



Search for CP Violations at Colliders

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Outline

-  **CP violating phases in SUSY (MSSM)**
-  **Constraints on SUSY CP phases : SUSY CP problem**

Solutions to SUSY CP problem

-  **CP violating Observables at collider**

CP Violating Phases in the MSSM

- First, consider only flavor-independent phases and neglect relative phases in the gaugino sector

SUSY parameter $W = \mu H_u H_d$ Higgsino mass

soft SUSY breaking parameters

$$\mathcal{L} = -\frac{1}{2}m_\lambda \lambda\lambda - A(h_u Q H_u \bar{u} - h_d Q H_d \bar{d} - h_e L H_d \bar{e}) - \mu B H_u H_d + h.c.$$

Gaugino mass Trilinear soft mass term B term for Higgs

Naively there are four CP violating phases, but only **two** of them are physical!



In the absence of the parameters above, two additional flavor conserving global U(1)'s: $U(1)_{PQ}$ and $U(1)_{R-PQ}$



We treat dimensionful parameters in non-gauge couplings which break the two U(1)'s as spurions with charges assigned to compensate those of fields. Dimopoulos and Thomas 1995

$$W = \mu H_u H_d$$

$$\mathcal{L} = -\frac{1}{2}m_\lambda \lambda \lambda - \mu B H_u H_d - A (h_u Q H_u \bar{u} - h_d Q H_d \bar{d} - h_e L H_d \bar{e}) + h.c.$$

	$U(1)_{PQ}$	$U(1)_{R-PQ}$
m_λ	0	-2
A	0	-2
μB	-2	0
μ	-2	2
H_u	1	0
H_d	1	0
$Q\bar{u}$	-1	2
$Q\bar{d}$	-1	2
$L\bar{e}$	-1	2



Physical phases should be invariant under reparametrization: linear combination of phases with zero total charge under both $U(1)$'s.

$$m_\lambda \mu (\mu B)^*, \quad A \mu (\mu B)^*, \quad A^* m_\lambda$$

Only two of them are independent.

	$U(1)_{PQ}$	$U(1)_{R-PQ}$
m_λ	0	-2
A	0	-2
μB	-2	0
μ	-2	2
H_u	1	0
H_d	1	0
$Q\bar{u}$	-1	2
$Q\bar{d}$	-1	2
$L\bar{e}$	-1	2



Flavor dependent phases and phase in the gaugino sector,

Two relative phases between gaugino masses $m_{\lambda}^{i*} m_{\lambda}^j$

Flavor dependent phases, Lebedev 2002

E.g., relative phases between off-diagonal A terms;
For the squark sector, at most 28 independent phases

$$\phi_0 = \text{Arg} \left[(Y^d Y^{d\dagger})_{12} (Y^d Y^{d\dagger})_{13}^* (Y^d Y^{d\dagger})_{23} \right] ,$$

$$\phi_i^a = \epsilon_{ijk} \text{Arg} \left[(Y^d Y^{d\dagger})_{jk} (F^a)_{jk}^* \right] ,$$

$$\chi_i^a = \epsilon_{ijk} \text{Arg} \left[(A^{u\dagger} Y^u + \text{h.c.})_{jk} (G^a)_{jk}^* \right] ,$$

$$\xi_i^a = \epsilon_{ijk} \text{Arg} \left[(A^{d\dagger} Y^d + \text{h.c.})_{jk} (H^a)_{jk}^* \right] ,$$

$$F^a = \{ M^{2q_L}, A^u A^{u\dagger}, A^d A^{d\dagger}, A^u Y^{u\dagger} + \text{h.c.}, A^d Y^{d\dagger} + \text{h.c.} \} ,$$

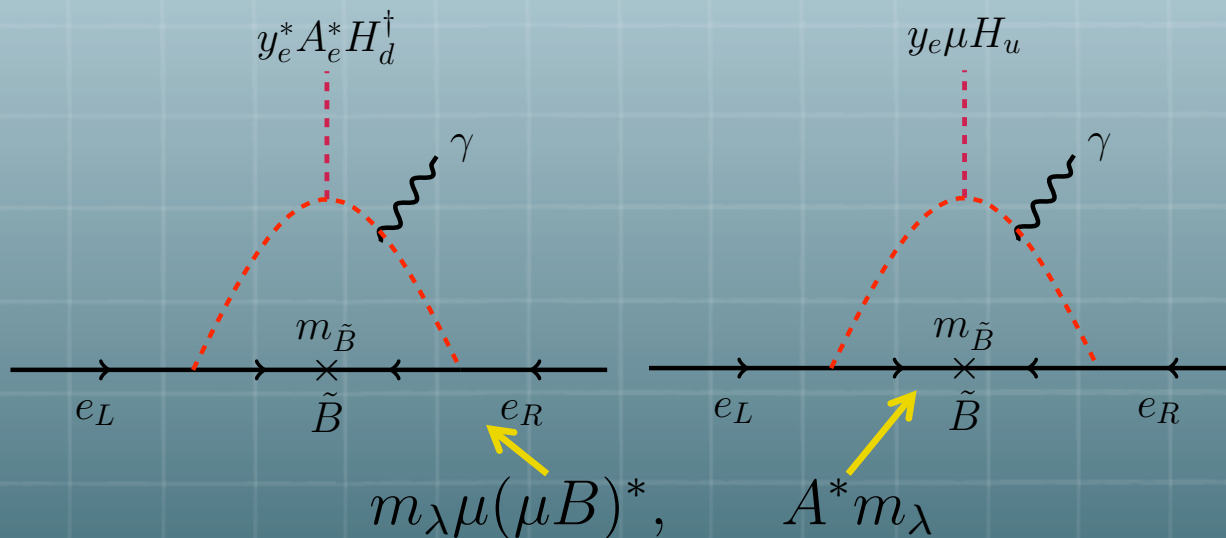
$$G^a = \{ M^{2u_R}, A^{u\dagger} A^u \} ,$$

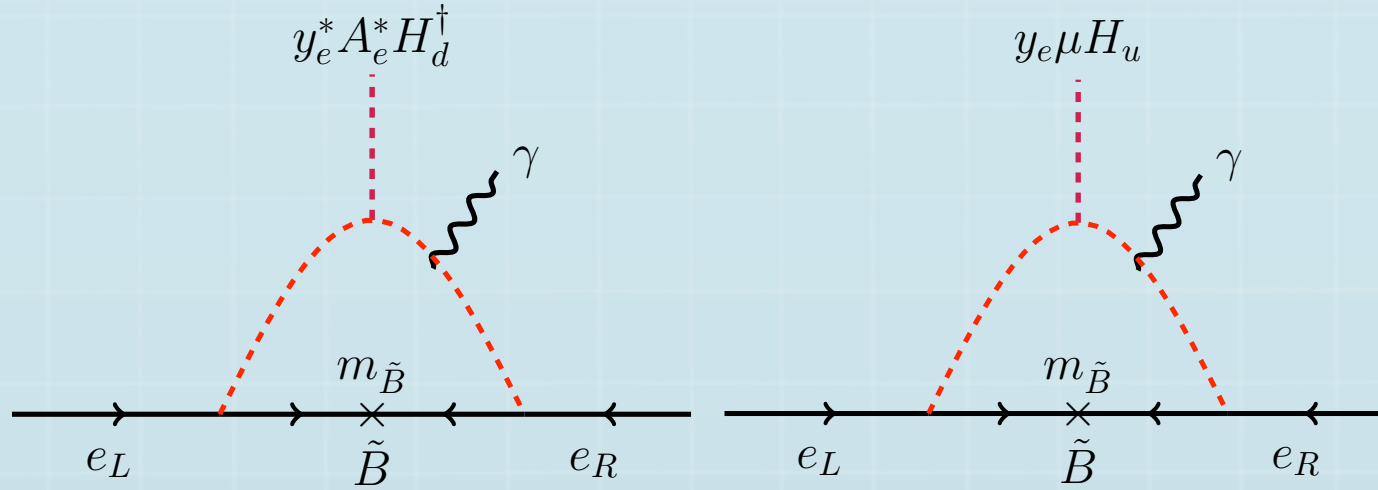
$$H^a = \{ M^{2d_R}, A^{d\dagger} A^d \} .$$

SUSY CP problem

- The fermion electric dipole moments receive one-loop contributions due to superpartner exchange which for generic phases can exceed the experimental bounds
- Phases that are constrained, e.g.:

For a review, Ellis, Lee and Pilaftsis 2008





$$m_\lambda \mu (\mu B)^*, \quad A^* m_\lambda$$

$$\frac{df}{e} \sim 10^{-25} \phi \left(\frac{100 \text{ GeV}}{\tilde{m}} \right)^2 \text{ cm}$$

$$d_e/e < 1.05 \times 10^{-27} \text{ cm}$$

$$d_n/e < 2.9 \times 10^{-26} \text{ cm (90\%)}$$

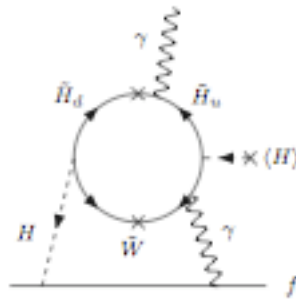
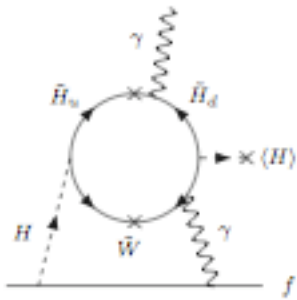
$$\phi \leq 10^{-2}$$



Current EDM bounds are sensitive to two-loop processes

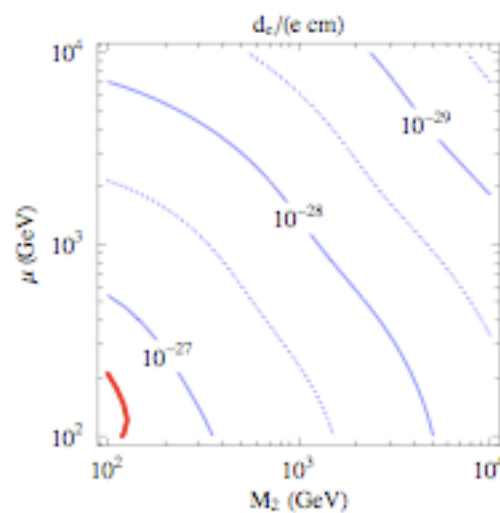
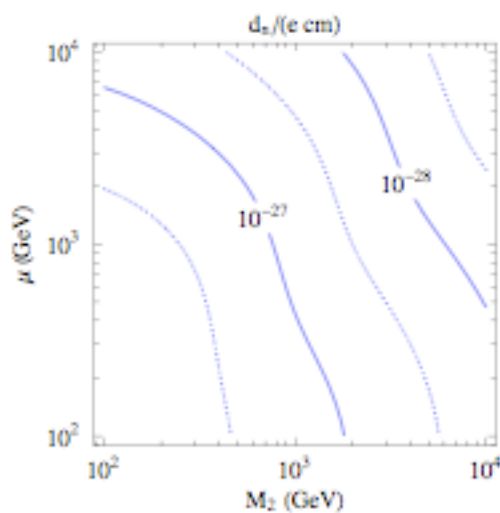
$$m_{\lambda\mu}(\mu B)^*$$

Chang, Keung , Pilaftsis, Keung;
Arkani-Hamed, Dimopoulos, Giudice, Romanino;
Li, Profumo, Ramsey-Musolf



$$\frac{c}{\Lambda^2} H^\dagger H F_{\mu\nu} \tilde{F}^{\mu\nu}$$

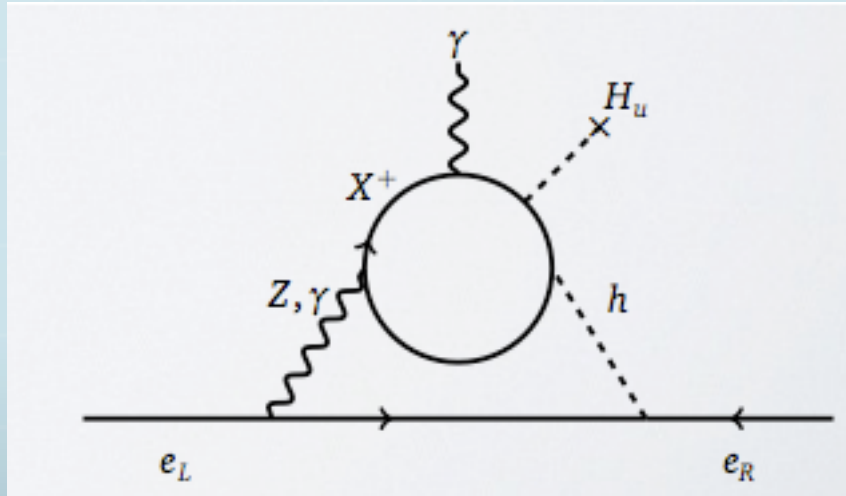
$$c = \frac{\alpha}{4\pi} g^2 \sin \beta \cos \beta \sin \phi; \Lambda^2 = M_2 \mu$$



$$\frac{d_f}{e} = -\frac{Q_f m_f c}{4\pi^2 \Lambda^2} \log \frac{\Lambda^2}{m_h^2}$$

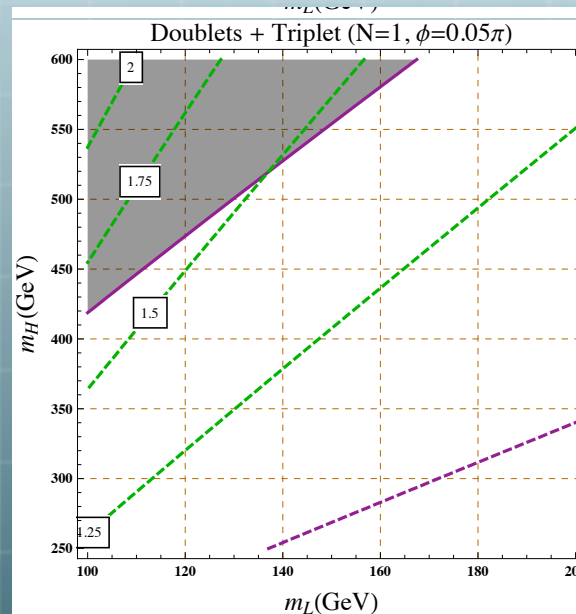
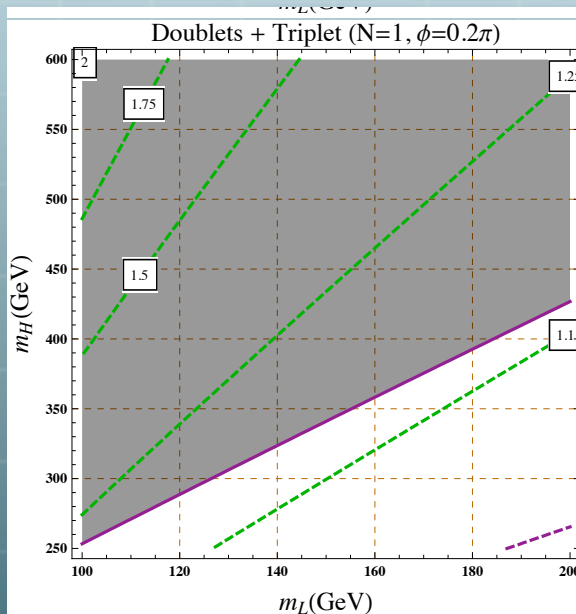
$$\frac{d_e}{e} < 10^{-27} \text{ cm} \rightarrow \Lambda \geq 700 \text{ GeV}$$

Interesting connection to a possible enhanced higgs diphoton rate:
(a possible Higgs CP problem?)




$$\mathcal{L}_M = - (\psi^{+Q} \chi^{+Q}) \begin{pmatrix} m_\psi & \frac{yv}{\sqrt{2}} \\ \frac{y^c v}{\sqrt{2}} & m_\chi \end{pmatrix} \begin{pmatrix} \psi^{-Q} \\ \chi^{-Q} \end{pmatrix} + cc,$$

$$\phi = \arg \left(m_\psi^* m_\chi^* y y^c \right).$$



Recently, McKeen, Pospelov
and Ritz 2012;
Fan and Reece 2013;

Ways around SUSY CP problem

-  **Heavy SUSY scalars: suppress some EDM diagrams**
 - a. First two generations are heavy but third generation, e.g., stops could be light**
 - b. Split SUSY: all scalars are heavy;**

There could still be two-loop chargino diagrams

Ways around SUSY CP problem

Accidental cancelations (tuning)

Cancelations exist between various one-loop diagrams contributing to EDMs. In other words, a tuning at 1% level is required.

Yet combining electron, neutron and mercury EDMs, one gets a general bound of $O(10^{-2})$ on SUSY phases in certain models, e.g, mSUGRA and D-brane models.

Abel, Khalil and Lebedev 2001 (Models with only two SUSY CP phases)

Ways around SUSY CP problem



CP symmetry Dimopoulos and Thomas 1995

An analogous SUSY PQ mechanism: SUSY phases are dynamical fields associated with spontaneous breakings of global symmetries at high energy in the SUSY breaking sector. The vacuum can then relax near a CP conserving point.

General gauge mediation: non-minimal messenger sector Carpenter, Dine, Festuccia and Mason 2008





Flavor off-diagonal CP violation

Abel, Bailin, Khalil and Lebedev 2001

Flavor-independent phases are zero and flavor off-diagonal phases are non-zero;

EDMs are suppressed but non-zero off-diagonal phases affect K and B physics

Recap




-  EDM experiments are sensitive to flavor-independent phases but could still be detectable at collider given tuning
-  Phases that EDM experiments are not sensitive to: off-diagonal phases; but flavor physics observables are sensitive to them.

Detect CP Violation at Collider

Asymmetries of decay rates, cross sections

Necessary conditions for a non-zero asymmetry (e.g, in decay rates)

$$\mathcal{A}_{\text{CP}} = \frac{\Gamma(M \rightarrow f) - \Gamma(\bar{M} \rightarrow \bar{f})}{\Gamma(M \rightarrow f) + \Gamma(\bar{M} \rightarrow \bar{f})}.$$

-  **Interference: Amplitude of the physical processes must be composed of at least two terms**
-  **The two terms must have different CP-even (“strong”) phases**
-  **The two terms must have different CP-odd (“weak”) phases**



Derivation

$$\mathcal{A}_{\text{CP}} = \frac{\Gamma(M \rightarrow f) - \Gamma(\bar{M} \rightarrow \bar{f})}{\Gamma(M \rightarrow f) + \Gamma(\bar{M} \rightarrow \bar{f})}.$$

$$\begin{aligned}\mathcal{M}(M \rightarrow f) &= |a_1|e^{i(\delta_1 + \phi_1)} + |a_2|e^{i(\delta_2 + \phi_2)}, \\ \mathcal{M}(\bar{M} \rightarrow \bar{f}) &= |a_1|e^{i(\delta_1 - \phi_1)} + |a_2|e^{i(\delta_2 - \phi_2)}.\end{aligned}$$

Two processes

Strong phases

weak phases

$$\Gamma(M \rightarrow f) \propto |\mathcal{M}(M \rightarrow f)|^2 \quad \Gamma(\bar{M} \rightarrow \bar{f}) \propto |\mathcal{M}(\bar{M} \rightarrow \bar{f})|^2$$

$$\mathcal{A}_{\text{CP}} \propto |a_1||a_2| \sin(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2),$$

Weak phases: CKM phase in the SM; complex phases of the Lagrangian parameters in general;

Strong phases: arise from strong-interactions/electromagnetic interactions among the particles in the final state and thus not always calculable or small;

Other calculable cases: in $B \rightarrow \Psi K_S$, through the time evolution of the intermediate $B^0 - \bar{B}^0$ system;

in processes involving a propagating intermediate unstable particle

$$\mathcal{M} = \mathcal{M}_1 \frac{1}{q^2 - m^2 + i\Gamma m} \mathcal{M}_2,$$

↑
CP even

A calculable strong phase $\arg \left(\frac{1}{q^2 - m^2 + i\Gamma m} \right)$

Strong phases: in processes involving a propagating intermediate unstable particle

$$\mathcal{M} = \mathcal{M}_1 \frac{1}{q^2 - m^2 + i\Gamma m} \mathcal{M}_2,$$

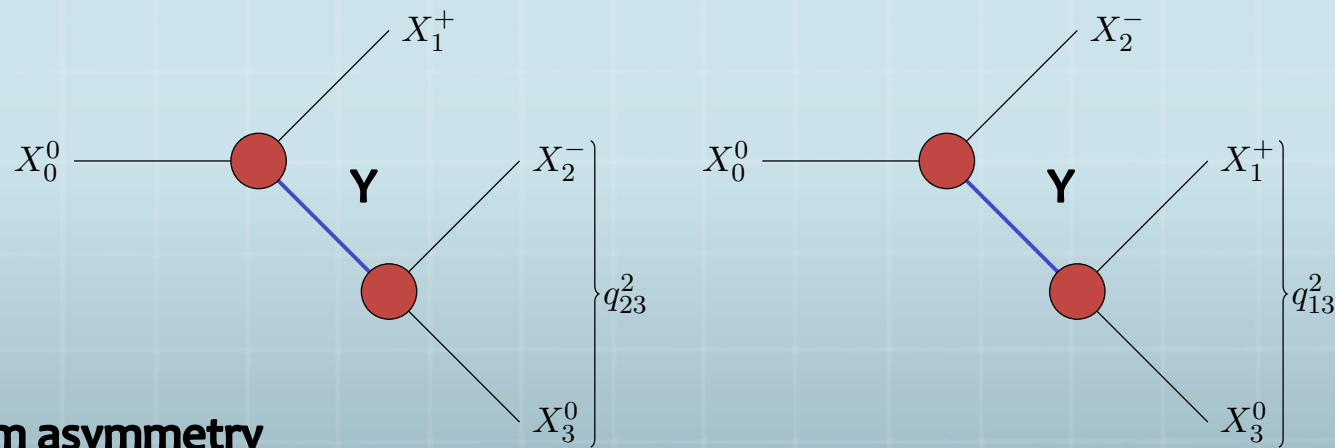
\uparrow
CP even

A calculable strong phase $\arg \left(\frac{1}{q^2 - m^2 + i\Gamma m} \right)$

Two ways to get different strong phases,

- a. The propagating particles could be different, thus different mass/width
(Eilam, Hewett, Soni 1991; Atwood, Eilam, Gronau, Soni 1994 in top, charged B decays)**
- b. The propagating particles could be the same, but off-shell by different amounts
(Berger, Blanke, and Grossman and Ray 2011, 2012);**

The propagating particles could be the same, but off-shell by different amounts
 (Berger, Blanke, and Grossman and Ray 2011, 2012):
 Amplitudes with different orderings

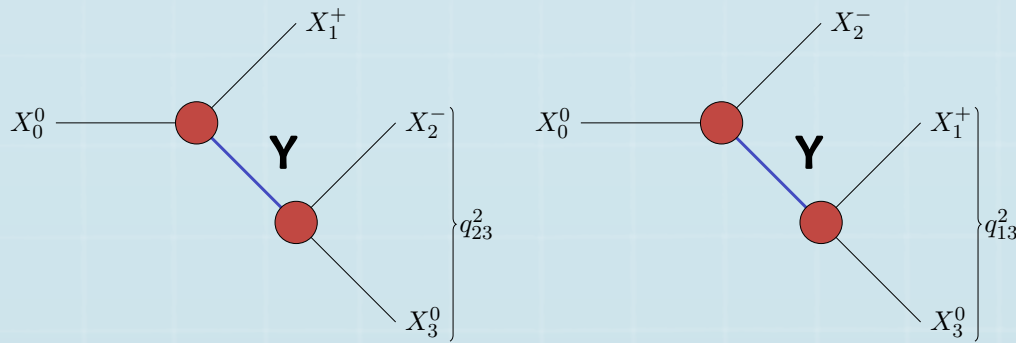


Momentum asymmetry

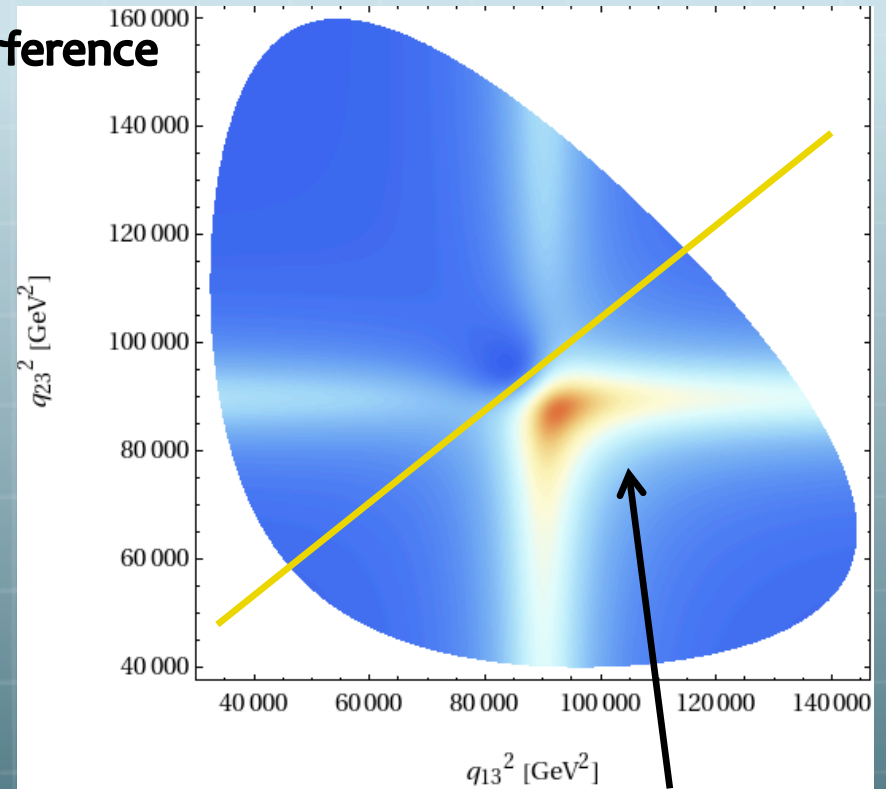
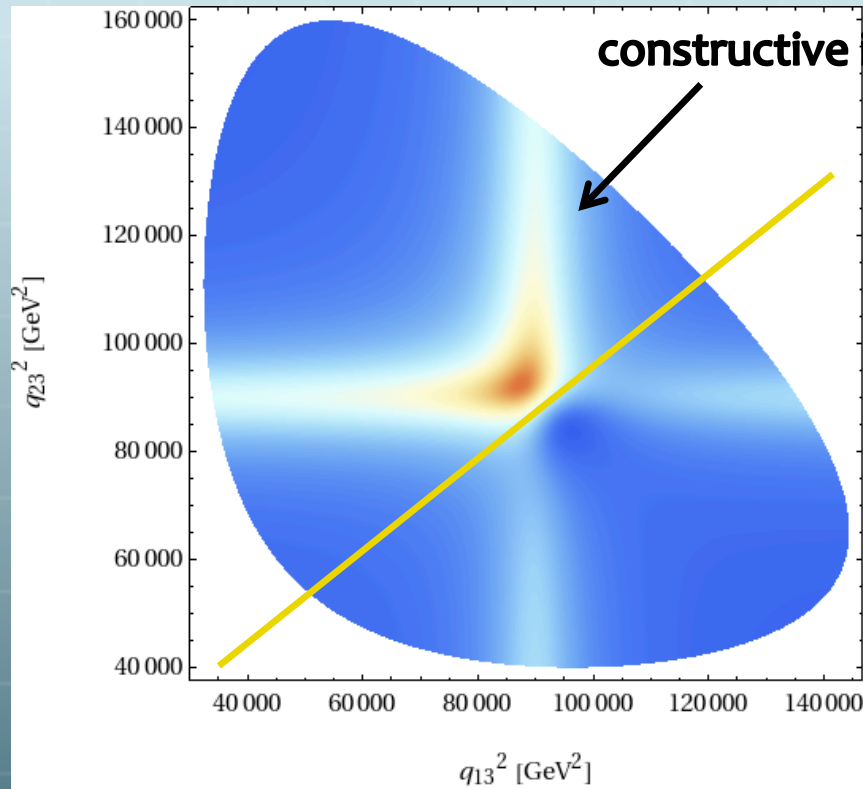
Differential asymmetry $\mathcal{A}_{\text{CP}}^{\text{diff}} = \frac{d\Gamma/dq_{13}^2 dq_{23}^2 - d\bar{\Gamma}/dq_{13}^2 dq_{23}^2}{d\Gamma/dq_{13}^2 dq_{23}^2 + d\bar{\Gamma}/dq_{13}^2 dq_{23}^2}.$

Weighted asymmetry: eliminate suppression when particles 1 and 2 are nearly degenerate

$$\mathcal{A}_{\text{CP}}^{\text{PS wgt}} = \frac{\left(N(q_{13}^2 > q_{23}^2) - N(q_{13}^2 < q_{23}^2) \right) - \left(\bar{N}(q_{13}^2 > q_{23}^2) - \bar{N}(q_{13}^2 < q_{23}^2) \right)}{N + \bar{N}},$$



Dalitz plots for the differential rates of CP conjugate processes

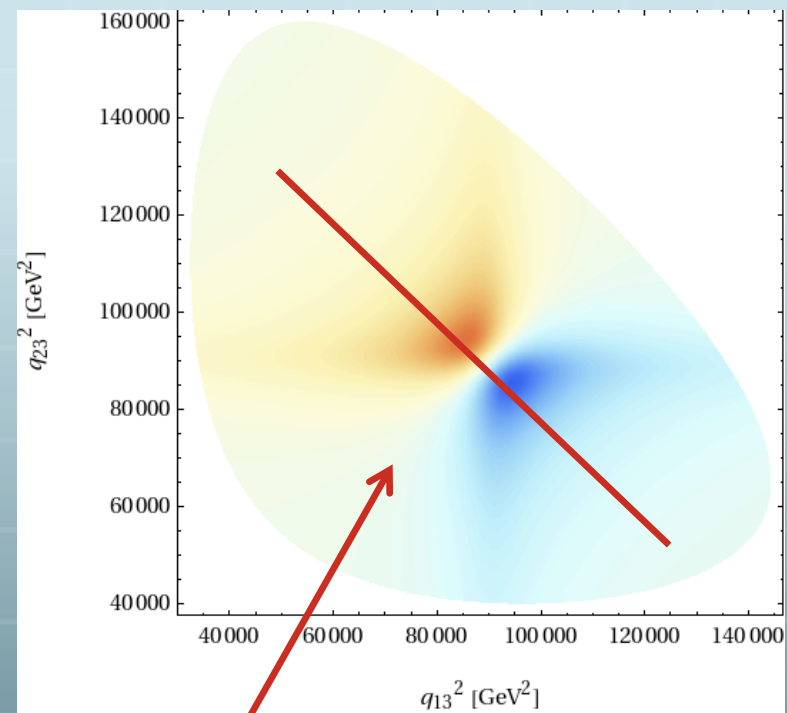
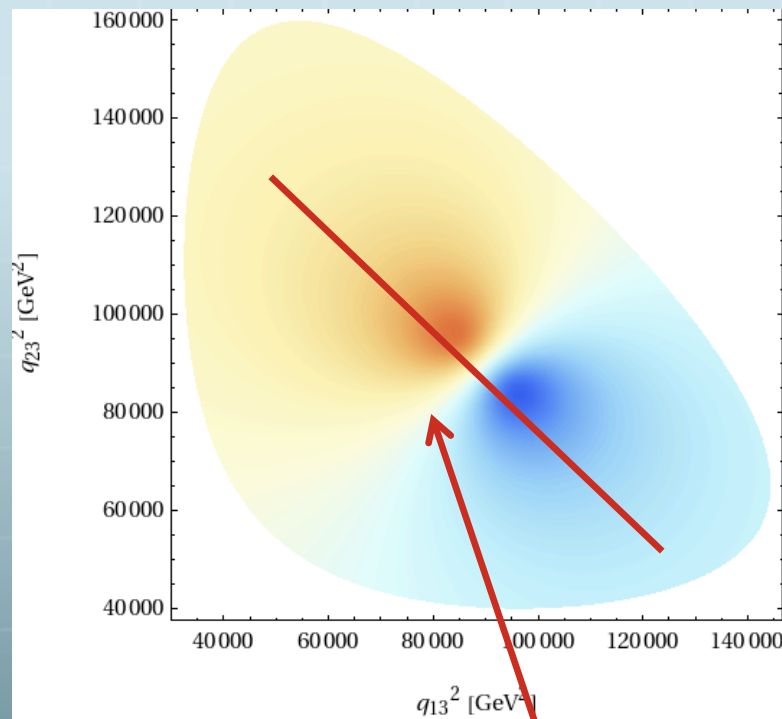


constructive interference

Asymmetry and differential asymmetry

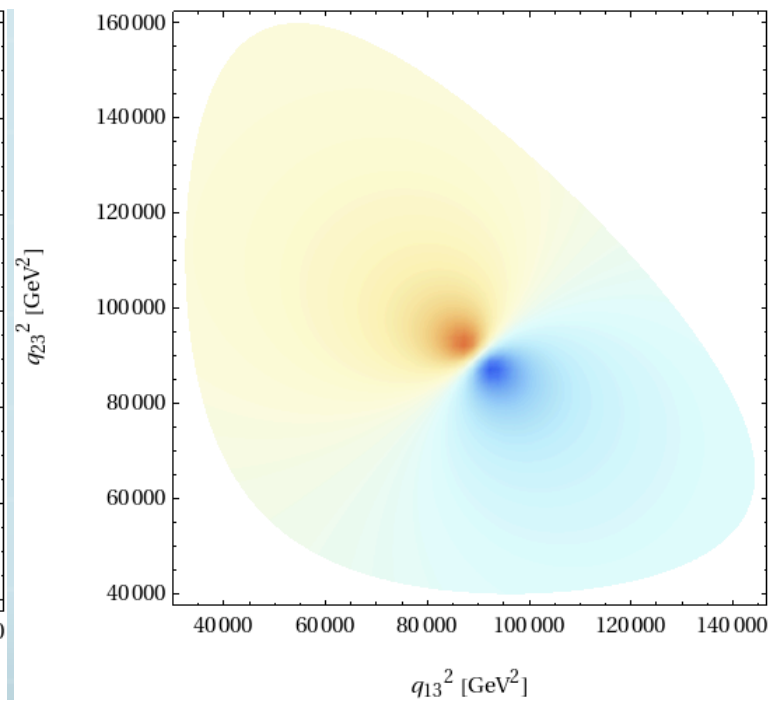
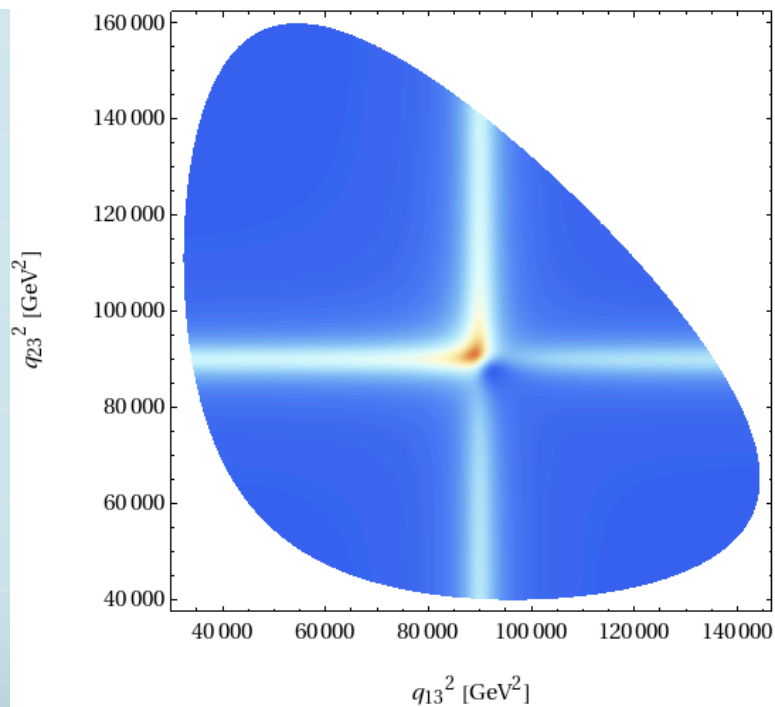
$$\mathcal{A}_{\text{CP}} = \frac{\Gamma(M \rightarrow f) - \Gamma(\bar{M} \rightarrow \bar{f})}{\Gamma(M \rightarrow f) + \Gamma(\bar{M} \rightarrow \bar{f})}.$$

$$\mathcal{A}_{\text{CP}}^{\text{diff}} = \frac{d\Gamma/dq_{13}^2 dq_{23}^2 - d\bar{\Gamma}/dq_{13}^2 dq_{23}^2}{d\Gamma/dq_{13}^2 dq_{23}^2 + d\bar{\Gamma}/dq_{13}^2 dq_{23}^2}.$$

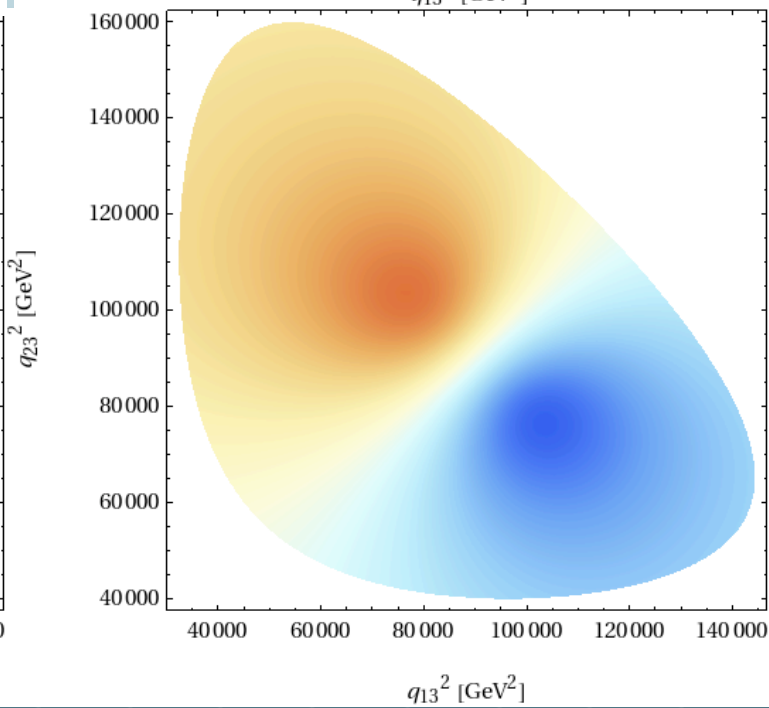
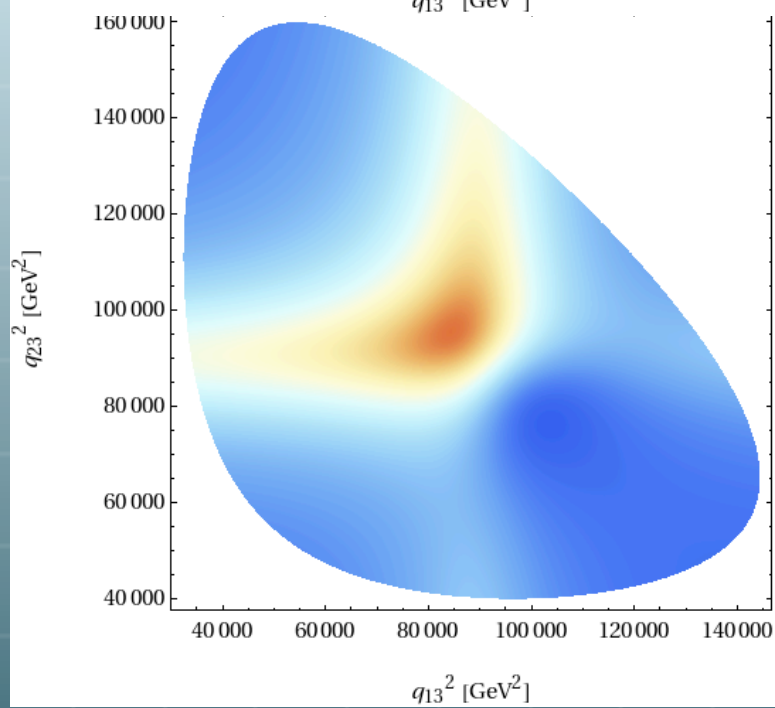


$$q_{13}^2 + q_{23}^2 = 2m_Y^2$$

$$\frac{\Gamma_Y}{m_Y} = 0.03$$



$$\frac{\Gamma_Y}{m_Y} = 0.15$$



Main problems:

- a. kinematics information is not all available, in particular, events with large boost and/or missing energy;

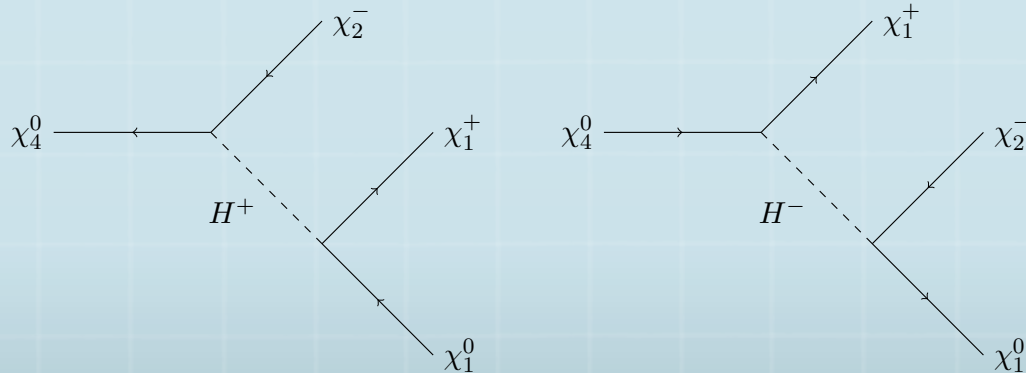
solution: p_T asymmetries;
$$\mathcal{A}_{\text{CP}}^{p_T} = \frac{N(p_{T,-} > p_{T,+}) - N(p_{T,+} > p_{T,-})}{N} .$$

- b. Energy smearing if the detector resolution is not sufficient to probe the width of the resonance;
- c. Combinatorics: cannot correctly determine which particles came from the same mother particle; calculate observables using all possible combinations.

Momentum asymmetries mostly useful in cases where the CP violation occurs in a three-body decay where the final state is stable and momentum cannot be measured.

Example:

$$m_{\chi_4^0} \sim M_1 \gg m_{\chi_i^0}, m_{\chi_j^\pm} \sim \sqrt{|\mu M_2|} > m_Z.$$



$$M_1 \gtrsim 3\sqrt{|\mu M_2|}.$$

$$m_{H^\pm} \gtrsim 2\sqrt{|\mu M_2|}.$$

weak phase:

$$\mu(\mu B)^* m_2$$

$$\mathcal{A}_{\text{CP}}^{\text{PS wgt}} \sim \frac{\Gamma_{H^\pm} |\mu m_2|}{m_{H^\pm} m_1^2}$$

Asymmetry is more evident with large width of charged Higgs and μ, M_2 close as possible to M_1 without cutting into phase space



Triple product asymmetries Valencia 1989; Kamionkowski 1990; Kayser 1990; Korner, Schilcher and Wu 1990

$$\epsilon_{\mu\nu\alpha\beta} p_0^\mu p_1^\nu p_2^\alpha p_3^\beta$$

In the rest frame of a decaying particle $p_0 = (M, 0, 0, 0)$

$$\mathcal{T} = -M \vec{p}_1 \cdot (\vec{p}_2 \times \vec{p}_3)$$

$$\overline{\mathcal{T}} = -M \vec{p}_1^c \cdot (\vec{p}_2^c \times \vec{p}_3^c)$$

$$\langle \mathcal{T} \rangle \sim \sin(\delta_1 - \delta_2) \cos(\phi_1 - \phi_2) + \cos(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)$$

$\langle \mathcal{T} \rangle \neq 0$: a strong phase or CP violation

One could separate the CP violating term:

$$\langle \mathcal{T} \rangle + \langle \overline{\mathcal{T}} \rangle \sim \cos(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2).$$



Triple product asymmetries Valencia 1989; Kamionkowski 1990; Kayser 1990; Korner, Schilcher and Wu 1990

$$\begin{aligned}\mathcal{T} &= -M \vec{p}_1 \cdot (\vec{p}_2 \times \vec{p}_3) \\ \overline{\mathcal{T}} &= -M \vec{p}_1^c \cdot (\vec{p}_2^c \times \vec{p}_3^c)\end{aligned}$$

$$\langle \mathcal{T} \rangle \sim \sin(\delta_1 - \delta_2) \cos(\phi_1 - \phi_2) + \cos(\delta_1 - \delta_2) \sin(\phi_1 - \phi_2)$$

$\langle \mathcal{T} \rangle \neq 0$: a strong phase or CP violation

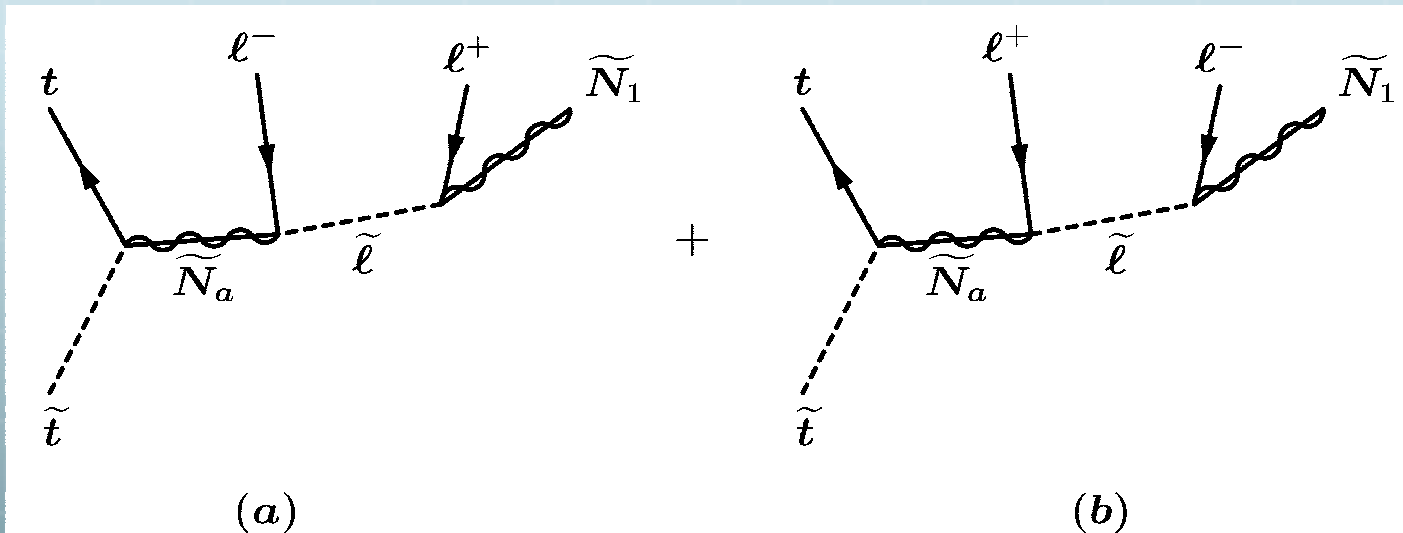
Momentum asymmetries: presence of both strong **and weak phases;**

Triple product asymmetry: either strong phase **or weak phase**



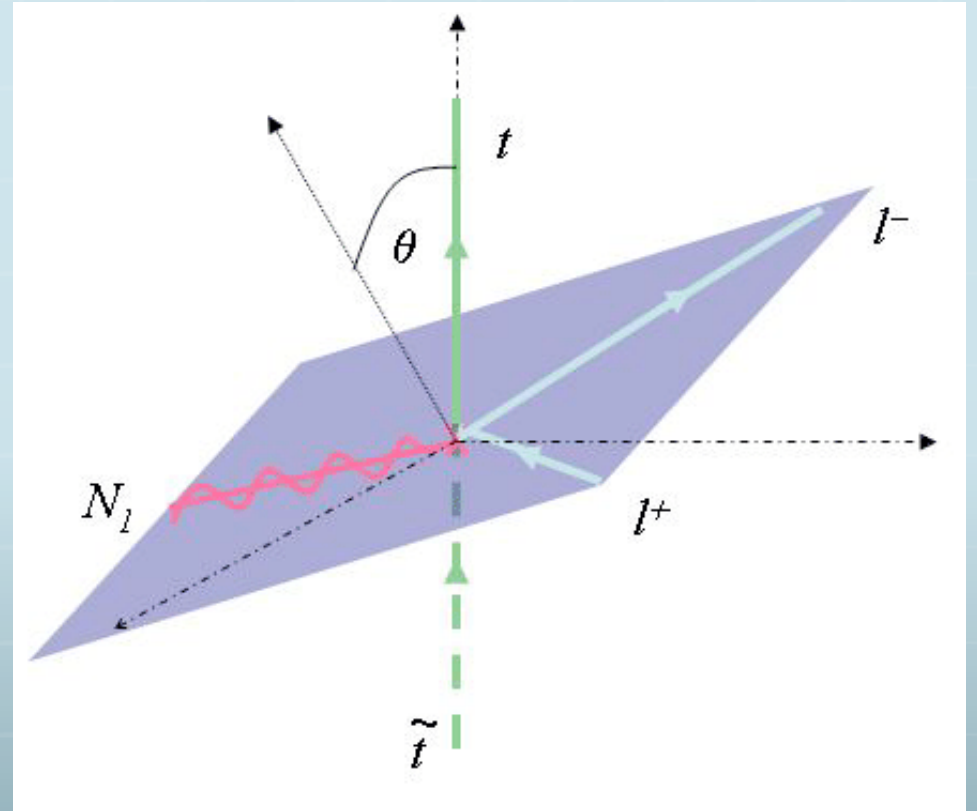
One example: Langacker, Paz, Wang and Yavin 2007; Moortgat-Pick, Rolbiecki, Tattersall and Wienemann 2009; Ellis, Moortgat, Moortgat – Pick, Smilie and Tattersall 2009, Deppisch, Kittel 2009

$$\tilde{t} \rightarrow t + \tilde{N}_a \rightarrow t + l^+ + l^- + \tilde{N}_1$$



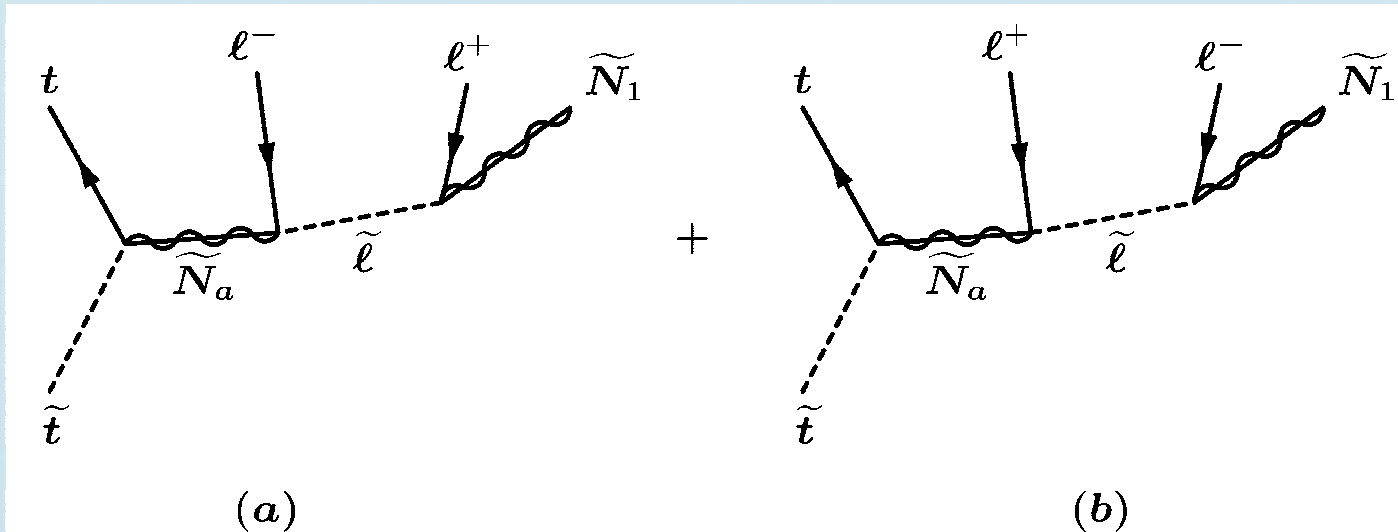
weak phase: $M_1^* M_2, A_t^* M_2$

$$\begin{aligned}\mathcal{T} &= -M_{\tilde{t}} \vec{p}_t \cdot (\vec{p}_{l+} \times \vec{p}_{l-}) \\ \overline{\mathcal{T}} &= -M_{\tilde{t}} \vec{p}_{t^c} \cdot (\vec{p}_{l-} \times \vec{p}_{l+})\end{aligned}$$



$$\eta = \frac{N_+ - N_-}{N_+ + N_-} = \frac{N_+ - N_-}{N_{total}},$$

$$N_+ = \int_0^1 \frac{d\Gamma}{d \cos \theta} d \cos \theta, \quad N_- = \int_{-1}^0 \frac{d\Gamma}{d \cos \theta} d \cos \theta$$



Amount of asymmetry depends on the spectrum. Here consider two limits:

a. \tilde{N}_a : wino; \tilde{N}_1 : bino, $M_{\tilde{l}}^2 < M_{\tilde{N}_a}^2$

$$\begin{aligned}
 \langle \epsilon_{\mu\nu\alpha\beta} p_t^\mu p_t^\nu p_{l^+}^\alpha p_{l^-}^\beta \rangle &= \frac{1}{24} M_{\tilde{t}}^2 M_{\tilde{N}_a}^2 \left(\frac{1}{\pi} \frac{\Gamma_{\tilde{l}}}{M_{\tilde{l}}} \right) \sqrt{\mu_1} \int dx_+ dx_- f(x_+, x_-) \\
 &\times \sin(2\varphi_L^{l1} - 2\varphi_L^{la})
 \end{aligned}$$

Weak phase: $M_1 * M_2$

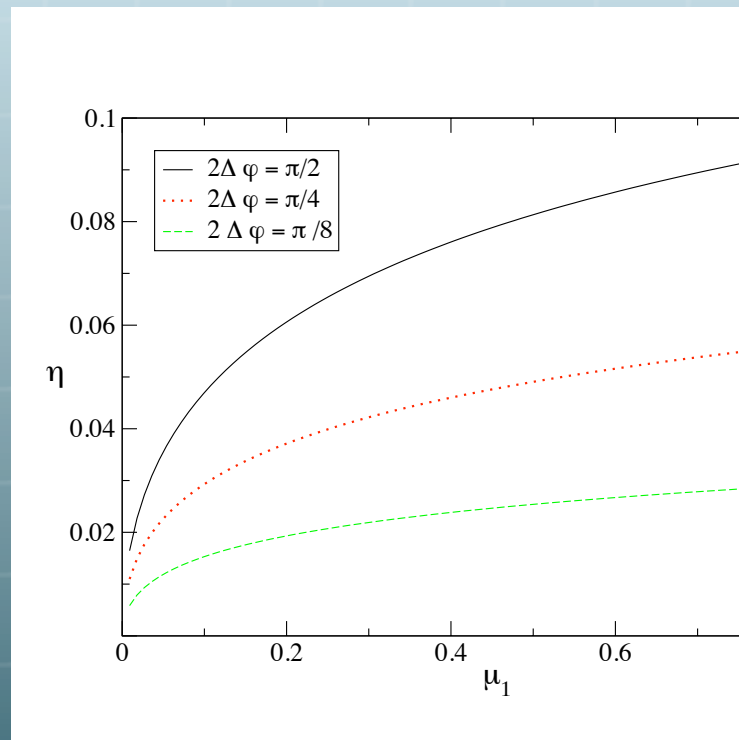
Suppression from width of slepton
 $\sim 1/300$

Asymmetry comes from the ratio of an off-shell process to an on-shell one;
when both processes are on-shell, no interferences!

b. \tilde{N}_a : wino; \tilde{N}_1 : bino, $M_{\tilde{l}}^2 \gg M_{\tilde{N}_a}^2$


$$\eta = \frac{\sqrt{\mu_1}}{2} \left(\frac{F(\mu_1)}{G_1(\mu_1) + G_2(\mu_1) \cos(2\Delta\varphi)} \right) \sin(2\Delta\varphi)$$

$$\mu_1 = \frac{M_{\tilde{N}_1}^2}{M_{\tilde{N}_a}^2} \quad \eta \text{ is an } \mathcal{O}(0.1) \text{ number for decays through off-shell sleptons!}$$



Ignoring experimental limitations, assuming Gaussian statistics, the number of events needed

$$N \sim \frac{100}{\sin^2(2\Delta\varphi)}$$


 $\sim \text{Arg} (M_1^* M_2)$

$$g_L^{la} = |g_L^{la}| \exp(i\varphi_L^{la})$$

$$\Delta\varphi = \varphi_L^{l1} - \varphi_L^{la}$$

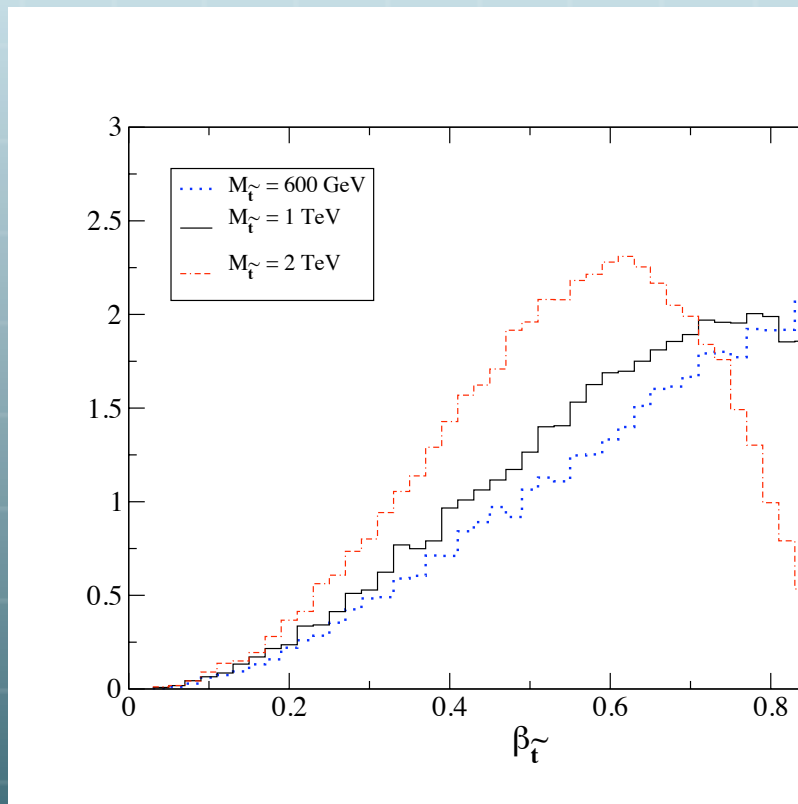
$M_{\tilde{t}_L}$	σ (fb)	$N[t\ell^+\ell^-]$ $\mathcal{L} = 300\text{fb}^{-1}$ (1 ab^{-1})
500 GeV	300	7300 (24000)
800 GeV	20	560 (1800)
1 TeV	4	120 (400)
1.2 TeV	1	30 (100)

Table 1. The production cross-section for $\tilde{t}_L \tilde{t}_L^c$ is shown in the middle column. The branching ratio for the reaction $\tilde{t} \rightarrow t + \tilde{N}_a \rightarrow t + l^+ + l^- + \tilde{N}_1$ was calculated using $M_{\tilde{t}} = 300$ GeV, $M_{\tilde{N}_2} = 140$ GeV, $M_{\tilde{N}_1} = 100$ GeV, and assuming that the gluino and squarks are sufficiently heavy to have little effect. (Under these assumptions and wino/bino dominated $\tilde{N}_{2,1}$ the branching ratio for $\tilde{t} \rightarrow t \tilde{N}_2$ is slightly less than 1/3 because of the top's mass, and those for $\tilde{N}_2 \rightarrow e^+ e^- \tilde{N}_1$ or $\mu^+ \mu^- \tilde{N}_1$ are about 1/6 each.)

Experimental limitations:

a. Impossible to reconstruct the rest frame of the decaying particle due to the missing energy;

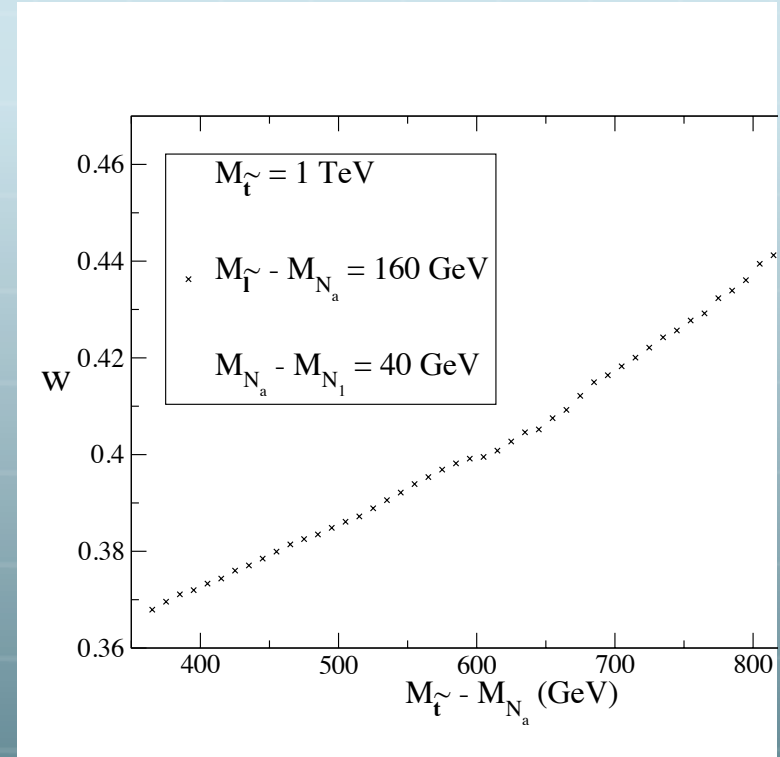
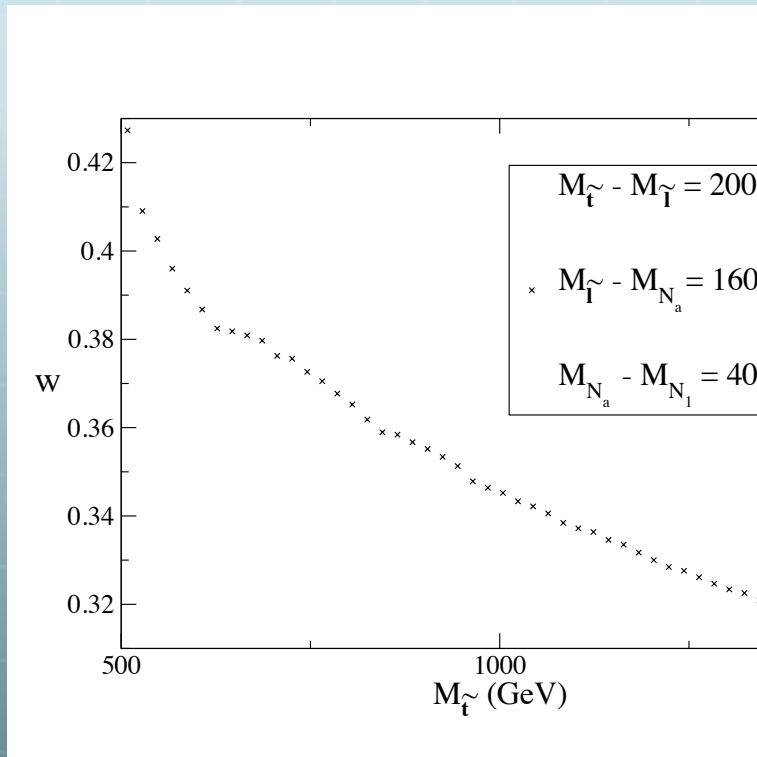
The decaying particles are produced very close to the threshold; thus could flip the sign of p_t or change the transverse orientation of the leptons



$$\eta_{lab} = \frac{N_+^{(lab)} - N_-^{(lab)}}{N_+^{(lab)} + N_-^{(lab)}} = \mathcal{D} \left(\frac{N_+^{(\tilde{N})} - N_-^{(\tilde{N})}}{N_+^{(\tilde{N})} + N_-^{(\tilde{N})}} \right)$$

$\mathcal{D} = 1 - 2w$

 \uparrow
Dilution factor



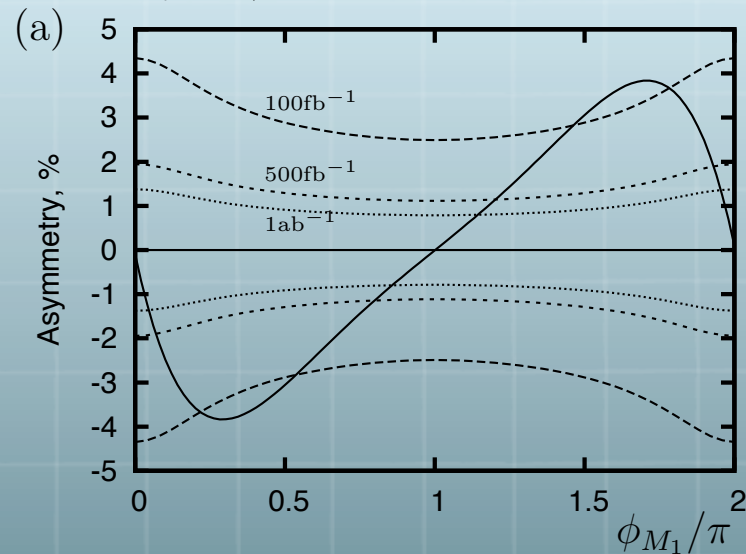
fix $M_{\tilde{t}} - M_{\tilde{N}_a}$ $M_{\tilde{t}} \uparrow w \downarrow D \uparrow$ fix $M_{\tilde{t}}$ $M_{\tilde{t}} - M_{\tilde{N}_a} \downarrow w \downarrow D \uparrow$

Other observables: $\mathcal{T}_b \sim \vec{p}_b \cdot (\vec{p}_{l+} \times \vec{p}_{l-})$

$$\mathcal{T}_{tb} \sim \vec{p}_b \cdot (\vec{p}_t \times \vec{p}_{l\pm})$$

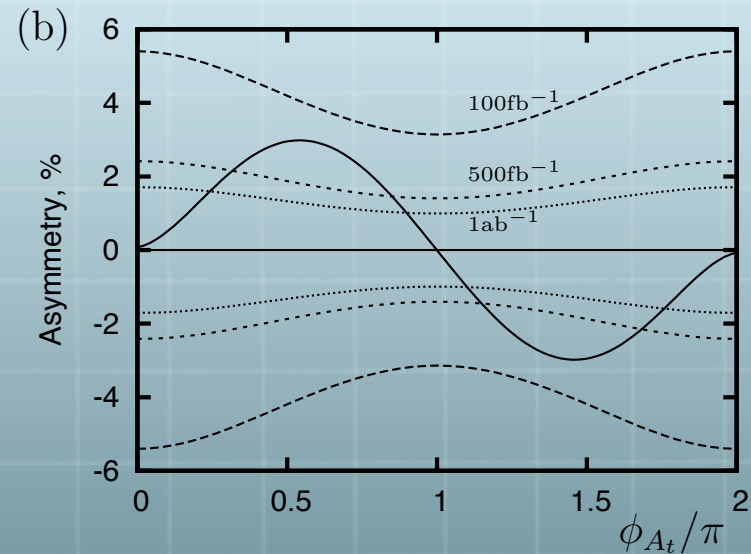
Include PDF (MRST 2004LO), Ellis, Moortgat, Moortgat – Pick, Smilie and Tattersall 2009

$\mathcal{A}_{\mathcal{T}_t}$, Scenario A ($M_1 = 130$ GeV,
 $\phi_{A_t} = 0$), $\sqrt{\hat{s}} = 14$ TeV



$$m_{\tilde{t}_1} = 396.5 \text{ GeV}, m_{\tilde{t}_2} = 595 \text{ GeV}$$

$\mathcal{A}_{\mathcal{T}_{tb}}$, Scenario A ($\phi_{M_1} = 0$), $\sqrt{\hat{s}} = 14$ TeV



A measurement of an asymmetry with an accuracy of a few % might be possible with 100 fb⁻¹ data

- b. Efficiency of identifying the top or anti-top, determining its charge and momentum, combinatorics (which pair of leptons come from top or anti-top)....**
- c. Strong phase contribution: electromagnetic interaction among leptons in the final state, of order $O(\alpha/\pi)$; finite width of sleptons, negligible for the more interesting off-shell slepton case.**

CP-odd triple gauge couplings

Dim-6 operators contributing to CP-odd TGCs also contribute to EDMs;
EDM constraints are much stronger than constraints from CP-odd TGCs without tuning

Collider study: Han and Li 2009;

$$pp \rightarrow W^+ W^- \rightarrow l^+ l^- \nu \bar{\nu}$$

$$\Phi \equiv \text{sgn}((\vec{\ell}^+ - \vec{\ell}^-) \cdot \hat{z}) \sin^{-1}(\hat{\ell}^+ \times \hat{\ell}^-) \cdot \hat{z},$$

$$\mathcal{A}_\Phi \equiv \frac{N_{\Phi>0} - N_{\Phi<0}}{N_{\Phi>0} + N_{\Phi<0}},$$

With 100 fb⁻¹ data at 14 TeV LHC, one could see ~ 5 σ signal if the CP-odd couplings ~ 0.1

Conclusions

- **EDM impose strong constraints on SUSY CP phases**
- **Still with tuning, one could still hope to explore CP violation directly at the colliders**
- **Quite a few challenges for measuring CP violating observables at the colliders: requires more theoretical and experimental inputs !**