

# Relativistic Heavy Ion Physics

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Rutgers University

# Why do we do Relativistic Heavy Ion Physics?

Goal: Create the hottest matter on earth  
(Quark-Gluon Plasma)

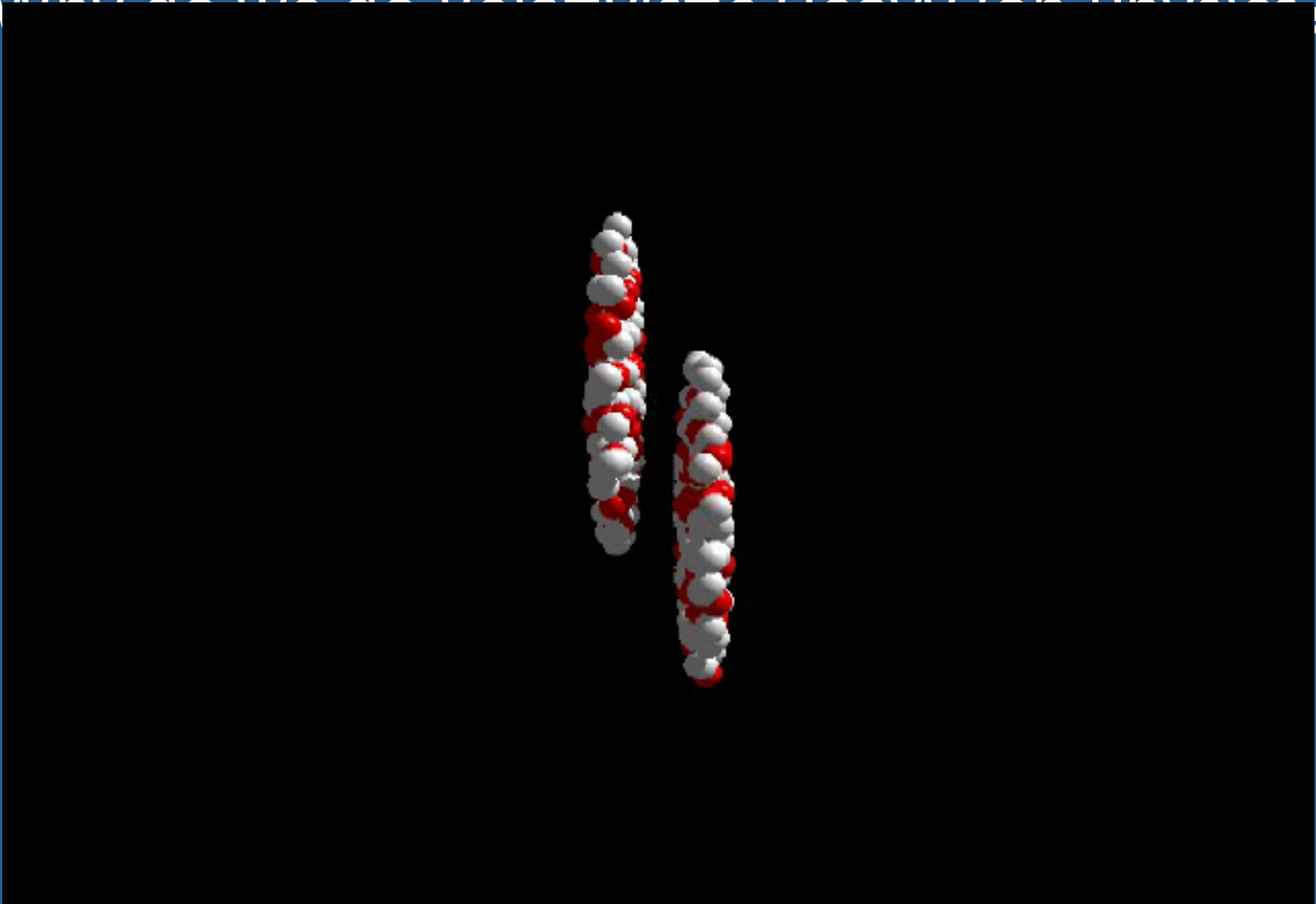
A relativistic heavy ion collision:

Two nuclei colliding at  $\sqrt{s} \sim 1 - 10000$  GeV

Thousands of new particles are produced.

The product of the collision is NOT a simple superposition of elementary nucleon-nucleon collisions.

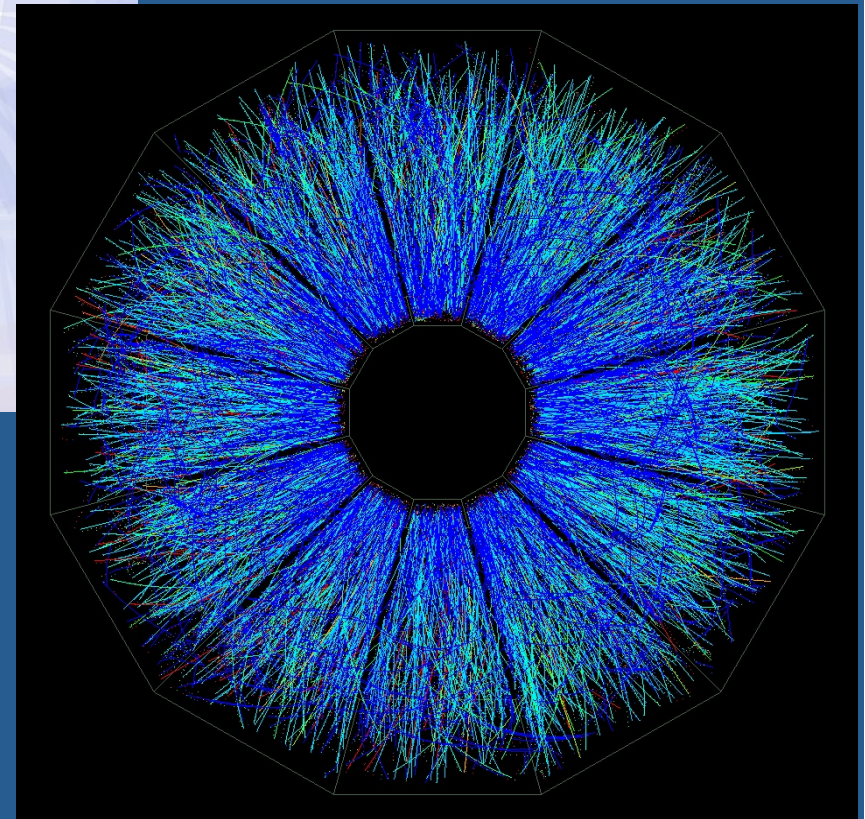
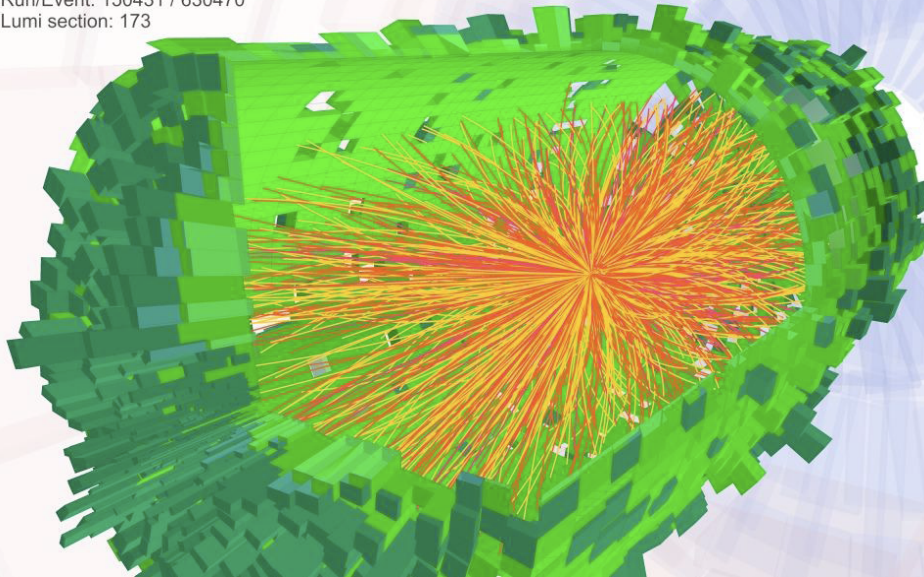
# Why do we do Relativistic Heavy Ion Physics?



# Heavy Ion Events in Detectors:



CMS Experiment at LHC, CERN  
Data recorded: Mon Nov 8 11:30:53 2010 CEST  
Run/Event: 150431 / 630470  
Lumi section: 173



**Q1:** *Why* measure such complexity?

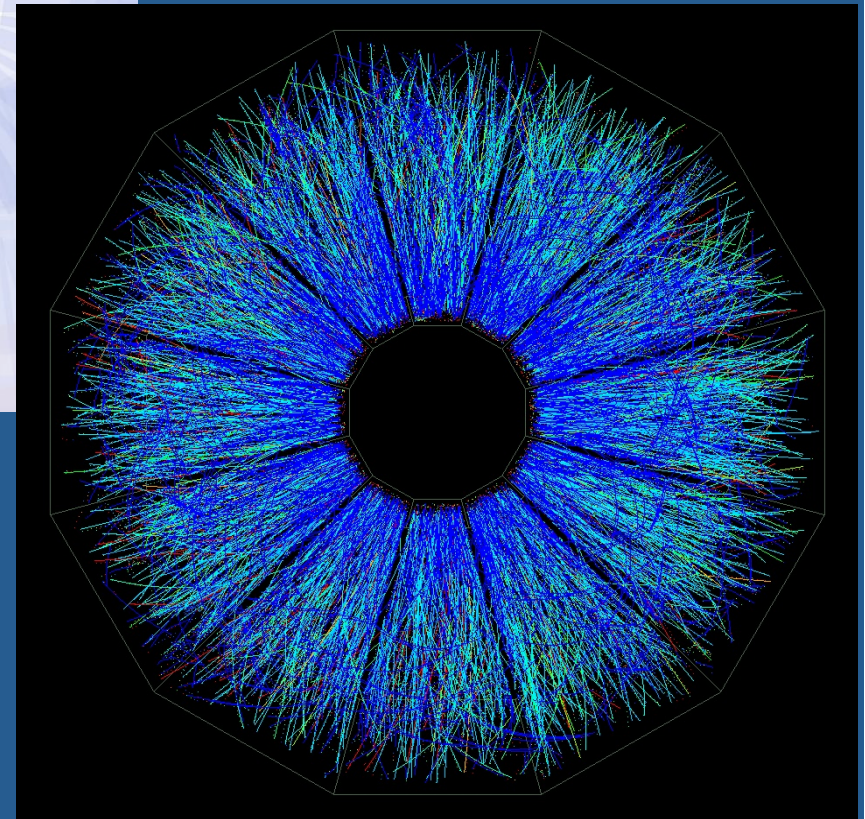
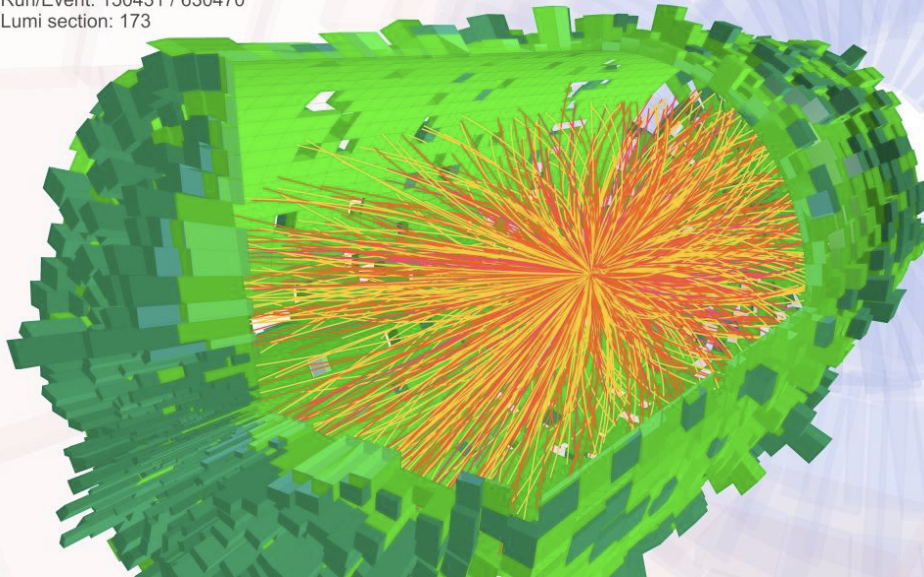
**Q2:** How to measure such complexity?

**Q3:** What did we learn so far?

# Heavy Ion Events in Detectors:



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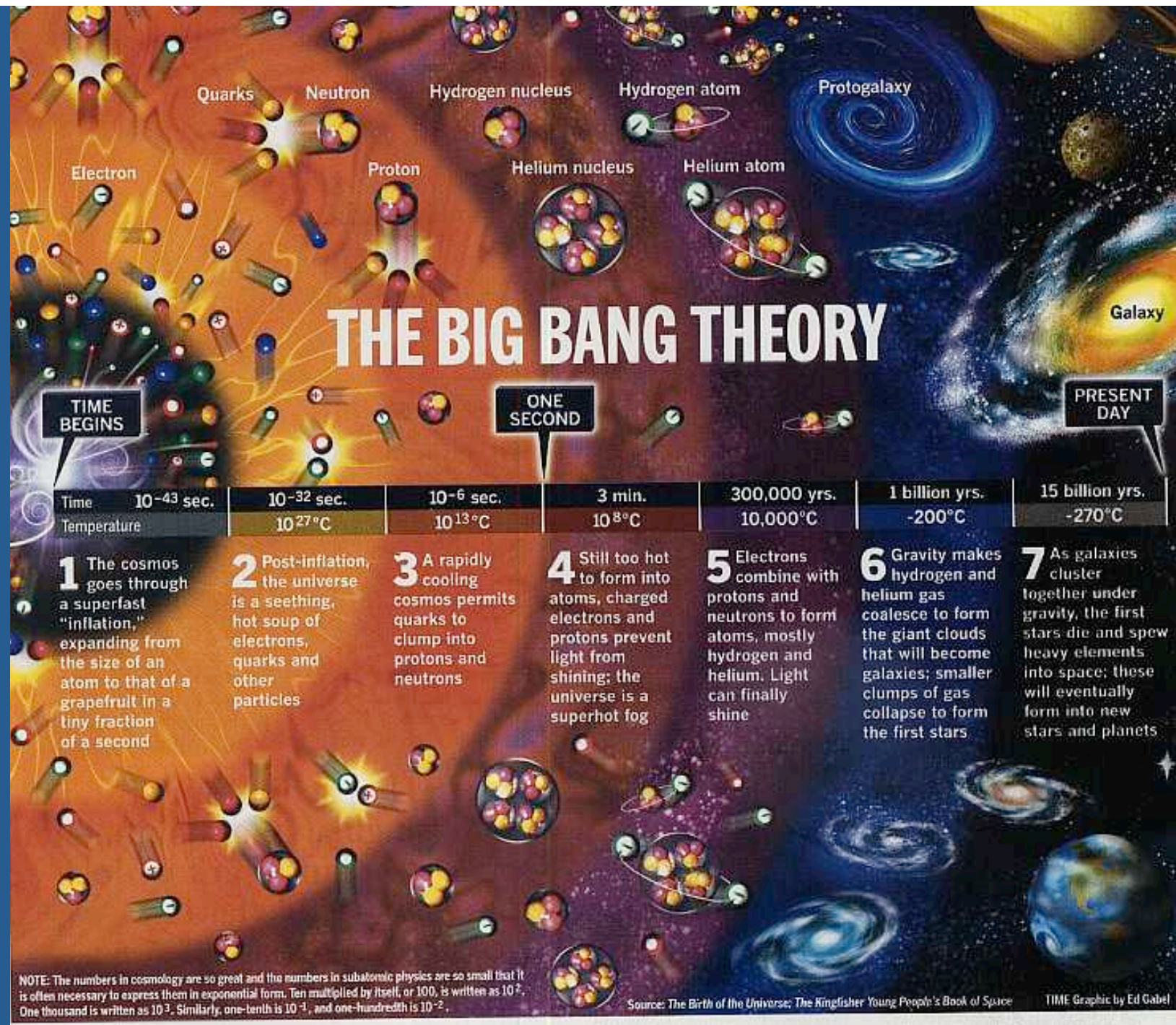


**Q1:** *Why* measure such complexity?

**Q2:** *How* to measure such complexity?

**Q3:** *What* did we learn so far?

- Verify existence of QGP
- Study properties of QGP
- Use external and internal probes
- Small viscosity perfect liquid.
- Opaque to fast partons



# QGP was there on the "First Day"

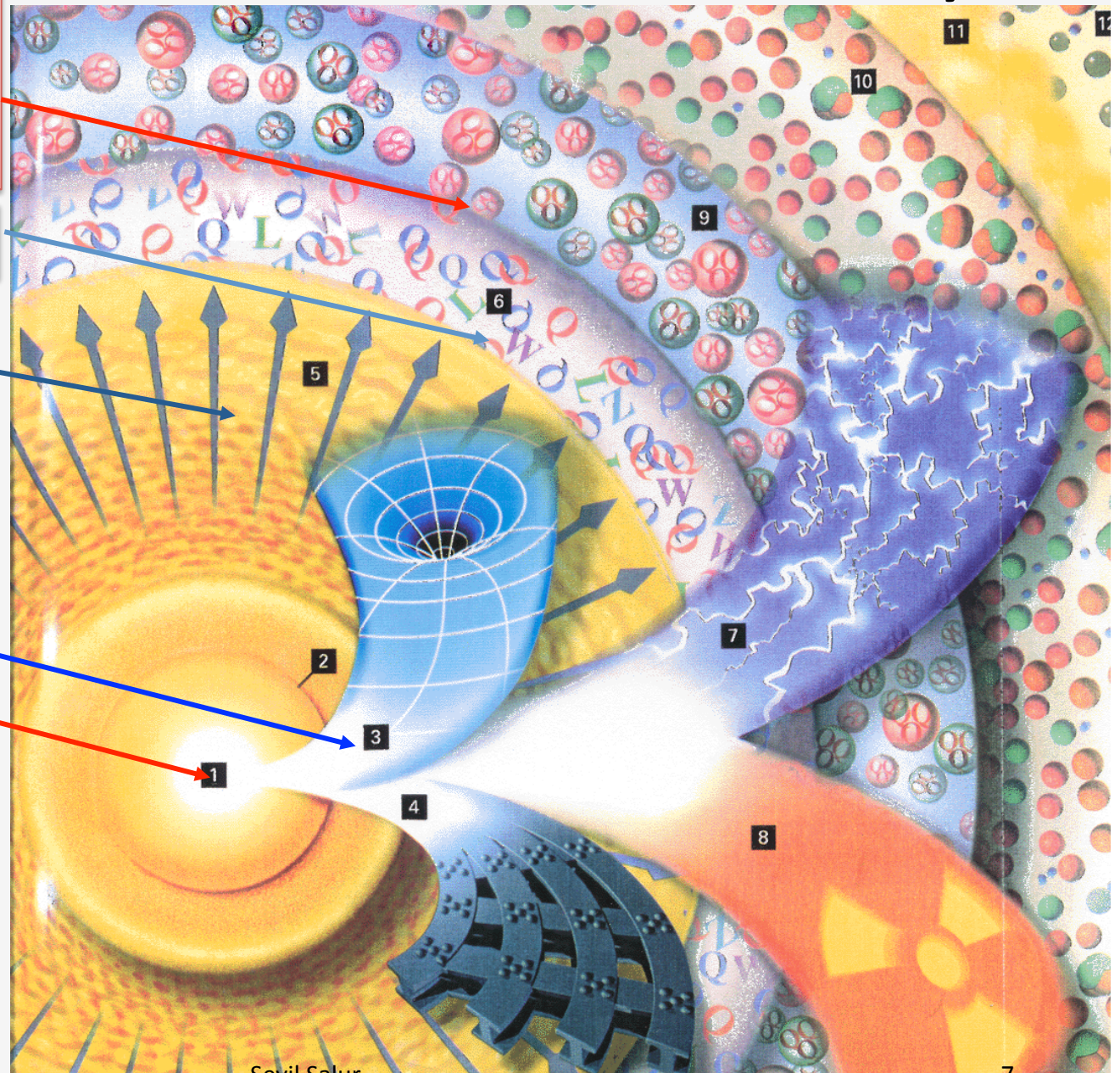
At 10  $\mu$ -seconds  
&  $\sim 10^{12}$  Kelvin  
Quark-to-hadron  
phase transition

Quark-Gluon Plasma

Rapid inflation

gravity, strong & E-W  
forces separate

'Big Bang'

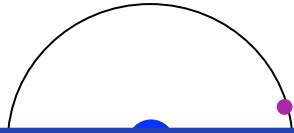


# How to measure such a complexity?

## An analogy... and a difference!

to study structure of an atom...

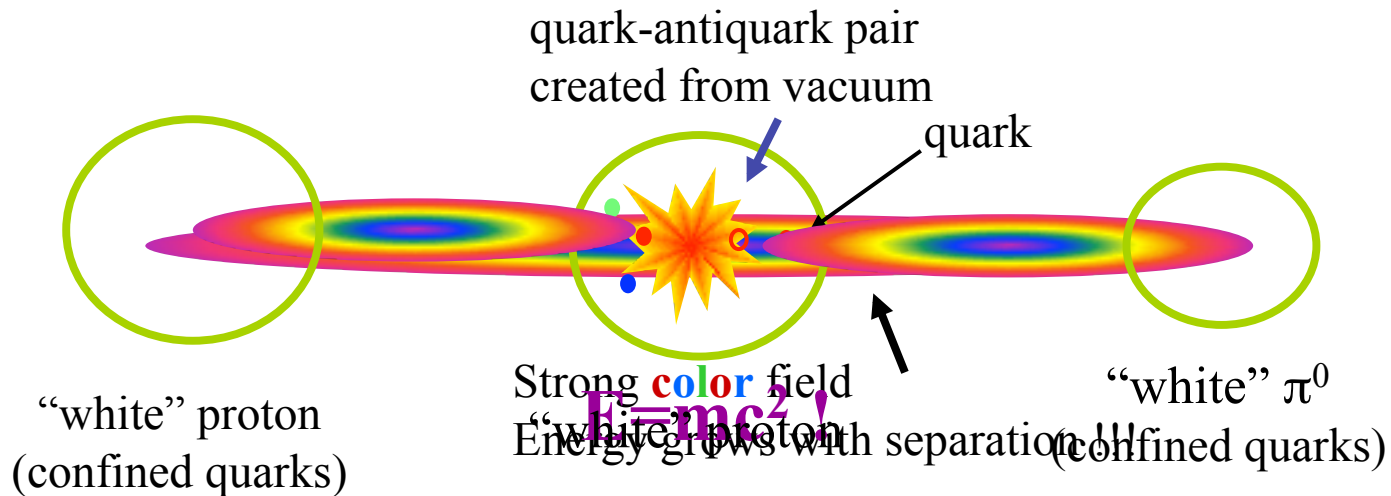
electron



separate constituents

To understand the strong force and the phenomenon of confinement:  
Create and study a system of deconfined colored quarks (and gluons)

**Confinement:** fundamental & crucial (but *not* understood!) feature of strong force  
- colored objects (quarks) have  $\infty$  energy in normal vacuum

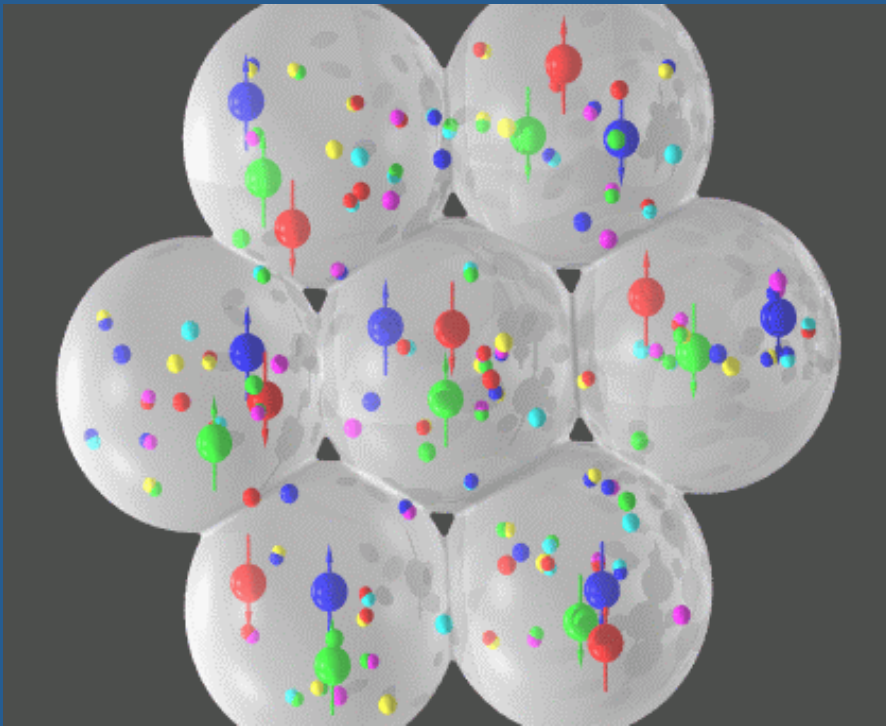




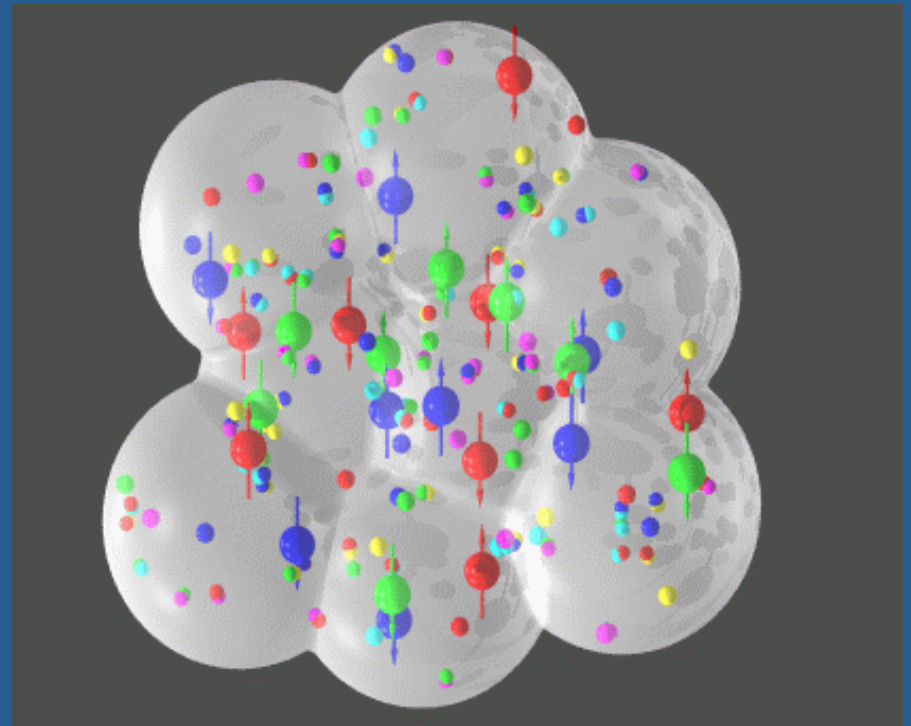
Increase the temperature and pressure.

Crush matter into a soup of its constituents.

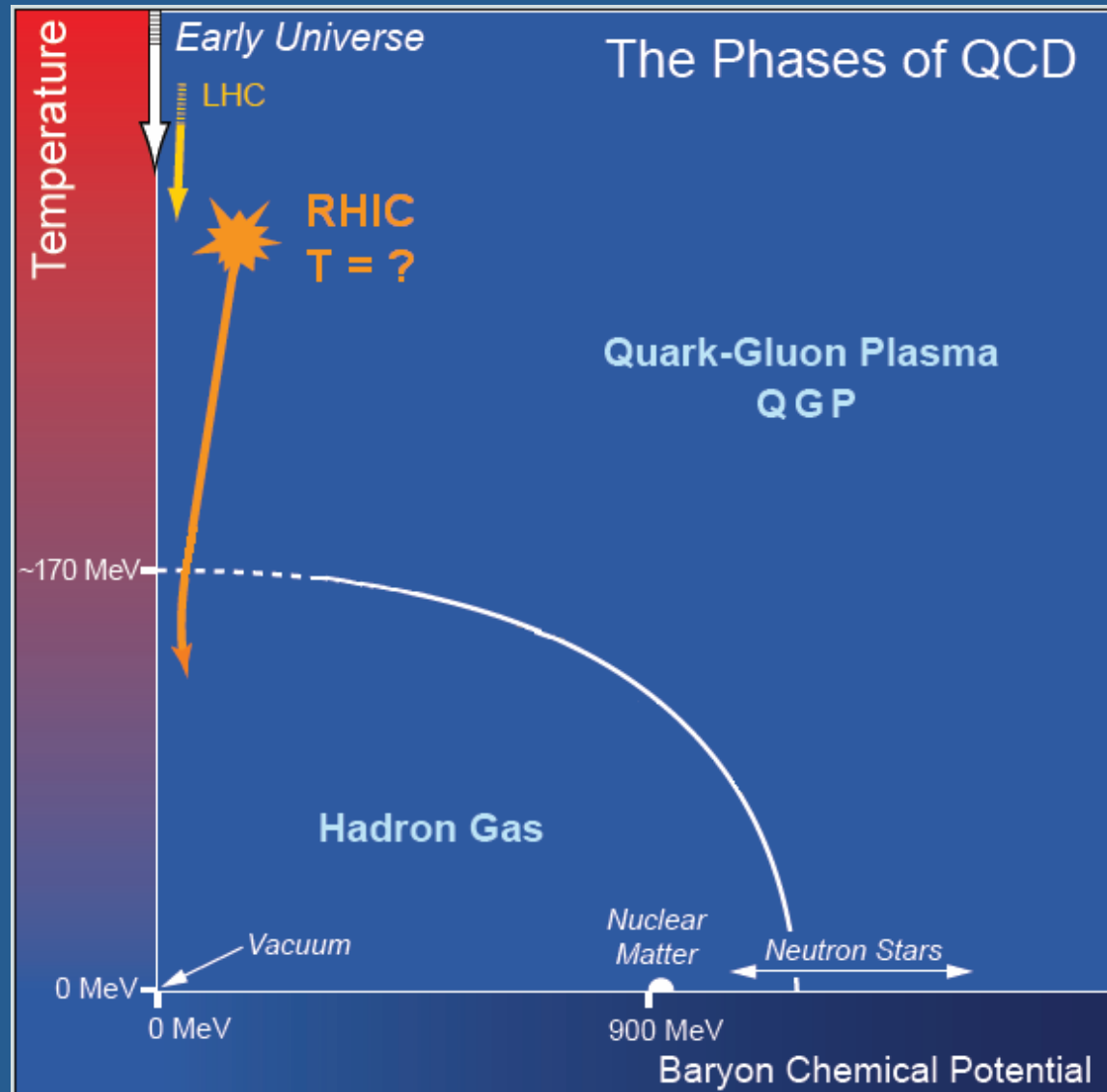
*Hadronic matter*



*Quark gluon plasma*  
A very hot soup at  $\sim 10^{12}K$



# The Landscape of QCD



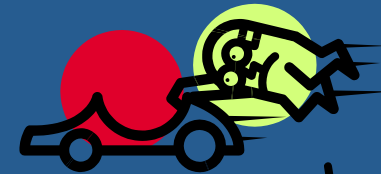
Heavy Ion Collisions at RHIC and LHC create conditions sufficient to “melt” matter into a quark gluon plasma

How can we experimentally study the thermodynamics of the STRONG force?



# Imagine...

- You know that ice exists...
- Your theory friends with huge computers tell you that there is something called water...
- You don't have a way to heat ice...
- So you put millions of ice cubes in an ice-accelerator
- Send them at 99.995% of the speed of light to collide
- Generating thousands of ice-cube+ice-cube collisions per second...
- And you watch it all from the vicinity of Mars!



# Producing “Bulk” nuclear Matter in the laboratory.

We must create/compress/heat a **bulk** (geometrically large) system

Freeze/melt a single H<sub>2</sub>O molecule?

Fundamental distinction from particle physics

*Only* achievable through collisions of the heaviest nuclei (Au, Pb) at the highest available energy— Relativistic Heavy Ion Collider (RHIC) and Large Hadron Collider (LHC)

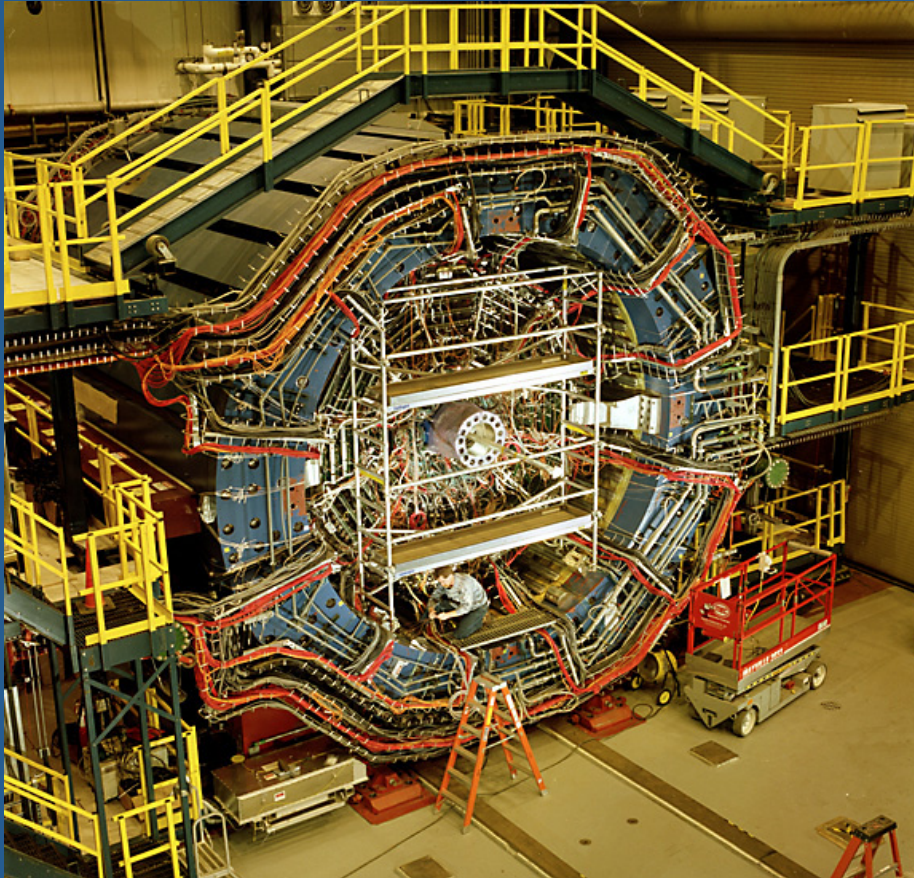
- **RHIC** ≡ **Relativistic Heavy Ion Collider**

- **3.83 km circumference**
- **Two independent rings**
  - ◆ 120 bunches/ring
- **Capable of colliding**  
**~any nuclear species**  
**on**  
**~any other species**
- **Energy:**
  - ➔ Up to 500 GeV for p+p
  - ➔ Up to 200 GeV for Au+Au  
(per N-N collision)
- **Luminosity**
  - ◆ Au+Au:  $2 \times 10^{26} \text{ cm}^{-2} \text{ s}^{-1}$
  - ◆ p+p :  $2 \times 10^{32} \text{ cm}^{-2} \text{ s}^{-1}$   
(*polarized*)



200 GeV)

# RHIC Experiments



*STAR ~550 Collaborators  
specialty: large acceptance  
Hadronic Observables  
Jets & Di-Hadron Physics  
High- $p_T$  Quarkonia*

*PHENIX ~550 Collaborators  
specialty: rare probes, leptons,  
and photons*

# Last 10 Years of Discoveries

- **Collective Flow:**
  - behaves more like liquid rather than gas.
  - small viscosity perfect liquid.
- **Particle Production:**
  - recombination/ coalescence dominates over fragmentation at medium  $p_T$
- **Jet Quenching:**
  - opaque to fast partons





Mont Blanc

## LHC: The Next Frontier...

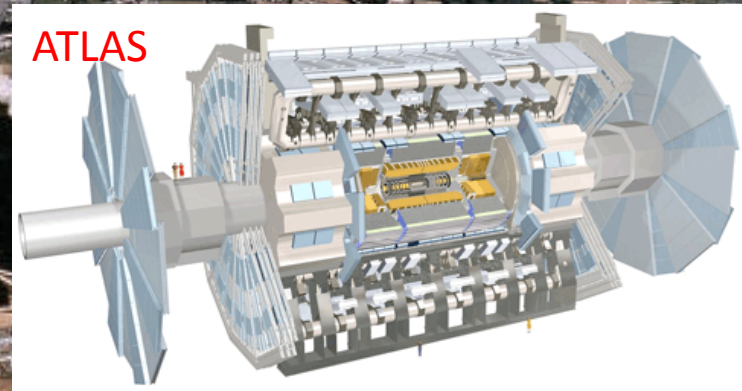
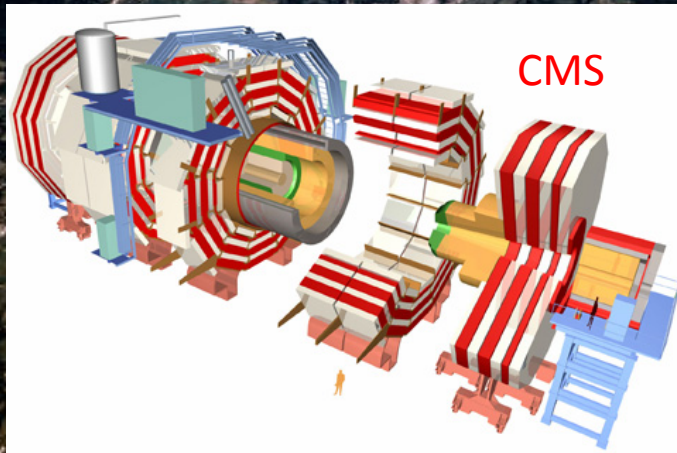
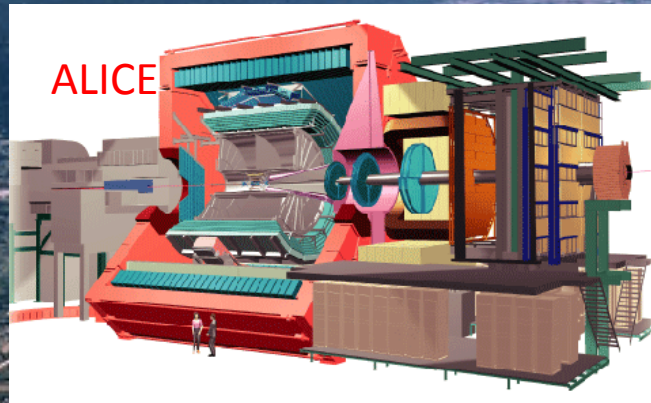
**LHC ≡ Large Hadron Collider**

**LHC is not only a p+p machine!  
At least 4 weeks in a year is devoted for heavy ions...**

- ❑ **27 km circumference**
- ❑ **100 m underground**
- ❑ **Two independent rings**
- ❑ **Capable of colliding  
~any nuclear species  
on  
~any other species**
- ❑ **Energy:**
  - ➔ **Up to 14000 GeV for p+p**
  - ➔ **Up to 5500 GeV for Pb+Pb  
(per N-N collision)**

# LHC Experiments

LHC Heavy Ion program started in late 2010 Pb+Pb and p+p at 2.76 TeV per NN!



## Why Study Heavy Ion Collisions at LHC ?

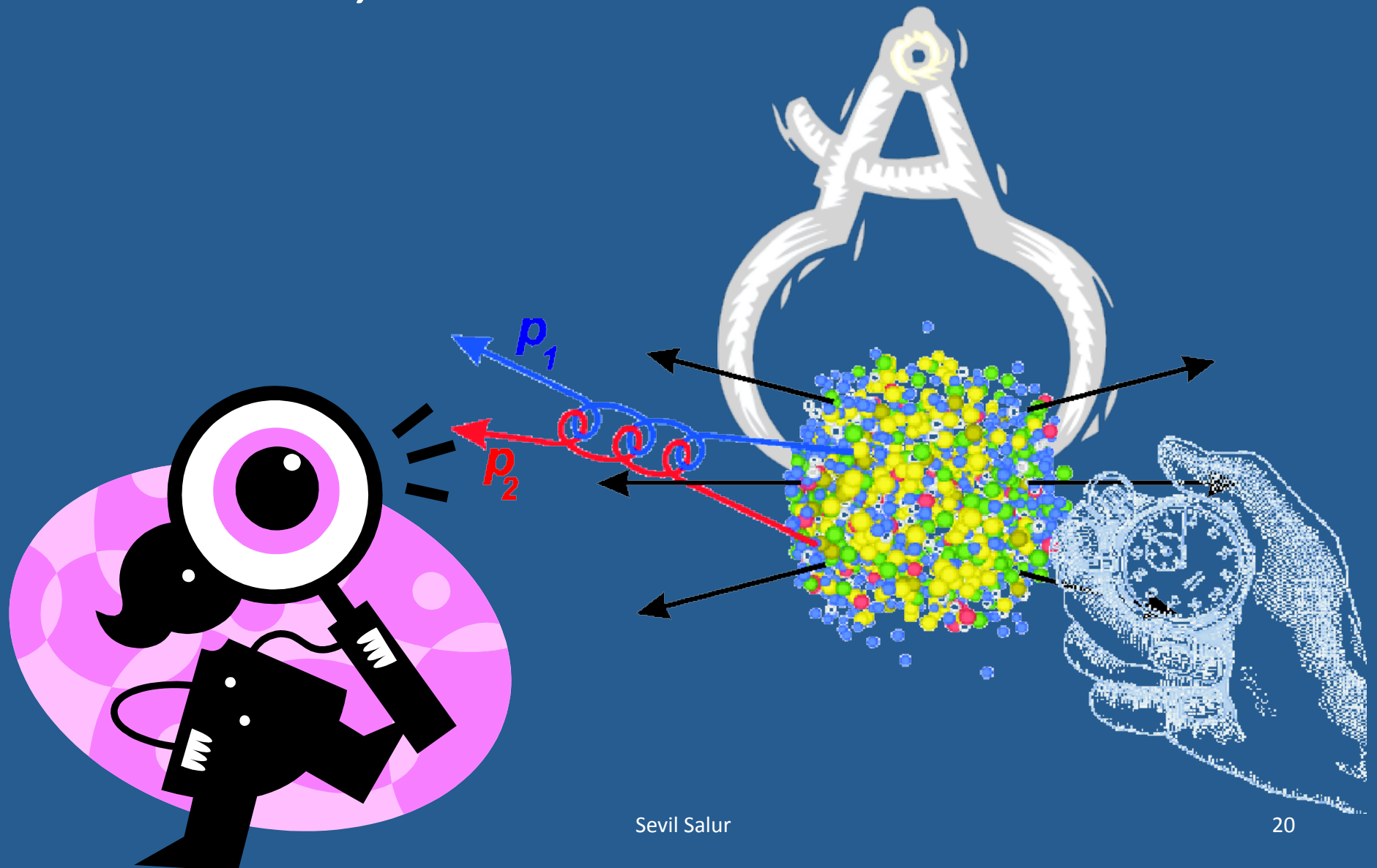
Central collisions	SPS	RHIC	LHC
$s^{1/2}(\text{GeV})$	17	200	5500
$dN_{\text{ch}}/dy$	500	700-1500	$3-10 \times 10^3$
$\varepsilon (\text{GeV}/\text{fm}^3)$	2.5	3.5-7.5	15-40
$\tau_{\text{QGP}} (\text{fm}/c)$	<1	1.5-4.0	4-10

J. Schukraft QM2001

LHC provides a **critical** lever arm in energy.

LHC : Longer - Hotter – Colossal (Bigger)

# So, what have we seen?



# Experimental search for “interesting” phenomena

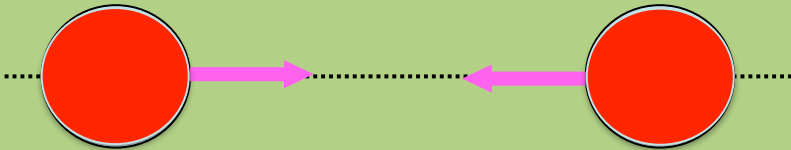
- Look at elementary p+p collisions
  - Measure an observable (e.g. Jet production)
- Look at Heavy Ion collisions
  - Measure the same observable as we do in p+p
- Compare them, is there something new?

# Geometry Matters!

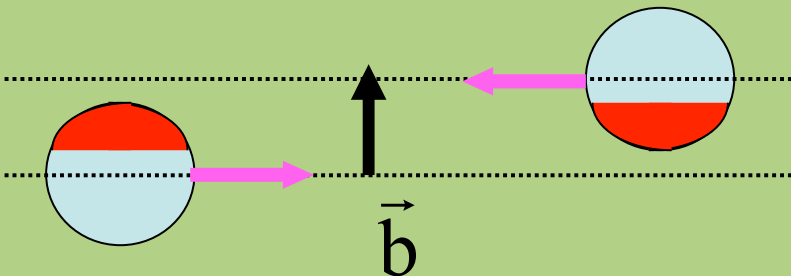
Impact parameter vector  $\vec{b}$  :

- $\perp$  beam direction
- connects centers of colliding nuclei

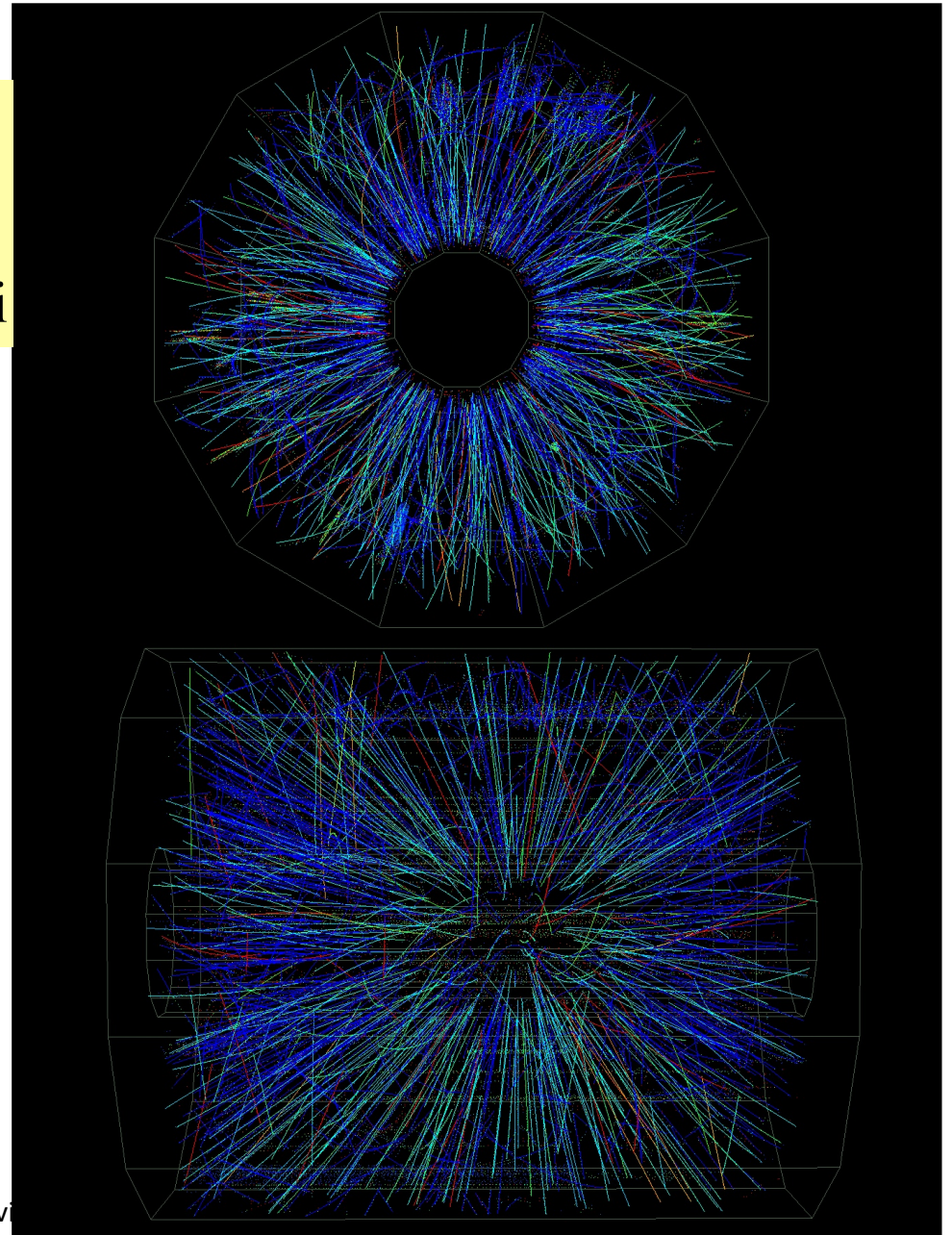
$b = 0 \Leftrightarrow$  “central collision”  
many particles produced



“peripheral collision”  
fewer particles produced

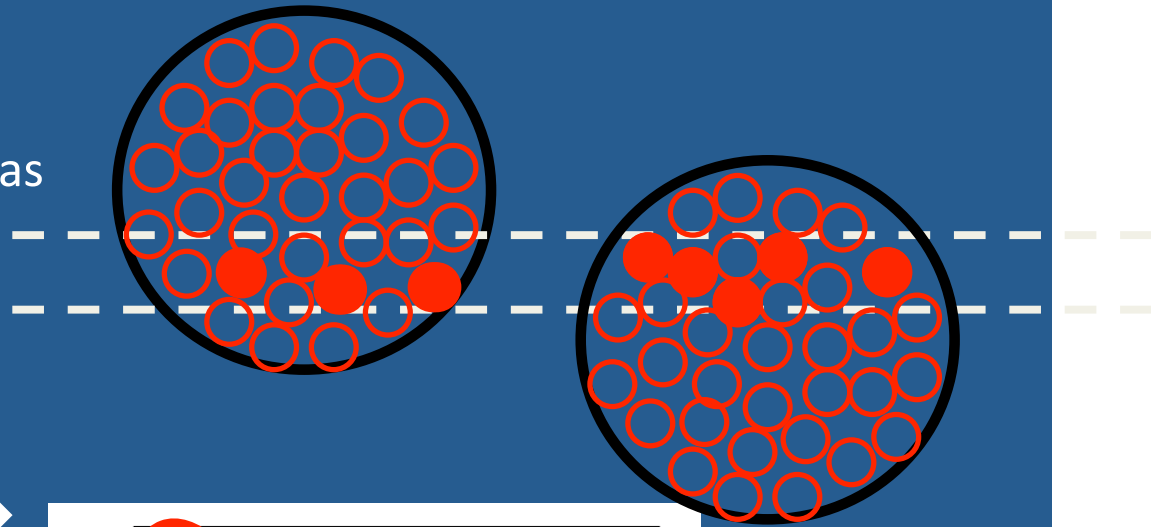


Sev

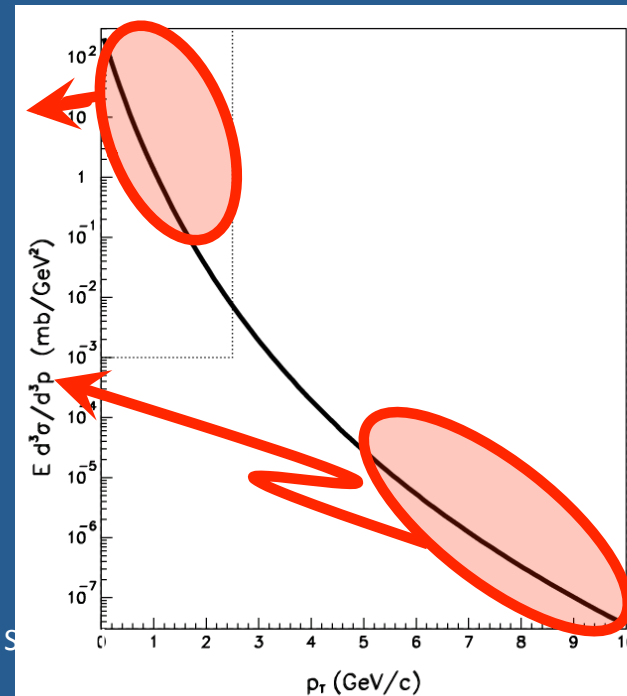


# Geometry Matters!

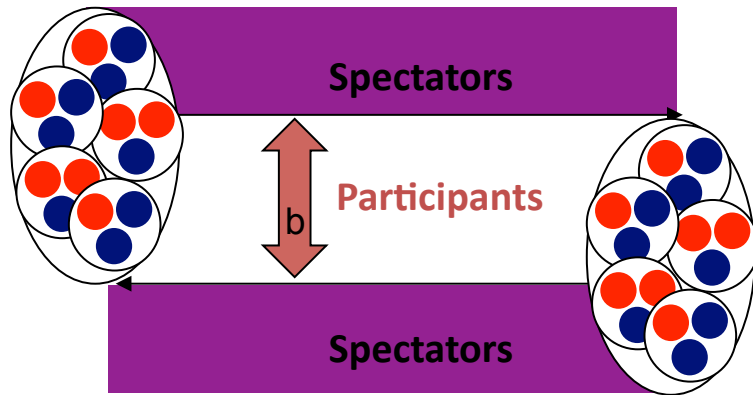
- Focus on some slice of the collision:
  - Assume 3 nucleons struck in A, and 5 in B
  - Do we weight this contribution as
    - $N_{\text{part}} (= 3 + 5) ?$
    - $N_{\text{Bin}} (= 3 \times 5) ?$



- Answer is a function of  $p_T$ :
  - Low  $p_T \rightarrow$  large cross sections  $\rightarrow$  yield  $\sim N_{\text{part}}$ 
    - Soft, non-perturbative, “wounded nucleons”, ...
  - High  $p_T \rightarrow$  small cross sections  $\rightarrow$  yield  $\sim N_{\text{Bin}}$ 
    - Hard, perturbative, “binary scaling”, point-like,  $A \cdot B$ , ...

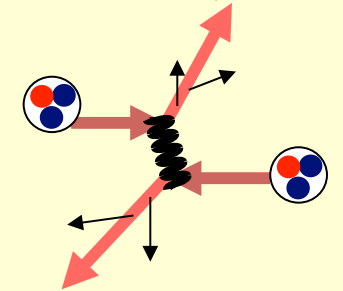


# Terminology: Centrality of A+A Collisions



Number of Binary Collisions:  
 (# of inelastic nucleon+nucleon collisions)

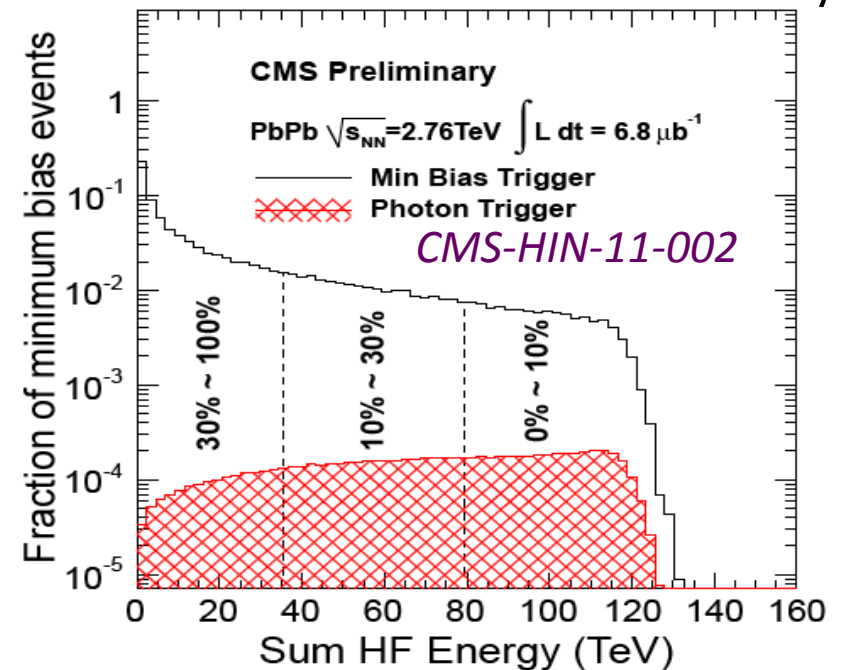
1. Jet Production
2. Heavy Flavor (s,c,b)



Number of Participant:  
 (# of incoming nucleons in the overlap area)

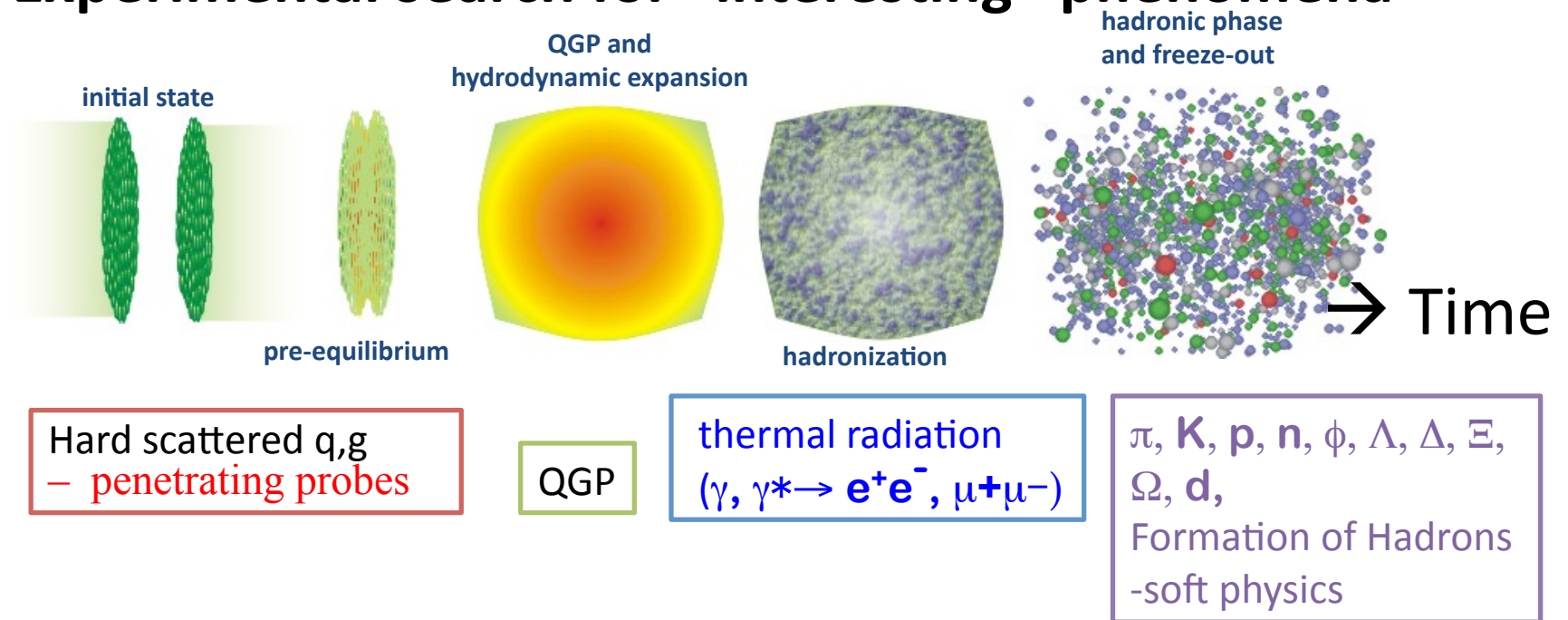
1. Soft Hadron Production
2. Transverse Energy

Fraction of cross section "centrality"

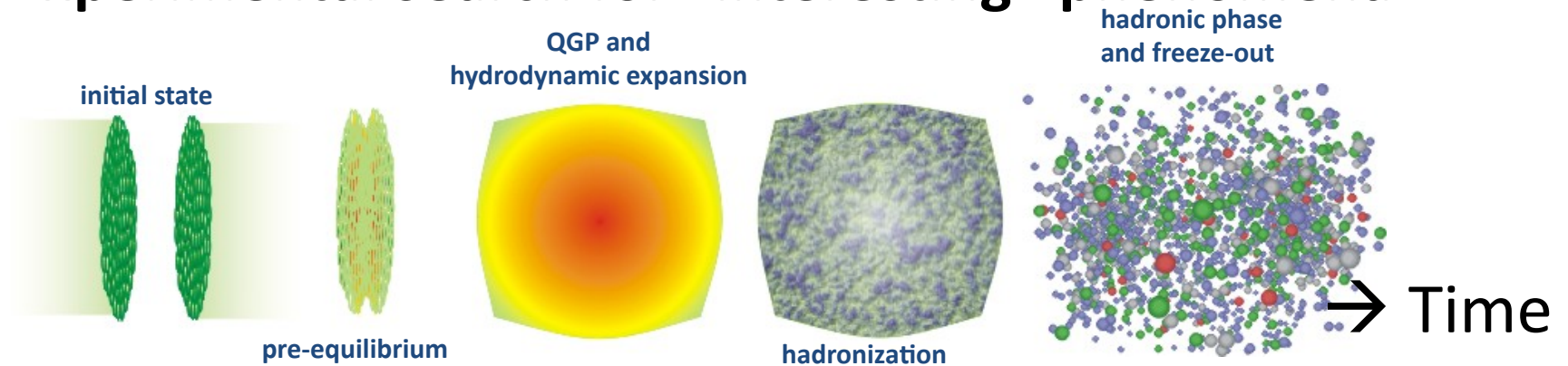




# Experimental search for “interesting” phenomena

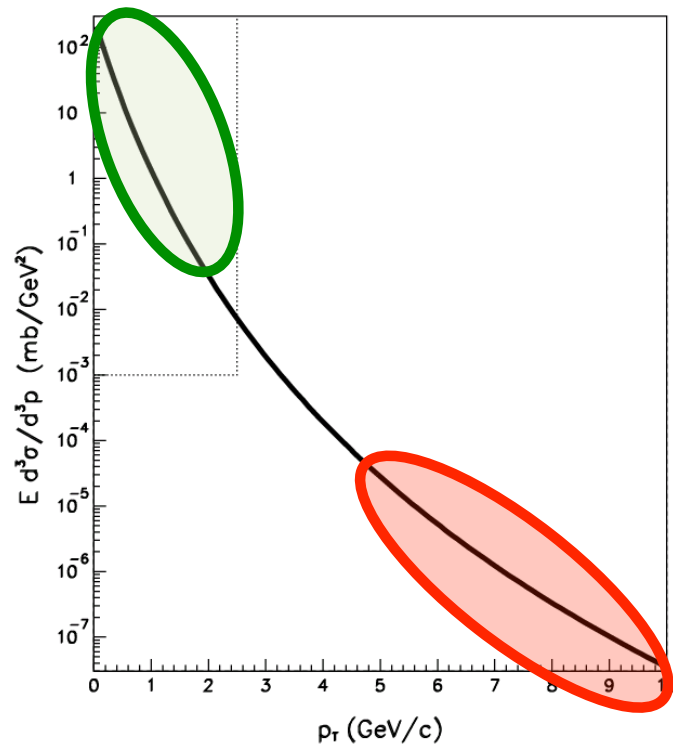


# Experimental search for “interesting” phenomena



*Hard Probes –  
penetrating probes*

*soft physics*

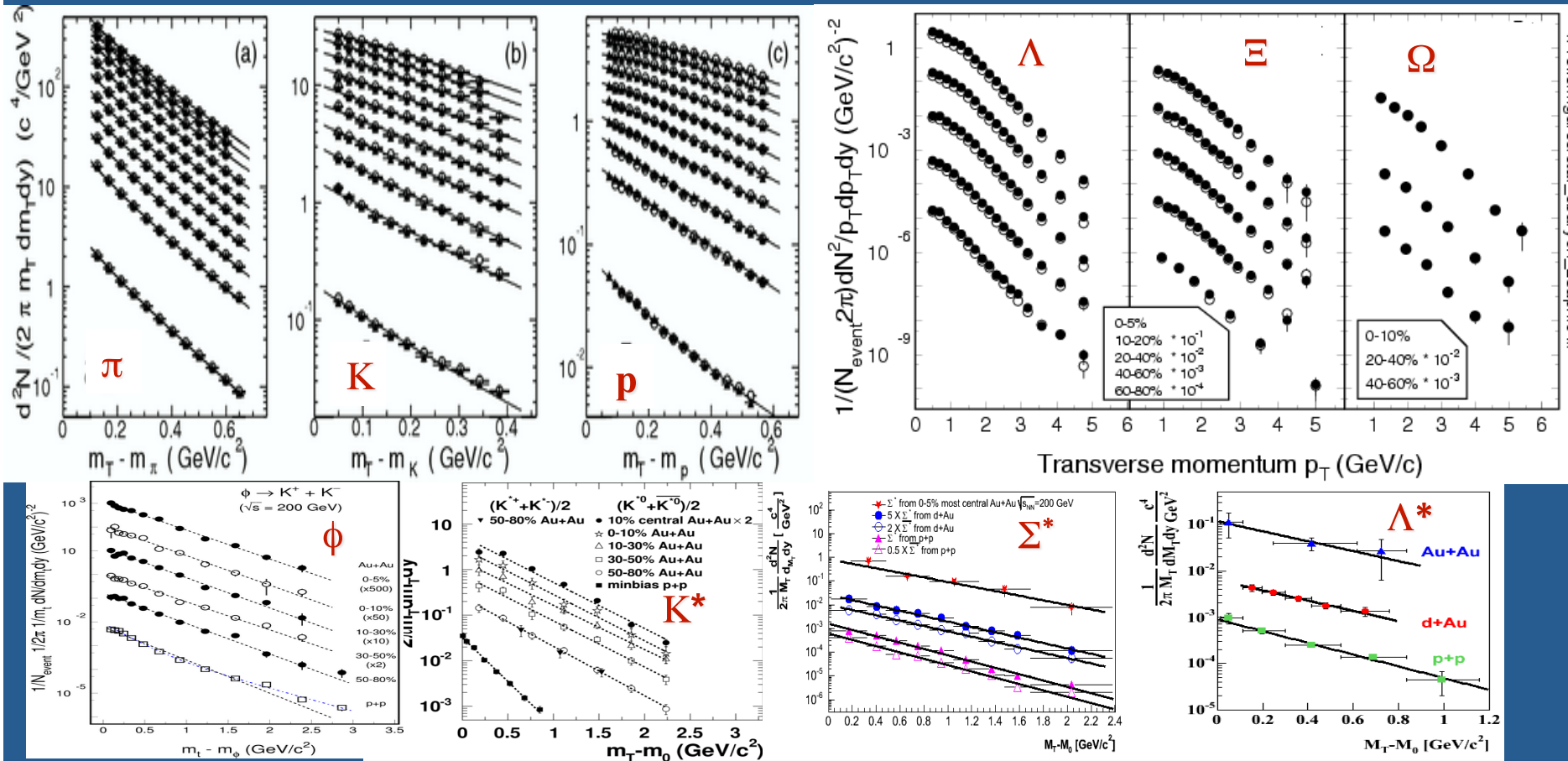


Soft Physics:  $p_T < \sim 1.5 \text{ GeV}/c$ :  
“thermal” particles radiated  
from bulk medium “internal”  
plasma probes

Hard Probes:  $p_T > 3 \text{ GeV}/c$ :  
large  $E_{\text{tot}}$  (high  $p_T$  or  $M$ )  
autogenerated “external” probe  
describe by perturbative QCD



# Lots of particles...



$e^\pm$ ,  $\pi^\pm$ ,  $\pi^0$ ,  $K^\pm$ ,  $K^{*0}(892)$ ,  $K_s^0$ ,  $\eta$ ,  $p$ ,  $d$ ,  $\rho^0$ ,  $\phi$ ,  $\Delta$ ,  $\Lambda$ ,  $\Sigma^*(1385)$ ,  $\Lambda^*(1520)$ ,  $\Xi^\pm$ ,  $\Omega$ ,  $D^0$ ,  $D^\pm$ ,  $D_s$ ,  $J/\Psi$ 's,  $\Upsilon$ 's (+ anti-particles) ...

How to characterize this richness of data?

# Particle Production and Volume

Particle production can be described by phase space!

Pointed out by Fermi and Hagedorn in 50-60's  
(and discussed much more since)

*Assume:* Ideal hadron resonance gas thermally and chemically **equilibrated**

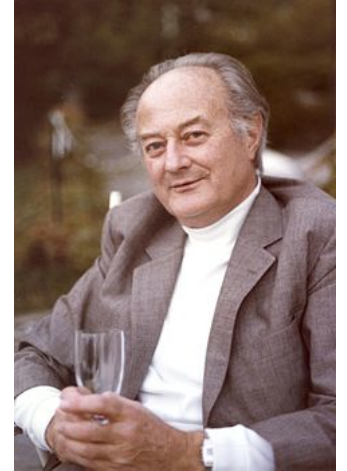
*Recipe:* Canonical (small system i.e. pp):

**Quantum Numbers conserved exactly.**

Grand Canonical limit (large system i.e. central AA):

**Quantum Numbers conserved on average** via chemical potential  
 $\Rightarrow$  partition function  $\Rightarrow$  density of particles of species  $\rho_I$

*Output:* temperature  $T$ , chemical potential  $\mu_i$  which generates particle-antiparticle difference and  $\gamma_i$  which regulates the sum of particle-antiparticle pairs



A multi-hadron state should be described by thermodynamics with a limiting temperature. If spectrum of resonant states is exponential, as higher states are populated,  $T$  increases.

If number of states increases exponentially,  $T$  saturates!

# Particle Production and Volume

Particle production can be described by phase space!

Pointed out by Fermi and Hagedorn in 50-60's  
(and discussed much more since)

Statistical models are used to estimate the equilibrium properties

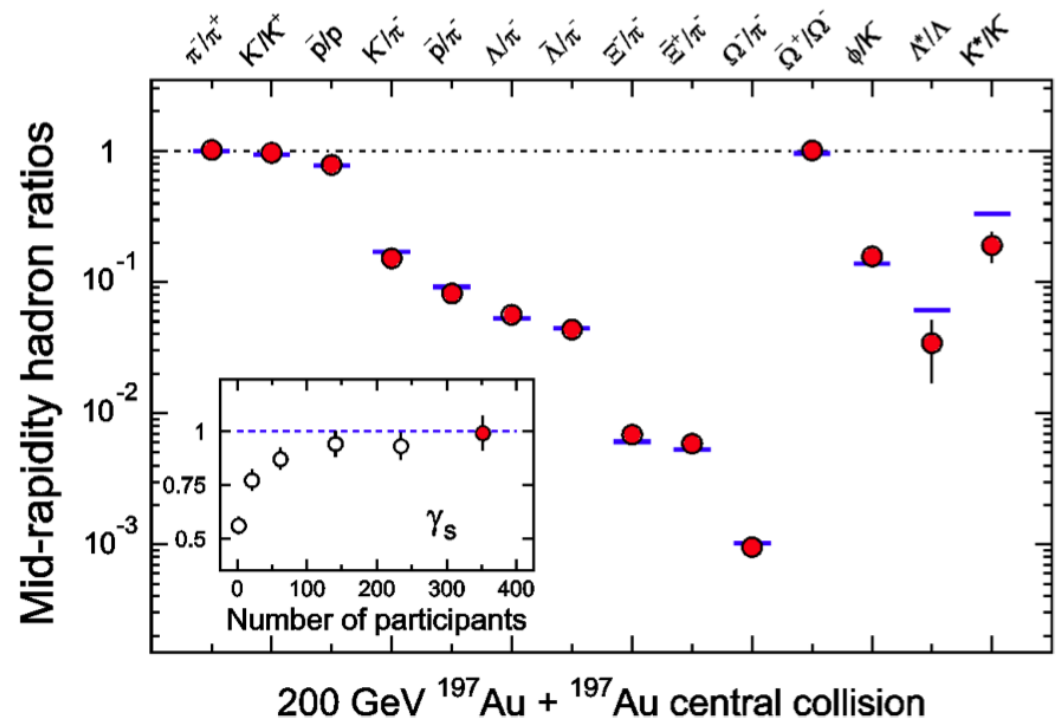
*Assume:* Ideal hadron resonance gas thermally and chemically **equilibrated**

*Input:* measured particle ratios

$$\frac{\bar{p}}{p} = \frac{e^{-(E+\mu)/T}}{e^{-(E-\mu)/T}} = e^{-2\mu/T}$$

*Output:*  $T = 163 \pm 4 \text{ MeV}$ ,  
 $\mu_B = 24 \pm 4 \text{ MeV}$

STAR Collaboration / Nuclear Physics A 757 (2005) 102–183



# The Limits of Thermodynamics

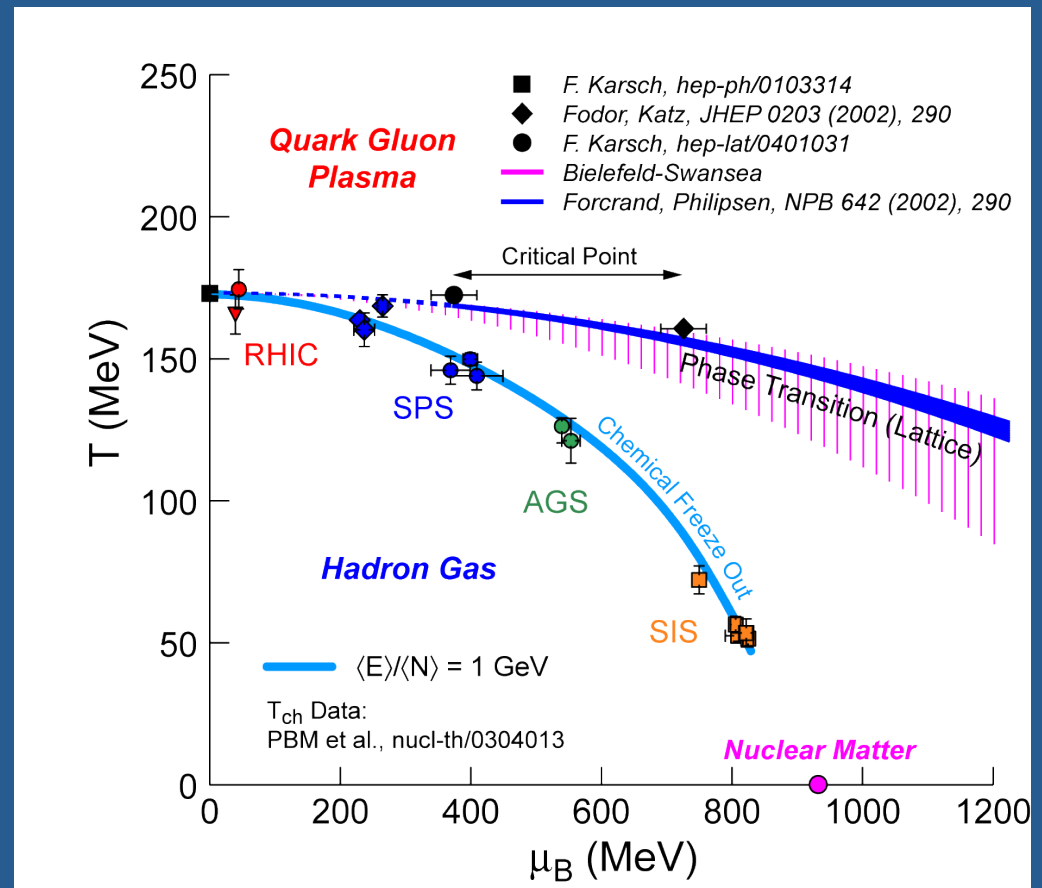
- This exercise in “hadro-chemistry”

- Applies to final-state (ordinary) hadrons
- Does not (necessarily) indicate

- QGP formation
- De-confinement
- New state of matter

- A smooth continuation of trends seen

- at lower energies
- in p-p, even  $e^+e^-$

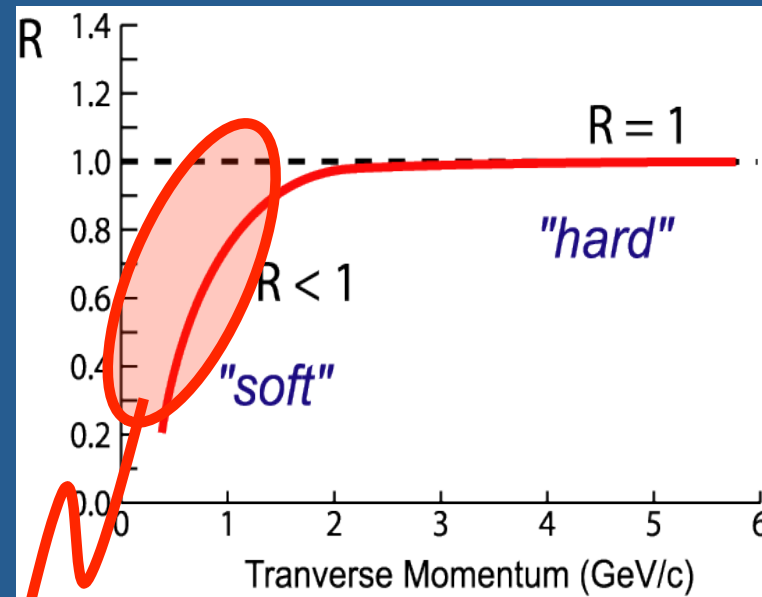


# Systematizing Our Expectations: Compare with p+p

- Describe in terms of *scaled ratio*  $R_{AA}$

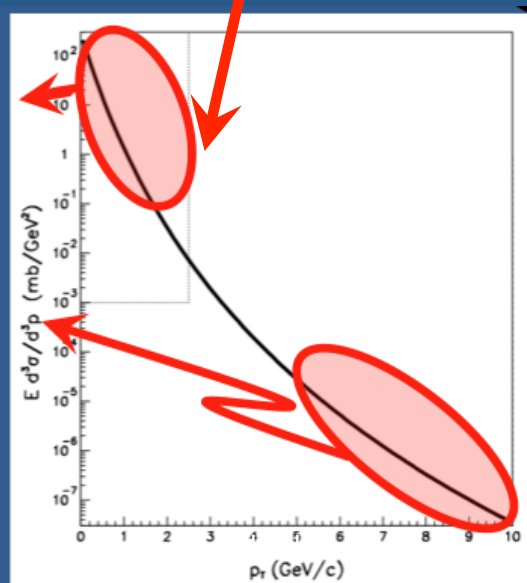
$$\equiv \frac{\text{Yield in Au + Au Events}}{N_{Bin} (\text{Yield in p+p Events})}$$

= 1 for “baseline expectations”



Answer is a function of  $p_T$ :

- Low  $p_T$   $\Rightarrow$  large cross sections  $\Rightarrow$  yield  $\sim N_{part}$ 
  - Soft, non-perturbative, “wounded nucleons”, ...
- High  $p_T$   $\Rightarrow$  small cross sections  $\Rightarrow$  yield  $\sim N_{Bin}$ 
  - Hard, perturbative, “binary scaling”, point-like,  $A*B$ , ...



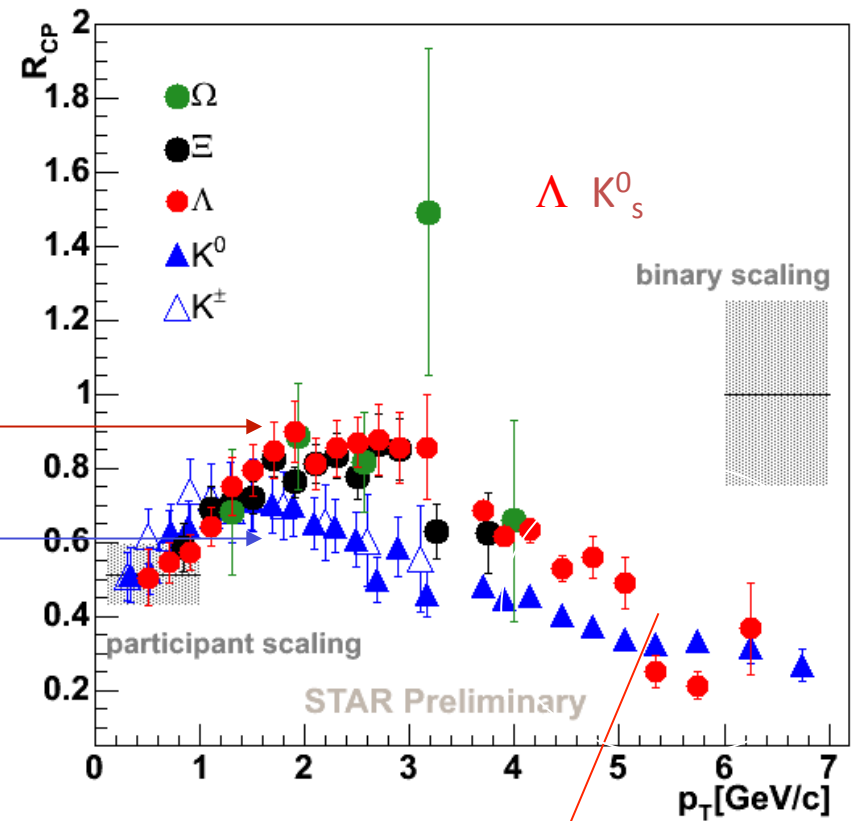


# Nuclear Modification Factors $R_{cp}$

$$R_{CP}^h(p_T) = \frac{\frac{dN_h}{dp_T} \frac{1}{\langle N_{Coll} \rangle} (central)}{\frac{dN_h}{dp_T} \frac{1}{\langle N_{Coll} \rangle} (peripheral)}$$

Baryons

Mesons



The 'quenching' of high pt particles due to partonic energy loss. (Lecture 2)

# Parton recombination at intermediate $p_T$

- in vacuo fragmentation of a high momentum quark to produce hadrons competes with in medium recombination of lower momentum quarks to produce hadrons

- 6 GeV/c particle via :  
fragmentation from high  $p_T$

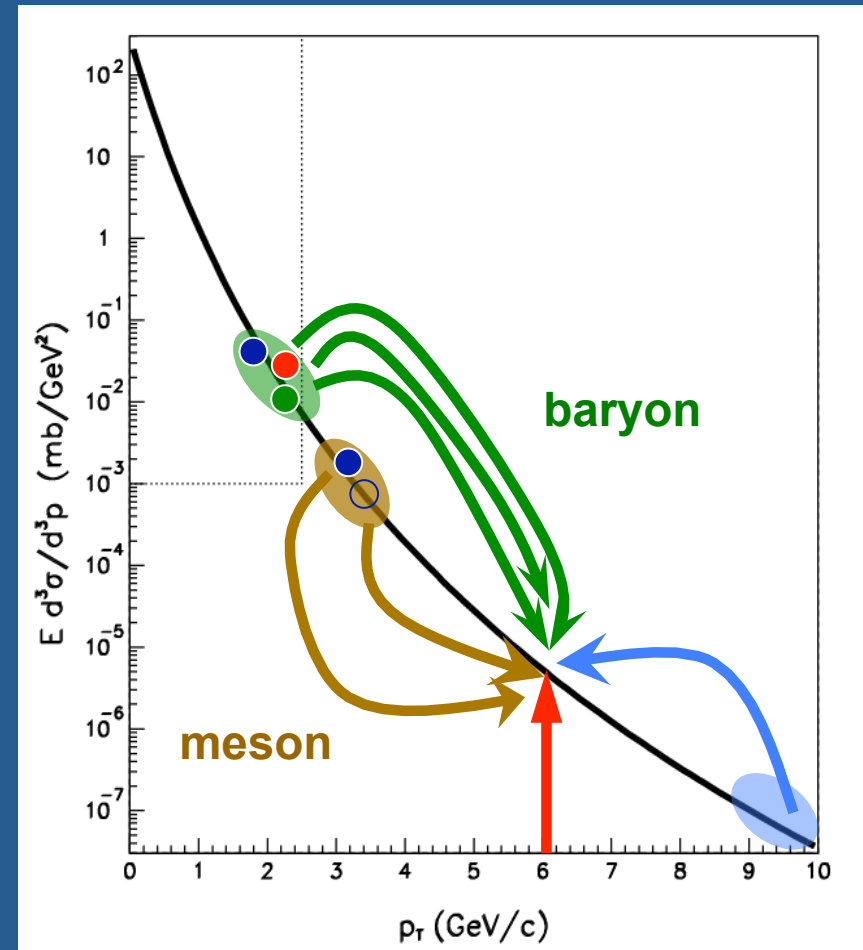
meson

- 2 quarks at  $p_T \sim 3$  GeV/c

baryon

- 3 quarks at  $p_T \sim 2$  GeV/c

Recombination produces more baryons than mesons at intermediate  $p_T$



*R.J. Fries et al., PRL 90 (202303) 2003*  
*V. Greco et al., PRL 90 (202302) 2003*

Quarks Degrees of freedom

# Bulk Behaviour

Energy is deposited in small volume.

~ size of Lorentz-contracted nuclear overlap.

→ Leads to formation of transient state.

State undergoes **hydrodynamical expansion**.

System cools down while expanding. →

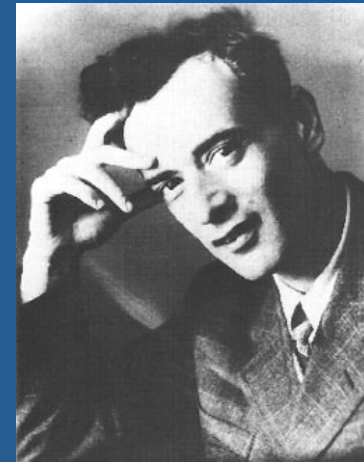
Reaches a **freeze out temperature**.  $T_f \sim m_\pi$

Below  $T_f$ , hadrons become free particles.



Sevil Salur

Landau



# Hydrodynamics:

**Assume:** local thermal equilibrium (zero mean-free-path limit)

**Solve:** equations of motion for fluid elements (not particles)

## Hydrodynamic Equations

$$\partial_\mu T^{\mu\nu} = 0, \quad \text{Energy-momentum conservation}$$

$$\partial_\mu n_i^\mu = 0 \quad \text{Charge conservations (baryon, strangeness, etc...)}$$

For perfect fluids (neglecting viscosity!),

$$T^{\mu\nu} = (e + P)u^\mu u^\nu - P g^{\mu\nu}$$

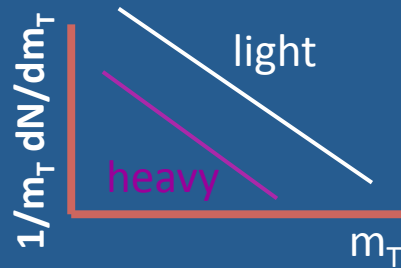
Energy density      Pressure      4-velocity

Within ideal hydrodynamics, pressure gradient  $dP/dx$  is the driving force of collective flow.

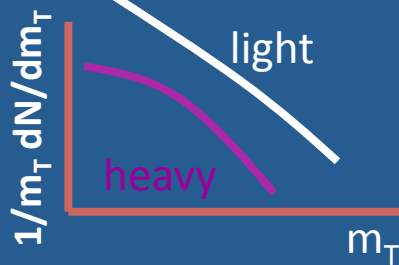
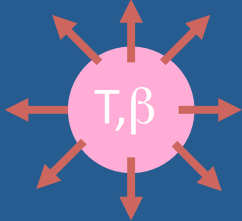
# Strong Collective Radial Expansion

Different spectral shapes for particles of differing mass  
 → strong collective radial flow

purely thermal source

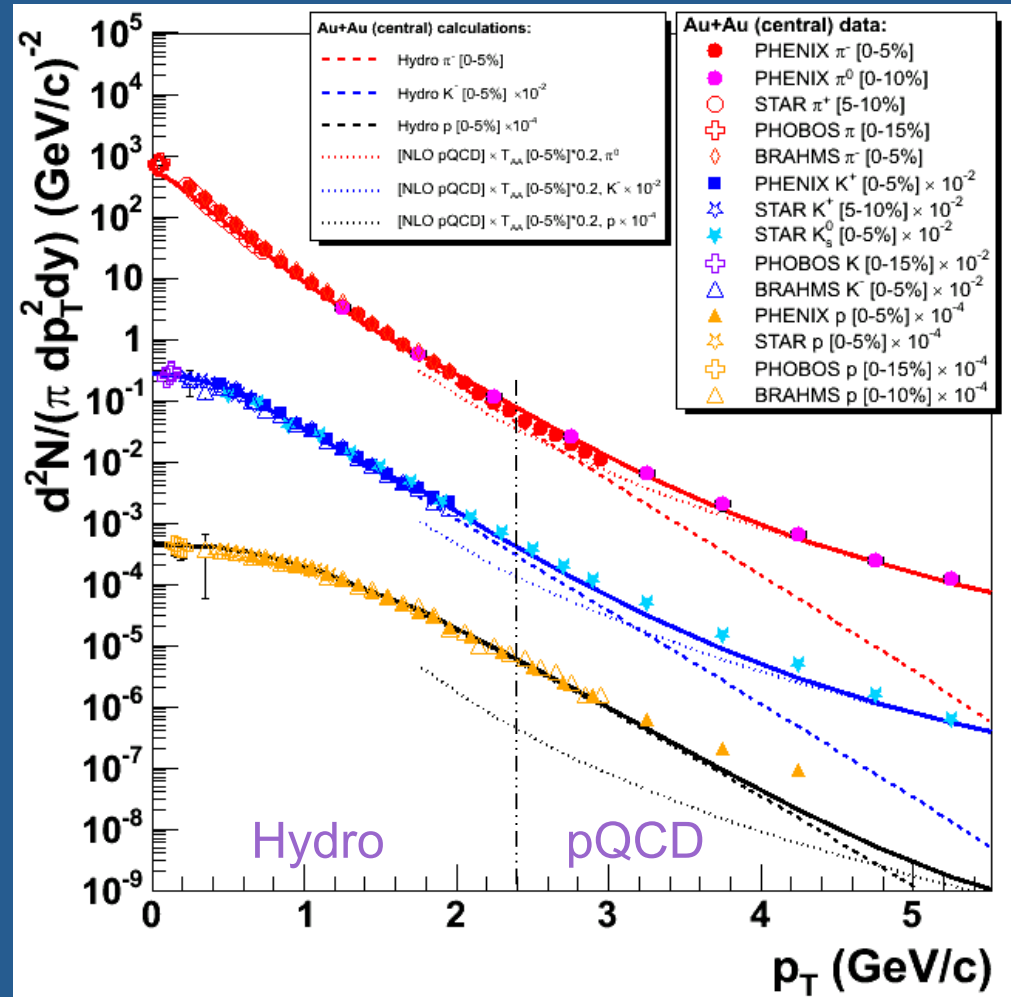


explosive source



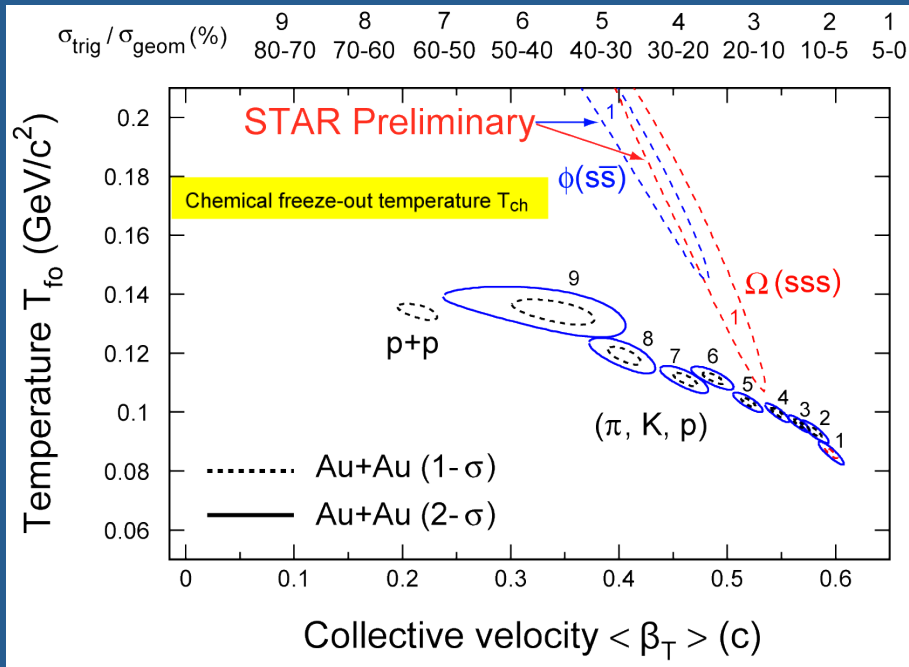
$$m_T = (p_T^2 + m^2)^{1/2}$$

Au+Au central,  $\sqrt{s} = 200$  GeV



$T_{fo} \sim 100$  MeV &  $\langle \beta_T \rangle \sim 0.55 c$

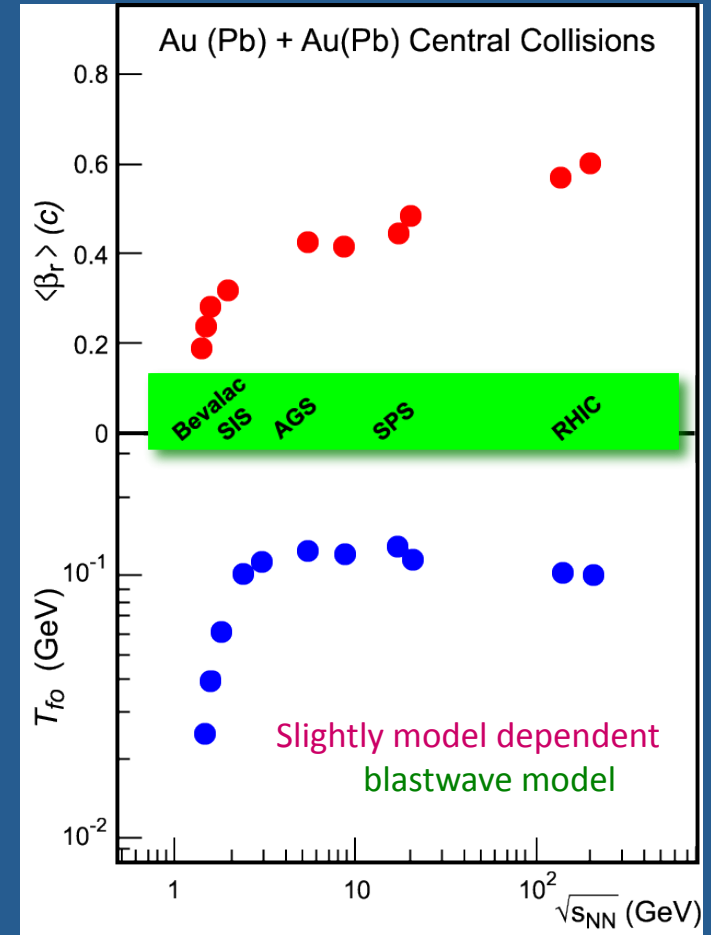
# Kinetic Freeze-Out @ 200 GeV



Strong collective radial expansion

⇒ high pressure

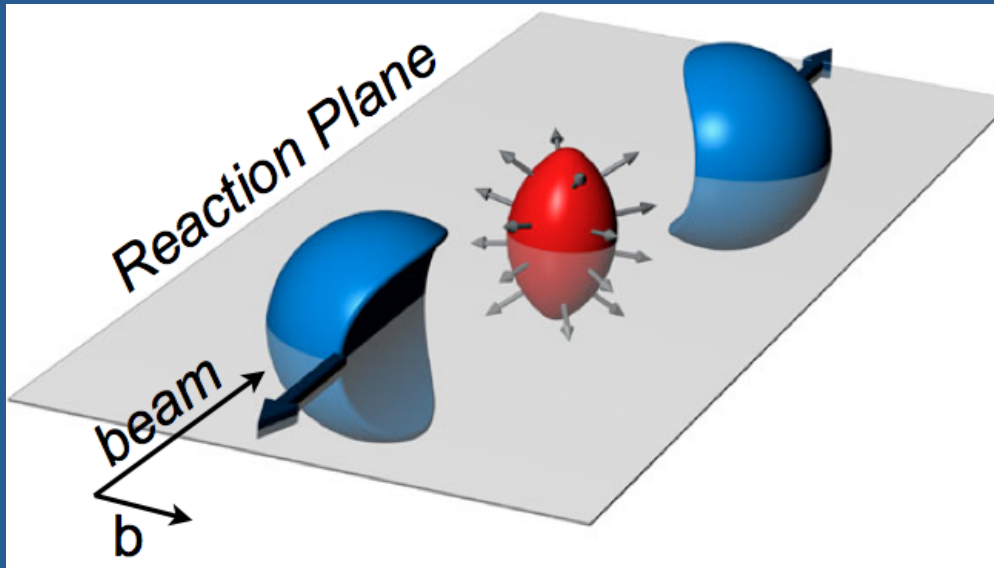
⇒ high rescattering rate



Radial flow  $\beta_T$ : increases with  $\sqrt{s}$  and centrality

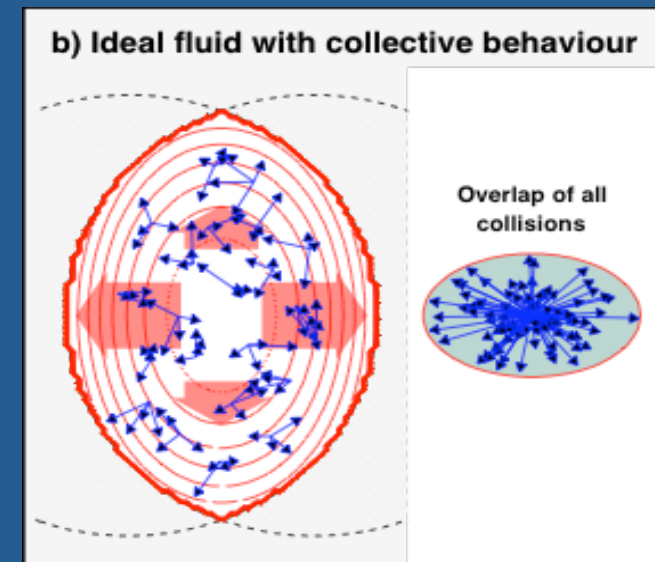
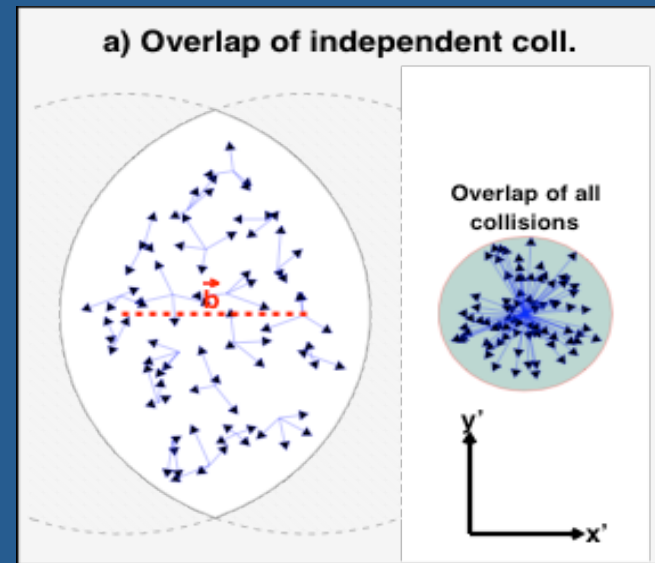
Freeze-out Temperature  $T_{fo}$ : decreases with centrality, constant in  $\sqrt{s}$   
(bigger systems freeze out later)

# Utilize Azimuthal Anisotropy

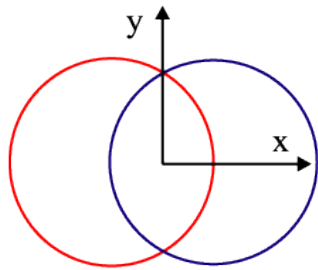


Expansion is driven by a gradient of pressure

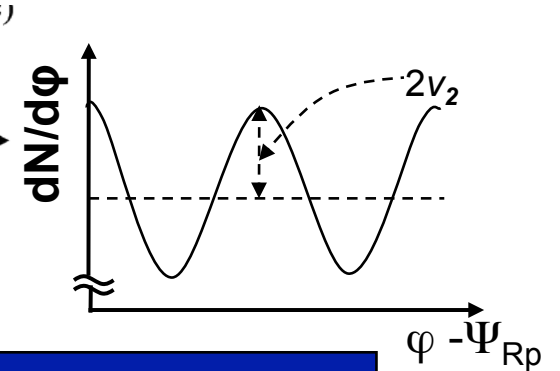
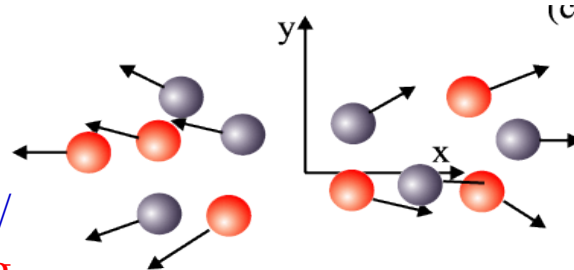
There is a preferential direction for particle emission (Anisotropy in momentum space)



# Azimuthal Anisotropy of Emission: Elliptic Flow



Interactions/  
Rescattering



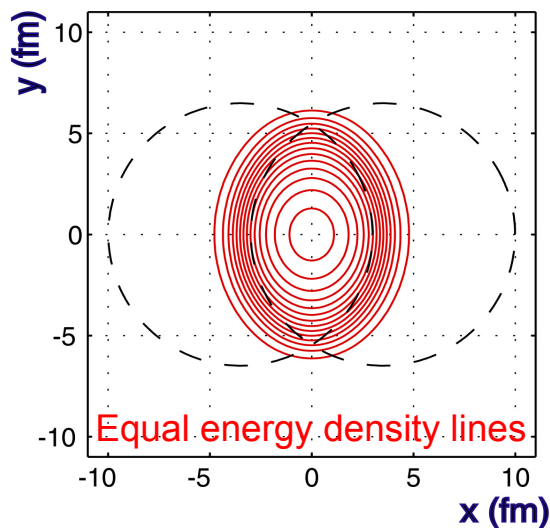
Almond shape overlap

Anisotropy in

Elliptic flow observable sensitive to early evolution of system

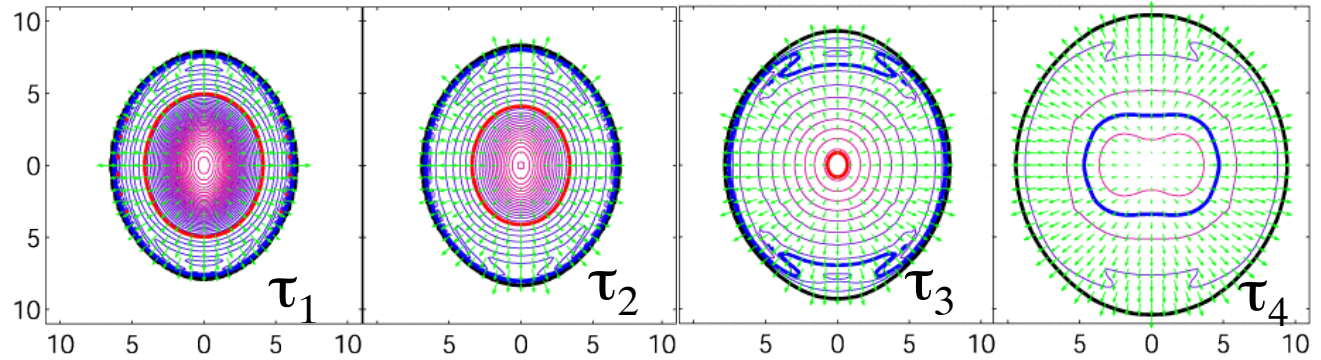
Large  $v_2$  is an indication of *early* thermalization

$v_2$ : 2<sup>nd</sup> harmonic Fourier coefficient in  $dN/d\phi$  with respect to the reaction plane



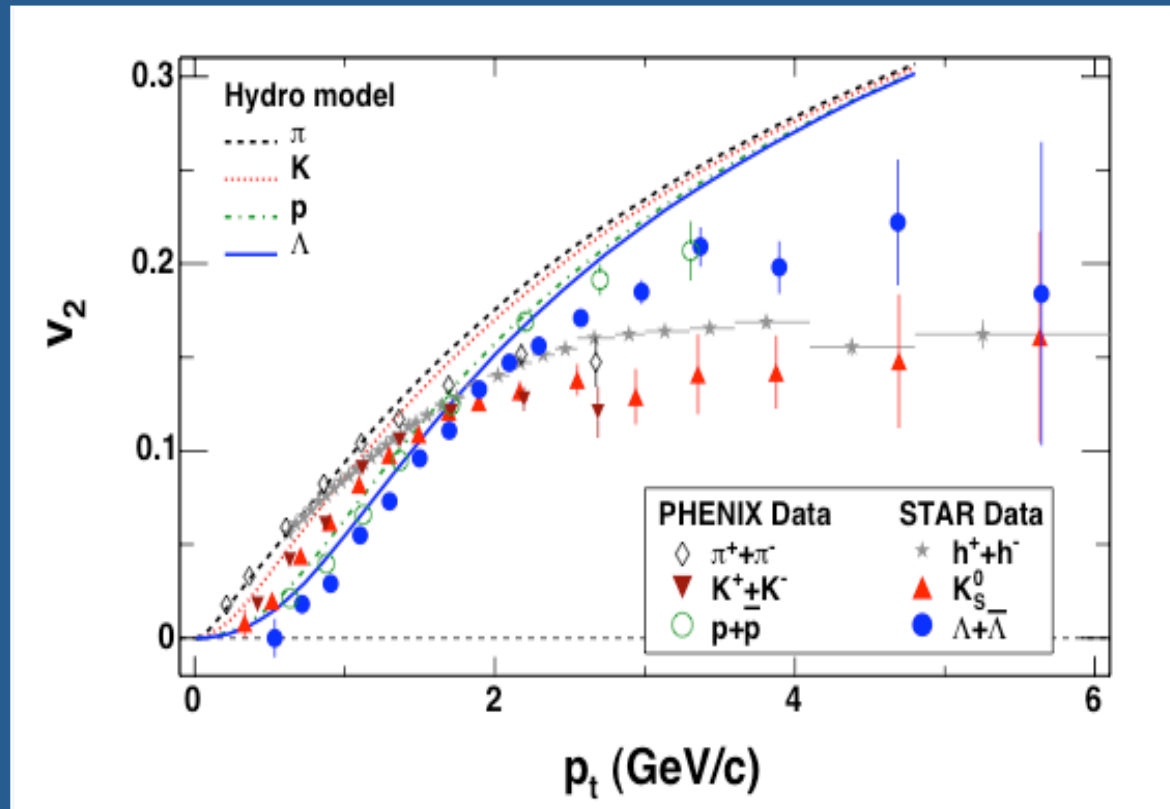
Au+Au at  $b=7$  fm

P. Kolb, J. Sollfrank, and U. Heinz





# Flows like a liquid



Phys. Rev. C 72 (2005) 014904

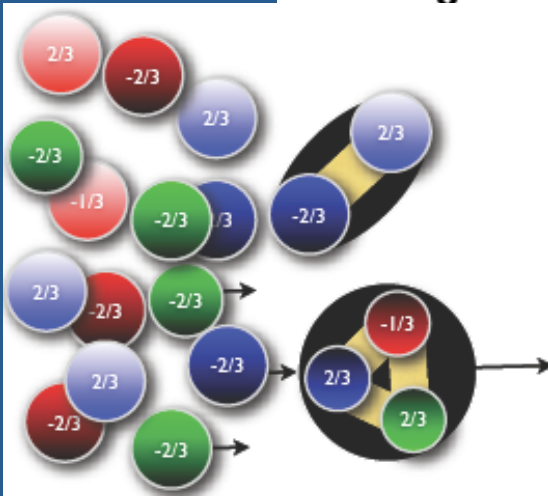
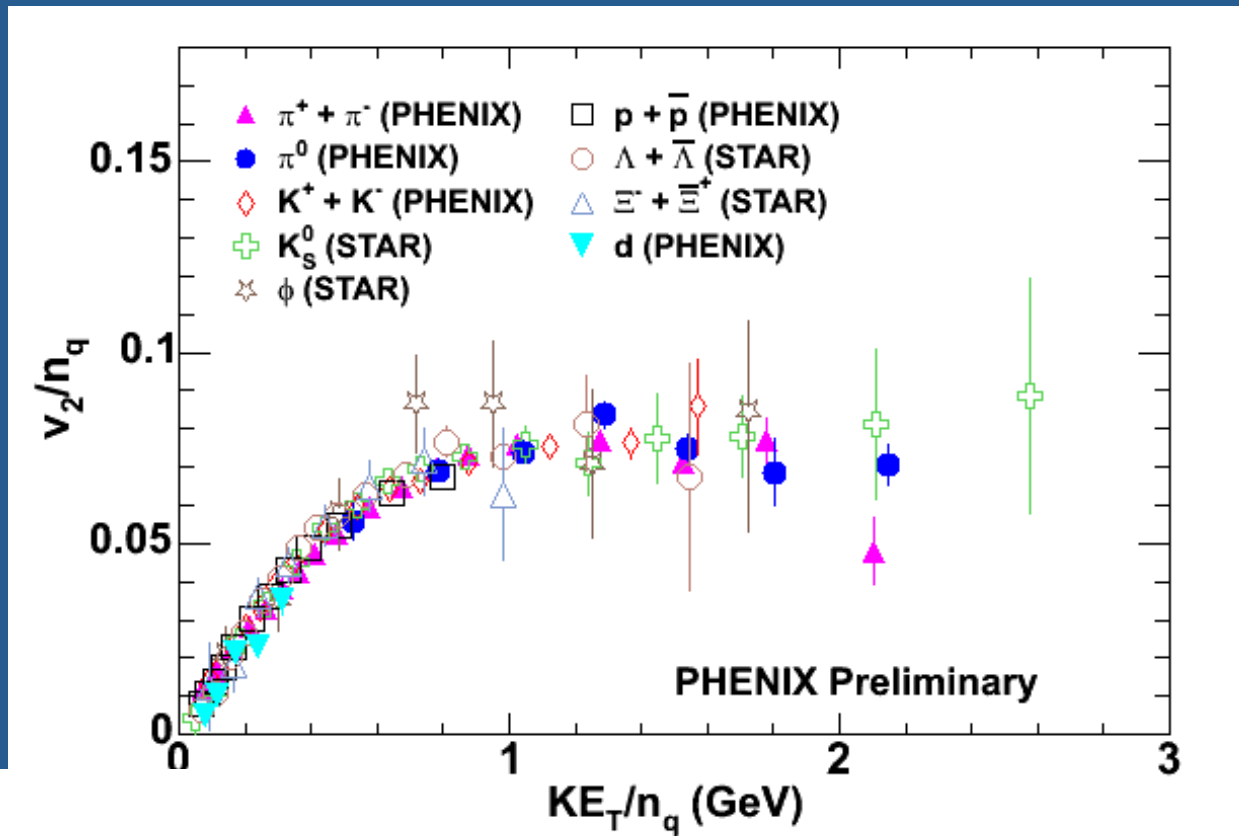
Hydrodynamical models describe data well for  $p_T (< 2.5 \text{ GeV}/c)$

$$v_2(\pi) > v_2(K) > v_2(p) \sim v_2(\Lambda)$$

⇒ compatible with early equilibration

Strongly suggests that this is *not* just a superposition of p+p collisions

# Quarks Flow



Phys. Rev. C 72 (2005) 014904

Phys. Rev. Lett. 95 (2005) 122301

D. Molnar, S.A. Voloshin Phys. Rev. Lett. 91, 092301 (2003)

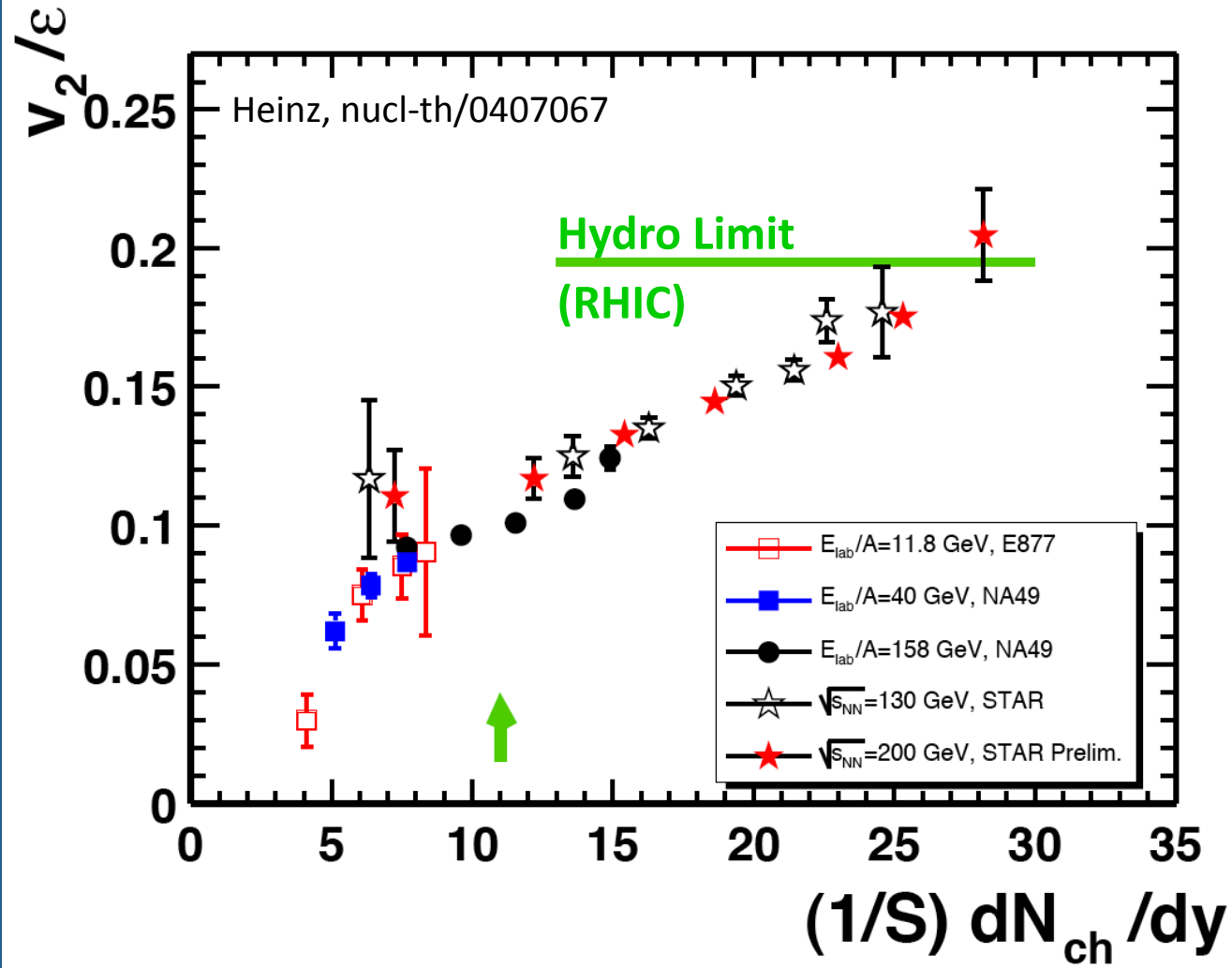
V. Greco, C.M. Ko, P. Levai Phys. Rev. C68, 034904 (2003)

R.J. Fries, B. Muller, C. Nonaka, S.A. Bass Phys. Rev. C68, 044902 (2003)

Z. Lin, C.M. Ko Phys. Rev. Lett. 89, 202302 (2002)

*implication: valence quarks, not hadrons, are relevant  
pressure builds early, dressed quarks are born of flowing field*

# Hydro Limits: Like a Perfect Liquid?

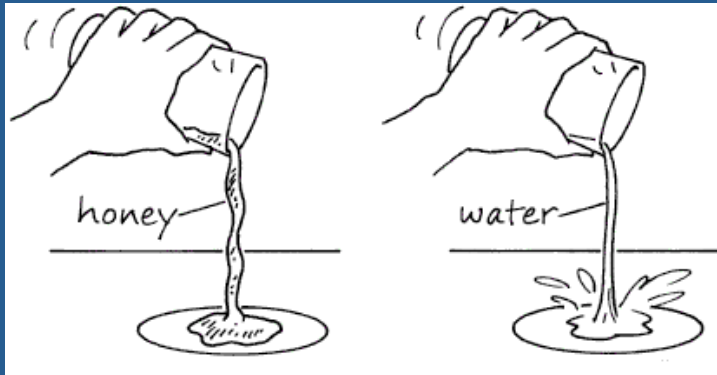


hydro- dynamics **without any viscosity** describes heavy ion reactions: Thermalization time  $\tau = 0.6$  fm/c, Energy Density:  $\epsilon=20$  GeV/fm<sup>3</sup>

$$\epsilon = \text{spatial eccentricity} = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$

S=overlap area

## Small Viscosity:



Viscosity describes a fluid's internal resistance to flow - inability to transport momentum & sustain a wave

Viscosity/entropy ( $\eta/s$ )  $\sim 1/4\pi$  limit  
→ liquid at RHIC is “perfect” !

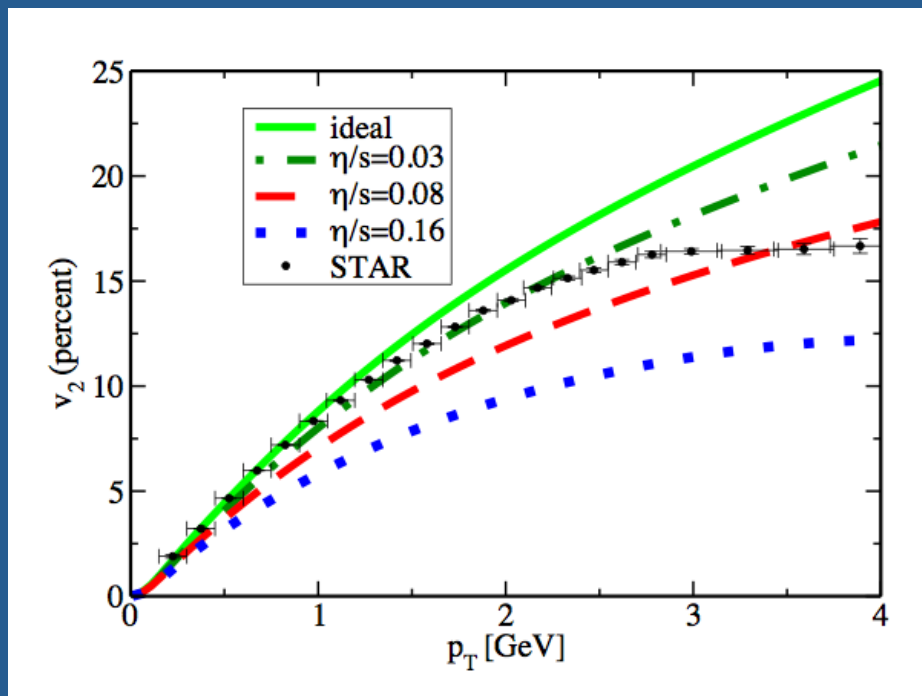
Good momentum transport:  
neighboring fluid elements “talk” to each other

Can we do better? How to quantify?

- Use hydrodynamics
- Set initial energy density to reproduce observed particle multiplicity
- Use various values of  $\eta/s$
- Constrain with data



# Viscous hydrodynamics & RHIC data



P. Romatschke et al.  
Phys. Rev. Lett. 99:172301 (2007)

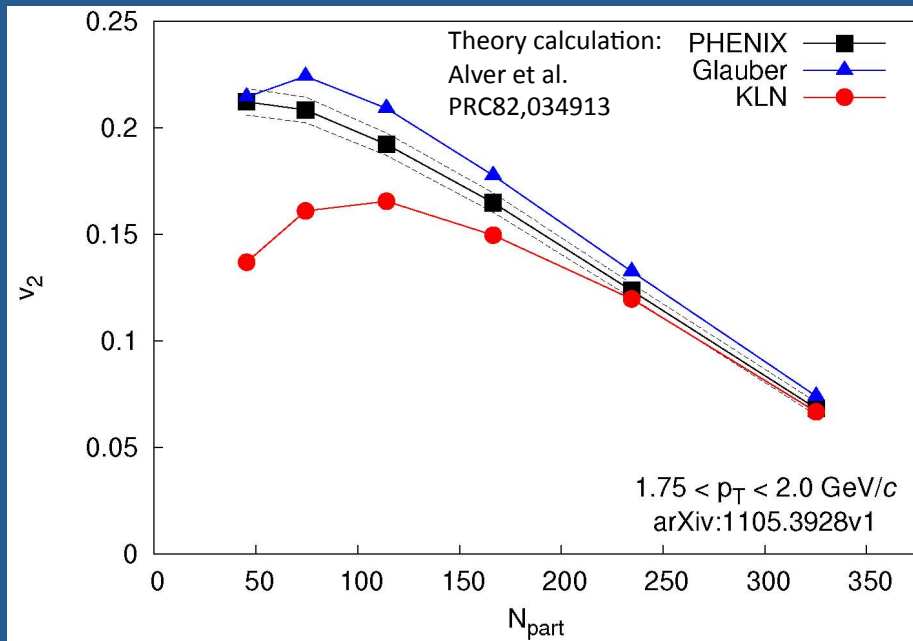
minimum bias  $v_2$  seems to favor  $\eta/s \simeq 0.03$ , at least at low momenta, where hydrodynamics is supposed to be most applicable. Note that this result could change drastically if the minimum bias data were decreased by 20%, which is the estimated systematic error quoted in [25].

There are, however, a number of caveats that should be considered before taking the above numbers literally. Firstly, we have only considered Glauber-type initial conditions, and assumed  $\Pi^{\mu\nu}(\tau_0) = 0$ . It has been suggested that CGC-type initial conditions lead to larger overall  $v_2$  [33] which in turn would raise the allowed values for  $\eta/s$  in our calculation. This is due to the larger eccentricities in this model [34] (note the issues raised in [35]). How-

Caveats: Details of hydro code, Viscous correction, Initial conditions, freezeout particle mix,  
What is  $\eta/s$ ?

# Viscous hydrodynamics & RHIC data

2 models with: Different fluctuations, Eccentricity,  $\rho$  distribution

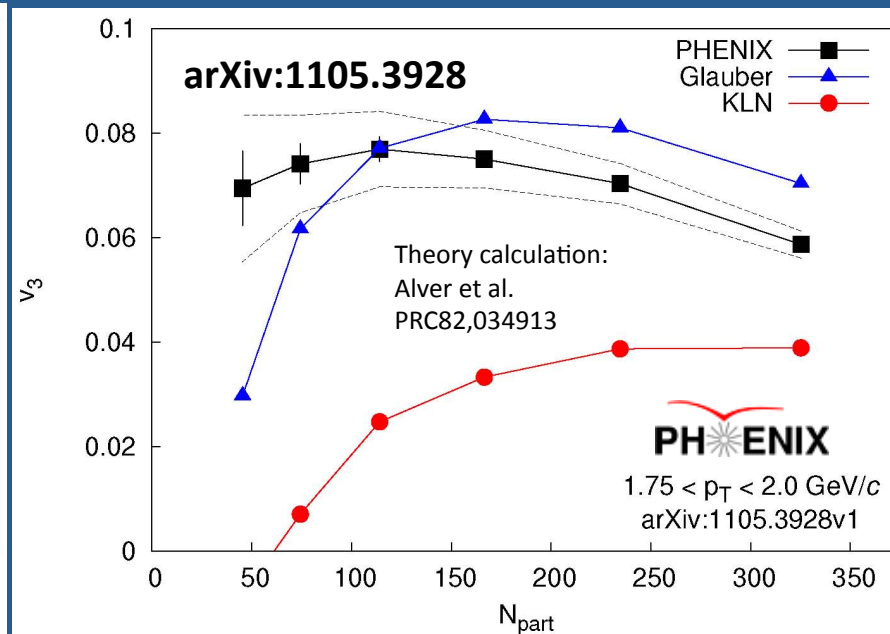
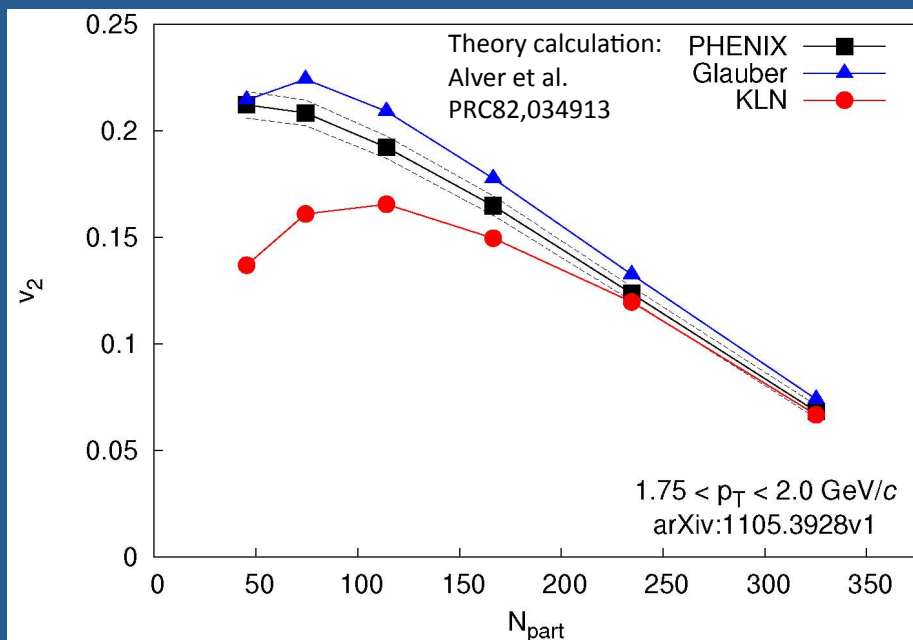


$v_2$  described by both Glauber and CGC  
*but different values of  $\eta/s$*

Lappi, Venugopalan, PRC74, 054905  
Drescher, Nara, PRC76, 041903

# Viscous hydrodynamics & RHIC data

2 models with: Different fluctuations, Eccentricity,  $\rho$  distribution



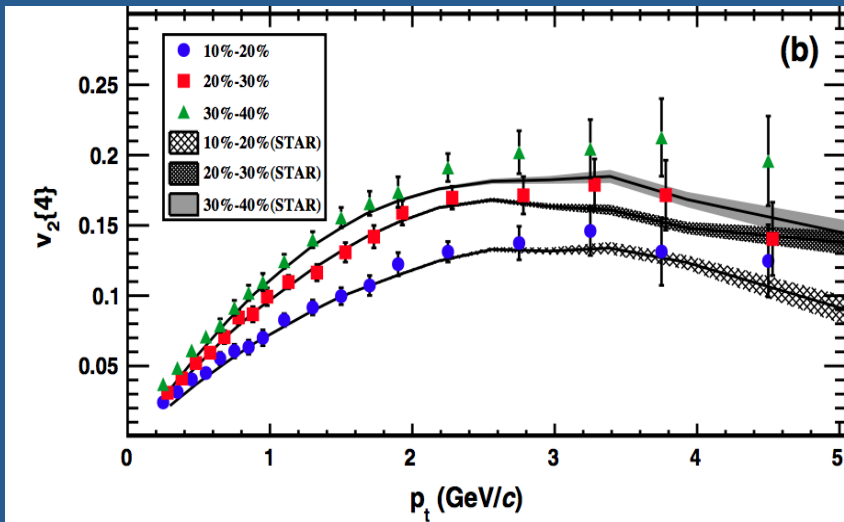
$v_2$  described by both Glauber and CGC  
but different values of  $\eta/s$

$v_3$  described only by Glauber  
breaks degeneracy

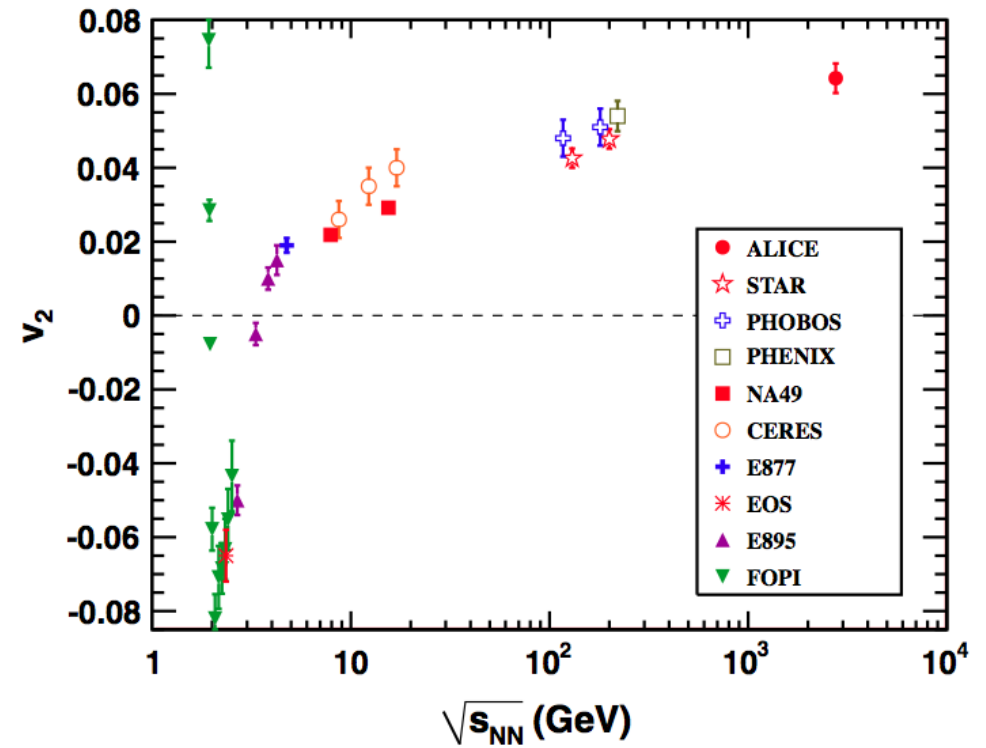
Lappi, Venugopalan, PRC74, 054905  
Drescher, Nara, PRC76, 041903

Initial conditions & hydro details are still on the works!

# Hydrodynamics at LHC



Pb+Pb at LHC flows similarly



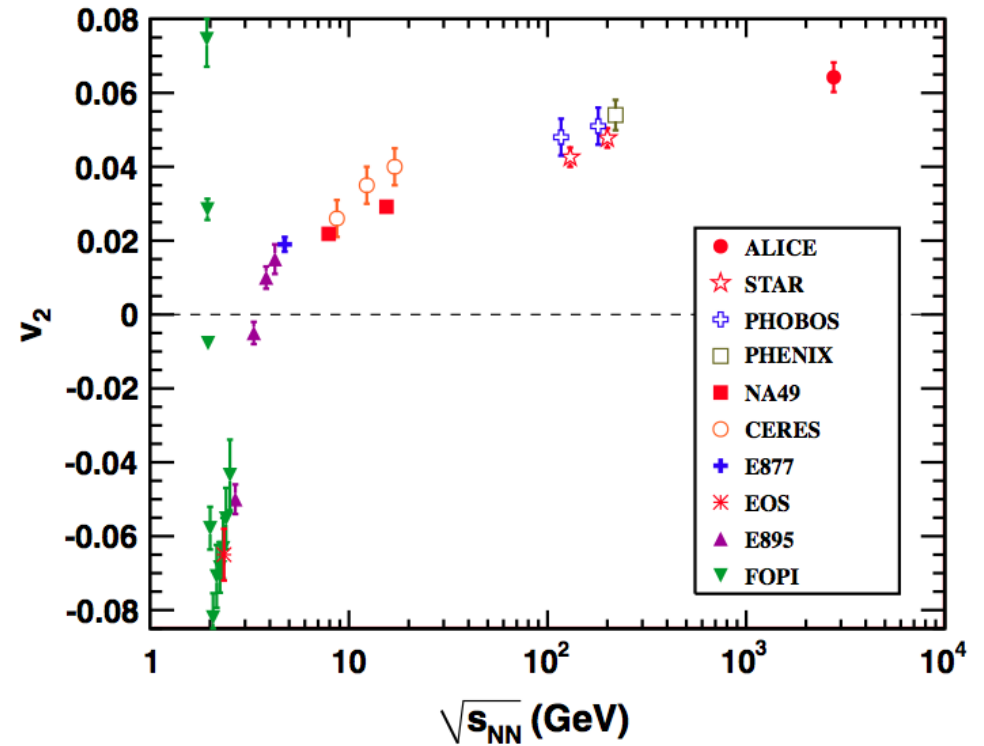
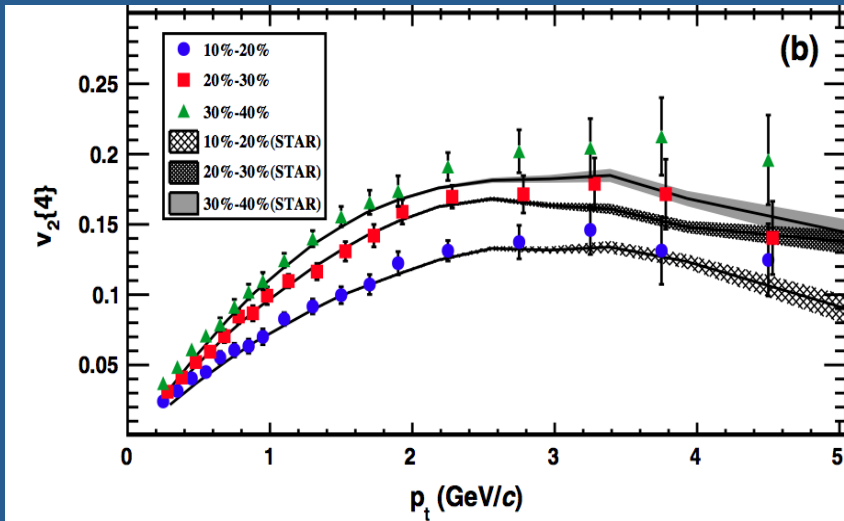
the integrated elliptic flow increases 30%  
(caused by the increase in the mean  $p_t$ )

ALICE Phys. Rev. Lett. 105, 252302 (2010)

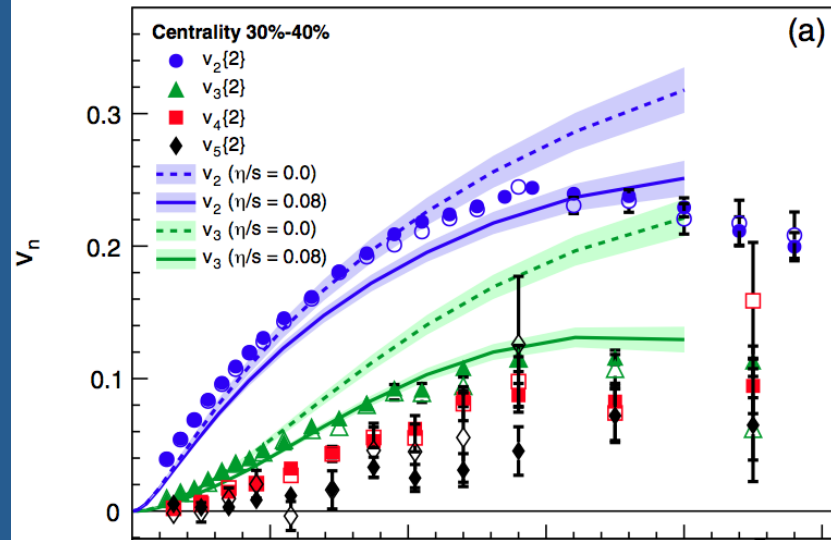
PRL 107, 032301 (2011)



# Hydrodynamics at LHC



Pb+Pb at LHC flows similarly



the integrated elliptic flow increases 30%  
(caused by the increase in the mean  $p_t$ )

ALICE Phys. Rev. Lett. 105, 252302 (2010)

PRL 107, 032301 (2011)

Favors a small value of Viscosity/entropy ( $\eta/s$ )

# Last 10 Years of Discoveries

- **Collective Flow:**
  - behaves more like liquid rather than gas.
  - small viscosity perfect liquid.
- **Particle Production:**
  - recombination/ coalescence dominates over fragmentation at medium  $p_T$
- **Jet Quenching:**
  - opaque to fast partons

