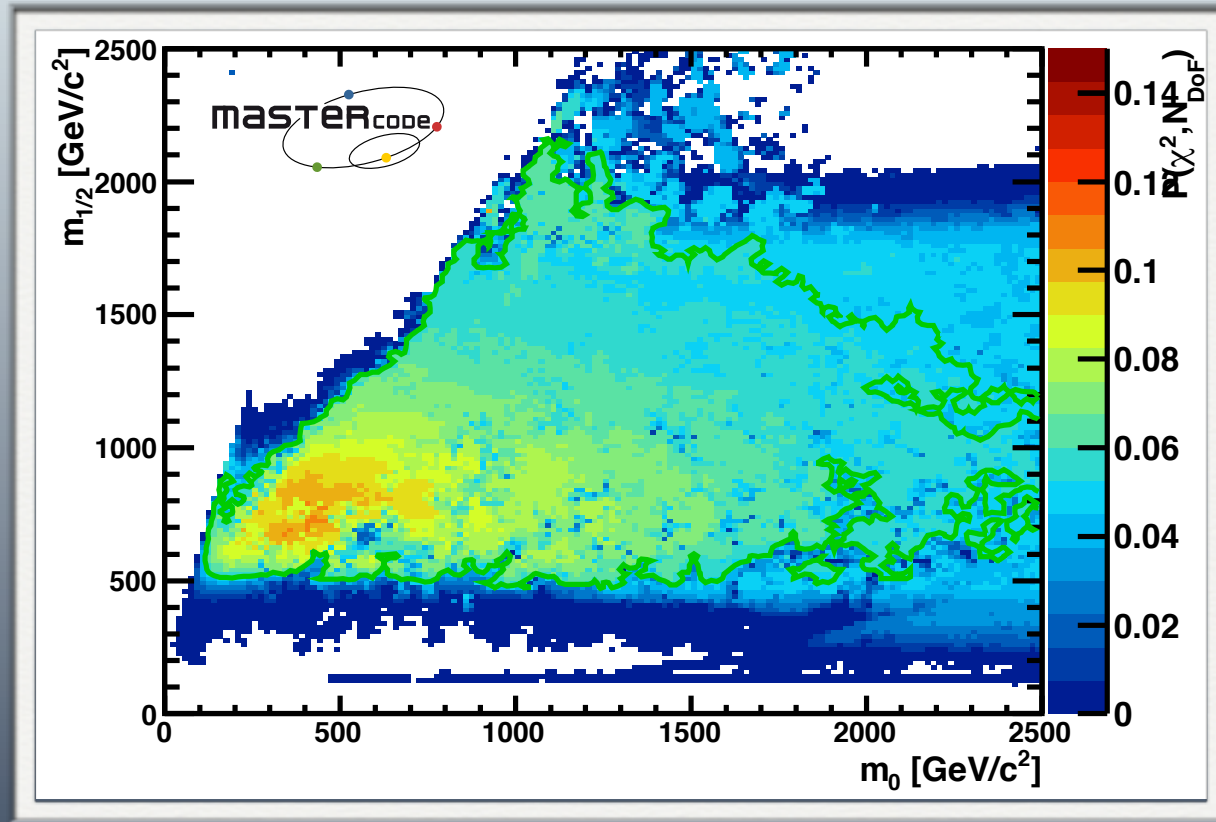


Confronting SUSY with LHC Data



O. Buchmüller, R. Cavanaugh, D. Colling, A. de Roeck, M.J. Dolan, J.R. Ellis,
H. Flaecher, S. Heinemeyer, G. Isidori, D. Martinez Santos, K.A. Olive, S.
Rogerson, F.J. Ronga, G. Weiglein

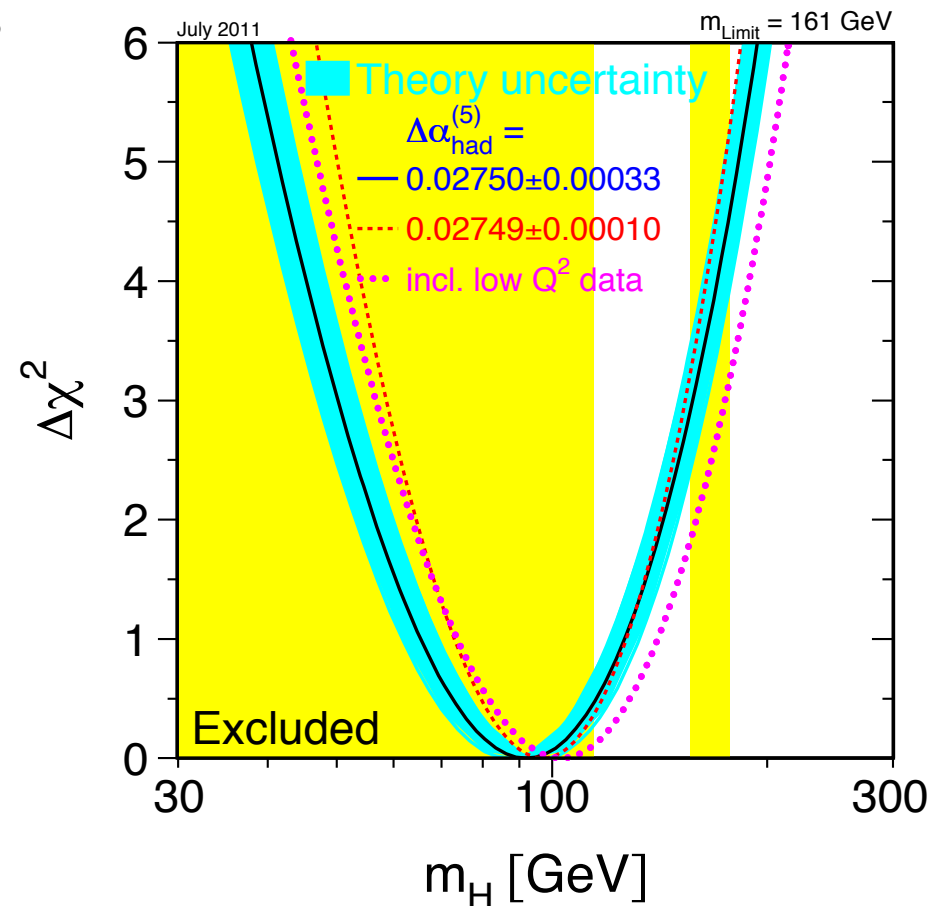
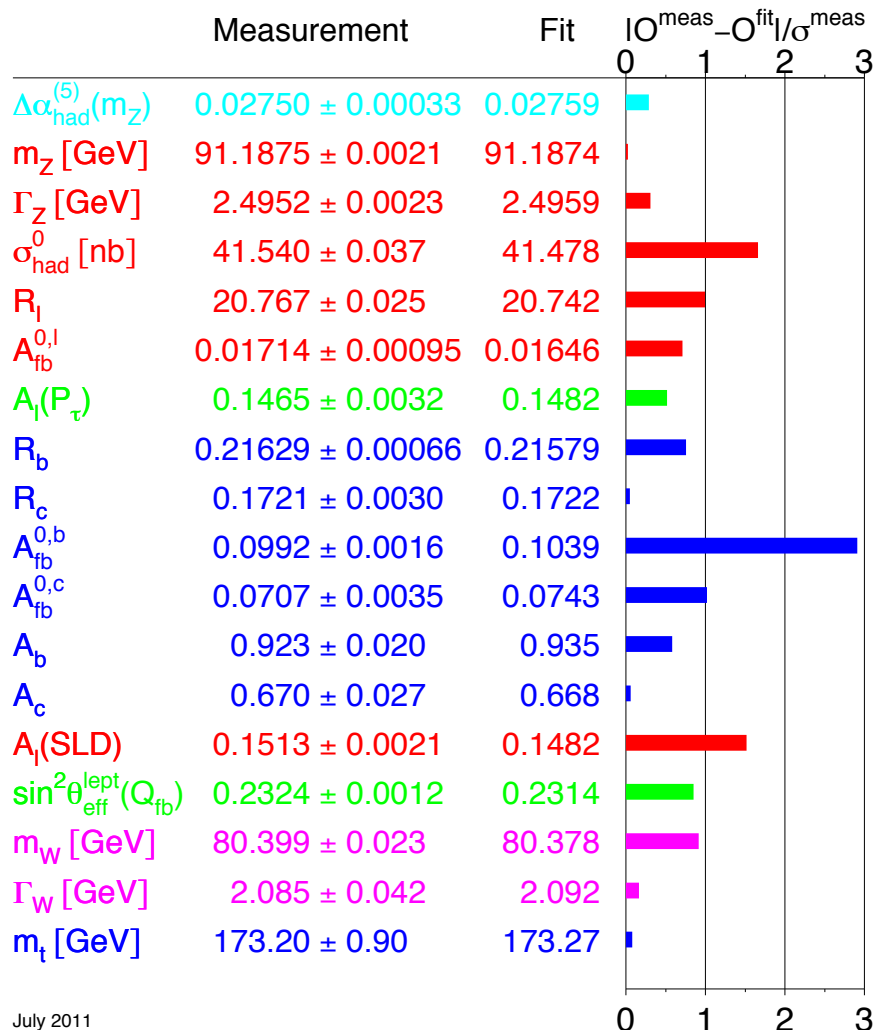
SUSY11

Fermilab, 28 August to 02 September, 2011

- Introduction
- Codes & Predictions
- Confronting Predictions with Data
- Conclusion

Introduction

- Well known global fit to all SM data: “Blue Band Plot”



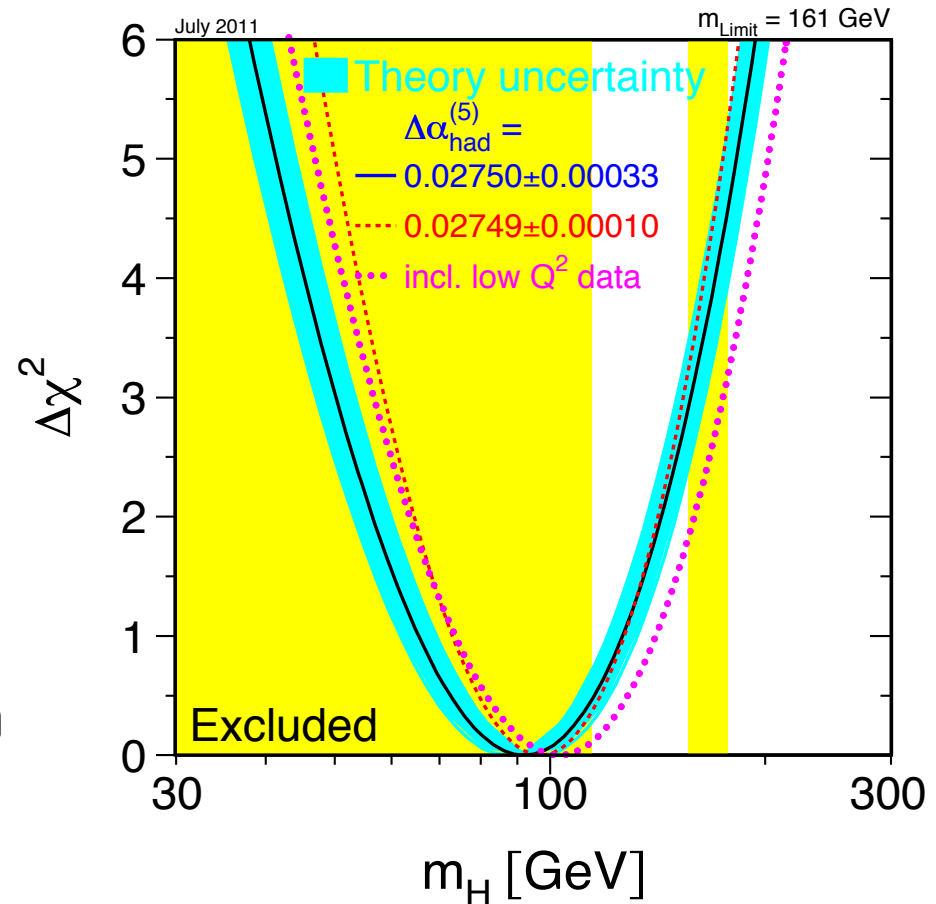
July 2011

- Well known global fit to all SM data: “Blue Band Plot”

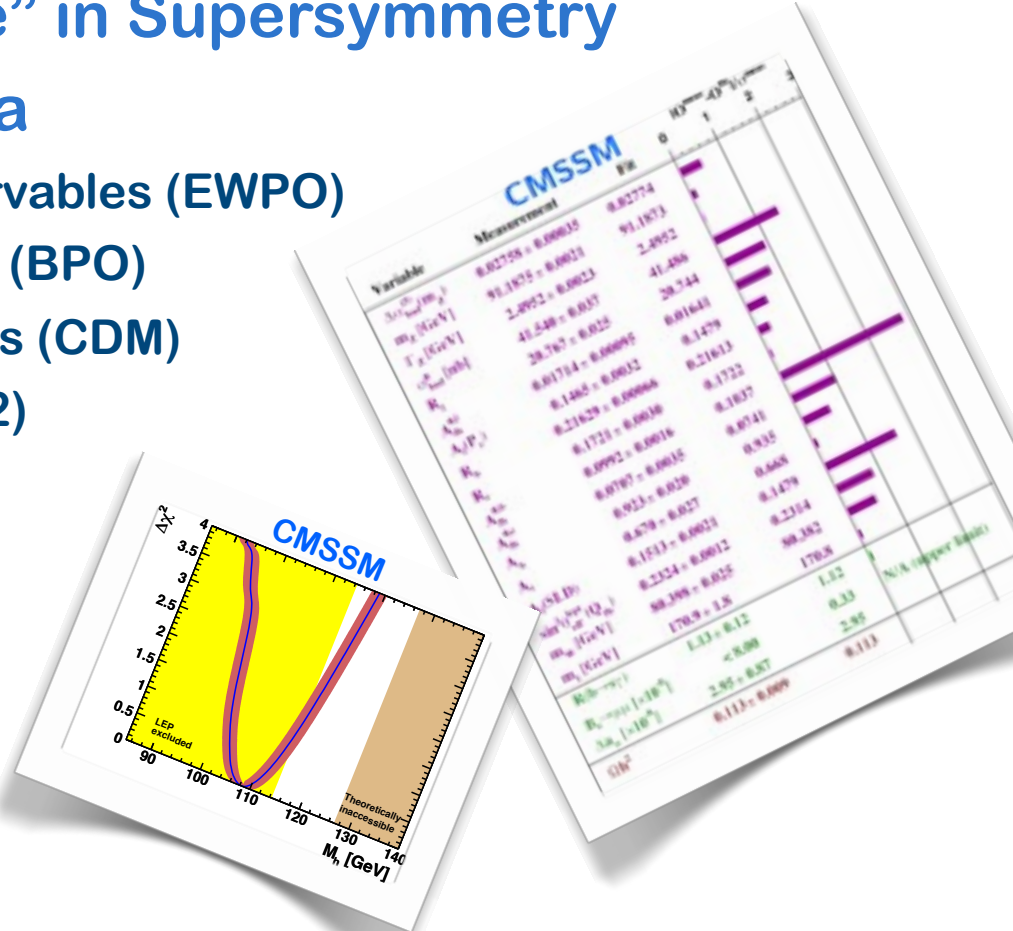
$$m_H = 92^{+34}_{-26} \text{ GeV}$$

$$m_H < 161 \text{ GeV} \\ \text{at 95\% CL}$$

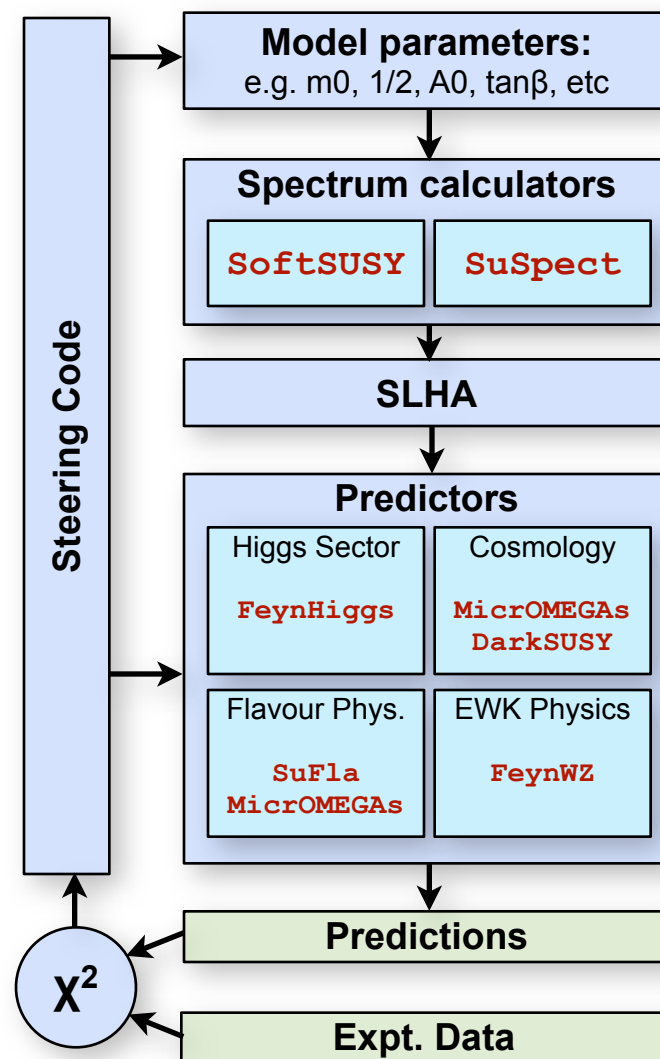
- Assumption for the fit :
SM including Higgs boson



- Main idea: do the “same” in Supersymmetry
- Combine all existing data
 - Electroweak precision observables (EWPO)
 - Flavour physics observables (BPO)
 - Cold dark matter observables (CDM)
 - Low Energy observables (g-2)
 - Direct Searches!
 - LHC
 - XENON100
- Predict
 - best-fit model space points
 - ranges for Higgs masses
 - ranges for SM parameters
 - ranges for SUSY masses (exclusion, reach, interpretation)
- Important! “Red Band” instead of “Blue Band” ;-)



- **Combines diverse set of tools**
 - different codes : all state-of-the-art
 - Electroweak Precision (**FeynWZ**)
 - Flavour (**SuFla**, **micrOMEGAs**)
 - Cold Dark Matter (**DarkSUSY**, **micrOMEGAs**)
 - Other low energy (**FeynHiggs**)
 - Higgs (**FeynHiggs**)
 - different precisions (one-loop, two-loop, etc)
 - different languages (Fortran, C++, English, German, Italian, etc)
 - different people (theorists, experimentalists)
- **Compatibility is crucial! Ensured by**
 - close collaboration of tools authors
 - standard interfaces



consistent use of most-up-to-date tools crucial for precision studies

List of Observables

Flavour and Low Energy Observables

$\text{BR}_{b \rightarrow s \gamma}^{\text{EXP}} / \text{BR}_{b \rightarrow s \gamma}^{\text{SM}}$	$\text{BR}_{K \rightarrow \pi \nu \nu}^{\text{EXP}} / \text{BR}_{K \rightarrow \pi \nu \nu}^{\text{SM}}$
$\text{BR}(B_s \rightarrow \mu \mu)$	$\Delta M_{B_s}^{\text{EXP}} / \Delta M_{B_s}^{\text{SM}}$
$\text{BR}_{B \rightarrow \tau \nu}^{\text{EXP}} / \text{BR}_{B \rightarrow \tau \nu}^{\text{SM}}$	$\frac{\Delta M_{B_s}^{\text{EXP}} / \Delta M_{B_s}^{\text{SM}}}{\Delta M_{B_d}^{\text{EXP}} / \Delta M_{B_d}^{\text{SM}}}$
$\text{BR}(B_d \rightarrow \mu \mu)$	$\Delta \epsilon_K^{\text{EXP}} / \Delta \epsilon_K^{\text{SM}}$
$\text{BR}_{B \rightarrow X_s l l}^{\text{EXP}} / \text{BR}_{B \rightarrow X_s l l}^{\text{SM}}$	$a_\mu^{\text{EXP}} - a_\mu^{\text{SM}}$

Dark Matter Observables

$$\Omega h^2$$

$$\sigma_p^{\text{SI}}$$

LHC High Energy Observables

$$\text{jets} + \cancel{E}_T$$

$$H/A, H^\pm$$

Electroweak Observables

Γ_Z	$A_{\text{fb}}(b)$
σ_{had}^0	$A_{\text{fb}}(c)$
R_l	A_b
$A_{\text{fb}}(l)$	A_c
$A_l(P_\tau)$	$A_l(\text{SLD})$
R_b	$\sin^2 \theta_W^l(Q_{\text{FB}})$
R_c	m_W

Standard Model Parameters

$$m_t$$

$$\Delta \alpha_{\text{had}}^{(5)}(m_Z^2)$$

$$m_Z$$

Light Higgs Sector

$$m_h$$

Model	Parameters	Boundary Conditions
CMSSM	$m_0, m_{1/2}, A_0, \tan(\beta), \text{sign}(\mu)$	Unification +
VCMSSM	$m_0, m_{1/2}, A_0, \text{sign}(\mu)$	$B_0 = A_0 - m_0$
mSUGRA	$m_0, m_{1/2}, A_0, \text{sign}(\mu)$	$B_0 = A_0 - m_0$
NUHM1	$m_0, m_{1/2}, A_0, m_{H_{1,2}}^2, \text{sign}(\mu)$	$m_{1,2} = m_0 + \Delta m_{H_{1,2}}$

Constructing the χ^2

$$\chi^2 = \sum_i^N \frac{(C_i - P_i)^2}{\sigma(C_i)^2 + \sigma(P_i)^2} + \sum_i^M \frac{(f_{\text{SM}_i}^{\text{obs}} - f_{\text{SM}_i}^{\text{fit}})^2}{\sigma(f_{\text{SM}_i})^2}$$

- N is number of observables studied
- M is number of SM parameters: $f_{\text{SM}_i} = \Delta\alpha_{\text{had}}, m_t, m_Z$
- C_i are experimentally measured values (constraint)
- P_i are MSSM parameter-dependent predictions

Constructing the χ^2

$$\chi^2 = \sum_i^N \frac{(C_i - P_i)^2}{\sigma(C_i)^2 + \sigma(P_i)^2} + \sum_i^M \frac{(f_{\text{SM}_i}^{\text{obs}} - f_{\text{SM}_i}^{\text{fit}})^2}{\sigma(f_{\text{SM}_i})^2}$$

- **Fit Methods (globally over all model parameters!)**
 - **Markov Chain Monte Carlo (MCMC)**
 - Actually used as a mere sampling method (sampling density not used)
 - success and failure of the steps defined by the χ^2
 - **χ^2 fit: Minuit minimisation**
 - used for “scans” or in conjunction with MCMCs to get overall best minimum

Constructing the χ^2

$$\chi^2 = \sum_i^N \frac{(C_i - P_i)^2}{\sigma(C_i)^2 + \sigma(P_i)^2} + \sum_i^M \frac{(f_{\text{SM}_i}^{\text{obs}} - f_{\text{SM}_i}^{\text{fit}})^2}{\sigma(f_{\text{SM}_i})^2} + \chi^2(b \rightarrow s\gamma) + \chi^2(g_\mu - 2) + \chi^2(\Omega h^2) + \chi^2(m_h)$$

- **Fit Methods (globally over all model parameters!)**

- **Markov Chain Monte Carlo (MCMC)**

- Actually used as a mere sampling method (sampling density not used)
- success and failure of the steps defined by the χ^2

- **χ^2 fit: Minuit minimisation**

- used for “scans” or in conjunction with MCMCs to get overall best minimum

- **Afterburners**

- **χ^2 terms additive $\rightarrow$ effects therefore also additive**

- **Study effect of “interesting” ($g-2$, $b \rightarrow s\gamma$, Ωh^2 , etc) observables!**

- sample space without “interesting” terms $\rightarrow$ larger, more general sampling
- a posteriori add “interesting” terms after general sampling
- Only need to sample multi-d space once! Enormous cost savings to due RGEs

$$\begin{aligned}\chi^2 = & \sum_i^N \frac{(C_i - P_i)^2}{\sigma(C_i)^2 + \sigma(P_i)^2} + \sum_i^M \frac{(f_{\text{SM}_i}^{\text{obs}} - f_{\text{SM}_i}^{\text{fit}})^2}{\sigma(f_{\text{SM}_i})^2} \\ & + \chi^2(b \rightarrow s\gamma) \quad + \chi^2(g_\mu - 2) \quad + \chi^2(\Omega h^2) \quad + \chi^2(m_h) \\ & + \chi^2(\text{BR}(B_s \rightarrow \mu\mu)) + \chi^2(\text{LHC}) \quad + \chi^2(\text{XENON100})\end{aligned}$$

- **Fit Methods (globally over all model parameters!)**

- **Markov Chain Monte Carlo (MCMC)**

- Actually used as a mere sampling method (sampling density not used)
- success and failure of the steps defined by the χ^2

- **χ^2 fit: Minuit minimisation**

- used for “scans” or in conjunction with MCMCs to get overall best minimum

- **Afterburners**

- **χ^2 terms additive $\rightarrow$ effects therefore also additive**

- **Study effect of “interesting” ($g-2$, $b \rightarrow s\gamma$, Ωh^2 , etc) observables!**

- sample space without “interesting” terms $\rightarrow$ larger, more general sampling
- a posteriori add “interesting” terms after general sampling
- Only need to sample multi-d space once! Enormous cost savings to due RGEs

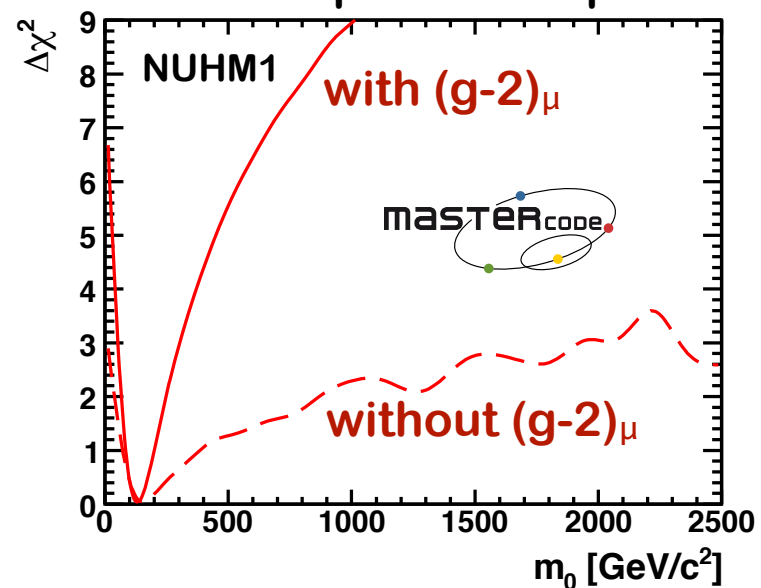
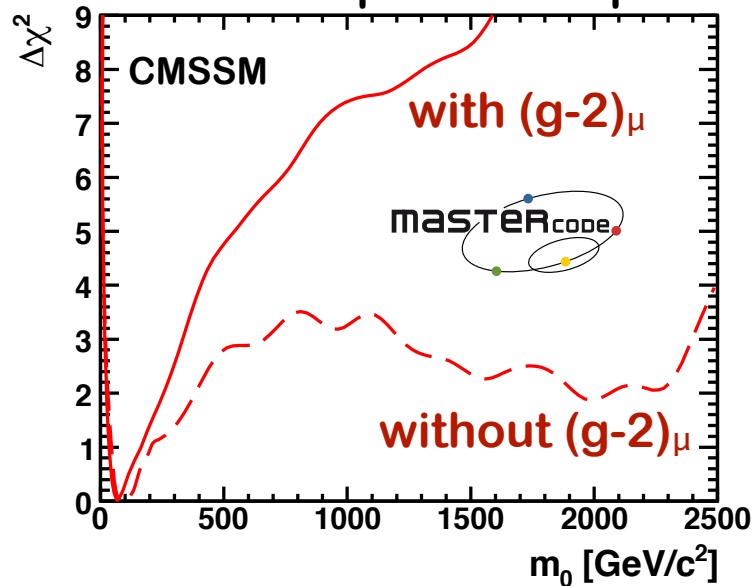
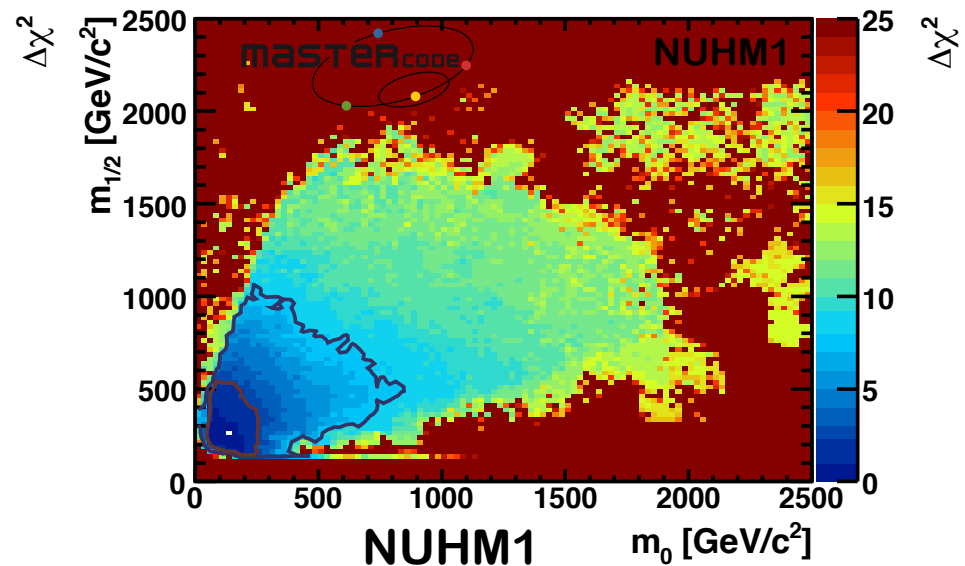
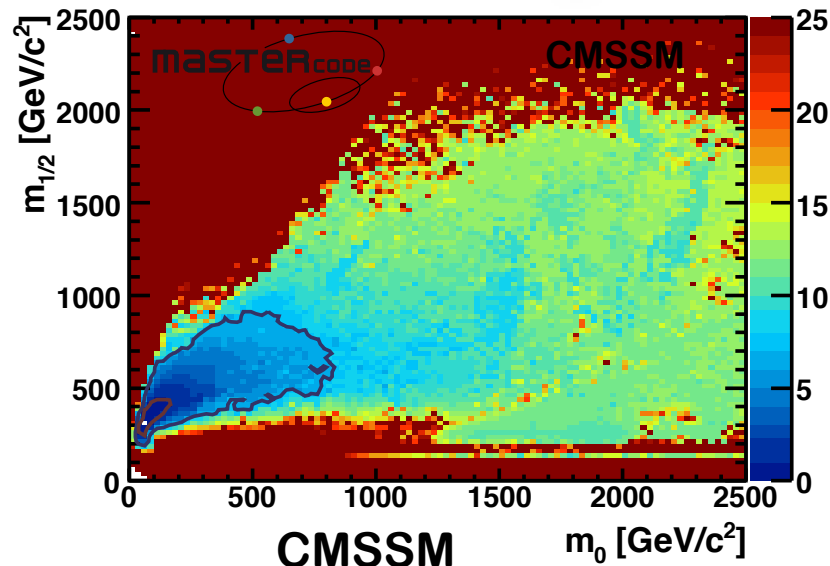
Constructing the χ^2

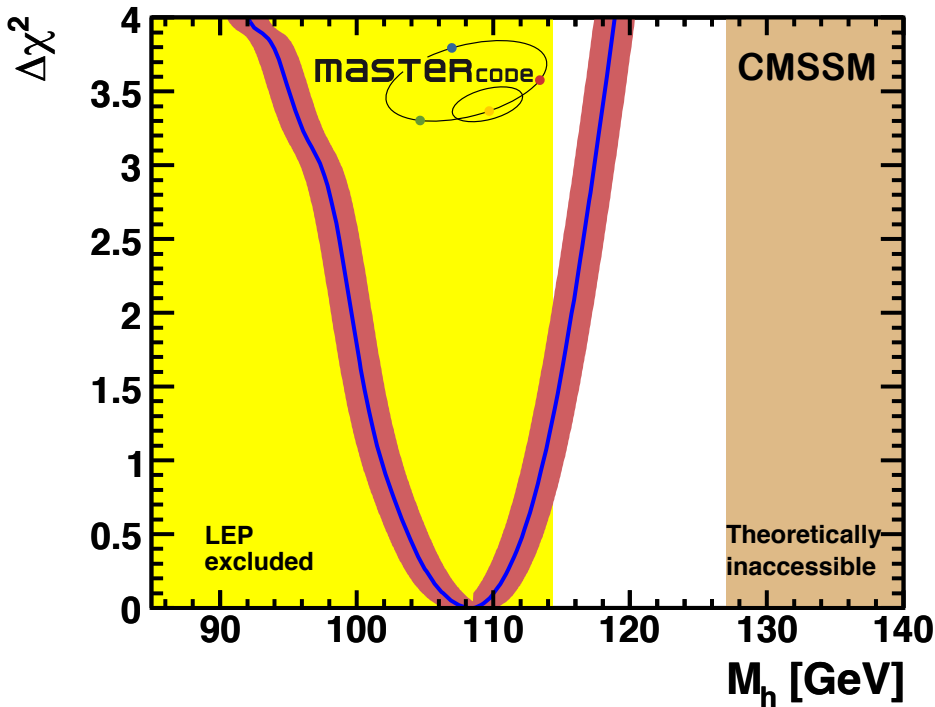
$$\begin{aligned}\chi^2 = & \sum_i^N \frac{(C_i - P_i)^2}{\sigma(C_i)^2 + \sigma(P_i)^2} + \sum_i^M \frac{(f_{\text{SM}_i}^{\text{obs}} - f_{\text{SM}_i}^{\text{fit}})^2}{\sigma(f_{\text{SM}_i})^2} \\ & + \chi^2(b \rightarrow s\gamma) + \chi^2(g_\mu - 2) + \chi^2(\Omega h^2) + \chi^2(m_h) \\ & + \chi^2(\text{BR}(B_s \rightarrow \mu\mu)) + \chi^2(\text{LHC}) + \chi^2(\text{XENON100})\end{aligned}$$

Recent Experimental Data!

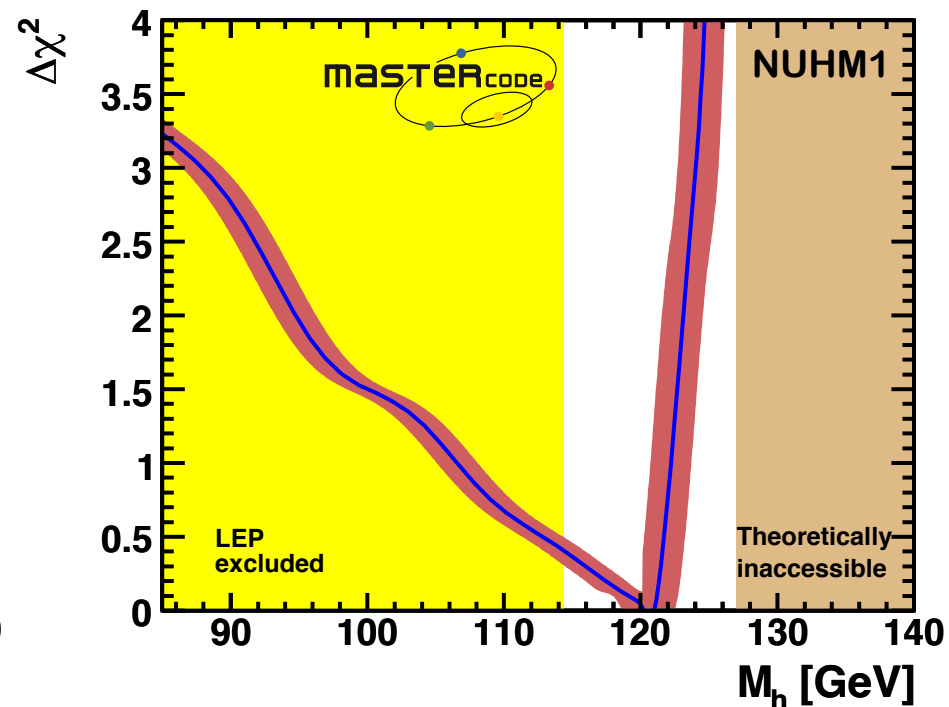
- **Fit Methods (globally over all model parameters!)**
 - **Markov Chain Monte Carlo (MCMC)**
 - Actually used as a mere sampling method (sampling density not used)
 - success and failure of the steps defined by the χ^2
 - **χ^2 fit: Minuit minimisation**
 - used for “scans” or in conjunction with MCMCs to get overall best minimum
- **Afterburners**
 - χ^2 terms additive $\rightarrow$ effects therefore also additive
 - **Study effect of “interesting” ($g-2$, $b \rightarrow s\gamma$, Ωh^2 , etc) observables!**
 - sample space without “interesting” terms $\rightarrow$ larger, more general sampling
 - a posteriori add “interesting” terms after general sampling
 - Only need to sample multi-d space once! Enormous cost savings to due RGEs

Pre-LHC, Pre-XENON100





CMSSM
25 million points sampled



NUHM1
25 million points sampled

SM Prediction: $m_H = 92^{+34}_{-26}$ GeV

Confronting SUSY with LHC

- ATLAS + CMS Direct Searches
- Combination of
 - CMS 1.1 fb^{-1} (α_T)
 - ATLAS 1.0 fb^{-1} (0-lepton)
- Assume

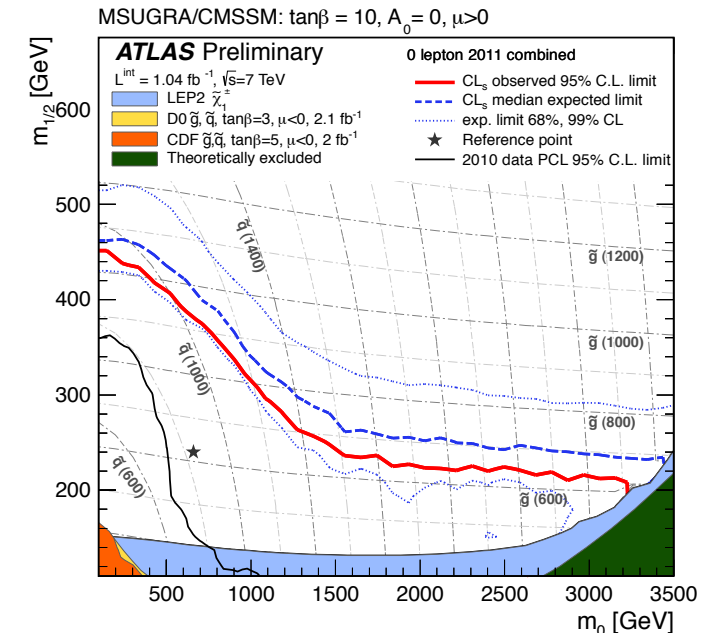
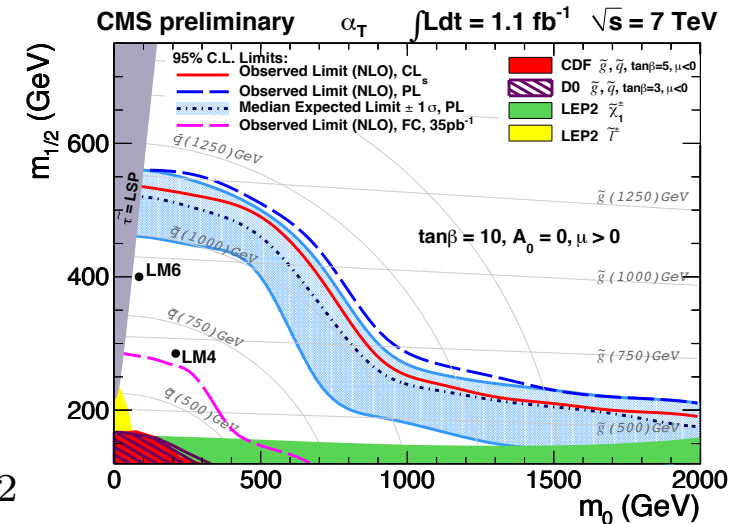
$$N_{\text{events}} \propto M^{-4} \quad \text{where} \quad M^2 = m_0^2 + m_{1/2}^2$$

then

$$\chi_p^2 \sim \chi_{95\%}^2 \times \left[\frac{M_p}{M_{95\%}} \right]^4$$

- For each point in $(m_0, m_{1/2})$ take

$$\max [\chi^2(\text{CMS}), \chi^2(\text{ATLAS})]$$



- For fixed values of M_A Assume

- Assume

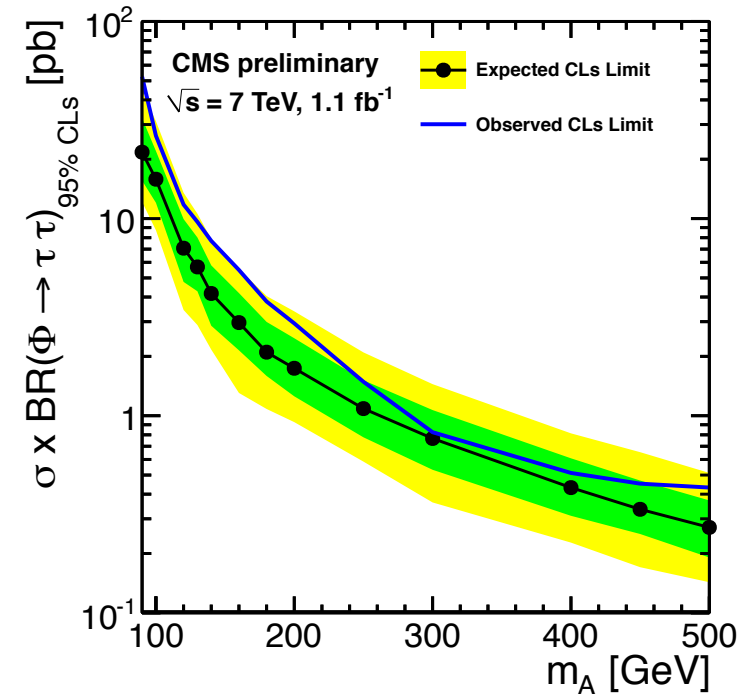
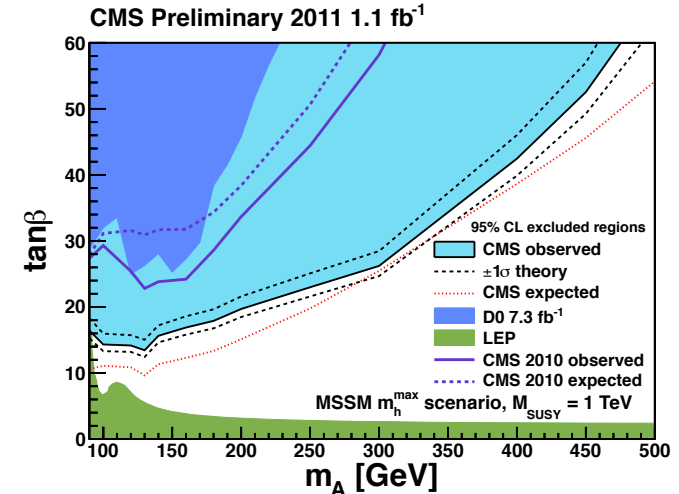
$$\chi^2 \propto (\sigma \times BR)^{p(M_A)}$$

- Now, in the region of interest

$$(\sigma \times BR) \propto \tan^2 \beta$$

- Hence,

$$\chi^2 \sim \left[\frac{\tan^2(\beta)}{\tan^2(\beta)_{68\%}} \right]^{p(M_A)}$$



- **LHCb**

- $\text{BR}(B_s \rightarrow \mu\mu) < 1.5 \times 10^{-8}$ at 95% CL

- **CMS**

- $\text{BR}(B_s \rightarrow \mu\mu) < 1.9 \times 10^{-8}$ at 95% CL

- **CDF**

- $\text{BR}(B_s \rightarrow \mu\mu) = (1.8^{+1.1}_{-0.9}) \times 10^{-8}$ at 95% CL

- $\text{BR}(B_s \rightarrow \mu\mu) < 4.0 \times 10^{-8}$ at 95% CL

- **Some tension with CMS, LHCb**

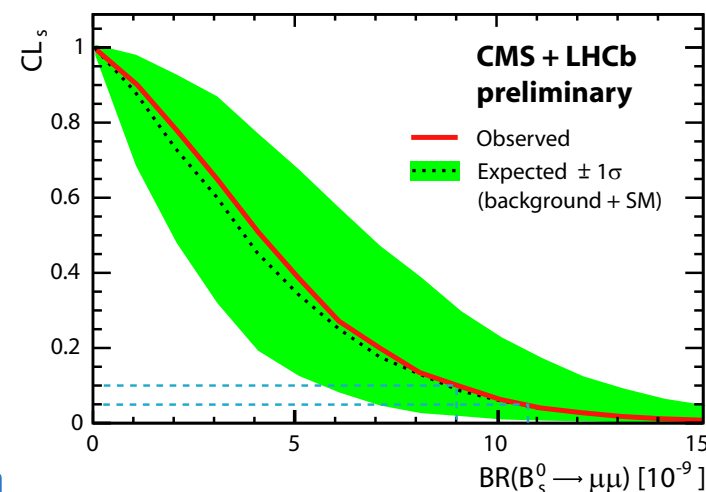
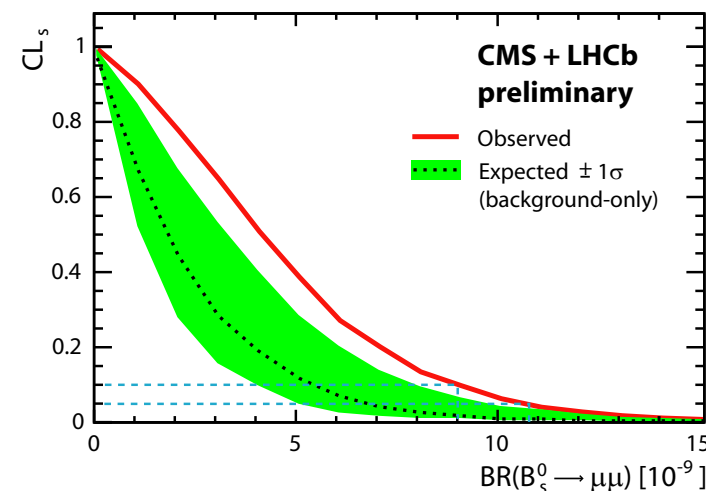
- but still compatible

- **Use combined CMS + LHCb**

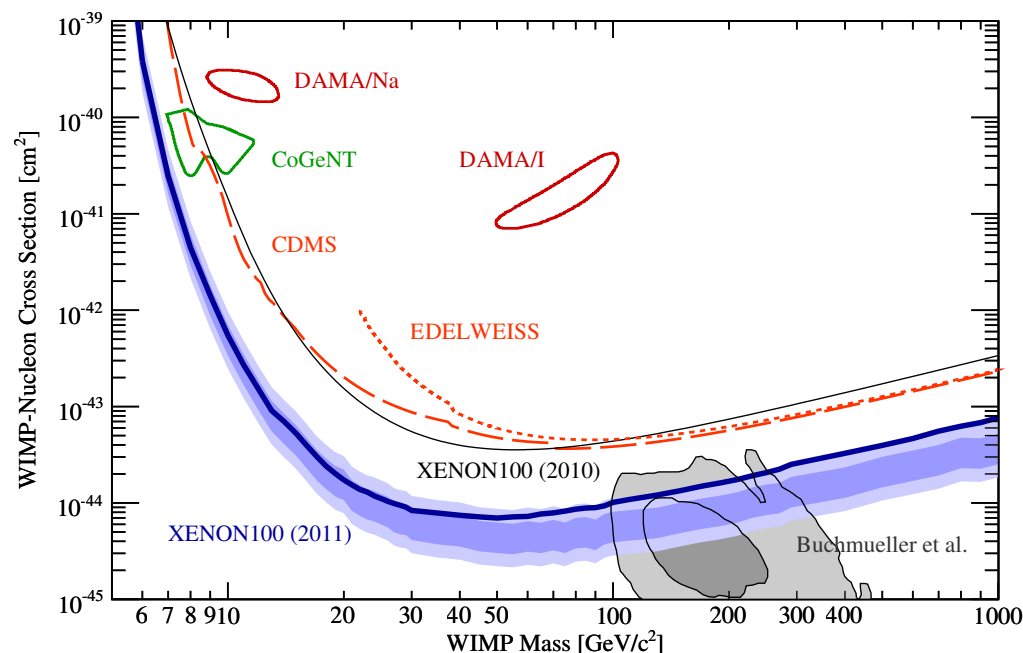
- $\text{BR}(B_s \rightarrow \mu\mu) < 1.08 \times 10^{-8}$ at 95% CL

- $\Delta\chi^2$ corresponds to full likelihood

- global minimum close to Standard Model value



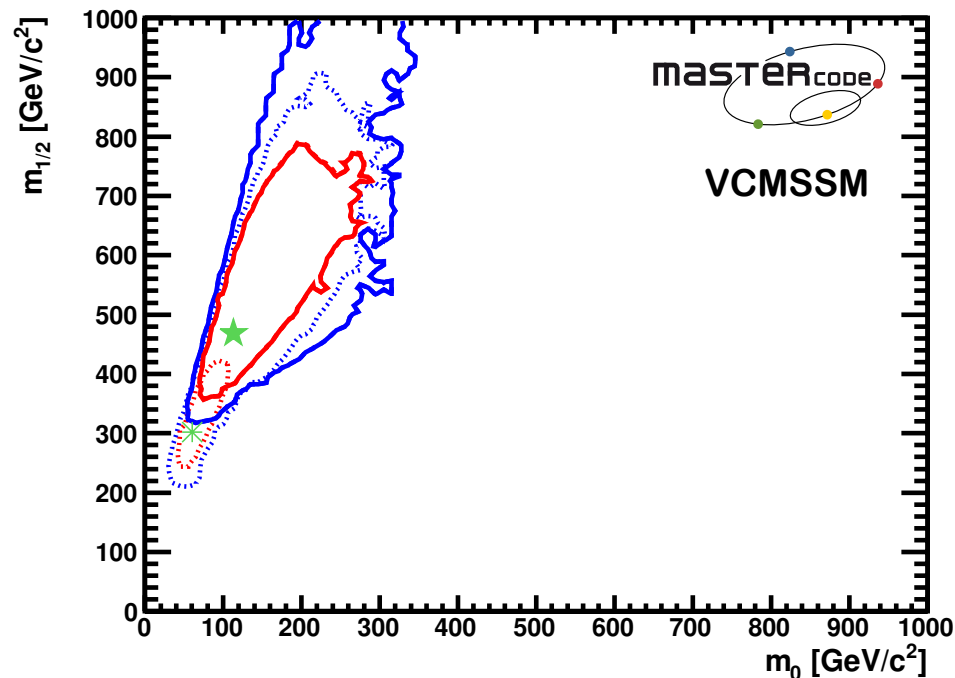
- Construct likelihood model for event numbers using CL_s method
 - Close to a Gaussian with $\mu = 1.2$, $\sigma = 3.2$
- 90% CL corresponds to 6.1 events, rescale from contour (right)



- The excess observed in XENON100 leads to a contribution of $\chi^2 = 0.3$ for small σ_p^{SI}
- The uncertainty on the π -nucleon σ term is also taken into account; we look at both
 - $\Sigma_{\pi N} = 50 \pm 14$
 - $\Sigma_{\pi N} = 64 \pm 8$

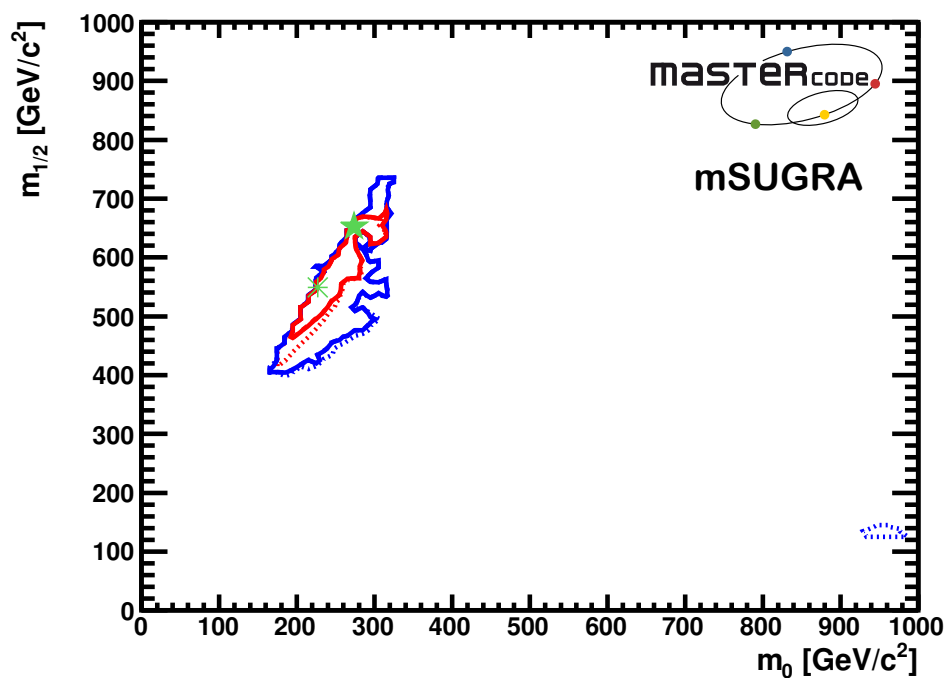
Post-LHC, Post-XENON100

2010 ATLAS + CMS with 36 pb⁻¹ of LHC Data



VCMSSM

60 million points sampled



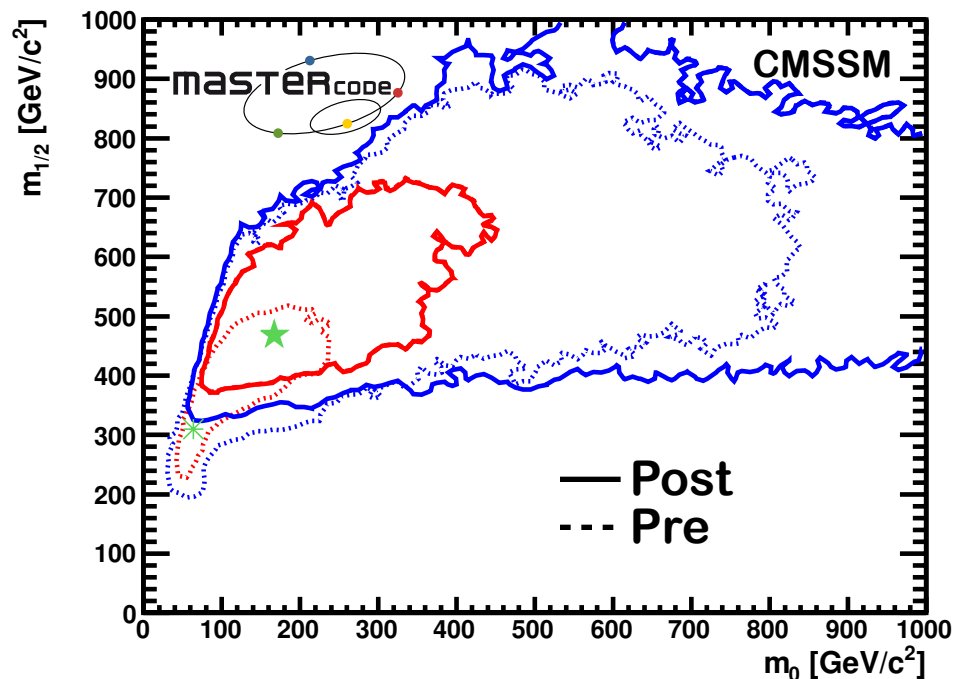
mSUGRA

60 million points sampled

Model	Min χ^2	Prob	$m_{1/2}$	m_0	A_0	$\tan \beta$
VCMSSM	22.5	31%	300	60	30	9
post-LHC/XENON100	27.1	13%	390	90	70	11
mSUGRA	29.4	6.1%	550	230	430	28
post-LHC/XENON100	30.9	5.7%	550	230	430	28

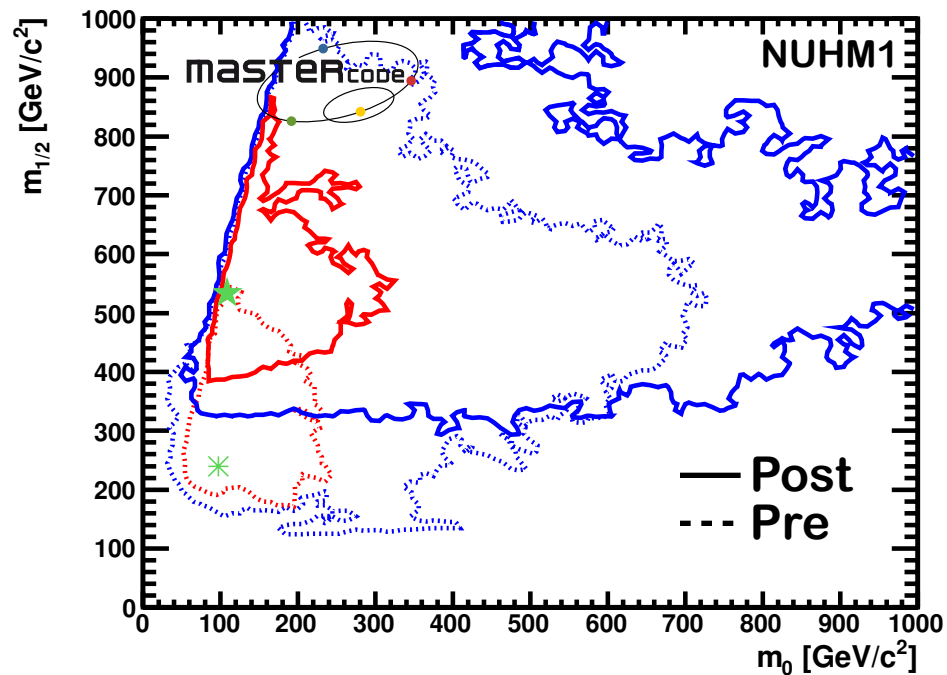
Post-LHC, Post-XENON100

2010 ATLAS + CMS with 36 pb⁻¹ of LHC Data



CMSSM

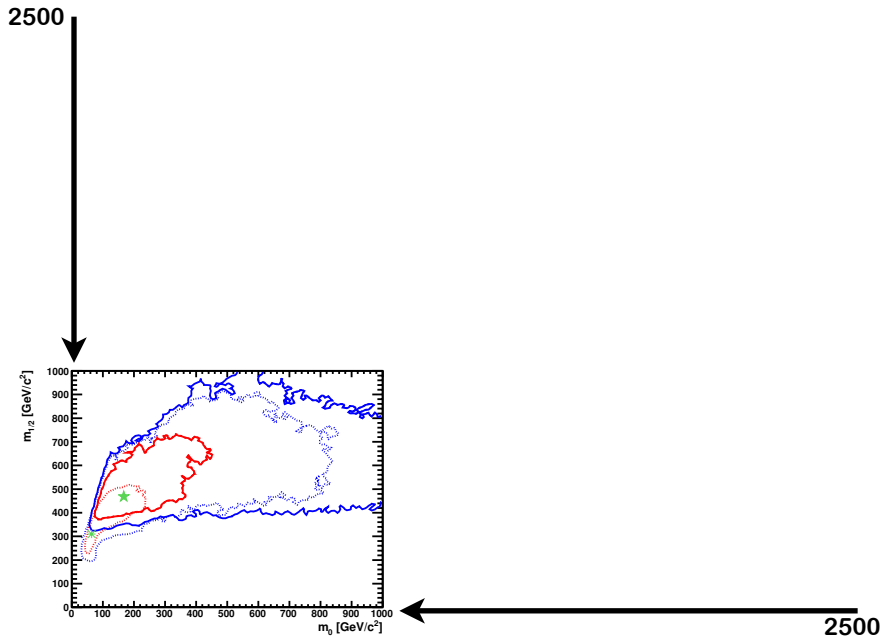
60 million points sampled



NUHM1

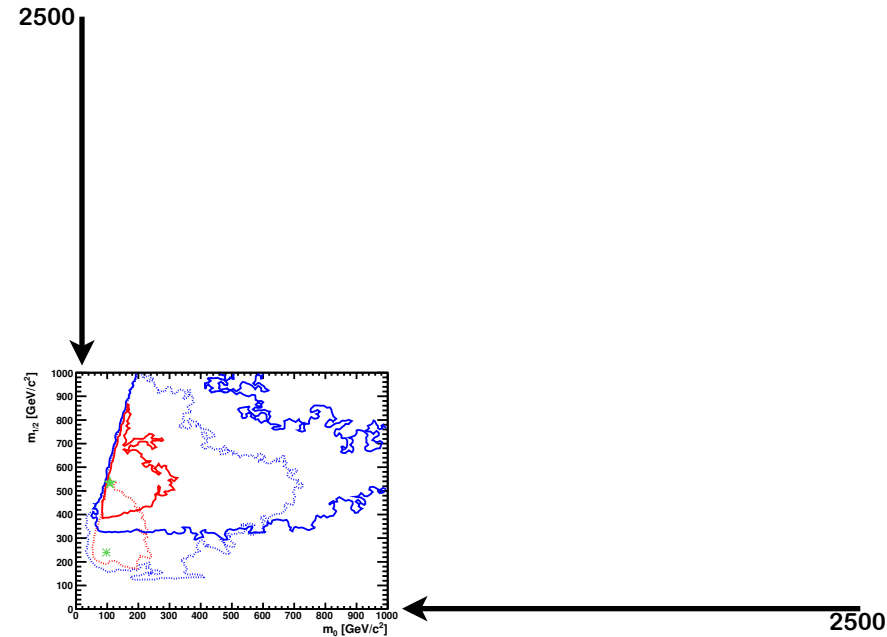
70 million points sampled

2010 ATLAS + CMS with 36 pb⁻¹ of LHC Data



CMSSM

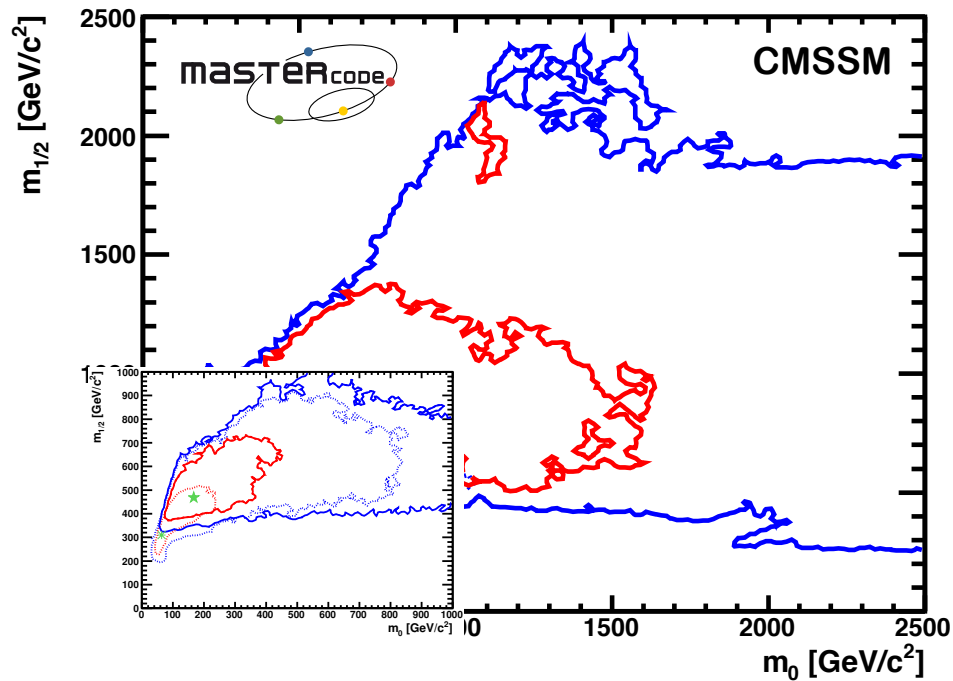
60 million points sampled



NUHM1

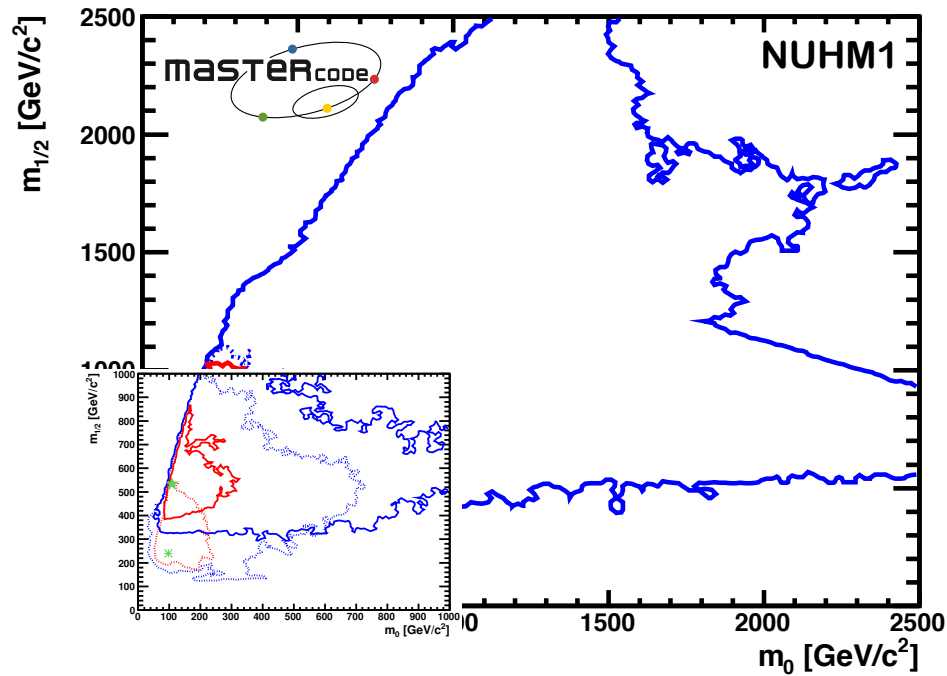
70 million points sampled

2011 ATLAS + CMS with 1 fb⁻¹ of LHC Data



CMSSM

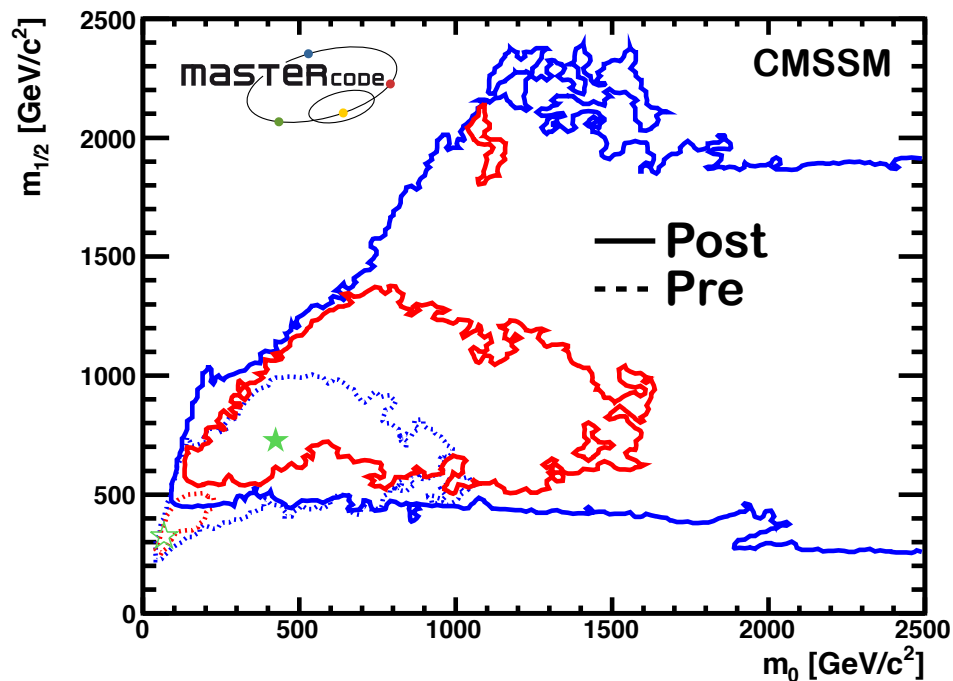
60 million points sampled



NUHM1

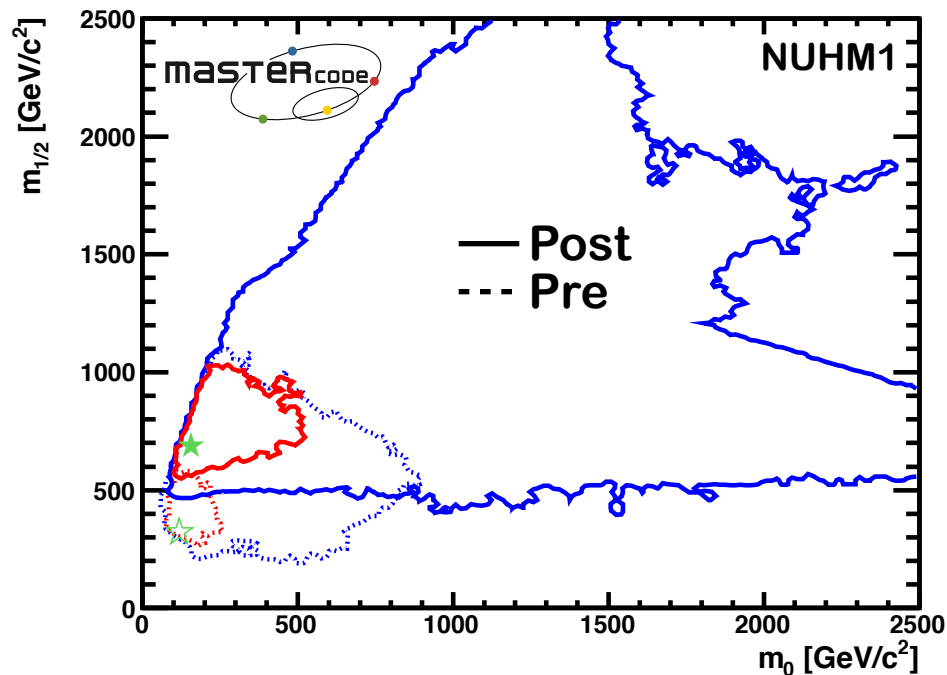
70 million points sampled

2011 ATLAS + CMS with 1 fb⁻¹ of LHC Data



CMSSM

60 million points sampled



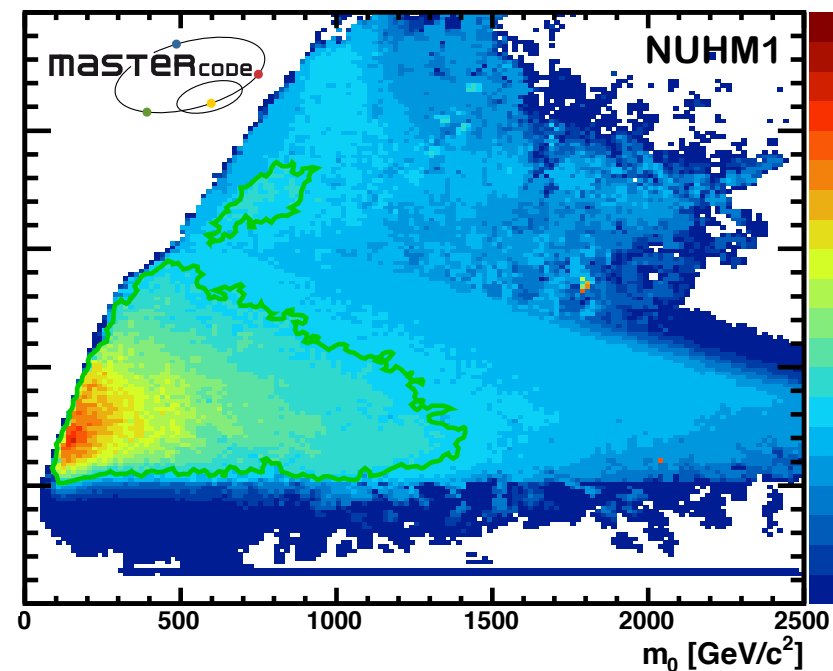
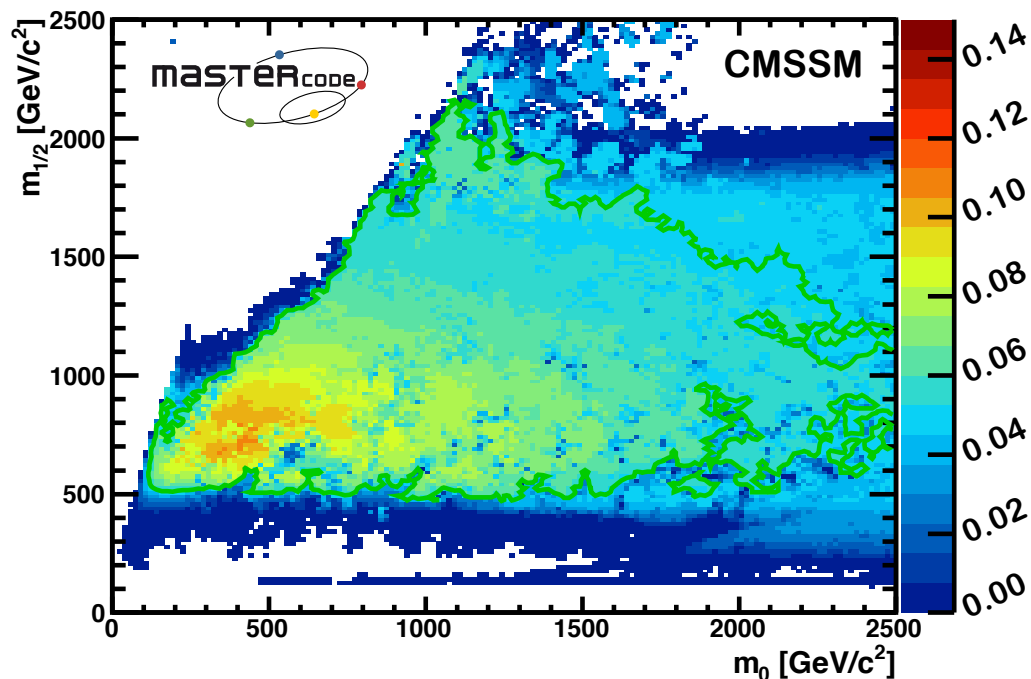
NUHM1

70 million points sampled

Red and blue curves represent $\Delta\chi^2$ from global minimum, located at ★

Preferred region “opens up” at cost of worsening global χ^2 value!

2011 ATLAS + CMS with 1 fb⁻¹ of LHC Data

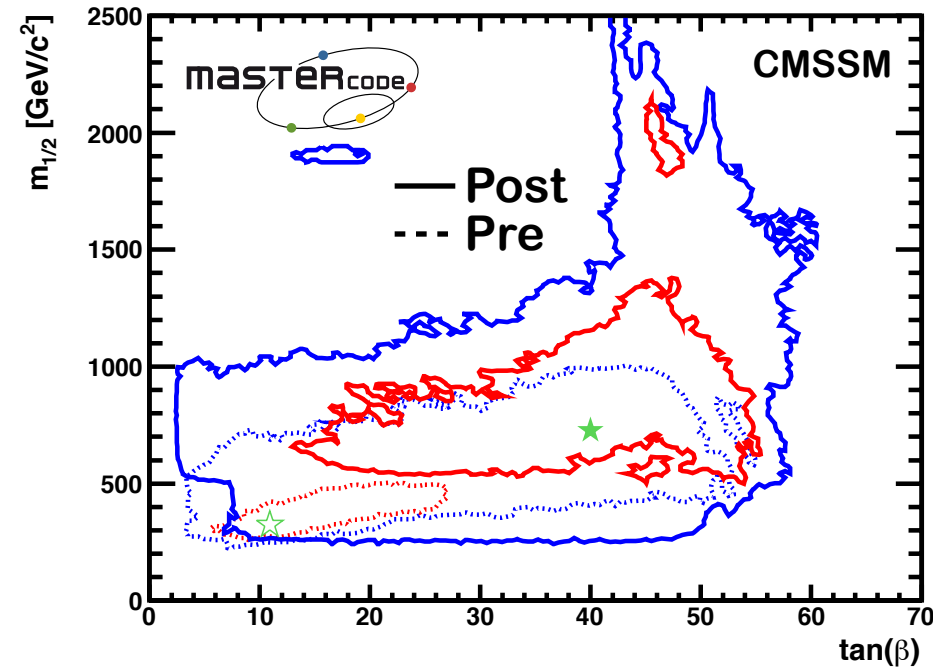


	Model	Min χ^2	Prob	$m_{1/2}$	m_0	A_0	$\tan \beta$
post-LHC/XENON100	CMSSM	22.5	26%	310	60	-60	10
	post-LHC/XENON100	29.3	11%	730	420	-1100	40
post-LHC/XENON100	NUHM1	20.5	25%	310	60	-60	10
	post-LHC/XENON100	27.3	13%	690	160	-880	33

With 1 fb⁻¹: CMSSM and NUHM1 still above 10% CL
 VCMSSM and mSUGRA now less than 5% CL

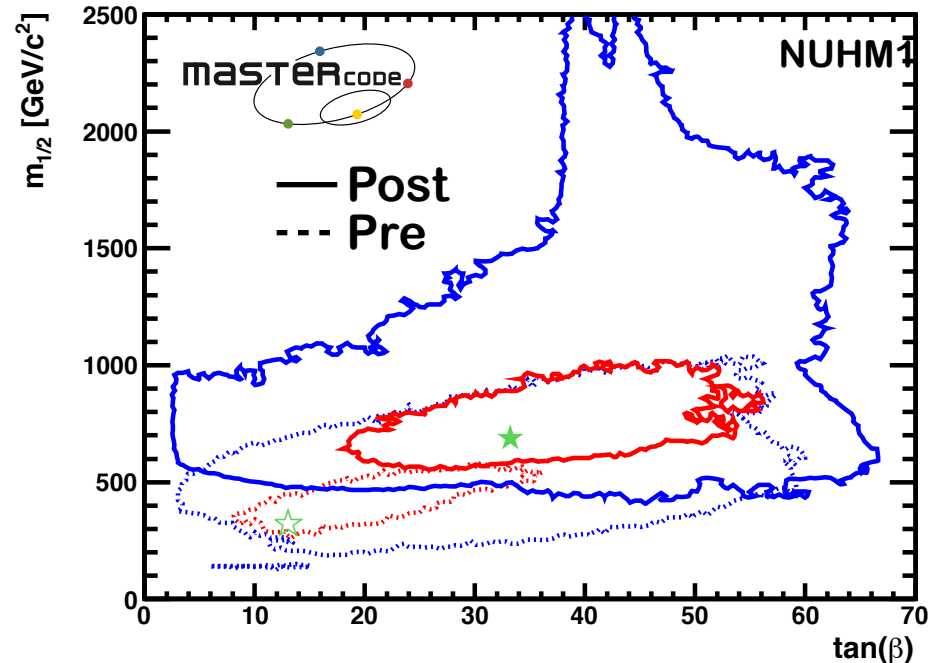
Post-LHC, Post-XENON100

2011 ATLAS + CMS with 1 fb^{-1} of LHC Data



CMSSM

60 million points sampled



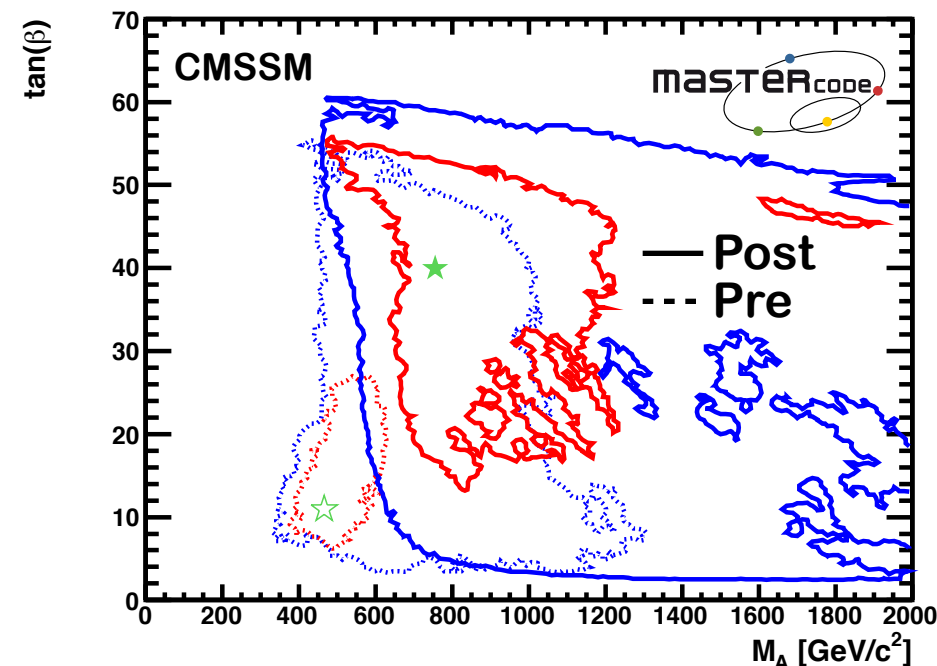
NUHM1

70 million points sampled

Red and blue curves represent $\Delta\chi^2$ from global minimum, located at ★

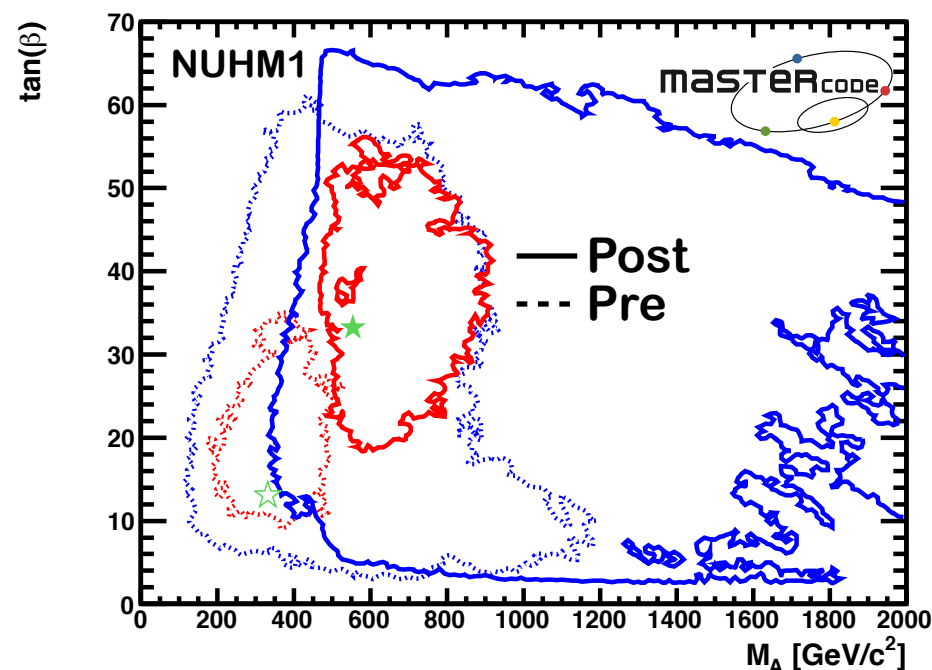
Preferred region “opens up” at cost of worsening global χ^2 value!

2011 ATLAS + CMS with 1 fb⁻¹ of LHC Data



CMSSM

60 million points sampled



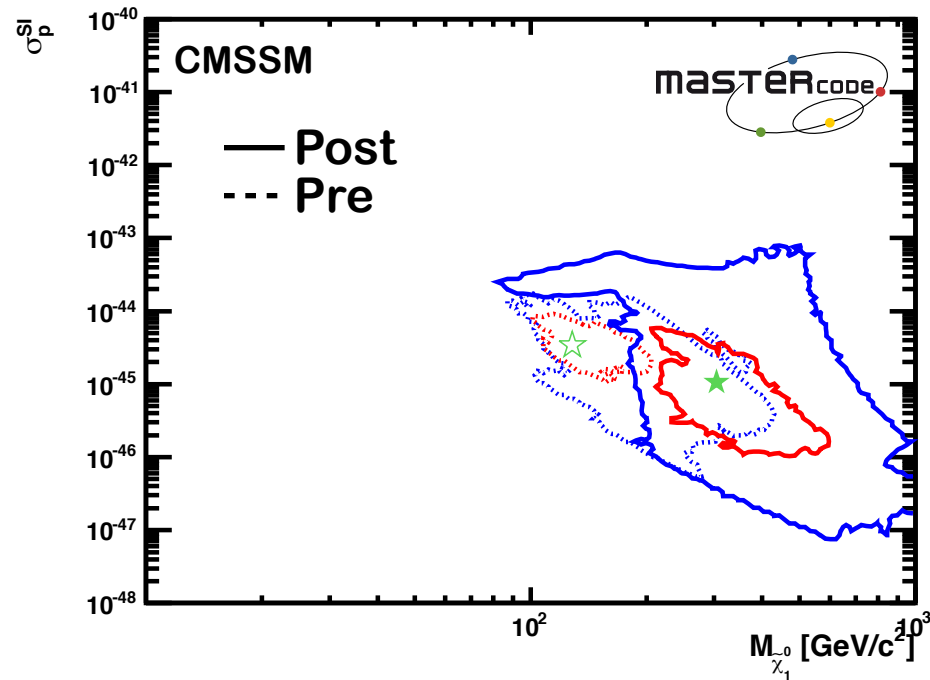
NUHM1

70 million points sampled

Red and blue curves represent $\Delta\chi^2$ from global minimum, located at ★

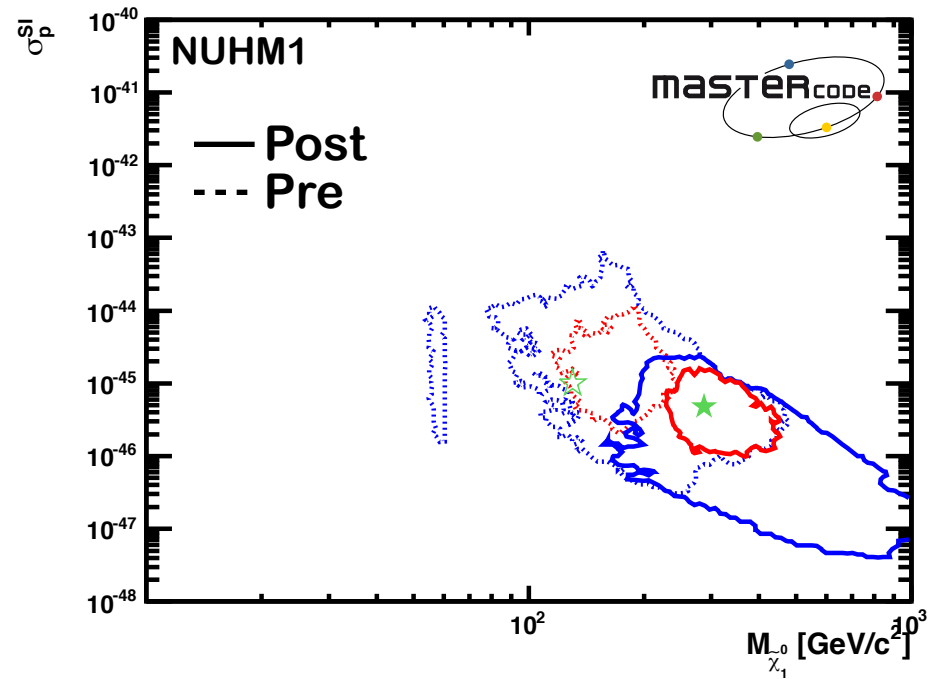
Preferred region “opens up” at cost of worsening global χ^2 value!

2011 ATLAS + CMS with 1 fb⁻¹ of LHC Data



CMSSM

60 million points sampled



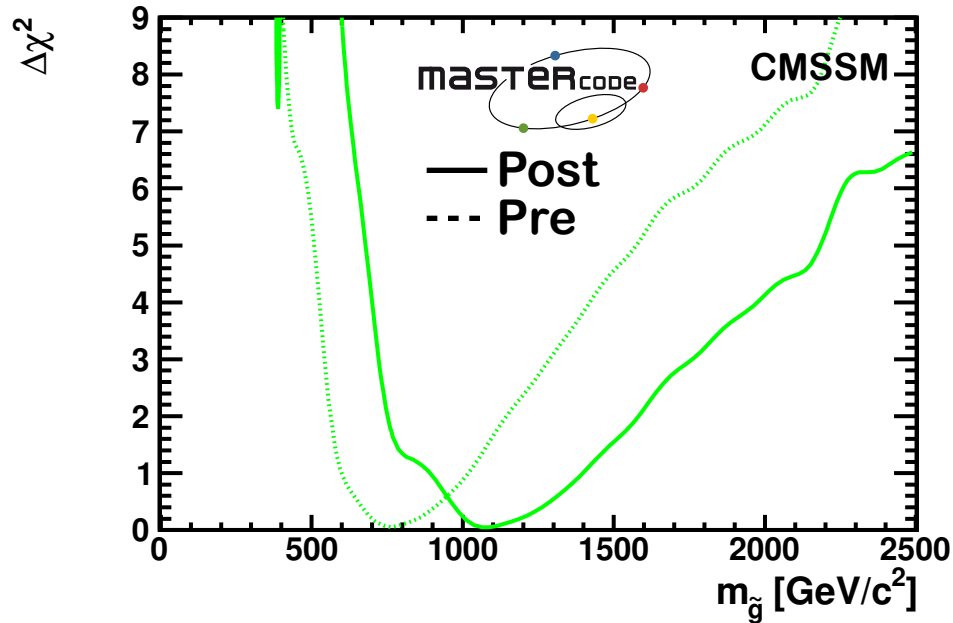
NUHM1

70 million points sampled

Red and blue curves represent $\Delta\chi^2$ from global minimum, located at ★

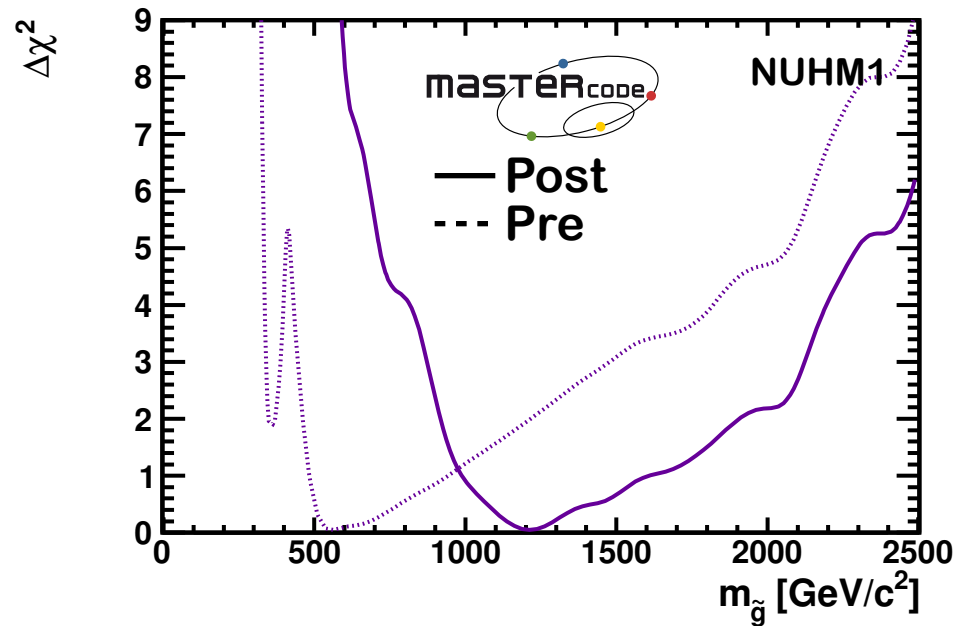
Preferred region “opens up” at cost of worsening global χ^2 value!

2010 ATLAS + CMS with 36 pb⁻¹ of LHC Data



CMSSM Prediction:

$$m_{\tilde{g}} = 1080^{+320}_{-100} \text{ GeV}$$

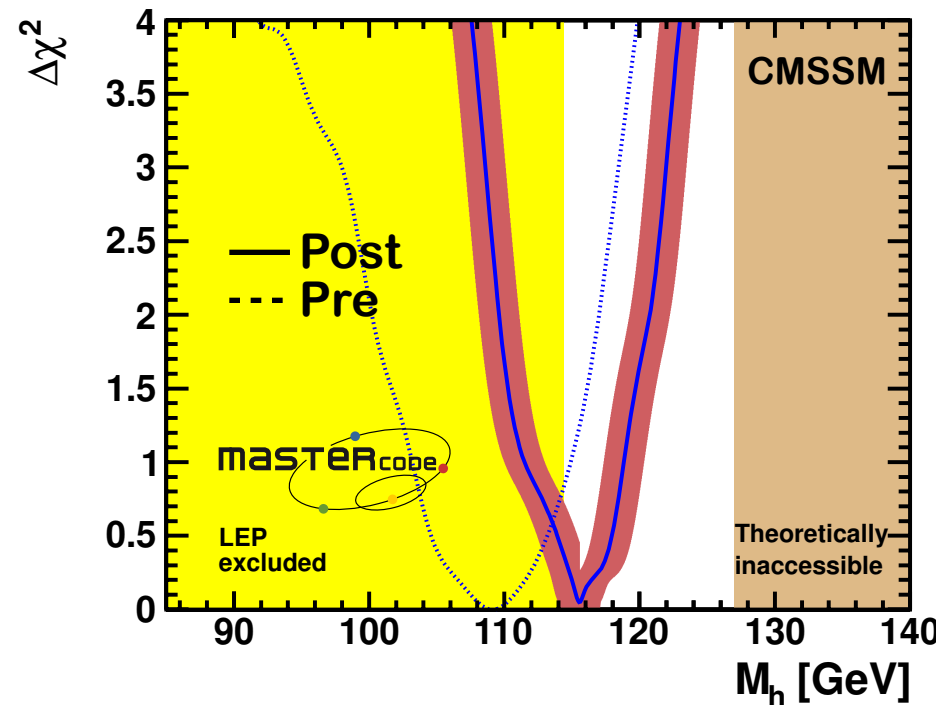


NUHM1 Prediction:

$$m_{\tilde{g}} = 1200^{+400}_{-200} \text{ GeV}$$

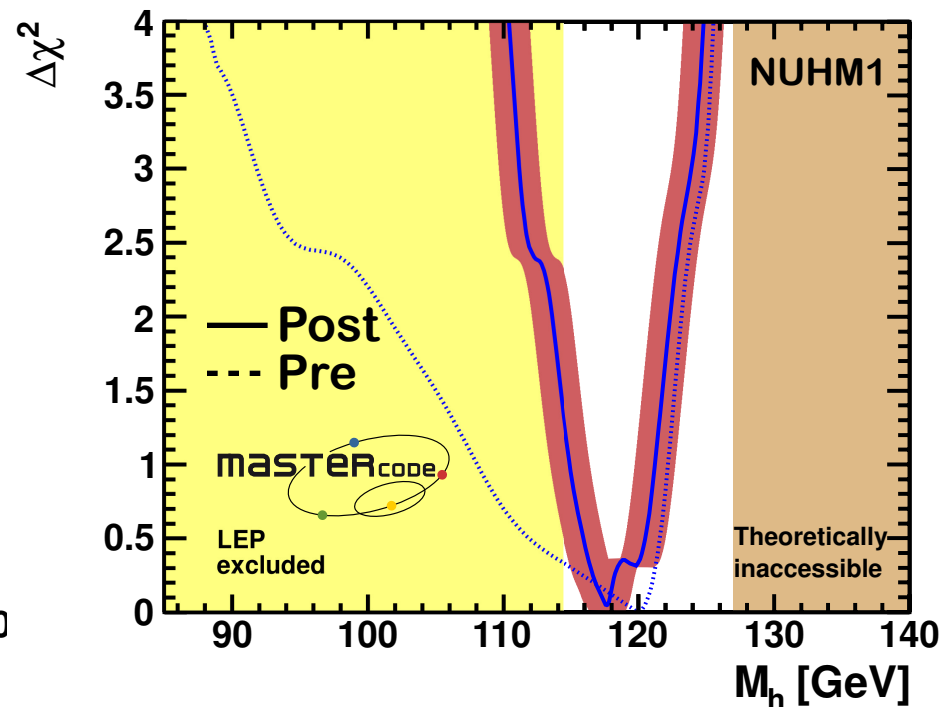
Post-LHC, Post-XENON100

2010 ATLAS + CMS with 36 pb^{-1} of LHC Data



CMSSM Prediction:

$$m_H = 116_{-6}^{+4} \text{ GeV}$$



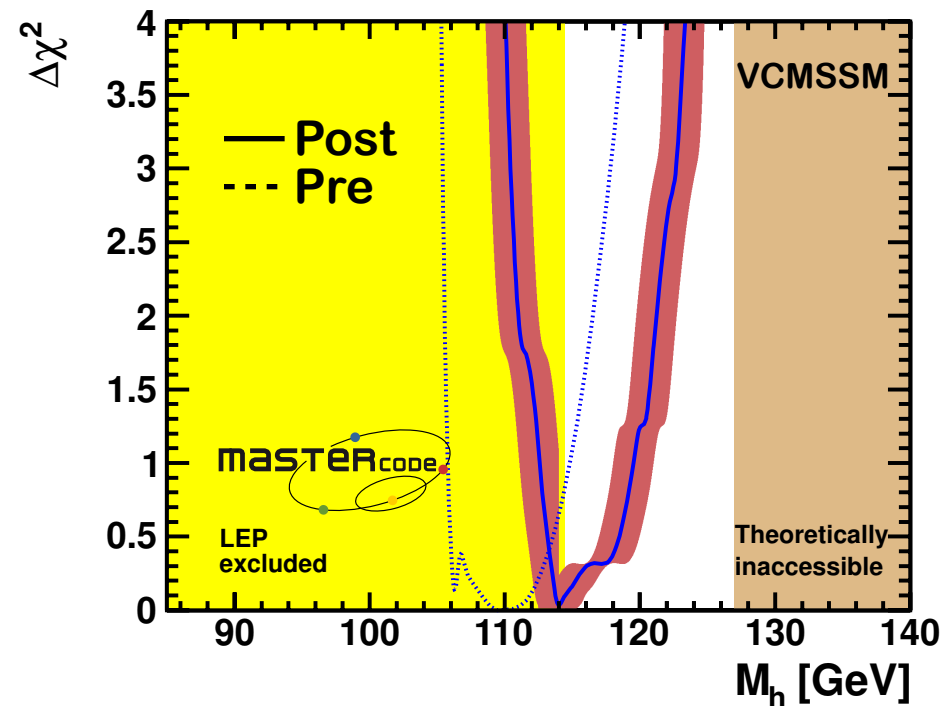
NUHM1 Prediction:

$$m_H = 118_{-4}^{+4} \text{ GeV}$$

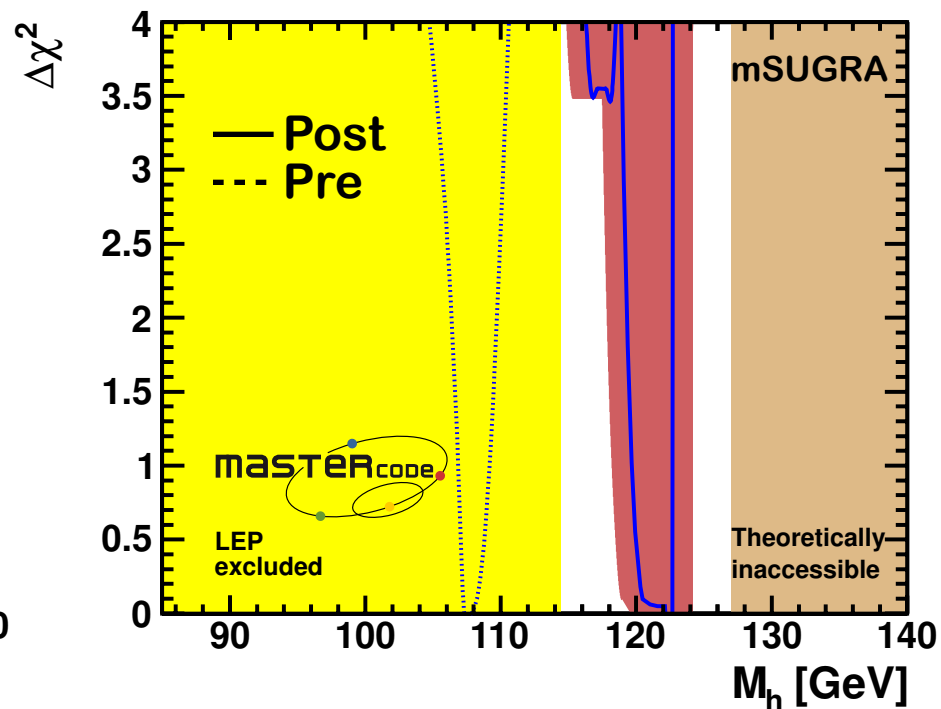
SM Prediction: $m_H = 92_{-26}^{+34} \text{ GeV}$

- **mSUGRA, VCMSSM**
 - With 1fb^{-1} , essentially excluded at 95% CL
- **CMSSM, NUHM1**
 - With 36pb^{-1} ,
 - gluino masses already preferred above TeV level
 - With 1fb^{-1} , still alive at the 10% level:
 - Tension between post-LHC reality high ($m_0, m_{1/2}$) and pre-LHC preferred low ($m_0, m_{1/2}$)
 - Tension partly compensated by higher $\tan\beta$
 - Lower preferred σ_p^{SI} and higher LSP mass
 - Lightest Higgs mass now preferred above LEP limit

2010 ATLAS + CMS with 36 pb^{-1} of LHC Data



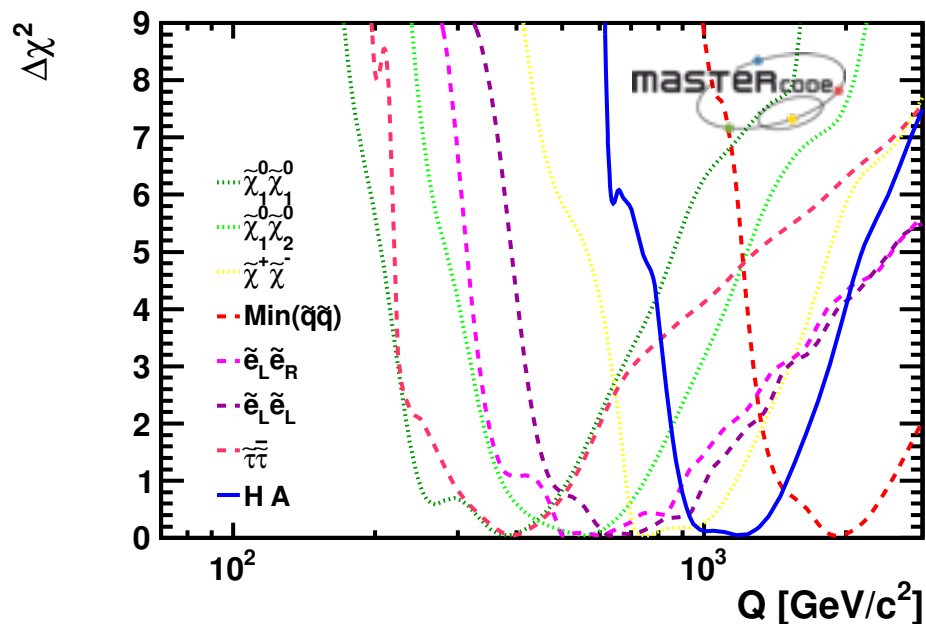
VCMSSM



mSUGRA

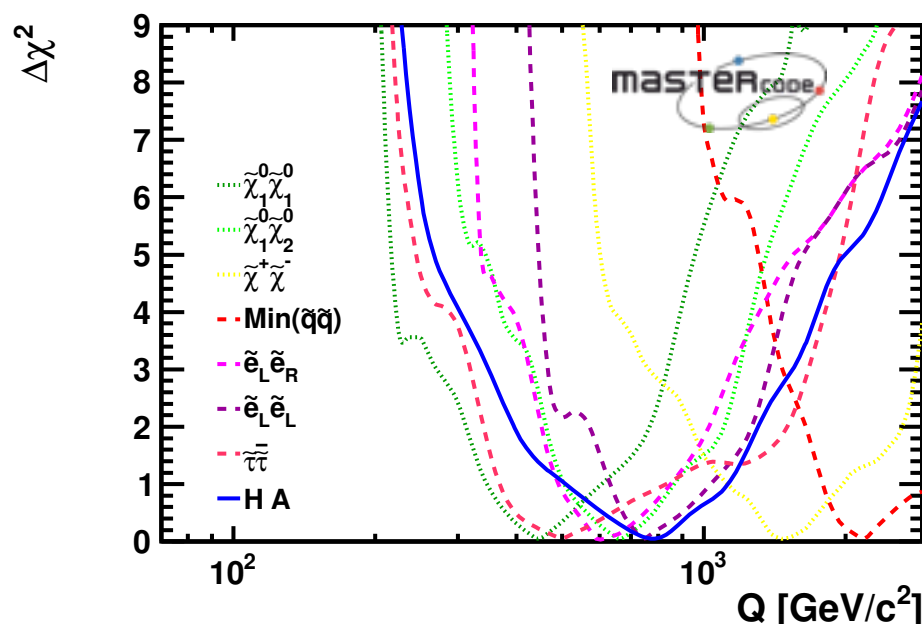
SM Prediction: $m_H = 92^{+34}_{-26} \text{ GeV}$

2010 ATLAS + CMS with 36 pb⁻¹ of LHC Data



CMSSM

60 million points sampled



NUHM1

70 million points sampled