes are relevant:



# A simple model for scalar decay – non-thermal spectra

The interplay between decay of  $S$  in-eq. and out-of-eq. can yield highly non-thermal spectra:



# A Primer in Cosmic Structure Formation.

# The Cosmic Web: Far from homogeneous on small scales

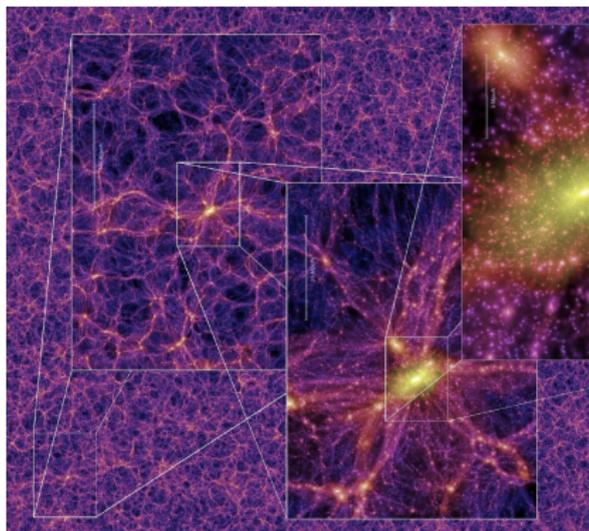


Figure: credit: MilleniumSimulation, Cold Dark Matter Simulation

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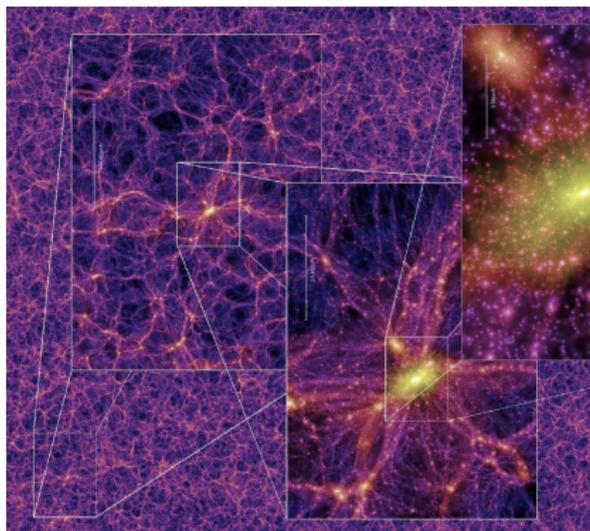


Figure: credit: MilleniumSimulation, Cold Dark Matter Simulation

Simulation matches observations very well, except for smallest scales (**Missing Satellites, Too-Big-Too-Fail, Cusp-Core-Problem**).

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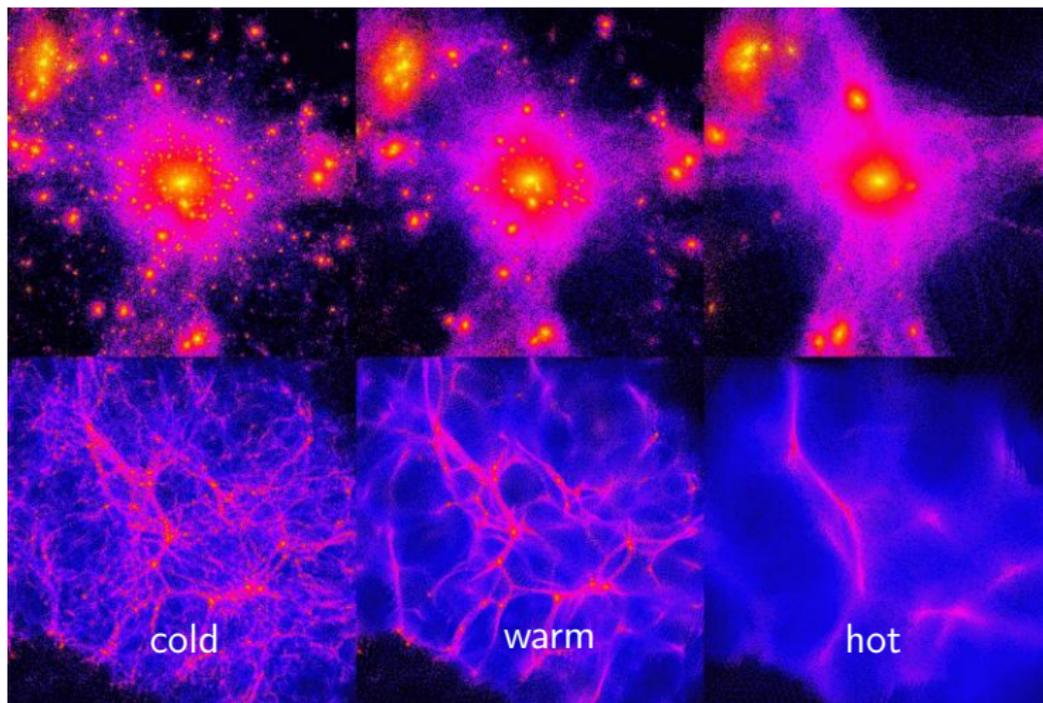
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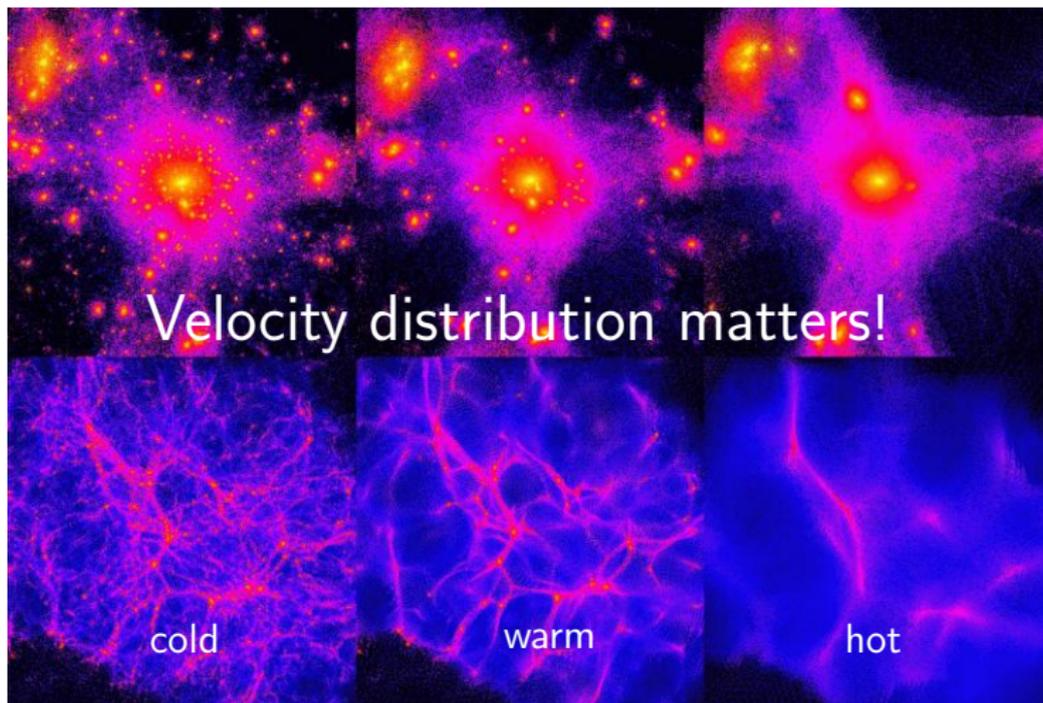
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- First, perturbations grow linearly (solve equations semi-analytically), then non-linearly (need for  $N$ -body simulations).

# Simulating the Cosmic Web



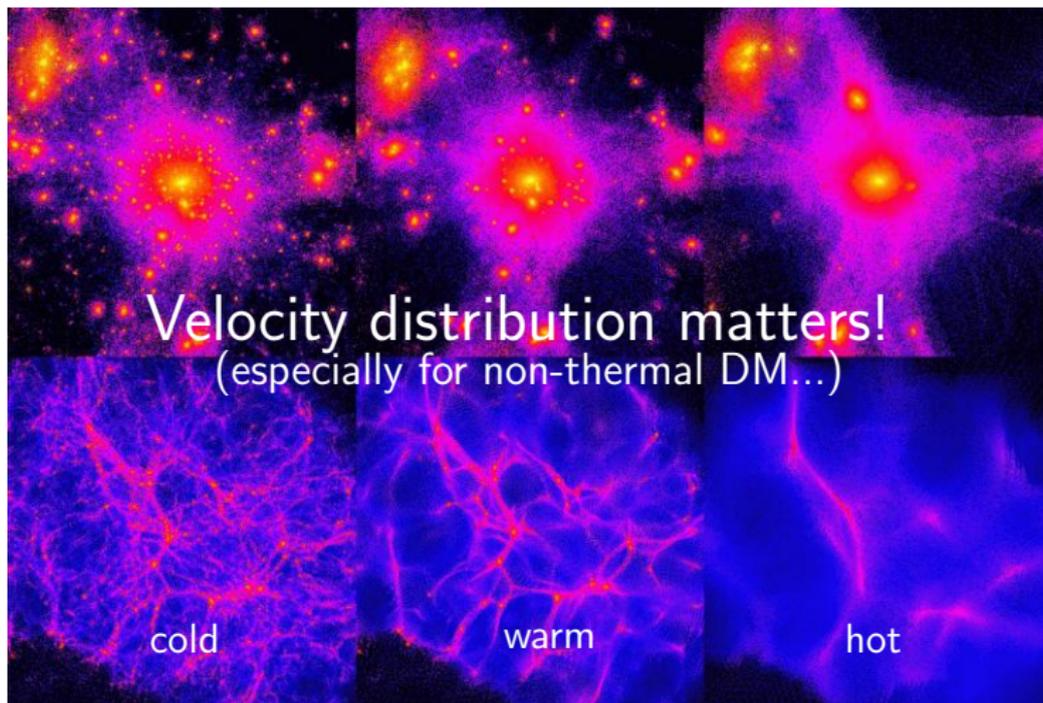
credit: ITC @ University of Zurich

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# Measuring the cosmic web: DM power spectrum $P(k)$

Different scales  $\rightarrow$  different techniques:

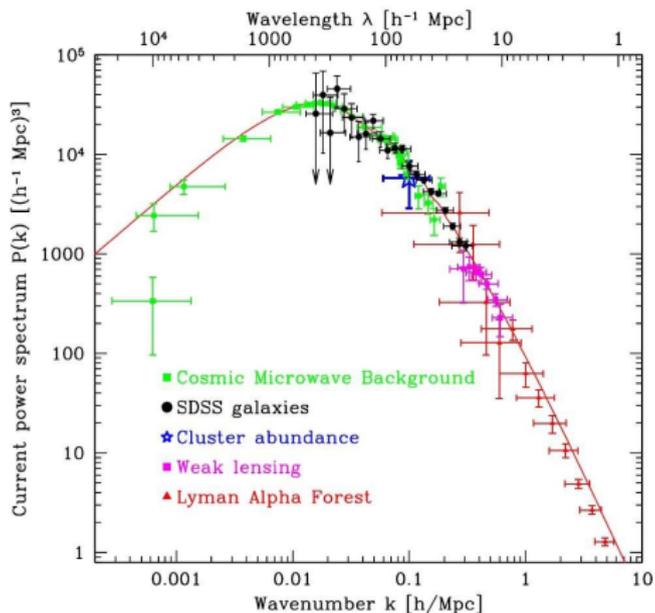


Figure: Small scales probed by Lyman- $\alpha$  forest. (taken from 1005.1100)

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>>> **Visual explanation** <<<
- $\Rightarrow$  many line-of-sight profiles allow for a 3D reconstruction of densities.

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Problem: **Average** might not be a good description, especially for non-thermal dark matter (more to come...)

## Leaving the comfort zone

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- Compute power spectrum  $P(k)$  and compare to observations.

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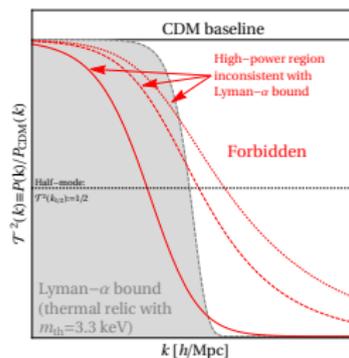
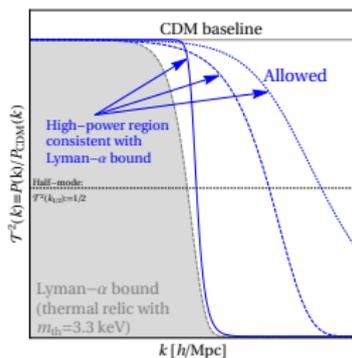
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- Problem: Most bounds obtained for **thermal** dark matter. Complete simulation of small-scale structure and statistical analysis non-trivial.
- Advantage: Thermal benchmark has only one parameter,  $\mathcal{T}_{\text{therm}}^2(k) = \mathcal{T}^2(k, m_{\text{therm}})$ .

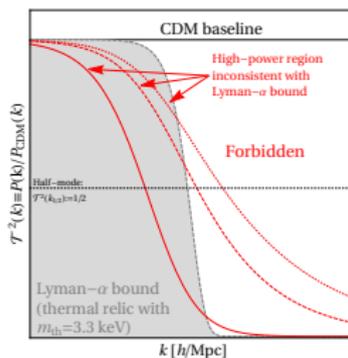
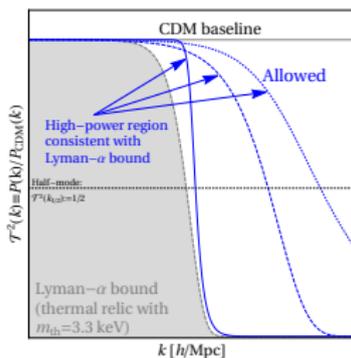
# Comparing a DM model to observations

A simple but reliable method: the half-mode analysis  
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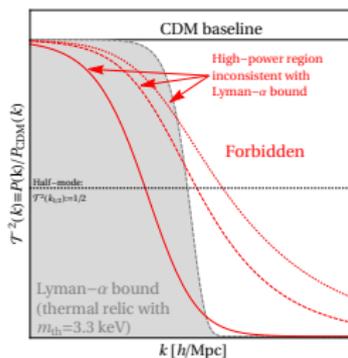
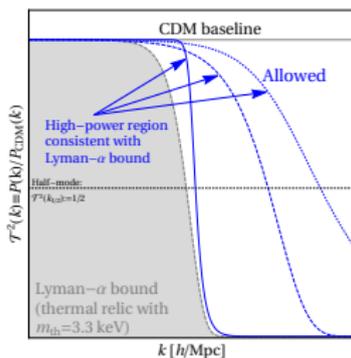
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- Only approximate, as we want to test **non-thermal** dark matter.

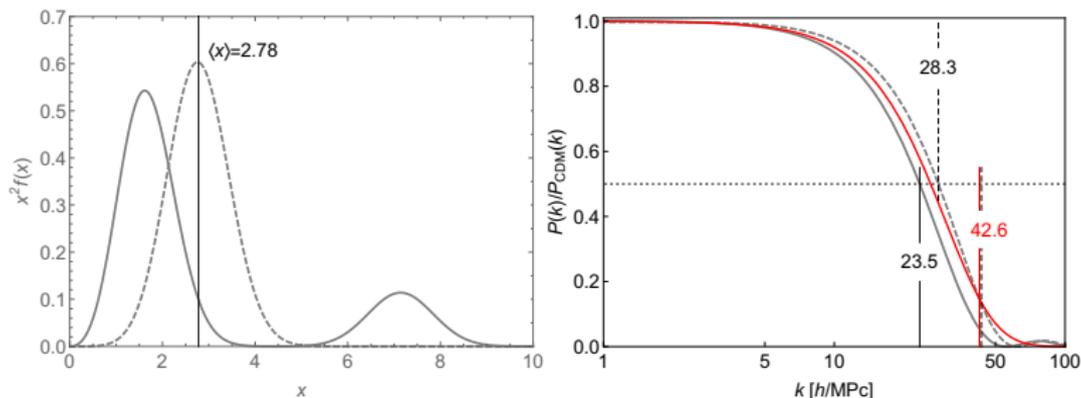
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**Figure:** Mock spectra with identical  $\langle x \rangle$  (by construction) but different squared transfer function  $\mathcal{T}^2$ .

## More advanced methods

The simple half-mode analysis has been tested in 1704.07838 and in ApJ 836(61) using

- integrated deviation of linear power spectrum from benchmark derived from Lyman- $\alpha$  data,
- the number of MW subhaloes in comparison to the number of observed satellites,
- the count of ultra-faint galaxies at redshift  $z = 6$ .

⇒ Very close agreement to half-mode analysis found!

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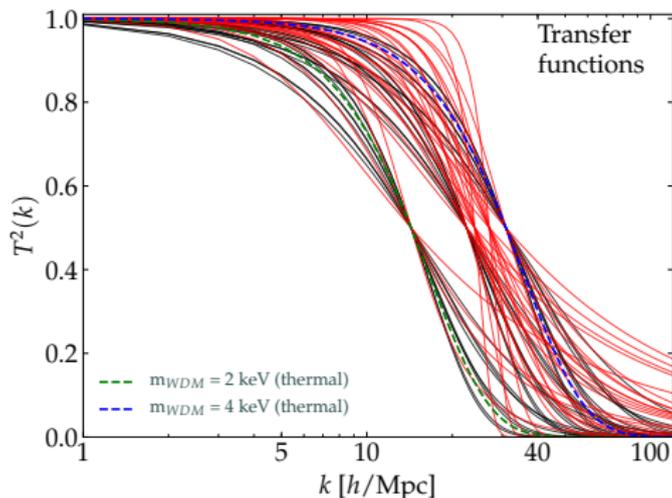
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- (Almost) any model's  $\mathcal{T}$  can be fitted to the above template, the estimators can be interpolated and compared to observations.
- Or: compute  $\delta A$  and  $N_{\text{sat}}$  analytically in linear theory (well backed by  $N$ -body simulations).

# A model independent approach (1704.07838)

The grid of reference power spectra:



Estimators  $\delta A$  and  $N_{\text{sat}}$  derived and compared to benchmark in 1704.07838.

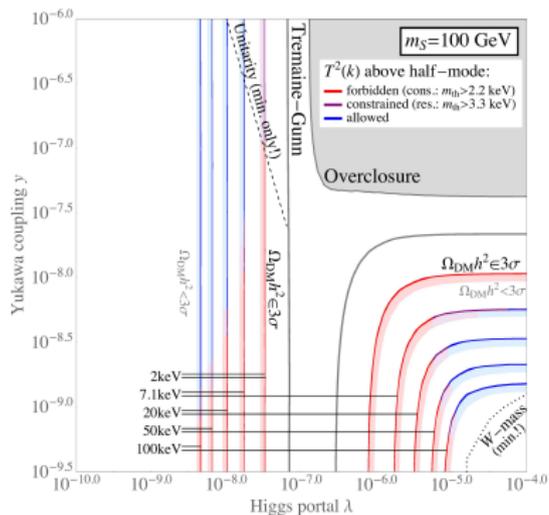
## A synopsis of methods: the SD model revisited

### Structure formation of the SD model

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Structure formation of the SD model  
Constraining the parameter space of the  
scalar decay model ( $\lambda, y, m_S, m_N$ ).

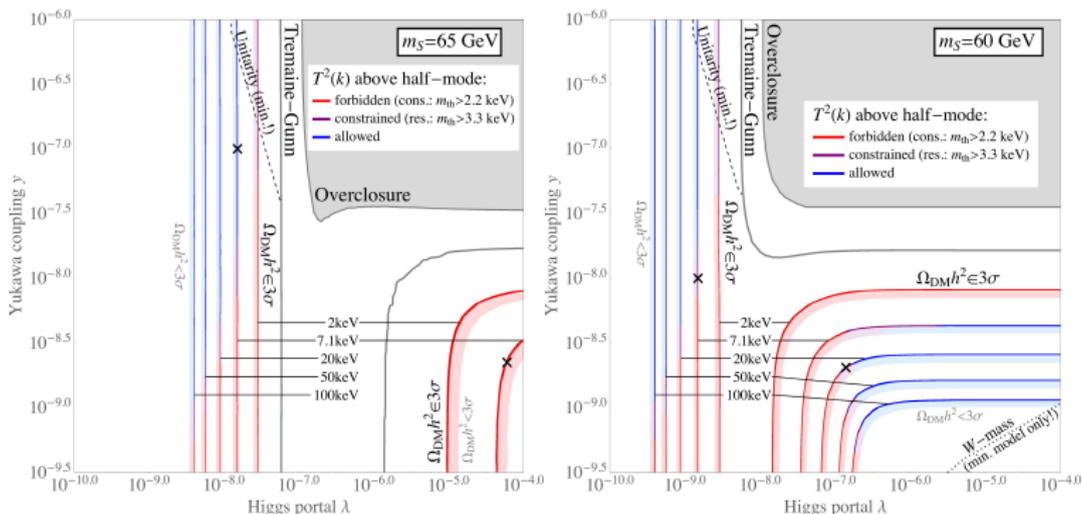
## SD model and the half-mode analysis



**Figure:** Constraints from structure formation in the plane  $\lambda$ -vs.- $y$  for  $m_S = 100 \text{ GeV}$ . Taken from JCAP 1611(038) (König, Merle, MT).

# SD model and the half-mode analysis

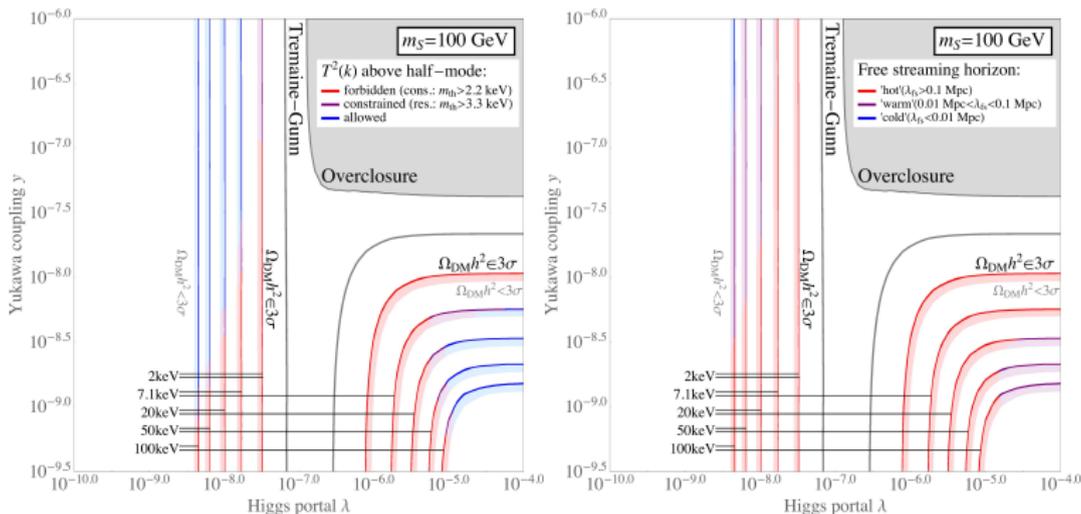
For other masses  $m_S$ , the picture looks similar but not identical:



**Figure:** For  $m_S = 65$  GeV, the 'freeze-out region' is completely forbidden!

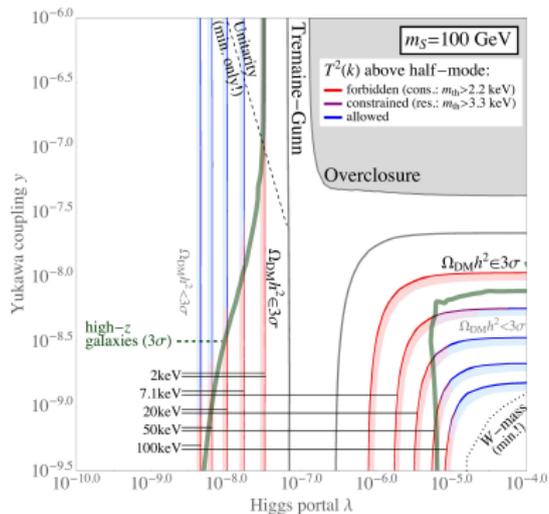
# Half-mode analysis vs. free-streaming

Comparison of the free-streaming approach and the half-mode analysis:



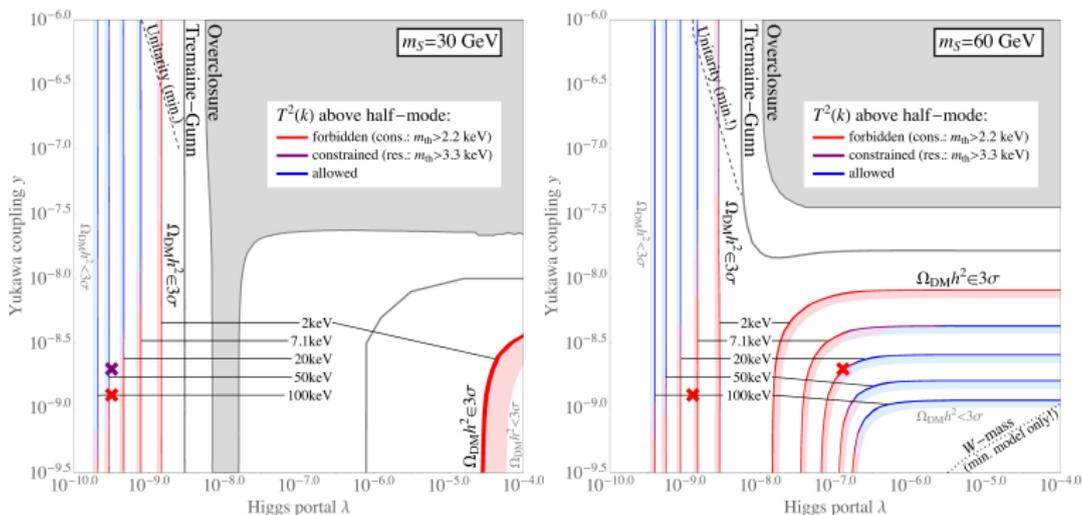
**Figure:** The free-streaming approach (with the standard boundaries) is much more restrictive!

# Half-mode analysis vs. high- $z$ galaxy count



**Figure:** Regions in accordance with the count of high- $z$  galaxies. Adapted from ApJ 836(61) (Menci, Merle, MT et al.).

# Half-mode analysis vs. refined Ly- $\alpha$ and MW satellite counts



**Figure:** Judgement from MW satellites and refined Ly- $\alpha$ . Note the slight offset of the crosses from the iso-mass-lines. Adapted 1704.07838 (Murgia, Viel, Merle, Schneider, MT).

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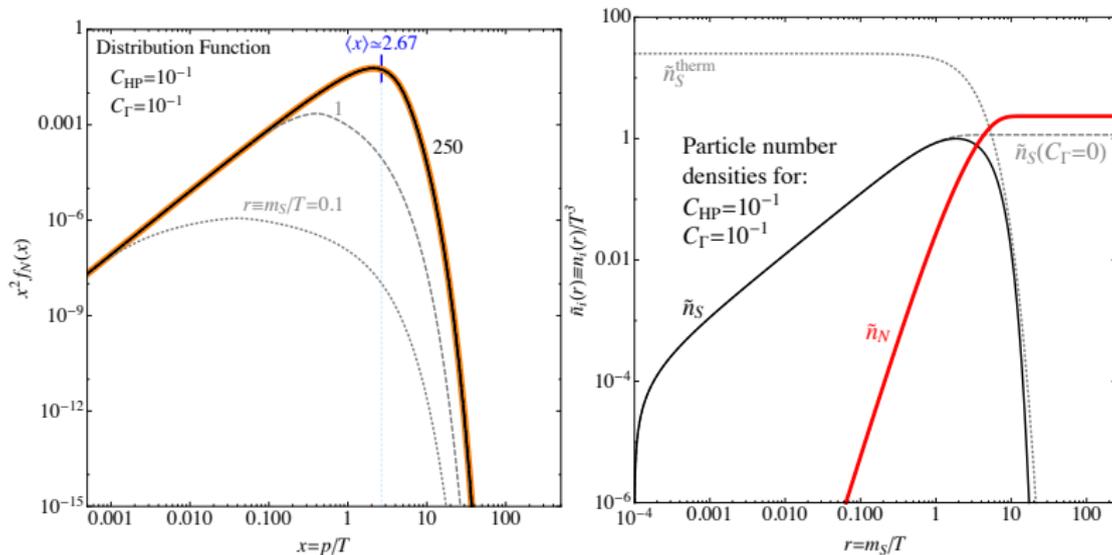
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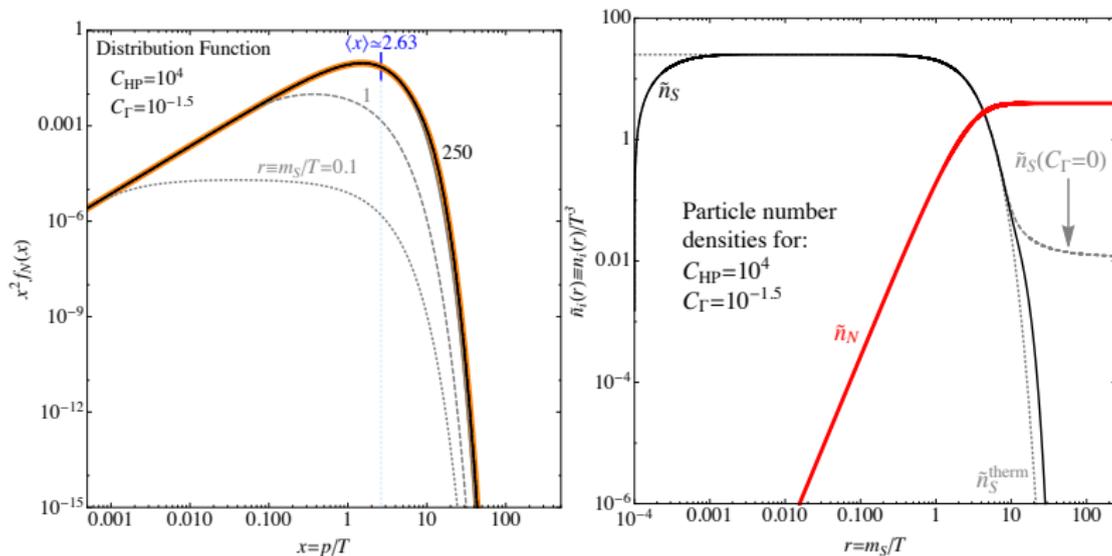
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- Free-streaming *not* very reliable for non-thermal spectra.
- Future experiments like **KATRIN–TRISTAN, ECH<sub>o</sub>, DyNO** will probe the parameter space  $m_N\text{-sin}(2\theta)$  in clean lab environments. They will either find nothing (sensitivity) or put Standard Cosmology into a lot of trouble.

Thank you for your attention!

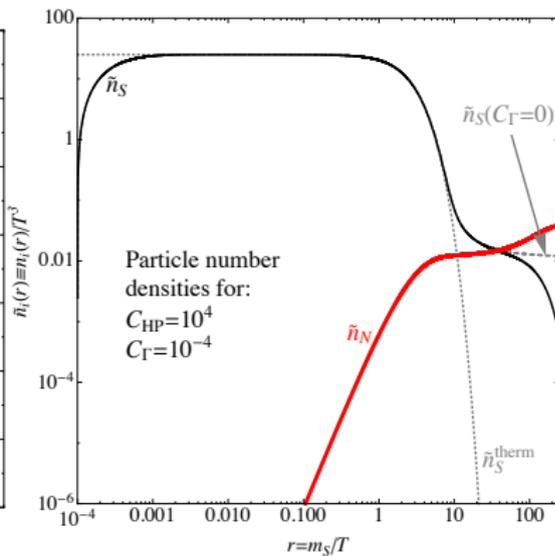
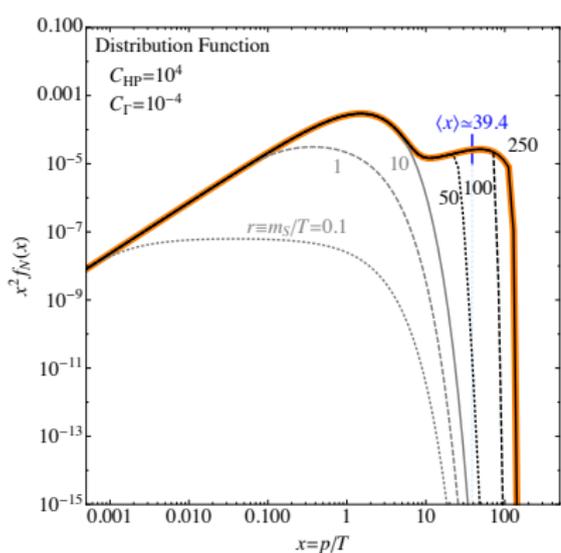
# Backup I – Evolution of abundances vs. evolution of distribution function



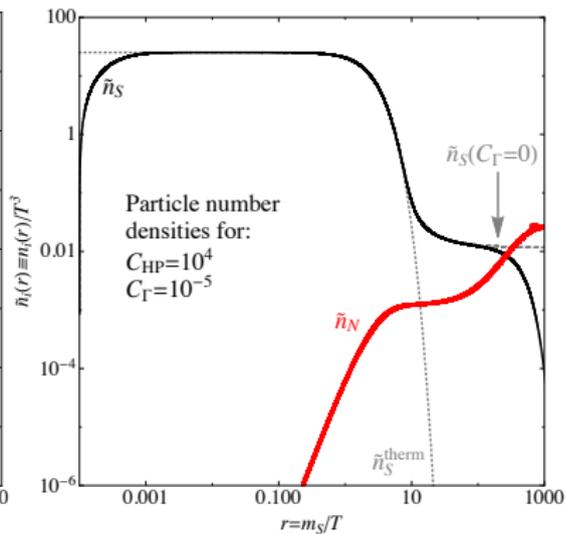
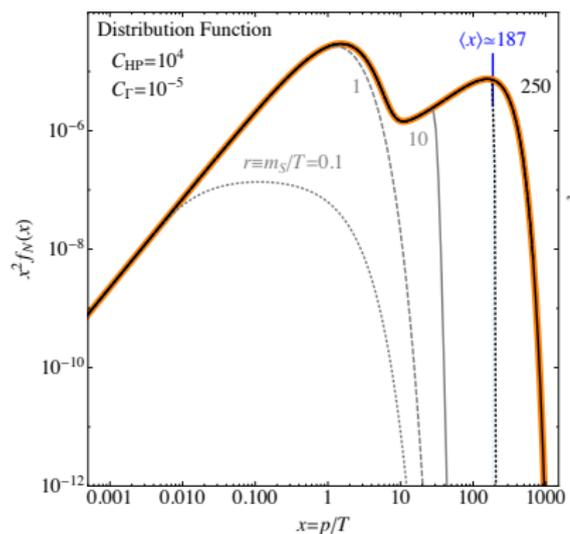
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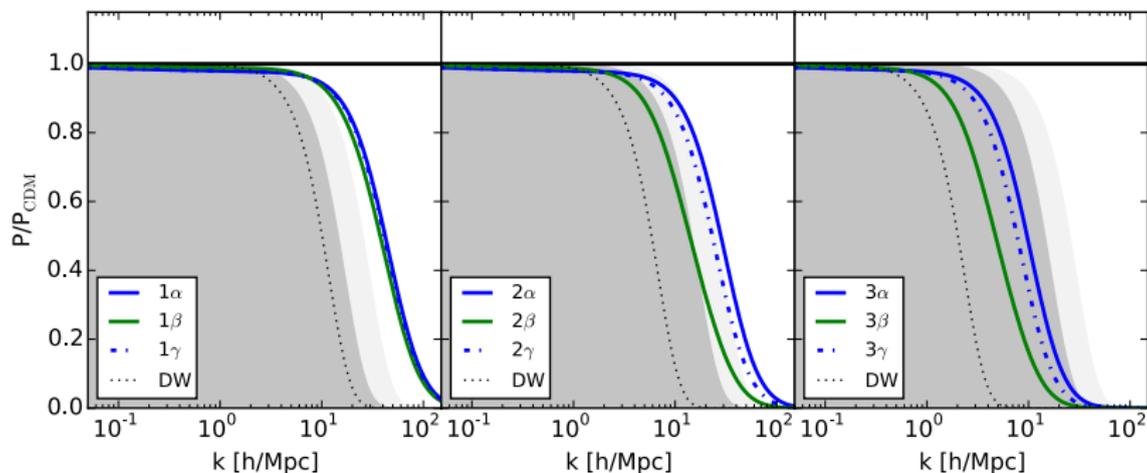
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## Backup II – Effect of DW on scalar decay



$\alpha$  :  $\text{SD}(\mathcal{C}_{\text{HP}}, \mathcal{C}_{\Gamma})$      $\beta$  :  $\text{SD}(\mathcal{C}_{\text{HP}}, \mathcal{C}_{\Gamma}) + \max \text{DW}$      $\gamma$  :  $\text{SD}(\mathcal{C}_{\text{HP}}, \mathcal{C}_{\Gamma}, m_N \stackrel{!}{=} m_N(\beta))$

Backup III – The estimators for Ly- $\alpha$  and MW satellites

- The estimator  $\delta A$  is derived from the power spectrum as follows:

- 1  $P_{1D}(k) \equiv 1/(2\pi) \int_k^\infty dk' k' P(k')$ .

- 2  $r(k) \equiv P_{1D}(k) / P_{1D}^{\Lambda\text{CDM}}(k)$ .

- 3  $A = \int_{k_{\min}}^{k_{\max}} dk r(k)$ .

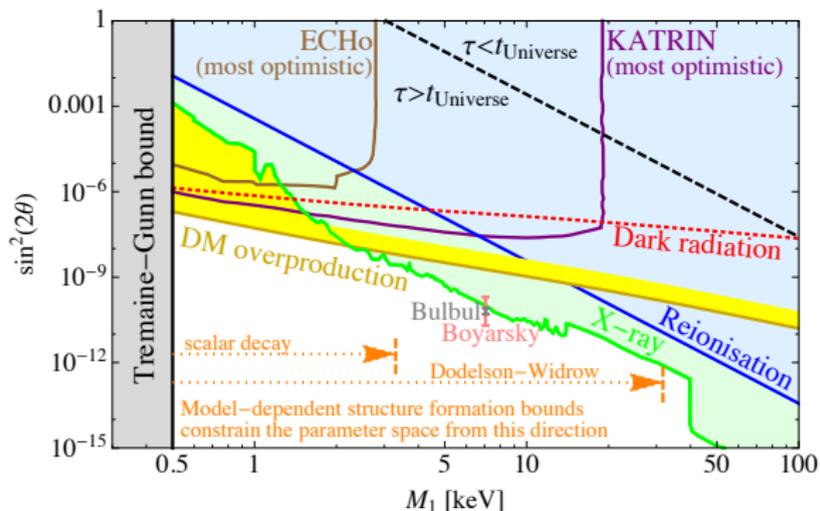
- 4  $\delta A = (A_{\Lambda\text{CDM}} - A) / A_{\Lambda\text{CDM}}$ .

- The estimator  $N_{\text{sat}}$  can be computed as

- 1 Start with differential halo mass function  $dN/dM_{\text{sub}}$  (also computable in linear theory with Press&Schechter approach).

- 2 Integrate from  $M_{\text{sub}} = 10^8 M_\odot / h$  (for  $M_{\text{MW}} = 1.7 \times 10^{12} M_\odot / h$ ).

## Backup IV – Bounds including lab experiments

Synopsis of bounds onto the plane of  $m_N$  vs.  $\sin^2(2\theta)$ :

Courtesy of A. Merle