

# Theory and phenomenology of CP violation

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# Outline

## **1. Present status of CP-violation**

## **2. Searches for CP-violation**

- LBL experiments**
- Neutrinoless double beta decay**

## **3. Leptogenesis**

## **4. Is there a connection between low energy CPV and leptogenesis?**

## **5. Conclusions**

# CP-violation in the leptonic sector

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_{21}/2} & 0 \\ 0 & 0 & e^{i\alpha_{31}/2} \end{pmatrix}$$

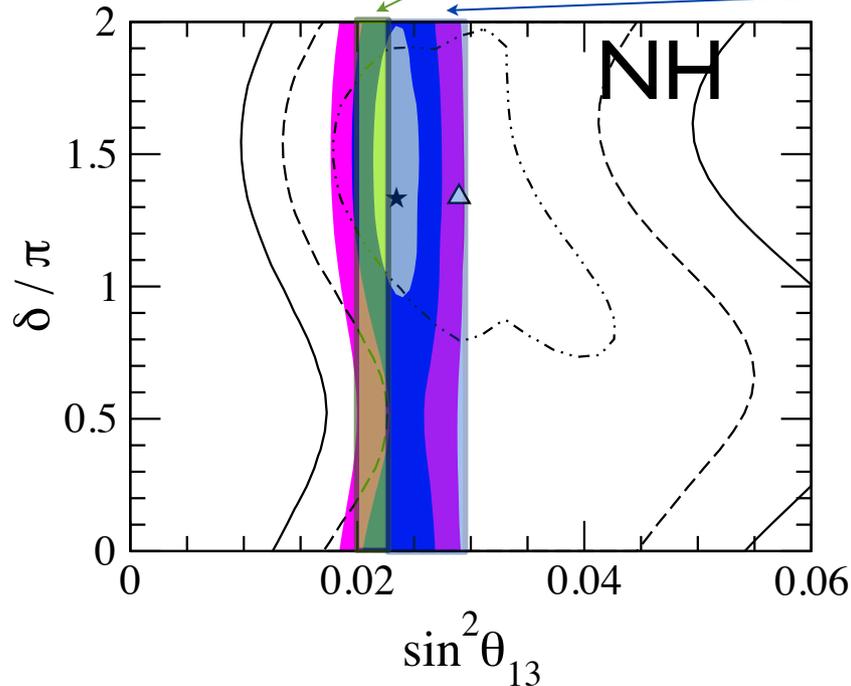
For antineutrinos,

$$U \rightarrow U^*$$

**CP-conservation** requires

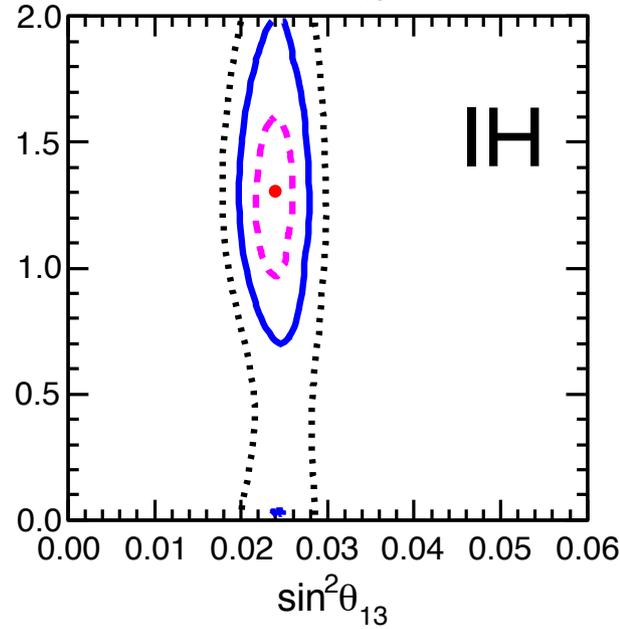
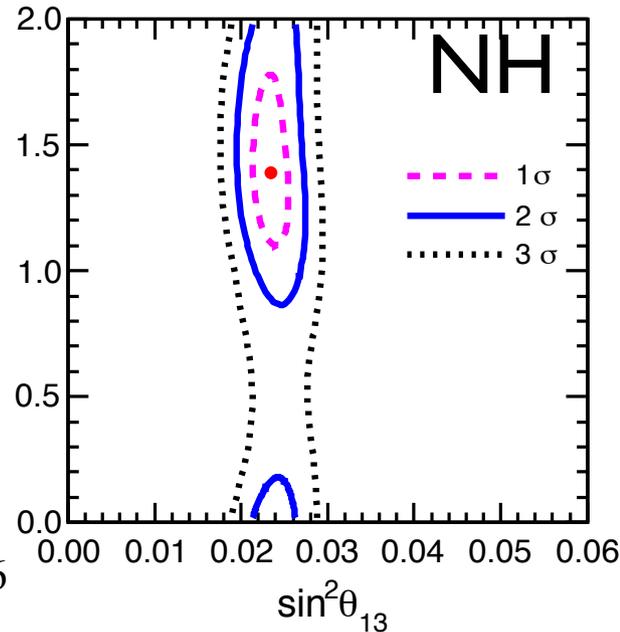
$$U \text{ is real} \Rightarrow \delta = 0, \pi$$

The delta phase can be tested in neutrino oscillations.  
The Majorana phases can enter only LNV processes and are currently completely unknown.

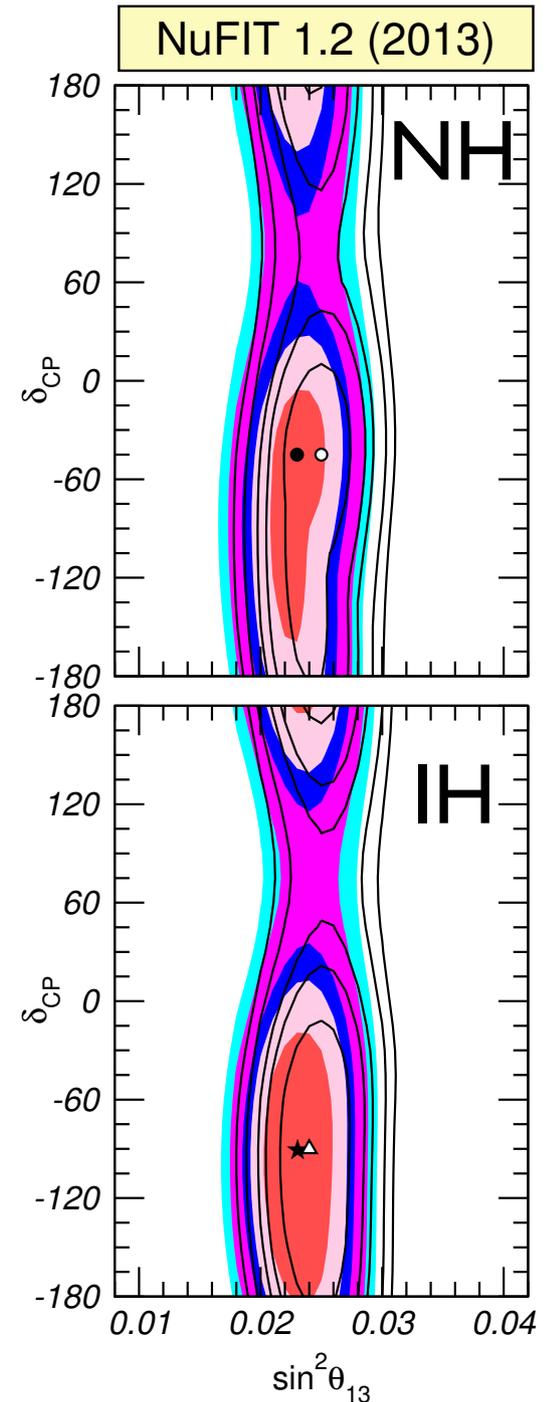


D.V. Forero et al., 1405.7540

There is a slight preference for CP-violation, which is mainly due to the combination of T2K and reactor neutrino data.



F. Capozzi et al., 1312.2878



NuFit: M. C. Gonzalez-Garcia et al., 1209.3023

**How can we search for  
leptonic CP-violation?**

# How can we search for leptonic CP-violation?

- Long baseline neutrino experiments
- (Atmospheric neutrinos)
- Neutrinoless double beta decay

# CP-violation in LBL experiments

CP-violation will manifest itself in neutrino oscillations, due to the delta phase. The CP-asymmetry:

$$P(\nu_\mu \rightarrow \nu_e; t) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e; t) =$$
$$= 4s_{12}c_{12}s_{13}c_{13}^2s_{23}c_{23}\sin\delta \left[ \sin\left(\frac{\Delta m_{21}^2 L}{2E}\right) + \sin\left(\frac{\Delta m_{23}^2 L}{2E}\right) + \sin\left(\frac{\Delta m_{31}^2 L}{2E}\right) \right]$$

- CP-violation requires all angles to be nonzero.
- It is proportional to the sine of the delta phase.
- If one can neglects  $\Delta m_{21}^2$ , the asymmetry goes to zero: effective 2-neutrino probabilities are CP-symmetric.

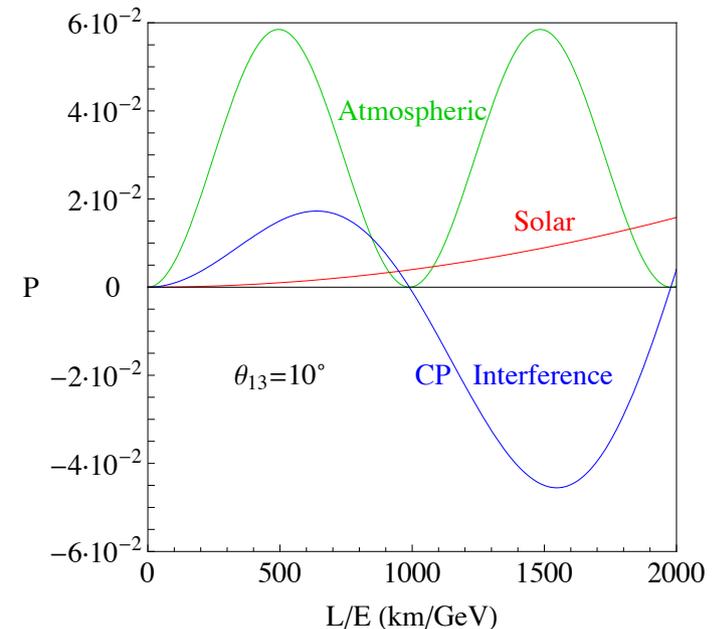
CPV needs to be searched for in **long baseline neutrino experiments** which have access to 3-neutrino oscillations.

$$\begin{aligned}
 P_{\mu e} \simeq & 4c_{23}^2 s_{13}^2 \frac{1}{(1-r_A)^2} \sin^2 \frac{(1-r_A)\Delta_{31}L}{4E} \\
 & + \sin 2\theta_{12} \sin 2\theta_{23} s_{13} \frac{\Delta_{21}L}{2E} \sin \frac{(1-r_A)\Delta_{31}L}{4E} \cos \left( \delta - \frac{\Delta_{31}L}{4E} \right) \\
 & + s_{23}^2 \sin^2 2\theta_{12} \frac{\Delta_{21}^2 L^2}{16E^2} - 4c_{23}^2 s_{13}^4 \sin^2 \frac{(1-r_A)\Delta_{31}L}{4E}
 \end{aligned}$$

A. Cervera et al., hep-ph/0002108;  
 K. Asano, H. Minakata, I 103.4387;  
 S. K. Agarwalla et al., I 302.6773...

See also W. Winter's talk

- The CP asymmetry peaks for  $\sin^2 2\theta_{13} \sim 0.001$ . Large  $\theta_{13}$  makes its searches possible but not ideal.
- Crucial to know mass ordering.
- CPV effects more pronounced at low energy.

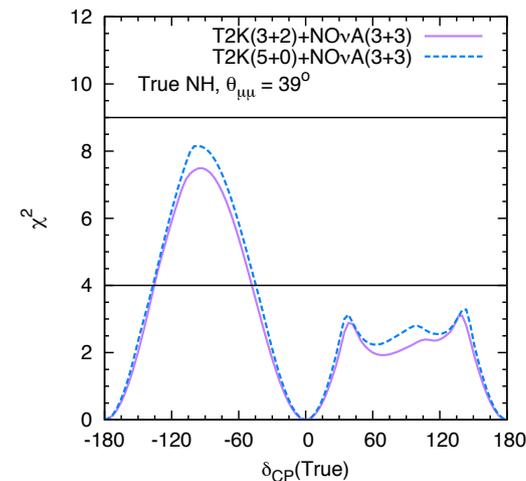
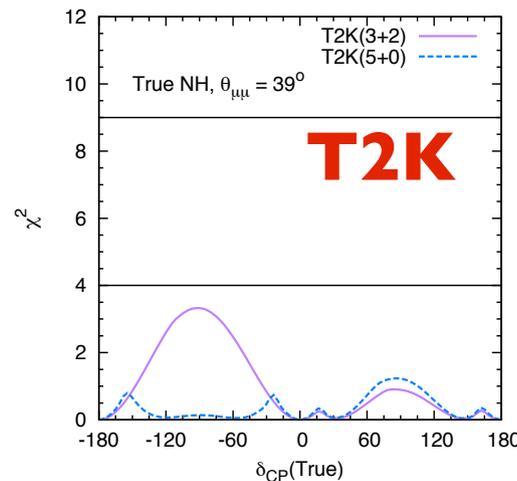
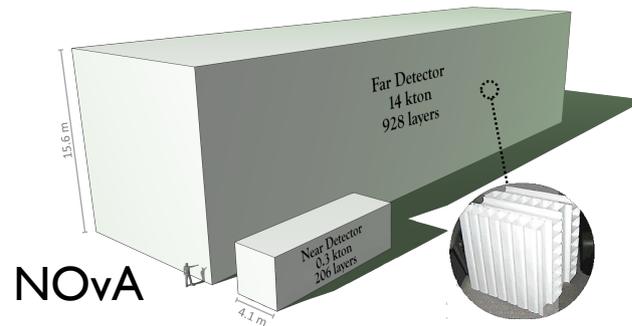
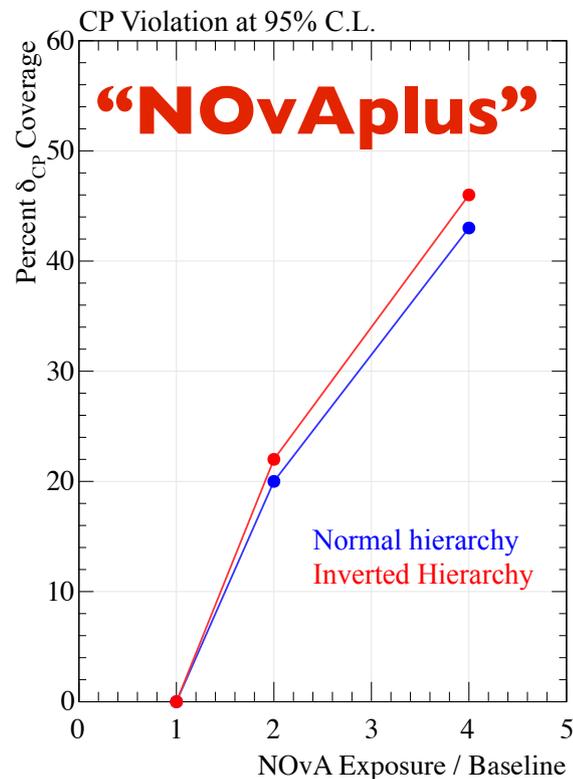
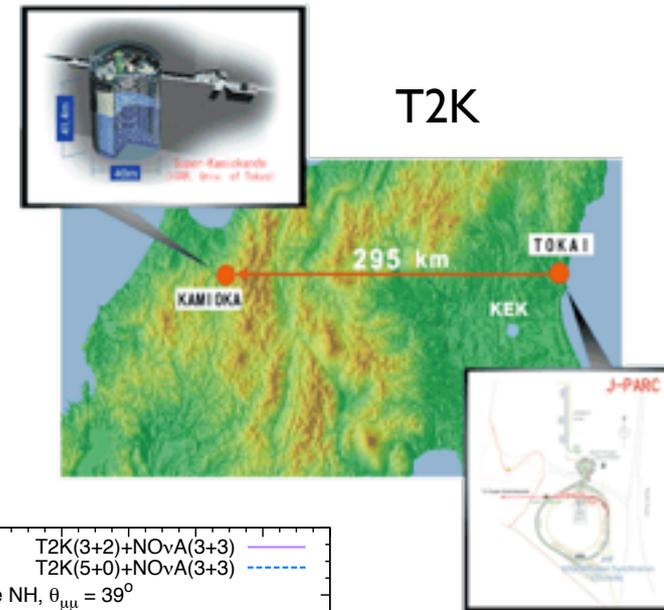


Category	Experiment	Status	Oscillation parameters
Accelerator	MINOS+ [74]	Data-taking	MH/CP/octant
Accelerator	T2K [21]	Data-taking	MH/CP/octant
Accelerator	NOvA [108]	Commissioning	MH/CP/octant
Accelerator	RADAR [76]	Design/ R&D	MH/CP/octant
Accelerator	CHIPS [75]	Design/ R&D	MH/CP/octant
Accelerator	LBNE [87]	Design/ R&D	MH/CP/octant
Accelerator	Hyper-K [97]	Design/ R&D	MH/CP/octant
Accelerator	LBNO [109]	Design/ R&D	MH/CP/octant
Accelerator	ESS $\nu$ SB [110]	Design/ R&D	MH/CP/octant
Accelerator	DAE $\delta$ ALUS [111]	Design/ R&D	CP

## CPV Searches

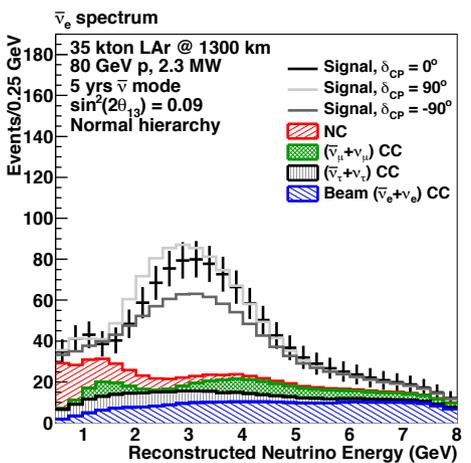
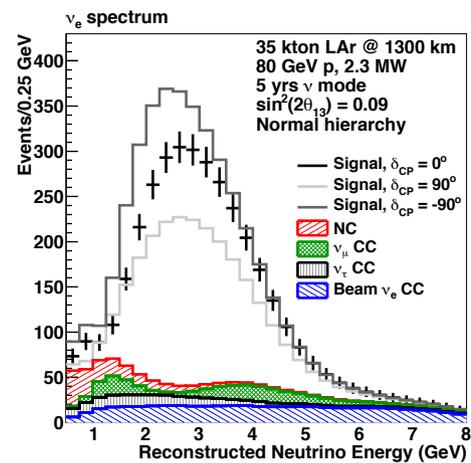
Near future: T2K and NOvA.  
Marginal sensitivity to CPV

WG Report: Neutrinos, de Gouvea (Convener) et al., I310.4340

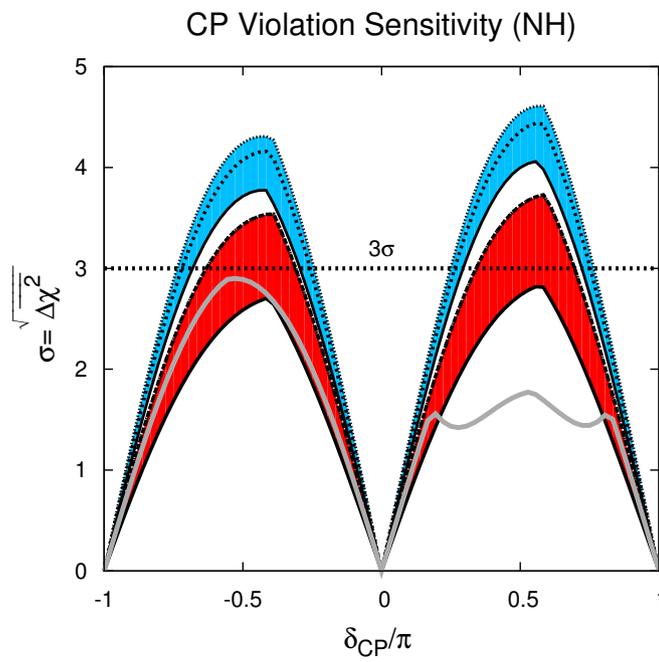


M. Gosh et al., I401.7243; see also Machado et al.; Huber et al.

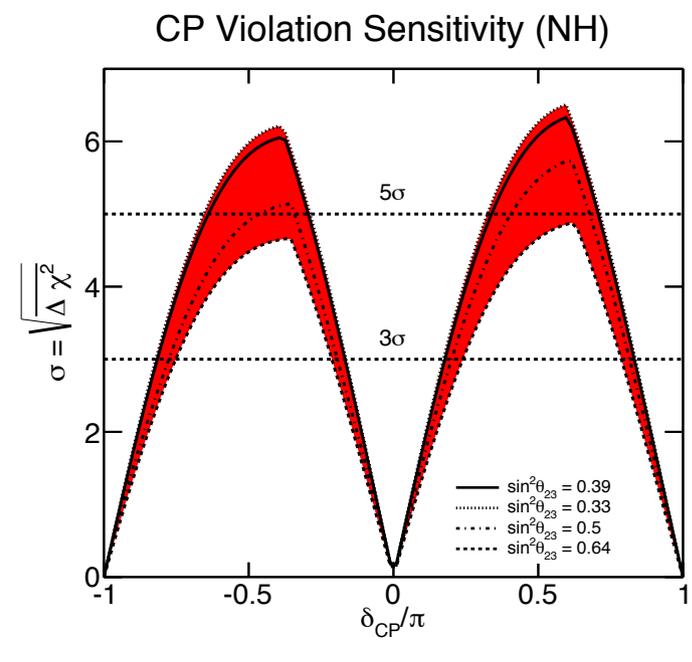
NOvA Coll., I308.0106



# LBNE-10Kton

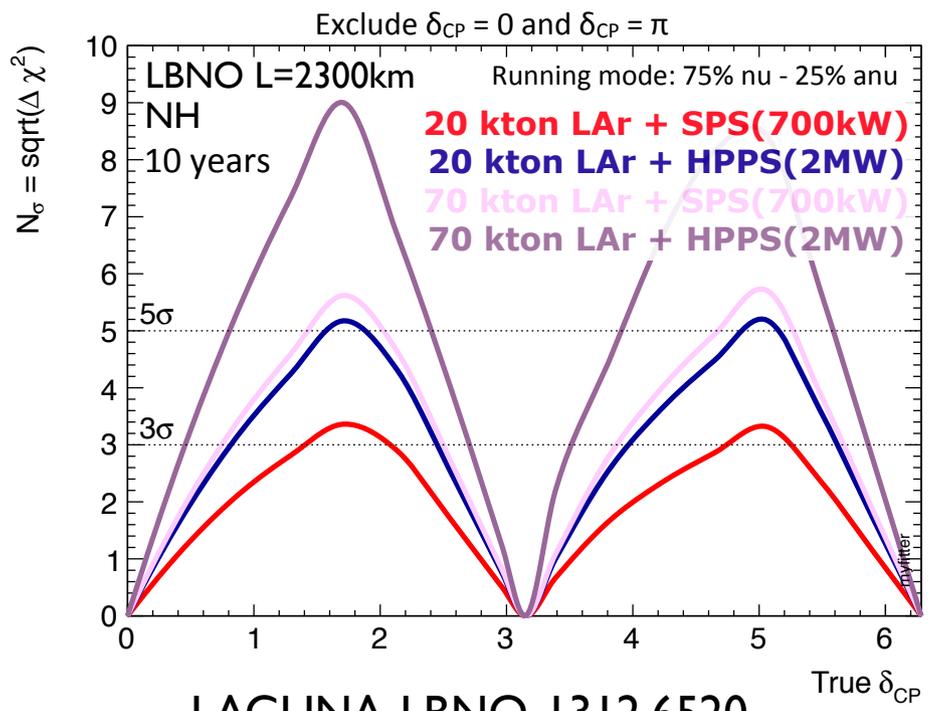
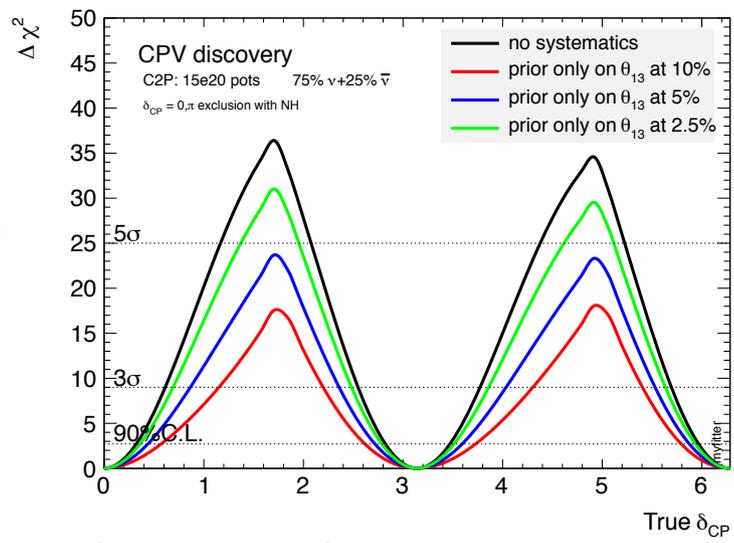


# LBNE-34kton



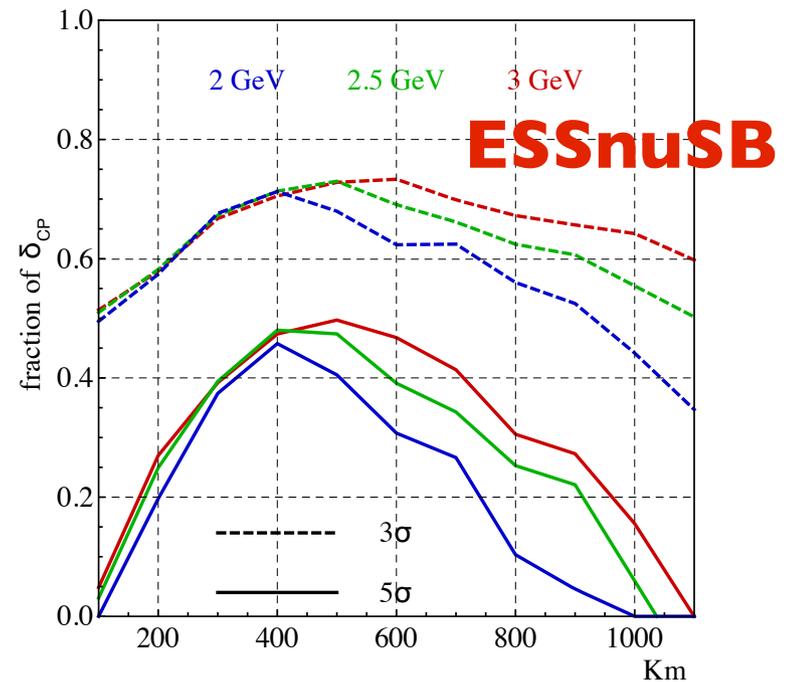
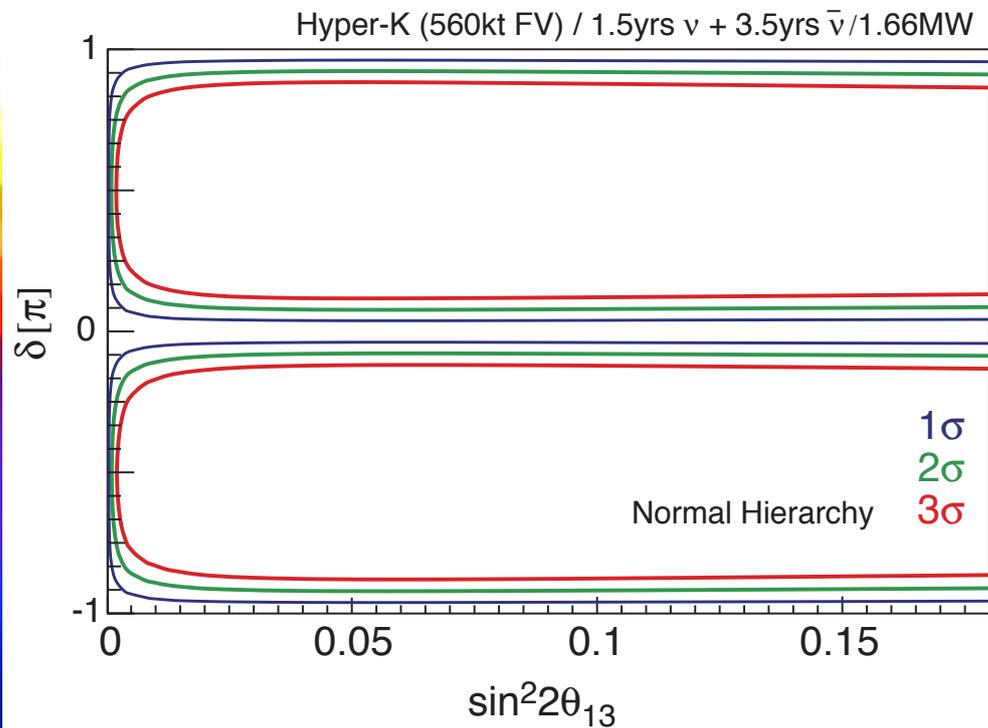
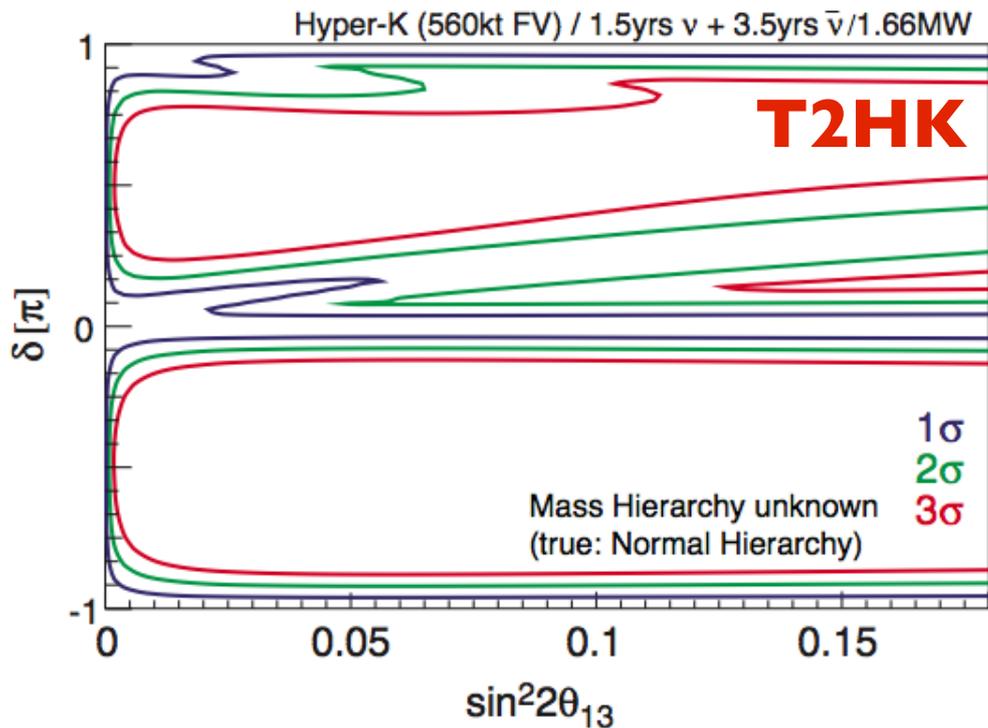
LBNE Coll.,  
1307.7335

# LBNO



LAGUNA-LBNO, 1312.6520

See T. Patzak's, R. Wilson's talk



ESSnuSB, I 309.7022

**T2HK:**

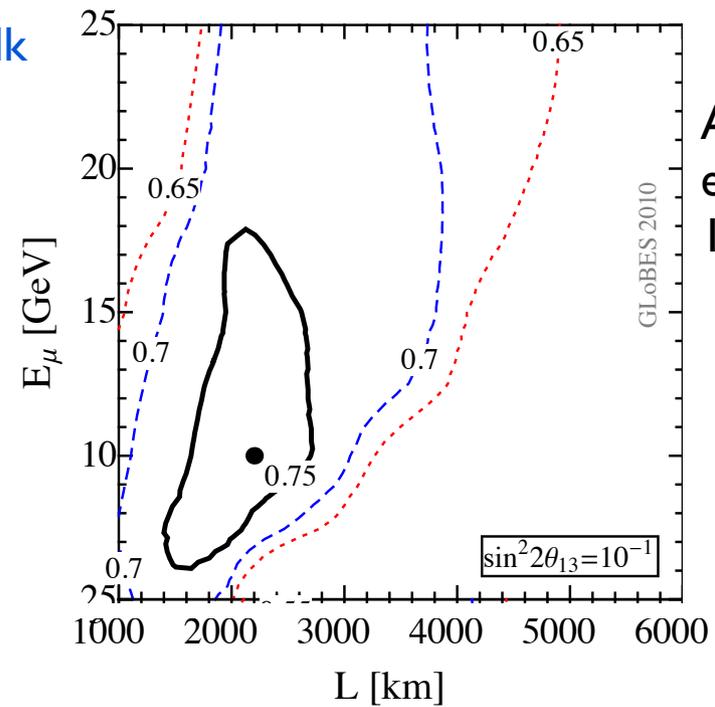
The knowledge of the mass ordering is crucial (CPV-mass ordering degeneracy)

**ESSnuSB:**

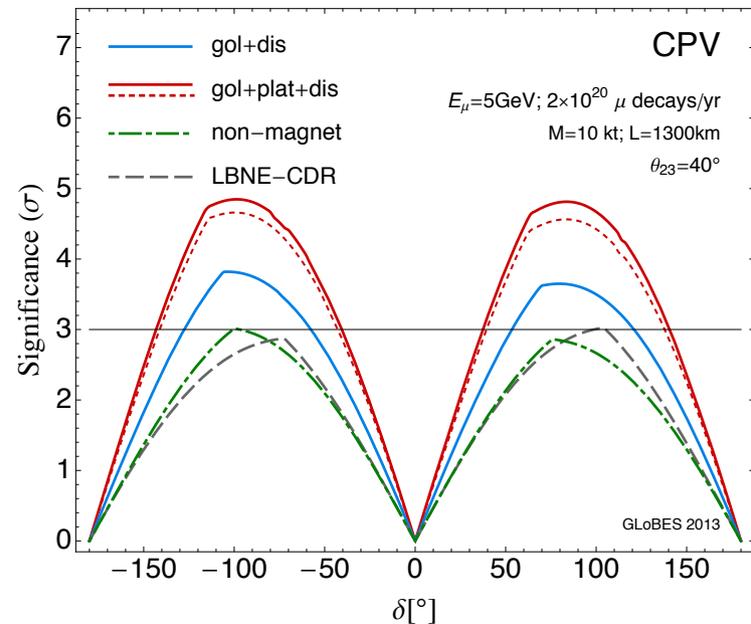
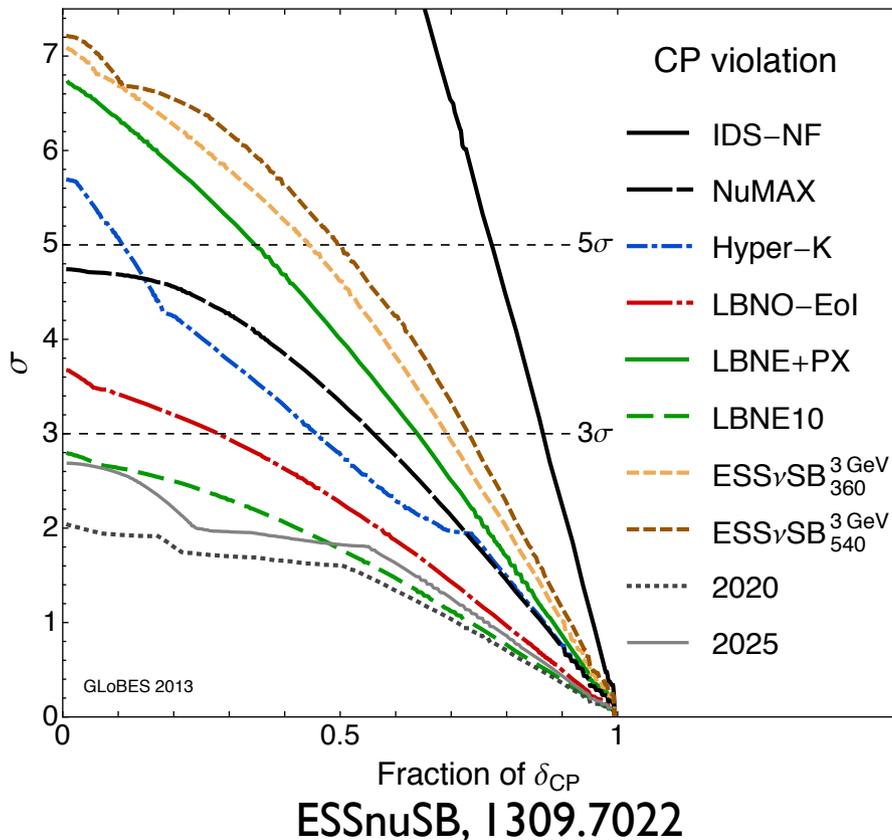
Use the information at low energy.

# Neutrino factory See P. Soler's talk

The neutrino factory has the best sensitivity to CPV. Due to large  $\theta_{13}$ , low energy muons and not-too-long baselines are needed.



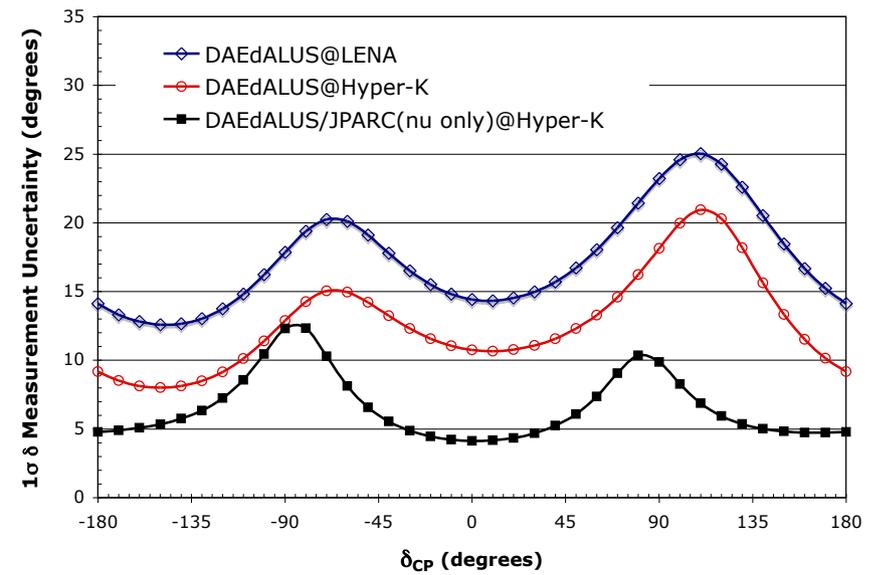
Agarwalla et al., JHEP 1101



Christensen et al., PRL 111. See also Geer, Mena SP, PRD 75, Bross et al, PRD77; Fernandez-Martinez, Li, Mena, SP, PRD 81; and Rubbia et al., 2001; IDS-NF..

# DAEdALUS

Uses the probability of oscillation of low energy muon antineutrino into electron antineutrinos at short baselines (1.5-20 Km).

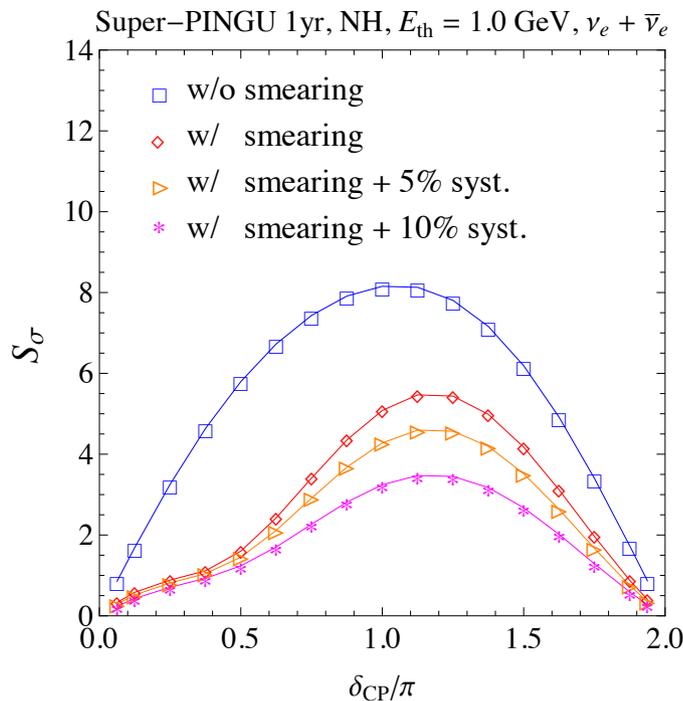


DAEdALUS Coll., I 307.2949

## Atmospheric neutrinos

These experiments have access to a broad range of baselines and energies. Limited energy and angular resolution and nu-anti nu discrimination affect their reach.

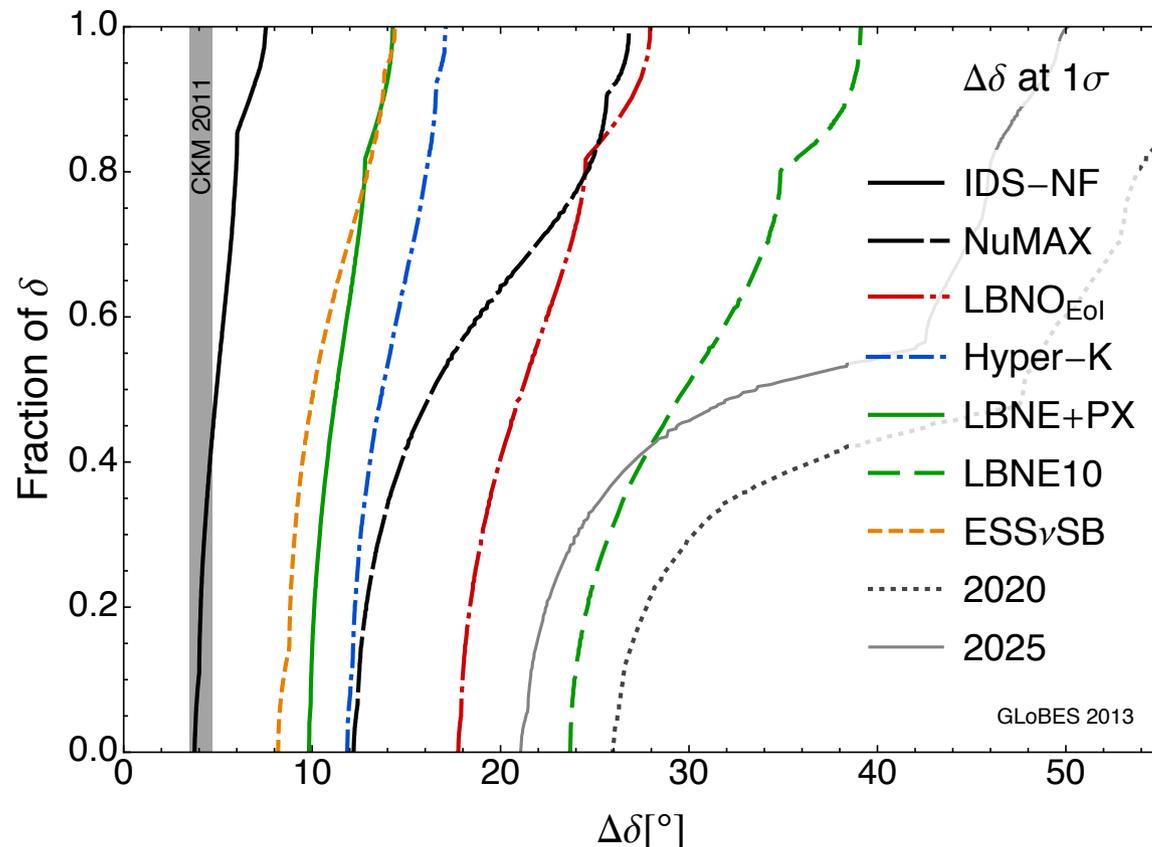
Peres, Smirnov; Kimura et al., Gonzalez-Garcia, Maltoni; Akhmedov et al.; Mena et al.; Hay, Latimer; Agarwalla et al.; Ohlsson et al.; Ge et al.; Abe et al.; Kearns et al.; Adams et al; ...



Razzaque, Smirnov, to appear

## Precision measurements of oscillation parameters

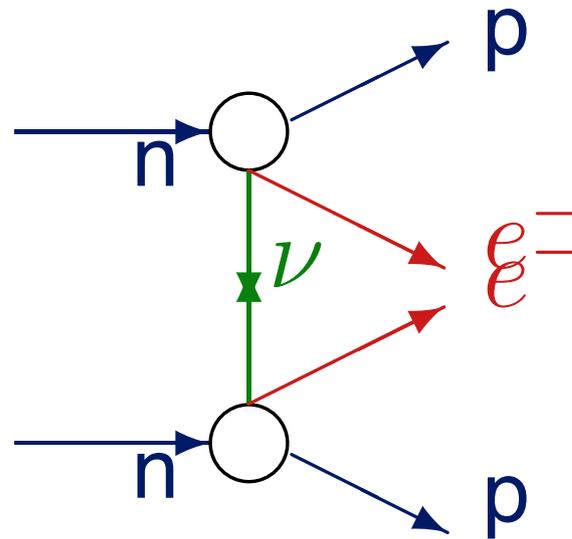
The precision measurement of the oscillation parameters will become very important once the mass hierarchy and CPV are established. LBL experiments can give information on  $\theta_{23}$ ,  $\theta_{13}$ ,  $\delta$ .



WG Report: Neutrinos, de Gouvea (Convener) et al., I310.4340; see also, Coloma et al., JHEP 1206; Minakata, Parke, PRD87; D. Meloni, PLB728

# Neutrinoless double beta decay

Neutrinoless double beta decay,  $(A, Z) \rightarrow (A, Z+2) + 2e^-$ , will test the nature of neutrinos.



This process has a special role in the study of neutrino properties as it probes **lepton number violation** and can provide information on neutrino masses and (possibly) on **CP-violation**.

The half-life time depends on neutrino properties

$$\left[ T_{0\nu}^{1/2}(0^+ \rightarrow 0^+) \right]^{-1} \propto |M_F - g_A^2 M_{GT}|^2 |\langle m \rangle|^2$$

- $|\langle m \rangle| = m_{ee}$  : the effective Majorana mass parameter

$$|\langle m \rangle| \equiv \left| m_1 |U_{e1}|^2 + m_2 |U_{e2}|^2 e^{i\alpha_{21}} + m_3 |U_{e3}|^2 e^{i\alpha_{31}} \right|,$$

Mixing angles (known)

CPV phases (unknown)

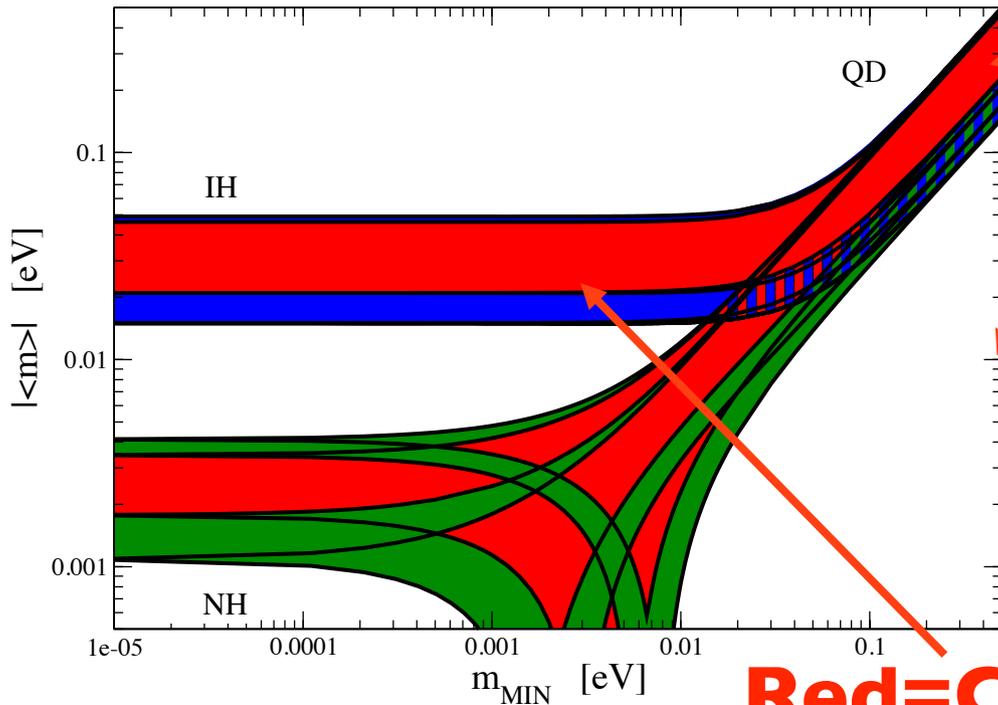
- $|M_F - g_A^2 M_{GT}|^2$  : the nuclear matrix elements. They need to be computed theoretically.

See J. Engel's talk

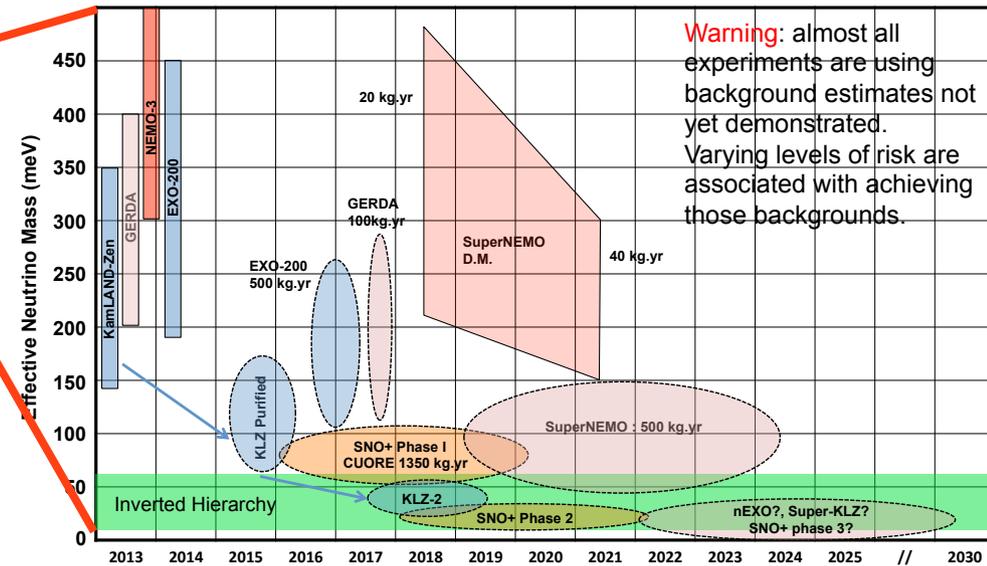
# Predictions for neutrinoless 2beta decay

Example: QD ( $m_1 \sim m_2 \sim m_3$ ):  $44 \text{ meV} < |\langle m \rangle| < m_1$

$$|\langle m \rangle| \simeq m_{\bar{\nu}_e} \left| \left( \cos^2 \theta_{\odot} + \sin^2 \theta_{\odot} e^{i\alpha_{21}} \right) \cos^2 \theta_{13} + \sin^2 \theta_{13} e^{i\alpha_{31}} \right|$$



**Red=CPV**



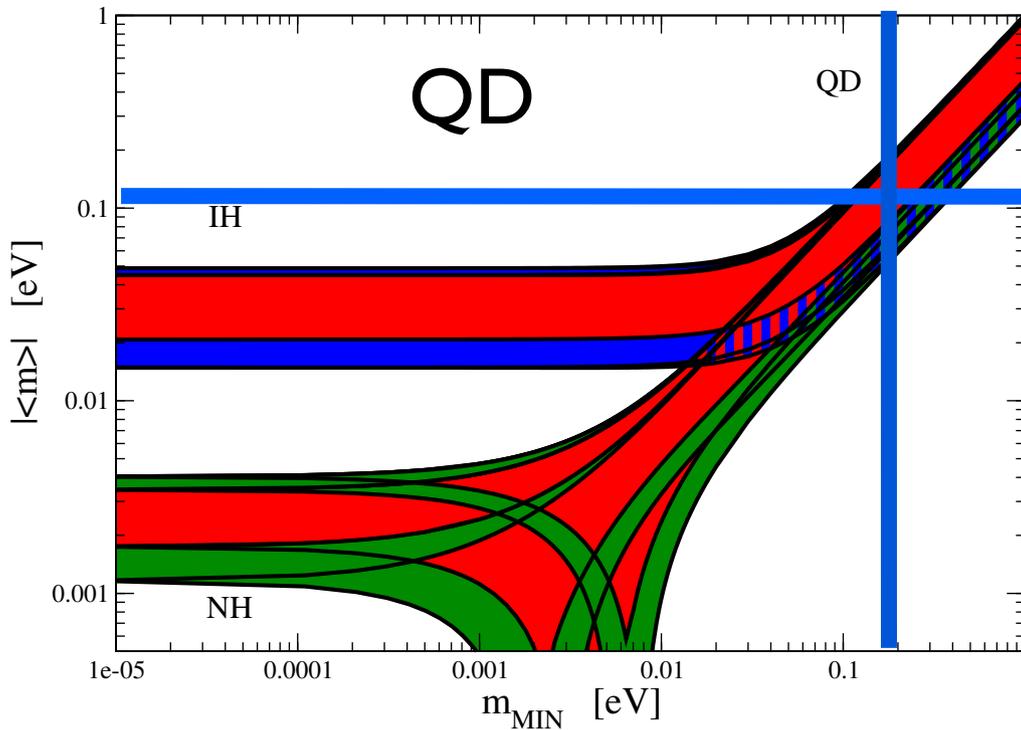
J. Hartnell, IOP meeting 2014

See Cremonesi's, Bongrand's, Schönert's, Shimizu's, Marino's, Winslow's talks

SP 2014, from Nakamura, Petcov review in PDG

**Broad experimental program** for the future: **a positive signal would indicate that L is violated!**

# Determining CP-violation with neutrinoless 2beta decay

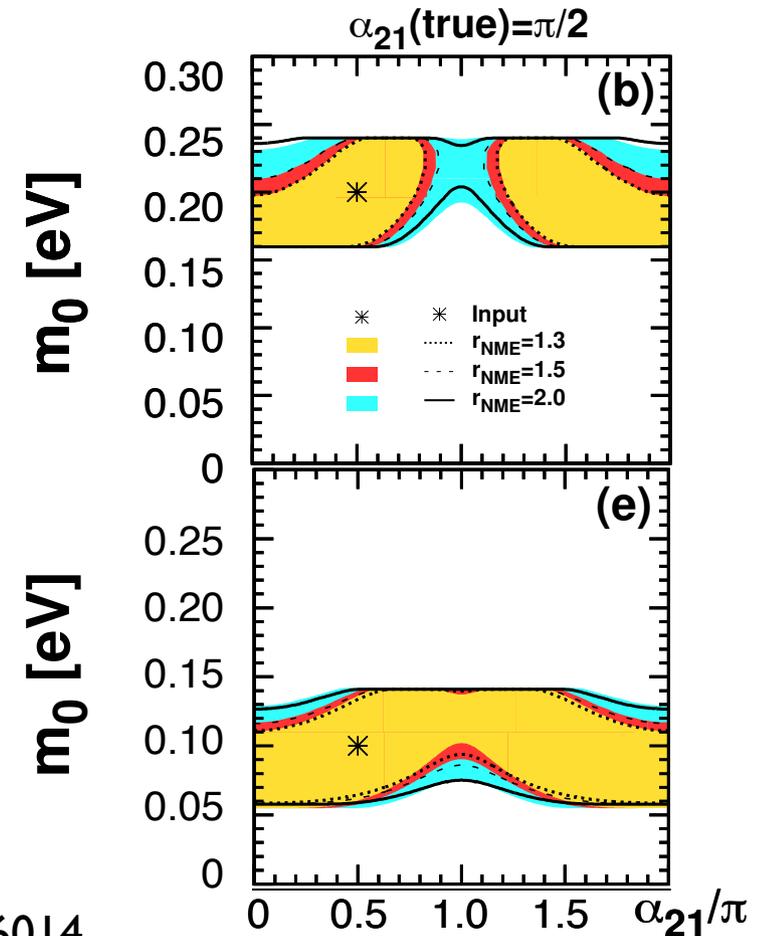


See also M. Hirsch's talk

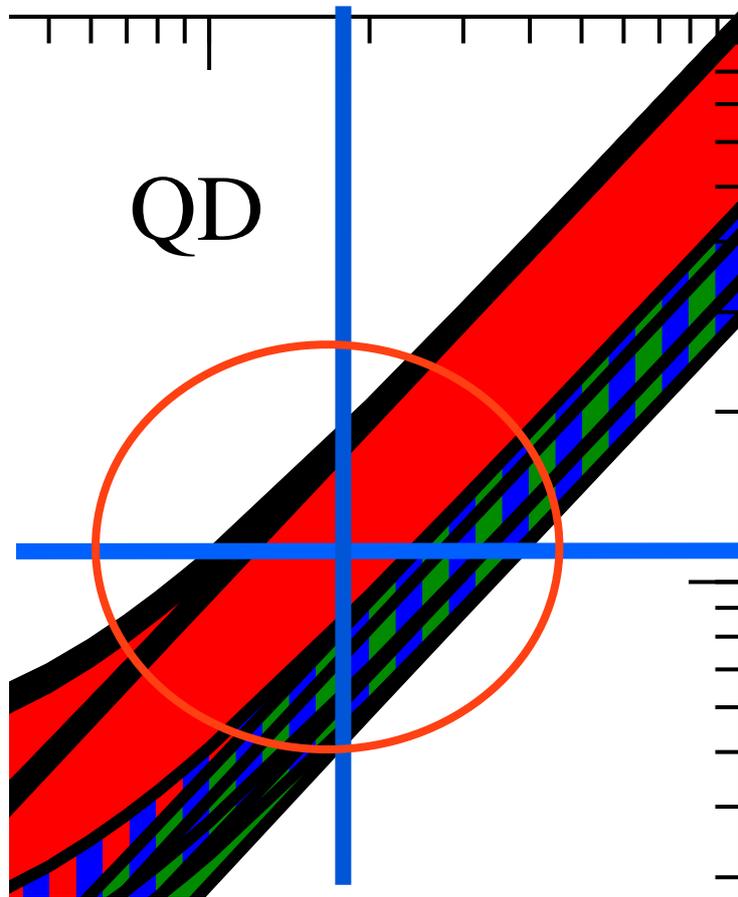
However, this requires also a very precise determination of NME.

See also, SP, Petcov and Wolfenstein, PLB524.; SP, S. Petcov, T. Schwetz, NPB734; F. Simkovic, et al., PRD 87; Joniec, Zralek, PRD73; Deppisch et al, PRD72; Bahcall et al., PRD70; de Gouvea et al, PRD67; SP, et al., PLB579; Nunokawa et al., PRD66; Barger et al., PLB540.

If  $|\langle m \rangle|$  and the masses are measured with sufficient precision, then it may be possible to establish CPV due to Majorana phases.



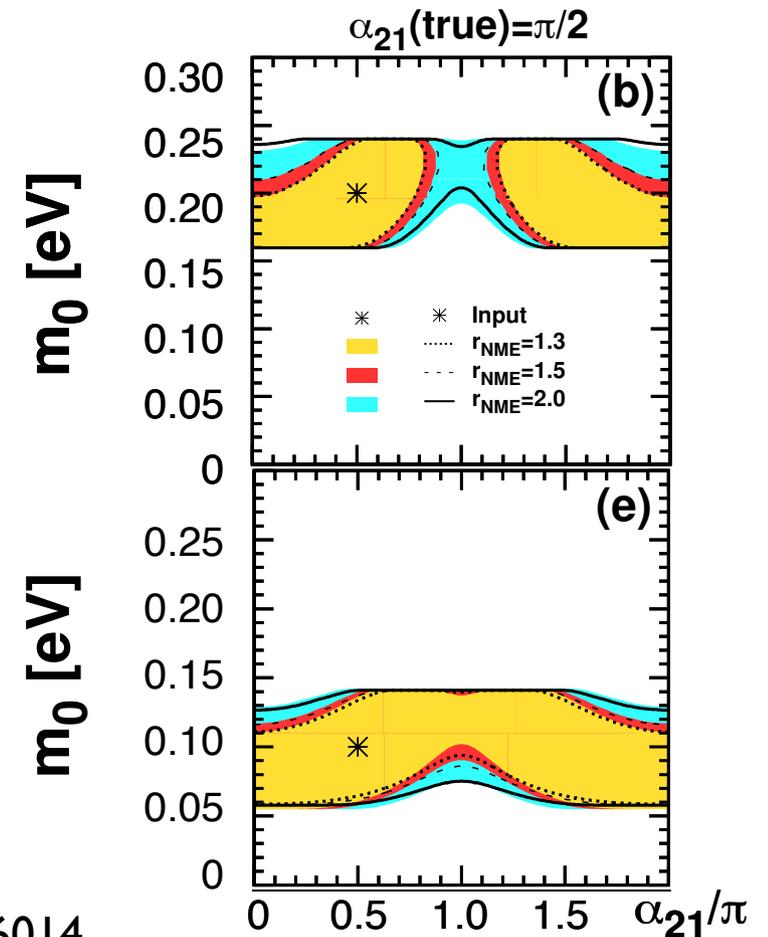
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# **Why is observing leptonic CP-violation important?**

**CP-violation has been observed in  
the quark sector. Does it occur also  
in the leptonic sector? and if so,  
what is its origin?**

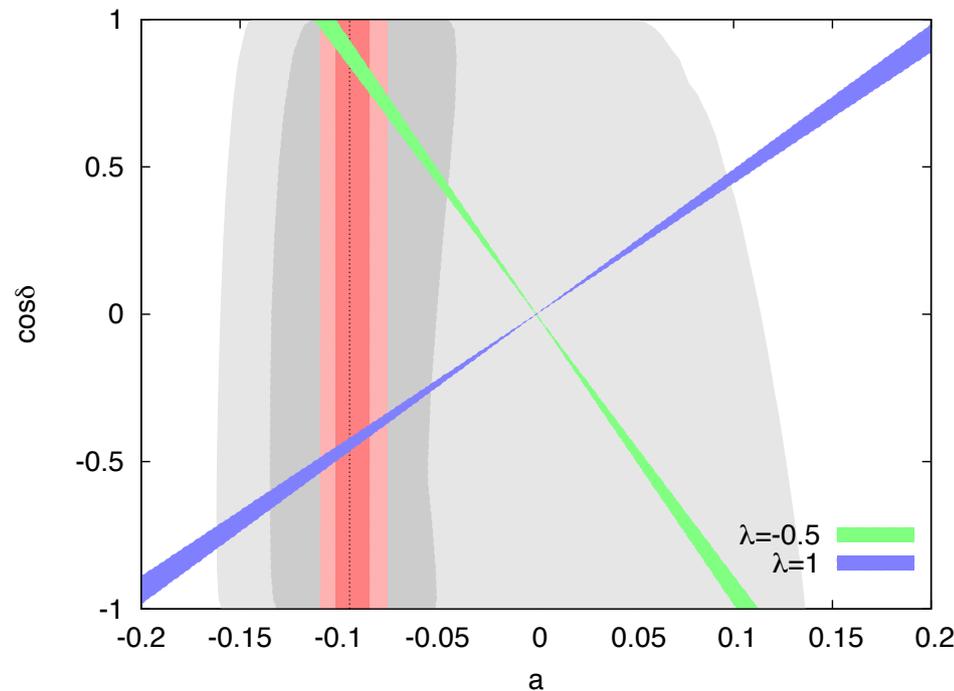
Different flavour models can lead to specific predictions for the value of the delta phase: [See M.Tanimoto's talk](#)

- Sum rules:  $\sin \theta_{12} = \frac{1+s}{\sqrt{3}}$ ,  $\sin \theta_{13} = \frac{r}{\sqrt{2}}$ ,  $\sin \theta_{23} = \frac{1+a}{\sqrt{2}}$  King, 0710.0530

$$a = a_0 + \lambda r \cos \delta + \text{higher orders}$$

- discrete symmetries models

- charged lepton corrections to  $U_\nu$ :  $U_{\text{PMNS}} = U_e^\dagger U_\nu$



Ballett, King, Luhn, SP, Schmidt, PRD89

M.-C. Chen and Mahanthappa; Girardi et al.; Petcov; Alonso, Gavela, Isidori, Maiani; Ding et al.; Ma; Hernandez, Smirnov; Feruglio et al.; Mohapatra, Nishi; Holthausen, Lindner, Schmidt; see also studies by Altarelli, Alonso, Ballett, Bazzocchi, Brahmachari, Branco, M.-C. Chen, Ding, Felipe, Ferreira, Feruglio, Fonseca, Frigerio, Gavela, Ge, Grimus, Gupta, Hagedorn, Hanlon, Hernandez, Holthausen, Hu, King, Joaquim, Joshipura, Ishimori, Lam, Lavoura, C.-C. Li, Lindner, Luhn, Ludl, B.-Q. Ma, E. Ma, Marzocca, Merle, Merlo, Meroni, Mohapatra, Morisi, Nishi, Ohlsson, Otto Ludl, Pascoli, Patel, Petcov, H. Qu, Rebelo, Repko, Rigolin, Romanino, Roy, Schmidt, Sevilla, Silva-Marcos, Smirnov, Stamou, Stuart, Tanimoto, Valle, Villanova del Moral, Vitale, Wegman, Zhang, Zhou, Ziegler...

# CPV and the Baryon asymmetry

There is evidence of the baryon asymmetry:

$$\eta_B \equiv \frac{n_B - n_{\bar{B}}}{n_\gamma} = (6.14 \pm 0.08) \times 10^{-10}$$

Planck, l303.5076

In order to generate dynamically a baryon asymmetry, the Sakharov's conditions need to be satisfied:

- B (or L) violation;
- C, CP violation;
- departure from thermal equilibrium.

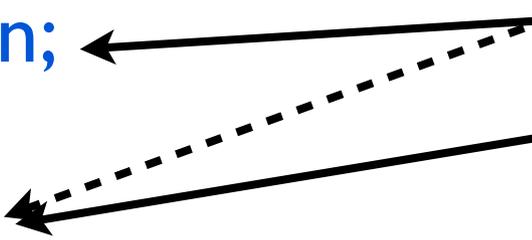
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**Neutrinoless double beta decay**

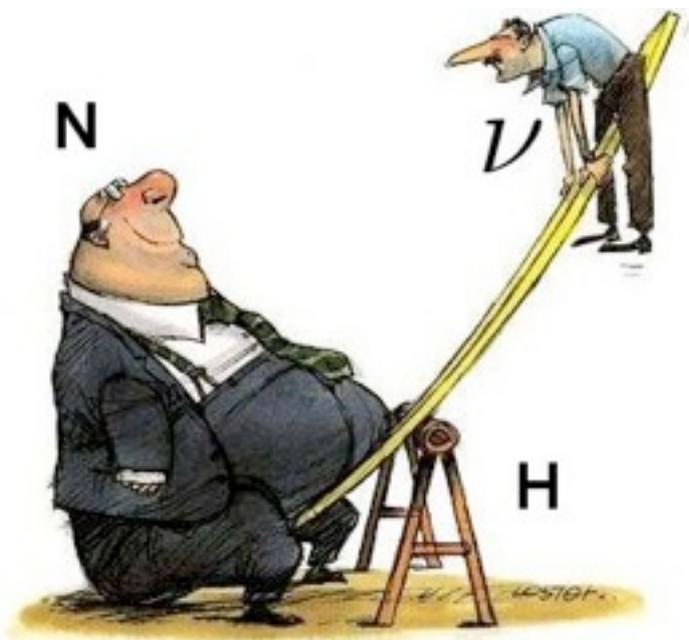
**LBL**

**Expansion of the Universe**

**Leptogenesis in models at the origin of  
neutrino masses**

# Neutrino masses BSM: see saw mechanism type I

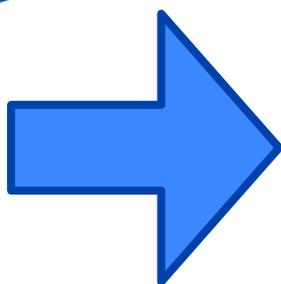
See Babu's talk



- Introduce a right handed neutrino **N**
- Couple it to the Higgs

$$\mathcal{L} = -Y_\nu \bar{N} L \cdot H - 1/2 \bar{N}^c M_R N$$

$$\begin{pmatrix} 0 & m_D \\ m_D^T & M_N \end{pmatrix}$$



$$m_\nu = \frac{Y_\nu^2 v_H^2}{M_N} \sim \frac{1 \text{ GeV}^2}{10^{10} \text{ GeV}} \sim 0.1 \text{ eV}$$

Minkowski; Yanagida; Glashow; Gell-Mann, Ramond, Slansky; Mohapatra, Senjanovic

See-saw type I models can be embedded in GUT theories and explain the baryon asymmetry via leptogenesis.

# Leptogenesis

- At  $T > M$ , the right-handed neutrinos  $N$  are in equilibrium thanks to the processes which produce and destroy them:



- When  $T < M$ ,  $N$  drops out of equilibrium



- A lepton asymmetry can be generated if

$$\Gamma(N \rightarrow \ell H) \neq \Gamma(N \rightarrow \ell^c H^c)$$

- Sphalerons convert it into a baryon asymmetry.

$T = 100$   
GeV

In order to compute the baryon asymmetry:

1. evaluate the CP-asymmetry

$$\epsilon \equiv \frac{\Gamma(N \rightarrow \ell H) - \Gamma(N^c \rightarrow \ell^c H^c)}{\Gamma(N \rightarrow \ell H) + \Gamma(N^c \rightarrow \ell^c H^c)}$$

2. solve the Boltzmann equations to take into account the wash-out of the asymmetry

$$Y_L = k\epsilon$$

3. convert the lepton asymmetry into the baryon one

$$Y_B = \frac{k}{g^*} c_s \epsilon \sim 10^{-3} - 10^{-4} \epsilon$$

For  $T < 10^{12}$  GeV, flavour effects are important.

**Is there a connection  
between low energy  
CPV and the baryon  
asymmetry?**

## The general picture

$\epsilon$  depends on the CPV phases in  $Y_\nu$

$$\epsilon \propto \sum_j \Im(Y_\nu Y_\nu^\dagger)_{1j}^2 \frac{M_j}{M_1}$$

and in the U mixing matrix via the **see-saw formula**.

$$m_\nu = U^* m_i U^\dagger = -Y_\nu^T M_R^{-1} Y_\nu v^2$$

Let's consider see-saw type I with 3 NRs.

High energy

$M_R$	3	0
$Y_\nu$	9	6

Low energy

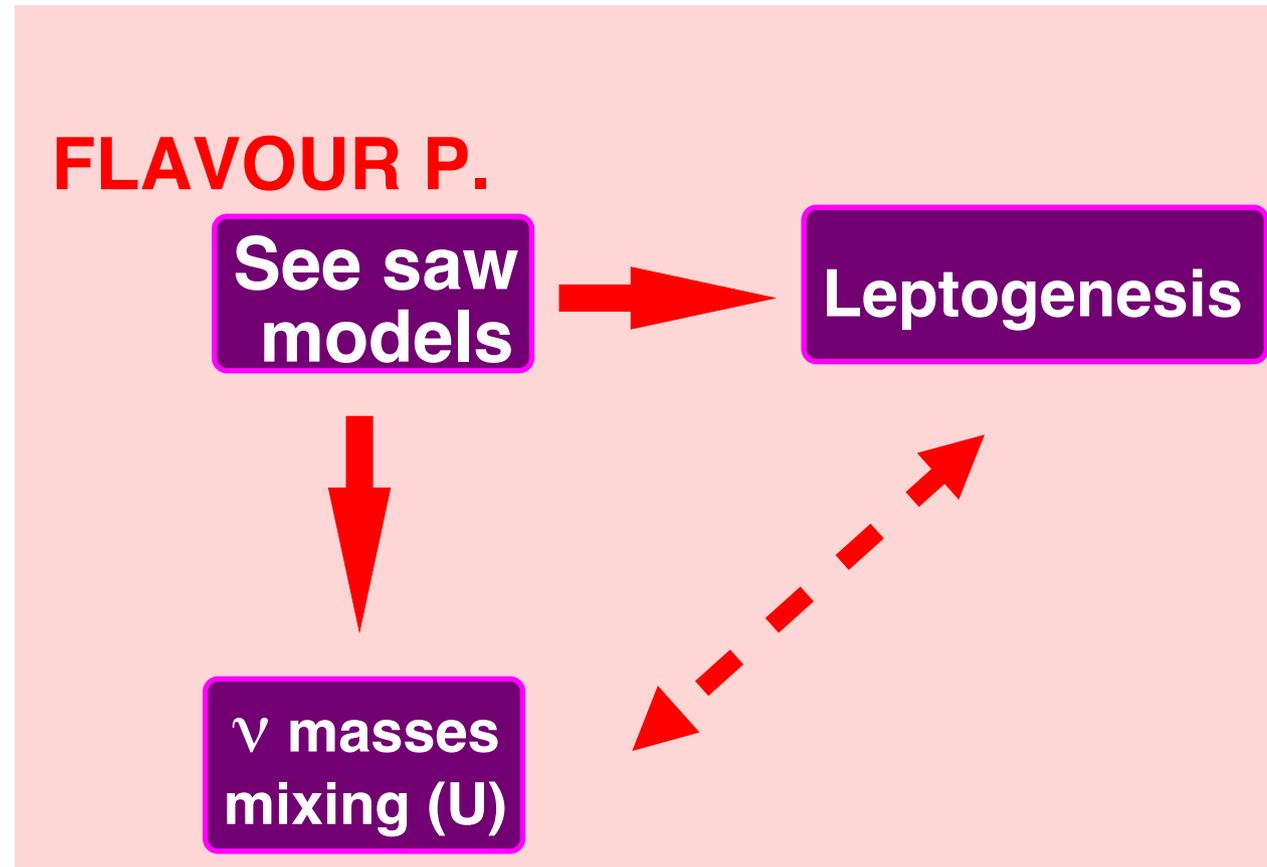
$m_i$	3	0
$U$	3	3

**3 phases missing!**

## *Specific flavour models*

In understanding the origin of the flavour structure, the see-saw models have a reduced number of parameters.

It may be possible to predict the baryon asymmetry from the Dirac and Majorana phases.

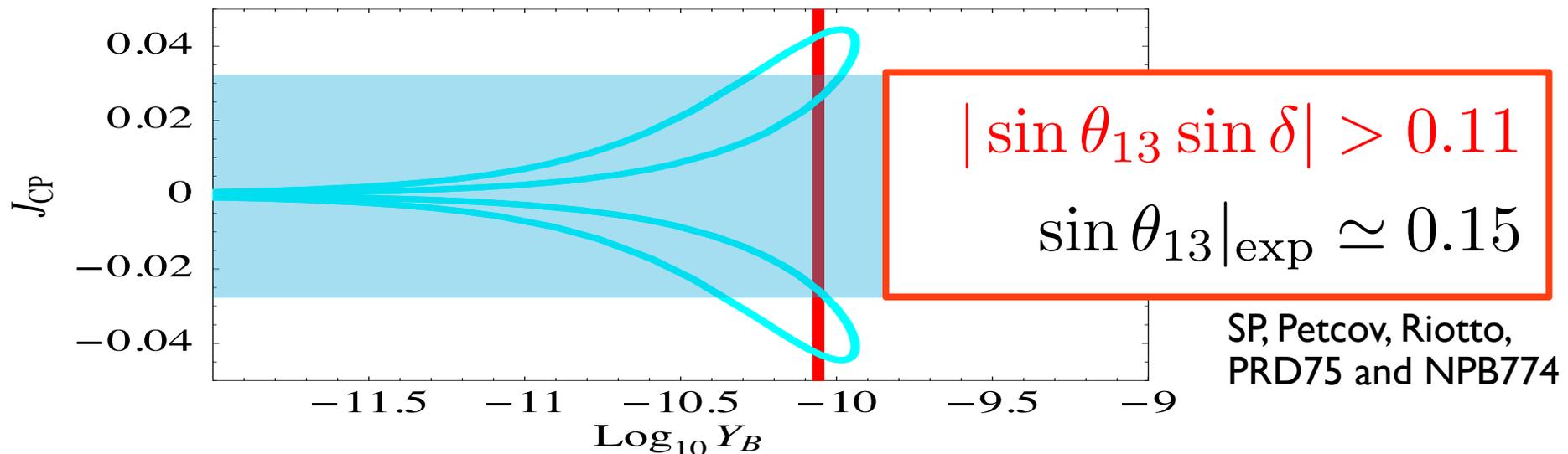


## Does observing low energy CPV imply a baryon asymmetry?

It has been shown that, thanks to flavour effects, the low energy phases enter directly the baryon asymmetry.

Example in see-saw type I, with NH ( $m_1 \ll m_2 \ll m_3$ ),  $M_1 < M_2 < M_3$ ,  $M_1 \sim 5 \cdot 10^{11}$  GeV:

$$\epsilon_\tau \propto M_1 f(R_{ij}) \left[ c_{23} s_{23} c_{12} \sin \frac{\alpha_{32}}{2} - c_{23}^2 s_{12} s_{13} \sin \left( \delta - \frac{\alpha_{32}}{2} \right) \right]$$



Large  $\theta_{13}$  implies that  $\delta$  can give an important (even dominant) contribution to the baryon asymmetry. Large CPV is needed and a NH spectrum.

# Conclusions

- There are current **intriguing hints** of CP-violation.
- Future **LBL experiments** will hunt for the delta phase and potentially measure it with precision. Neutrinoless double beta decay could point towards Majorana CPV.
- **CP-violation**, together with **L violation**, is the key ingredient of **leptogenesis**.

**The observation of L violation and of CPV in the lepton sector would be a strong indication (even if not a proof) of leptogenesis as the origin of the baryon asymmetry.**