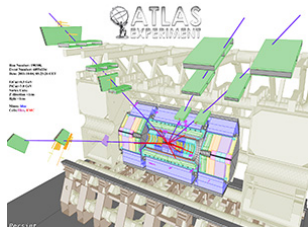


# Precision physics with dibosons at hadron colliders

Marat Freytsis

University of Oregon

WIN2017 — UC, Irvine, June 20, 2016



MF, Chris Frye, Jakub Scholtz, Matt Strassler  
JHEP 1603, 171 [arXiv:1510.08451], ...

# Why precision? Why dibosons?

- in the era of precision Higgs physics
- ...but not all EW physics easy to tie to Higgs measurements
  - ▶ BSM might not be easy to connect either
- non-Higgs precision measurements are the next frontier
- large part of this effort hinges on precision calculations  
q.v. T. Neumann's talk
- but clever choices of observables can also help  
*cf.* hadronic or Higgs decay ratios
- diboson rates related by  $SU(2)_L \times U(1)_Y$  relations  
also custodial  $SU(2)$ 
  - ▶ broken at low energies, but restored above the EW scale
  - ▶ is there any way to take advantage of this?

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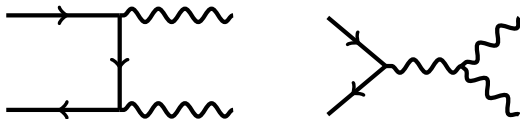
# Plan

- **Leading order**
  - ▶ Structure of partonic cross sections
  - ▶ Ratio observables
- Prospects for measurement
- Next-to-leading order
  - ▶ NLO corrections for  $\sigma(\gamma\gamma)$ ,  $\sigma(Z\gamma)$ ,  $\sigma(ZZ)$
  - ▶ Other higher-order issues
  - ▶ Photon isolation
- Theoretical uncertainties
- Summary and outlook

# (Nearly) massless gauge bosons at high $\sqrt{s}$

expand around unbroken  $SU(2)_L \times U(1)_Y$  (gauge bosons:  $w^a, b$ )

- corrections at  $(m_{W,Z}/E)^2$



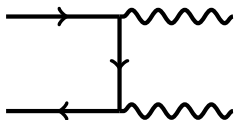
$$bb_1 \equiv bb : |bb\rangle$$

$$wb_3 \equiv wb : \{|w^+b\rangle, |w^3b\rangle, |w^-b\rangle\}$$

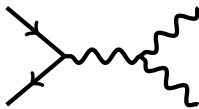
$$ww_1 : |w^-w^+\rangle + |w^-w^+\rangle - |w^3w^3\rangle$$

$$ww_3 : \{|w^+w^3\rangle - |w^3w^+\rangle, |w^+w^-\rangle - |w^-w^+\rangle, \\ |w^3w^-\rangle - |w^-w^3\rangle\}$$

# Amplitudes



(1)



(2)



(3)

schematically define coupling-stripped amplitudes:

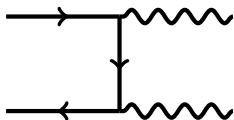
$\phi^a$  goldstones to unitarize  $a_{1,3}$  once  $m_V \neq 0$

$$a_1 = (1), \quad a_3 = (1) + (2), \quad a_L = (3)$$

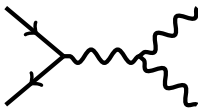
matrix elements of interest:

$$\begin{aligned} a_1 &\sim \mathcal{M}(bb) && \sim \mathcal{M}(ww_1) && \propto t\text{-, } u\text{-channel} \\ a_3 &\sim \mathcal{M}(ww_3) && && \propto s\text{-, } t\text{-, } u\text{-channel} \end{aligned}$$

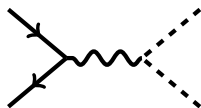
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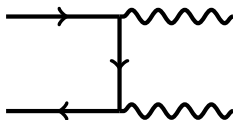
$$a_1 \sim \mathcal{M}(bb) \sim \mathcal{M}(wb) \sim \mathcal{M}(ww_1)$$

$\propto t\text{-}, u\text{-channel}$

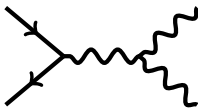
$$a_3 \sim \mathcal{M}(ww_3)$$

$\propto s\text{-}, t\text{-}, u\text{-channel}$

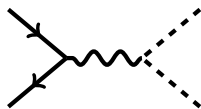
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$\propto t\text{-}, u\text{-channel}$

$$a_3 \sim \mathcal{M}(ww_3)$$

$\propto s\text{-}, t\text{-}, u\text{-channel}$

$$a_L \sim \mathcal{M}(\phi\phi)$$

$\propto s\text{-channel}$



# Amplitudes

*at high energies*

boson statistics fix amplitudes under  $\hat{t} \leftrightarrow \hat{u}$

- $a_1, a_L$  symmetric
- $a_3$  antisymmetric

$\implies a_3$  vanishes at threshold,  $\text{Re}(a_1^\dagger a_3)$  vanishes in asymmetries

$$\begin{aligned} |a_1|^2 &= \frac{\hat{t}}{\hat{u}} + \frac{\hat{u}}{\hat{t}} \\ 2\text{Re}(a_1^\dagger a_3) &= \frac{\hat{t} - \hat{u}}{2\hat{s}} + \frac{1}{4} \left( \frac{\hat{t}}{\hat{u}} - \frac{\hat{u}}{\hat{t}} \right) \\ |a_3|^2 &= \frac{\hat{u}\hat{t}}{4\hat{s}^2} - \frac{1}{8} + \frac{1}{32} \left( \frac{\hat{t}}{\hat{u}} + \frac{\hat{u}}{\hat{t}} \right) \\ |a_L|^2 &= \frac{\hat{u}\hat{t}}{4\hat{s}^2} \end{aligned}$$

# Amplitudes

*with mass corrections*

boson statistics fix amplitudes under  $\hat{t} \leftrightarrow \hat{u}$

- $a_1, a_L$  symmetric
- $a_3$  antisymmetric

$\implies a_3$  vanishes at threshold,  $\text{Re}(a_1^\dagger a_3)$  vanishes in asymmetries

$$|A_1|^2 = (\hat{t}\hat{u} - m_1^2 m_2^2) \left( \frac{1}{\hat{t}^2} + \frac{1}{\hat{u}^2} \right) + \frac{2\hat{s}(m_1^2 + m_2^2)}{\hat{t}\hat{u}}$$

$$\begin{aligned} \text{Re}(A_1^\dagger A_3) &= P_s \left( \hat{t}\hat{u} - m_1^2 m_2^2 - \hat{s}(m_1^2 + m_2^2) \right) \left( \frac{1}{\hat{u}} - \frac{1}{\hat{t}} \right) \\ &\quad + \frac{1}{4} (\hat{t}\hat{u} - m_1^2 m_2^2) \left( \frac{1}{\hat{u}^2} - \frac{1}{\hat{t}^2} \right) \end{aligned}$$

$$|A_3|^2 = \dots$$

$$|A_L|^2 = P_s^2 \left( \hat{t}\hat{u} - m_1^2 m_2^2 + 2\hat{s}(m_1^2 + m_2^2) \right)$$

finite  $m$  effects have uniform structure

# $\gamma\gamma, Z\gamma, ZZ$ Partonic rates

electroweak symmetry breaking

$$\gamma = c_W b + s_W w^3, \quad Z = c_W w^3 - s_W b$$

neutral boson pairs built from  $bb, wb, ww_1$ .

partonic rates all proportional:

$$\frac{d\hat{\sigma}_{q\bar{q}\rightarrow 12}}{d\hat{t}} = \frac{C_{q\bar{q}\rightarrow 12}}{\hat{s}^2} |A_1|^2$$

where

$$C_{q\bar{q}\rightarrow\gamma\gamma} = \frac{1}{2} \frac{\pi\alpha_2^2 s_W^4}{N_c} (Q^4 + Q^4)$$

$$C_{q\bar{q}\rightarrow Z\gamma} = \frac{\pi\alpha_2^2 s_W^2 c_W^2}{N_c} (L^2 Q^2 + R^2 Q^2)$$

$$C_{q\bar{q}\rightarrow ZZ} = \frac{1}{2} \frac{\pi\alpha_2^2 c_W^4}{N_c} (L^4 + R^4)$$

$$L = T_3 - Y_L t_W^2$$

$$R = -Y_R t_W^2$$

$$\frac{d\sigma_{pp \rightarrow V_0^1 V_0^2}}{d\mathcal{O}} = \sum_q \int dx_1 dx_2 f_q(x_1) f_{\bar{q}}(x_2) \frac{d\hat{\sigma}_{q\bar{q} \rightarrow V_0^1 V_0^2}}{d\mathcal{O}} + (x_1 \leftrightarrow x_2)$$

change to more natural variables  $(\hat{s}, y, m_T)$

$$\sigma_{pp \rightarrow V_0^1 V_0^2} = \sum_q \int \frac{d\hat{s}}{s} \int dm_T \frac{d\hat{\sigma}_{q\bar{q} \rightarrow V_0^1 V_0^2}}{dm_T} \int dy f_q f_{\bar{q}}$$

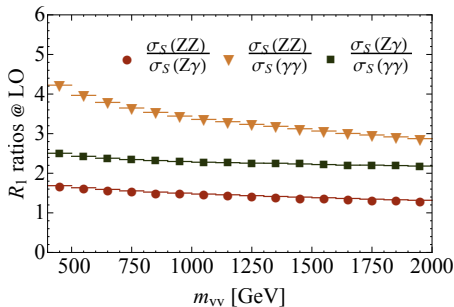
grouping couplings with PDFs into weighted parton luminosities

$$\frac{d\sigma_{pp \rightarrow V_0^1 V_0^2}}{dm_T} = \frac{1}{s} \int d\hat{s} \left| \frac{d\hat{t}}{dm_T} \right| \frac{|A_1|^2}{\hat{s}^2} \underbrace{\sum_q C_{q\bar{q} \rightarrow V_0^1 V_0^2} \int dy f_q f_{\bar{q}}}_{\mathcal{L}_{12}(\hat{s})}$$

# $\gamma\gamma, Z\gamma, ZZ$ Ratio observables

ratios of  $\sigma$ s determined primarily by parton luminosities

$$\left[ \frac{d\sigma_{pp \rightarrow Z\gamma}}{d\sigma_{pp \rightarrow \gamma\gamma}} \right]_{\hat{s}} = \frac{\mathcal{L}_{Z\gamma}(\hat{s})}{\mathcal{L}_{\gamma\gamma}(\hat{s})} \left( 1 + \frac{m_Z^2}{\hat{s}} + \dots \right)$$



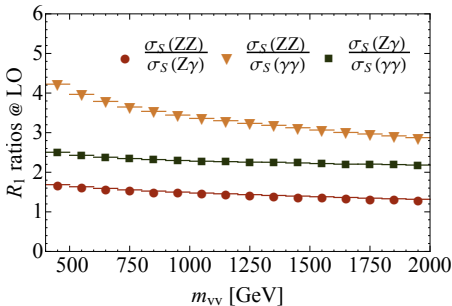
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$V_1^0 V_2^0$	$C_{12}^u \cdot 10^5$	$C_{12}^d \cdot 10^5$
$\gamma\gamma$	1.2	0.07
$Z\gamma$	2.2	0.7
$ZZ$	1.6	3.3



# $\gamma\gamma, Z\gamma, ZZ$

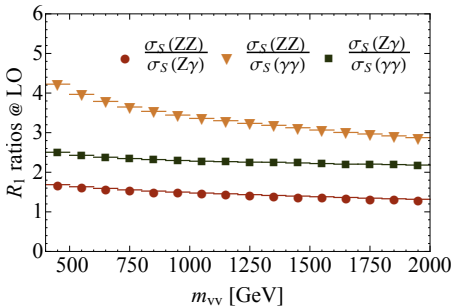
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$u\bar{u}$  dominates – PDFs mostly cancel



## $W^\pm\gamma, W^\pm Z$ at LO

$W^\pm\gamma$  and  $W^\pm Z$  built from  $wb$  and  $ww_3 \implies$  Need  $A_1$  and  $A_3$ .

Also  $A_L$  for  $\phi^\pm\phi^3$  component of  $W^\pm Z$ .

$$\frac{d\hat{\sigma}_{u\bar{d}\rightarrow W^\pm\gamma}}{d\hat{t}} = \frac{\pi|V_{ud}|^2\alpha_2^2 s_W^2}{N_c \hat{s}^2} \left( \frac{Y_L^2}{2} |A_1|^2 \pm 2Y_L \text{Re}(A_1^\dagger A_3) + |A_3|^2 \right)$$

$$\begin{aligned} \frac{d\hat{\sigma}_{u\bar{d}\rightarrow W^\pm Z}}{d\hat{t}} = & \frac{\pi|V_{ud}|^2\alpha_2^2}{N_c \hat{s}^2} \left( \frac{s_W^4 Y_L^2}{2c_W^2} |A_1|^2 \mp 2s_W^2 Y_L \text{Re}(A_1^\dagger A_3) \right. \\ & \left. + 4c_W^2 |A_3|^2 + \frac{1}{2} |A_L|^2 \right) \end{aligned}$$



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numerically small

$$\implies W\gamma/WZ \sim \tan^2\theta_W$$

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Also  $A_L$  for  $\phi^\pm\phi^3$  component of  $W^\pm Z$ .

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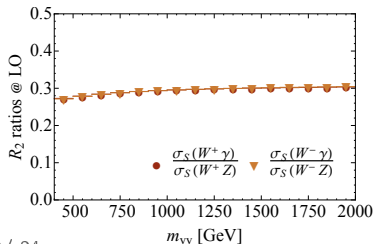
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numerically small

$$\implies W_\gamma/W_Z \sim \tan^2 \theta_W$$

rad. zero at threshold

$$\implies W_\gamma/W_Z \sim 0.19$$

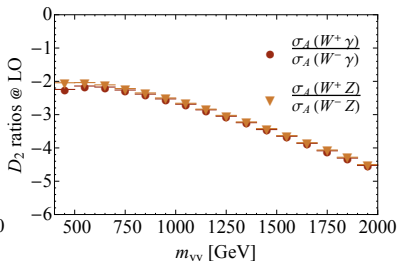
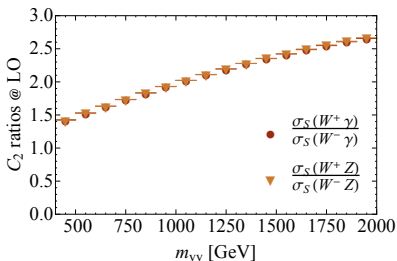


# $W^\pm\gamma, W^\pm Z$ ratio observables

$CP$  symmetry controls  $W^-V^0$  rates:

$$d\hat{\sigma}_S(u\bar{d} \rightarrow W^+V^0) = d\hat{\sigma}_S(d\bar{u} \rightarrow W^-V^0)$$

$$d\hat{\sigma}_A(u\bar{d} \rightarrow W^+V^0) = -d\hat{\sigma}_A(d\bar{u} \rightarrow W^-V^0)$$

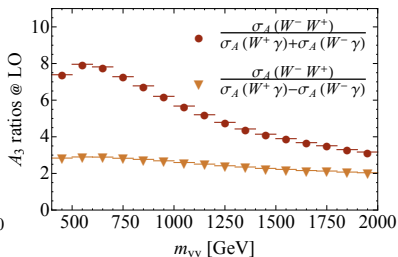
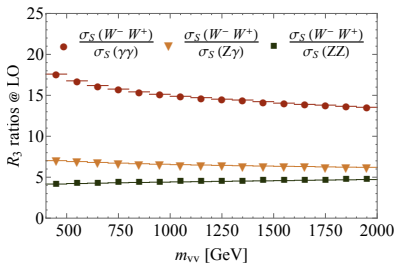


ratios roughly  $\sim f_u/f_d$

# $W^+W^-$ partonic rate

$W^+W^-$  built from  $ww_1, ww_3, \phi^+\phi^-$ .  
Very similar to  $W^\pm\gamma$ .

$$\frac{\sigma_A(W^+W^-)}{a\sigma_A(W^+\gamma) + b\sigma_A(W^-\gamma)} \sim \frac{\mathcal{L}_{u\bar{u}}^A - \mathcal{L}_{d\bar{d}}^A}{4|V_{ud}|^2 s_W^2 Y_L (a\mathcal{L}_{u\bar{d}}^A - b\mathcal{L}_{d\bar{u}}^A)}$$



# Full family of ratio observables

$$\begin{aligned} \bullet R_{1a} &= \frac{\sigma_S(\mathbf{Z}\gamma)}{\sigma_S(\gamma\gamma)}, & R_{1b} &= \frac{\sigma_S(\mathbf{Z}\mathbf{Z})}{\sigma_S(\gamma\gamma)}, & R_{1c} &= \frac{\sigma_S(\mathbf{Z}\mathbf{Z})}{\sigma_S(\mathbf{Z}\gamma)}, \\ \bullet C_{2a} &= \frac{\sigma_S(\mathbf{W}^+\gamma)}{\sigma_S(\mathbf{W}^-\gamma)}, & C_{2b} &= \frac{\sigma_S(\mathbf{W}^+\mathbf{Z})}{\sigma_S(\mathbf{W}^-\mathbf{Z})}, \\ D_{2a} &= \frac{\sigma_A(\mathbf{W}^+\gamma)}{\sigma_A(\mathbf{W}^-\gamma)}, & D_{2b} &= \frac{\sigma_A(\mathbf{W}^+\mathbf{Z})}{\sigma_A(\mathbf{W}^-\mathbf{Z})}, \\ R_2^\pm &= \frac{\sigma_S(\mathbf{W}^\pm\mathbf{Z})}{\sigma_S(\mathbf{W}^\pm\gamma)}, & A_2^\pm &= \frac{\sigma_A(\mathbf{W}^\pm\mathbf{Z})}{\sigma_A(\mathbf{W}^\pm\gamma)}, \\ \bullet R_3 &= \frac{\sigma_S(\mathbf{W}^+\mathbf{W}^-)}{\sigma_S(\mathbf{V}_1^0\mathbf{V}_2^0)}, & A_3 &= \frac{\sigma_A(\mathbf{W}^+\mathbf{W}^-)}{\sigma_A(\mathbf{W}\mathbf{V}^0)}, \end{aligned}$$

For rest of the talk focus on  $R_1$  family

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# Experimental issues

some issues cancel...

- luminosity
- jet energy scale

dominant part of exp. systematics

... some don't

- $Z \rightarrow$  leptons  $\Rightarrow$   $Z$  need additional cuts  
or  $Z \rightarrow \nu\bar{\nu}$  — has it's own issues
  - ▶ some  $Z$ s lost when leptons escape detection
  - ▶ losses decrease at higher  $p_T$
- Finite  $m_Z$  window:  $|m_{\ell\ell} - m_Z| < 25$  GeV
  - ▶ some admixture of  $\gamma^*$  in  $Z$  sample
  - ▶ small effect
- small  $O(5\%)$  shift, calculable with negligible uncertainties

# Variable bin widths

problem: very few  $Z$  decays to leptons

$V_1 V_2$	$N_f + N_b$	$N_f - N_b$
$\gamma\gamma$	12 000	0
$Z\gamma$	2000	0
$ZZ$	220	0
$W^+\gamma$	3300	-500
$W^-\gamma$	2100	220
$W^+Z$	790	33
$W^-Z$	520	-16
$W^-W^+$	9500	-430

choose bin widths for 5% statistical uncertainty.

$R_{1a} = \sigma_S(Z\gamma)/\sigma_S(\gamma\gamma)$  not statistics limited with  $300 \text{ fb}^{-1}$

$C_{2a}, D_{2a}, R_3$  too, but wait for next paper...

others will have to wait until  $3000 \text{ fb}^{-1}$



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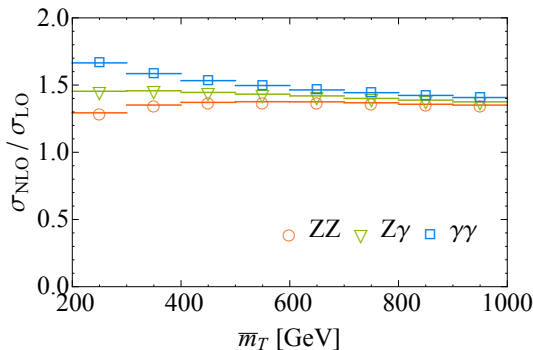
# NLO corrections to diboson production

EW processes at LHC typically have large  $O(\alpha_s)$  corrections

$qg \rightarrow V_1 V_2 q$  appears at  $O(\alpha_s)$ , and  $f_g \gg f_{\bar{q}}$

large uncertainties if  $d\sigma$  “effectively LO” somewhere in PS

$$\bar{m}_T = \frac{1}{2}(m_{T1} + m_{T2}) = \min. E \text{ at } \theta_{CM} = \pi/2$$



# NLO corrections to diboson production

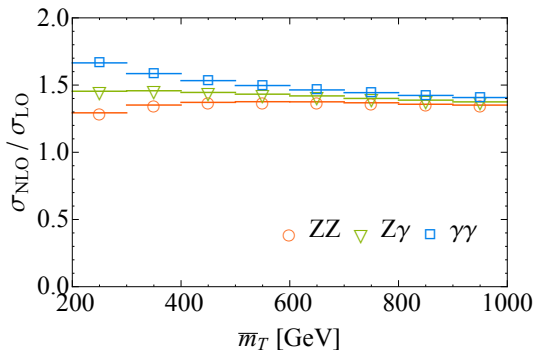
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radiation can never reduce this variable



# NLO corrections to diboson production

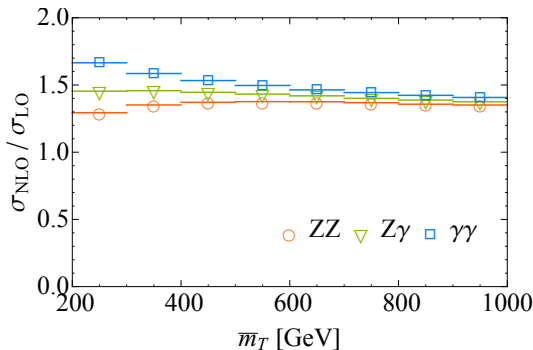
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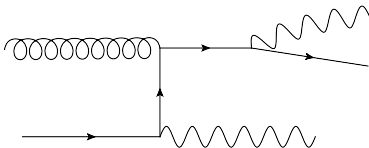
Choose cuts to avoid measurements with large kinematic logs

$$H_T < \frac{1}{2} p_{T,\min}^V, \quad p_{T,\min}^V > \frac{1}{2} p_{T,\max}^V$$

Fixed order calculation reliable



# Photon IR divergences



divergence in  $qg$  process when  $q\gamma$  are collinear  
without photon isolation, configuration will dominate  
will introduce sensitivity to NP IR physics if not careful

# Smooth-cone isolation

*The theorist's solution*

eliminate collinear singularity using “smooth cone” isolation

[Frixione, 1998]

choose parameters  $\epsilon$  and  $\delta$  and require

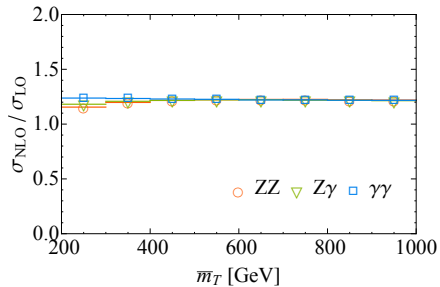
$$\sum_{h \in (\theta < \delta)} p_T^h < \epsilon p_T^\gamma \left( \frac{1 - \cos \theta}{1 - \cos \delta} \right)$$

no partons allowed with  $\theta = 0 \implies$  no collinear singularity

**but**, enhancement at small  $\theta$  for  $\gamma$ , “dead cone” around  $Z$ :  $\theta_{\text{dc}} \approx \frac{m_Z}{m_{\text{VV}}}$

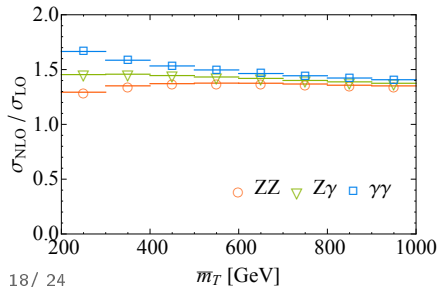
... and requires infinite resolution

# Collinear $qV$ region



$$(\delta, \epsilon) = (1.2, 0.2)$$

$$(\delta, \epsilon) = (0.4, 0.5)$$

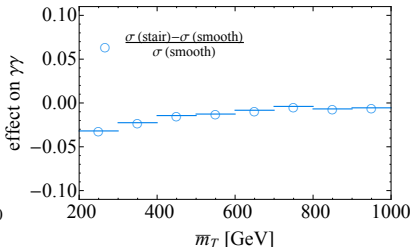
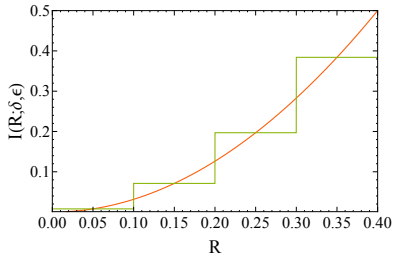


# Staircase isolation

“practical” smooth-cone isolation:

- stairs of width  $\Delta R = 0.1$
- heights match smooth cone at midpoint
- never take heights below 25 GeV (pileup/resolution)

minimize sensitivity to frag. functions & large  $\log(\epsilon)$   
experimentally viable





# gg initial states at NNLO

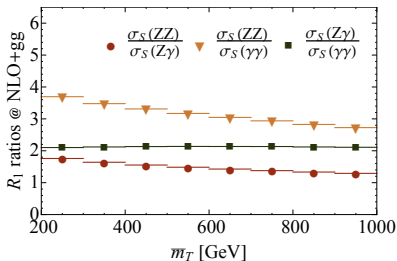
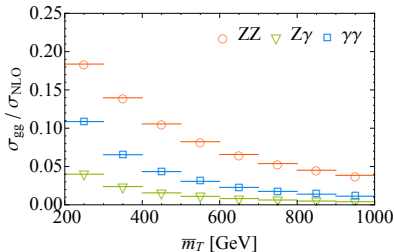
$gg \rightarrow V_1 V_2$

- formally NNLO
- numerically important because of large  $f_g$
- finite, so can be included without full  $O(\alpha_s^2)$  correction

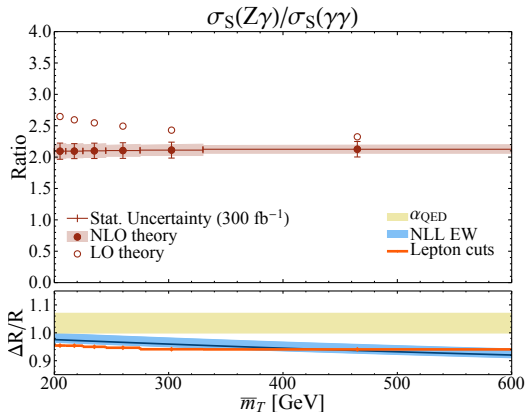
smaller enhancement for  $gg \rightarrow Z\gamma$  due to vanishing of  $gg \rightarrow w^3 b$

$gg \rightarrow \gamma\gamma$  at 2-loop publicly available

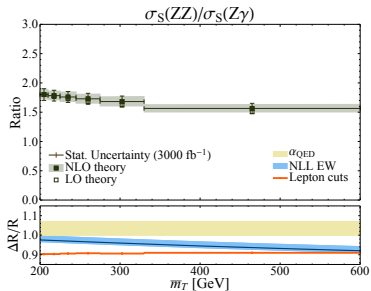
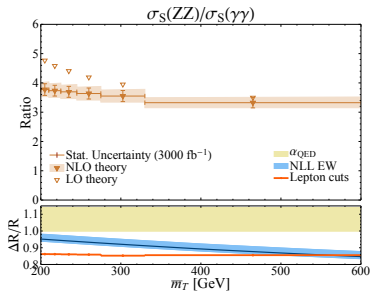
can be used to set scales in  $gg \rightarrow Z\gamma, ZZ$



# Predicted ratios



# Predicted ratios



# Plan

- Leading order
  - ▶ Structure of partonic cross sections
  - ▶ Ratio observables
- Prospects for measurement
- Next-to-leading order
  - ▶ NLO corrections for  $\sigma(\gamma\gamma)$ ,  $\sigma(Z\gamma)$ ,  $\sigma(ZZ)$
  - ▶ Other higher-order issues
  - ▶ Photon isolation
- **Theoretical uncertainties**
- Summary and outlook

# Uncertainty budget

Effect	$R_{1a}$ ( $Z\gamma/\gamma\gamma$ )	$R_{1b}$ ( $ZZ/\gamma\gamma$ )	$R_{1c}$ ( $ZZ/Z\gamma$ )	Comments
$qq \rightarrow VVqq$	2–3%	3–3.5%	1.5–2.5%	extrapolating $p_{T,\min}^j \rightarrow 0$
$\mu_R, \mu_F$ ( $gg$ )	0.5–1%	1%	1–2%	uses NLO $gg \rightarrow \gamma\gamma$
$\mu_R, \mu_F$ (NLO)	0.5–1%	1.5–2.5%	1–1.5%	varied independently
PDF	0.5%	1–1.5%	0.5–1%	MSTW2008 using MCFM
$\gamma$ isolation	< 0.1%	< 0.1%	< 0.1%	Uncertainty in frag. fun.
$\alpha_{\text{QED}}$	7%	14%	7%	Fully correlated
EW (LL)	+2% –1%	+3% –1%	+2% –1%	EFT scale uncertainty

# Plan

- Leading order
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# Summary & outlook

$SU(2)_L \times U(1)_Y$  structure of diboson rates at LO suggests organizing data in cross section ratios

observables based on this structure:

- low uncertainties, small QCD corrections

- candidates for (even) high(er)-precision calculation

certainly useful as check that we understand SM backgrounds

how to best use this for new physics?

- reliable characterization of new resonances?

- increased sensitivity to non-resonant effects?

- can anything be done with less luminosity?

Thank you!