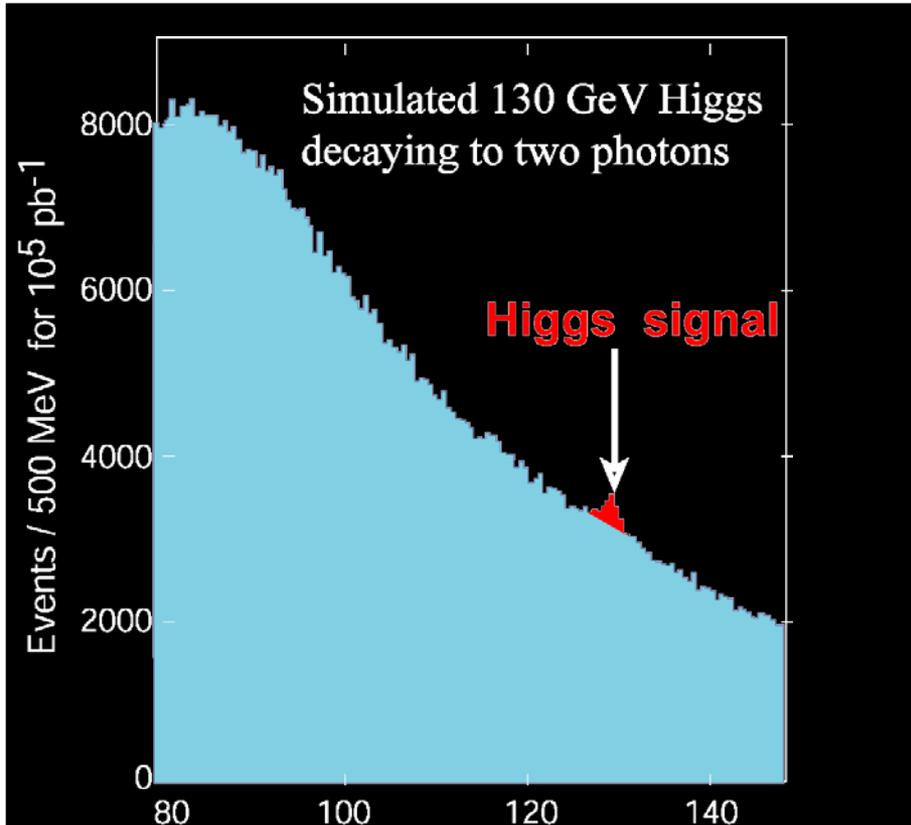


# Calorimetry Lecture 3: Using Calorimeter Information



Jane Nachtman  
University of Iowa

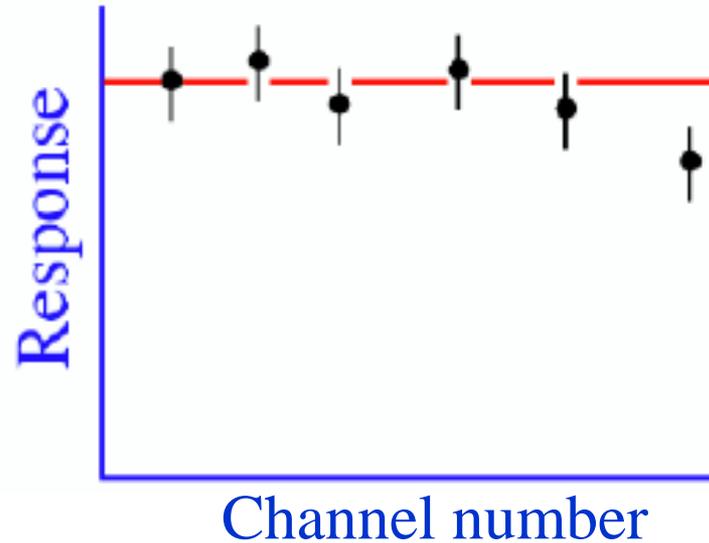
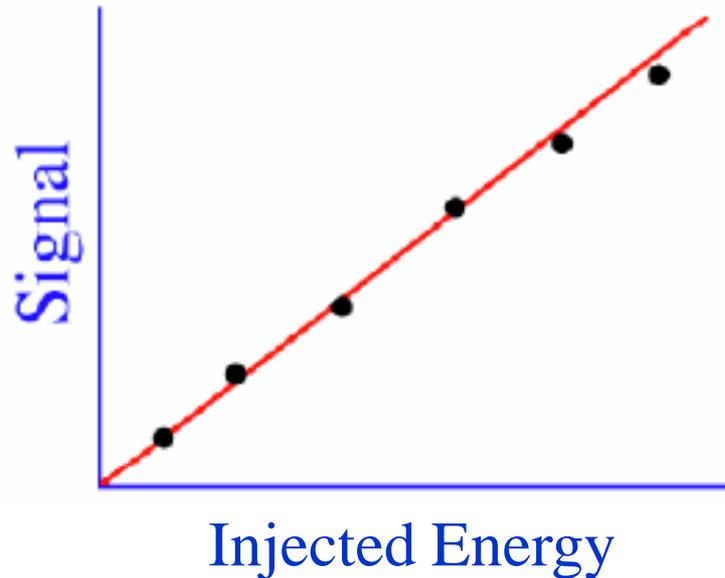
CERN/Fermilab  
summer school  
August 19, 2010

*Thanks to Beate Heinemann, Chris Tully, Joanna Weng, ICHEP speakers!*

# Topics in Lecture 3

- Using calorimeter information
  - Calibration
  - Complementarity of tracking and calorimetry
- Reconstruction of jets
  - Algorithms
  - Jet Energy Corrections

# Calibration and Linearity



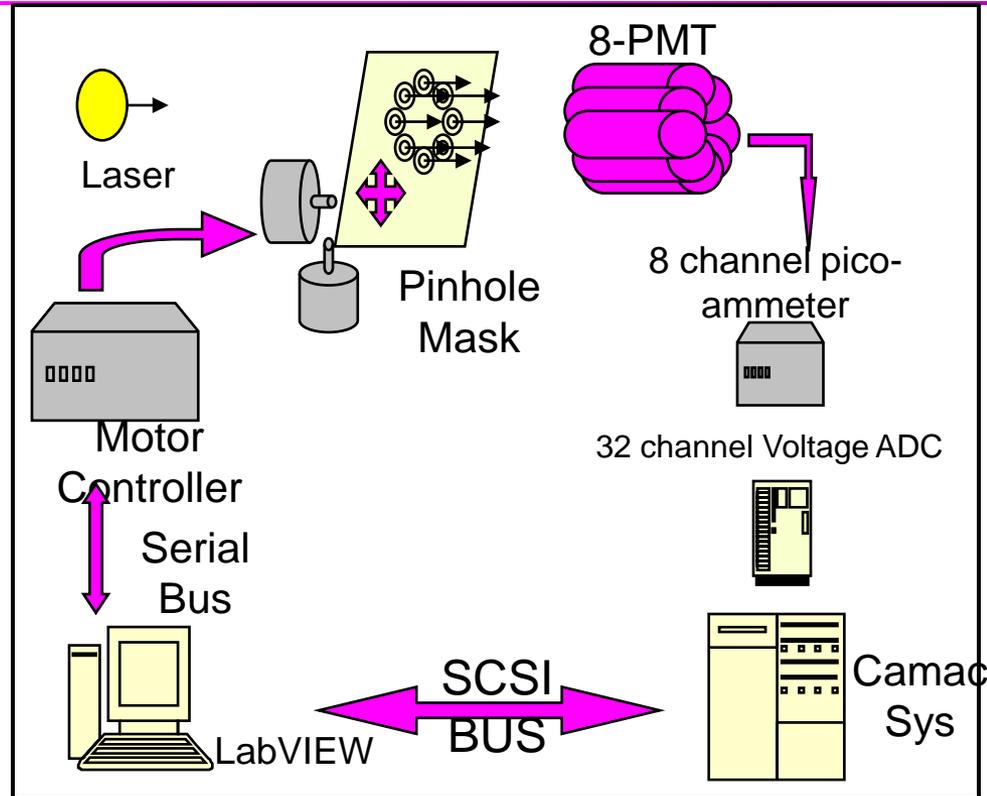
- Goal : uniform and known response to a given calorimeter signal
- For example, signal (charge) from detector is in pC, digitized to ADC counts
  - want linear response
  - channel-to-channel differences : leakage, upstream material, electronics
- Calibrations:
  - Relative calibration normalizes the response between all channels
  - Absolute calibration translates it to energy units (from ADC counts)<sub>3</sub>
- How-to : testbeam, electronics calibration, in-situ, simulation

# To get to physics, first must calibrate

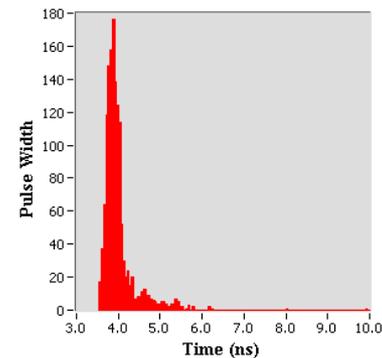
- Component calibration
  - For example, all PMT's are tested standalone
- Testbeam – operate detector (or part of) in a known-energy, known-species beam
  - In addition to R&D for new detectors, provide a testbench for the final modules of the calorimeter
- In-situ calibration
  - Pulse detector with known energy, measure response
  - Cosmic muons, single particles
- Physics object calibration
  - “tag and probe”, dijet balance, photon+jet balance,  $W$  in top events

# Component testing and calibration

- Example – PMT's for CMS HCAL (HF)
  - Test station – dark box, laser input
  - Individual testing, relative calibration
  - PMT's characterized, data put into database for later calibration input:
    - Double-pulse linearity,
    - Gain vs HV
    - Single photoelectron spectrum
    - X-Y scan (spatial uniformity)
    - Lifetime, pulse width, rise time
    - Transit time and spread
    - Anode dark current
    - Relative gain coupled with cathode sensitivity
    - Pulse linearity
    - Quality control decision
- All (or as many as possible) components of detector are calibrated long before they are integrated into detector

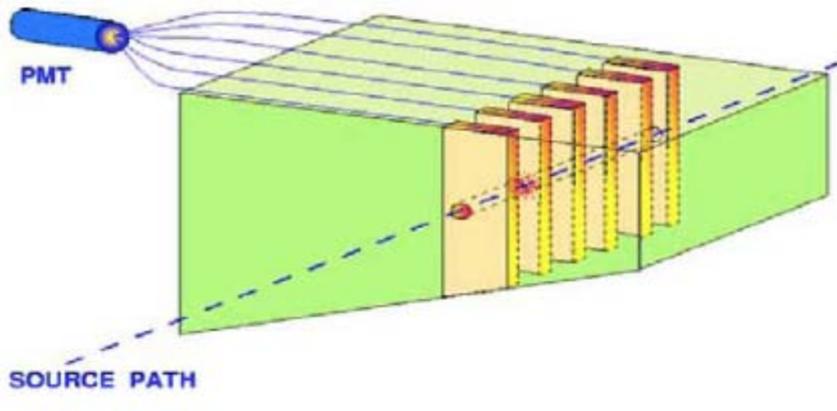


Pulse width  
for 1550  
PMT's

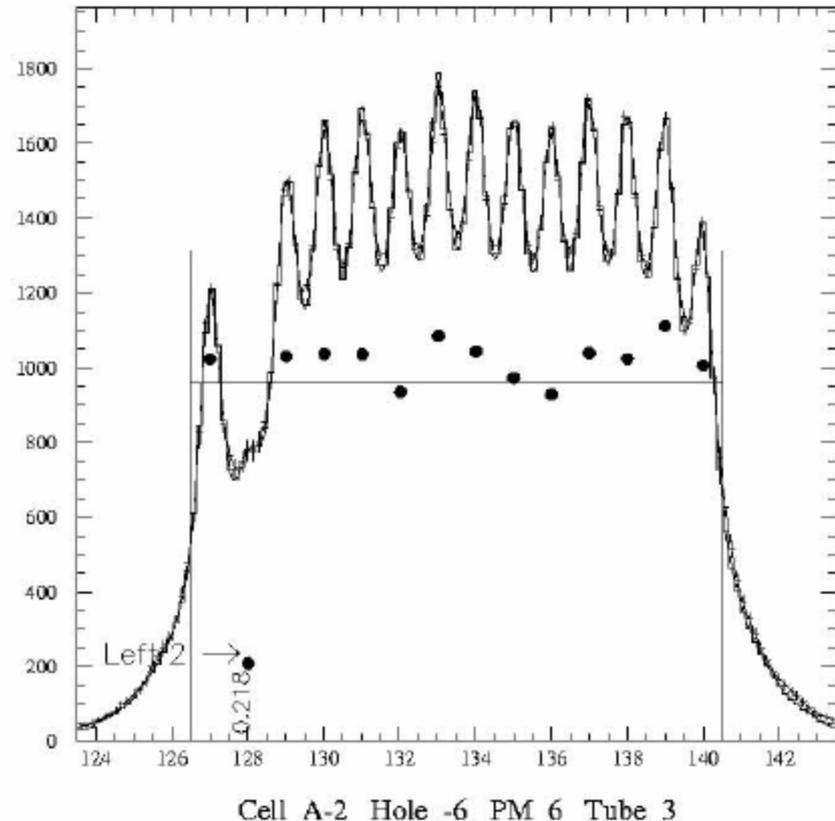


# In-situ Detector/Electronics Calibration

- Example: inject known-energy pulse (eg from radioactive source or laser), then normalize readout of all channels
- Example: Atlas and CMS -- similar methods:



Atlas Source Path

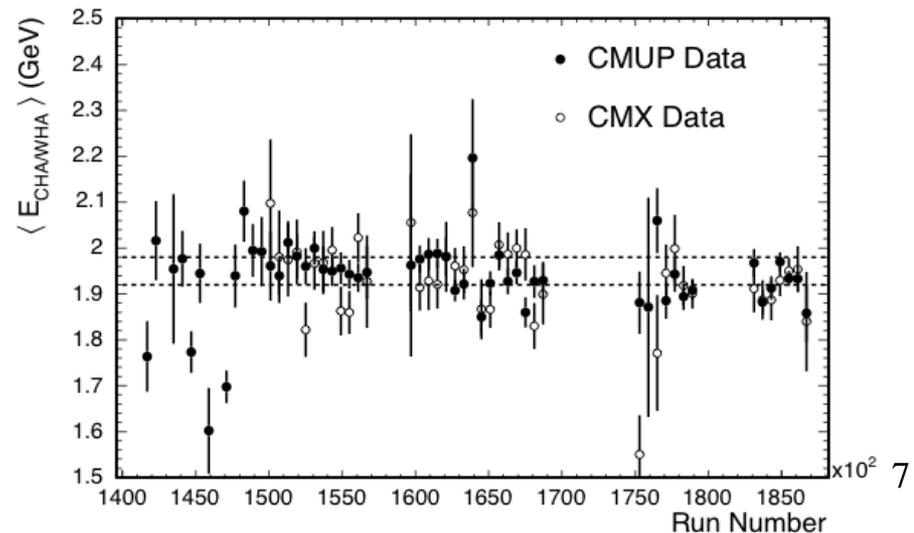
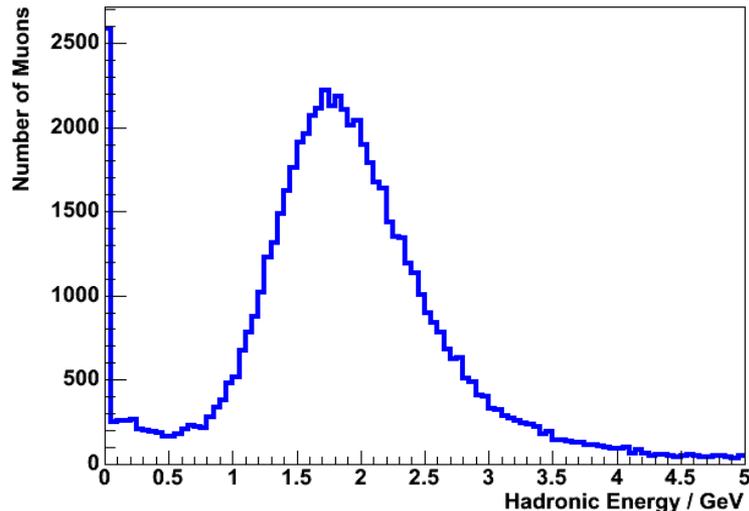


Response by location

# Calibration with Muons

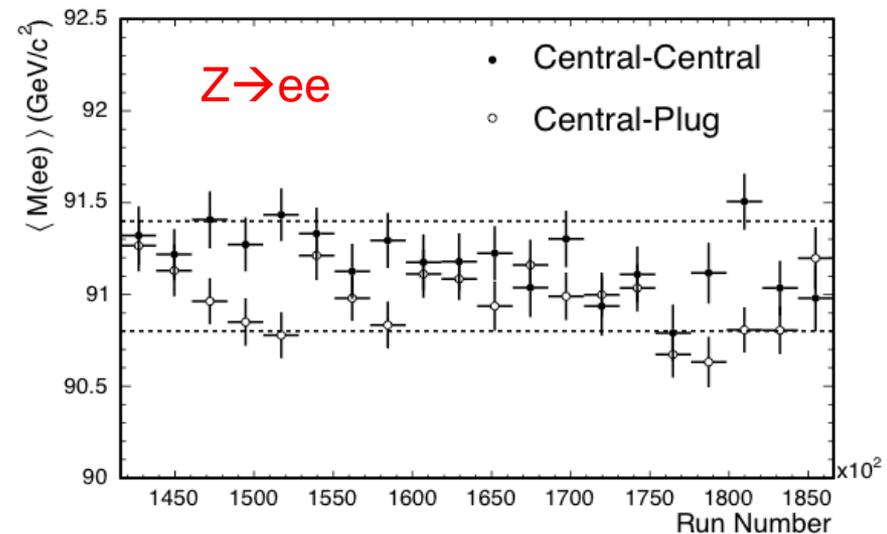
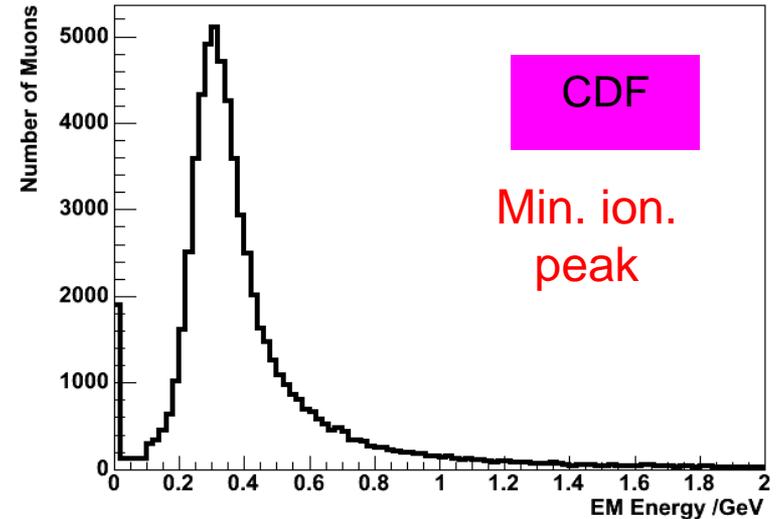
- Use muons from cosmic rays, testbeam, or physics events
  - Will give MIP response in calorimeter cell
  - Equalize channel-to-channel response

- CDF:
  - select muons from  $J/\psi$  and  $W$
  - peak in HAD calo:  $\approx 2$  GeV (in CDF)
- Check time stability



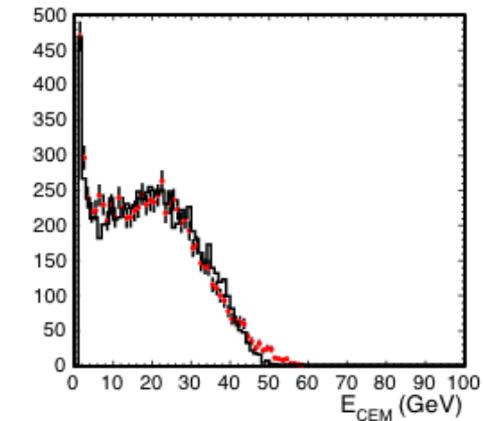
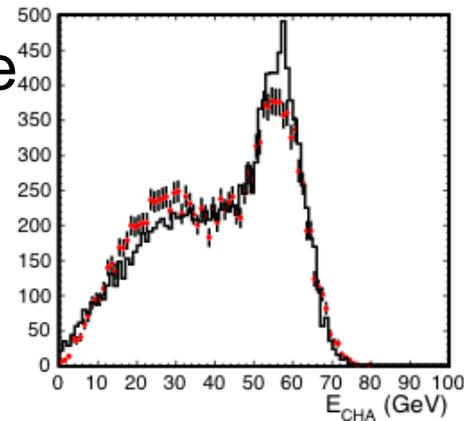
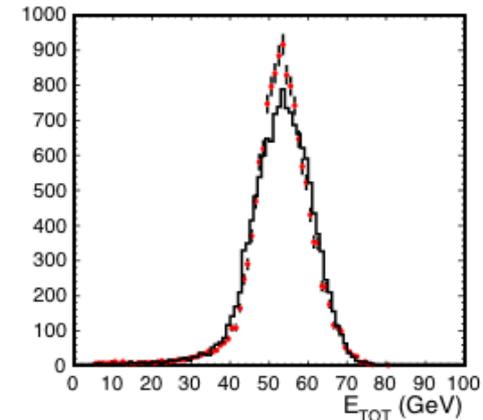
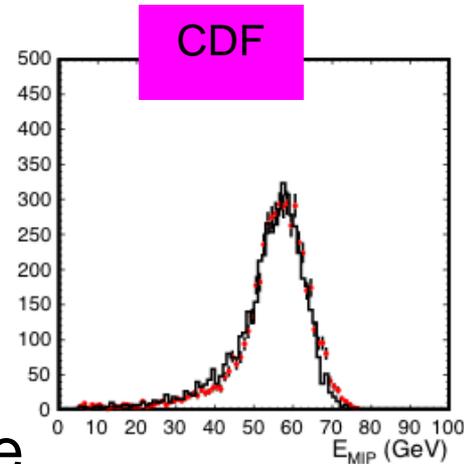
# In Situ Calorimeter Calibration: EM Energy

- MIP peak:
  - CDF → 300 MeV
- $Z \rightarrow ee$  peak:
  - Set absolute EM scale in central and endcap
- E/p for electrons
  - After having calibrated p and material, see response in E



# Single Particle Response Simulation

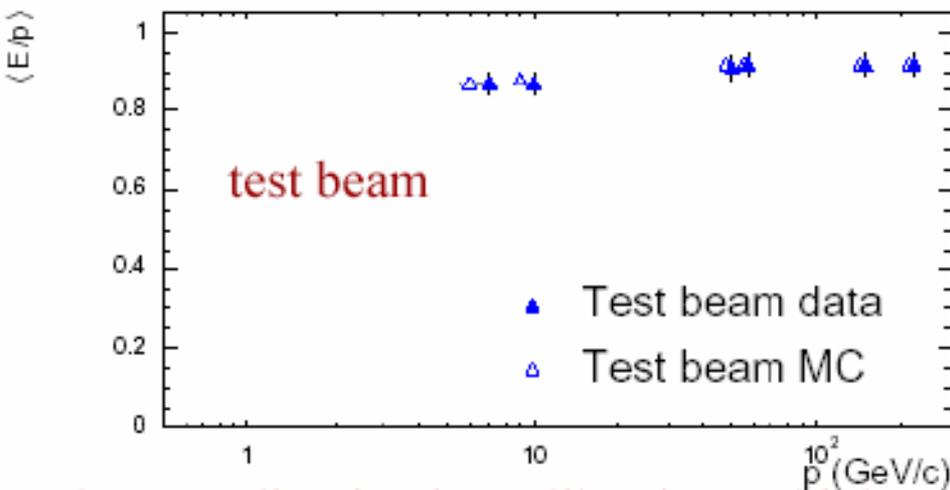
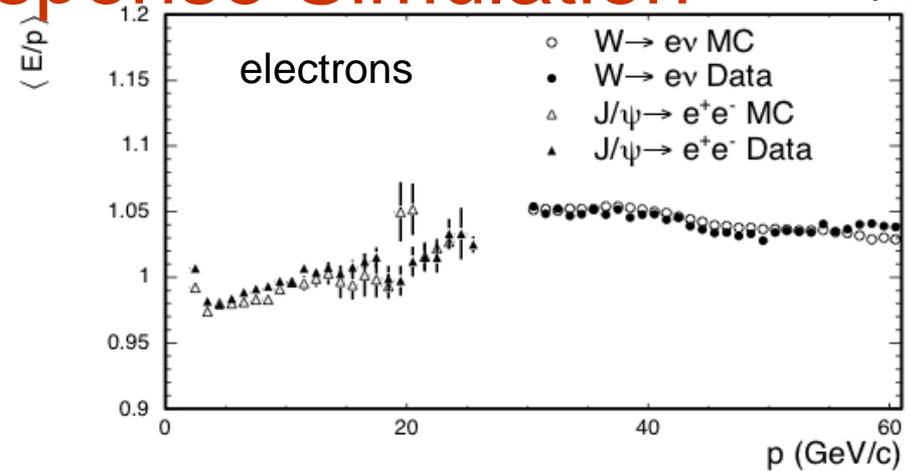
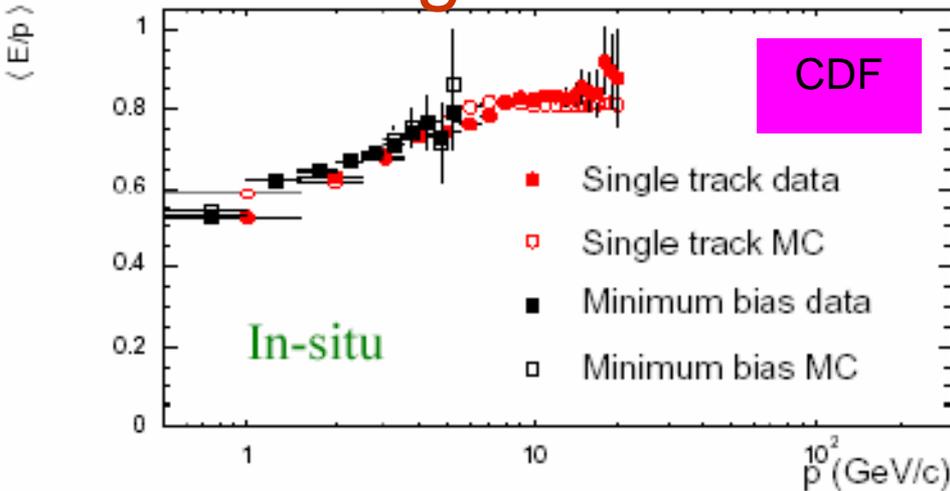
- Single particle response:
  - Measure with test beam
  - In situ:
    - Select “isolated” tracks and measure energy in tower behind them
  - Tune simulation to describe E/p distributions at each p (use  $\pi/p/K$  average mixture in MC)



• Test beam data

— CDF simulation

# Single Particle Response Simulation



Typical jet composition:

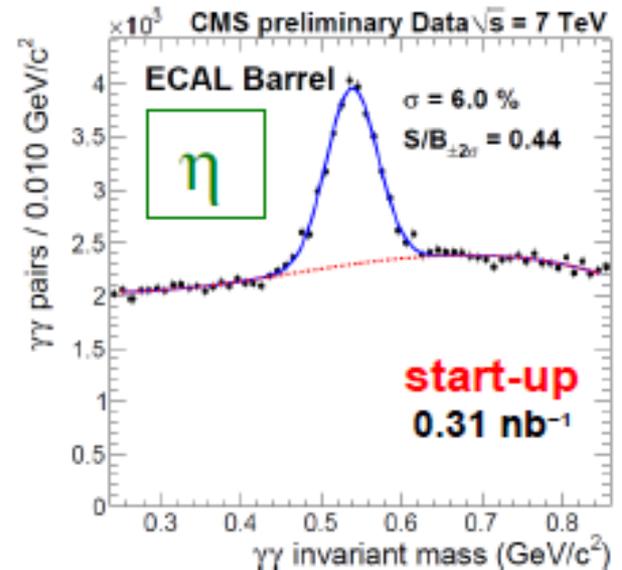
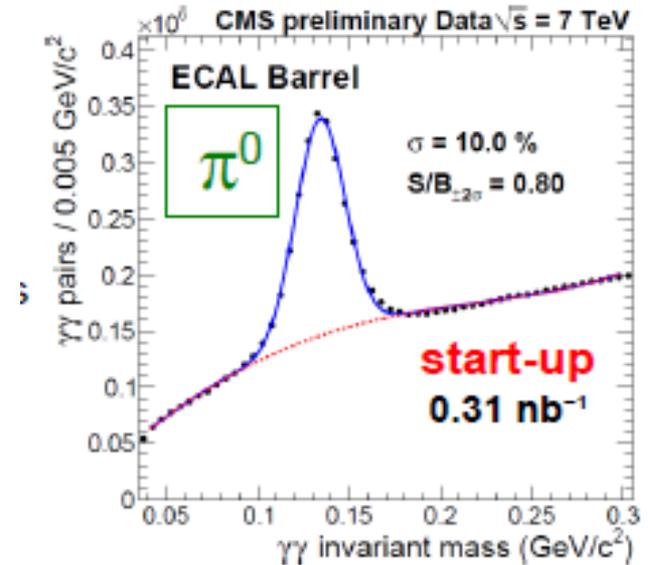
- 60% charged particles
- 10% protons
- 90% pions
- 30% neutral pions ( $\rightarrow \gamma\gamma$ )  
(EM response)
- 10% other (neutrons,...)

- MC models

- Hadron response at low  $p_T$  (in situ data) and high  $p_T$  (test beam data)
- Electron response

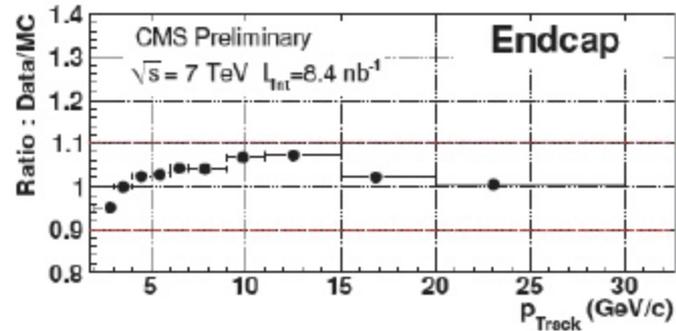
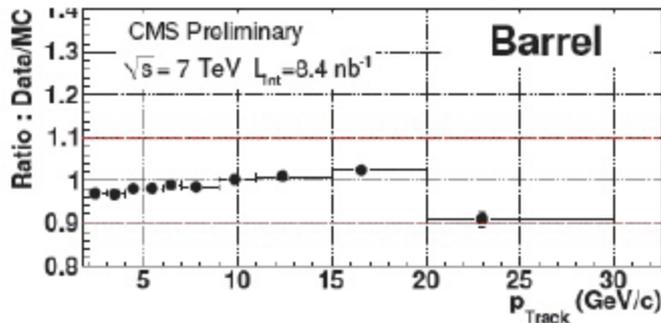
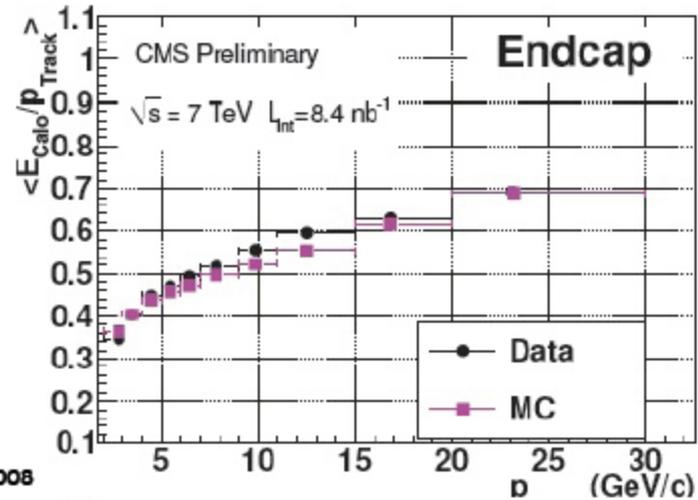
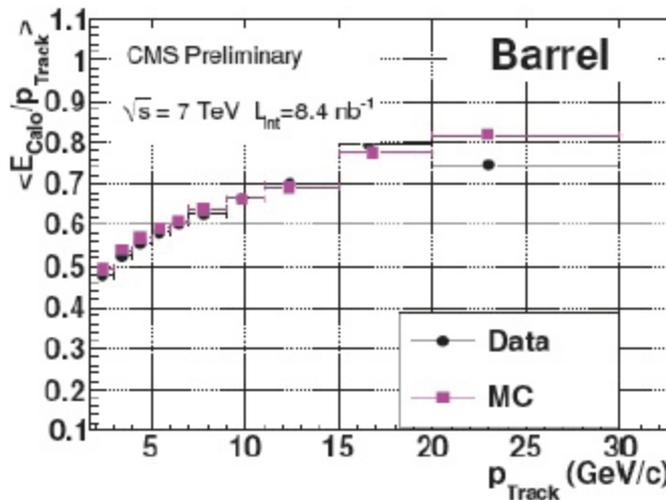
# CMS ECAL calibration

- Startup calibration based on 10 years of test beam and cosmic ray pre-calibration,  $\pi^0$  calibration
- Precision of startup calibration
  - ECAL Barrel 0.5 – 2.2%
    - 1.2% in central region
  - ECAL Endcap 5%
  - Target with 10/pb: 0.5% EB, 1-2% in EE
- Calibration validated by observation of  $\pi^0$  and  $\eta \rightarrow \gamma\gamma$



# Single-particle response in CMS

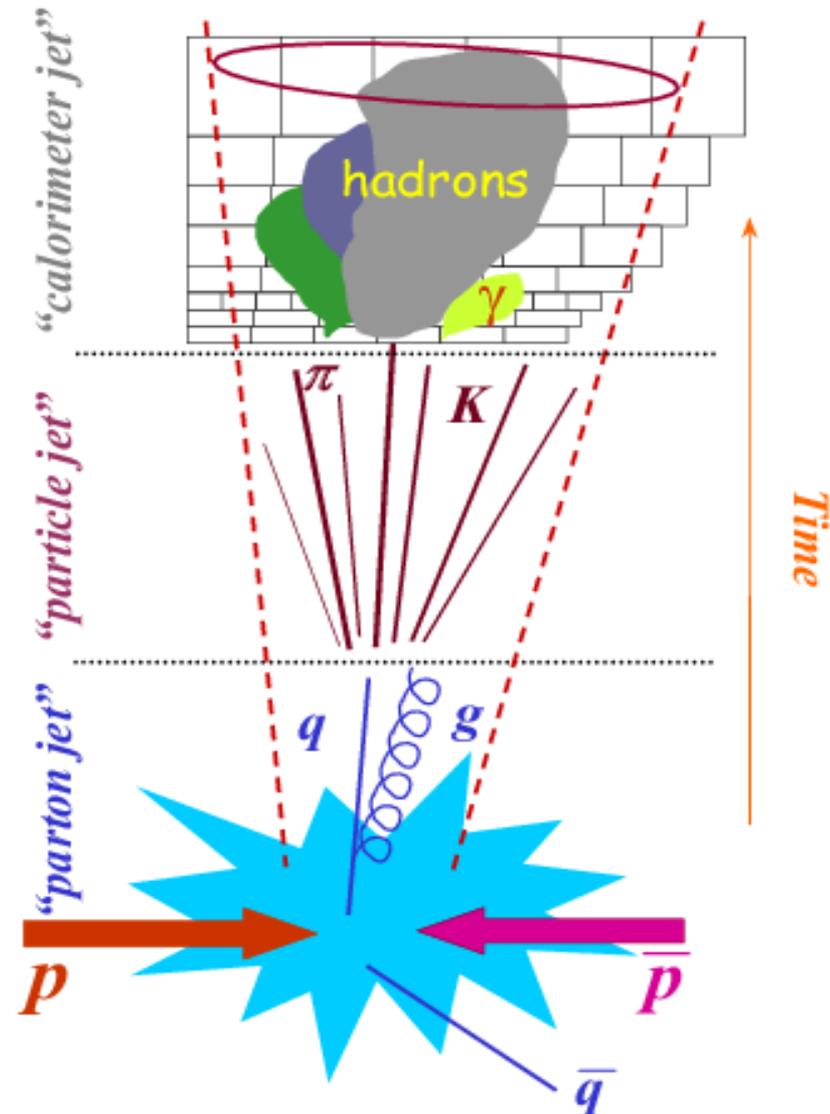
- Compare response of isolated tracks with low ECAL energy in MinBias events with single pions from Monte Carlo



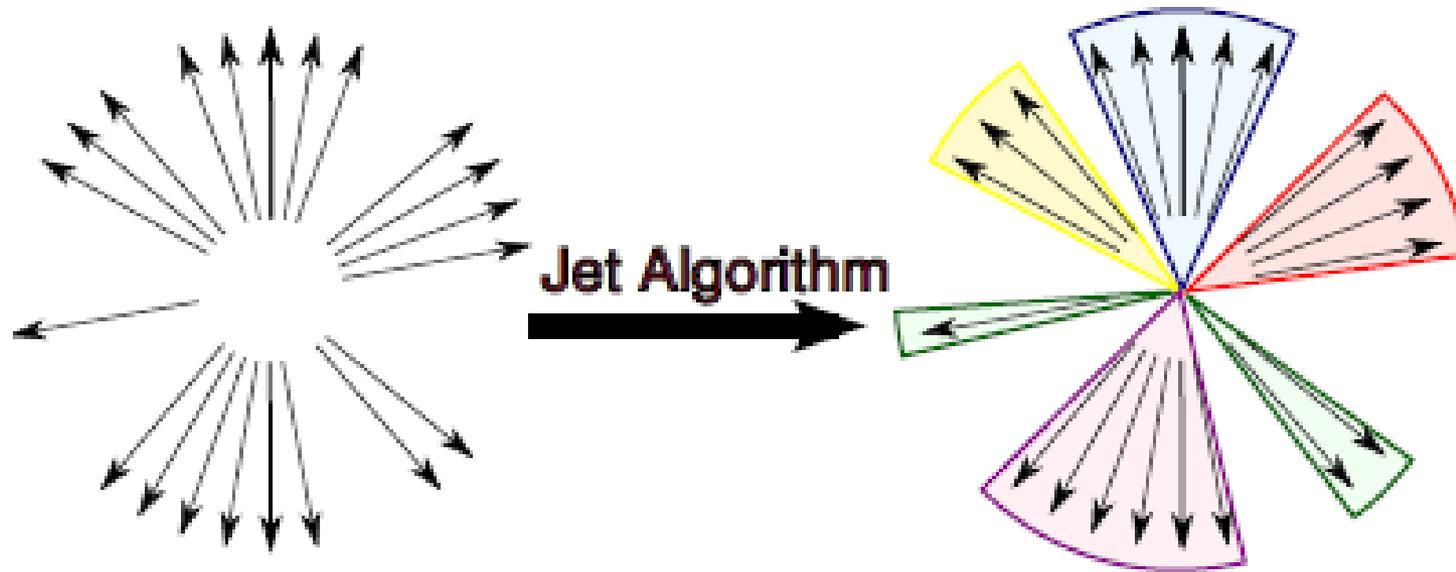
Mean response in Data and MC agree within 2-3% in barrel region  
 In endcap, simulation is lower than data (~4%)

# Jets from Collisions

- QCD interactions → Jets
- Types of Jets
  - Parton level – quarks/gluons from initial collision
  - Hadron level – fragmentation, decay, hadronization produce particles
  - Experimental – what we see in the calorimeter, and how we interpret it
- Goal – take detector information, reconstruct parton level physics



# Jet Algorithms

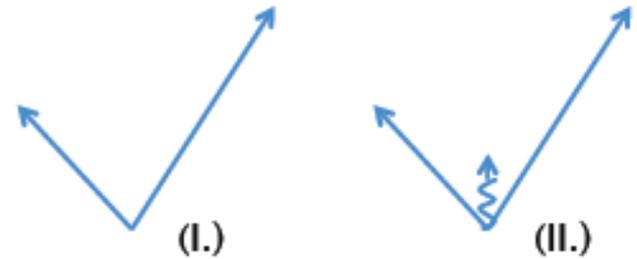


Graphics from  
Kerstin Perez,  
ISSP 2009

- Procedure to turn recorded detector info into jets
  - Or, looking at it from the other way, turn partons into jets
- Constraints:
  - Infrared and collinear safe (see next slide)
  - Invariant under boost (important for hadron colliders)
  - Independent of level (parton, hadron, calorimeter) and detector
  - Easy to implement and use (computer resources), calibrate

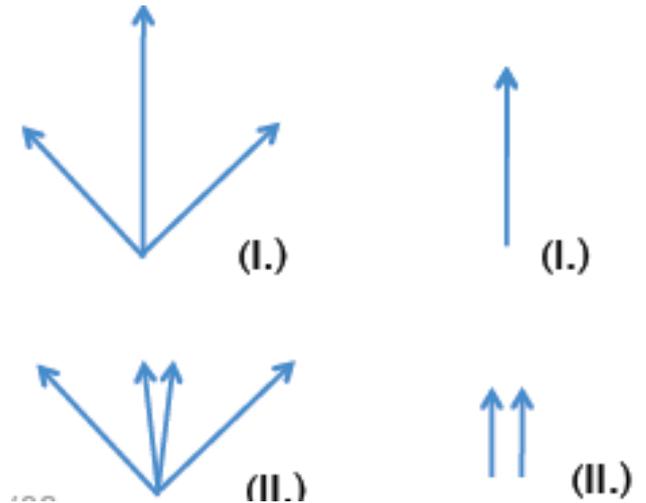
# Technical terms

- Infrared safe – same jets even if one of the partons emits a soft gluon



These situations would have the same jets

- Collinear safe – same jets even if outgoing partons split



# Jet Algorithms used at Hadron Colliders

- Choice of jet algorithms is an involved topic – theorists and experimentalists have been working together for years to find the perfect scheme
  - True to parton-level
  - True to experimental (detector) level
  - Taking into account detector effects, pileup, etc.
- There are many possible algorithms to choose from – we won't cover them all
  - Here are examples from CMS: **Anti-kT, SISCone and kT** jet algorithms:
    - Then, generator jets, calorimeter jets, calorimeter+track, and particle-flow jets for these jet algorithms

# Cone Algorithms

- Cone (traditional)
  - clusters nearby in angular space
  - Problem : seeded – introduces bias especially with pileup
  - Problem : needs merging/overlap scheme, which every experiment implements differently
    - Difficult to compare, feedback to theorists
- If you don't seed the jets, takes  $N 2^N$  time to find jets among  $N$  particles (“unseeded”)
  - unusable at hadron level (think of “simple” event with 100 particles...)
  - reduce to  $N^2 \ln(N)$  time – SIScone algorithm

# JADE → Durham → kT

- kT

- Clusters nearby in momentum space
- Based on JADE or Durham algorithm -- exclusive iterative pairwise clustering scheme
  - JADE algorithm uses test variable  $y_{ij}$ , and a combination procedure.
  - Test if objects  $i$  and  $j$  should be combined according to whether  $y_{ij} < y_{cut}$ .
  - Also, consider next pair to combine (smallest value of  $y_{ij}$ ).
  - Original JADE  $y_{ij} = M_{ij}^2/Q^2$  where  $Q$  is the hard scale (i.e. the centre-of-mass in  $e^+e^-$  annihilation) and  $M_{ij}^2 = 2E_i E_j (1 - \cos \theta_{ij})$ , (invariant mass-squared)
  - Repeated until no objects can be combined further
- Problem with JADE – not IR, collinear safe
- Durham mod -- consists of replacing  $M_{ij}^2$  in test variable by  $k_{Tij}^2$ ,
  - $k_{Tij}^2 = 2\min\{E_i, E_j\}^2 (1 - \cos \theta_{ij})$  -- relative transverse momentum-squared of  $i$  and  $j$ .

# kT and anti-kT

- Advantages of kT
  - Jet identification is unique – no merge/split stage
- Disadvantage of kT
  - Resulting jets are more amorphous, energy calibration difficult (subtraction for UE?), and analysis can be very computer intensive (time grows like  $N^3$ )
- Anti-kT
  - Like kT, only uses  $1/p_T$  as the distance parameter
  - Improves performance with pileup

# Testing Jet Definitions

- See this very nice webpage

<http://www.lpthe.jussieu.fr/~salam/jet-quality/>

→ By M. Cacciari, J. Rojo, G.P. Salam, and G. Soyez  
[arXiv:0810.1304](https://arxiv.org/abs/0810.1304)

→ You choose two jet algorithms, set the parameters, and it compares dijet mass distributions with your conditions

Your input –  
twice for  
comparison

$k_t$ 
 C/A
  anti- $k_t$ 
 SISCone
  C/A-filt

Q:  R = 0.7

$Q_{T=z}^W$ 
  $Q_{W=xv/M}^{1/f}$ 
 x 2

rebin = 2

qq
  gg

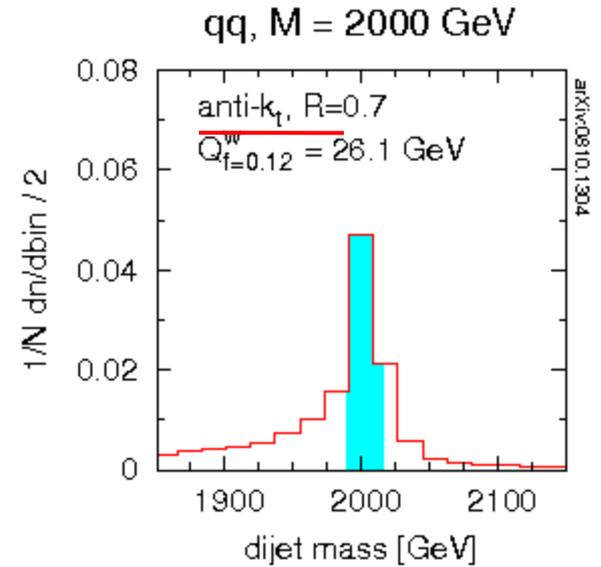
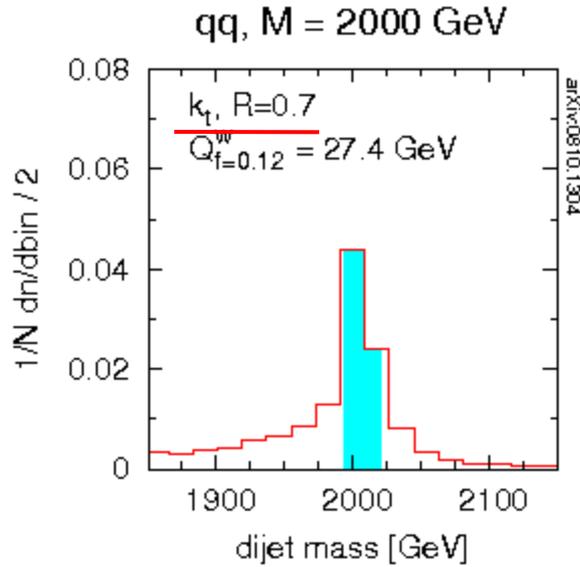
mass = 2000

pileup:  none
  0.05
  0.25  $\text{mb}^{-1}/\text{ev}$

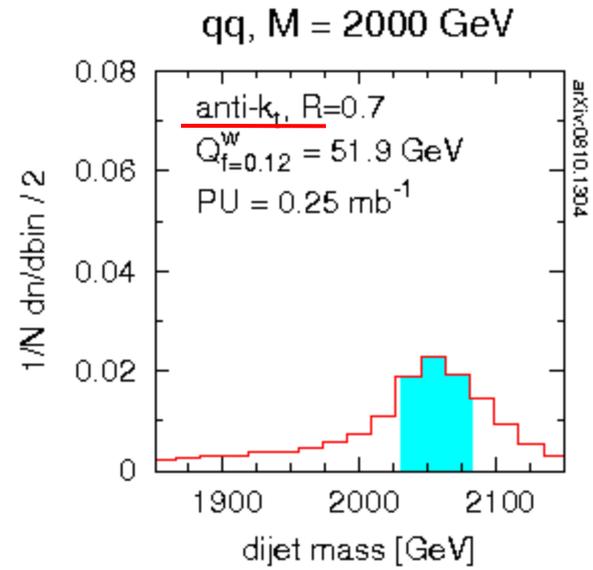
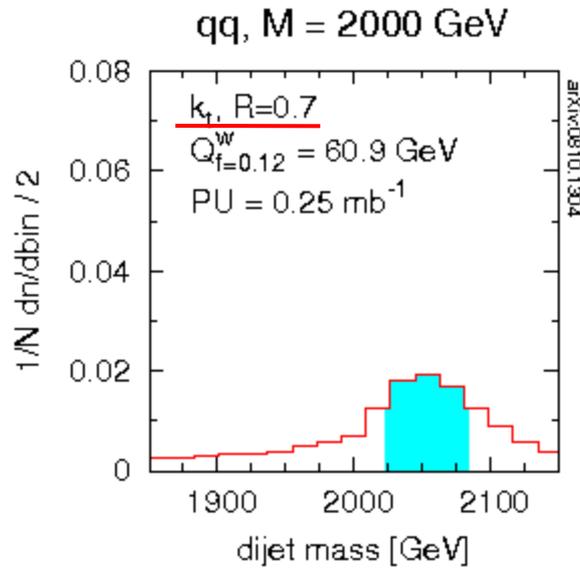
subtraction:

# Example: compare kT to anti-kT

Without Pileup



With pileup



# More on jet algorithms

- Algorithms often designed from parton point of view
- From the detector point of view
  - What information goes into a jet?
    - Calorimeter, tracking
    - “Energy flow”
  - Jet corrections, systematics
  - Integration into experimental software.

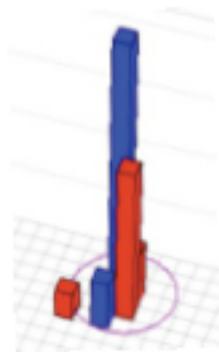
# For Example, CMS Jets

- CMS has chosen the anti-kT algorithm, with  $R=0.5$ , as the default. Then, 4 types of jets reconstructed:

## Calorimeter Jets

Jets clustered from ECAL and HCAL deposits (Calo Towers)  
Accordingly:

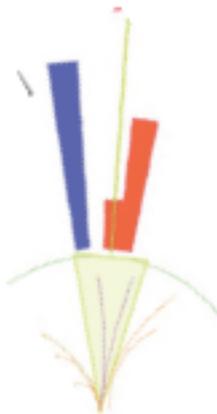
Calo MET



## Jet-Plus-Track Jets (JPT)

Subtract average calorimeter response from CaloJet and replace it with the track measurement  
Accordingly:

Tc MET

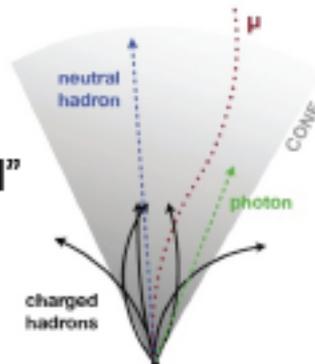


## Particle Flow Jets (PF)

Cluster Particle Flow objects:  
Unique list of calibrated particles "a la Generator Level"  
Accordingly:

PF MET

F. Beaudette  
01/22.7 17:15

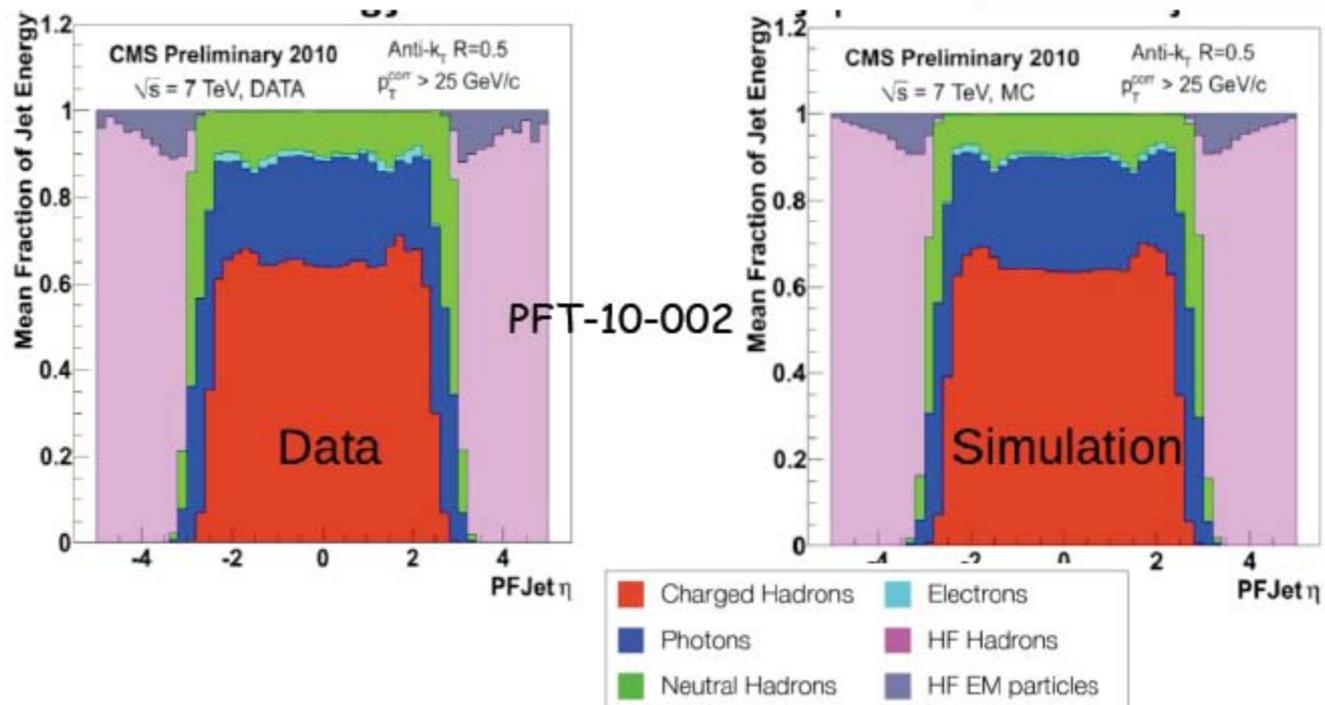


## Track Jets

Reconstructed from tracks of charged particles, independent from calorimetric jet measurements

# Particle Flow Jets

- Combines info from all subdetectors to produce particles
  - Charged hadrons – from tracks
  - Photons, neutral hadrons from ECAL, HCAL energy
    - Clusters with no tracks
  - Neutral particle overlapping with charged particles – subtract charged pt from cluster, remaining is neutral particle
- jets from resulting particles – charged hadrons and  $\gamma$  are 90% of jet energy

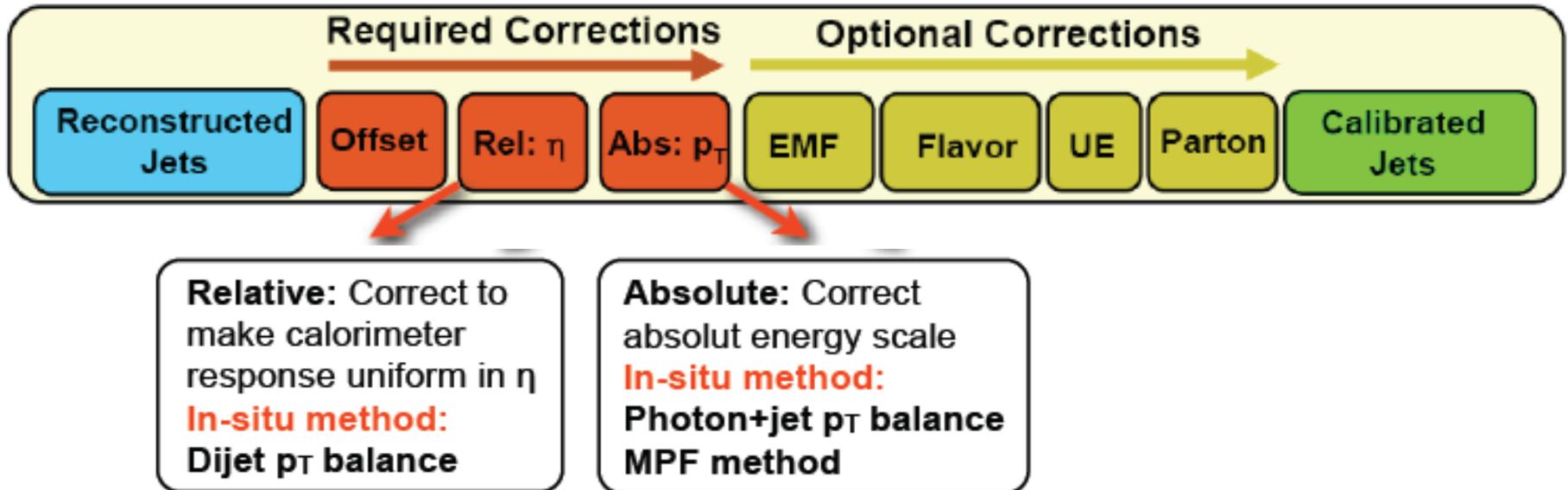


# Jet Energy Scale

- Determine the energy of the partons produced in the hard scattering process
- Corrections needed for:
  - **Detector effects:**
    - Non-linearity of calorimeter
    - Response to hadrons
    - Poorly-instrumented or non-functional regions
  - **Physics effects:**
    - Initial and final state radiation
    - Hadronization
    - Underlying event
    - Parton flavor
- Need corrections for data and MC, validate in both

# Jet Corrections

- Use CMS as an example, also show others
  - CMS uses factorized approach

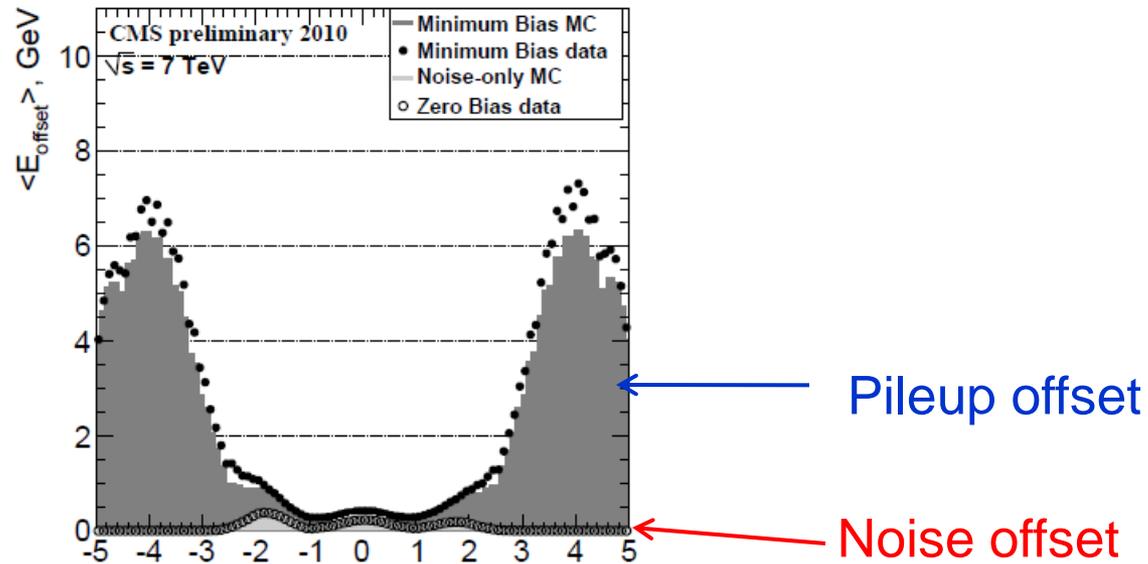


- apply Jet Corrections as :

$$E_{\text{corrected}} = (E_{\text{uncorrected}} - E_{\text{offset}}) \times C_{\text{rel}}(\eta, p''_T) \times C_{\text{abs}}(p'_T)$$

Where  $p''_T$  is the jet  $p_T$  corrected for offset, and  $p'_T$  is corrected for offset and  $\eta$  dependence (Relative corr).

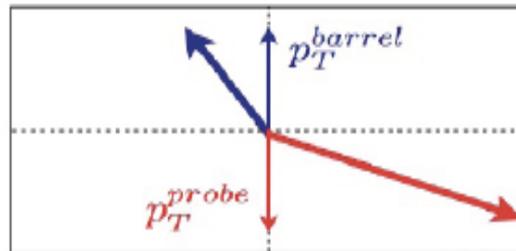
# Offset correction



- Measure noise with Zero Bias trigger, with Minimum Bias trigger vetoed (MinBias requires coincidence in Beam Scintillating counters, indicating pp interaction)
- Measure pileup – select MinBias events in early data (most events 0,1 int.)
- $E_{\text{offset}}$  -- average calorimeter energy summed in a cone of radius  $R=0.5$  at a given  $\eta$  -- Offset from noise is below 400 MeV in energy
- Offset from one pile-up event: Up to 7 GeV in energy
- Probability of pile-up in 2010 data typically ~50%
- correction is small -- not yet being applied on CMS jets

# Relative Correction from Dijet $p_T$ balance

**Barrel Jet**



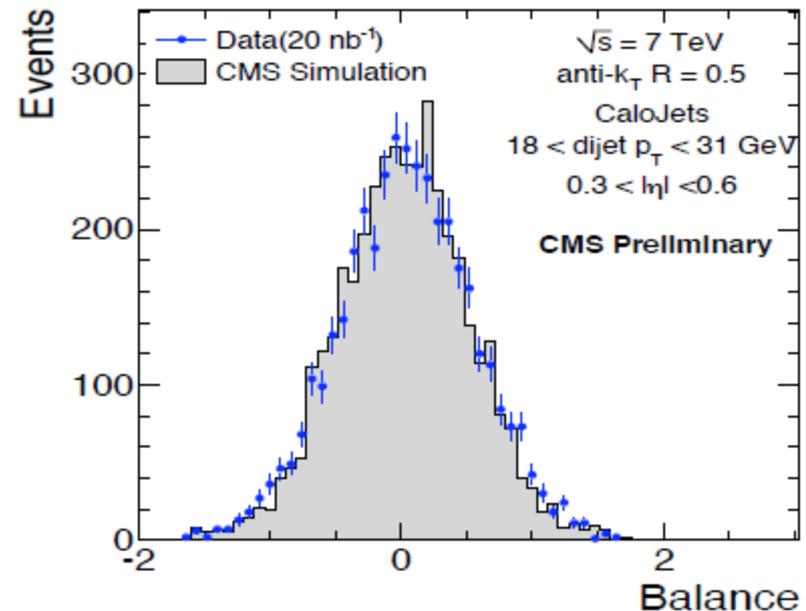
**Probe Jet**

$$p_T^{dijet} = \frac{p_T^{probe} + p_T^{barrel}}{2}$$

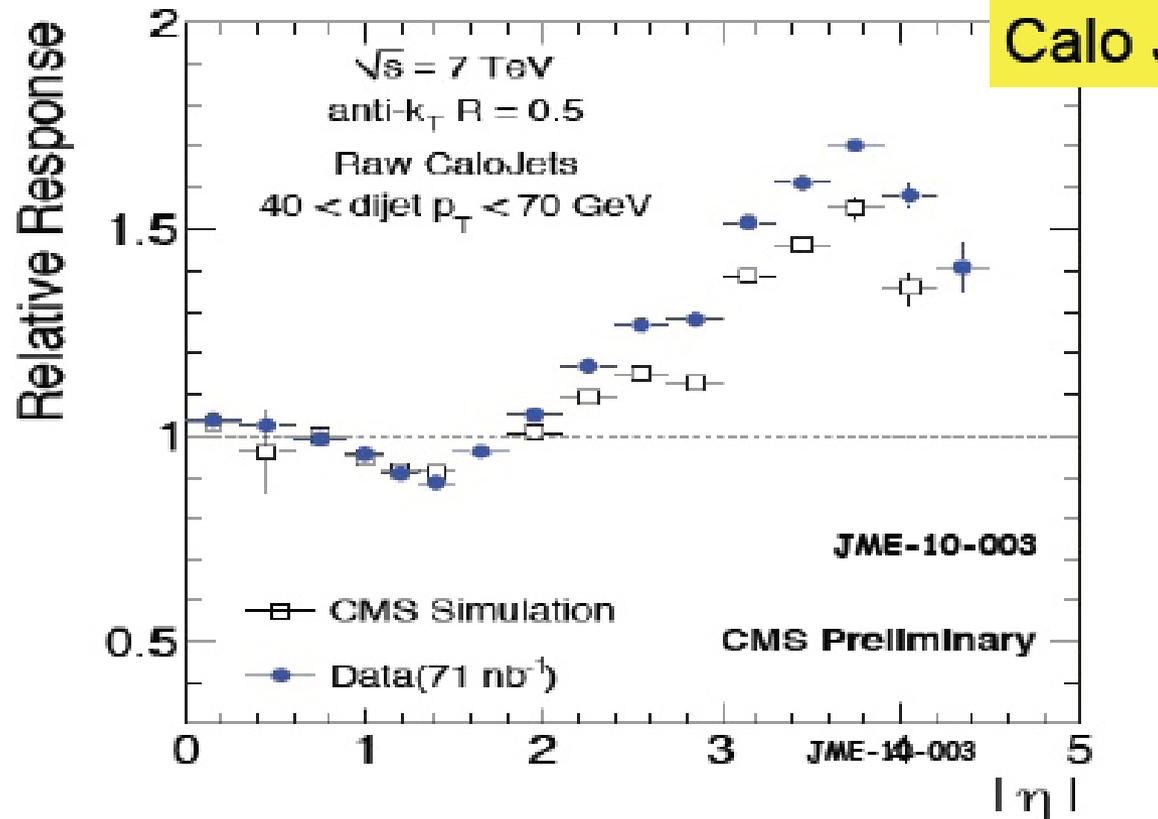
$$B = \frac{p_T^{probe} - p_T^{barrel}}{p_T^{dijet}}$$

$$r = \frac{2 + \langle B \rangle}{2 - \langle B \rangle}$$

- Require at least 2 jets, one in central region (Tag)
- $\Delta\phi > 2.7$
- Veto 3<sup>rd</sup> jet ( $p_T^{3rd}/p_T^{dijet} < 0.2$ )
- Measure Balance variable  $B$  in bins of  $p_T(dijet)$  and  $\eta$
- $\langle B \rangle$  in each bin is used to construct  $r$ 
  - Measure of relative response

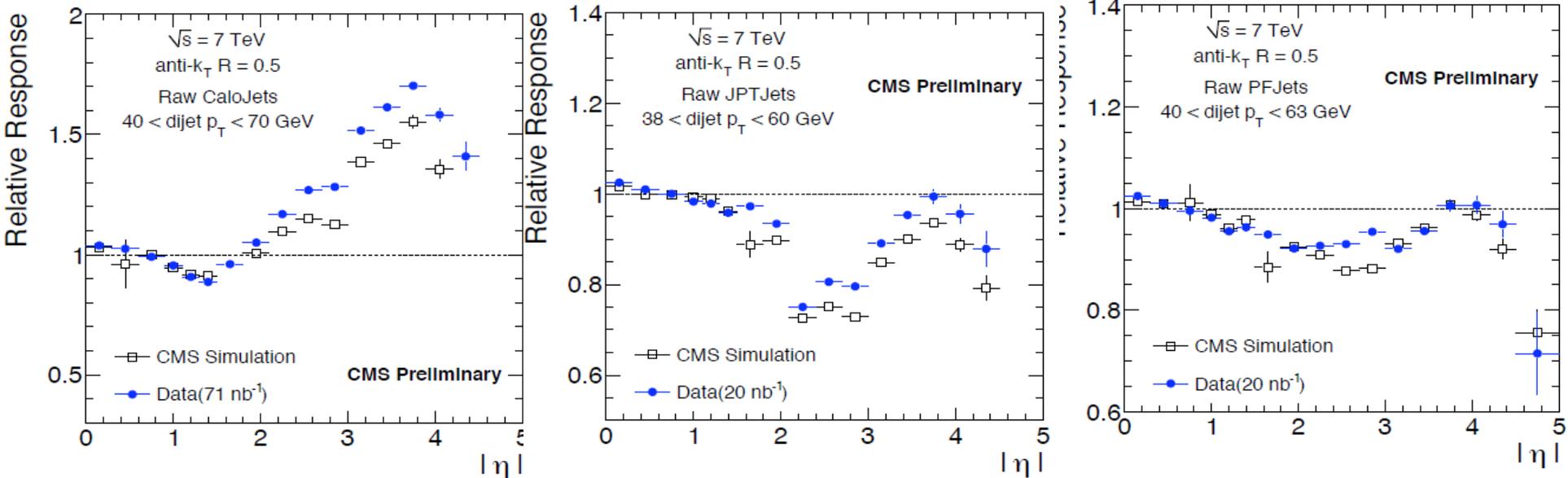


# Relative response in $\eta$



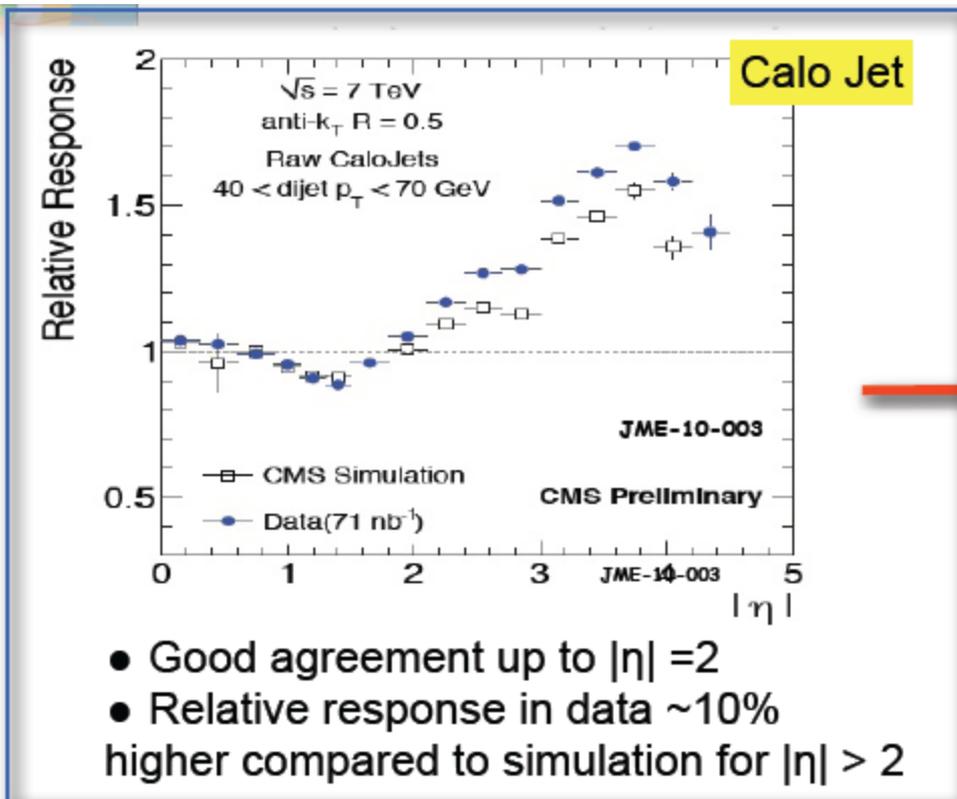
- Same dijet balance is applied to simulation
- Good agreement Data/MC for  $|\eta| < 2$
- Calorimeter transition
  - Barrel to endcap at  $|\eta| = 1.3$
  - Endcap to forward at  $|\eta| = 3$

# Compare different CMS jets



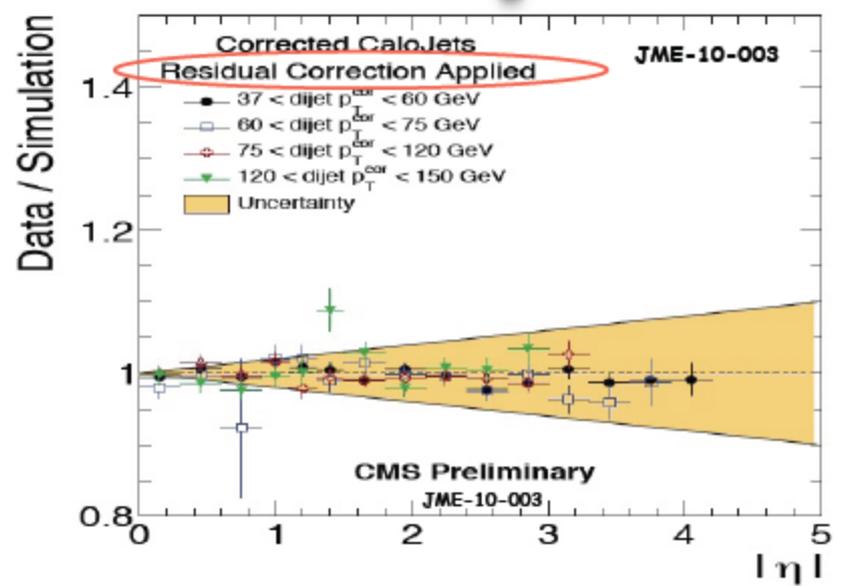
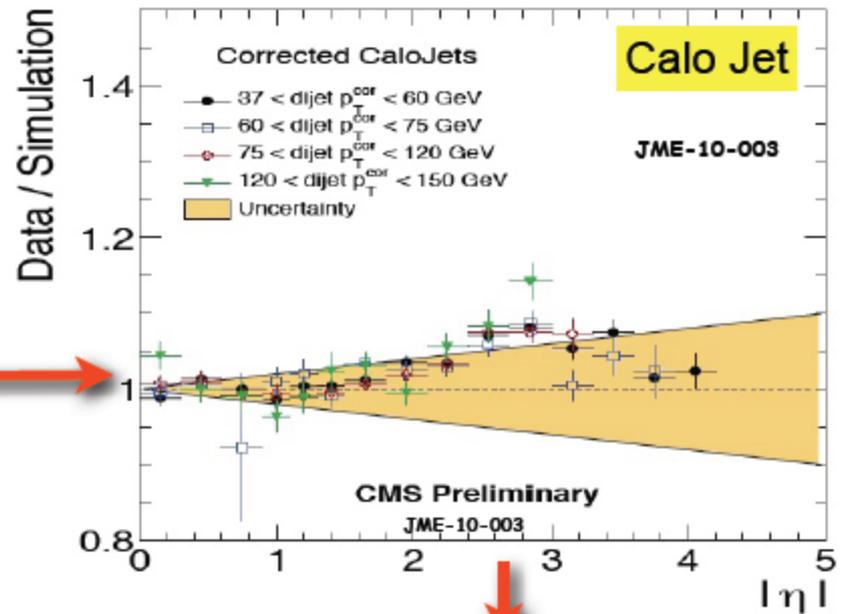
- JPT and PF jets – rely on tracking with calorimetry – response reflects tracking detector coverage as well as calorimeter
  - ➔ Steep falloff in track efficiency and resolution for  $|\eta| > 2$ , none for  $|\eta| > 2.5$

# Relative JEC : Data/MC

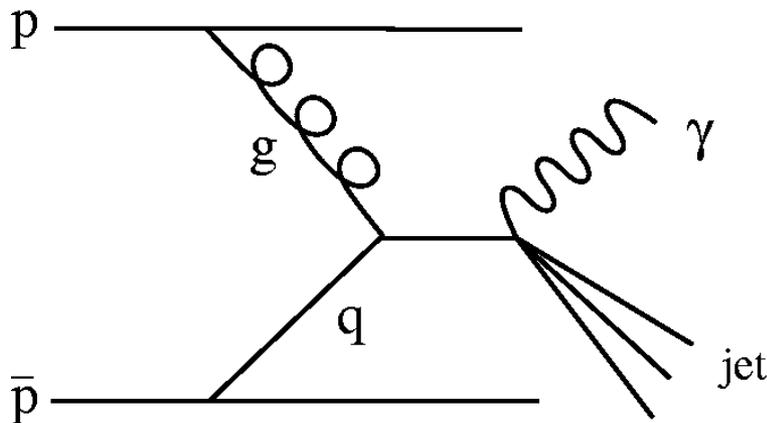


- Good agreement up to  $|\eta| = 2$
- Relative response in data  $\sim 10\%$  higher compared to simulation for  $|\eta| > 2$

=> Data/MC close to unity after the residual correction  
 => Data/MC deviations are covered by conservative  $\eta$ -dependent systematic uncertainty of  $\pm 2\% \times |\eta|$



# Absolute Jet Energy Correction at CMS

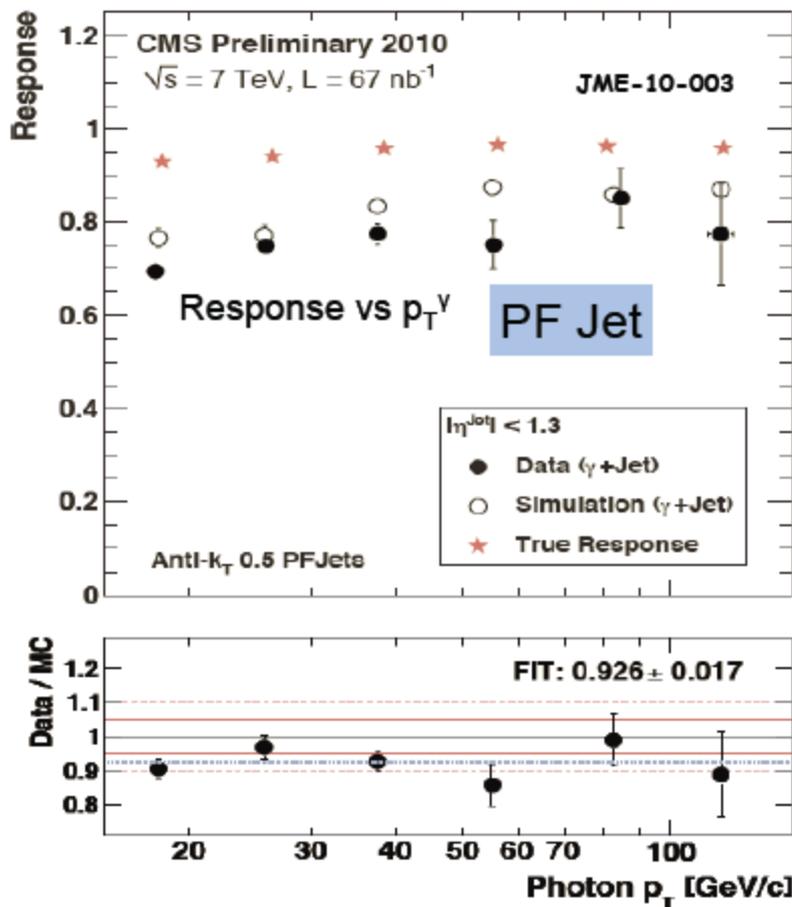
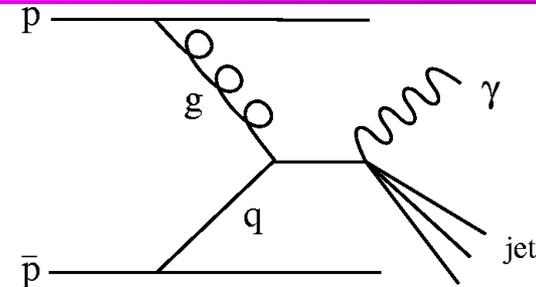


- Goal – want calorimeter energy response to a particle jet to be 1 and independent of  $p_T$ 
  - Absolute Jet Energy Correction
- When combined with offset and relative corrections, this is all that is needed for most analyses
- Use photon+jet events
  - $\gamma$ +jet balance
  - MPF
- Start with isolated photon,  $p_T > 15$  GeV, in barrel region ( $|\eta| < 1.3$ ), + 1 barrel jet

# Absolute Correction from Photon + jet

- $p_T$  balance in back-to-back  $\gamma$ +jet events

→  $\gamma$  is the reference, test response  $p_T/p_T^\gamma$



- Compare data, simulation to true from MC
- Bias due to soft veto on 2<sup>nd</sup> jet
- D0 – developed **MPF** method
- Missing ET Projection Fraction – uses MET to measure the balance, less sensitive to QCD radiation

# Jet Response from MPF in $\gamma$ +jet

- Basics of MPF (Missing Momentum Fraction; developed at D0)

- ❖ Ideally:  $\vec{p}_T^\gamma + \vec{p}_T^{\text{recoil}} = \vec{0}$

- ❖ Add in the detector:  $R_\gamma \vec{p}_T^\gamma + R_{\text{recoil}} \vec{p}_T^{\text{recoil}} = -\vec{E}_T^{\text{miss}}$

- ❖ Solving:  $R_{\text{recoil}}/R_\gamma = 1 + \frac{\vec{E}_T^{\text{miss}} \cdot \vec{p}_T^\gamma}{|\vec{p}_T^\gamma|^2} \equiv R_{\text{MPF}}$

- $R_{\text{MPF}}$  is assigned as the response of the recoil jet

- Advantage of MPF: Low sensitivity to extra radiation

- Smaller error bars: Widths of distributions are narrower → fewer fluctuations from the impact of extra radiation

- Smaller bias wrt MC-truth than  $p_T^{\text{jet}}/p_T^\gamma$  for current very loose cuts on extra radiation

- Helps to fully exploit the accuracy of PF method

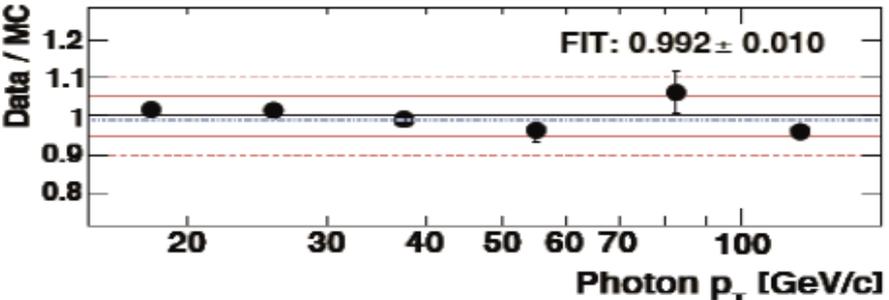
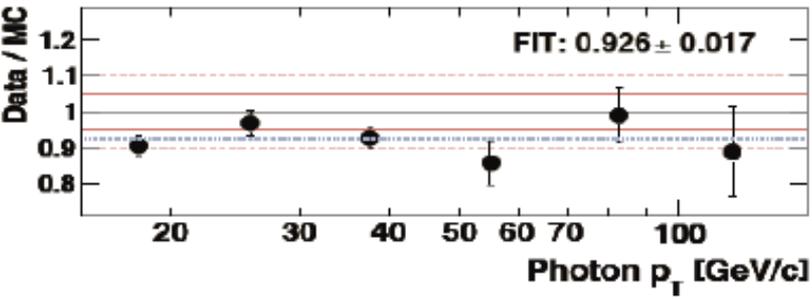
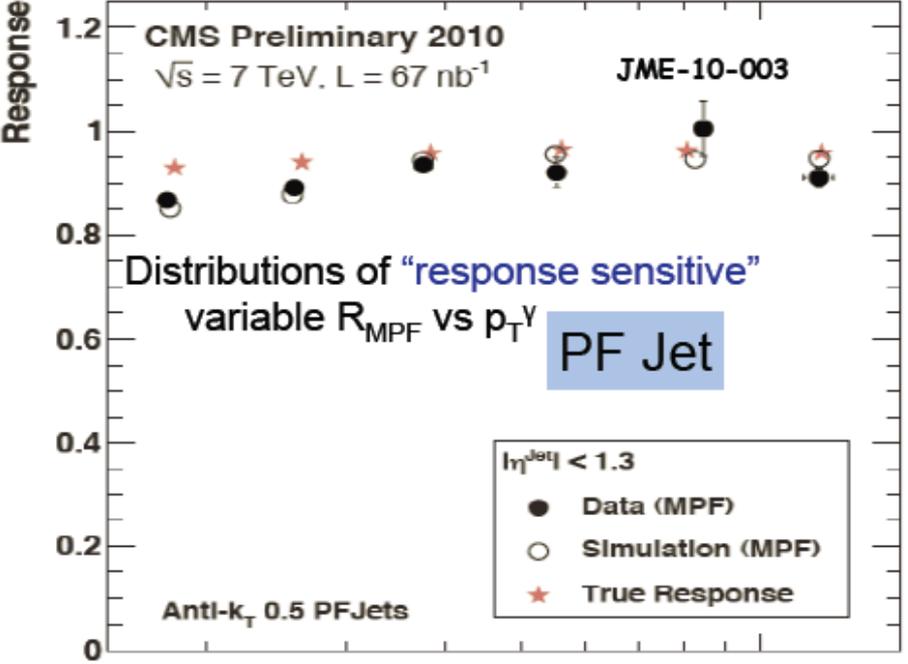
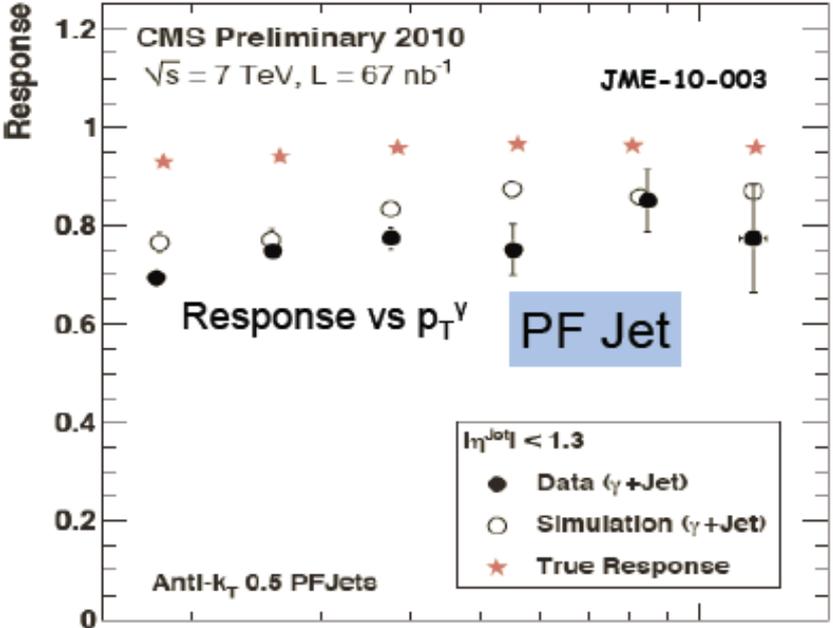
- MPF method demonstrates the accuracy of JES for different types of jets more clearly than  $\gamma$ -jet balancing method does

# MPF at CMS

$\gamma$ +jet

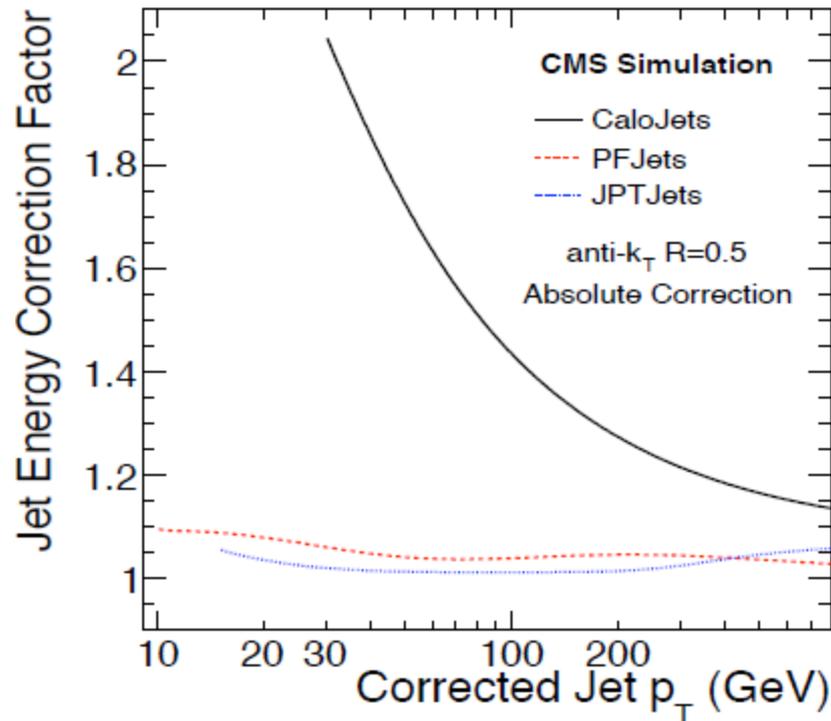


MPF



# Absolute Correction Factors

- Absolute jet energy correction factors  $C_{\text{abs}}$  derived from simulation for CaloJets, PF Jets, JPT jets, at 7 TeV, as a function of corrected jet  $p_T$



Note large correction factors at low  $p_T$  for CaloJets – due to non-compensation of CMS calorimeters

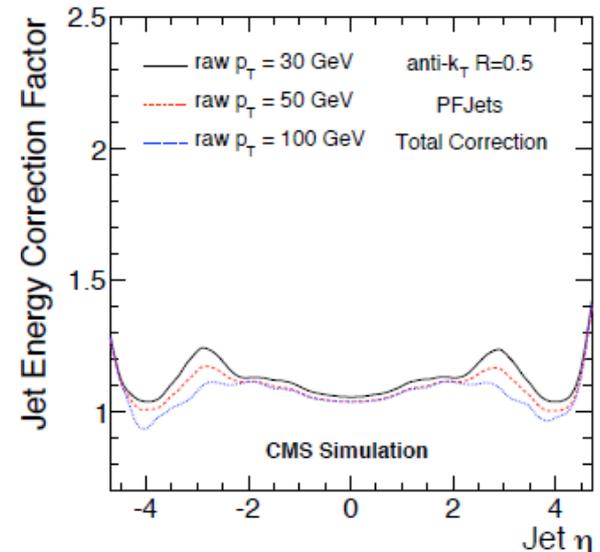
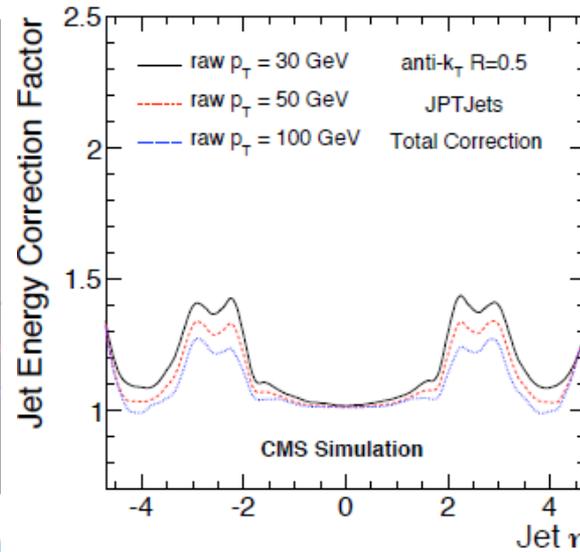
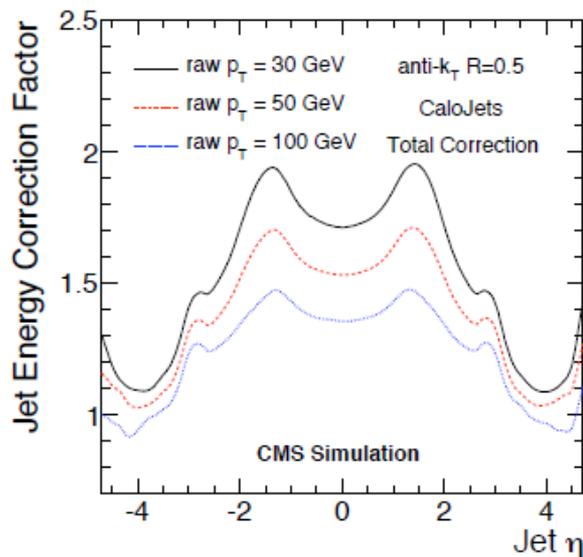
# Correcting Simulated Jets

- Derive corrections for Monte Carlo jets – match reconstructed jets to MC-generator level jets
- In CMS, first three levels are put together in one correction (offset, relative, absolute)

Calojets

JPT Jets

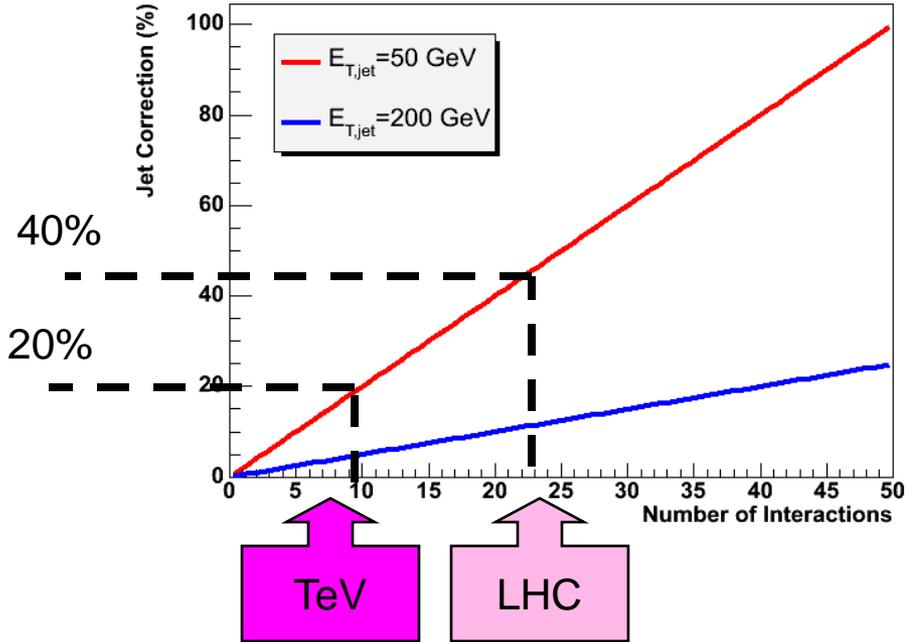
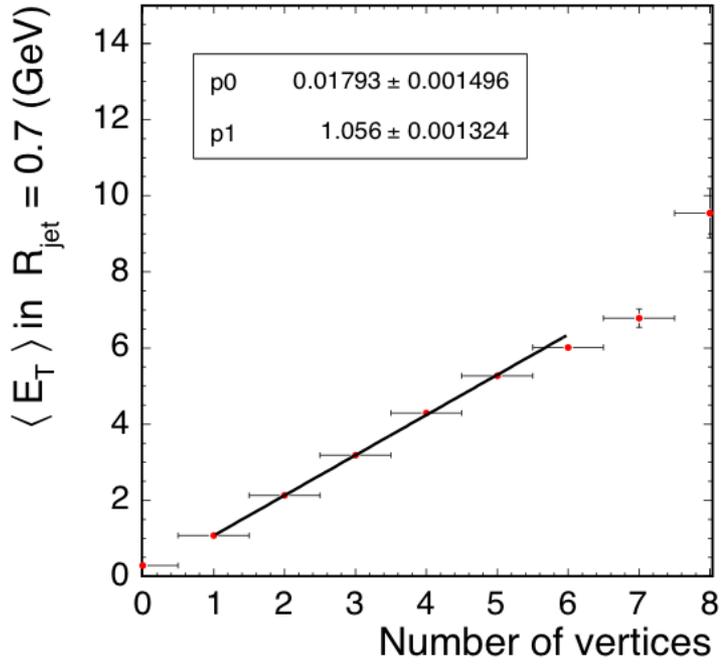
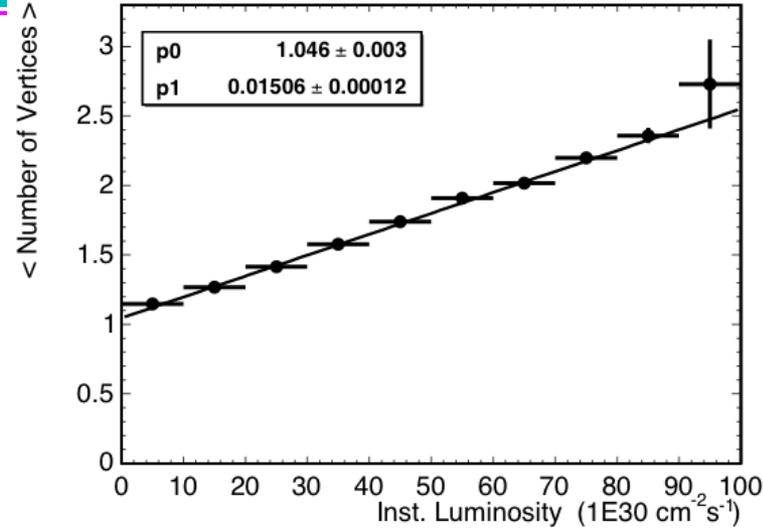
PF Jets



- Mature Tevatron experiments have sophisticated jet correction algorithms
  - Use some of the same that I showed for CMS
- I will show some examples

# Multiple Interactions (MI) at the Tevatron

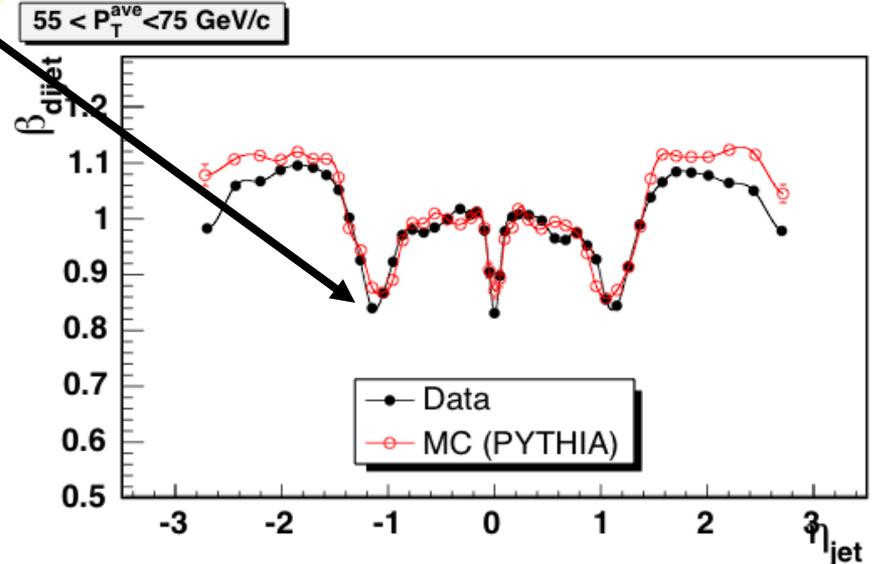
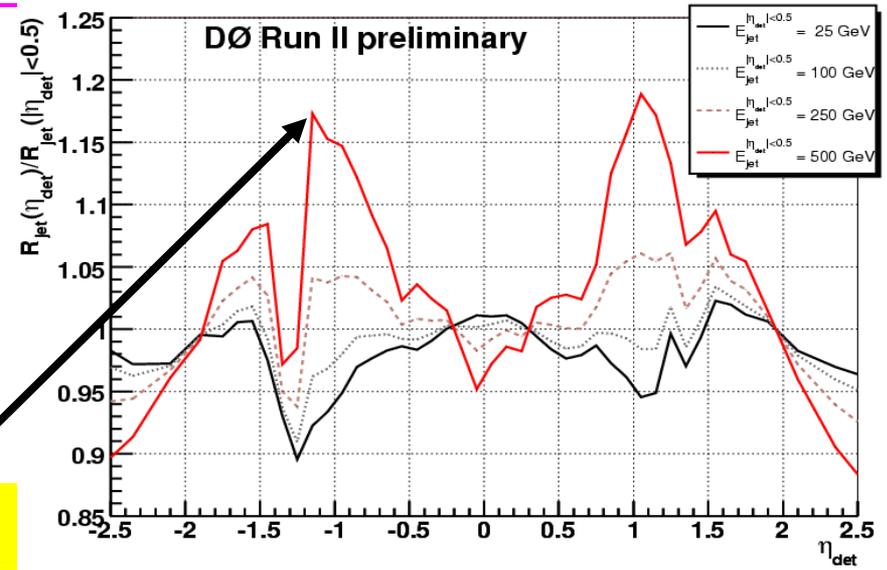
- Need to know how many interactions there were:
  - ➔ # of z-vertices  $\sim$  # of interactions
- Throw random cones in Minimum Bias events
  - ➔ Determine average  $E_T$  per cone, e.g. CDF: 1 GeV for  $R=0.7$



# Relative Corrections

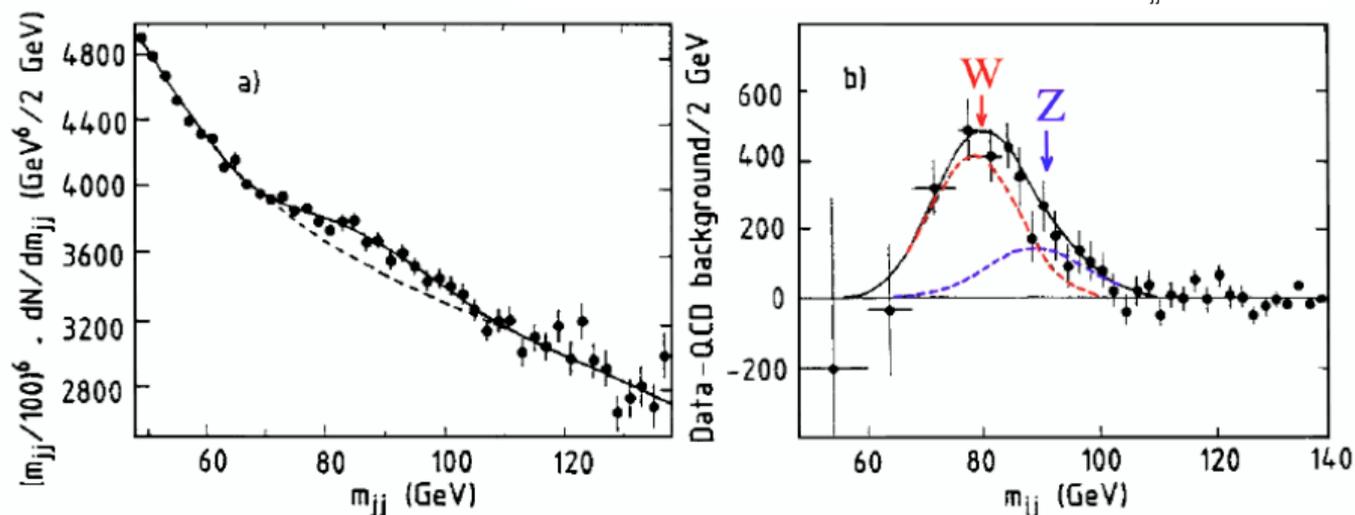
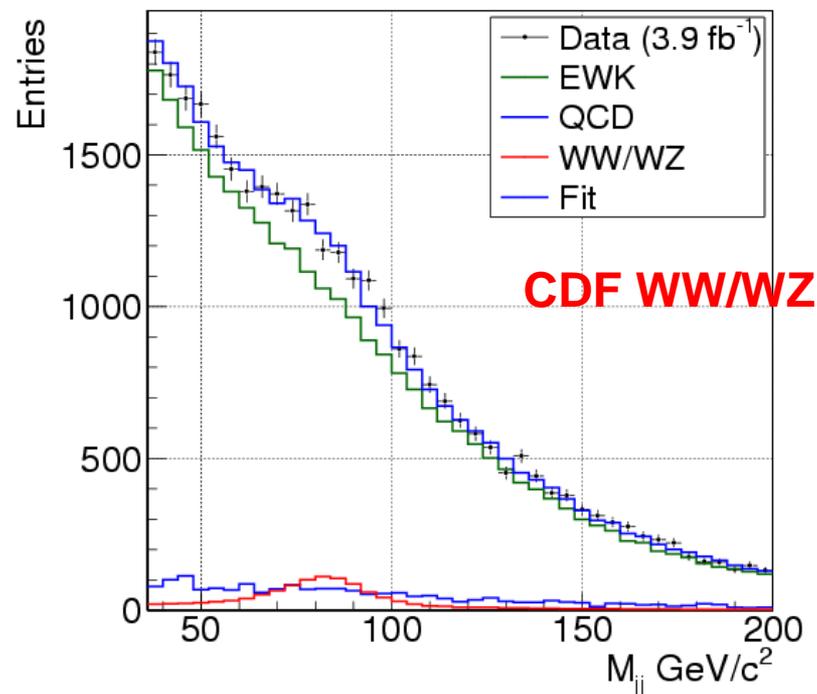
- Mapping out cracks and response of calorimeter
- Central at  $\sim 1$  by definition
- D0:
  - Response similar in central and forward
  - Two rather large cracks
- CDF:
  - Response of forward better than of central
  - Three smaller cracks
- Difficulties:
  - depends on  $E_T$
  - Can be different for data and MC

Cracks

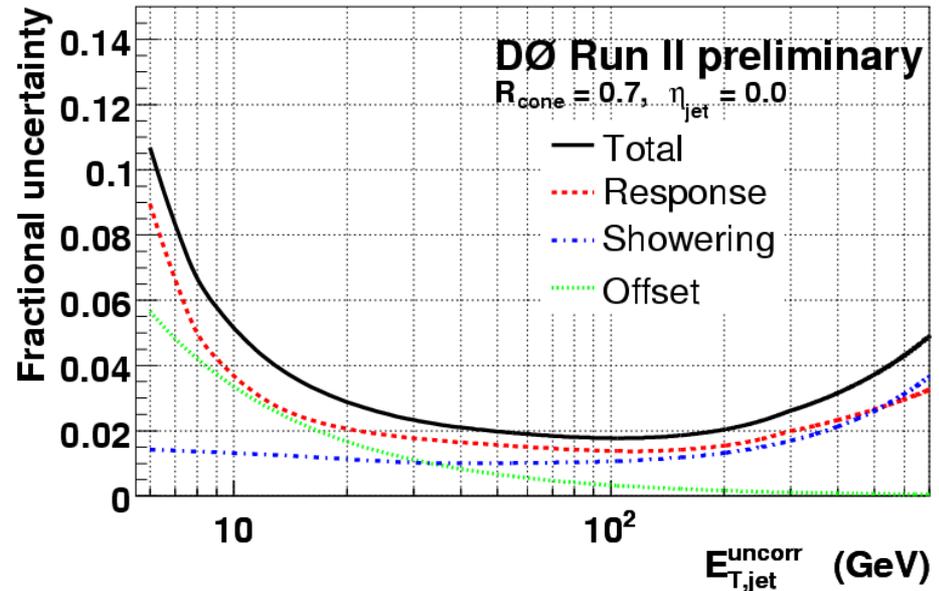
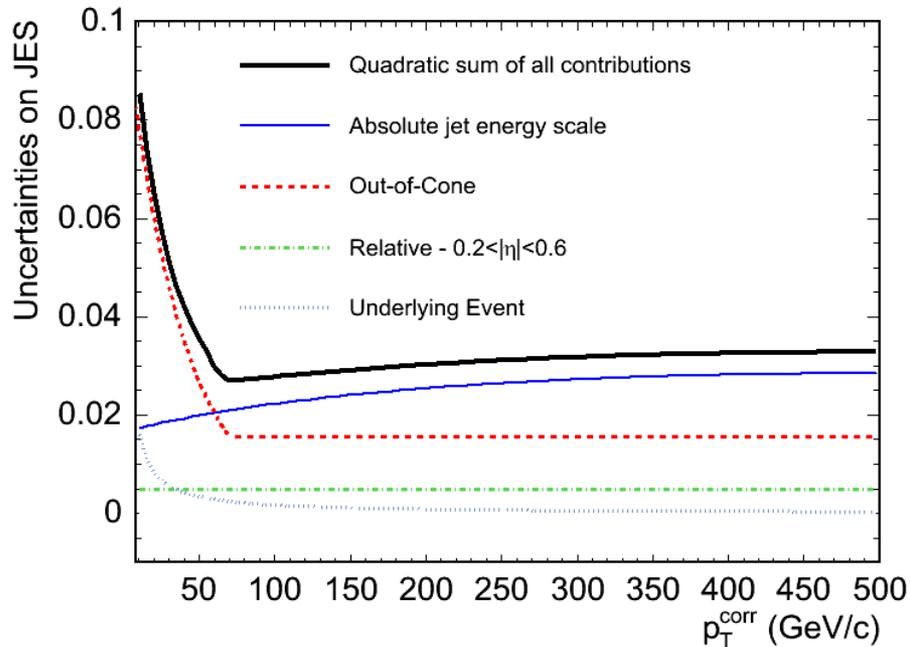


# Calibration Peaks from W's and Z's

- Would like to use W,Z for calibration – same mass scale as Higgs
- Difficult to see inclusive decays of W's and Z's to jets
  - Small signal on huge background
- Two best opportunities:
  - W in top quark decays
  - Z in bb decay mode



# Jet Energy Scale Uncertainties



- Uncertainty on Jet Energy Scale determines how well you can measure mass (of W, H, new resonance, etc) – extremely important to reduce, and understand
- CDF and DØ achieve similar uncertainties
- CMS – 10% based on Monte Carlo studies – initial data validates that this is conservative → Will improve with more data

# Summary

- I've tried to show aspects of calibration of calorimeters at many levels
  - detector components
    - Testbeam, in-situ
  - Single-particle
  - Physics objects
- Using calorimeter information
  - Jet construction algorithms
- Corrections at the physics level
  - It comes back to how the detector was designed and built
  - Important to physics results!

Thanks for your attention and participation!!  
Enjoy the rest of the summer school!!

# Extra slides

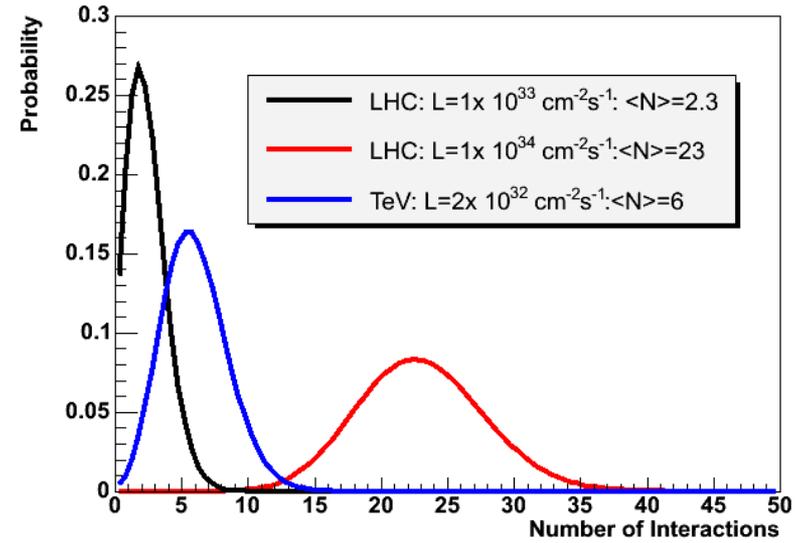
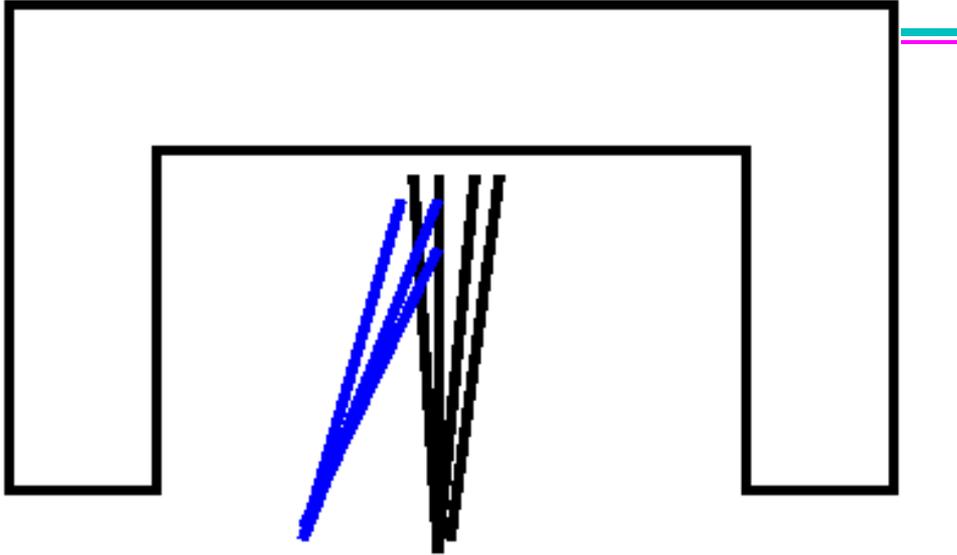
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$$d_{ij} = \min \left( k_{T,i}^{-2}, k_{T,j}^{-2} \right) \frac{\Delta R_{ij}^2}{R^2}$$

$$\Delta R_{i,j}^2 = (y_i - y_j)^2 + (\phi_i - \phi_j)^2$$

- ◆ New development in the jet clustering theory.
- ◆ Tends to cluster the energy around the hardest particles.
  - ▶ essentially behaves like a cone algorithm giving perfectly round jet areas
- ◆ Belongs to the “ $k_T$ ” family.
  - ▶ merging of 4-vector pairs based on transverse momentum weighted distance in  $y$ - $\phi$  plane.
  - ▶ the clustering terminates when the weighted distance between particles is greater than a specific value  $R$  (resolution parameter).
  - ▶ the quantity  $R$  is of the order of unity.
- ◆ infrared and collinear safe (suitable for theory calculations).

# Multiple pp Interactions

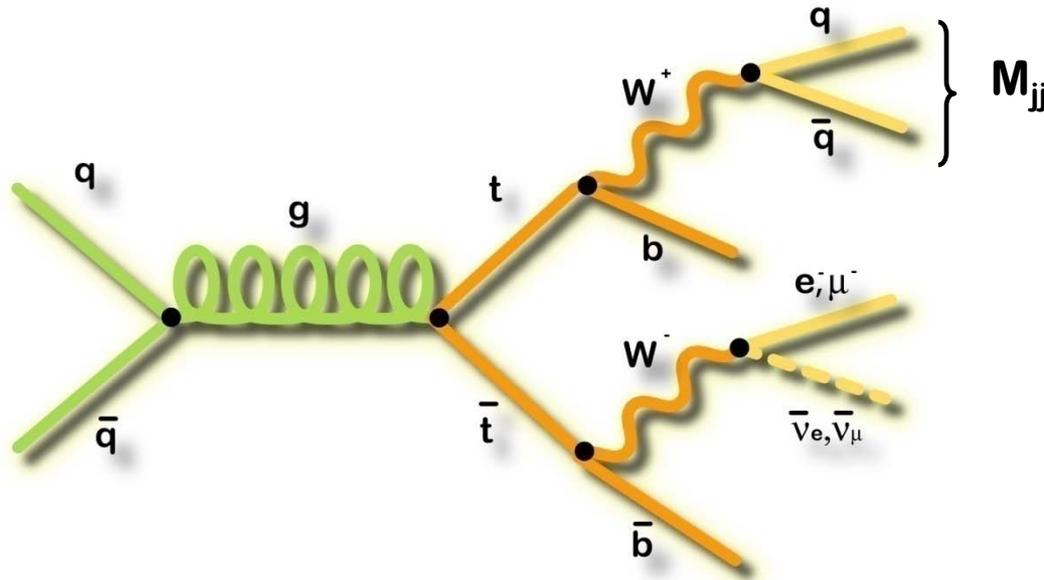


- Overlapping interactions can overlap the jet
- Number of extra interactions depends on luminosity
  - LHC:
    - Low lumi ( $L=1 \times 10^{33} \text{ cm}^{-2}\text{s}^{-1}$ ):  $\langle N \rangle = 2.3$
    - High lumi ( $L=1 \times 10^{34} \text{ cm}^{-2}\text{s}^{-1}$ ):  $\langle N \rangle = 23$
  - Tevatron:
    - $L=2 \times 10^{32} \text{ cm}^{-2}\text{s}^{-1}$ :  $\langle N \rangle = 6$

Offset depending on number of interactions

# In-situ Measurement of JES

- Additionally, use  $W \rightarrow jj$  mass resonance ( $M_{jj}$ ) to measure the jet energy scale (JES) uncertainty



2D fit of the invariant mass of the non-b-jets and the top mass:

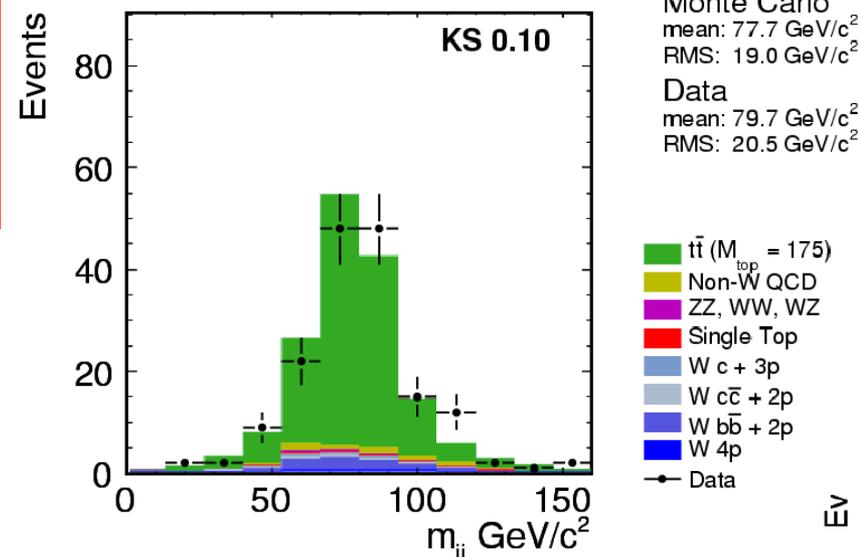
$JES \propto M(jj) - 80.4 \text{ GeV}/c^2$

Measurement of JES scales directly with data statistics

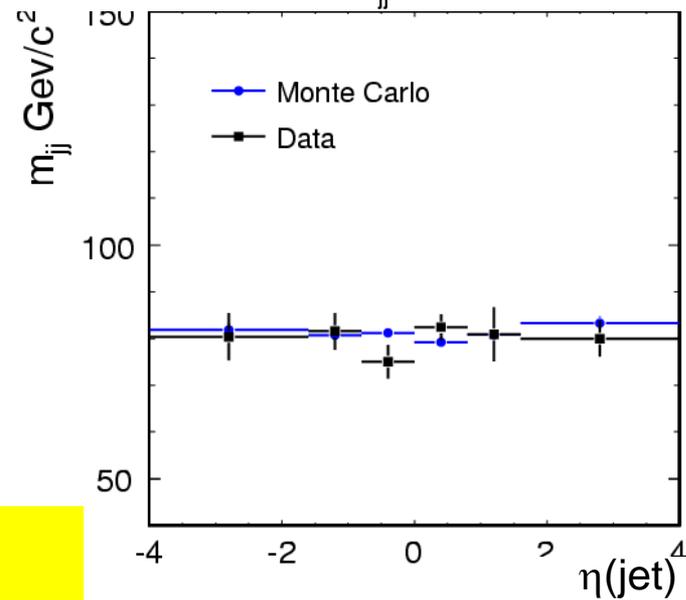
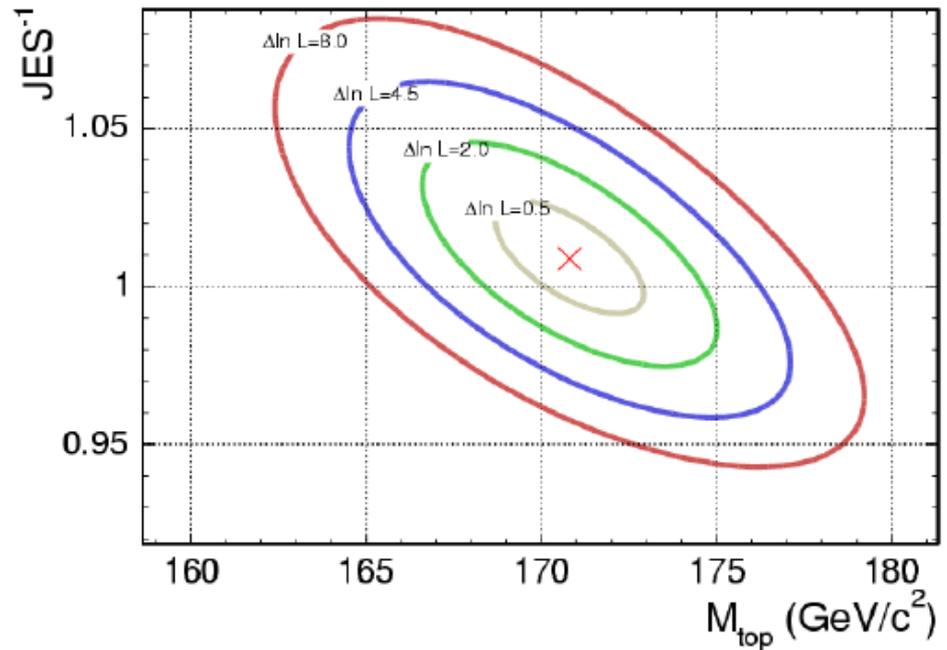
# W → jj Calibration in Top Events

- Fit for ratio of JES in data to JES in MC  
**CDF (1 fb<sup>-1</sup>):  $\delta_{\text{JES}} = 0.99 \pm 0.02$**   
**DØ (0.3 fb<sup>-1</sup>):  $\delta_{\text{JES}} = 0.99 \pm 0.03$**
- Constrain JES to 2% using 166 events

CDF Run II Preliminary (955 pb<sup>-1</sup>)



CDF Preliminary 955 pb<sup>-1</sup>



At LHC will have 45,000 top events/month!

# Streamlined Seedless Algorithm

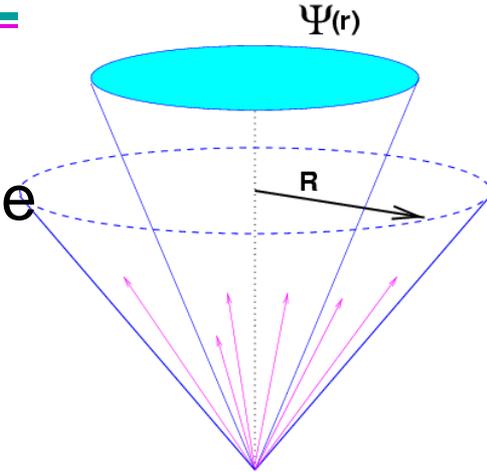
- Data in form of 4 vectors in  $(\eta, \varphi)$
- Lay down grid of cells (~ calorimeter cells) and put trial cone at center of each cell
- Calculate the centroid of each trial cone
- If centroid is outside cell, remove that trial cone from analysis, otherwise iterate as before
- Approximates looking everywhere; converges rapidly
- Split/Merge as before

# Corrections from Particle Jet to Parton

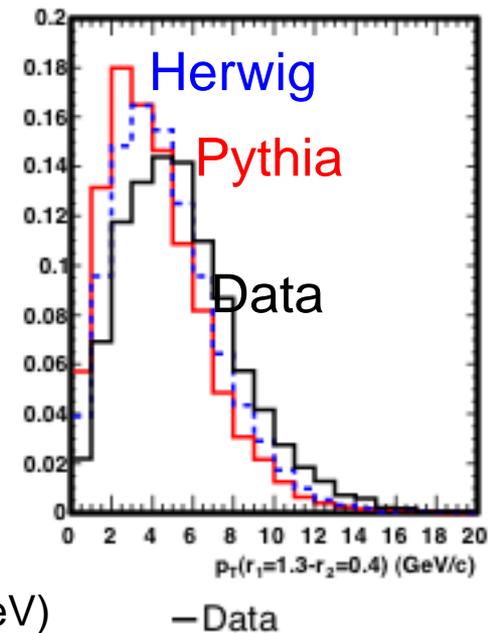
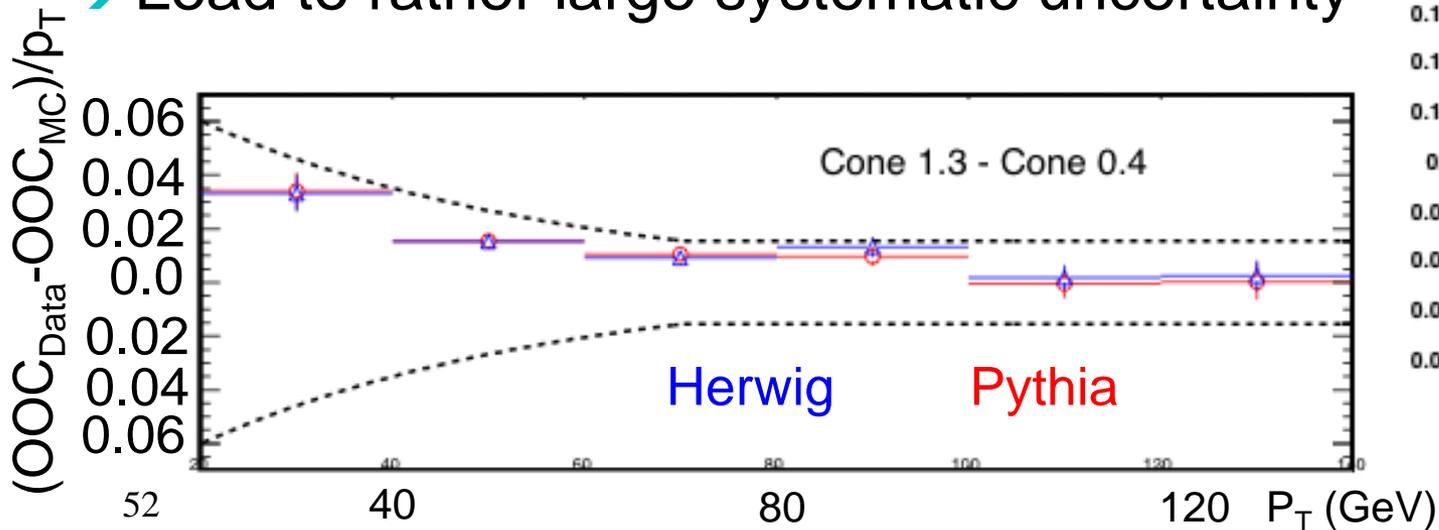
- Underlying event (UE) and Out-of-cone (OOC) energy
  - Only used if parton energy is wanted
  - Requires MC modeling of UE and OOC
    - Differences are taken as systematic uncertainty

$$P_{T,parton} = P_{T,particle} - UE + OOC$$

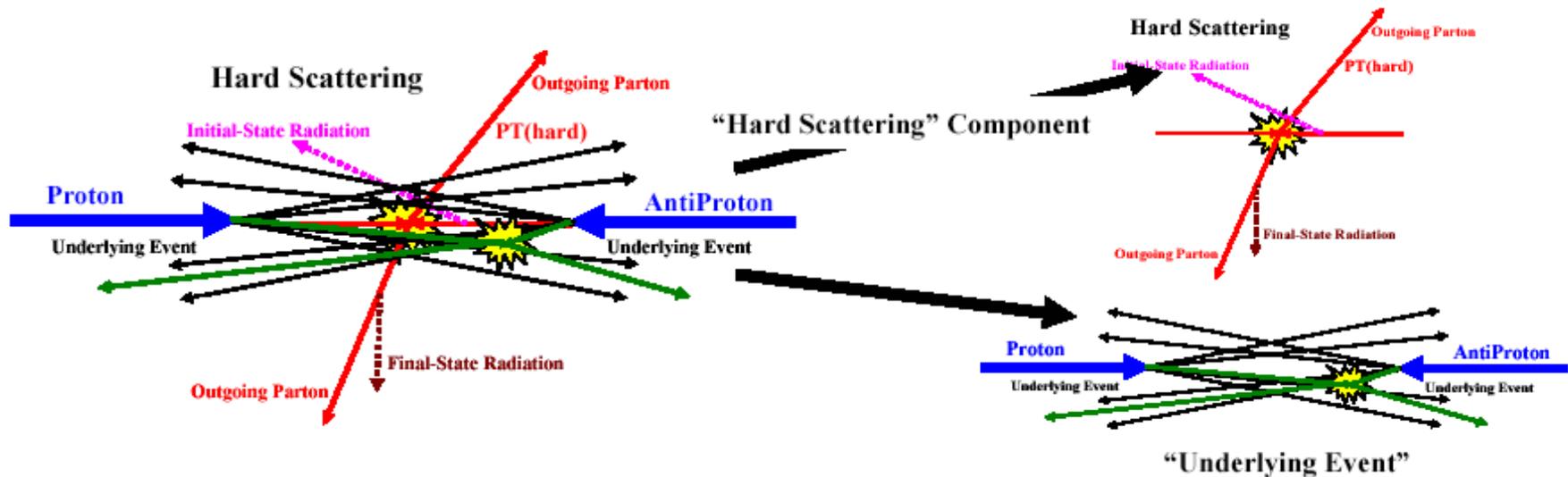
# Out of Cone Energy (OOC)



- Out-of-Cone Energy:
  - Original parton energy that escapes the cone
    - E.g. due to gluon radiation
  - Jet shape in MC must describe data:
    - measure energy flow in annuli around jet
- Differences between data and MC
  - Lead to rather large systematic uncertainty



# Underlying Event



- Consists of:

- "beam-beam remnants": energy from interaction of spectator partons
- "Initial state radiation": energy radiated off hard process before main interaction

# Measuring the Underlying Event

Leading Jet Direction

“Transverse” region very sensitive to the “underlying event”!

