



Precision Measurement of the W Boson Mass at CDF

Bodhitha Jayatilaka
Duke University

45th Annual Fermilab Users Meeting
Tollestrup Award Presentation

June 13, 2012

Duke
UNIVERSITY

Introduction: a testament to insanity

Introduction: a testament to insanity



“A low mass bison at Fermilab”
*-**The Guardian** (J. Butterworth)*
from “W Marks the Spot” (2-Mar-2012)

Introduction: a testament to insanity

- This measurement did take nearly five years



*“A low mass bison at Fermilab”
-**The Guardian** (J. Butterworth)
from “W Marks the Spot” (2-Mar-2012)*

Introduction: a testament to insanity

- This measurement did take nearly five years
- A true end-to-end analysis
 - Detailed understanding of theoretical model, detector response, and experimental environment
 - Bespoke tools
 - Convincing collaborators to read 400+ pages of documentation



*“A low mass bison at Fermilab”
-**The Guardian** (J. Butterworth)
from “W Marks the Spot” (2-Mar-2012)*

Introduction: a testament to insanity

- This measurement did take nearly five years
- A true end-to-end analysis
 - Detailed understanding of theoretical model, detector response, and experimental environment
 - Bespoke tools
 - Convincing collaborators to read 400+ pages of documentation
- End result: **single most precise** measurement of the W boson mass



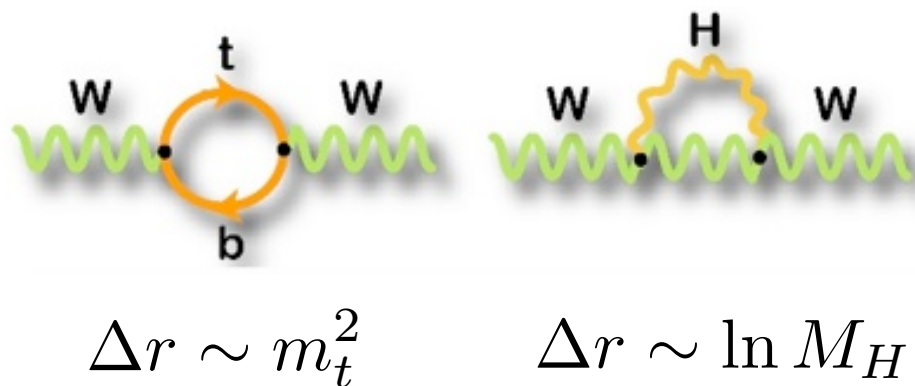
*“A low mass bison at Fermilab”
-**The Guardian** (J. Butterworth)
from “W Marks the Spot” (2-Mar-2012)*

The electroweak sector and M_W

$$M_W^2 \left(1 - \frac{M_W^2}{M_Z^2} \right) = \frac{\pi \alpha_{EM}}{\sqrt{2} G_F} \frac{1}{(1 - \Delta r)}$$

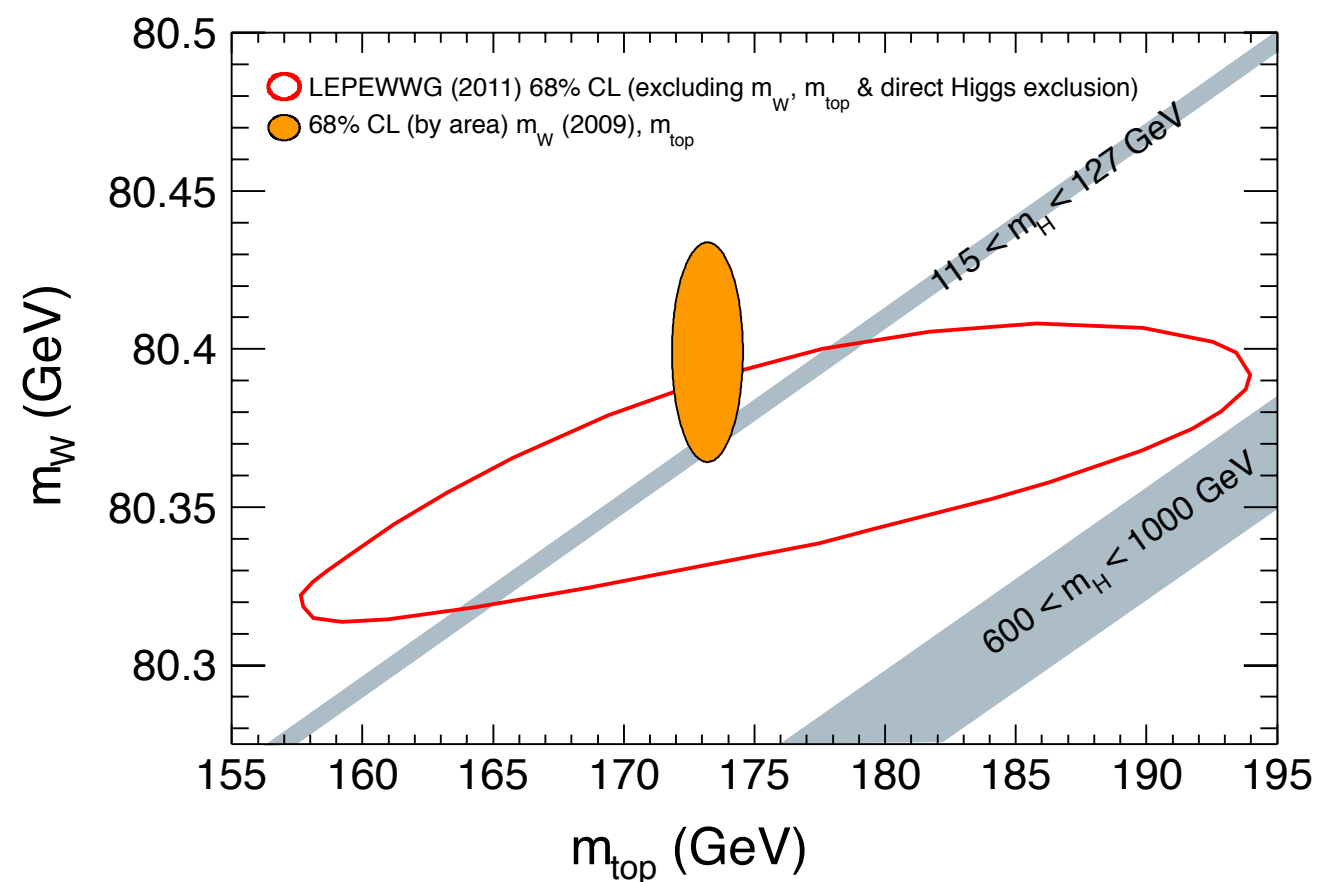
$G_F = 1.16637(1) \times 10^{-5} \text{ GeV}^{-2}$
 $\alpha_{EM}(Q^2 = M_Z^2) = 1/127.918(18)$
 $M_Z = 91.1876(21) \text{ GeV}/c^2$

- Radiative corrections Δr dominated by top and Higgs loops



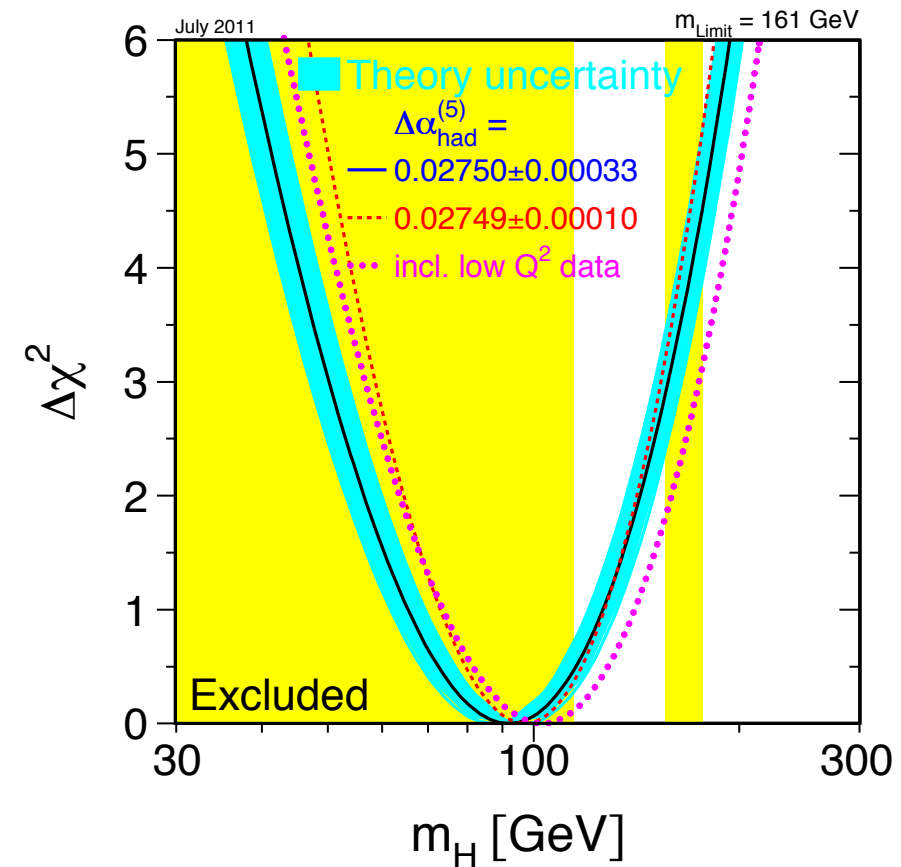
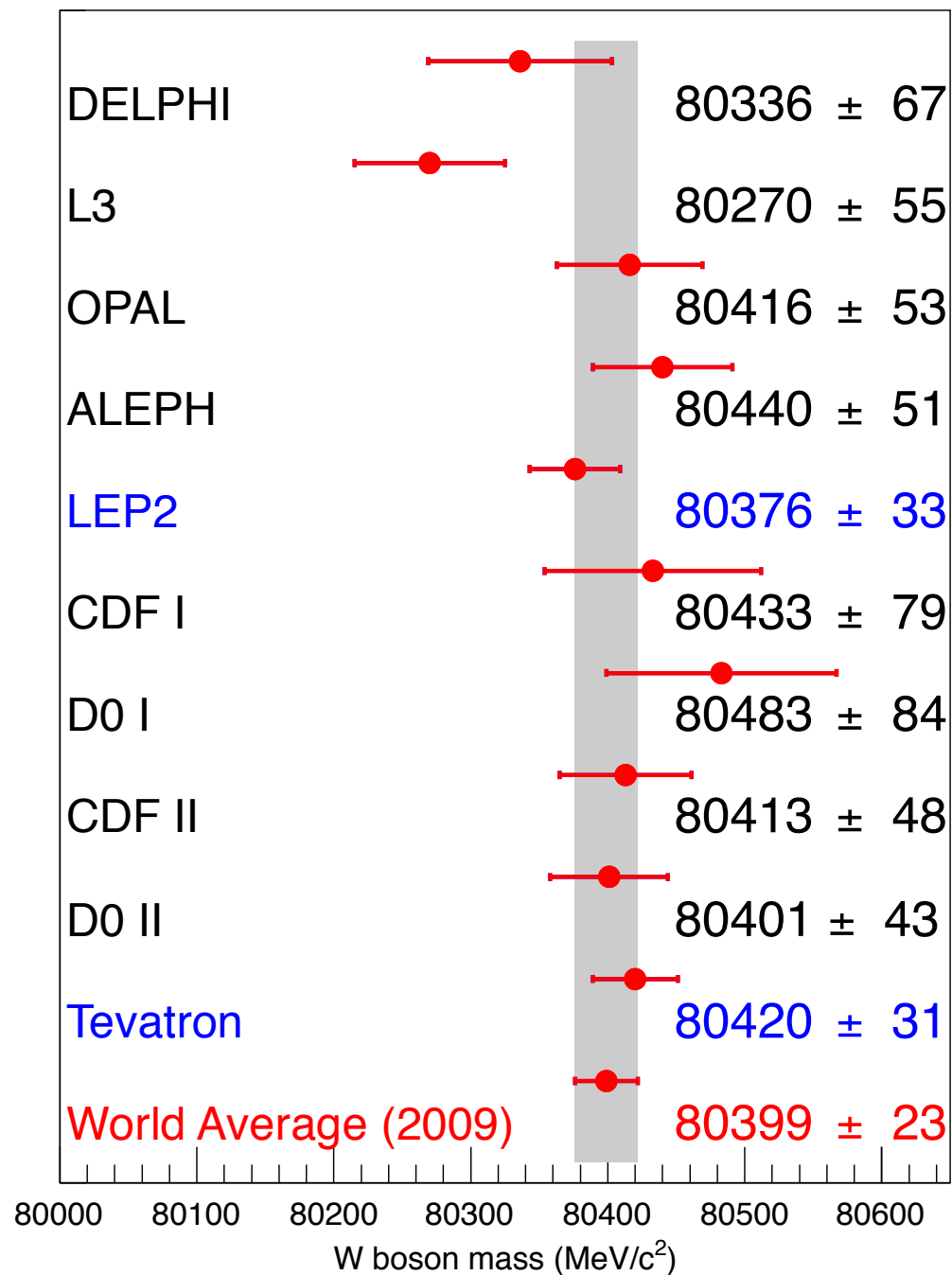
- Precision measurements in M_W and m_t constrain SM Higgs mass

Where should the Higgs be?



M_W history and Higgs mass constraint

As of January 2012

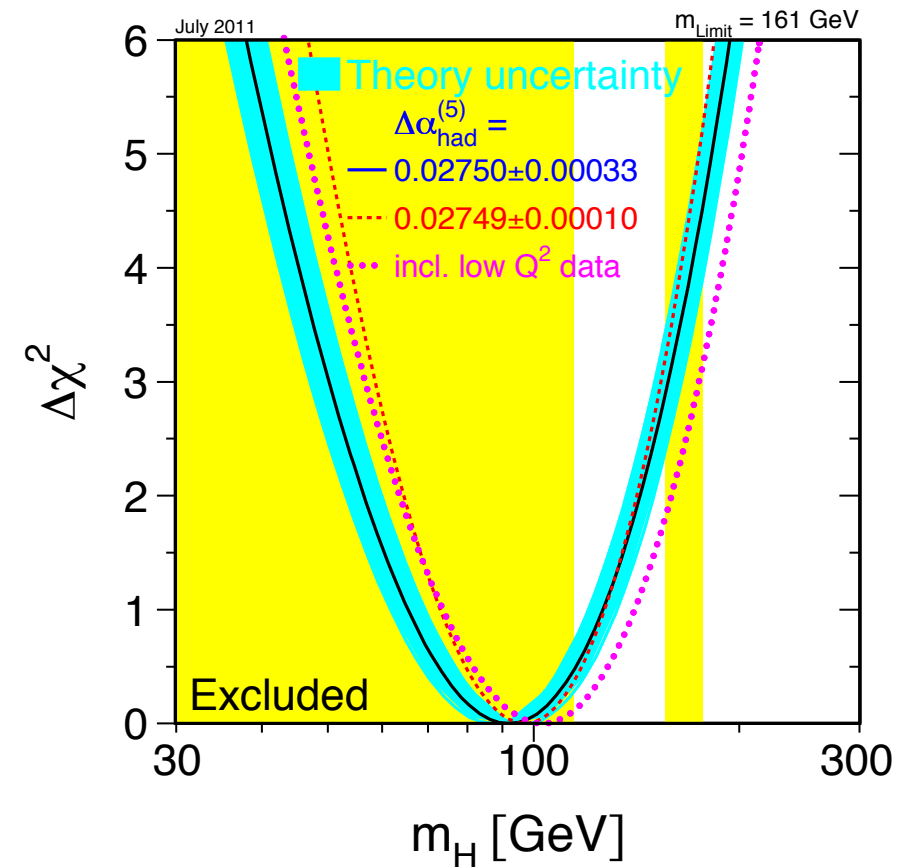
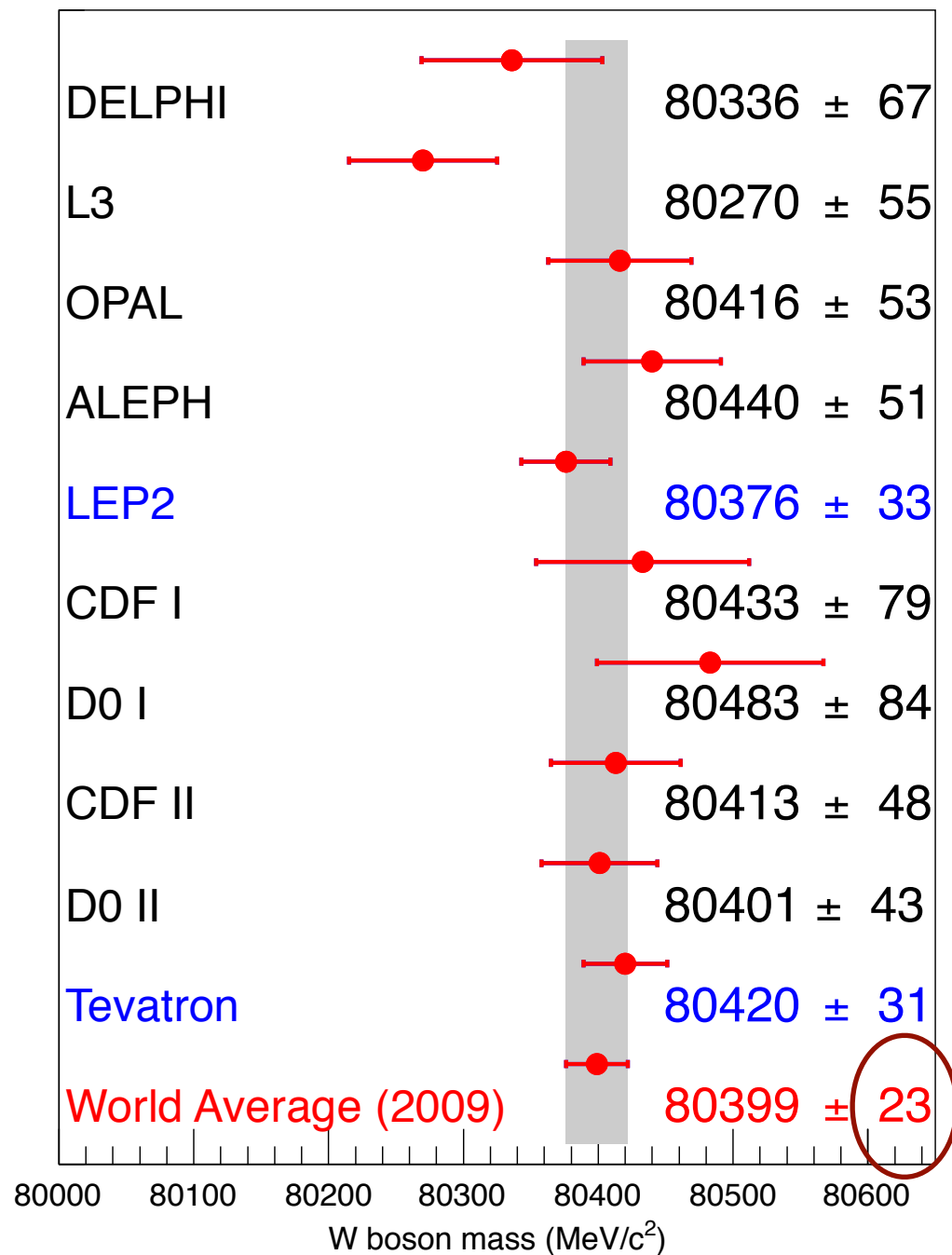


$m_t = 173.2 \pm 0.9$ GeV
 $M_W = 80.399 \pm 0.023$ GeV
 $m_H = 92^{+34}_{-26}$ GeV
 $m_H < 161$ GeV @95% CL

Δm_t of 0.9 GeV
 equivalent to
 ΔM_W of 6 MeV

M_W history and Higgs mass constraint

As of January 2012



$m_t = 173.2 \pm 0.9$ GeV
 $M_W = 80.399 \pm 0.023$ GeV
 $m_H = 92^{+34}_{-26}$ GeV
 $m_H < 161$ GeV @95% CL

Δm_t of 0.9 GeV
 equivalent to
 ΔM_W of 6 MeV

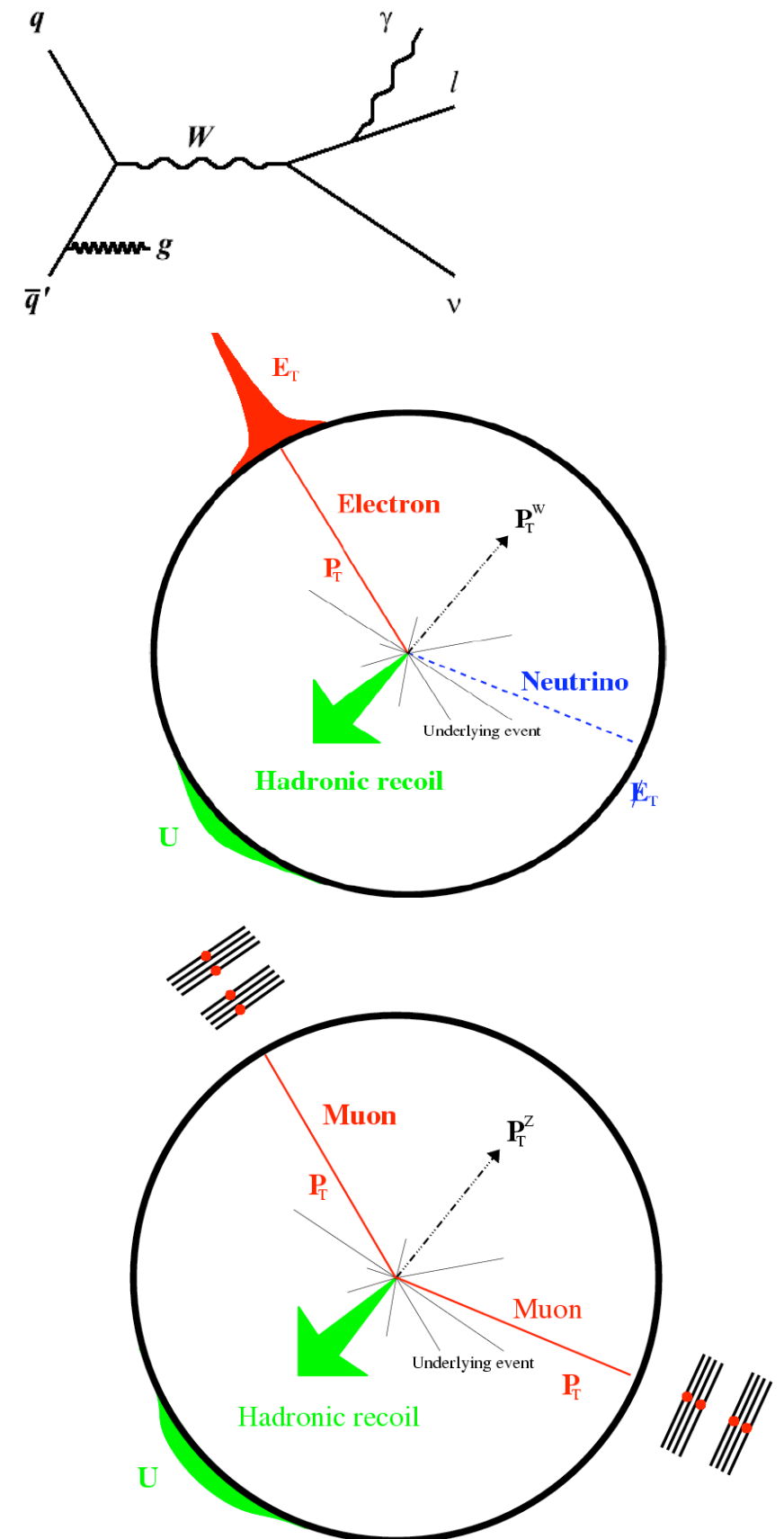
Can we exceed this precision with a single measurement?

Measuring M_W

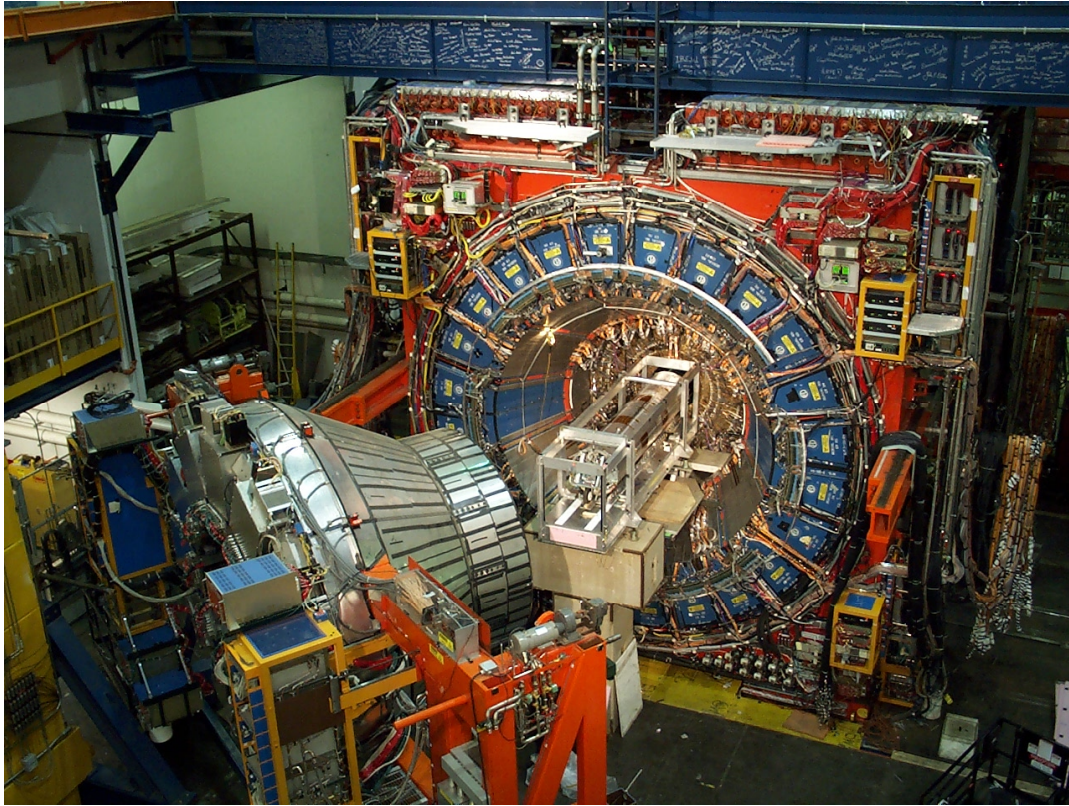
- Use electron and muon decays of W bosons
- **Lepton** p_T^l carries most information: measure as precisely as possible (e.g. 0.01% at CDF)
 - Calibrate using dimuon resonances
- Measure transverse **hadronic recoil**
 - Sum of all transverse energy minus lepton
 - Calibrate using Z boson events
- Infer **neutrino energy** $p_T^\nu = -(p_T^l + u_T)$
 - Perform mass fits using transverse quantities (p_T^l , p_T^ν , and m_T)

$$m_T = \sqrt{2p_T^\ell p_T^\nu (1 - \cos \Delta\theta_{\ell\nu})}$$

- Build parameterized (tunable) detector model
 - Accurate production model (incl. QED rad. corr.)
 - Calibrate tunable parameters using data (e.g. J/ψ , Z)



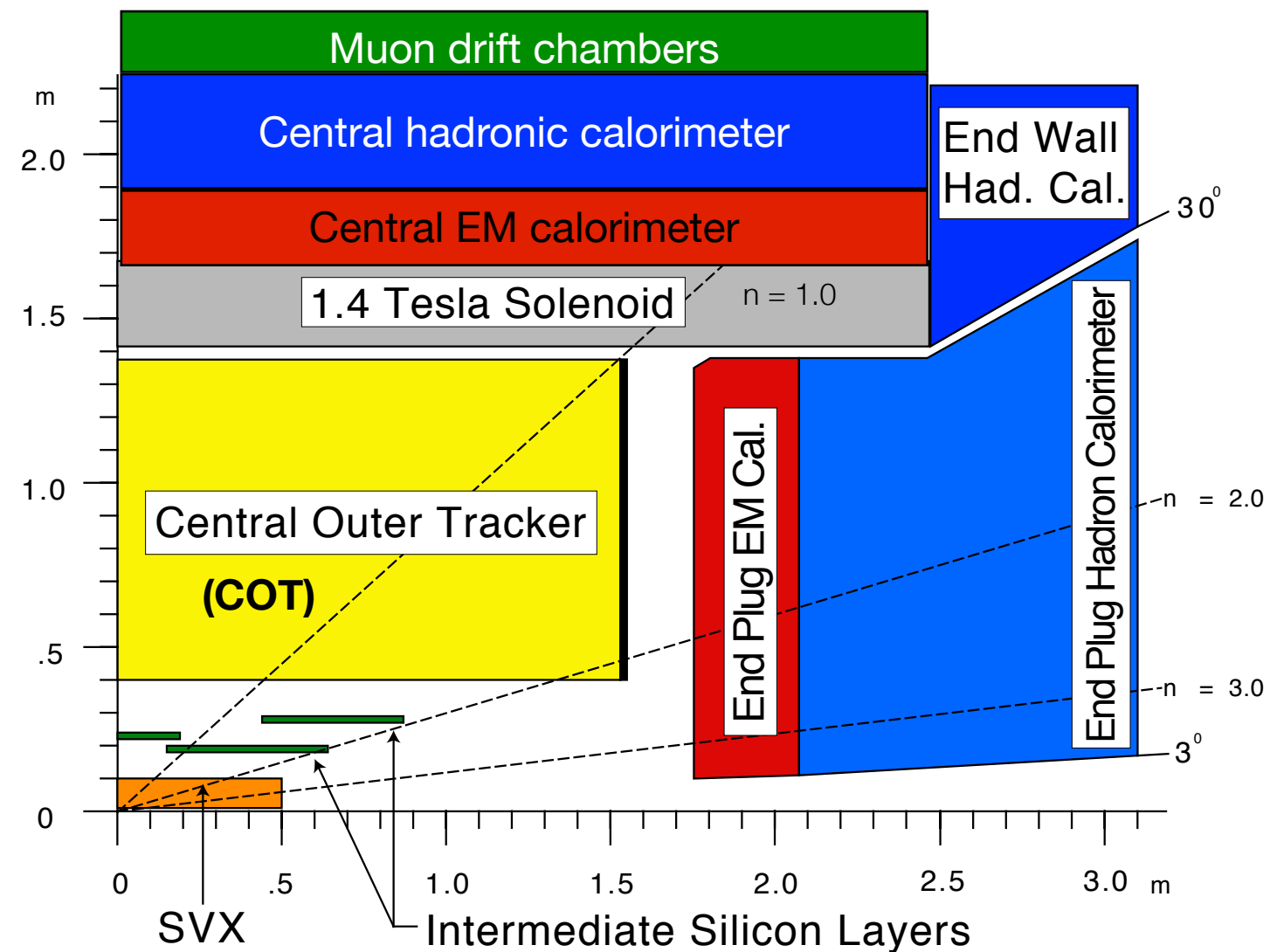
CDF II (2001-2011)



Analysis dataset: **2.2 fb^{-1}**

Candidate events:

W : 470,126 (e); 624,708 (μ)



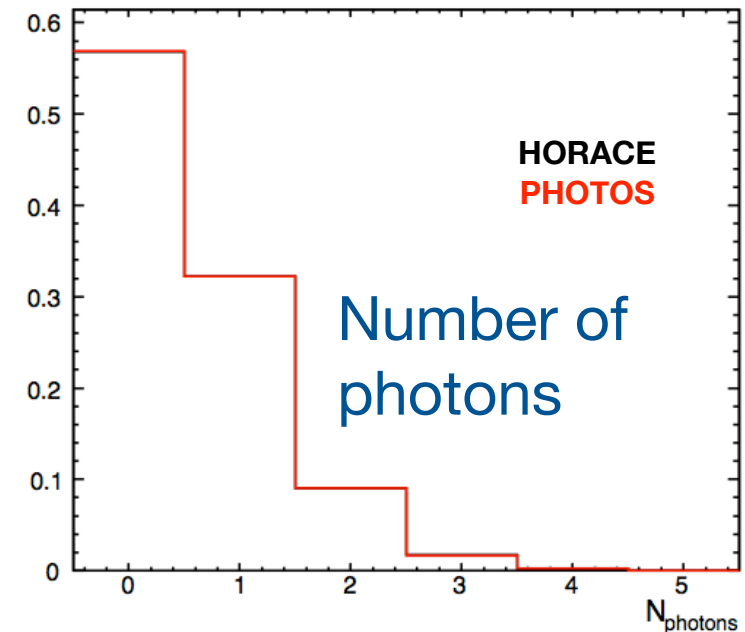
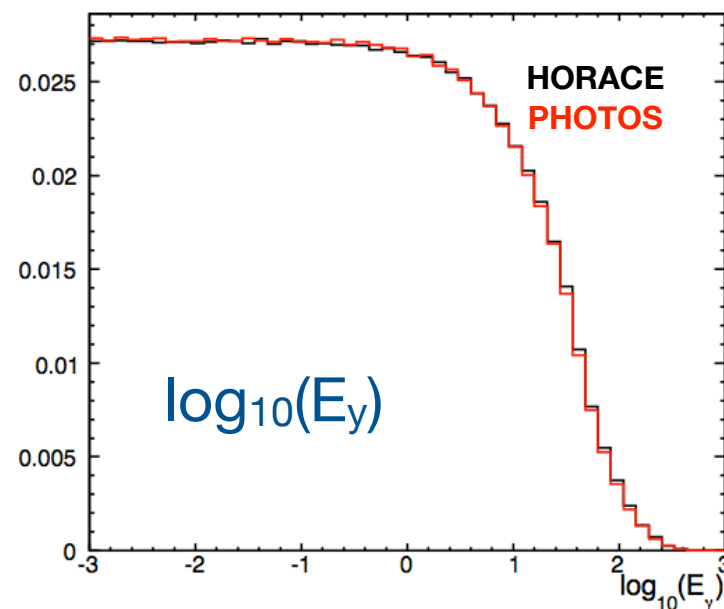
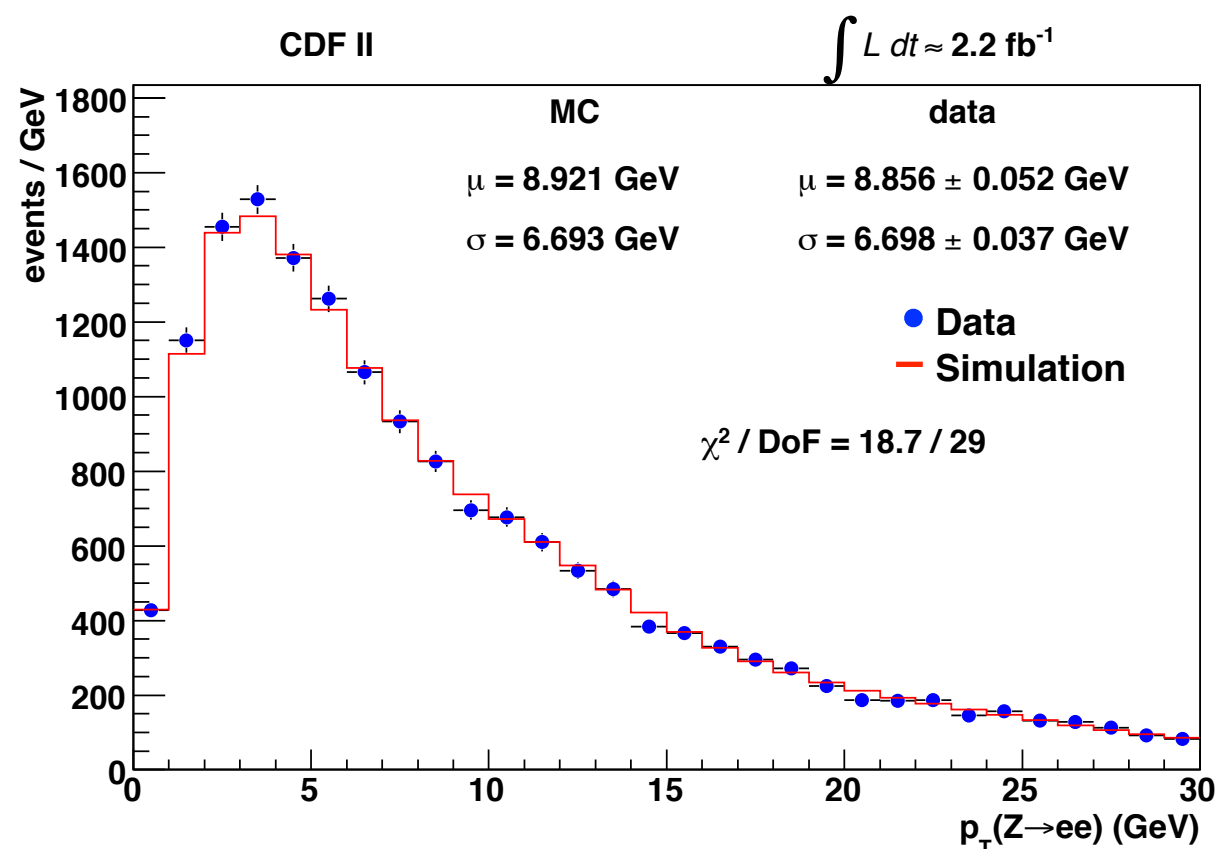
Theoretical model

Boson p_T

- Calculate at NNLO using RESBOS
- Non-perturbative QCD controlled by tunable parameters
 - Fit parameters with measured Z boson p_T spectrum
- Uncertainty results in $\Delta M_W = 5 \text{ MeV}$

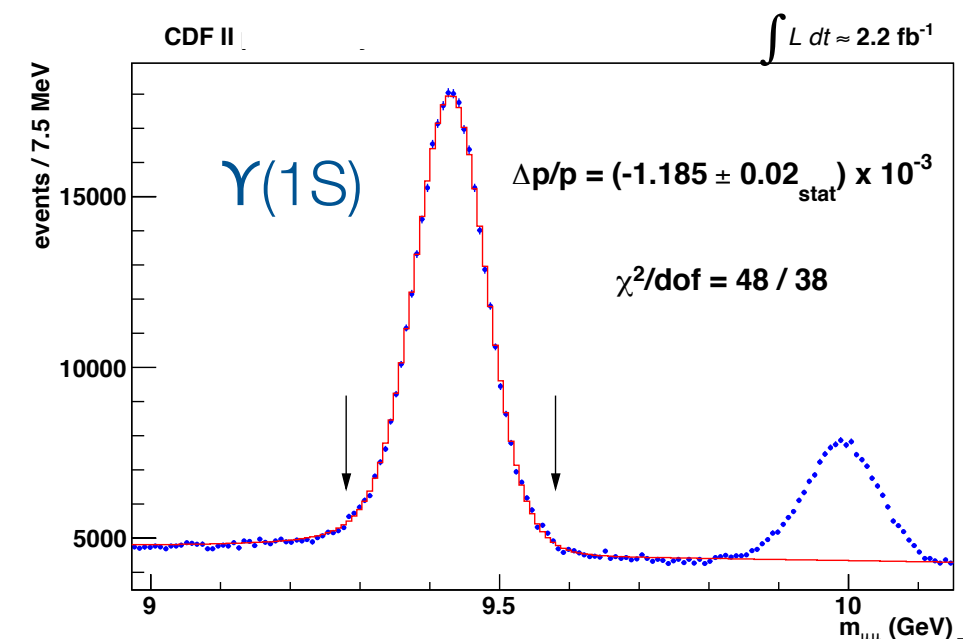
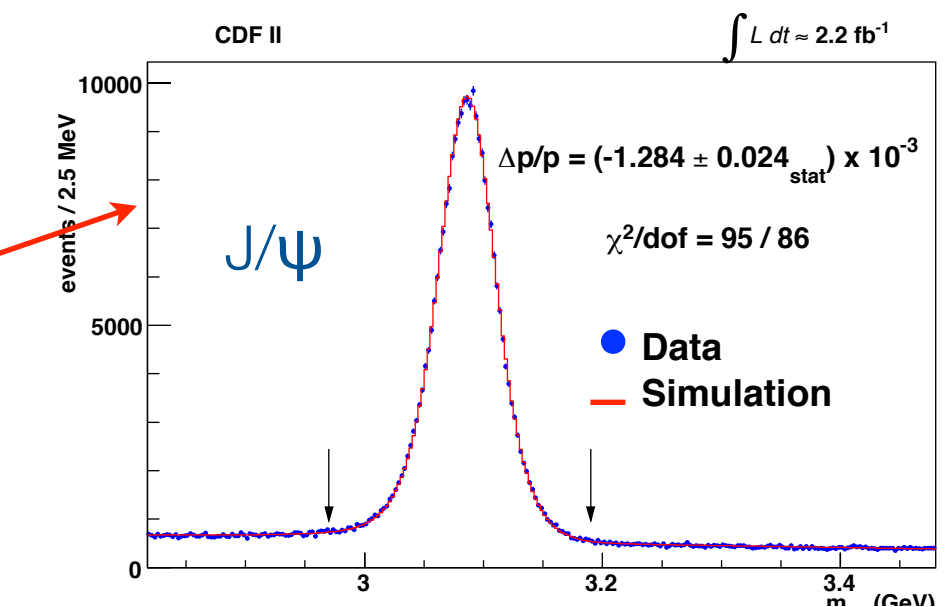
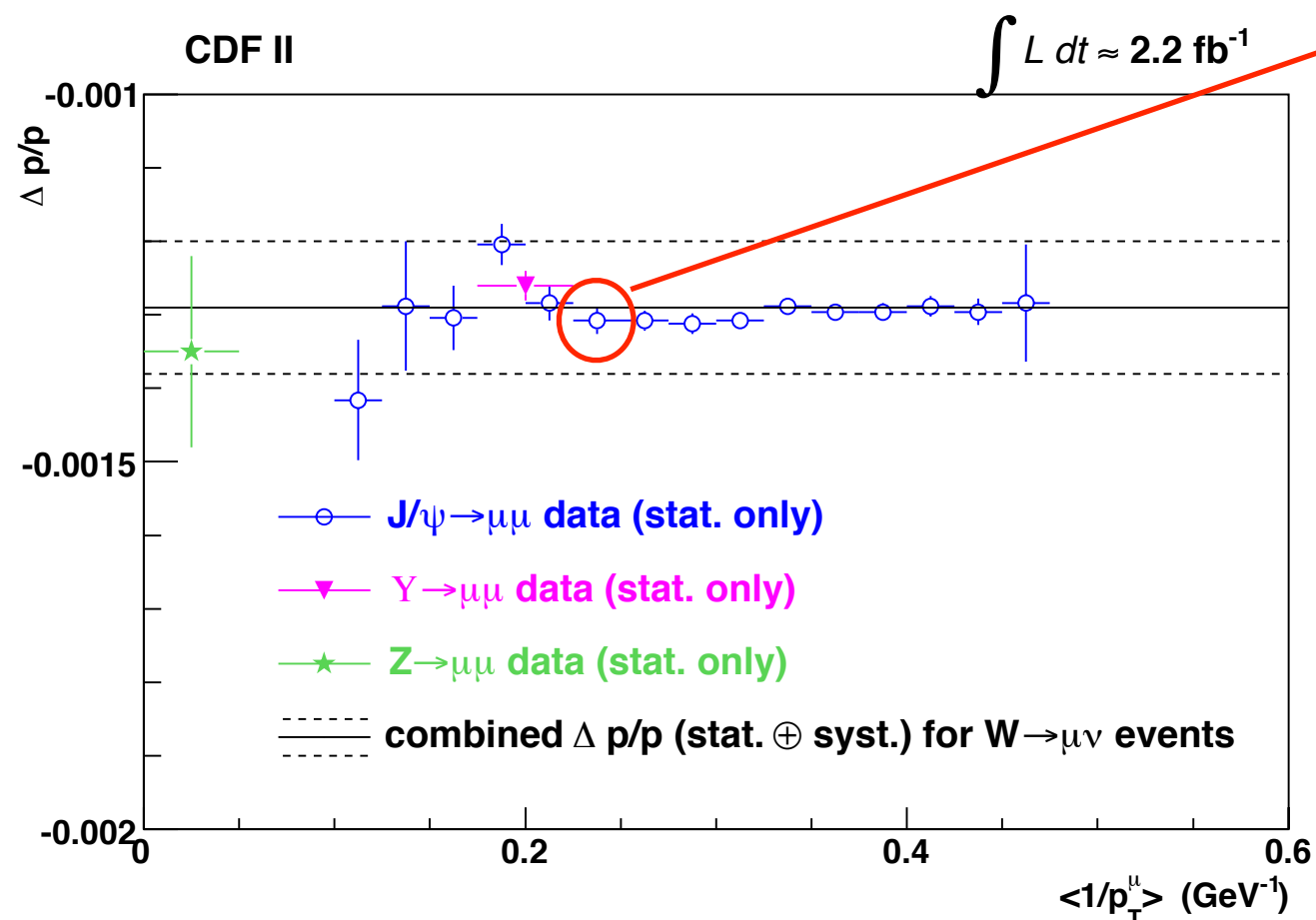
QED radiation

- Simulate LL FSR photons using PHOTOS
- Cross-check against HORACE
 - Study ISR/FSR, pair creation, etc.
- Uncertainty results in $\Delta M_W = 4 \text{ MeV}$



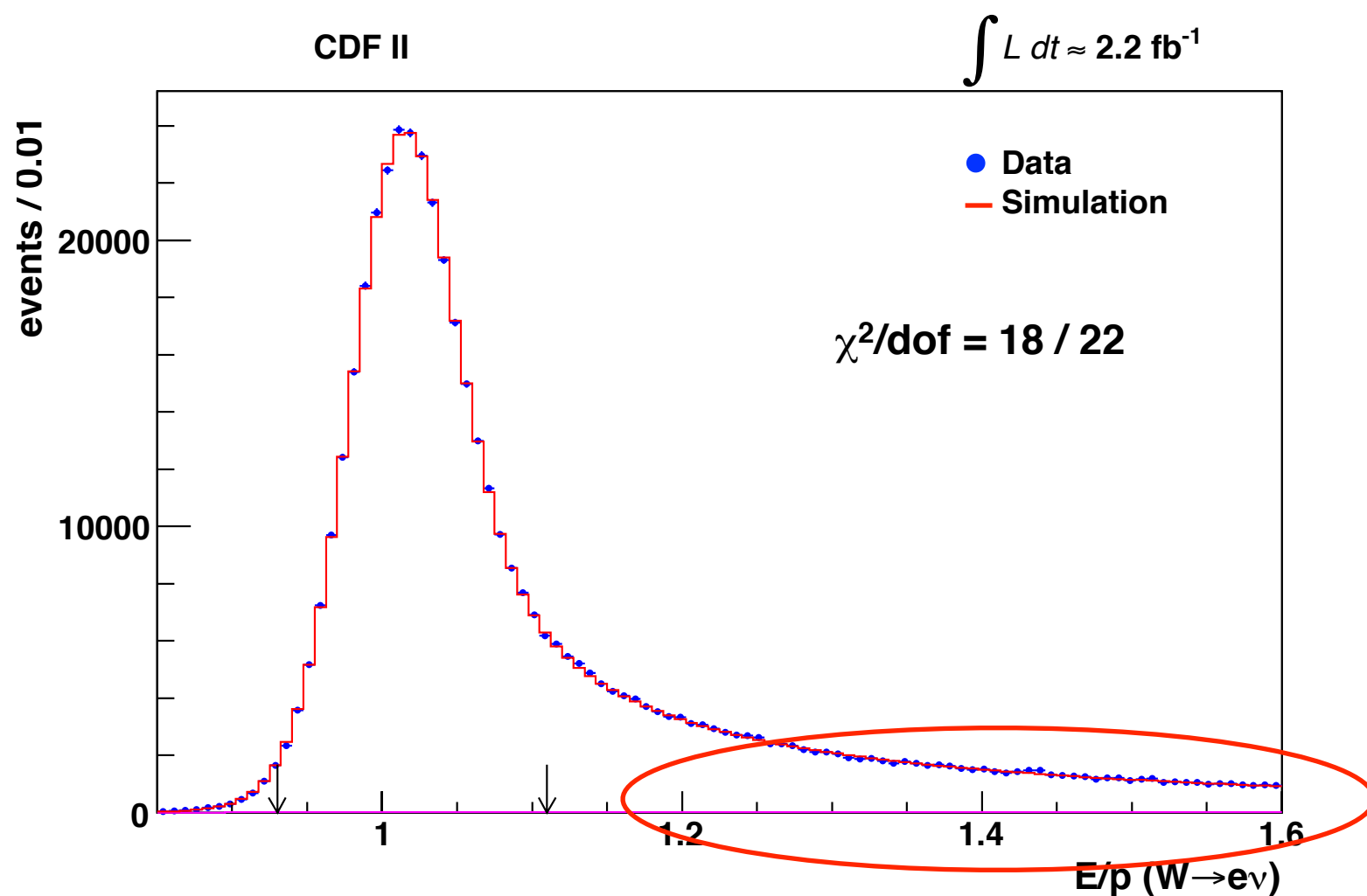
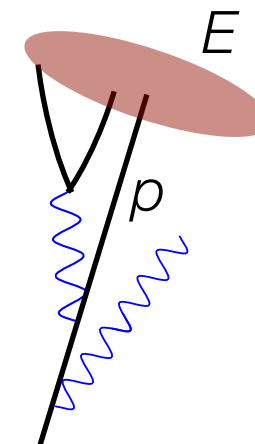
Track momentum scale

- Foundation of analysis is track p_T measurement with the COT
- Perform alignment using cosmic ray data: $\sim 50\mu\text{m} \rightarrow \sim 5\mu\text{m}$ residual
- Calibrate scale using large sample of dimuon resonances (J/ψ , Υ)
 - Span a large range of p_T
 - Flatness is a test of dE/dx modeling
 - Final scale error of 9×10^{-5}

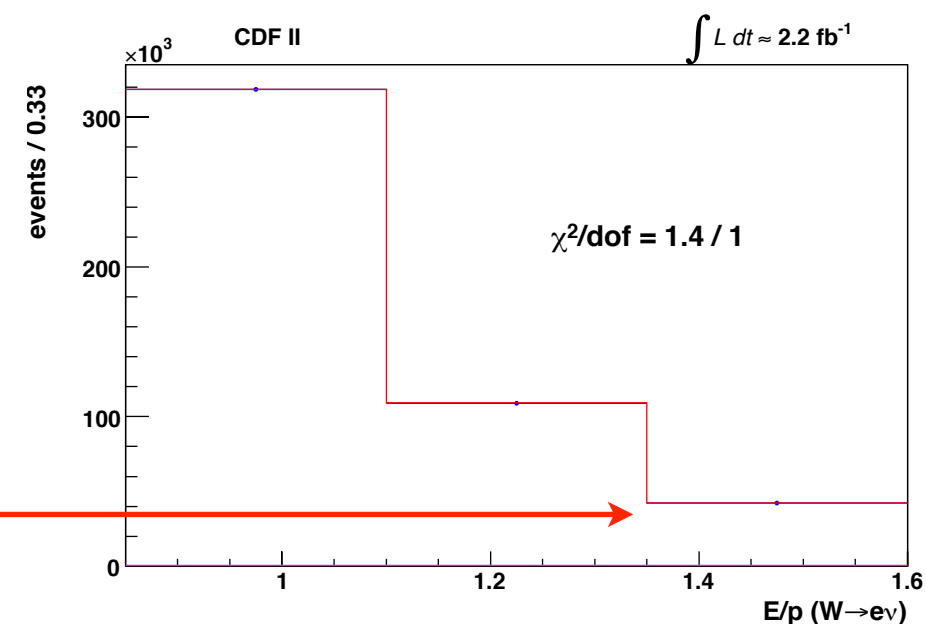
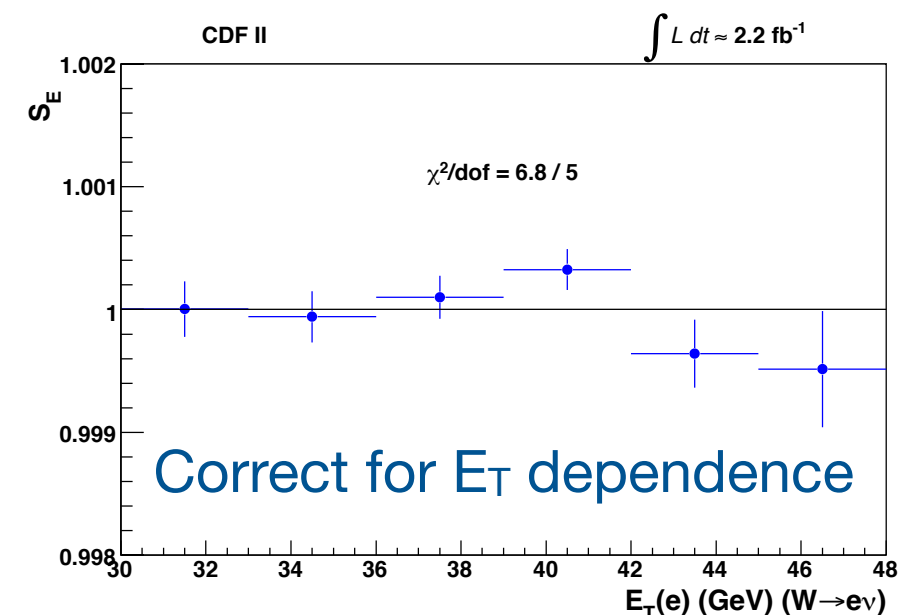


EM energy scale

- Apply calibrated track momentum scale to set EM scale
- E/p of W and Z events
 - Overall scale from peak
 - Radiative tail used to tune material model

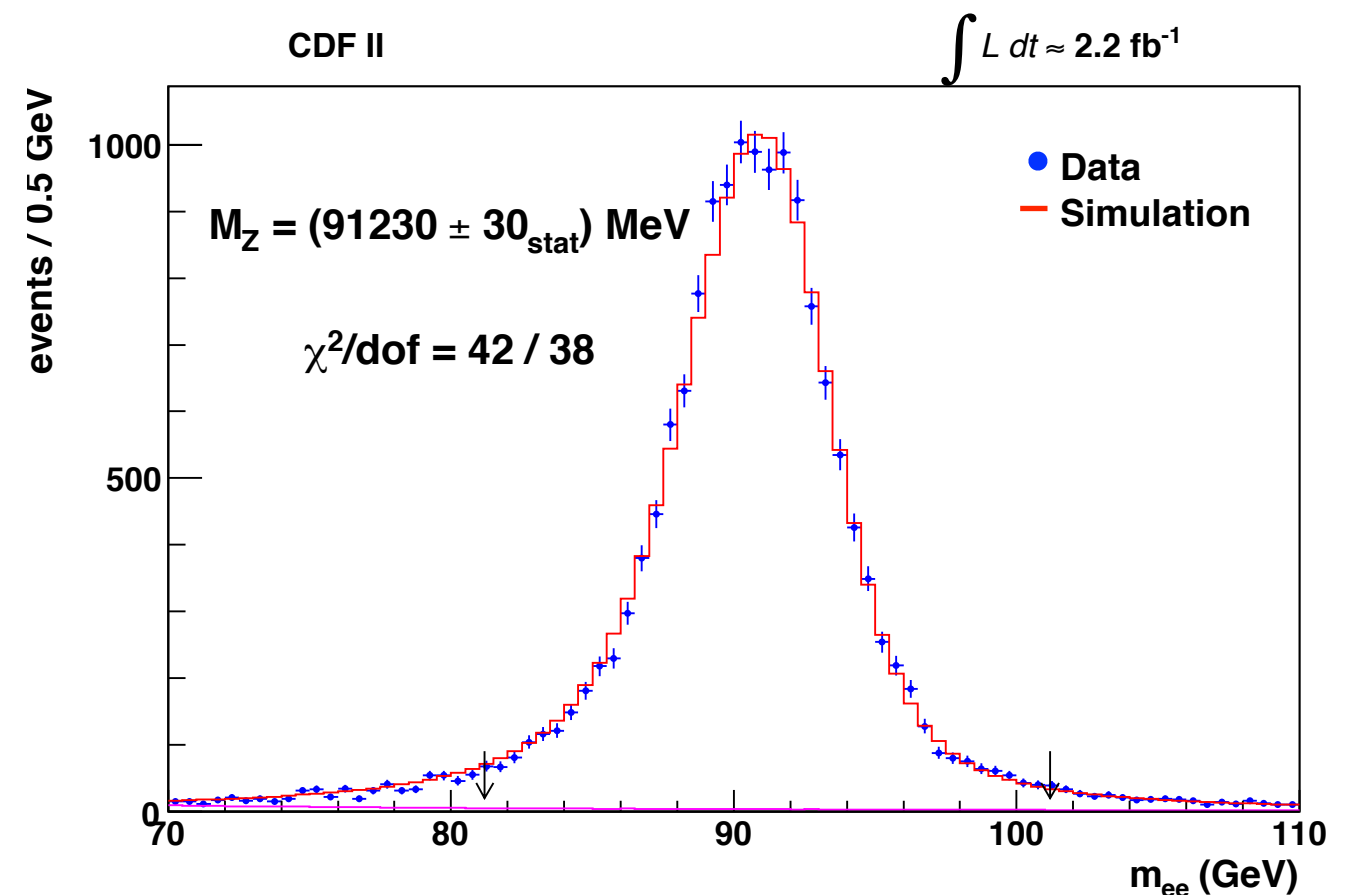
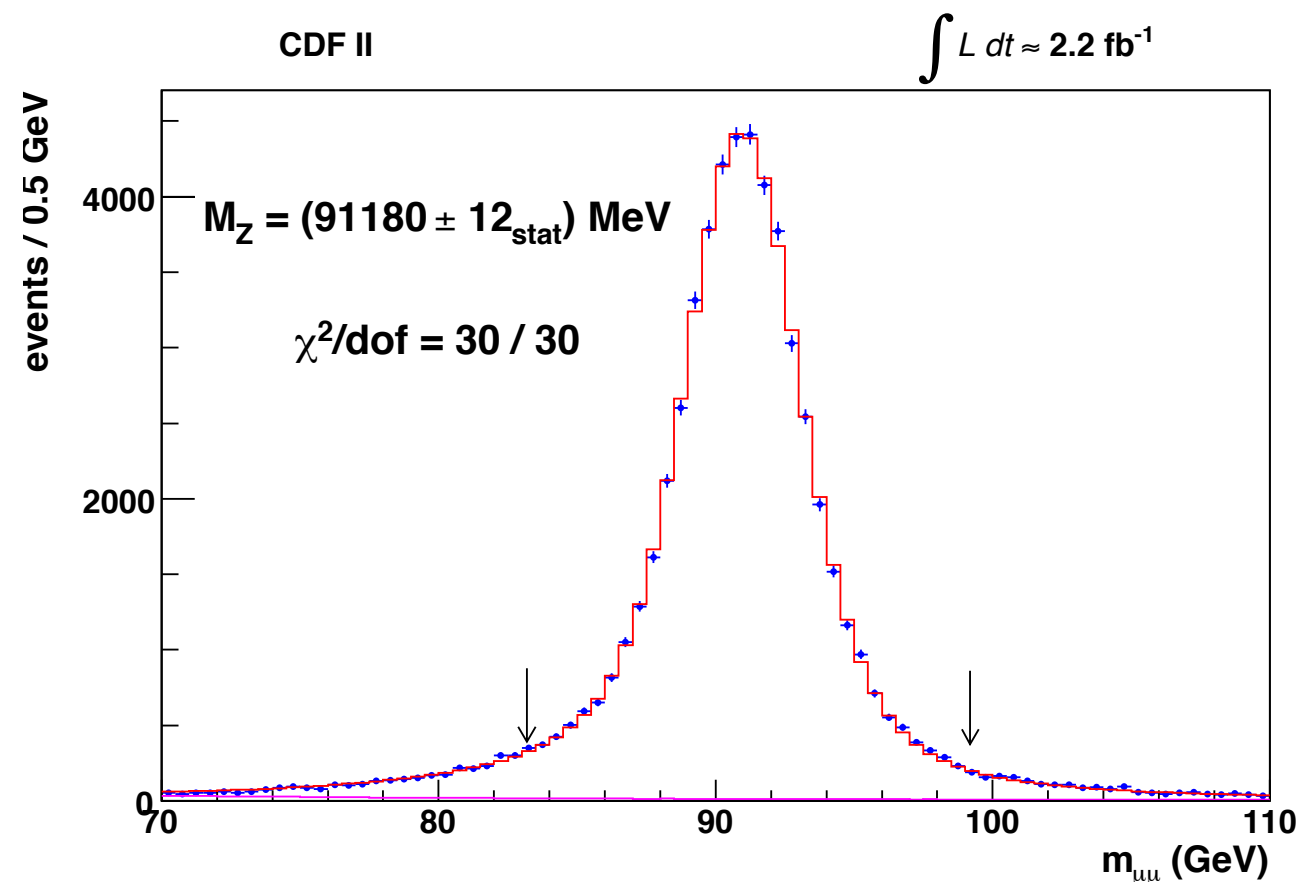


Scale radiative material in simulation



Cross-check and further calibration with M_Z

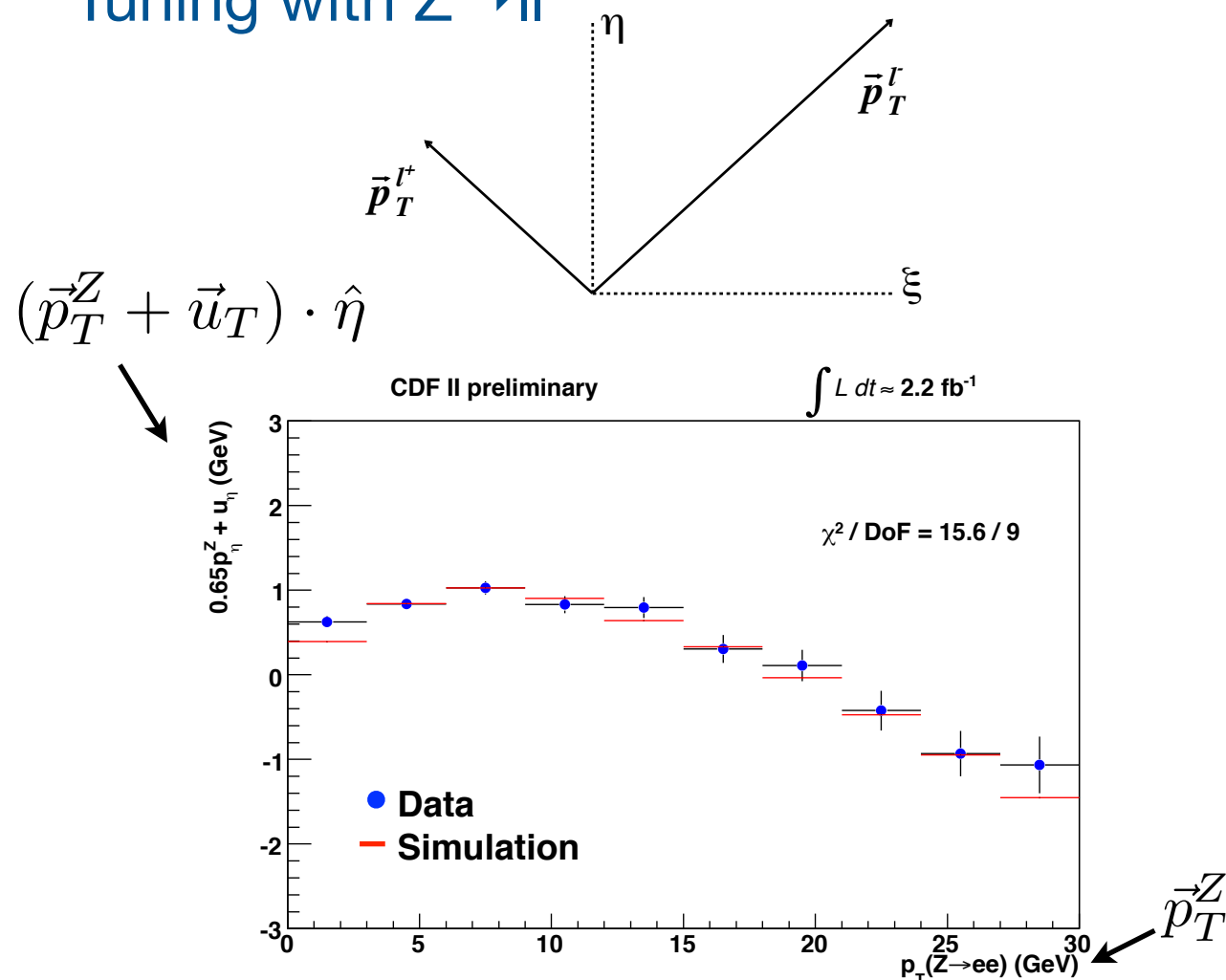
- Perform blinded measurement of Z mass using scales not calibrated to M_Z
- Most precise measurement of M_Z at a hadron collider!
 - Comparison to LEP value of $M_Z=91188\pm2$ MeV is a powerful cross-check of calibration
- After unblinding, M_Z added as further calibration to both track momentum and EM energy scales
 - Combined: $\Delta M_W = 7$ MeV (momentum scale), $\Delta M_W = 10$ MeV (EM scale)



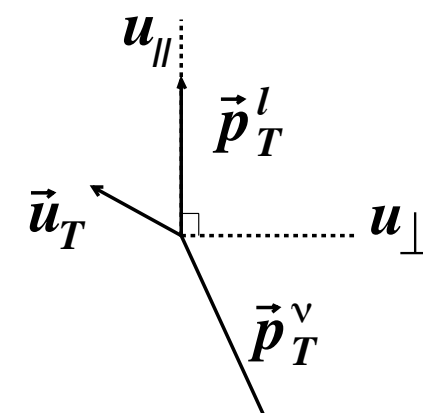
Recoil

- Measured recoil: all calorimeter energy minus measured lepton
 - Contains 1) hard recoil from hadronic activity in W/Z event, 2) underlying event/spectator interaction energy
- Tune using Z and minimum-bias data
- Validate using measured recoil in W events

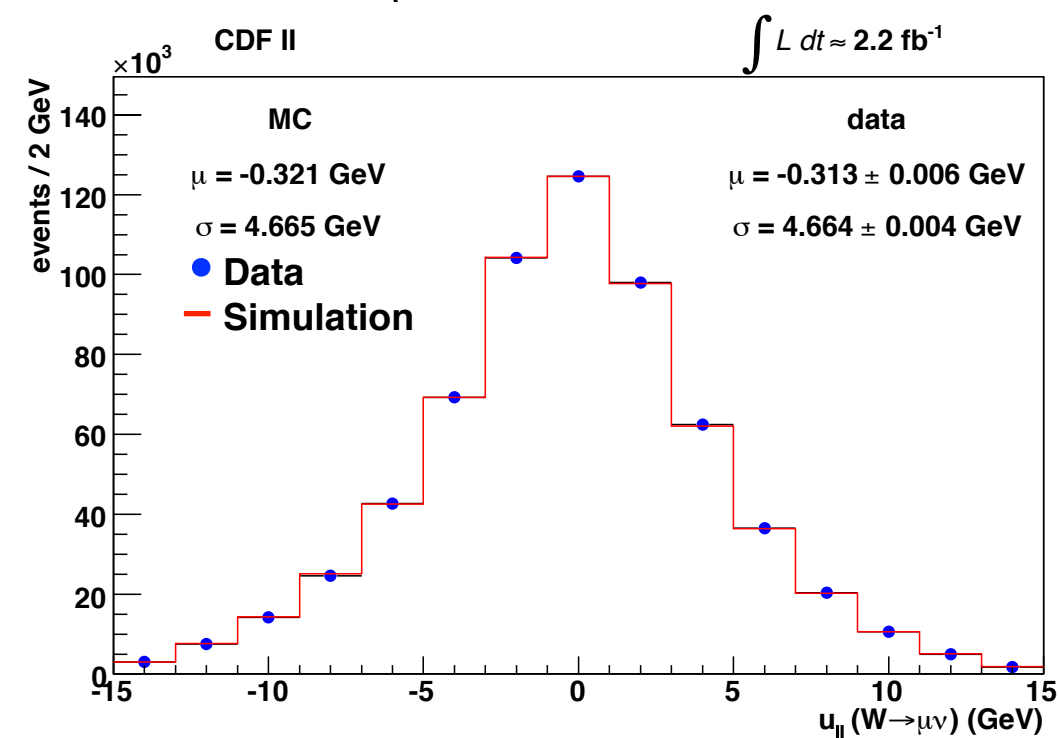
Tuning with $Z \rightarrow \ell\ell$



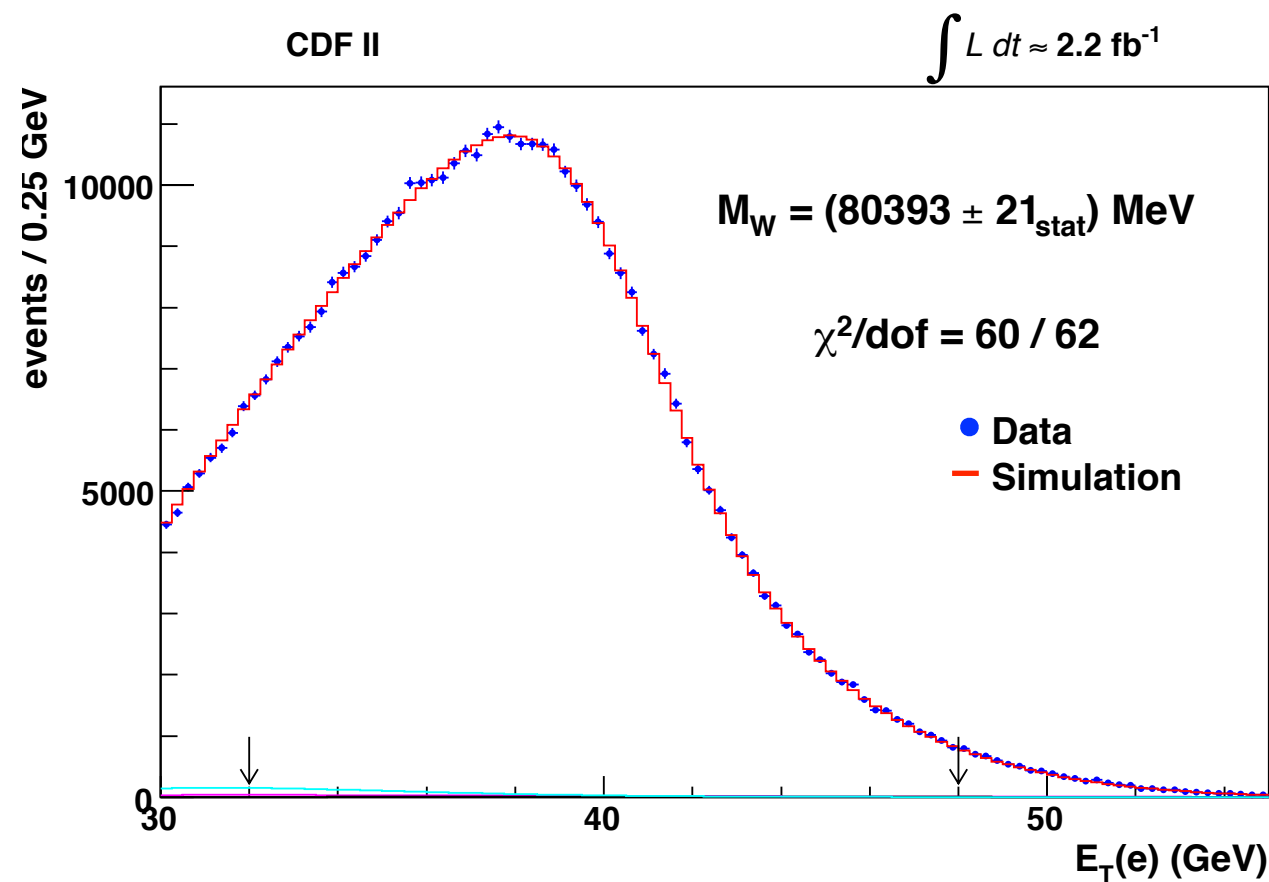
Validating with $W \rightarrow \ell\nu$



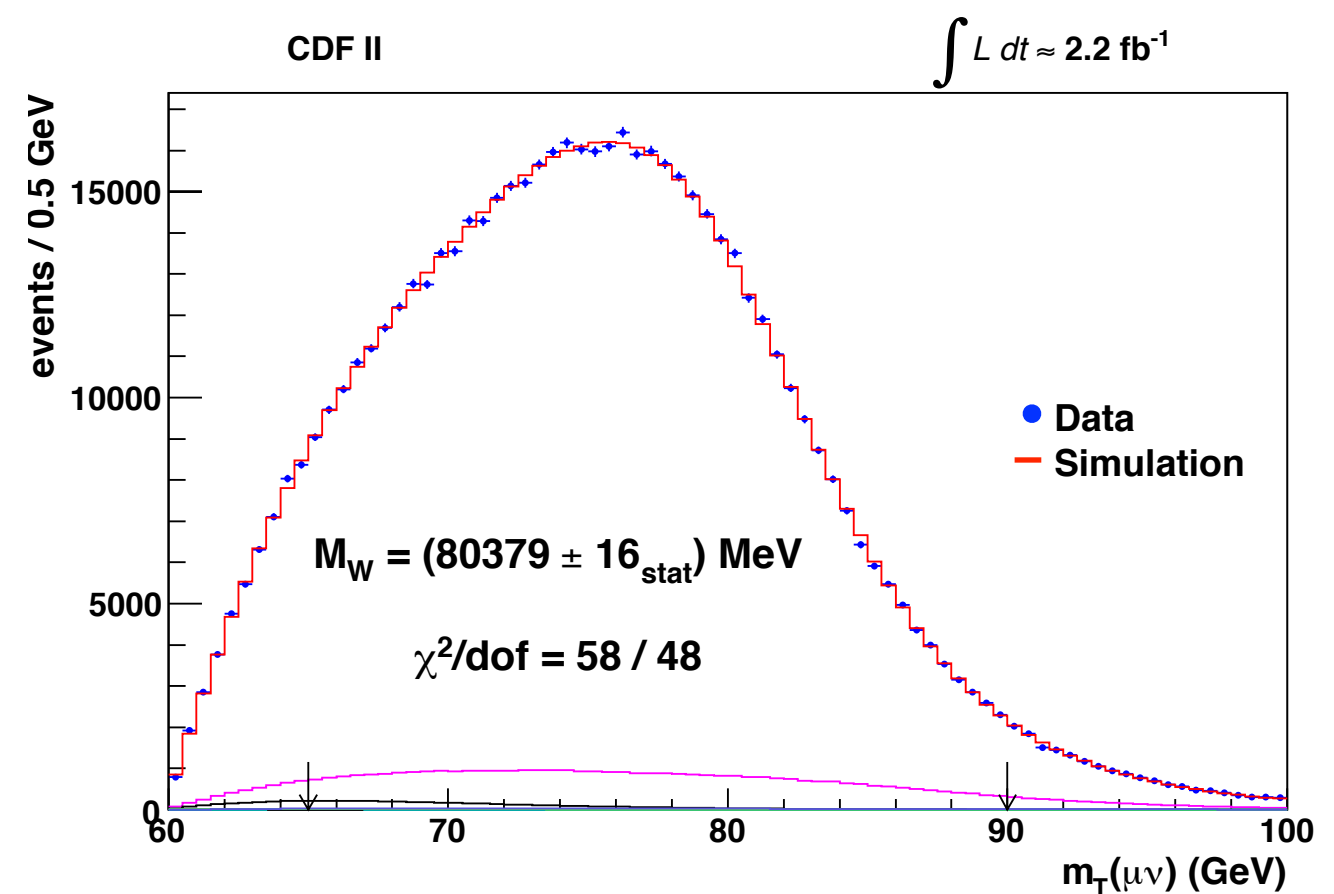
for $u \ll p_T^l$:
 $m_T \approx 2p_T^l + u_\parallel$
 $p_T^\nu \approx 2p_T^l + 2u_\parallel$
 mis-modeled $u_\parallel$ directly
 biases measured M_W



Example mass fits



p_T : electrons

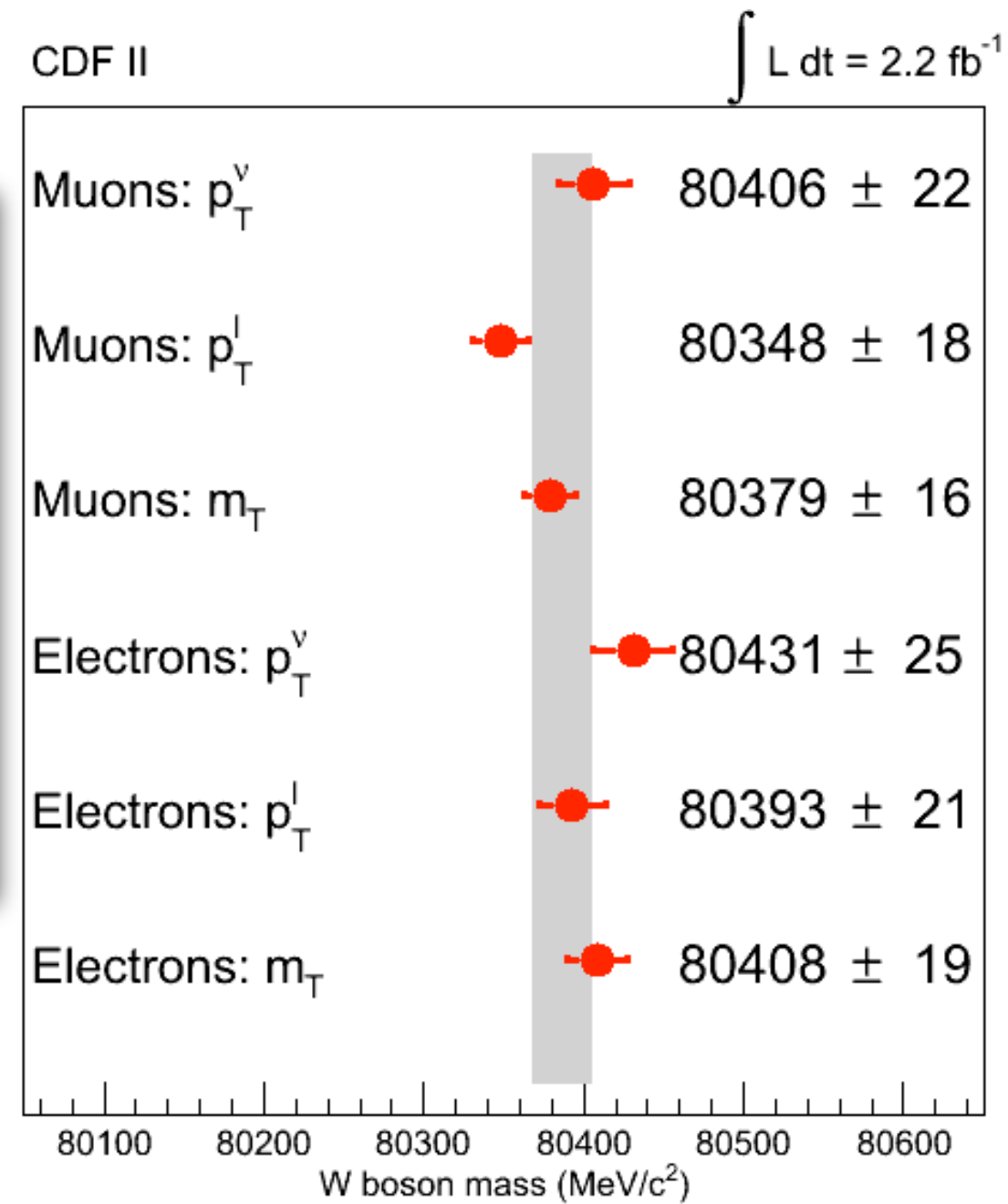


m_T : muons

- All fits kept **blinded** during analysis
 - Random, common, offset from $[-75, +75] \text{ MeV}$ added to all fits
 - Offset only removed after analysis is frozen

All fits

Fit	Fit result (MeV)	χ^2/dof
$W \rightarrow e\nu$ (m_T)	80408 ± 19	52/48
$W \rightarrow e\nu$ (p_T^l)	80393 ± 21	60/62
$W \rightarrow e\nu$ (p_T^ν)	80431 ± 25	71/62
$W \rightarrow \mu\nu$ (m_T)	80379 ± 16	57/48
$W \rightarrow \mu\nu$ (p_T^l)	80348 ± 18	58/62
$W \rightarrow \mu\nu$ (p_T^ν)	80406 ± 22	82/62



Combined results

- All electron fits combined

$$M_W = 80406 \pm 25 \text{ MeV}, \chi^2/\text{dof} = 1.4/2 (49\%)$$

- All muon fits combined

$$M_W = 80374 \pm 22 \text{ MeV}, \chi^2/\text{dof} = 4/2 (12\%)$$

- All fits combined

$$M_W = 80387 \pm 19 \text{ MeV}, \chi^2/\text{dof} = 6.6/5 (25\%)$$

Combine using *BLUE*
L. Lyons, D. Gibaut, and P. Clifford,
NIM A **270**, 110 (1988).

Combined uncertainties

Source	Uncertainty 2.2 fb ⁻¹ (MeV)
Lepton energy scale	7
Lepton energy resolution	2
Recoil energy scale	4
Recoil energy resolution	4
Lepton removal	2
Backgrounds	3
p _T (W) model	5
PDFs	10
QED radiation	4
<i>Total systematics</i>	<i>15</i>
W statistics	12
<i>Total</i>	<i>19</i>

$$M_W = 80387 \pm 12_{\text{stat}} \pm 15_{\text{syst}} \text{ MeV}/c^2$$

Combined uncertainties

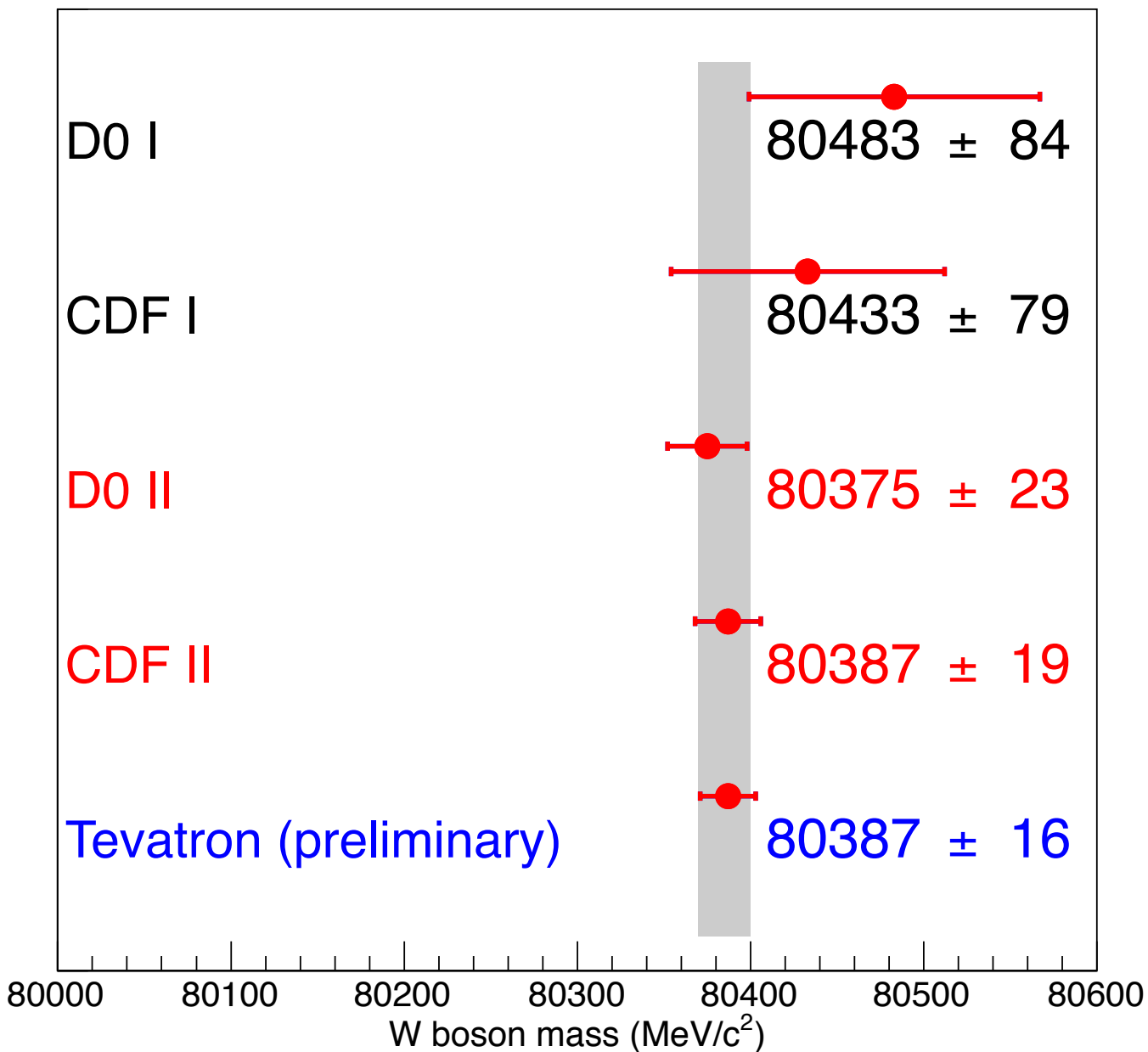
Statistics limited by
control data

Theory based
(external inputs)

Source	Uncertainty 2.2 fb ⁻¹ (MeV)	Uncertainty 0.2 fb ⁻¹ (MeV)
Lepton energy scale	7	23
Lepton energy resolution	2	4
Recoil energy scale	4	8
Recoil energy resolution	4	10
Lepton removal	2	6
Backgrounds	3	6
p _T (W) model	5	4
PDFs	10	11
QED radiation	4	10
<i>Total systematics</i>	<i>15</i>	<i>34</i>
W statistics	12	34
Total	19	48

$$M_W = 80387 \pm 12_{\text{stat}} \pm 15_{\text{syst}} \text{ MeV}/c^2$$

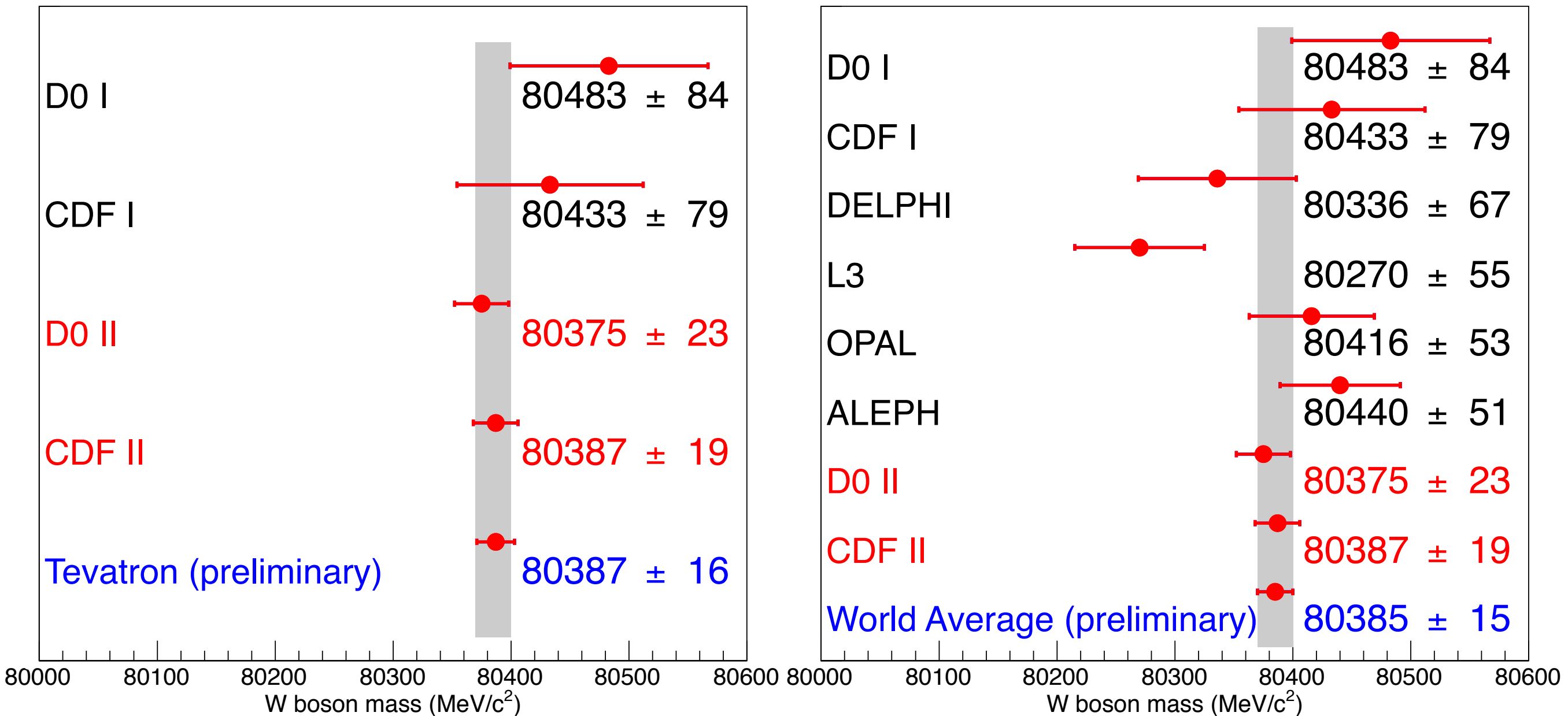
Tevatron and world combinations



nb: 2009 world average

$$M_W = 80399 \pm 23 \text{ MeV}$$

Tevatron and world combinations



nb: 2009 world average

$$M_W = 80399 \pm 23 \text{ MeV}$$

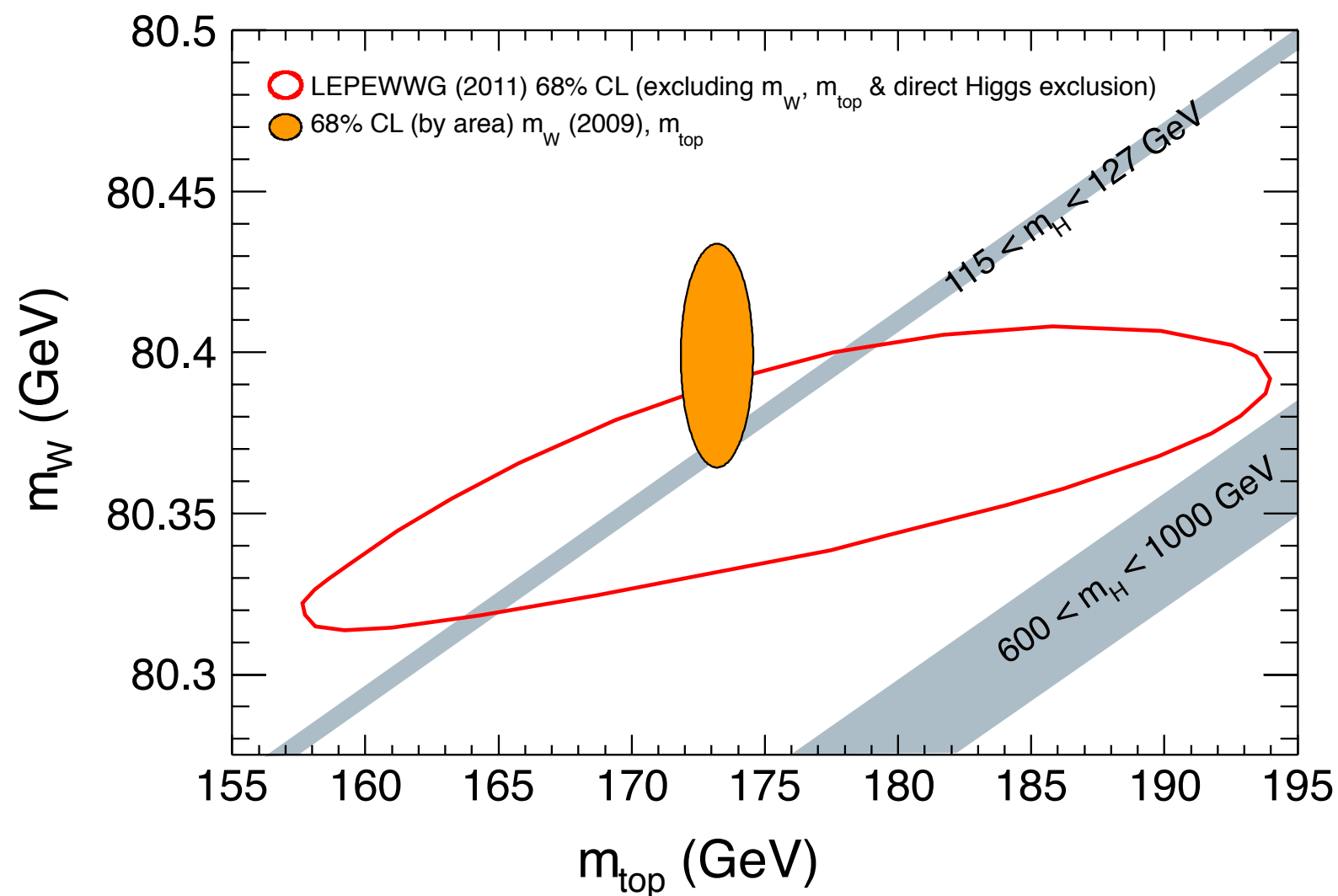
W mass vs. top mass

With $M_W = 80399 \pm 23$ MeV

$M_H = 92^{+34}_{-26}$ GeV

$M_H < 161$ GeV @95% CL

LEPEWWG/ZFitter



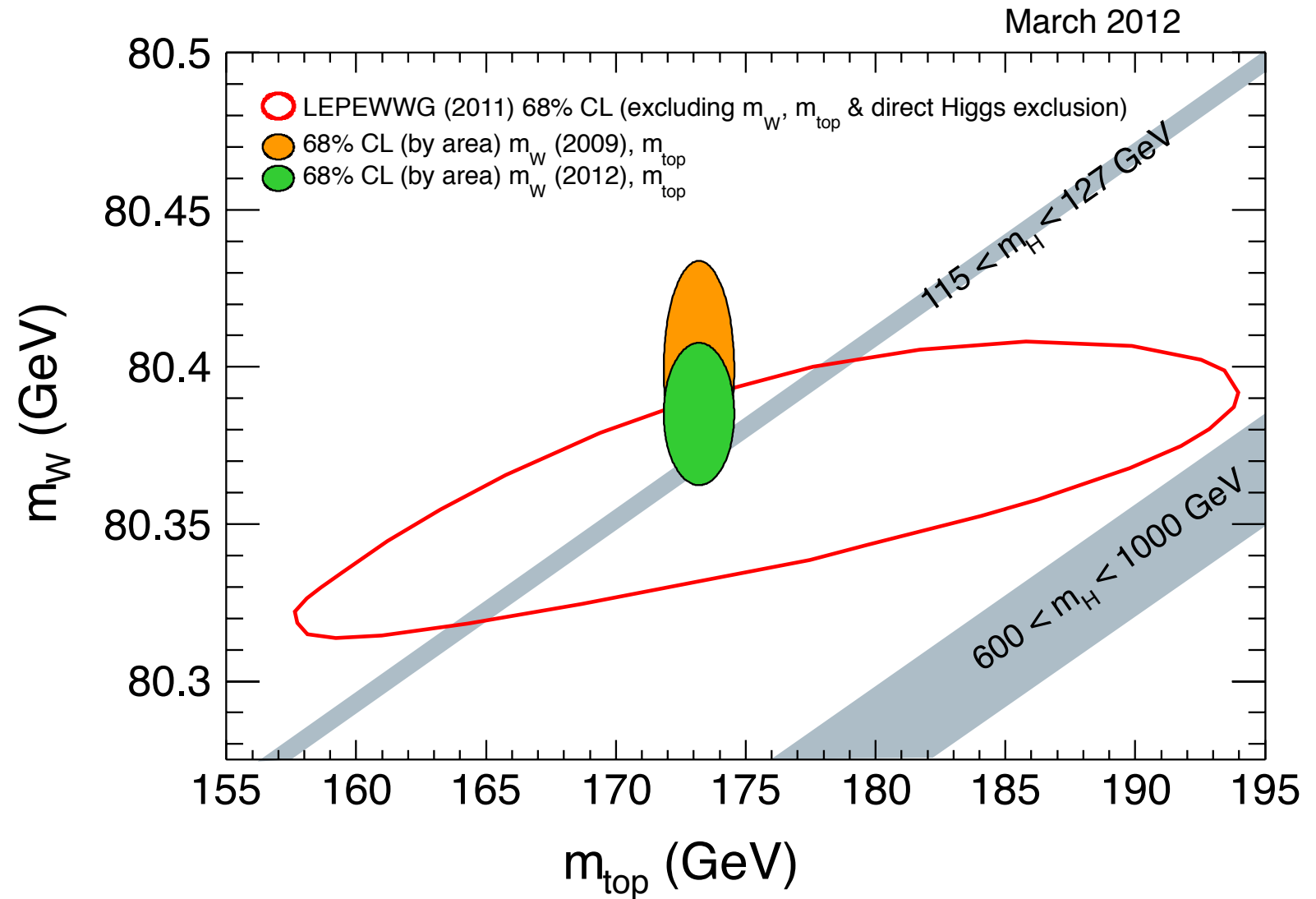
W mass vs. top mass

With $M_W = 80385 \pm 15$ MeV

$M_H = 94^{+29}_{-24}$ GeV

$M_H < 152$ GeV @95% CL

LEPEWWG/ZFitter



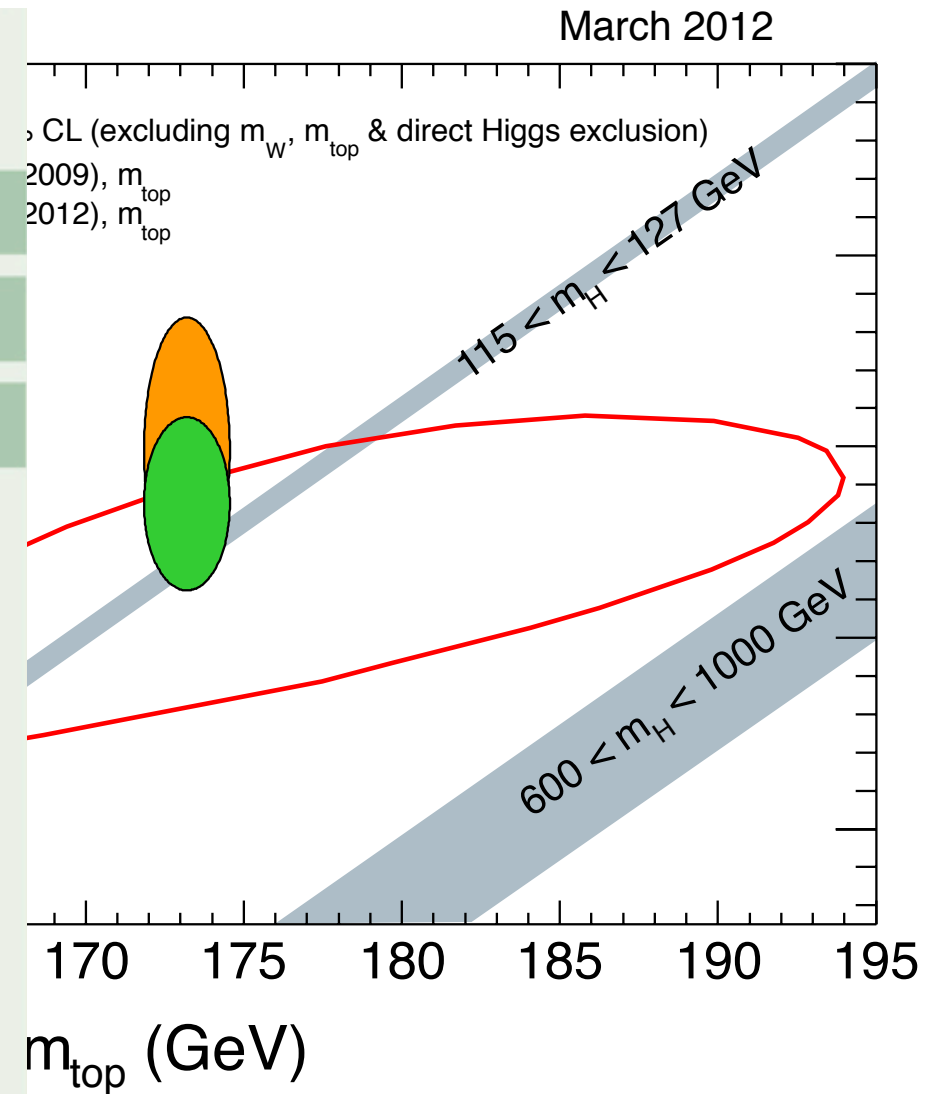
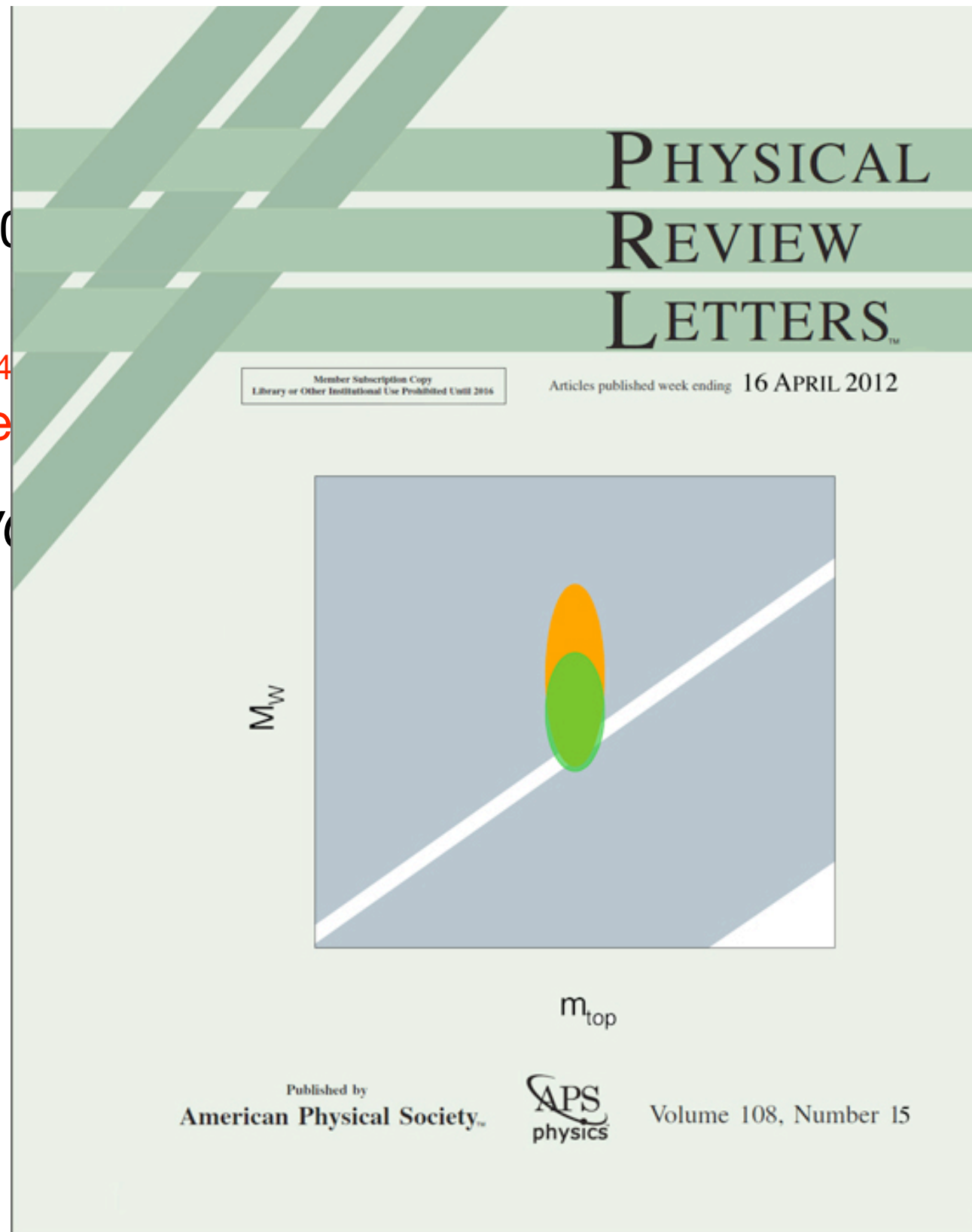
W mass vs. top mass

With $M_W = 80$

$M_H = 94^{+29}_{-24}$

$M_H < 152$ GeV

LEPEWW



CDF: PRL **105**, 151803 (2012)
 DØ: PRL **105**, 151804 (2012)
PRL Editors' Suggestions

And finally...

And finally...

- An award for the entire ~~CDF Collaboration~~ **Tevatron physics program**
 - $\Delta M_W = 16$ MeV is a true legacy measurement

And finally...

- An award for the entire ~~CDF Collaboration~~ **Tevatron physics program**
 - $\Delta M_W = 16$ MeV is a true legacy measurement
- A team effort over ~5 years

And finally...

- An award for the entire ~~CDF Collaboration~~ **Tevatron physics program**
 - $\Delta M_W = 16$ MeV is a true legacy measurement
- A team effort over ~5 years

<http://www-cdf.fnal.gov/physics/ewk/2012/wmass/>

Measurement of the W Boson Mass with 2.2/fb of Data at CDF II

Bodhitha Jayatilaka, Ashutosh Kotwal, Ravi Shekhar, Siyuan Sun, Yu Zeng

Duke University

Oliver Stelzer-Chilton

TRIUMF

Larry Nodulman

Argonne National Laboratory

Daniel Beecher, Ilija Bizjak, Mark Lancaster, Sarah Malik, Tom Riddick, David Waters

University College London

Christopher Hays, Peter Renton

University of Oxford

And finally...

- An award for the entire ~~CDF Collaboration~~ **Tevatron physics program**
 - $\Delta M_W = 16$ MeV is a true legacy measurement
- A team effort over ~5 years

<http://www-cdf.fnal.gov/physics/ewk/2012/wmass/>

Measurement of the W Boson Mass with 2.2/fb of Data at CDF II

Bodhitha Jayatilaka, Ashutosh Kotwal, Ravi Shekhar, Siyuan Sun, Yu Zeng

Duke University

Oliver Stelzer-Chilton

TRIUMF

Larry Nodulman

Argonne National Laboratory

Daniel Beecher, Ilija Bizjak, Mark Lancaster, Sarah Malik, Tom Riddick, David Waters

University College London

Christopher Hays, Peter Renton

University of Oxford

- Thanks to everyone else at CDF who helped
 - And the Tevatron

Review committee: F. Bedeschi, M. Shochet, B. Ashmanskas, K. Hatakeyama

And finally...

- An award for the entire ~~CDF Collaboration~~ **Tevatron physics program**
 - $\Delta M_W = 16$ MeV is a true legacy measurement
- A team effort over ~5 years

<http://www-cdf.fnal.gov/physics/ewk/2012/wmass/>

Measurement of the W Boson Mass with 2.2/fb of Data at CDF II

Bodhitha Jayatilaka, Ashutosh Kotwal, Ravi Shekhar, Siyuan Sun, Yu Zeng

Duke University

Oliver Stelzer-Chilton

TRIUMF

Larry Nodulman

Argonne National Laboratory

Daniel Beecher, Ilija Bizjak, Mark Lancaster, Sarah Malik, Tom Riddick, David Waters

University College London

Christopher Hays, Peter Renton

University of Oxford

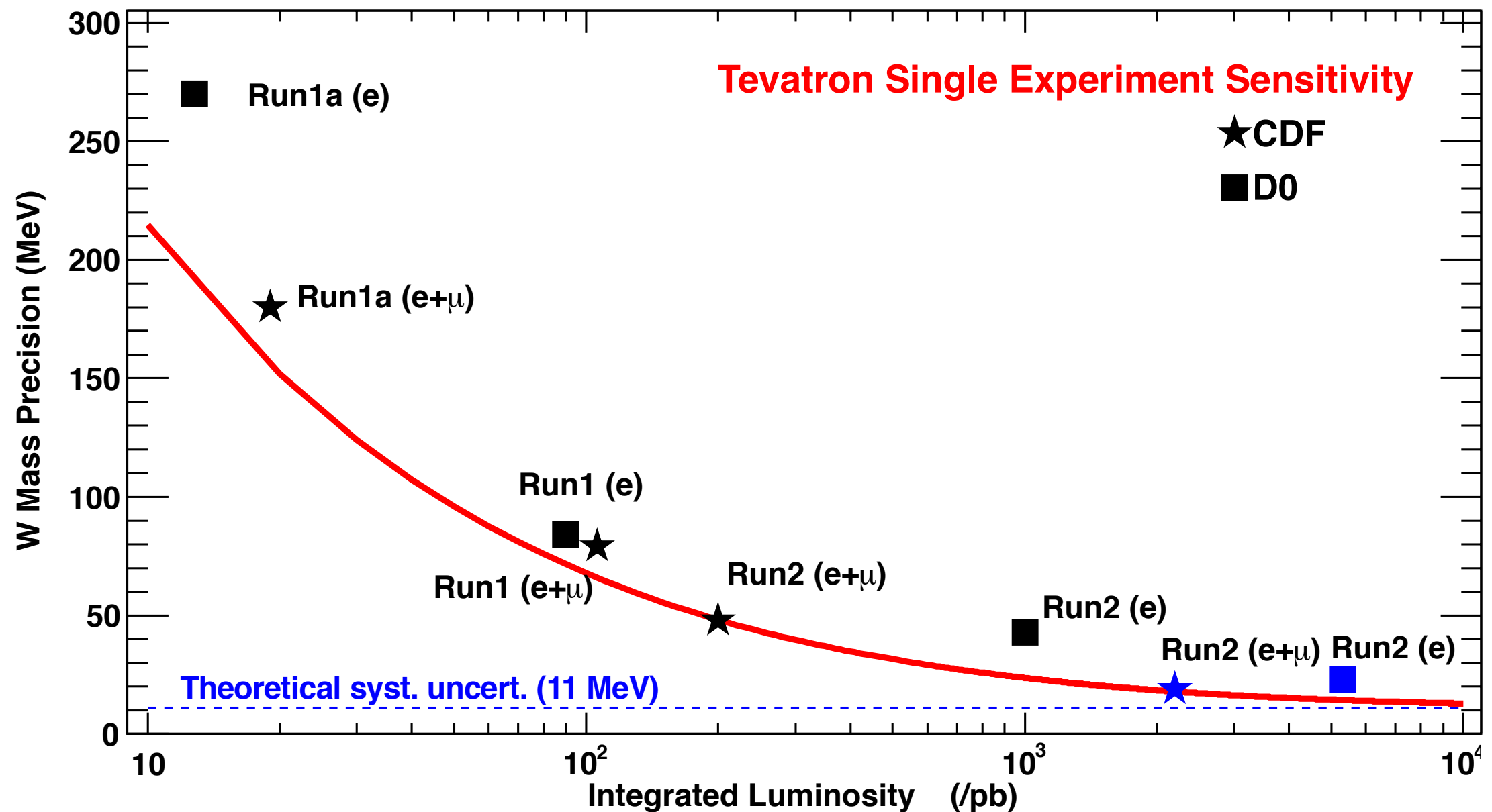
- Thanks to everyone else at CDF who helped
 - And the Tevatron

Review committee: F. Bedeschi, M. Shochet, B. Ashmanskas, K. Hatakeyama

- Thanks to the URA, Tollestrup award committee, and UEC

Backup

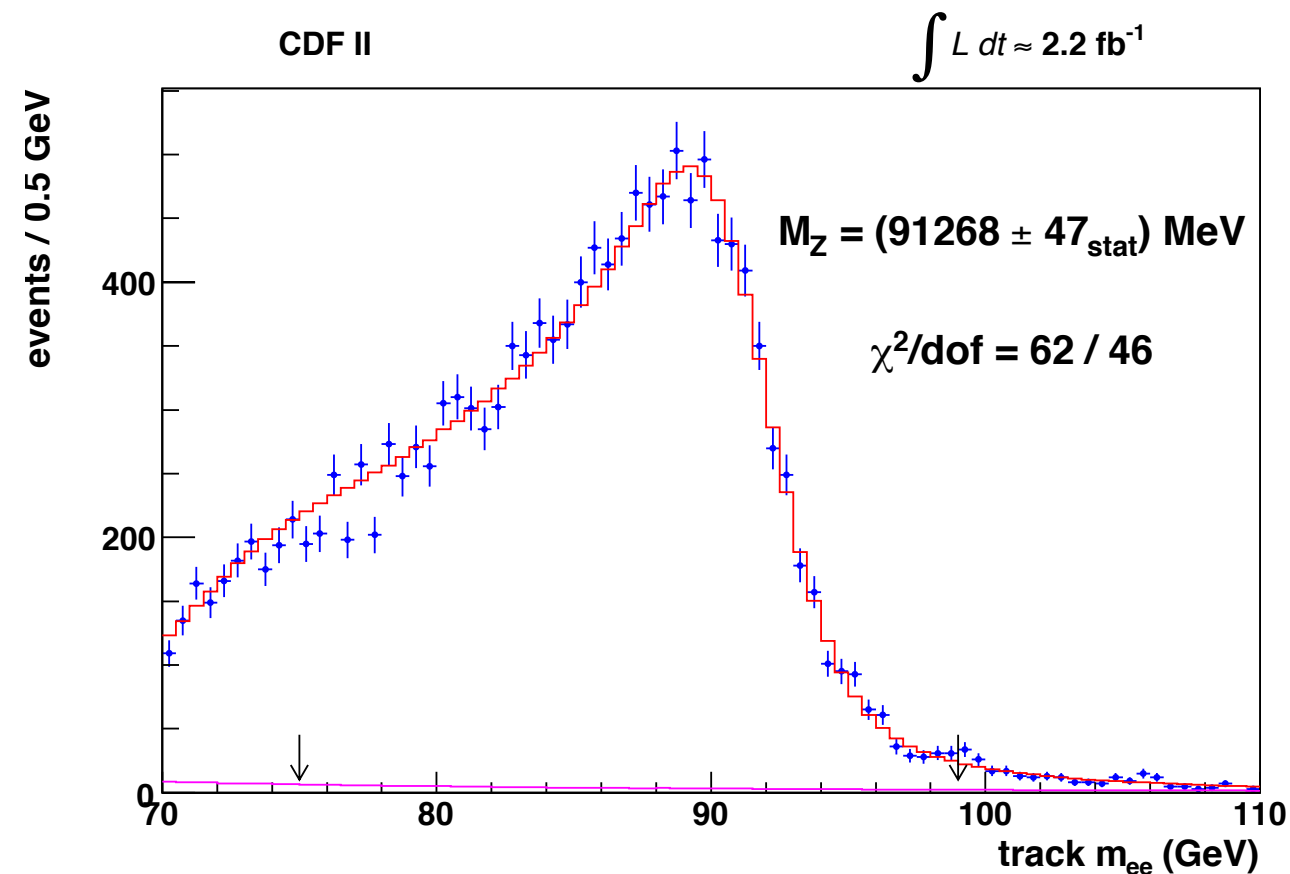
Uncertainty projections



- Projection assumes PDF+QED errors (11 MeV) fixed
 - Become limiting uncertainty for measurements with full Tevatron dataset

Z mass with electron tracks

- Measurement made with only track momenta of Z electrons
- Validates material model and application of momentum scale to high- p_T electron tracks



Parton distribution functions and backgrounds

PDFs

- Utilize CTEQ6.6 PDF as default
- Evaluate 90% CL uncertainty eigenvectors for MSTW2008 and CTEQ6.6 (consistent)
- Use 68% CL MSTW2008 to determine systematic $\Delta M_W = 10 \text{ MeV}$

Backgrounds

- Estimated using a combination of data and MC-driven methods
- Except $Z \rightarrow \mu\mu$ (lost forward muon), backgrounds are small
- Include all estimated background shapes in final templates

Background	Fraction of W data (%)		$\Delta m_W \text{ (MeV)}$					
			m_T	p_T^l		p_T^ν		
$Z \rightarrow ll$	7.35 ± 0.09	0.139 ± 0.014	2	1	4	2	5	1
$W \rightarrow \tau\nu$	0.880 ± 0.004	0.93 ± 0.01	0	1	0	1	0	1
QCD	0.035 ± 0.025	0.39 ± 0.14	1	4	1	2	1	4
Decay-in-flight	0.24 ± 0.02		1		3		1	
Cosmic Rays	0.02 ± 0.02		1		1		1	
<i>Total</i>			3	4	5	3	6	4

muons
electrons

Uncertainty progress

