

#### Standing on the Shoulders of Giants: Future Charged Lepton Flavor Violation Experiments



R. Bernstein Fermilab

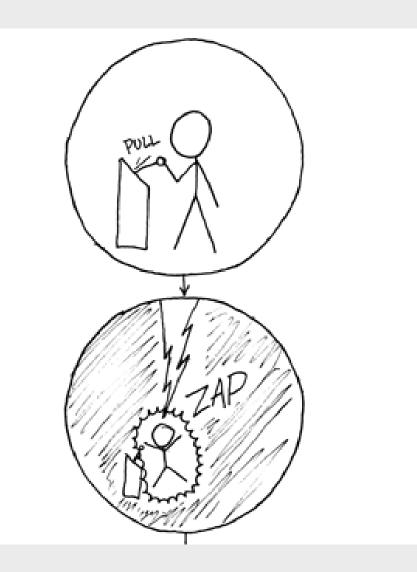
http://lccn.loc.gov/50041709

R. Bernstein, FNAL

Academic Lectures: Future CLFV Experiments

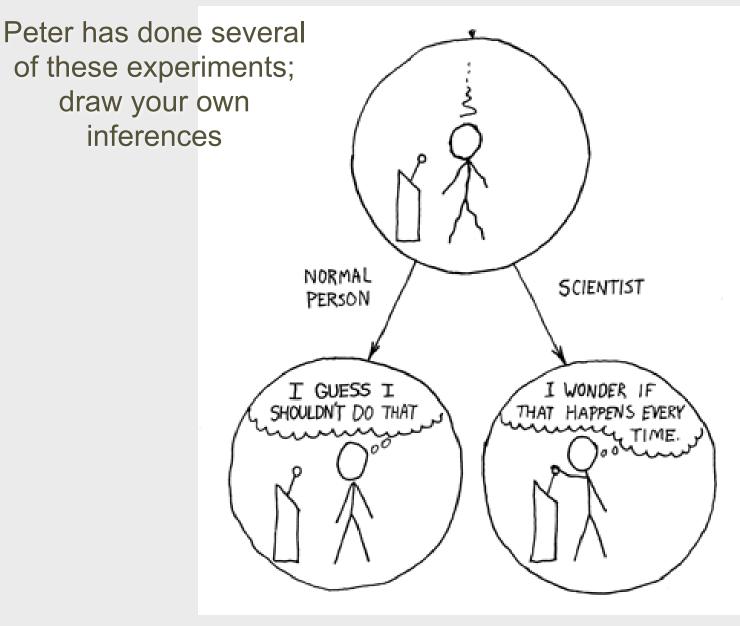
#### Alternative Title and Def'n of Insanity

http://xkcd.com/242/



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#### Problem with Review Talks





#### leave out someone's favorite topic

cover everything

I will do both, but one promise:

#### Will Not Talk About Reviews



Kepler at CD review

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#### Last Disclaimer

 Unless otherwise stated, none of these are official Mu2e (not official µ2e slides) and have not been vetted

#### Outline

- Review:
  - experimental methods and limitations
- New Methods for Muon-to-Electron Conversion
  - new designs and new problems
- Back to the Future
  - $\mu \to e\gamma$  and  $\mu \to ee^+e^-$

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What is 
$$\mu e$$
 Conversion?  
muon converts to electron in the field of a nucleus  
 $\mu^- N \rightarrow e^- N$   
 $R_{\mu e} = \frac{\Gamma(\mu^- + N(A,Z) \rightarrow e^- + N(A,Z))}{\Gamma(\mu^- + N(A,Z) \rightarrow all muon captures)}$ 

- Standard Model Background of 10<sup>-54</sup>
- Charged Lepton Flavor Violation (CLFV)
  - can measure a signal with SES of 2.3 x 10<sup>-17</sup>
- Related Processes:  $\mu$  or  $\tau \rightarrow e\gamma$ ,  $\tau \rightarrow 3l$ ,  $K_L \rightarrow \mu e$ , and more

7

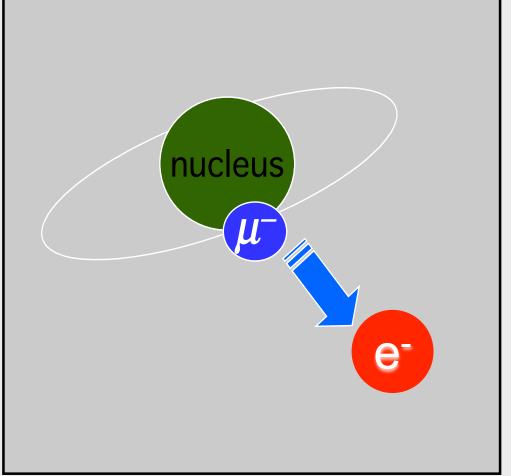
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# Experimental Signal $\mu^- N \rightarrow e^- N$

- A Single Monoenergetic Electron
- If *N* = AI, E<sub>e</sub> = 105. MeV
  - electron energy depends on Z
- Nucleus coherently recoils off outgoing electron, no breakup



#### A Sketch of the Experiment

- Get muons in a 1s state around a nucleus
- Let them interact
- Measure a ratio of how often conversion happens normalized to something we can
  - detect
  - calculate

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# Understanding the Normalization

- How does the muon get captured by the nucleus?
  - through the weak interaction
    - (and many details cancel in the ratio we measure)
- But first the wave functions have to overlap:
  - what's the Bohr radius for a 1s muon in Aluminum?  $\hbar^2$  o m = 1

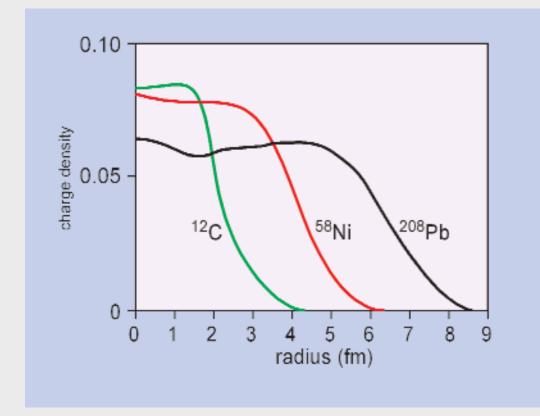
$$a_{0} = \frac{\hbar^{2}}{Zm_{\mu}c^{2}} = 0.529 \overset{o}{A} \times (\frac{m_{e}}{m_{\mu}}) \times \frac{1}{13} = 2 \times 10^{-4} \overset{o}{A}$$
$$= 20 \text{ fermi}$$

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#### How Big Is A Nucleus?

 A few fermi for the relevant nuclei

 I wish I hadn't completely avoided nuclear physics as an undergrad and grad student <sup>(3)</sup>



http://www.nupecc.org/pans/Data/CHAPT\_4.PDF

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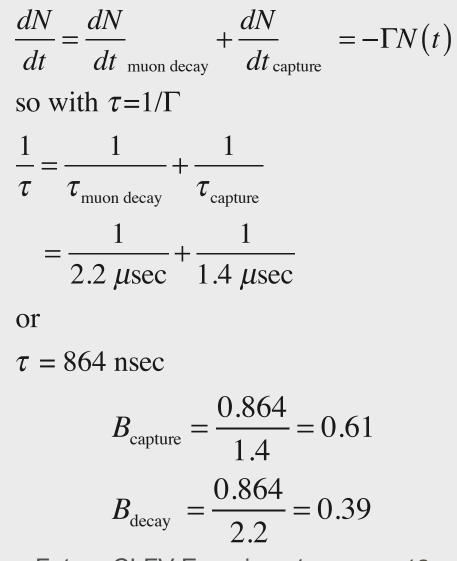
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## How Long Does this Take?

• What's the Hamiltonian?

 $H = H_{\text{muon decay}} + H_{\text{capture}}$ 

- 2.2  $\mu$ sec is from the strength of the weak interaction and G<sub>F</sub>
- 0.864 μsec is measured
- and then the branching fractions are:



#### What Happens Now?

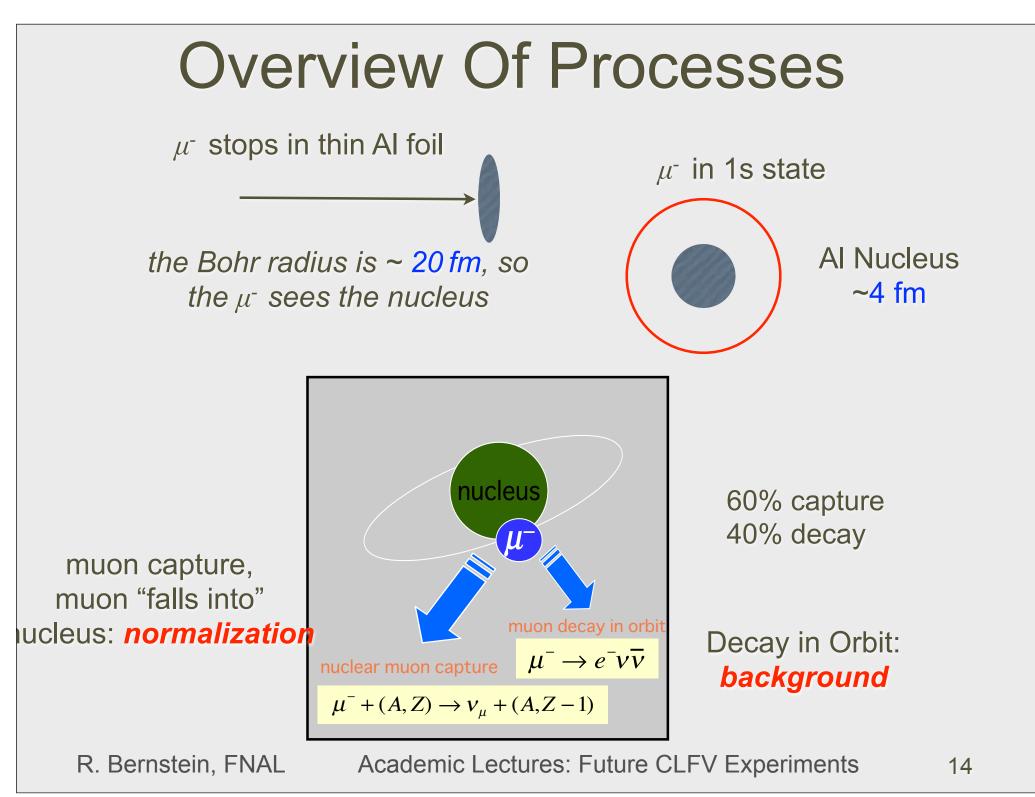
• The muon and nuclear wave functions overlap

probability of overlap:

~ 0.001 for a muon vs  $10^{-13}$  for an electron

- Don't try to do this calculation at home
  - doing it right involves relativistic wave functions and Dirac spinors (especially if new physics!!)
- In fact, a theorist got it wrong and a team of experimenters worked for a year as a result
  - hint: don't trust theorists (most important thing to learn)

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# Measuring 10<sup>-17</sup> in Collider Units

- The captured muon is in a 1s state and the wave function overlaps the nucleus (picture ~ to scale)
- We can turn this into an effective luminosity
- Luminosity = density x velocity

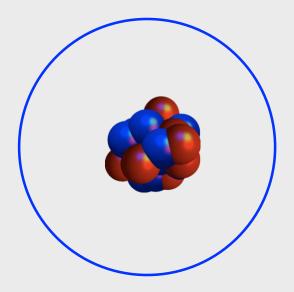
$$|\psi(0)|^2 \times \alpha Z = \frac{m_{\mu}^3 Z^4 \alpha^4}{\pi} = 8 \times 10^{43} \text{ cm}^{-2} \text{ sec}^{-1}$$

- Times 10<sup>10</sup> muons/sec X 2  $\mu$ sec lifetime
- Effective Luminosity of 10<sup>48</sup> cm<sup>-2</sup>sec<sup>-1</sup>

μ

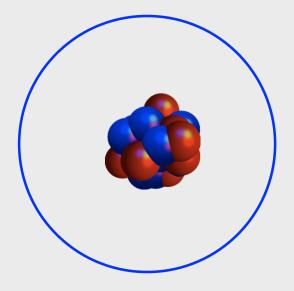
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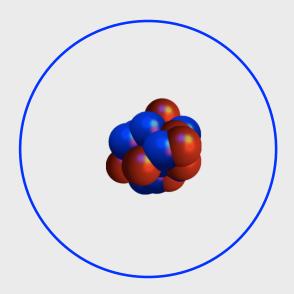
A. Czarnecki, <u>clfv.le.infn.it</u>

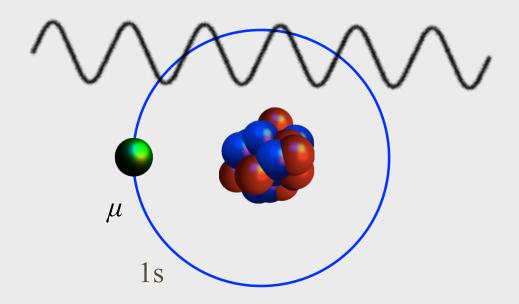


muon stops









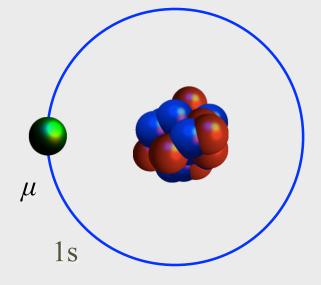
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#### Three Possibilities: Normalization X-Rays from cascade (occurs in <psec)

detect these for normalization

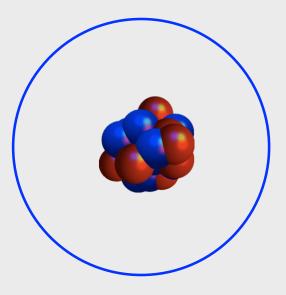
Transition	Energy
3d→ 2p	66 keV
2p→ 1s	356 keV
$3d \rightarrow 1s$	423 keV
4p→ 1s	446 keV



 $\sim \sim \sim \sim$ 

#### 1) measure stop rate 2) calculate capture rate/stop

Kitano et al. ,Phys.Rev.D66:096002,2002, Erratum-ibid.D76:059902,2007. e-Print: hep-ph/0203110

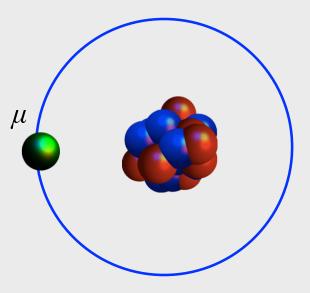


then compute 
$$R_{\mu e} = \frac{\mu N \rightarrow e N}{\mu N \rightarrow \text{ all captures}}$$
  
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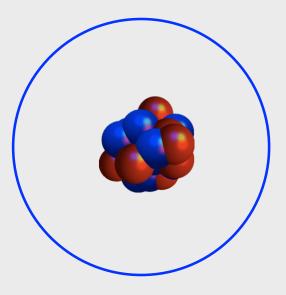
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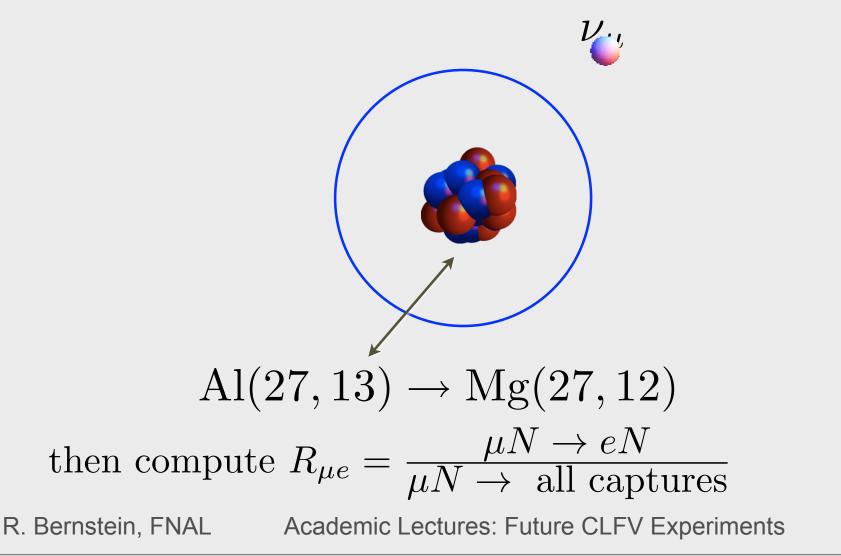


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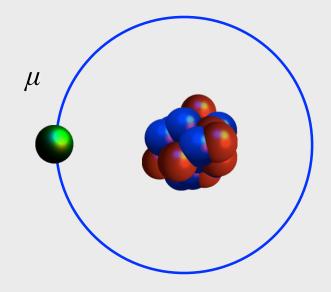
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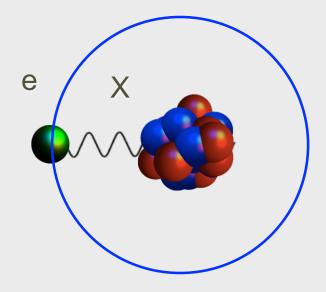
## **Counting Stops**

- Easier Said than Done
- Very High Rate Germanium
  - technically challenging
  - expensive?
  - work in progress
- Normalize to DIO instead?
  - use region where calculation robust
  - then subject to theory uncertainty but does not harm discovery potential; just a bad measurement of conversion rate...





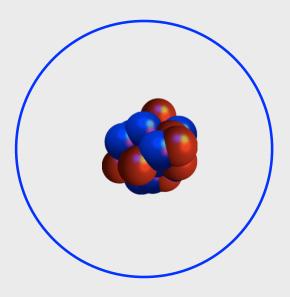




# Three Possibilities: Signal



е

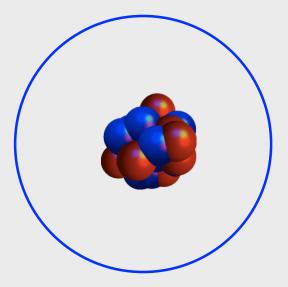


# Three Possibilities: Signal



off to detector!

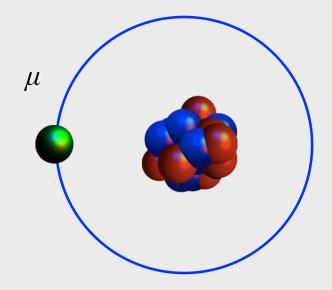




coherent recoil of nucleus

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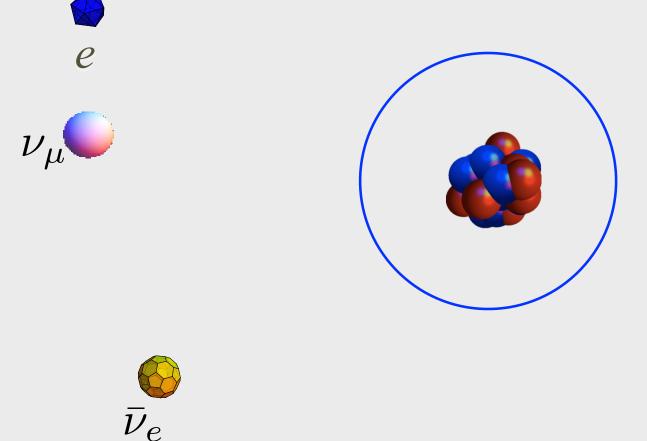
## Three Possibilities: Background



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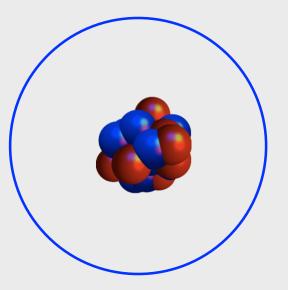
20

# Three Possibilities: Background



# Three Possibilities: Background

this electron can be background; let's see how





e

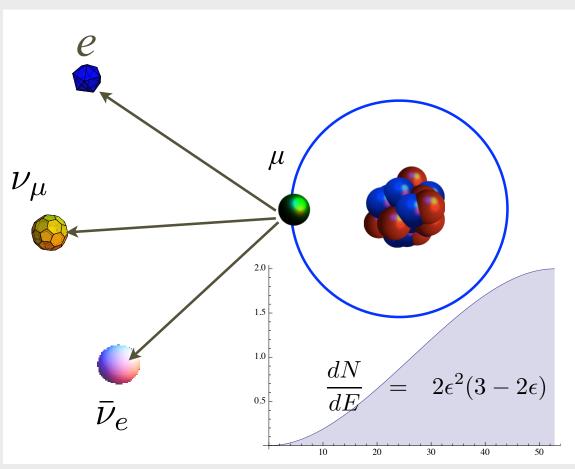
 $\nu_{\mu}$ 

## Decay-In-Orbit: Not always Background

• Peak and Endpoint of Michel Spectrum is at

$$E_{\max} = \frac{m_{\mu}^2 + m_e^2}{2m_{\mu}} \approx 52.8 \text{ MeV}$$

- Detector will be insensitive to electrons at this energy
- Recall signal at 105 MeV>>52.8 MeV

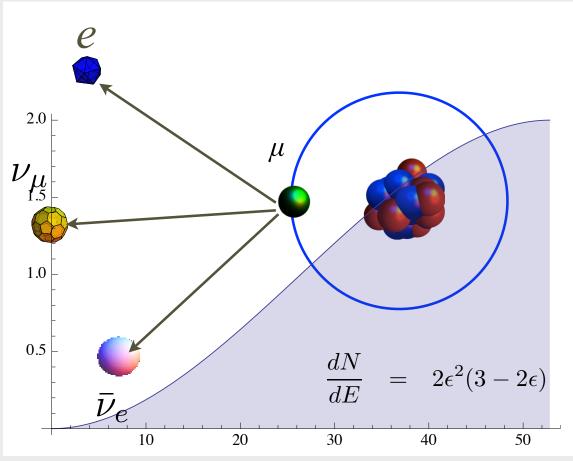


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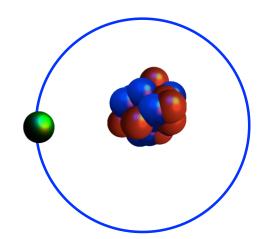
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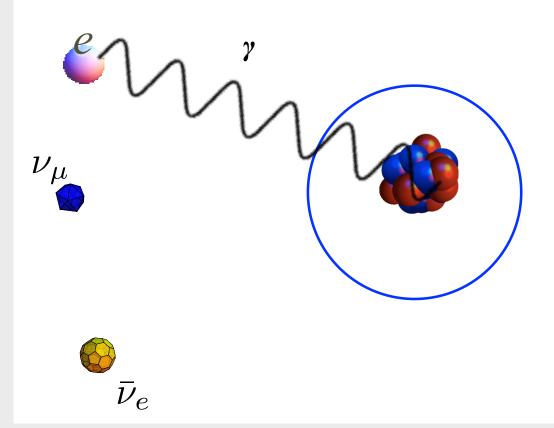
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- Same process as before
- But this time, include electron recoil off nucleus
- If neutrinos are at rest, the DIO electron can be exactly at conversion energy (up to neutrino mass)



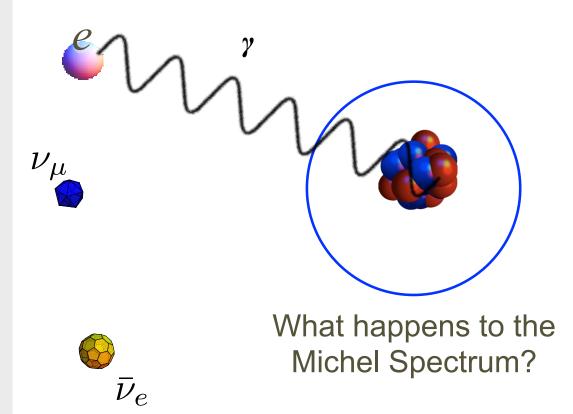
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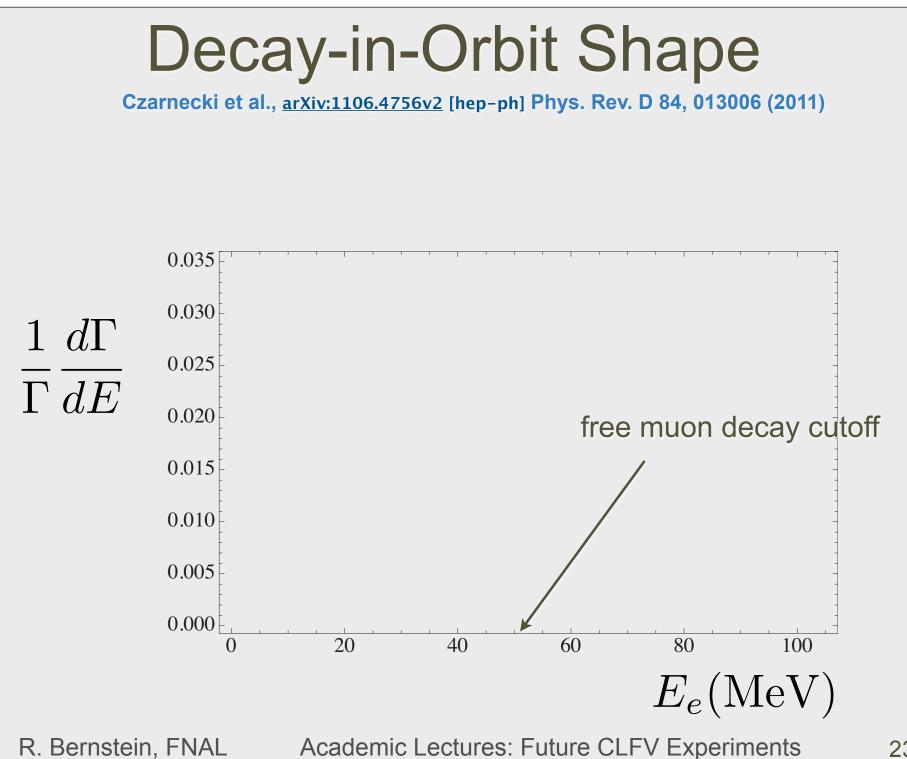
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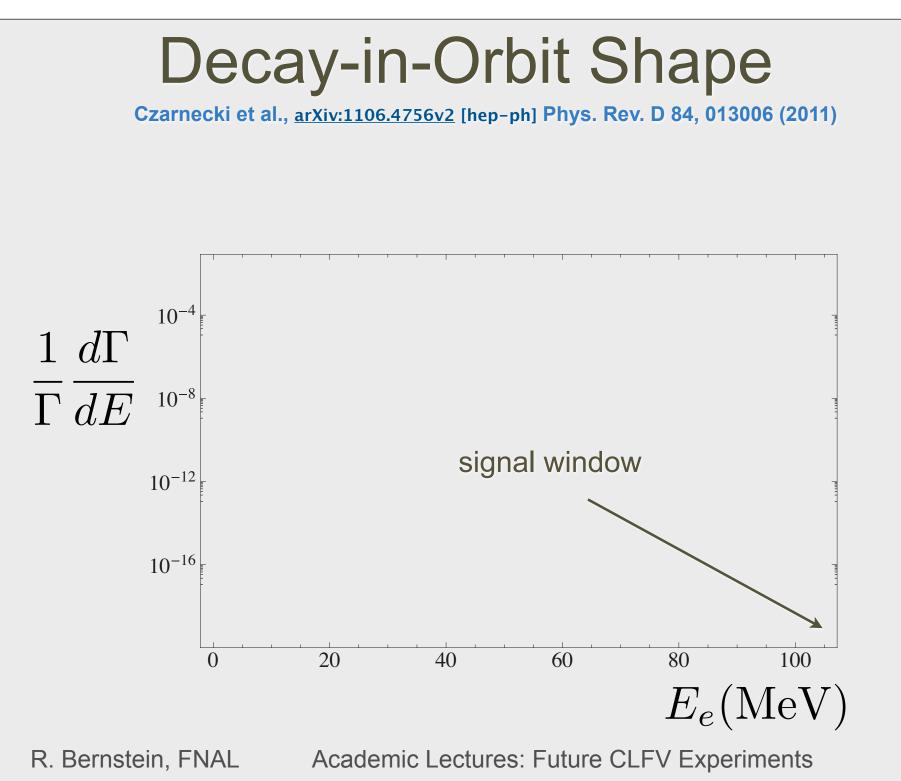


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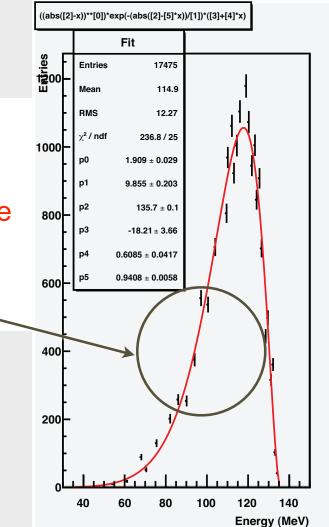
## **Prompt Backgrounds**

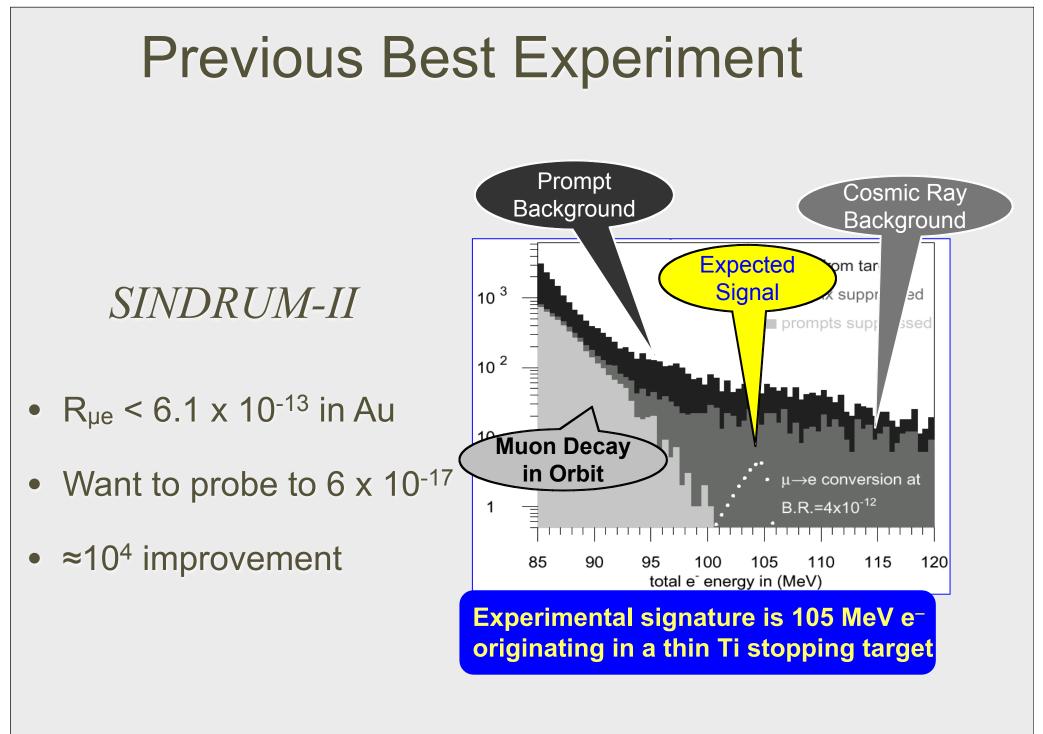
Particles produced by proton pulse which interact almost immediately when they enter the detector:  $\pi$ , neutrons, pbars

- Radiative pion capture,  $\pi$ -+A(N,Z)  $\rightarrow \gamma$  +X.
  - γ up to mπ, peak at 110 MeV; γ→ e+e-; if one electron ~ 100 MeV in the target, looks like signal: *limitation in best existing experiment, SINDRUM II?*

energy spectrum of  $\gamma$  measured on Mg J.A. Bistirlich, K.M. Crowe et al., Phys Rev C5, 1867 (1972)

also included internal conversion,  $\pi^- N \rightarrow e^+ e^- X$ 





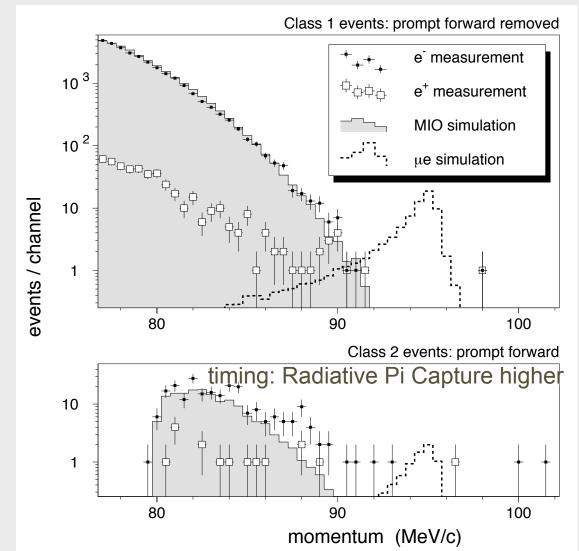
## **SINDRUM-II Results**

W. Bertl et al., Eur. Phys. J. C 47, 337-346 (2006)

• Final Results on Au:  $B_{\mu e}^{\rm Au} < 7 \times 10^{-13} @ 90\% {\rm CL}$ 

51 MHz (20 nsec) repetition rate, width of pulse ~0.3 nsec

little time separation between signal and prompt background



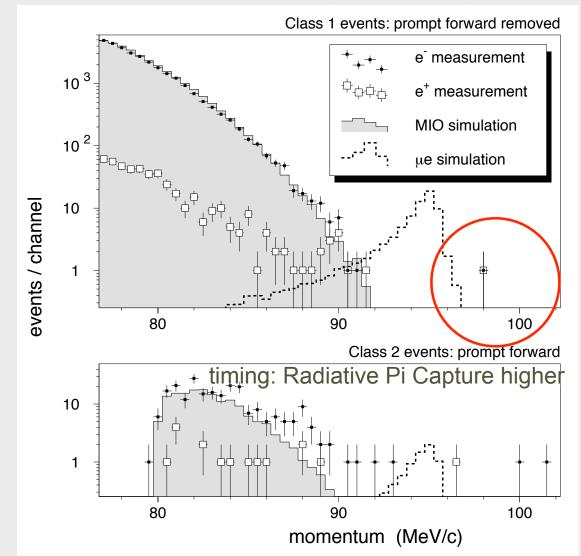
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#### How Can We Do Better?

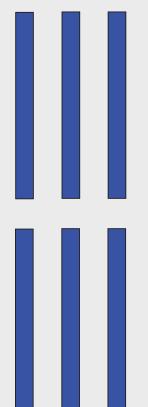
#### >10<sup>3</sup> increase in muon intensity from SINDRUM

#### Requiring

Pulsed Beam to Eliminate prompt backgrounds like radiative  $\pi$  capture and CR

protons out of beam pulse/ protons in beam-pulse < 10<sup>-10</sup> and we must measure it

target foils: muon converts here

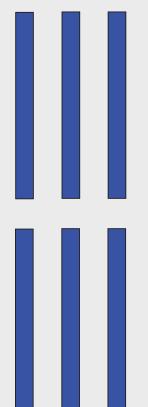




arrow strain for the strain term of term of

pulsed beam lets us wait until after prompt backgrounds disappear and rate lowered

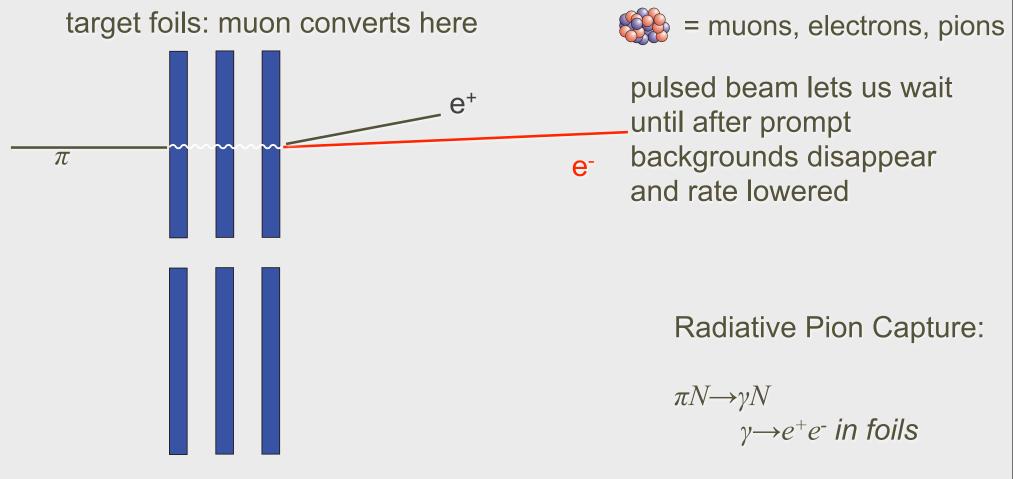
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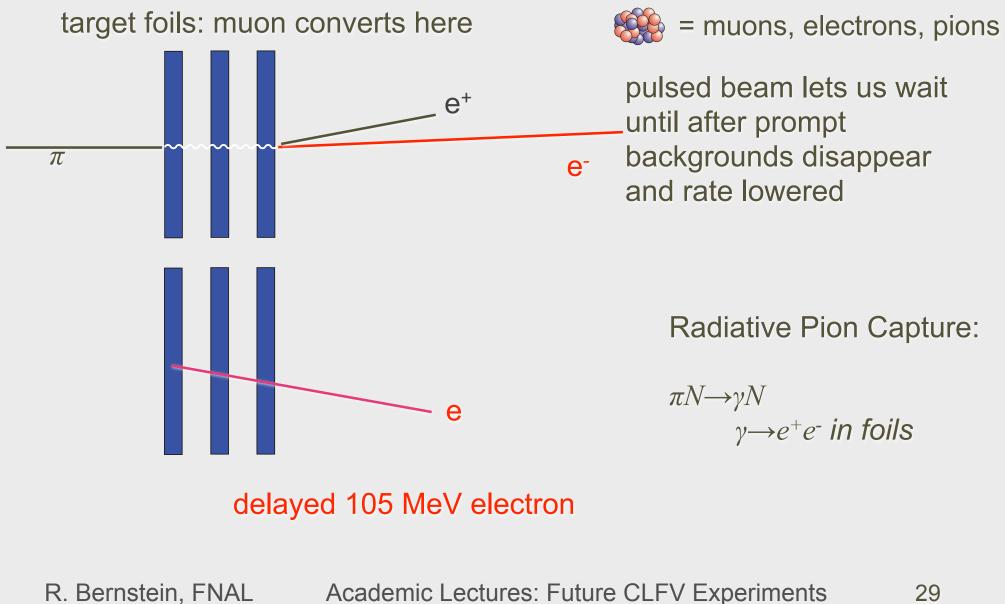




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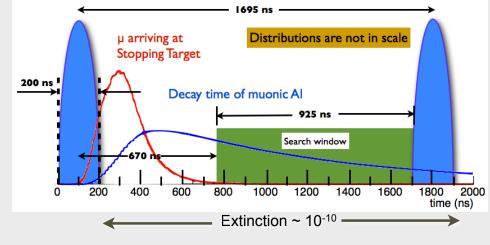




#### **Pulsed Beam Structure**

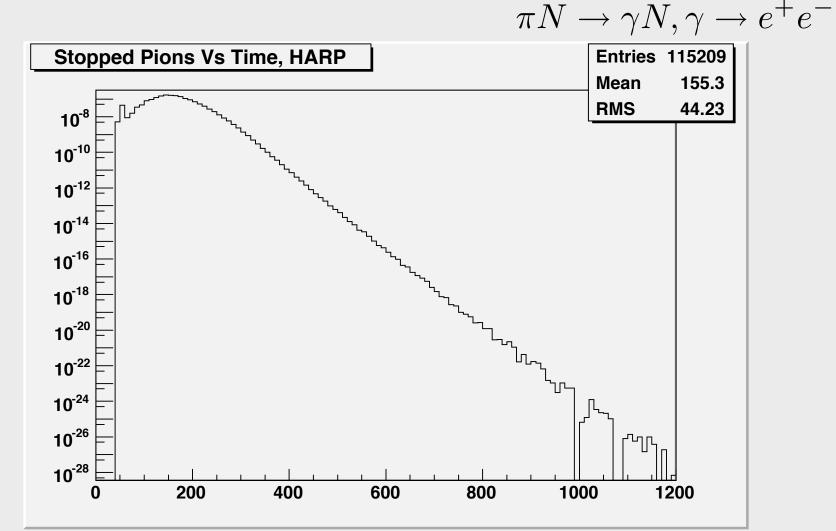
- Tied to prompt rate and machine: FNAL "perfect"
- Want pulse duration <<  $\tau_{\mu}^{\rm Al}$  , pulse separation  $\thickapprox \tau_{\mu}^{\rm Al}$ 
  - FNAL Debuncher has circumference 1.7 $\mu$ sec , ~x2 $au_{\mu}^{
    m Al}$
- Extinction between pulses < 10<sup>-10</sup> needed





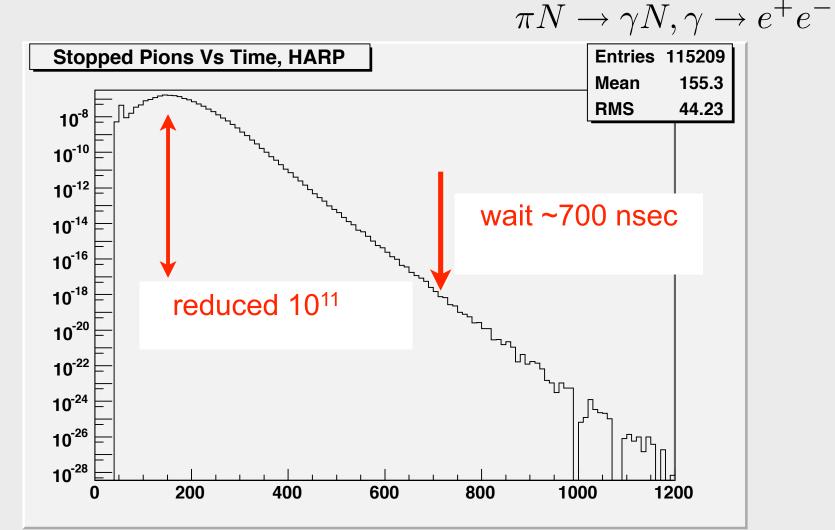
 10<sup>-10</sup> based on simulation of prompt backgrounds and beamline

# Pulsed Beam Structure and Radiative $\pi$ Capture



need a beam that lets us wait this long: pulsed with long spacing

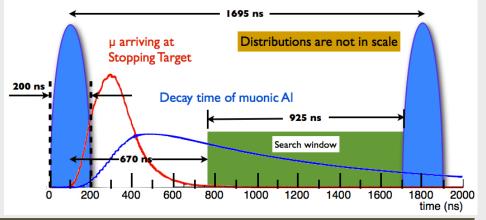
# Pulsed Beam Structure and Radiative $\pi$ Capture



need a beam that lets us wait this long: pulsed with long spacing

## Prompt Background and Choice of Z

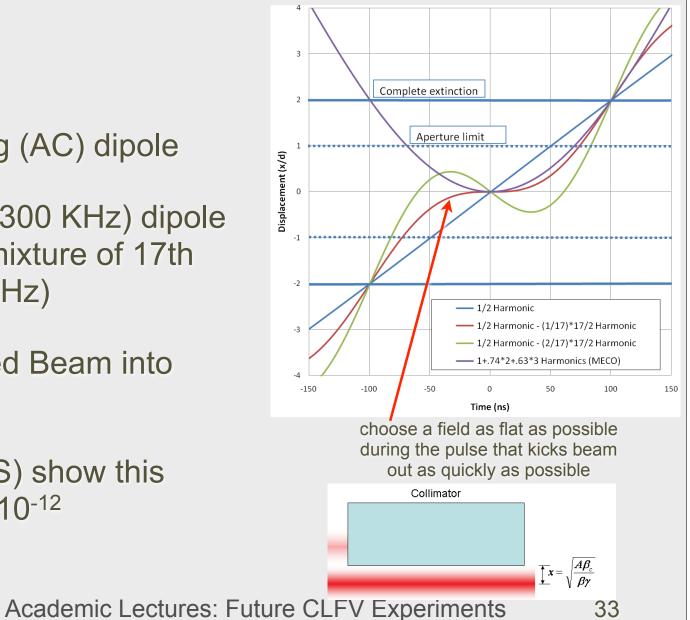
choose Z based on tradeoff between rate and lifetime: longer lived reduces prompt backgrounds

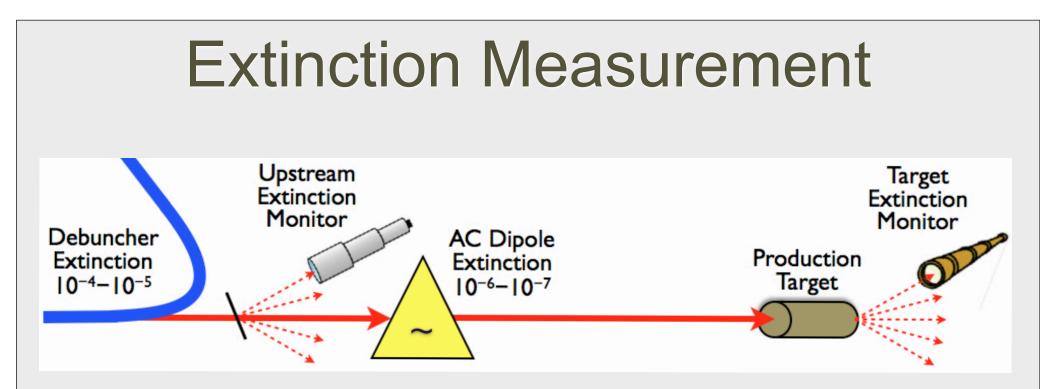


Nucleus	R <sub>µe</sub> (Z) / R <sub>µe</sub> (AI)	Bound Lifetime	Conversion Energy
AI(13,27)	1.0	864 nsec	104.96 MeV
Ti(22,~48)	1.7	328 nsec	104.18 MeV
Au(79,~197)	~0.8-1.5	72.6 nsec	95.56 MeV

## **Extinction Scheme**

- External: oscillating (AC) dipole
  - high frequency (300 KHz) dipole with smaller admixture of 17th harmonic (5.1 MHz)
  - Sweep Unwanted Beam into collimators
- Calculations (MARS) show this combination gets ~10<sup>-12</sup>

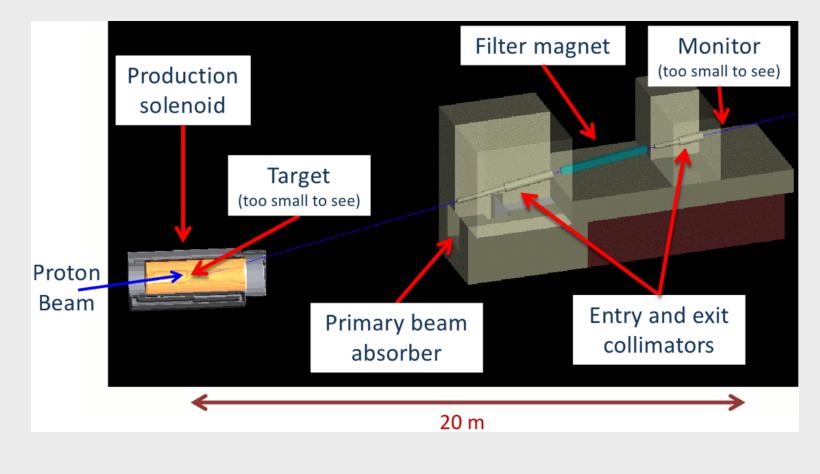




- Beam Formation and AC-Dipole provide extinction
- Measure with:
  - Thin foils in 8 GeV transport line (fast feedback on machine performance)
  - Off-axis telescope looking at production target (time scale of hour)
    - pixel-based telescope looking at few GeV protons

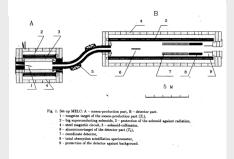
### **Extinction Detector**

- Si pixel telescope spectrometer with narrow view of target
- Measure extinction to 10<sup>-10</sup> in ~1 hour

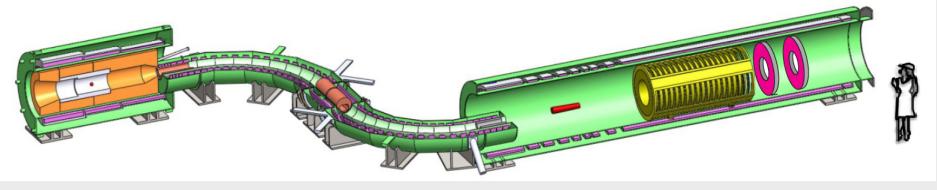


## Mu2e Overview

#### V. Lobashev, MELC 1992:



• *Production*: Magnetic mirror traps  $\pi$ 's, which decay into accepted  $\mu$ 's



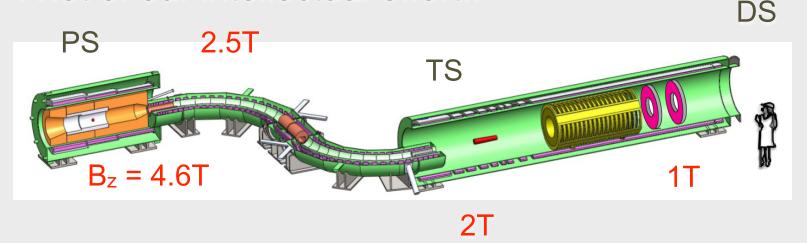
• *Transport:* S-curve eliminates backgrounds and sign-selects

 Detector:
 Stopping Target, Tracking and Calorimeter

entire system in vacuum < 10<sup>-4</sup> torr

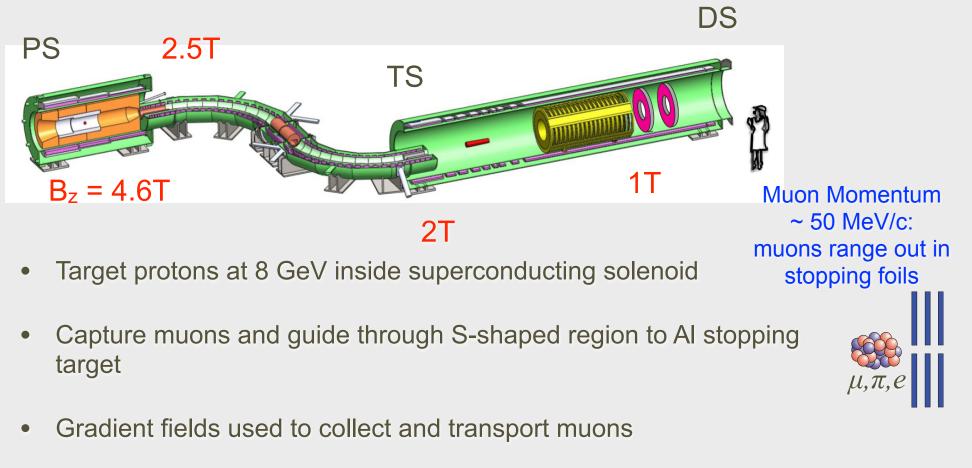
## Gradient Fields in Mu2e

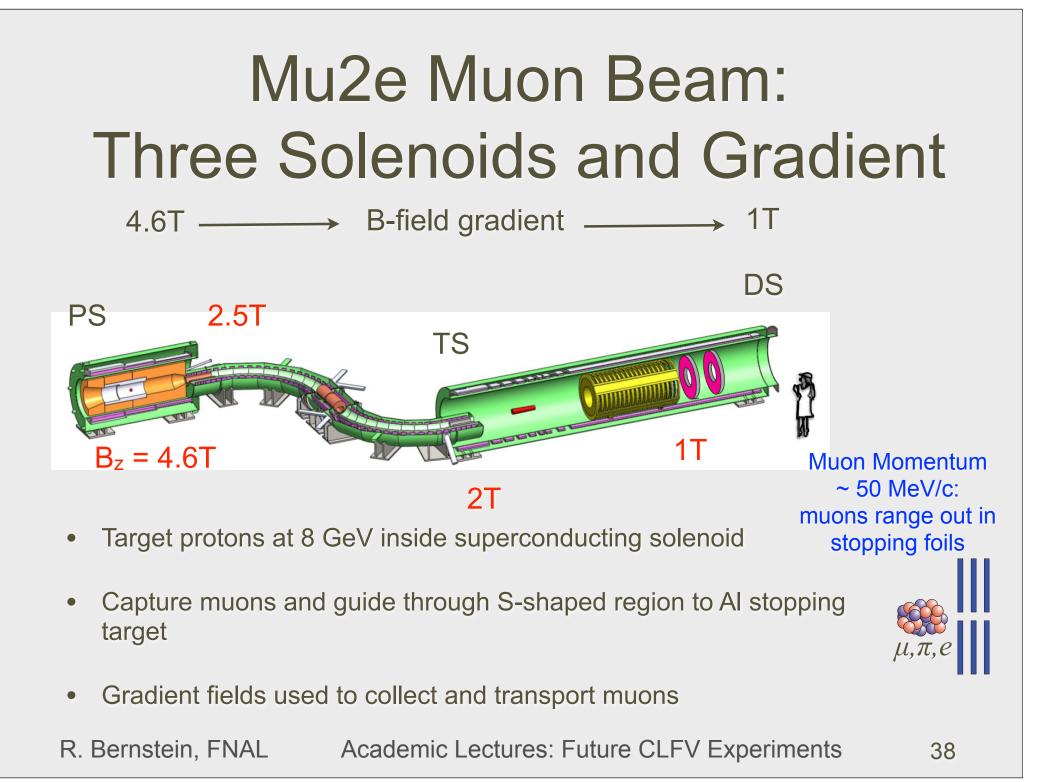
- Play a vital role throughout the design
- A lot of our intellectual effort!!

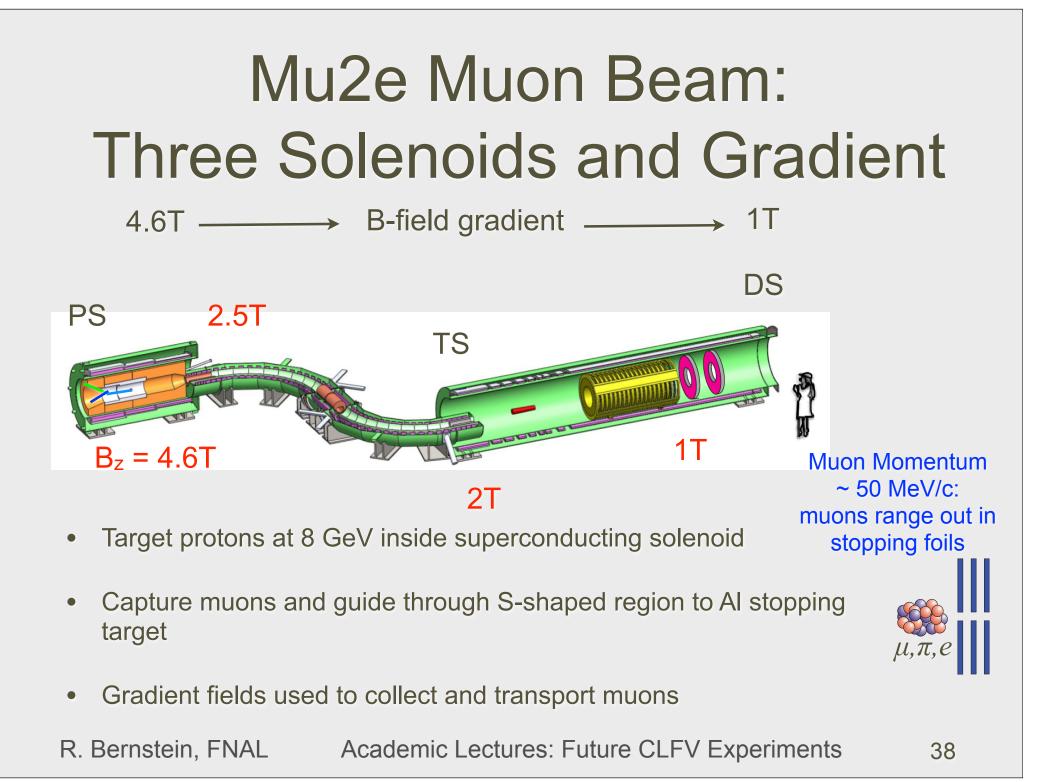


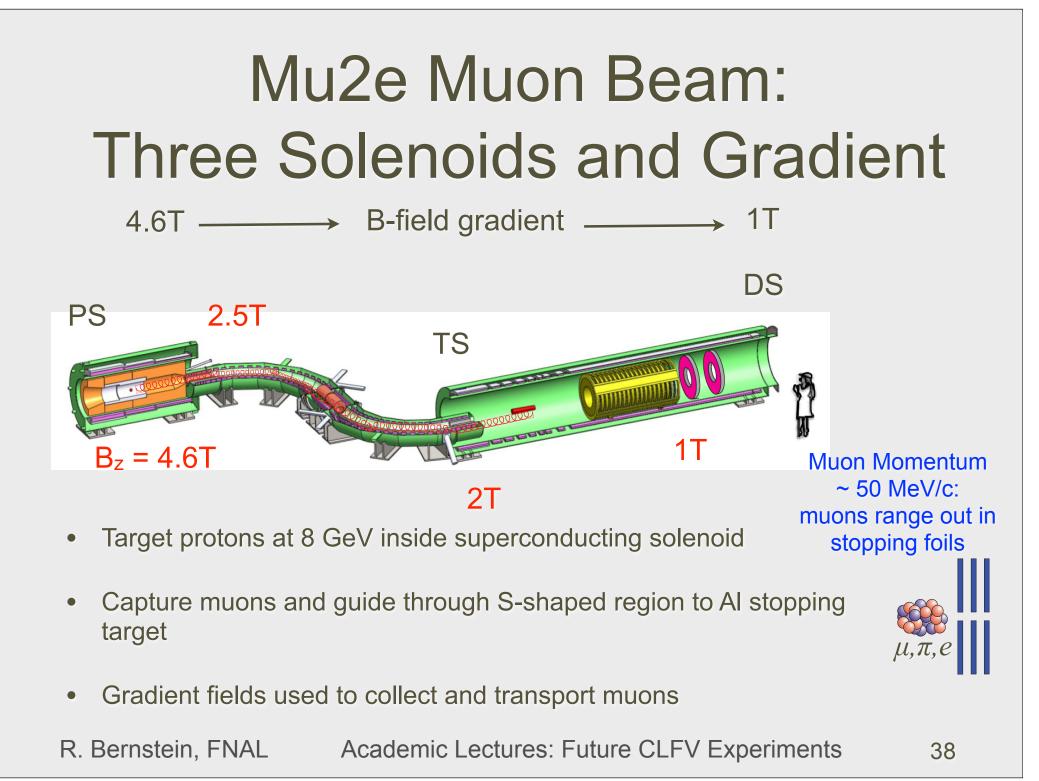
- "push" muons out of PS into TS and into DS so we can study them
- keep particles from spiraling around, arriving late
- conversions are isotropic in stopping target; the gradient over stopping target "reflects" backward going muons and nearly doubles the acceptance

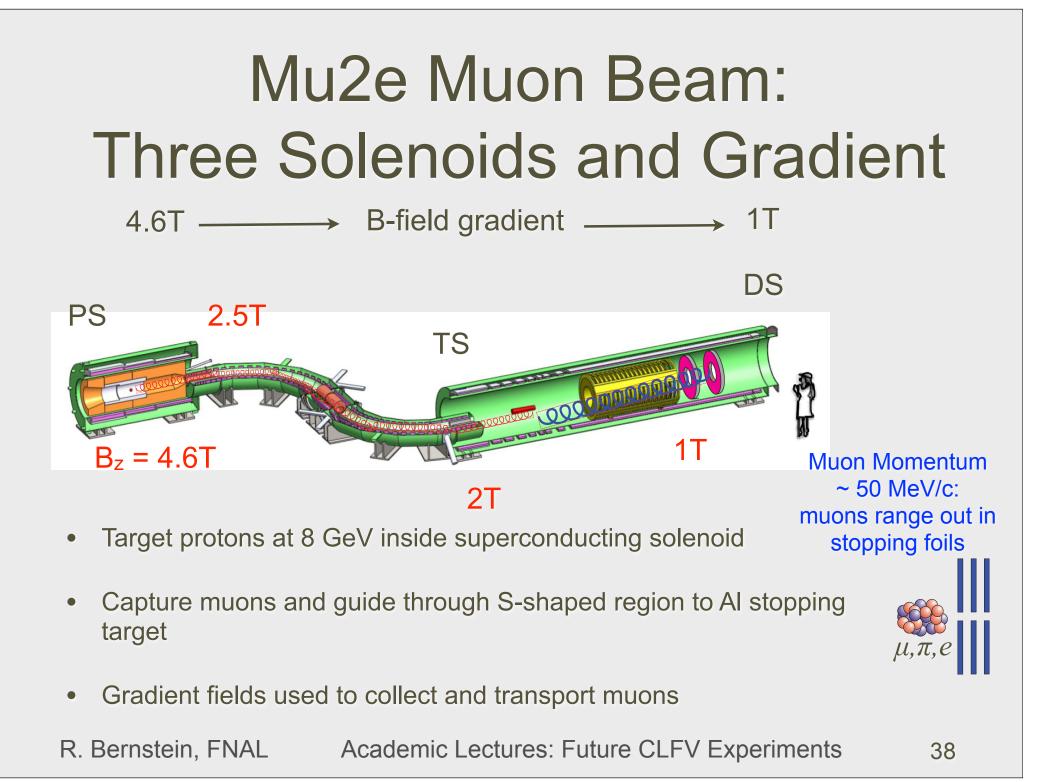
## Mu2e Muon Beam: Three Solenoids and Gradient

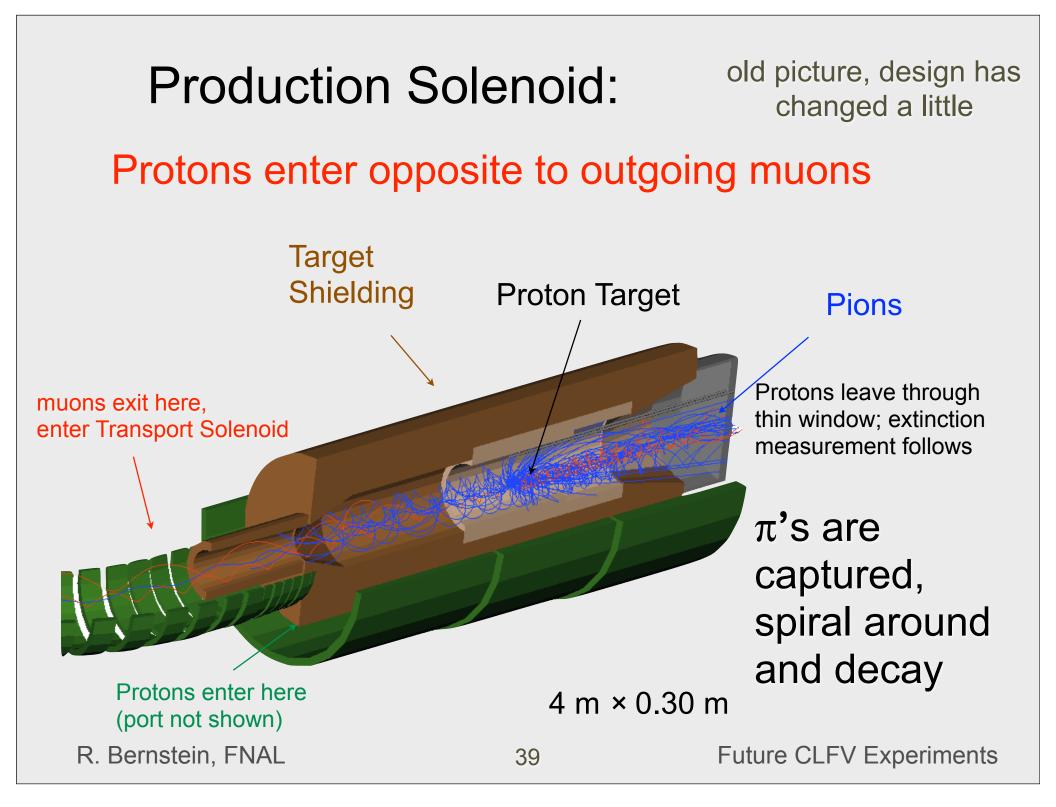








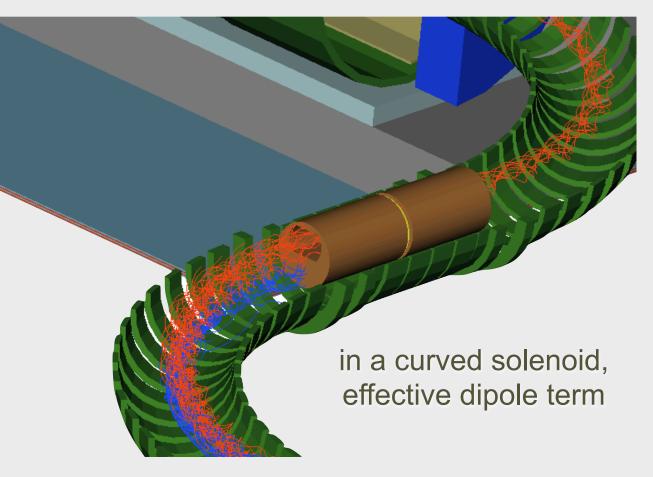




## **Transport Solenoid**

old picture, design has changed a little

- Curved solenoid eliminates line-of-sight transport of photons and neutrons
- Curvature drift and collimators sign and momentum select beam



13.1 m along axis × ~0.25 m

R. Bernstein, FNAL

Future CLFV Experiments

#### Detector Solenoid octagonal tracker surrounding central region:

radius of helix proportional to momentum, p=qBR old picture, calorimeter design has changed

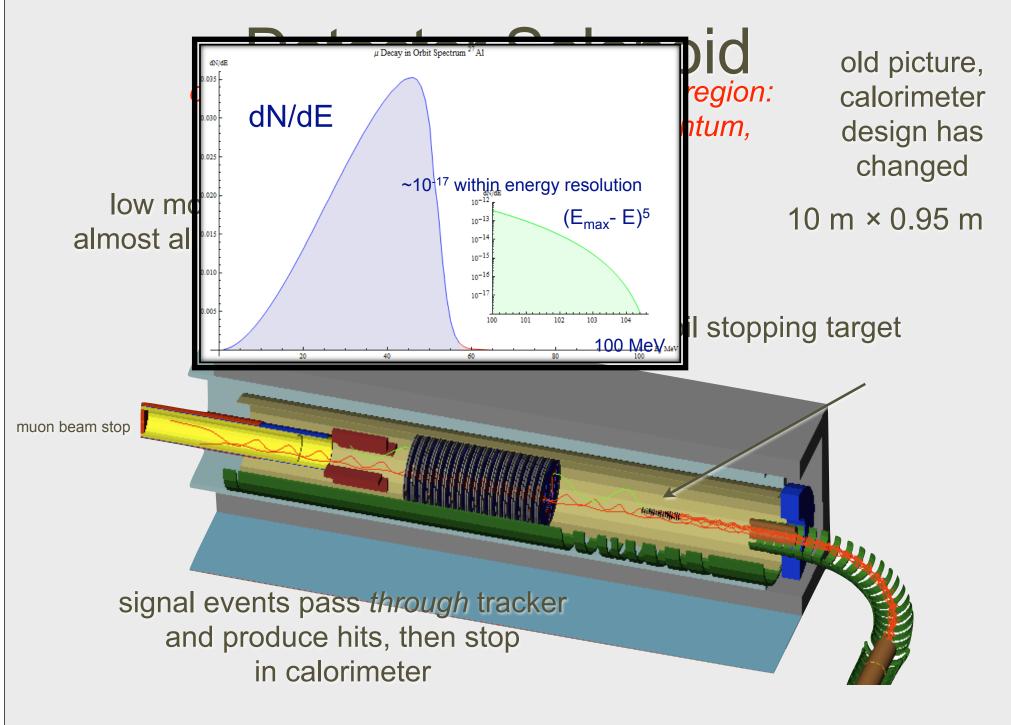
low momentum particles and almost all DIO background passes down center

10 m × 0.95 m

Al foil stopping target

muon beam stop

signal events pass *through* tracker and produce hits, then stop in calorimeter



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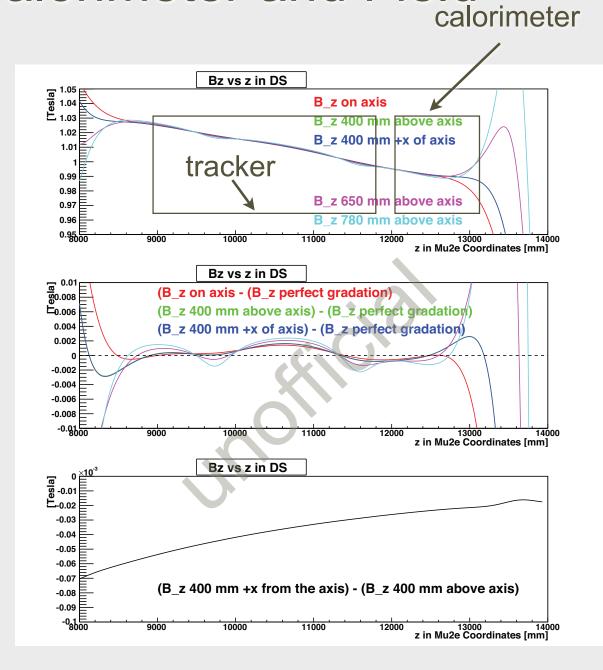
## **Sculpting Magnetic Fields**

- Overall, the field is solenoidal steadily decreasing until we get to the tracker and then keep it as constant as possible
- This also "pushes" particles along the system
  - avoids trapped particles looping around and ending up getting to the detector late
- After that, tons of details

#### Tracker, Calorimeter and Field

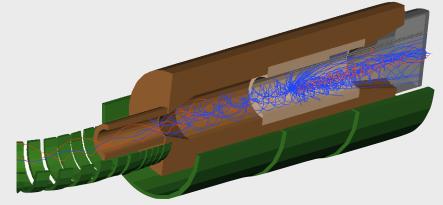
- Actually put slight gradient over tracker region to minimize small negative gradients and trapped particles
- Can see coil structure
- >100 Personyears

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## **Sculpting Magnetic Fields**



- In PS:
  - proton beam enters in opposite direction from solenoid system
  - extinction measurement out the back
  - solenoidal field increases along proton direction, creating a magnetic mirror, but ~80-85% of flux from backwards going pions
    - cross-sections are poorly known (+- 20%)

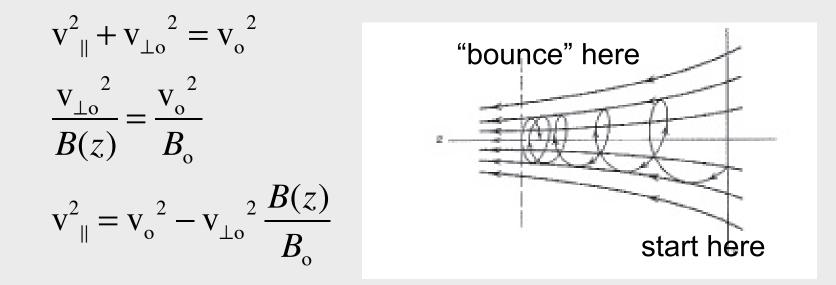
# Magnetic Mirror

- Magnetic Fields do no work! (ever hear that?)
- See Jackson, 2nd Ed. Sec. 12.4. If the field changes sufficiently slowly,

 $Ba^{2}$  $p_{\perp}^{2}/B$  $\gamma\mu$  (the magnetic moment of the current loop)

#### are adiabatic invariants

### **Therefore for Our Solenoids**



as *B* grows, V  $_{\parallel}$  goes to zero and the particle turns around with constant  $\mid \vec{p} \mid -$  a magnetic mirror

# **Selecting Negative Muons**

• E&M to the rescue:



- Jackson, 2nd Ed., Sec 12.5: particle drifts in Nonuniform, Static Magnetic Fields
- Curve of Solenoid gives "centrifugal acceleration" from an effective electric field

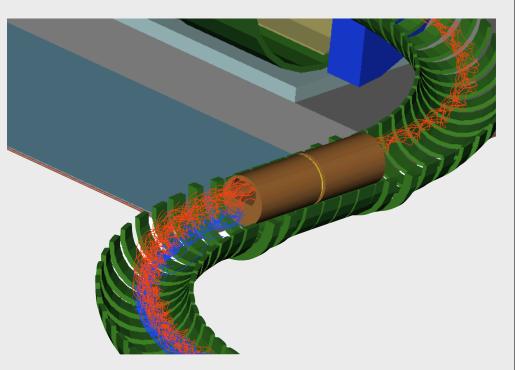
$$\vec{E}_{\text{effective}} = \frac{\gamma m}{e} \frac{\vec{R}}{R^2} v_{\parallel}^2$$

note the sign of the field flips with the sign of the charge

# So This is What Happens:

- Negative muons go one way, positive muons the other
- A rotatable collimator lets us pick one charge or the other: see calibration discussion later
- And the 2nd half of the "S" brings the beam back on axis

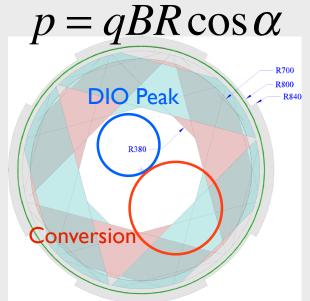
#### 13 m along the axis, 25 cm across



green represents the coils of superconducting cable

# Design and Getting to 10<sup>-17</sup>

- The trick, of course, is not to have to reject 10<sup>17</sup> events
- There are multiple ways to solve this problem.
- Mu2e:
  - use a central hole
  - only see ~few x 10<sup>5</sup> events
  - 10<sup>5</sup> << 10<sup>17</sup>

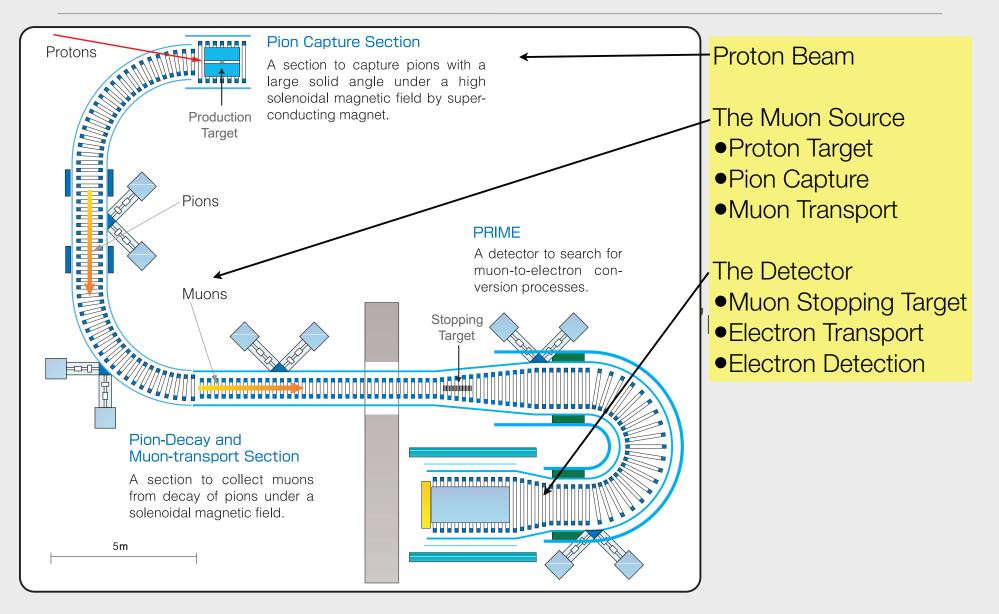


DIO's up to ~ 80 MeV/c stay in central hole; conversions seen by tracker

## Theme and Variations: COMET

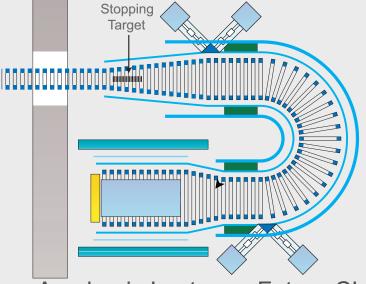
• Here's another way: (not as good but I'm biased)

## **Theme and Variations: COMET**



## 2nd Bend

- DIO's below some momentum hit walls of solenoid and never make it to the tracker
- Tracker has no hole
- But a "DIO-blocker" is needed inside bend, creating accidental activity and reducing acceptance; design not final and effect not included



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## For the Astute

- You'll notice I said the second part of the Mu2e "S" brought the muons back on axis
- COMET has a C: are the muons drifting off somewhere?
  - No, they have (IM¬HO) a complicated dipole correction system 1(s)p(s-1)

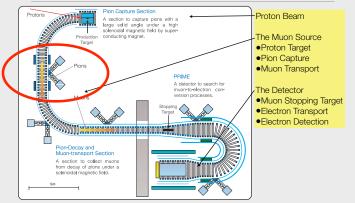
$$D(s) = \frac{1}{qB} \left(\frac{s}{R}\right) \frac{p}{2} \left(\cos\theta + \frac{1}{\cos\theta}\right)$$

apply compensating dipole field

$$\mathbf{B} = \frac{1}{qR} \frac{p_0}{2} \left( \cos \theta_0 + \frac{1}{\cos \theta_0} \right)$$

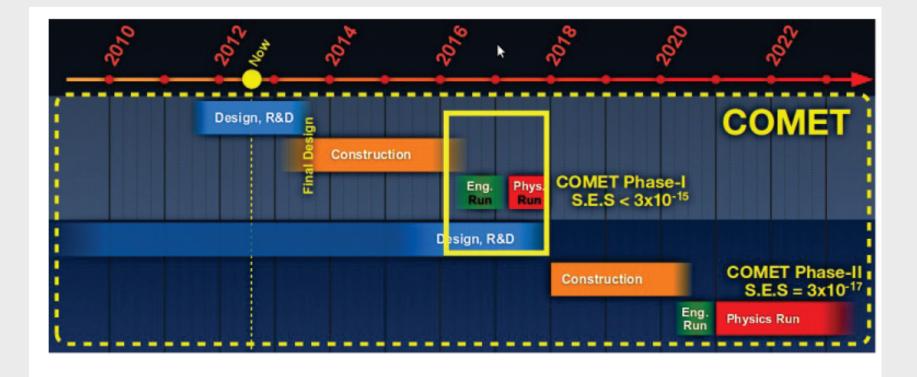
# **COMET** Status

- Broken into two phases:
  - Phase I: up through central bend



- Want to do measurements of flux with one detector and a second detector to do ~x100 better than SINDRUM, same style of cylindrical detector as SINDRUM
- Phase II: full detector as shown >=2021
- Design of Phase I in progress
  - a test coil is in the purchase process

## **COMET Schedule**



#### Mu2e Schedule

