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# Evasion of the helicity selection rule and its implications in heavy quarkonium decays

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# Motivations

- Charmonium decays as a probe for non-perturbative QCD mechanisms
- pQCD helicity selection rule is badly violated in exclusive processes
- Several existing puzzles in low-lying vector charmonium decays

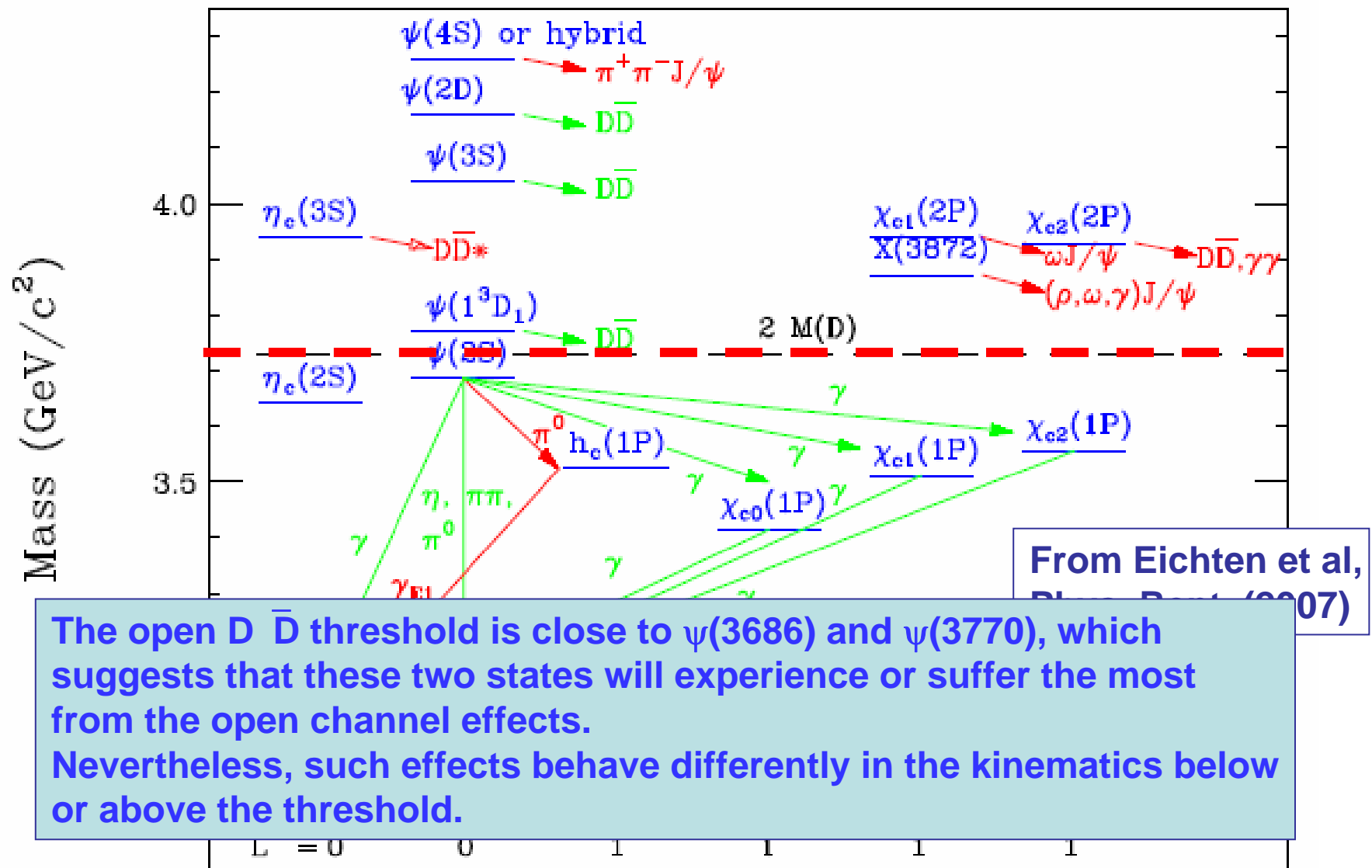
# Several well-known puzzles in charmonium decays

- $\psi(3770)$  non-D  $\bar{D}$  decay
- “ $\rho\pi$  puzzle” in  $J/\psi, \psi' \rightarrow VP$  decay
- Large  $\eta_c \rightarrow VV$  branching ratios
- M1 transition problem in  $J/\psi, \psi' \rightarrow \gamma \eta_c, (\gamma \eta_c')$
- Isospin-violating decay of  $\psi' \rightarrow J/\psi \pi^0$ , and  $\psi' \rightarrow h_c \pi^0$
- Could be more ... ..

Conjecture:

- 1) These puzzles could be related to non-pQCD mechanisms in charmonium decays due to intermediate D meson loops.
- 2) The intermediate meson loop transition could be a mechanism for the evasion of the helicity selection rule.

# Charmonium spectrum



# Outline

- Introduction to the helicity selection rule
- Long-distance contribution from intermediate hadron loop transitions
  - $\psi(3770)$  non-D  $\bar{D}$  decays
  - “ $\rho\pi$  puzzle”
  - $\chi_{c1} \rightarrow VV$  **and**  $\chi_{c2} \rightarrow VP$
  - $\eta_c, \chi_{c0}, h_c \rightarrow \text{Baryon} + \text{Antibaryon}$
- Summary

# Helicity selection rule

According to the perturbative method of QCD, Chernyark and Zitnitsky showed that the asymptotic behavior for some exclusive processes has a power-counting as follows:

$$BR_{J_{c\bar{c}}(\lambda) \rightarrow h_1(\lambda_1)h_2(\lambda_2)} \sim \left( \frac{\Lambda_{QCD}^2}{m_c^2} \right)^{|\lambda_1 + \lambda_2| + 2}$$

**Chernyark and Zitnitsky, Phys. Rept. 112, 173 (1984); Brodsky and Lepage, PRD24, 2848 (1981).**

The QCD leading term will contribute when  $\lambda_1 + \lambda_2 = 0$ , while the next to leading order contribution will be suppressed by a factor of  $\Lambda_{QCD}^2/m_c^2$

# Helicity selection rule

An alternative description of this selection rule with the quantum number named “naturalness”

$$\sigma \equiv P(-1)^J$$

The selection rule requires that

$$\sigma^{initial} = \sigma_1 \sigma_2$$

Take the process  $J/\psi \rightarrow VP$  as an example ( $\sigma^{initial} \neq \sigma_1 \sigma_2$ )

$$\mathcal{M}_{J/\psi(\lambda_\psi) \rightarrow V(\lambda_V)P(\lambda_P)} \propto \epsilon_{\mu\nu\alpha\beta} p_\psi^\mu \epsilon_\psi^\nu(p_\psi, \lambda_\psi) p_V^\alpha \epsilon_V^{*\beta}(p_V, \lambda_V)$$

In the rest frame of initial state, it requires  $\lambda_V=0$  at leading twist accuracy.  $\epsilon_V$  can be approximately expressed as a linear combination of the final state momenta, which then results in a vanishing amplitude.

# S- and P-wave charmonium exclusive decays

	$PP$	$PV$	$VV$
$\eta_c$	-	( $\checkmark$ )	$\epsilon$
$\psi(3770)$	( $\checkmark$ )	$\epsilon$	( $\checkmark$ )
$\chi_{c0}$	$\checkmark$	-	$\checkmark$
$\chi_{c1}$	-	( $\checkmark$ )	$\epsilon$
$\chi_{c2}$	$\checkmark$	$\epsilon$	$\checkmark$

“-” : forbidden by angular-momentum and parity conserv.

“ $\epsilon$ ” : to leading twist order forbidden in pQCD

“ $\checkmark$ ” : to leading twist order allowed in pQCD

“( )” : either G-parity or isospin are violated

Feldmann and Kroll, PRD62, 074006 (2000)

$\psi(3770)$  non-D  $\bar{D}$  decays into VP

$$BR(\chi_{c1} \rightarrow K^{*0} \bar{K}^{*0}) = (1.6 \pm 0.4) \times 10^{-3} \quad \text{PDG2008}$$

The helicity selection rule seems to be violated badly in charmonium decays!



$\psi(3770)$  non- $D \bar{D}$  decay

-- IML as a mechanism for evading the  
helicity selection rule

$\psi(3770)$ 

$$J^{PC} = 0^-(1^--)$$

## $\psi(3770)$ MASS

OUR FIT includes measurements of  $m_{\psi(2S)}$ ,  $m_{\psi(3770)}$ , and  $m_{\psi(3770)} - m_{\psi(2S)}$ .

VALUE (MeV)	EVTS	DOCUMENT ID	TECN	COMMENT
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**3772.92 ± 0.35 OUR FIT** Error includes scale factor of 1.1.

**3775.2 ± 1.7 OUR AVERAGE** Error includes scale factor of 1.4. See the ideogram below.

3772.0 ± 1.9		<sup>1</sup> ABLIKIM	08D BES2	$e^+e^- \rightarrow \text{hadrons}$
3775.5 ± 2.4 ± 0.5	57	AUBERT	08B BABR	$B \rightarrow D\bar{D}K$
3776 ± 5 ± 4	68	BRODZICKA	08 BELL	$B^+ \rightarrow D^0\bar{D}^0K^+$
3778.8 ± 1.9 ± 0.9		AUBERT	07BE BABR	$e^+e^- \rightarrow D\bar{D}\gamma$

## $\psi(3770)$ WIDTH

<u>VALUE (MeV)</u>	<u>EVTs</u>	<u>DOCUMENT ID</u>	<u>TECN</u>	<u>COMMENT</u>
<b>27.3<math>\pm</math> 1.0 OUR FIT</b>				
<b>27.6<math>\pm</math> 1.0 OUR AVERAGE</b>				
30.4 $\pm$ 8.5	68	<sup>4</sup> ABLIKIM	08D BES2	$e^+e^- \rightarrow \text{hadrons}$
27 $\pm$ 10 $\pm$ 5		BRODZICKA	08 BELL	$B^+ \rightarrow D^0 \bar{D}^0 K^+$
28.5 $\pm$ 1.2 $\pm$ 0.2		ABLIKIM	07E BES2	$e^+e^- \rightarrow \text{hadrons}$
23.5 $\pm$ 3.7 $\pm$ 0.9		AUBERT	07BE BABR	$e^+e^- \rightarrow D \bar{D} \gamma$
26.9 $\pm$ 2.4 $\pm$ 0.3		ABLIKIM	06L BES2	$e^+e^- \rightarrow \text{hadrons}$
24 $\pm$ 5		SCHINDLER	80 MRK2	$e^+e^-$
24 $\pm$ 5		BACINO	78 DLCO	$e^+e^-$
28 $\pm$ 5		RAPIDIS	77 LGW	$e^+e^-$

<sup>4</sup> Reanalysis of data presented in BAI 02C. From a global fit over the center-of-mass energy region 3.7–5.0 GeV covering the  $\psi(3770)$ ,  $\psi(4040)$ ,  $\psi(4160)$ , and  $\psi(4415)$  resonances. Phase angle fixed in the fit to  $\delta = 0^\circ$ .

## $\psi(3770)$ DECAY MODES

In addition to the dominant decay mode to  $D\bar{D}$ ,  $\psi(3770)$  was found to decay into the final states containing the  $J/\psi$  (BAI 05, ADAM 06). ADAMS 06 and HUANG 06A searched for various decay modes with light hadrons and found a statistically significant signal for the decay to  $\phi\eta$  only (ADAMS 06).

	Mode	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level
$\Gamma_1$	$D\bar{D}$	$(85.3 \pm 3.2) \%$	
$\Gamma_2$	$D^0\bar{D}^0$	$(48.7 \pm 3.2) \%$	
$\Gamma_3$	$D^+D^-$	$(36.1 \pm 2.8) \%$	
$\Gamma_4$	$J/\psi \pi^+ \pi^-$	$(1.93 \pm 0.28) \times 10^{-3}$	
$\Gamma_5$	$J/\psi \pi^0 \pi^0$	$(8.0 \pm 3.0) \times 10^{-4}$	
$\Gamma_6$	$J/\psi \eta$	$(9 \pm 4) \times 10^{-4}$	
$\Gamma_7$	$J/\psi \pi^0$	$< 2.8 \times 10^{-4}$	CL=90%
$\Gamma_8$	$\gamma \chi_{c0}$	$(7.3 \pm 0.9) \times 10^{-3}$	
$\Gamma_9$	$\gamma \chi_{c1}$	$(2.9 \pm 0.6) \times 10^{-3}$	
$\Gamma_{10}$	$\gamma \chi_{c2}$	$< 9 \times 10^{-4}$	CL=90%
$\Gamma_{11}$	$e^+e^-$	$(9.7 \pm 0.7) \times 10^{-6}$	S=1.2
$\Gamma_{26}$	$\phi\eta$	$(3.1 \pm 0.7) \times 10^{-4}$	

# □ $\psi(3770)$ non- $D \bar{D}$ decay

## ■ Experimental discrepancies:

Exclusive  $D \bar{D}$  cross sections are measured at BES and CLEO-c:

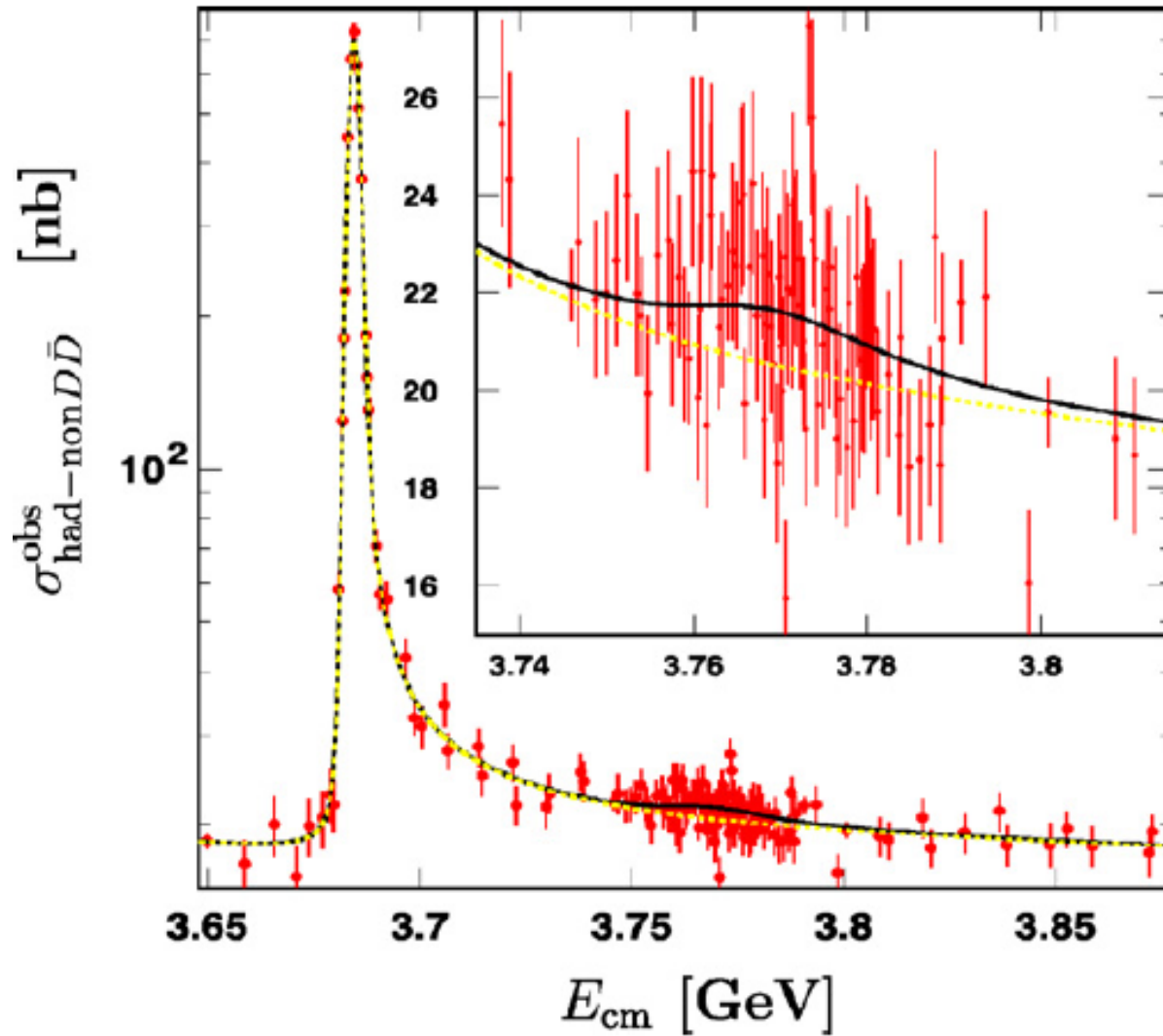
M. Ablikim *et al.*, Phys. Rev. Lett. **97**, 121801 (2006); M. Ablikim *et al.*, Phys. Lett. B **641**, 145 (2006); M. Ablikim *et al.*, Phys. Rev. D **76**, 122002 (2007); M. Ablikim *et al.*, Phys. Lett. B **659**, 74 (2008).

$$\sigma_{D\bar{D}}^{\text{obs}} = (6.07 \pm 0.40 \pm 0.35) \text{ nb}$$

S. Dobbs *et al.*, Phys. Rev. D **76**, 112001 (2007).

Quantity	Value
$\sigma(e^+e^- \rightarrow D^0\bar{D}^0)$	$(3.66 \pm 0.03 \pm 0.06) \text{ nb}$
$\sigma(e^+e^- \rightarrow D^+D^-)$	$(2.91 \pm 0.03 \pm 0.05) \text{ nb}$
$\sigma(e^+e^- \rightarrow D\bar{D})$	$(6.57 \pm 0.04 \pm 0.10) \text{ nb}$
$\sigma(e^+e^- \rightarrow D^+D^-)/\sigma(e^+e^- \rightarrow D^0\bar{D}^0)$	$0.79 \pm 0.01 \pm 0.01$

## Inclusive non-D $\bar{D}$ hadronic cross sections from BES



- **BES-II:** non- $D \bar{D}$  branching ratio can be up to 15%

$$\sigma_{\text{non-}D\bar{D}}^{\text{obs}} = (1.08 \pm 0.40 \pm 0.15) \text{ nb}$$

- **CLEO-c:**  $\text{BR}_{\psi(3770) \rightarrow D\bar{D}} = (103.0 \pm 1.4^{+5.1}_{-6.8})\%$

The lower bound suggests the maximum of non- $D \bar{D}$  b.r. is about 6.8%.

**Updated results from CLEO-c : 1004.1358[hep-ex]**

$$\mathcal{B}(\psi(3770) \rightarrow \text{non-}D\bar{D}) = (-3.3 \pm 1.4^{+6.6}_{-4.8}) \%$$

$< 9\%$  at 90% confidence level

## ■ Theoretical discrepancies:

### In theory

Y. P. Kuang and T. M. Yan, Phys. Rev. D **41**, 155 (1990).

Y. B. Ding, D. H. Qin, and K. T. Chao, Phys. Rev. D **44**, 3562 (1991).

J. L. Rosner, Phys. Rev. D **64**, 094002 (2001).

J. L. Rosner, Ann. Phys. (N.Y.) **319**, 1 (2005).

E. Eichten, S. Godfrey, H. Mahlke, and J. L. Rosner, Rev. Mod. Phys. **80**, 1161 (2008).

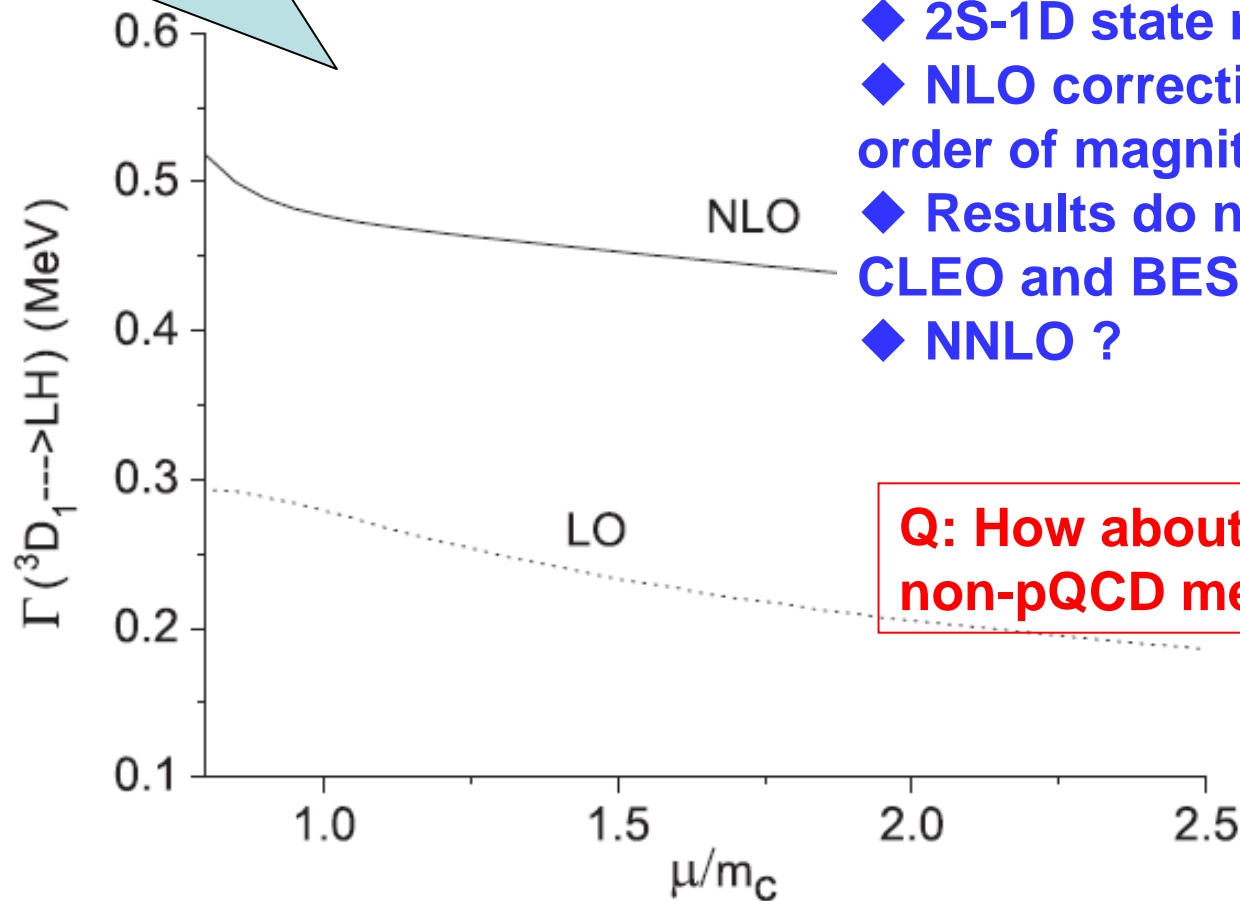
M. B. Voloshin, Phys. Rev. D **71**, 114003 (2005).

N. N. Achasov and A. A. Kozhevnikov, Phys. At. Nucl. **69**, 988 (2006).

Z. G. He, Y. Fan, and K. T. Chao, Phys. Rev. Lett. **101**, 112001 (2008).



pQCD calculation:  
 $\text{BR}(\text{non-}D \rightarrow \bar{D}) < 5\%$



- ◆ Short-range pQCD transition;
- ◆ Color-octet contributions are included;
- ◆ 2S-1D state mixings are small;
- ◆ NLO correction is the same order of magnitude as LO.
- ◆ Results do not favor both CLEO and BES
- ◆ NNLO ?

Q: How about the long-range non-pQCD mechanisms?

Z.G. He, Y. Fan, and K.T. Chao, Phys. Rev. Lett. **101**, 112001 (2008).

# □ Recognition of possible long-range transition mechanisms

## pQCD (non-relativistic QCD):

◆ If the heavy  $c \bar{c}$  are good constituent degrees of freedom,  $c$  and  $\bar{c}$  annihilate at the origin of the  $(c \bar{c})$  wavefunction. Thus, NRQCD should be valid.

◆ pQCD is dominant in  $\psi(3770)$  → light hadrons via  $3g$  exchange, hence the OZI rule will be respected.

⇒  $\psi(3770)$  non- $D \bar{D}$  decay will be suppressed.

## Non-pQCD:

◆ Are the constituent  $c \bar{c}$  good degrees of freedom for  $\psi(3770)$  → light hadrons? Or is pQCD dominant at all?

◆ If not, how the OZI rule is violated?

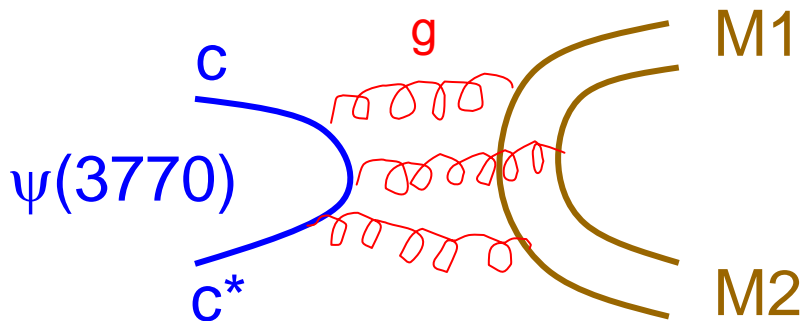
⇒ **Could the OZI-rule violation led to sizeable  $\psi(3770)$  non- $D \bar{D}$  decay?**

⇒ **How to quantify it?**

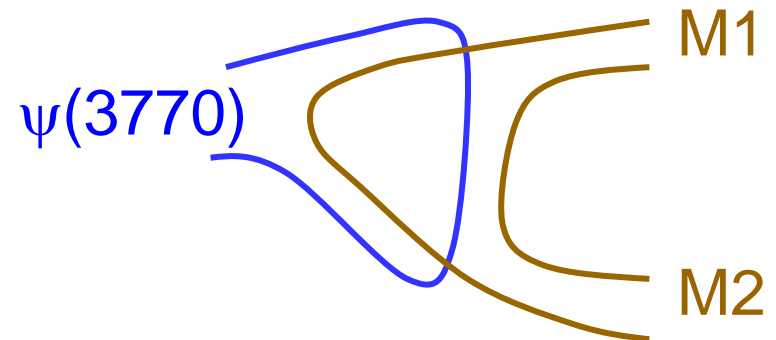
## □ Recognition of long-range transition mechanisms

in  $\psi(3770)$  non-D  $\bar{D}$  decays

Short-range pQCD transition  
via single OZI (SOZI) process



Long-range OZI evading transition



# $\psi(3770)$ decays to vector and pseudoscalar via $D \bar{D}$ and $D \bar{D}^* + \text{c.c.}$ rescatterings

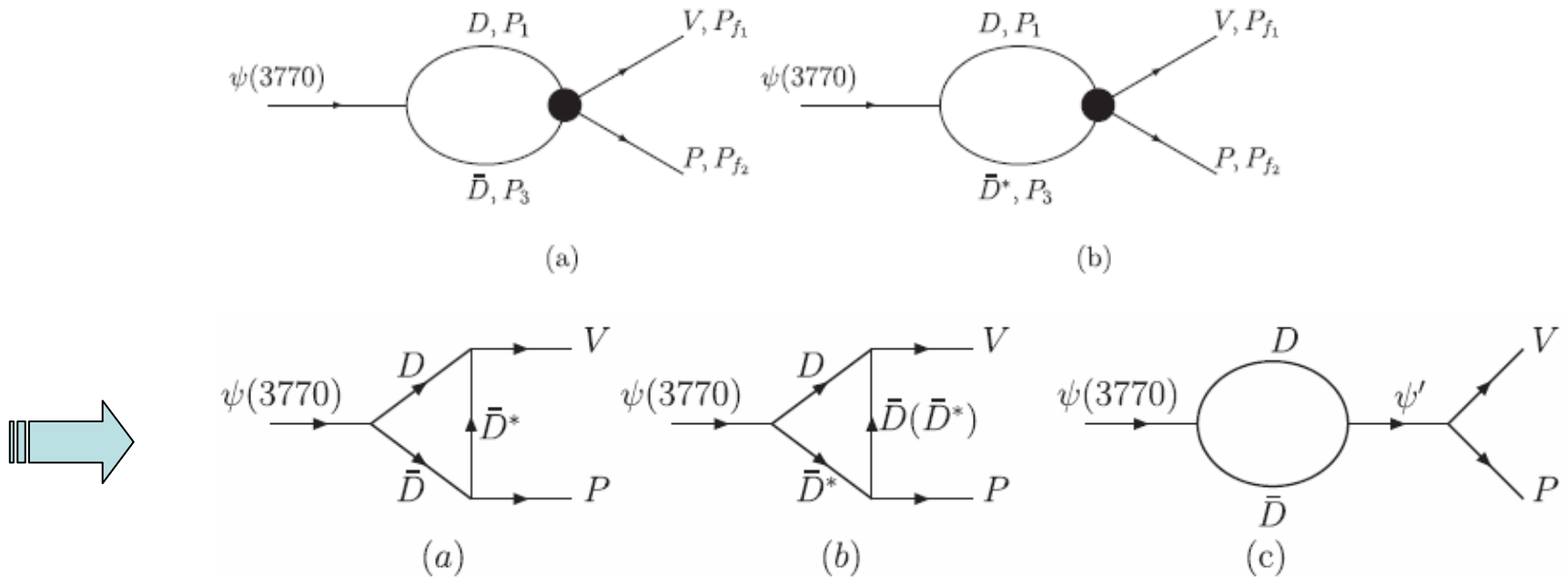


FIG. 2. The  $t$ - [(a) and (b)] and  $s$ -channel (c) meson loops in  $\psi(3770) \rightarrow VP$ .

The  $V \rightarrow VP$  transition has only one single coupling of anti-symmetric tensor form

Transition amplitude can thus be decomposed as:

Long-range non-  
pQCD amp.

Short-range  
pQCD amp.

$$\mathcal{M}_{fi} = \mathcal{M}^L + e^{i\delta} \mathcal{M}^{\text{SOZI}} \equiv i[g_L + e^{i\delta} g_S \mathcal{F}_S(\vec{p}_V)] \\ \times \varepsilon_{\alpha\beta\mu\nu} P_\psi^\alpha \epsilon_\psi^\beta P_V^\mu \epsilon_V^{*\nu} / M_{\psi(3770)},$$

## ■ Effective Lagrangians for meson couplings

$$\begin{aligned}
 \mathcal{L}_{\psi D \bar{D}} &= g_{\psi D \bar{D}} \{ D \partial_\mu \bar{D} - \partial_\mu D \bar{D} \} \psi^\mu, \\
 \mathcal{L}_{V D \bar{D}^*} &= -i g_{V D \bar{D}^*} \epsilon_{\alpha\beta\mu\nu} \partial^\alpha V^\beta \partial^\mu \bar{D}^{*\nu} D + \text{H.c.}, \\
 \mathcal{L}_{\mathcal{P} D^* \bar{D}^*} &= -i g_{\mathcal{P} D^* \bar{D}^*} \epsilon_{\alpha\beta\mu\nu} \partial^\alpha D^{*\beta} \partial^\mu \bar{D}^{*\nu} \mathcal{P} + \text{H.c.}, \\
 \mathcal{L}_{\mathcal{P} \bar{D} D^*} &= g_{D^* \mathcal{P} \bar{D}} \{ \bar{D} \partial_\mu \mathcal{P} - \partial_\mu \bar{D} \mathcal{P} \} D^{*\mu} + \text{H.c.},
 \end{aligned}$$

**Coupling constants:**

$$g_{\psi(3770) D^+ D^-} = 12.71 \quad g_{\psi(3770) D^0 \bar{D}^0} = 12.43$$

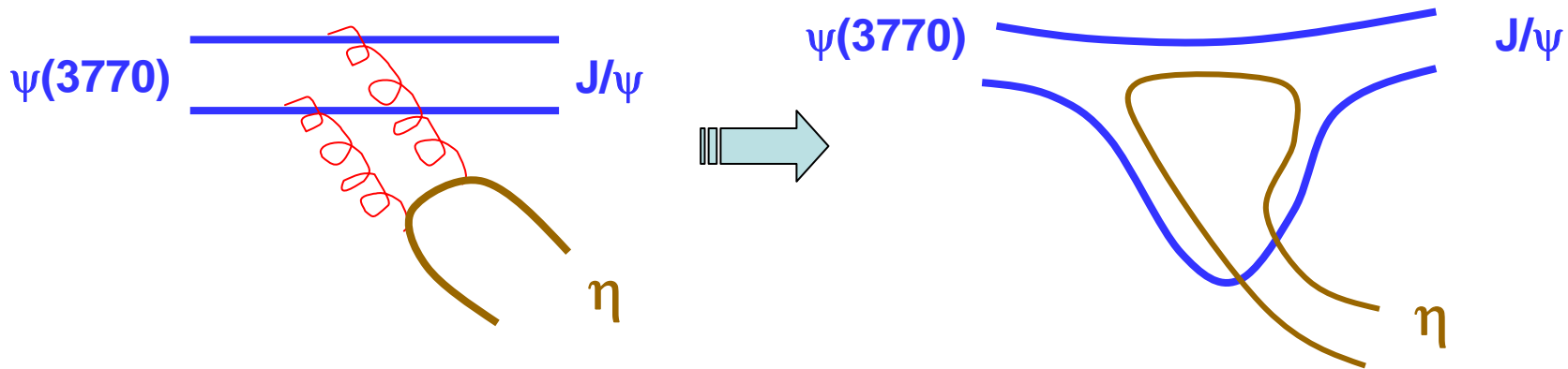
$$g_{D^* D \pi} = \frac{2}{f_\pi} g \sqrt{m_D m_{D^*}}, \quad g_{D^* D^* \pi} = \frac{g_{D^* D \pi}}{\tilde{M}_D},$$

$$g_{D^* D \rho} = \sqrt{2} \lambda g_\rho, \quad g_{D D \rho} = g_{D^* D \rho} \tilde{M}_D,$$

where  $f_\pi = 132$  MeV is the pion decay constant, and  $\tilde{M}_D \equiv \sqrt{m_D m_{D^*}}$  sets a mass scale. The parameters  $g_\rho$  respect the relation  $g_\rho = m_\rho / f_\pi$  [20]. We take  $\lambda = 0.56 \text{ GeV}^{-1}$  and  $g = 0.59$  [21,22].

**Cacalbuoni et al, Phys. Rept. (1997).**

i) Determine long-range parameter in  $\psi(3770) \rightarrow J/\psi \eta$ .



$$\text{BR}_{J/\psi \eta}^{\text{exp}} = (9.0 \pm 4) \times 10^{-4}$$

$$\mathcal{F}(q^2) = \left( \frac{\Lambda^2 - m_{\text{ex}}^2}{\Lambda^2 - q^2} \right)^2,$$

where  $\Lambda \equiv m_{\text{ex}} + \alpha \Lambda_{\text{QCD}}$ , with  $\Lambda_{\text{QCD}} = 0.22 \text{ GeV}$ .

◆ Soft  $\eta$  production

◆  $\eta$ - $\eta'$  mixing is considered

◆ a form factor is needed to kill the loop integral divergence

$$\alpha = 1.73$$

The cut-off energy for the divergent meson loop integral can be determined by data, and then extended to other processes.

**ii) Determine short-range parameter combining  $\psi(3770) \rightarrow \phi\eta$  and  $\psi(3770) \rightarrow \rho\pi$ .**

**Relative strengths among pQCD transition amplitudes:**

$$g_S^{\rho^0\pi^0} : g_S^{K^{*+}K^-} : g_S^{\omega\eta} : g_S^{\omega\eta'} : g_S^{\phi\eta} : g_S^{\phi\eta'}$$

$$= 1:1:\cos\alpha_P:\sin\alpha_P:(-\sin\alpha_P):\cos\alpha_P$$

$$\begin{cases} \eta = \cos\alpha_P |n\bar{n}\rangle - \sin\alpha_P |s\bar{s}\rangle, \\ \eta' = \sin\alpha_P |n\bar{n}\rangle + \cos\alpha_P |s\bar{s}\rangle, \end{cases}$$

With  $\alpha = 1.73$  fixed, we can then determine the other two parameters  $g_S \equiv g_S^{\rho^0\pi^0} = 0.085$  and  $\delta = -66^\circ$  by experimental data, i.e.,  $\text{BR}_{\phi\eta} = (3.1 \pm 0.7) \times 10^{-4}$  [8] and  $\text{BR}_{\rho\pi} < 0.24\%$  with C.L. of 90% [28].

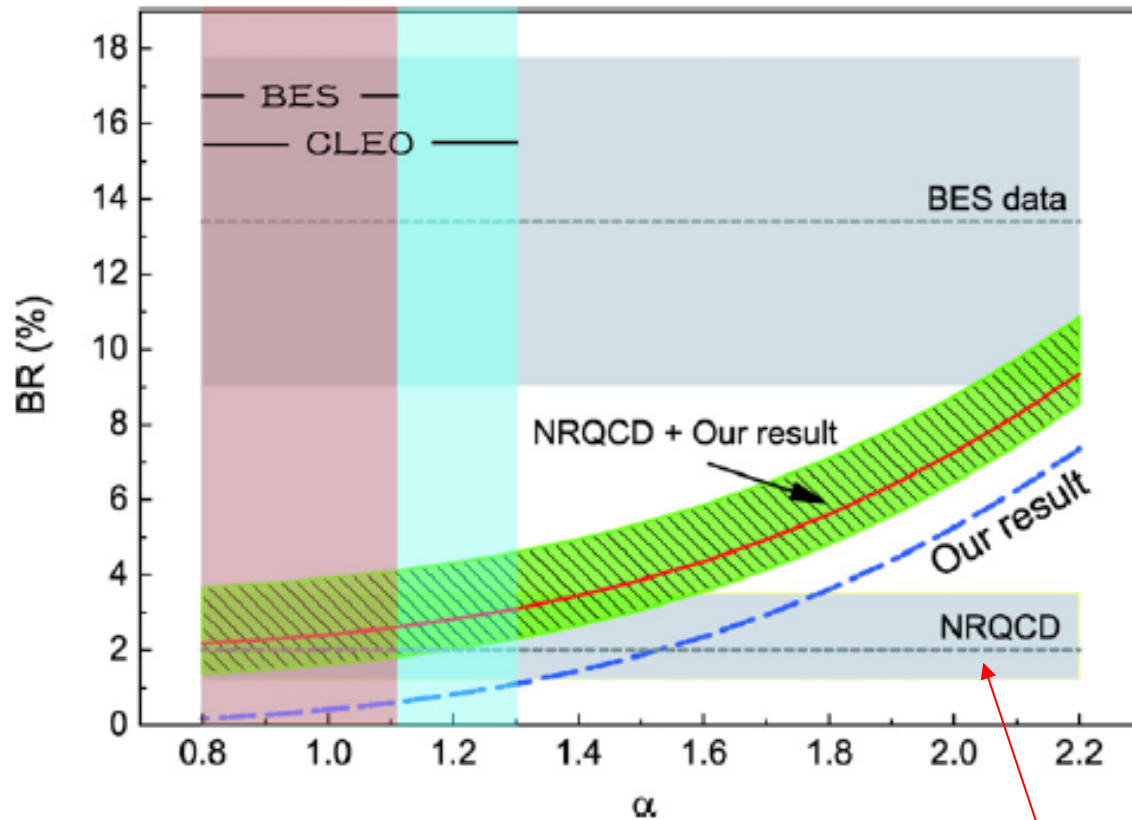


### iii) Predictions for $\psi(3770) \rightarrow VP$ .

BR ( $\times 10^{-4}$ )	$t$ channel	$s$ channel	SOZI	Total
$J/\psi \eta$	8.44	0.13	$\dots$	9.0
$J/\psi \pi^0$	0.1	$2.58 \times 10^{-2}$	$\dots$	$4.4 \times 10^{-2}$
$\rho \pi$	34.45	$7.69 \times 10^{-5}$	8.53	24.0
$K^{*+} K^- + \text{c.c}$	10.97	$6.83 \times 10^{-6}$	5.72	8.91
$K^{*0} \bar{K}^0 + \text{c.c}$	11.80	$4.38 \times 10^{-5}$	5.72	9.90
$\phi \eta$	1.25	$1.13 \times 10^{-5}$	1.16	3.1
$\phi \eta'$	0.87	$2.53 \times 10^{-5}$	1.86	3.78
$\omega \eta$	6.83	$9.64 \times 10^{-6}$	1.88	4.69
$\omega \eta'$	0.58	$2.87 \times 10^{-5}$	0.97	0.39
$\rho \eta$	$1.88 \times 10^{-2}$	$1.77 \times 10^{-5}$	$\dots$	$1.8 \times 10^{-2}$
$\rho \eta'$	$1.08 \times 10^{-2}$	$1.54 \times 10^{-5}$	$\dots$	$1.0 \times 10^{-2}$
$\omega \pi^0$	$2.57 \times 10^{-2}$	$1.82 \times 10^{-5}$	$\dots$	$2.5 \times 10^{-2}$
Sum	75.34	0.16	25.84	63.87

By varying  $\delta$ , but keeping the  $\phi \eta$  rate unchanged (i.e.  $g_S$  will be changed), we obtain a lower bound for the sum of branching ratios  $\sim 0.41\%$ .

X. Liu, B. Zhang and X.Q. Li, PLB675, 441(2009)



Z. G. He, Y. Fan, and K. T. Chao, Phys. Rev. Lett. **101**, 112001 (2008).

## ■ Further evidence for the role played by IHL

### ◆ “ $\rho\pi$ puzzle” in $J/\psi$ , $\psi(3686) \rightarrow VP$ .

[Zhao, Li and Chang, PLB645, 173(2007); Li, Zhao, and Chang, JPG (2008); Zhao, Li and Chang, arXiv:0812.4092[hep-ph], and work in progress]

### ◆ Isospin-violating decays as a probe for IML, e.g. $\psi' \rightarrow J/\psi \pi^0$ , $h_c \pi^0$ , etc.

[Guo, Hanhart, and Meissner, PRL103, 082003(2009); Guo et al, 1002.2712[hep-ph], and also talk by Hanhart at this conference]

### ◆ An analogue to the $\psi(3770)$ non-D $\bar{D}$ decay: the $\phi(1020)$ non-K $\bar{K}$ decay

[Li, Zhao and Zou, PRD77, 014010(2008); Li, Zhang and Zhao, JPG36, 085008(2009)].

◆ Helicity selection rule evading in  $\chi_{c1} \rightarrow VV$ ,  $\chi_{c2} \rightarrow VP$ , and  $\eta_c$ ,  $\chi_{c0}$ ,  $h_c \rightarrow B \bar{B}$ ,

[Liu and Zhao, PRD81, 014017(2010); arXiv: 1004.0496]

◆ More to be studied in order to gain systematic insights into the underlying mechanisms ...



***Thanks !***

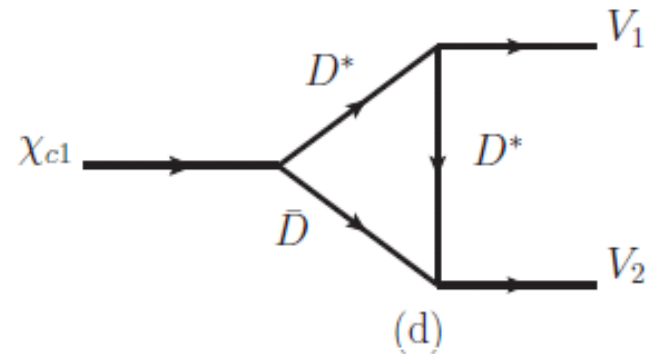
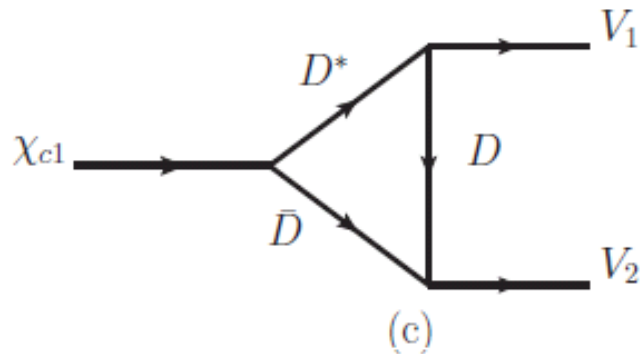
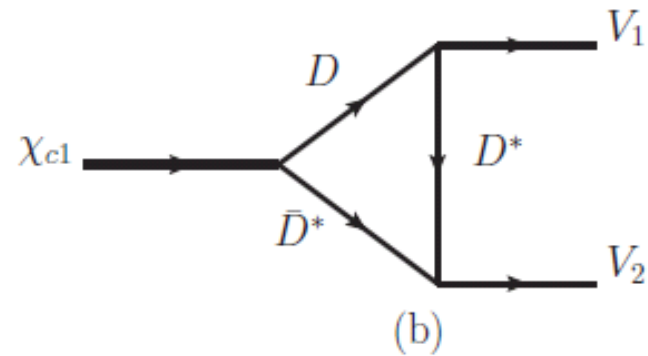
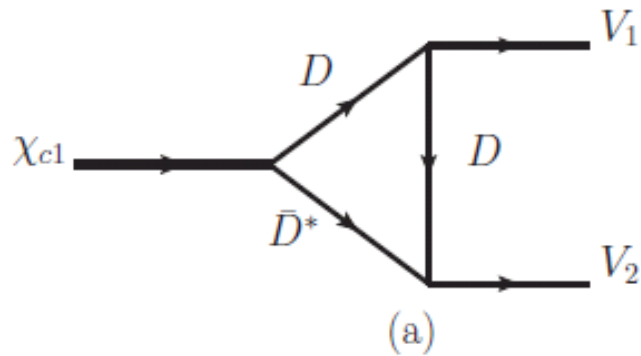
## *Backup slides*

$\chi_{c1} \rightarrow VV$  and  $\chi_{c2} \rightarrow VP$

-- further evidence for the IML

# Long-distance contribution

Intermediate charmed meson loop transitions  
in  $\chi_{c1} \rightarrow VV$



# Wavefunctions and effective Lagrangian based on heavy quark symmetry and SU(3) flavor symmetry

The spin multiplet for these four  $P$ -wave charmonium states are expressed as

$$P_{c\bar{c}}^\mu = \left( \frac{1 + \not{v}}{2} \right) \left( \chi_{c2}^{\mu\alpha} \gamma_\alpha + \frac{1}{\sqrt{2}} \epsilon_{\mu\nu\alpha\beta} v^\alpha \gamma^\beta \chi_{c1}^\nu + \frac{1}{\sqrt{3}} (\gamma^\mu - v^\mu) \chi_{c0} + h_c^\mu \gamma_5 \right) \left( \frac{1 - \not{v}}{2} \right).$$

The charmed and anti-charmed meson triplet read

$$\begin{aligned} H_{1i} &= \left( \frac{1 + \not{v}}{2} \right) [\mathcal{D}_i^{*\mu} \gamma_\mu - \mathcal{D}_i \gamma_5], \\ H_{2i} &= [\bar{\mathcal{D}}_i^{*\mu} \gamma_\mu - \bar{\mathcal{D}}_i \gamma_5] \left( \frac{1 - \not{v}}{2} \right), \end{aligned}$$

$$\text{where } \mathcal{D}^{(*)} = (D^{0(*)}, D^{+(*)}, D_s^{+(*)}).$$

**Effective Lagrangian for the P-wave charmonium couplings to charmed mesons:**

$$\mathcal{L}_1 = ig_1 \text{Tr}[P_{c\bar{c}}^\mu \bar{H}_{2i} \gamma_\mu \bar{H}_{1i}] + H.c.$$



The effective Lagrangians describe the couplings of charmed mesons to light hadrons read

$$\begin{aligned}
\mathcal{L}_{\mathcal{D}\mathcal{D}\mathcal{V}} &= -ig_{DDV}\bar{\mathcal{D}}_i\overset{\leftrightarrow}{\partial}_\mu\mathcal{D}_j(\mathcal{V}^\mu)_{ij}, \\
\mathcal{L}_{\mathcal{D}^*\mathcal{D}\mathcal{V}} &= -2f_{D^*DV}\epsilon_{\mu\nu\alpha\beta}(\partial^\mu\mathcal{V}^\nu)_{ij}(\bar{\mathcal{D}}_i\overset{\leftrightarrow\alpha}{\partial}\mathcal{D}_j^{*\beta}-\bar{\mathcal{D}}_i^{*\beta}\overset{\leftrightarrow\alpha}{\partial}\mathcal{D}_j), \\
\mathcal{L}_{\mathcal{D}^*\mathcal{D}^*\mathcal{V}} &= ig_{D^*D^*V}\bar{\mathcal{D}}_i^{*\nu}\overset{\leftrightarrow}{\partial}_\mu\mathcal{D}_{j\nu}^*(\mathcal{V}^\mu)_{ij}+4if_{D^*D^*V}\bar{\mathcal{D}}_i^{*\mu}(\partial_\mu\mathcal{V}_\nu-\partial_\nu\mathcal{V}_\mu)_{ij}\mathcal{D}_j^{*\nu}, \\
\mathcal{L}_{\mathcal{D}^*\mathcal{D}\mathcal{P}} &= -ig_{D^*DP}(\bar{\mathcal{D}}_i\partial_\mu\mathcal{P}_{ij}\mathcal{D}_j^{*\mu}-\bar{\mathcal{D}}_i^{*\mu}\partial_\mu\mathcal{P}_{ij}\mathcal{D}_j), \\
\mathcal{L}_{\mathcal{D}^*\mathcal{D}^*\mathcal{P}} &= \frac{1}{2}g_{D^*D^*P}\epsilon_{\mu\nu\alpha\beta}\bar{\mathcal{D}}_i^{*\mu}\partial^\nu\mathcal{P}_{ij}\overset{\leftrightarrow\alpha}{\partial}\mathcal{D}_j^{*\beta},
\end{aligned}$$

$$\mathcal{V} = \begin{pmatrix} \frac{1}{\sqrt{2}}(\rho^0 + \omega) & \rho^+ & K^{*+} \\ \rho^- & \frac{1}{\sqrt{2}}(-\rho^0 + \omega) & K^{*0} \\ K^{*-} & \bar{K}^{*0} & \phi \end{pmatrix}$$

$$\mathcal{P} = \begin{pmatrix} \frac{1}{\sqrt{2}}(\pi^0 + \eta) & \pi^+ & K^+ \\ \pi^- & \frac{1}{\sqrt{2}}(-\pi^0 + \eta) & K^0 \\ K^- & \bar{K}^0 & -\sqrt{\frac{2}{3}}\eta \end{pmatrix}$$

# Transition amplitudes for $\chi_{c1} \rightarrow VV$

With an effective Lagrangian method considering heavy quark symmetry and SU(3) symmetry, the IML amplitudes are expressed as

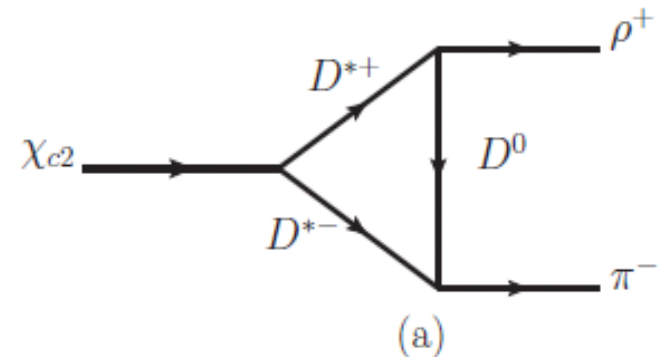
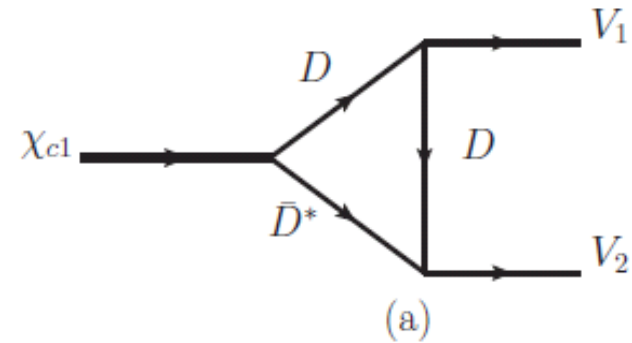
$$\begin{aligned}\mathcal{M}_{1a} &= 2ig_{DD^*\chi_{c1}}g_{DDV}f_{D^*DV}\epsilon_{\lambda}^{\chi_{c1}}\epsilon_1^{*\sigma}\epsilon_2^{*\tau}\int\frac{d^4q}{(2\pi)^4} \\ &\times (q_{1\sigma}+q_{\sigma})\epsilon_{\mu\tau\alpha\beta}p_2^{\mu}(q^{\alpha}-q_2^{\alpha})\frac{g^{\lambda\beta}-q_2^{\lambda}q_2^{\beta}/m_{D^*}^2}{D_aD_1D_2}\mathcal{F}(q^2) \\ \mathcal{M}_{1b} &= 2ig_{DD^*\chi_{c1}}g_{DDV}f_{D^*DV}\epsilon_{\lambda}^{\chi_{c1}}\epsilon_1^{*\sigma}\epsilon_2^{*\tau}\int\frac{d^4q}{(2\pi)^4} \\ &\times \epsilon_{\mu\sigma\alpha\beta}p_1^{\mu}(q_1^{\alpha}+q^{\alpha})\left[g_{D^*D^*V}(q_{2\tau}-q_{\tau})g_{\gamma\delta}+4f_{D^*D^*V}(p_{2\delta}g_{\tau\gamma}-p_{2\gamma}g_{\delta\tau})\right] \\ &\times (g^{\beta\gamma}-q^{\beta}q^{\gamma}/m_{D^*}^2)(g^{\lambda\delta}-q_2^{\lambda}q_2^{\delta}/m_{D^*}^2)\times\frac{1}{D_bD_1D_2}\mathcal{F}(q^2)\end{aligned}$$

The phenomenologically introduced form factor:

$$\mathcal{F}(q^2) = \prod_i \left( \frac{m_i^2 - \Lambda_i^2}{q_i^2 - \Lambda_i^2} \right)$$

where  $\Lambda_i = m_i + \alpha\Lambda_{QCD}$

## Couplings for $\chi_{c1}$ and $\chi_{c2}$ to charmed mesons



$$g_{DD^*\chi_{c1}} = 2\sqrt{2}g_1\sqrt{m_D m_{D^*} m_{\chi_{c1}}},$$

$$g_{D^*D^*\chi_{c2}} = 4g_1 m_{D^*} \sqrt{m_{\chi_{c2}}},$$

$$g_1 = -\sqrt{\frac{m_{\chi_{c0}}}{3}} \frac{1}{f_{\chi_{c0}}},$$

with  $f_{\chi_{c0}} \simeq 0.51 \text{ GeV}$

Casalbuoni et al, Phys. Rept. 281, 145(1997); Cheng, Chua, and Soni, PRD71, 014030 (2005)

# Numerical Result for $\chi_{c1} \rightarrow VV$

BR ( $\times 10^{-4}$ )	$K^{*0} \bar{K}^{*0}$	$\rho\rho$	$\omega\omega$	$\phi\phi$
Exp. data	$16 \pm 4$	—	—	—
Meson loop	$12 \sim 20$	$26 \sim 54$	$8.7 \sim 18$	$2.7 \sim 4.6$
SU(3) ( $R = 1$ )	16.0	26.8	8.8	6.8
SU(3) ( $R = 0.838$ )	16.0	32.0	10.6	4.0

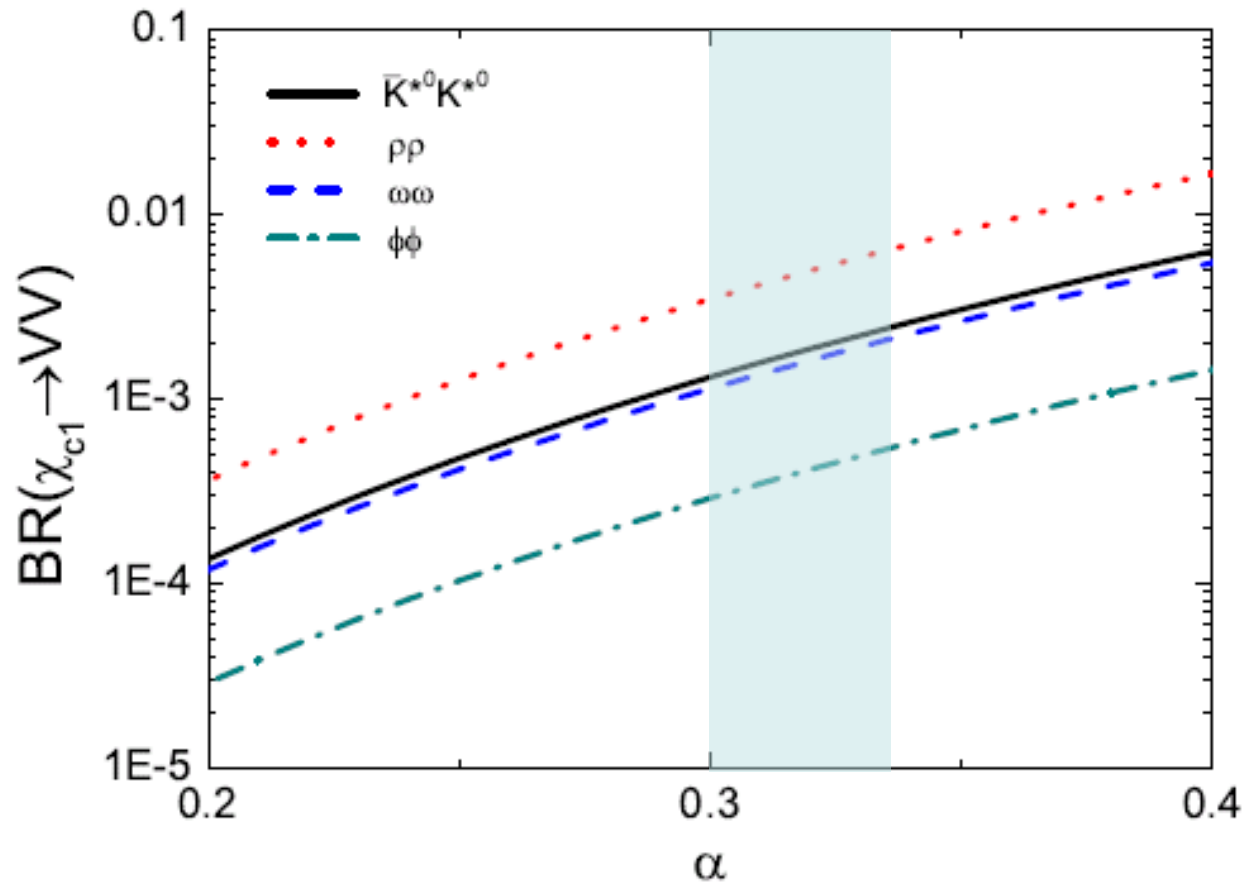
$\alpha=0.3 \sim 0.33$

The results of a simple parameterization method based on SU(3) flavour symmetry are also presented in the table, where

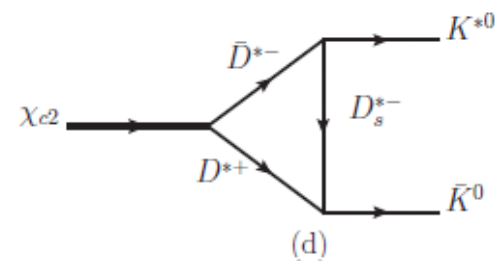
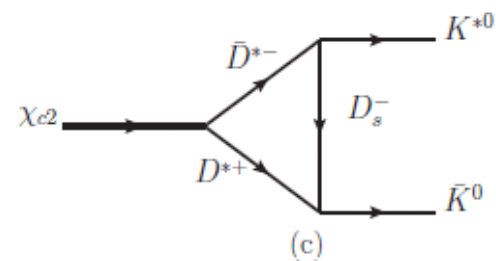
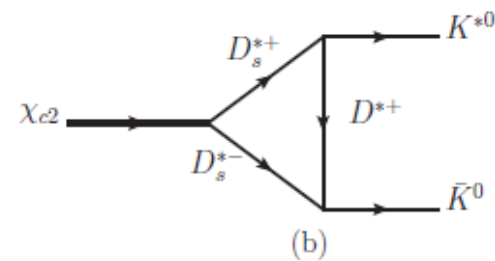
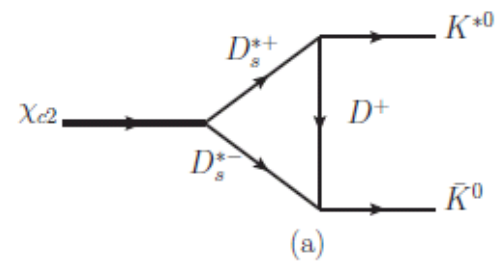
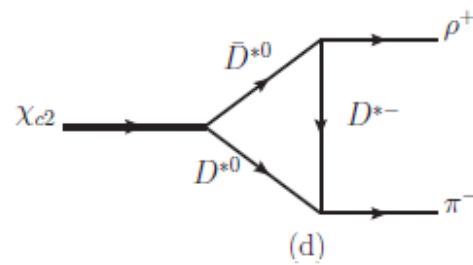
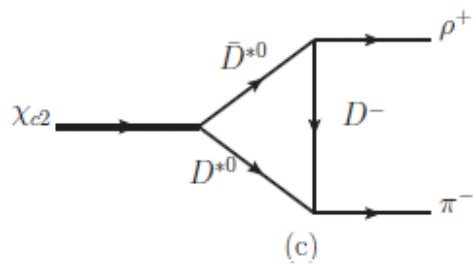
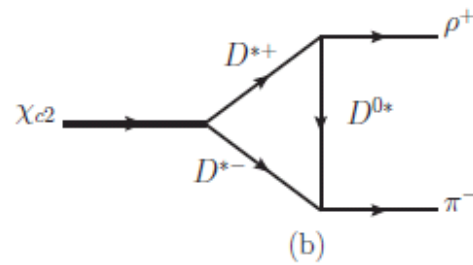
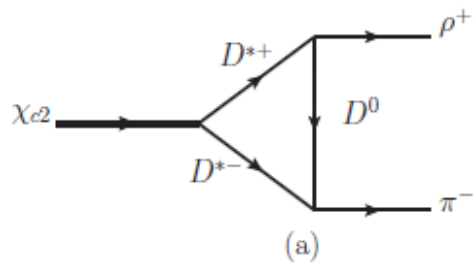
$$R \equiv \langle (q\bar{s})_{V_1} (s\bar{q})_{V_2} | \hat{H} | \chi_{c1} \rangle / \langle (q\bar{q})_{V_1} (q\bar{q})_{V_2} | \hat{H} | \chi_{c1} \rangle$$

and  $R \simeq f_\pi / f_K$

# Model-dependence on $\alpha$



# $\chi_{c2} \rightarrow VP$



◆ Further suppressed by approximate G-parity or isospin/U-spin conservation.

◆ Decay to neutral VP is forbidden by C-parity conservation.

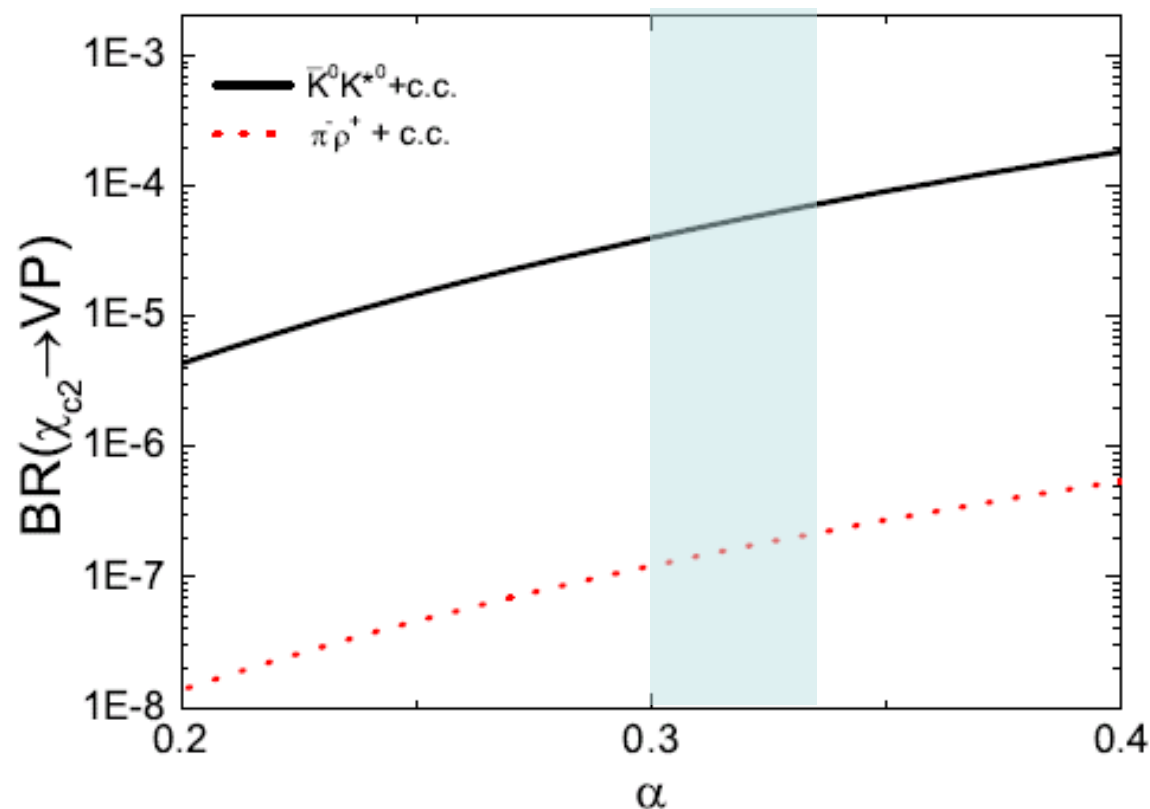
# Transition amplitudes for $\chi_{c2} \rightarrow VP$

$$\begin{aligned}
 \mathcal{M}_{2a} &= 2ig_{D^*D^*\chi_{c2}}f_{D^*DV}g_{D^*DP}\epsilon_{\xi\eta}^{\chi_{c2}}\epsilon_{\rho+}^{\nu}\int\frac{d^4q}{(2\pi)^4}\epsilon_{\mu\nu\alpha\beta}p_1^{\mu}(q_1^{\alpha}+q^{\alpha})p_2^{\lambda} \\
 &\times (g^{\xi\beta}-q_1^{\xi}q_1^{\beta}/m_{D^*}^2)(g^{\eta\lambda}-q_2^{\eta}q_2^{\lambda}/m_{D^*}^2)\frac{1}{D_aD_1D_2}\mathcal{F}(q^2), \\
 \mathcal{M}_{2b} &= -\frac{1}{2}ig_{D^*D^*\chi_{c2}}g_{D^*D^*P}\epsilon_{\xi\eta}^{\chi_{c2}}\epsilon_{\rho+}^{\tau}\int\frac{d^4q}{(2\pi)^4}\epsilon_{\rho\sigma\alpha\beta}p_2^{\sigma}(q^{\alpha}-q_2^{\alpha}) \\
 &\times [-g_{D^*D^*V}(q_{1\tau}+q_{\tau})g^{\gamma\delta}-4f_{D^*D^*V}(p_1^{\gamma}g_{\tau}^{\delta}-p_1^{\delta}g_{\tau}^{\gamma})] \\
 &\times (g^{\xi\gamma}-q_1^{\xi}q_1^{\gamma}/m_{D^*}^2)(g^{\eta\beta}-q_2^{\eta}q_2^{\beta}/m_{D^*}^2)(g^{\delta\rho}-q^{\delta}q^{\rho}/m_{D^*}^2)\frac{1}{D_bD_1D_2}\mathcal{F}(q^2)
 \end{aligned}$$

# $\chi_{c2} \rightarrow VP$

$BR(\times 10^{-5})$	$K^{*0} \bar{K}^0 + c.c.$	$K^{*+} K^- + c.c.$	$\rho^+ \pi^- + c.c.$
Meson loop	4.0 ~ 6.7	4.0 ~ 6.7	$(1.2 \sim 2.0) \times 10^{-2}$
Exp. data	—	—	—

$\alpha = 0.3 \sim 0.33$





# Summary

- ◆ The long-distance rescattering effects can give sizeable contributions to the processes  $\chi_{c1} \rightarrow VV$  and  $\chi_{c2} \rightarrow VP$ , which are supposed to be suppressed according to the helicity selection rule.
- ◆ With the parameter  $\alpha$  constrained by the measured  $\text{BR}(\chi_{c1} \rightarrow \bar{K}^{*0}K^{*0})$ ,  $\text{BR}(\chi_{c1} \rightarrow VV)$  are predicted to be at least at the order of  $10^{-4}$ , and  $\text{BR}(\chi_{c2} \rightarrow \bar{K}^{*0}K + \text{c.c.})$  is at the order of  $10^{-5}$  that may be detectable.
- ◆ The P-wave charmonium decay should be ideal for examining the evading mechanisms of the helicity selection rule. The huge data sample accumulated by BESIII provide a good opportunity to check this.
- ◆ Similar mechanisms via intermediate hadron loops are also studied in  $\eta_c, \chi_{c0}, h_c \rightarrow B \bar{B}$ .