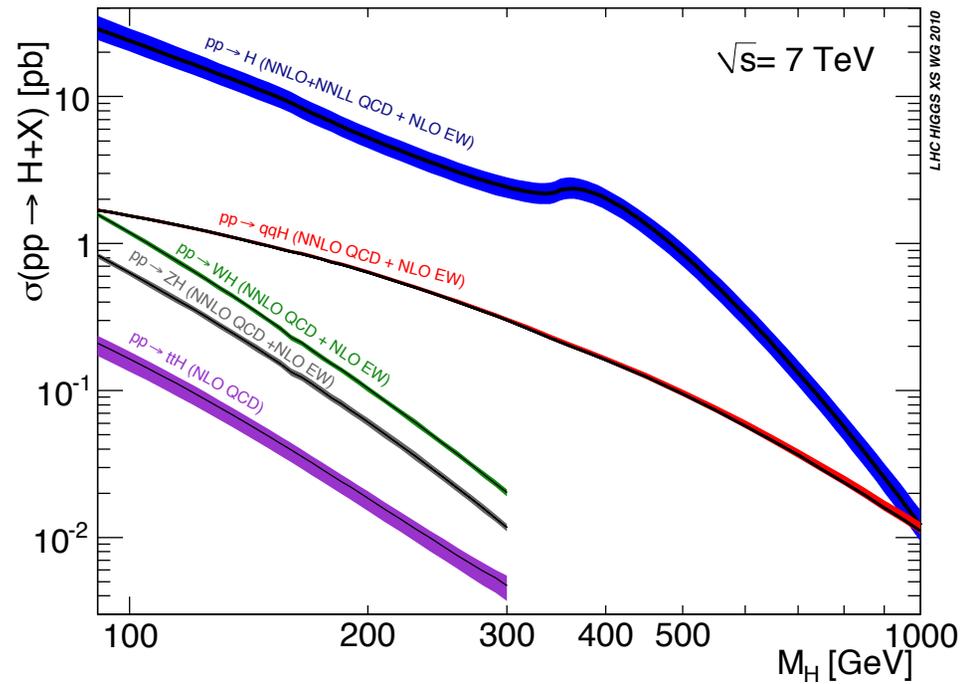


New Era of Higgs Physics  
S. Dawson  
Lecture 3, Fermilab 2012

- Vector Boson Fusion and Higgs-strahlung
- Characterize this Higgs-like object
  - What are its couplings? (remember in SM no freedom to adjust these)
  - What are the spin/parity properties?
  - Theoretical issues with the Higgs mechanism

The decade of precision Higgs physics

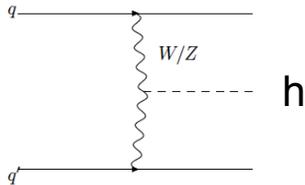
# Higgs at the LHC



$M_h = 125 \text{ GeV}$ ,  $\sigma(gg \rightarrow H)$  at 7 TeV: 15.3 pb  
at 8 TeV: 19.5 pb  
at 14 TeV: 49.9 pb

# Vector Boson Fusion

- Sensitive to VVh couplings
- Remember:
  - $g_{WWH} = gM_W = 2M_W^2/v$ ,  $g_{ZZH} = gM_Z/\cos\theta_W = 2M_Z^2/v$
- Interaction vanishes if  $v=0$  (not true for fermion Higgs Yukawa couplings!)



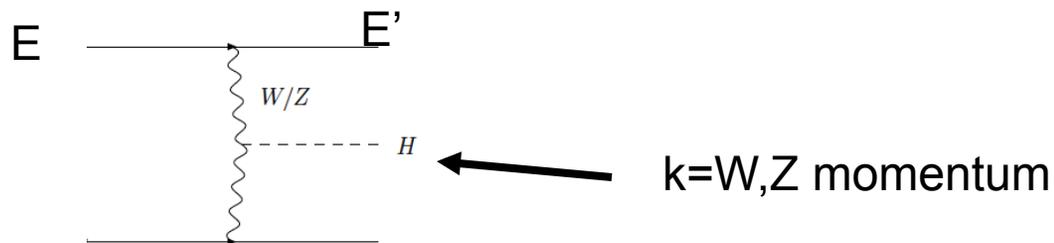
*Changing ratio of  $g_{WWH}/g_{ZZH}$  implies isospin violation... must be small variation from SM*

## Vector Boson Fusion

- $W^+W^- \rightarrow X$  is a real process:  $\sigma_{pp \rightarrow WW \rightarrow X}(s) = \int dz \frac{dL}{dz} \Big|_{pp/WW} \hat{\sigma}_{WW \rightarrow X}(zs)$
- Rate increases at large  $s$ :  $\sigma \approx (1/M_W^2) \log(s/M_W^2)$
- Integral of cross section over final state phase space has contribution from  $W$  boson propagator:

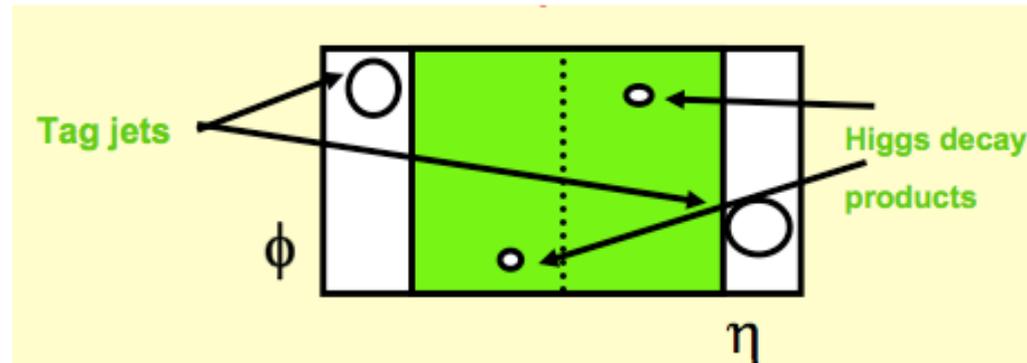
$$\int \frac{d\theta}{(k^2 - M_W^2)^2} \approx \int \frac{d\theta}{(2EE'(1 - \cos\theta) + M_W^2)^2} \quad \boxed{\text{Peaks at small } \theta}$$

- Outgoing jets are mostly forward and can be tagged



# Vector Boson Fusion

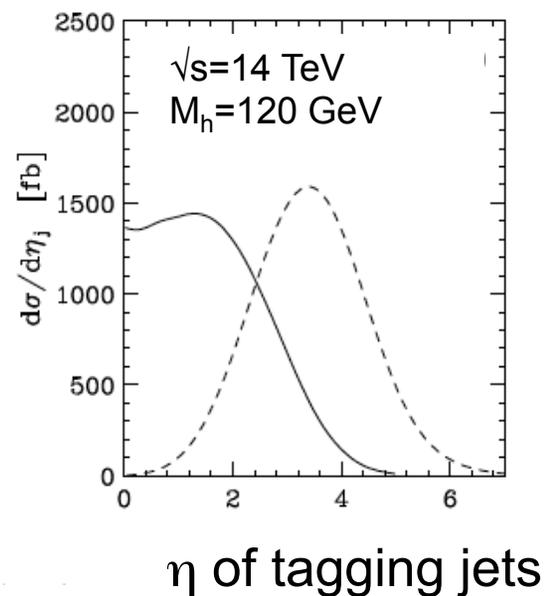
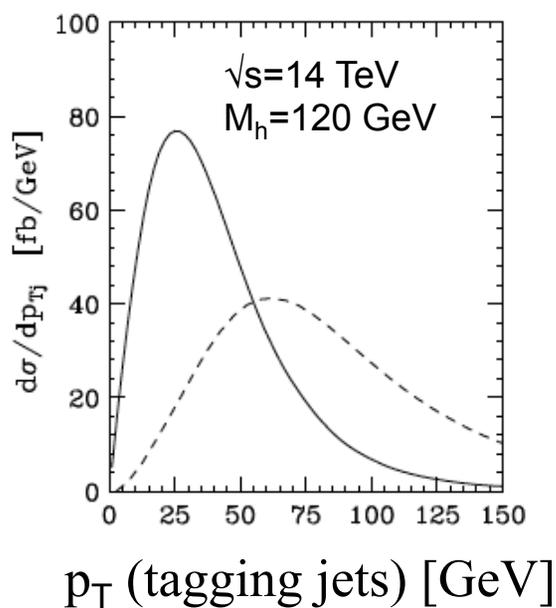
- Idea: Tag 2 high-mass jets with large rapidity gap in between
- No color flow between tagged jets – suppressed hadronic activity in central region



# Distinctive Distributions in VBF

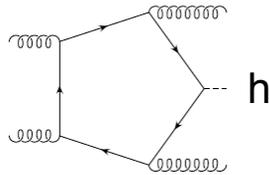
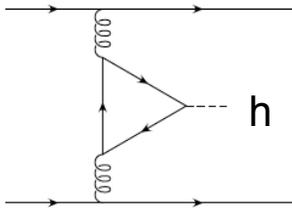
- Higgs decay products are central
- Tagging jets are forward with large energy, small  $p_T$  and produced at small angle

$$\eta = \frac{1}{2} \log \left( \frac{1 + \cos \theta}{1 - \cos \theta} \right)$$



# Is VBF a different process from gluon fusion?

- Can we separate VBF from gluon fusion?
  - Would like to do this for coupling measurements

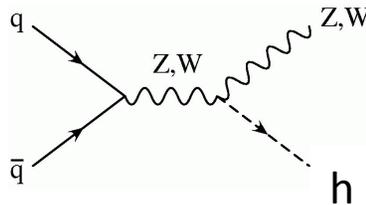


Both part of higher order contribution to Higgs plus 2 jet production

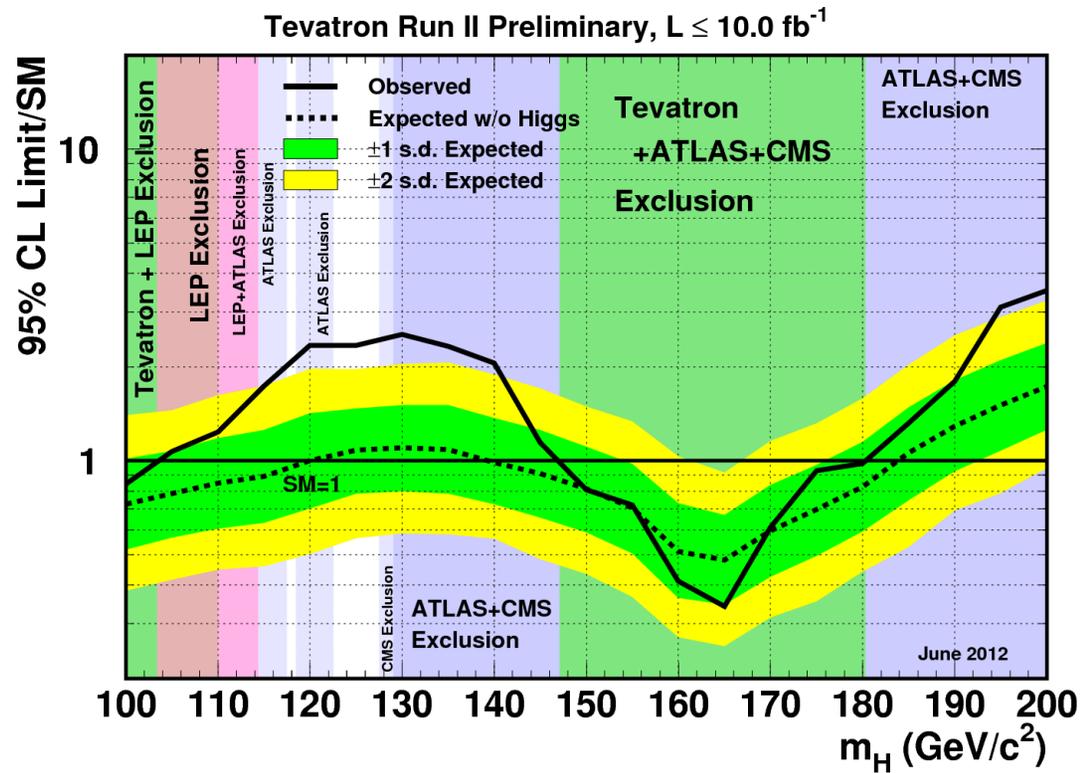
Cuts can effectively isolate VBF like diagrams from gluon fusion contributions

## W(Z)-strahlung

- W(Z)-strahlung ( $q\bar{q} \rightarrow Wh, Zh$ ) important at Tevatron
  - Same couplings as vector boson fusion
  - Rate proportional to **weak** coupling
- Theoretically very clean channel
  - Important at the Tevatron
  - Can be used for high  $p_T$  Higgs at the LHC



# CDF & D0 Searches

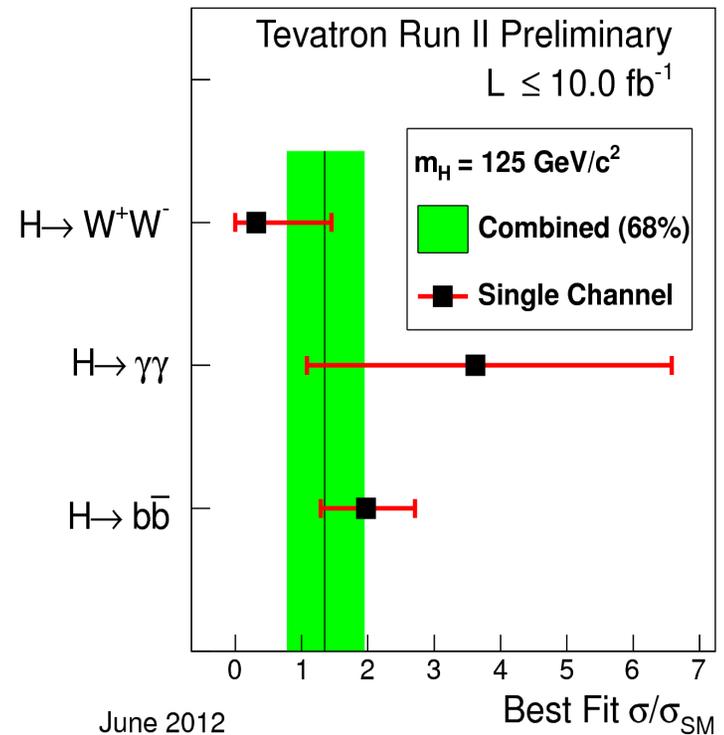


Excess at low Higgs mass in  $h \rightarrow bb$  channel  $3.3\sigma$

# Tevatron Higgs Search

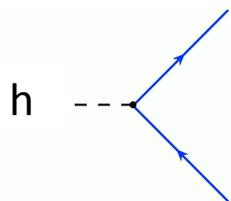
- Tevatron data are compatible with SM Higgs boson production in the mass range

$120 \text{ GeV} < M_h < 135 \text{ GeV}$   
in all studied channels



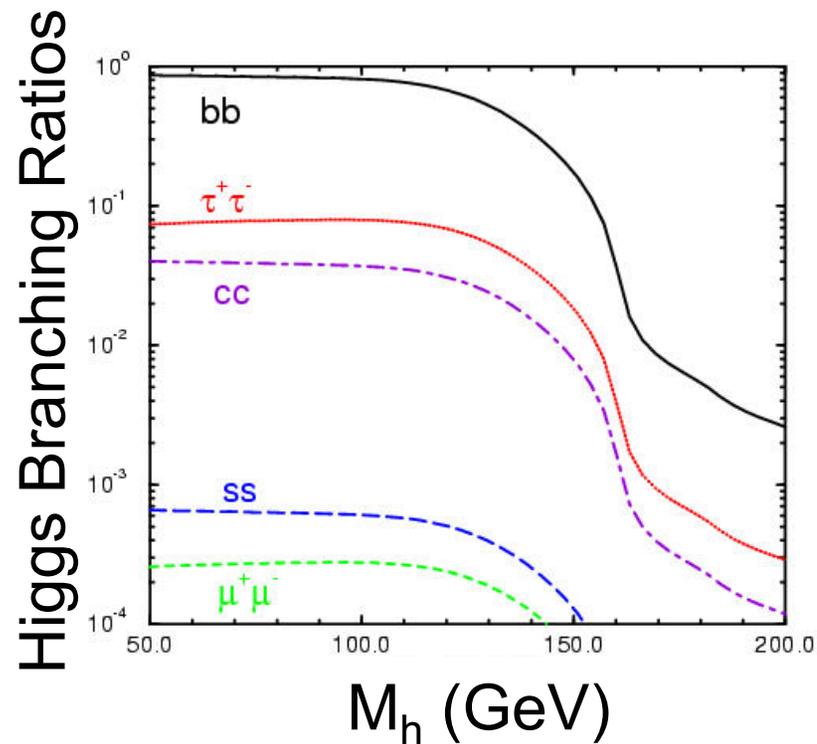
# Higgs Decays

- $h \rightarrow f\bar{f}$  proportional to  $m_f^2$



$$\frac{BR(h \rightarrow b\bar{b})}{BR(h \rightarrow \tau^+\tau^-)} \approx N_c \left( \frac{m_b^2}{m_\tau^2} \right)$$

$$\Gamma_{ff} = N_c \frac{G_F}{4\sqrt{2}\pi} M_H m_f^2 \left( 1 - \frac{4m_f^2}{M_H^2} \right)^{3/2}$$

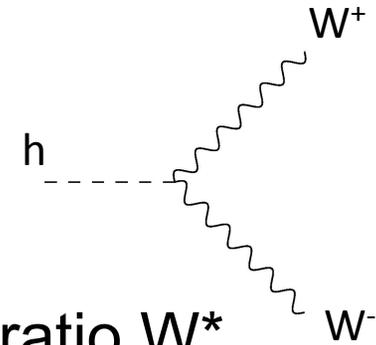


For  $M_h < 2M_W$ , decays to  $b\bar{b}$  most important

# Higgs Decays to W/Z

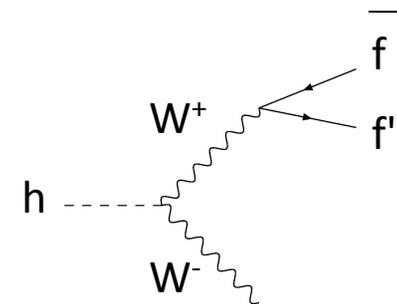
- Tree level decay

$$\Gamma(h \rightarrow W^+W^-) = \frac{\alpha}{16s_W^2} \frac{M_h^3}{M_W^2} \sqrt{1-x_W} \left( 1-x_W + \frac{3}{4}x_W^2 \right) \quad x_W = 4 \frac{M_W^2}{M_h^2}$$



- Below threshold,  $h \rightarrow WW^*$  with branching ratio  $W^* \rightarrow ff'$  implied
- Final state has both transverse and longitudinal polarizations

Below threshold rates become quite small:  $BR(h \rightarrow ZZ \rightarrow 4 \text{ leptons}) = 2 \times 10^{-4}$



## Higgs decays to VV

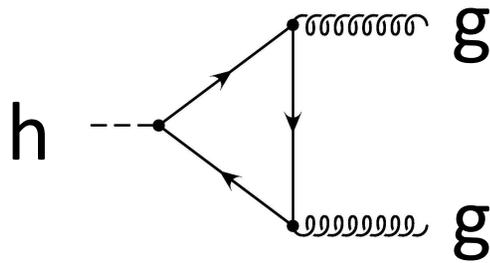
- $\Gamma_{VV} \sim M_H^3$  comes from longitudinal gauge modes

$$A(h \rightarrow W_L^+ W_L^-) = \frac{2M_W^2}{v} \epsilon_L^+ \cdot \epsilon_L^- \quad \epsilon_L \sim \frac{p_W}{M_W}$$
$$A(h \rightarrow W_L^+ W_L^-) \sim -\frac{M_H^2}{v}$$

$$\boxed{\Gamma_{WW} \rightarrow \frac{G_F M_H^3}{8\pi\sqrt{2}}}$$

*Heavy Higgs is very broad*

# Higgs Decays to Gluons



- Top quark contribution most important
- Doesn't decouple for large  $m_t$

• *Decoupling theorem doesn't apply to particles which couple to mass (ie Higgs!)*

- Decay sensitive to extra generations

$$\Gamma(h \rightarrow gg) \approx \frac{\alpha_s^2 \alpha}{72\pi^2 s_W^2} \frac{M_h^3}{M_W^2} + O\left(\frac{M_h^2}{M_t^2}\right)$$

# Higgs Decays to Photons

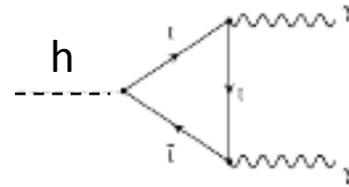
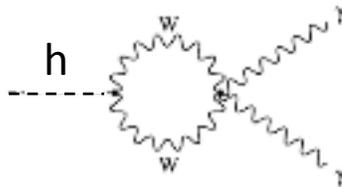
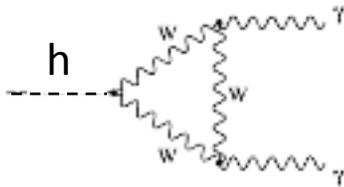
- Dominant contribution is W loops
- Contribution from top is small

*Note opposite signs of t/W loops*

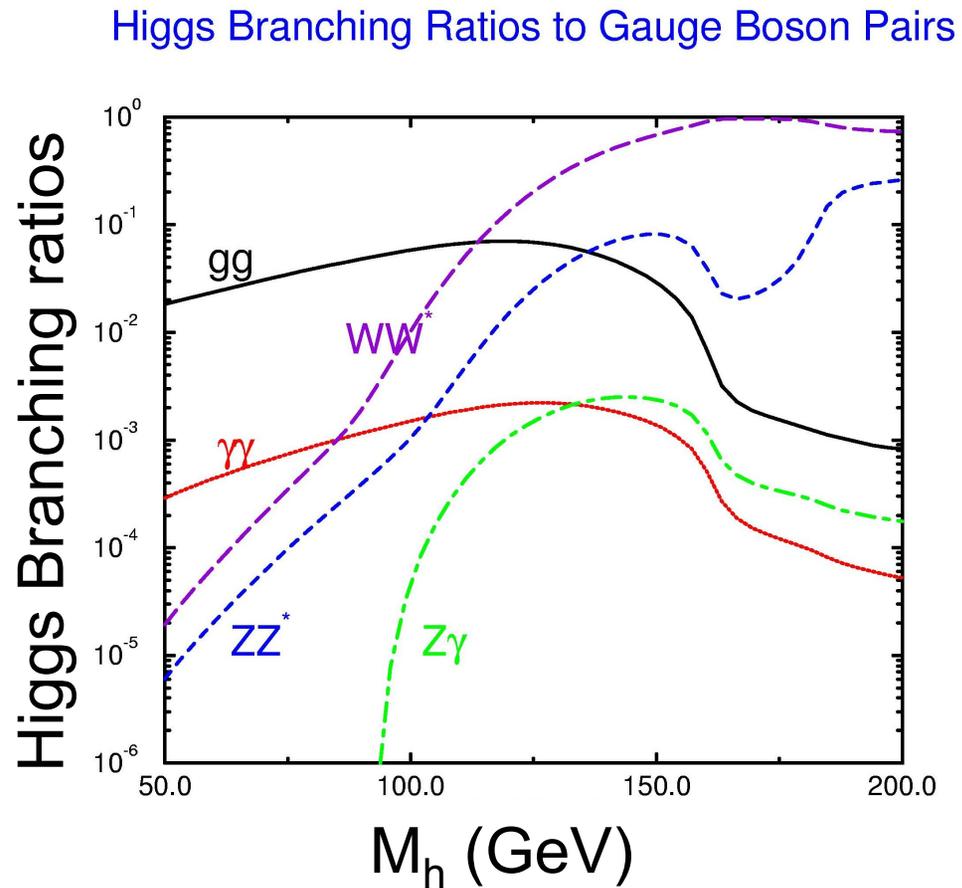
$$\Gamma(h \rightarrow \gamma\gamma) \approx \frac{\alpha^3}{256\pi^2 s_W^2} \frac{M_h^3}{M_W^2} \left| 7 - \frac{16}{9} + \dots \right|^2$$

W

top



# Higgs decays to gauge bosons

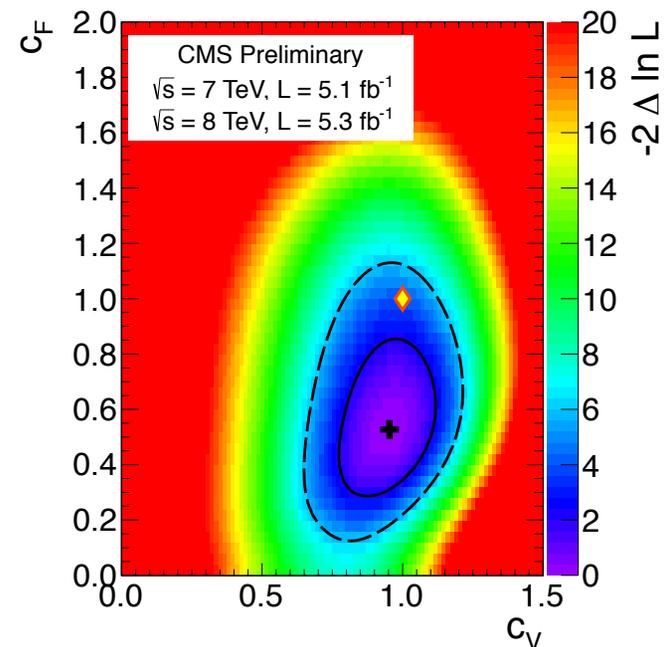


# Suppose we want to enhance $h \rightarrow \gamma\gamma$ ?

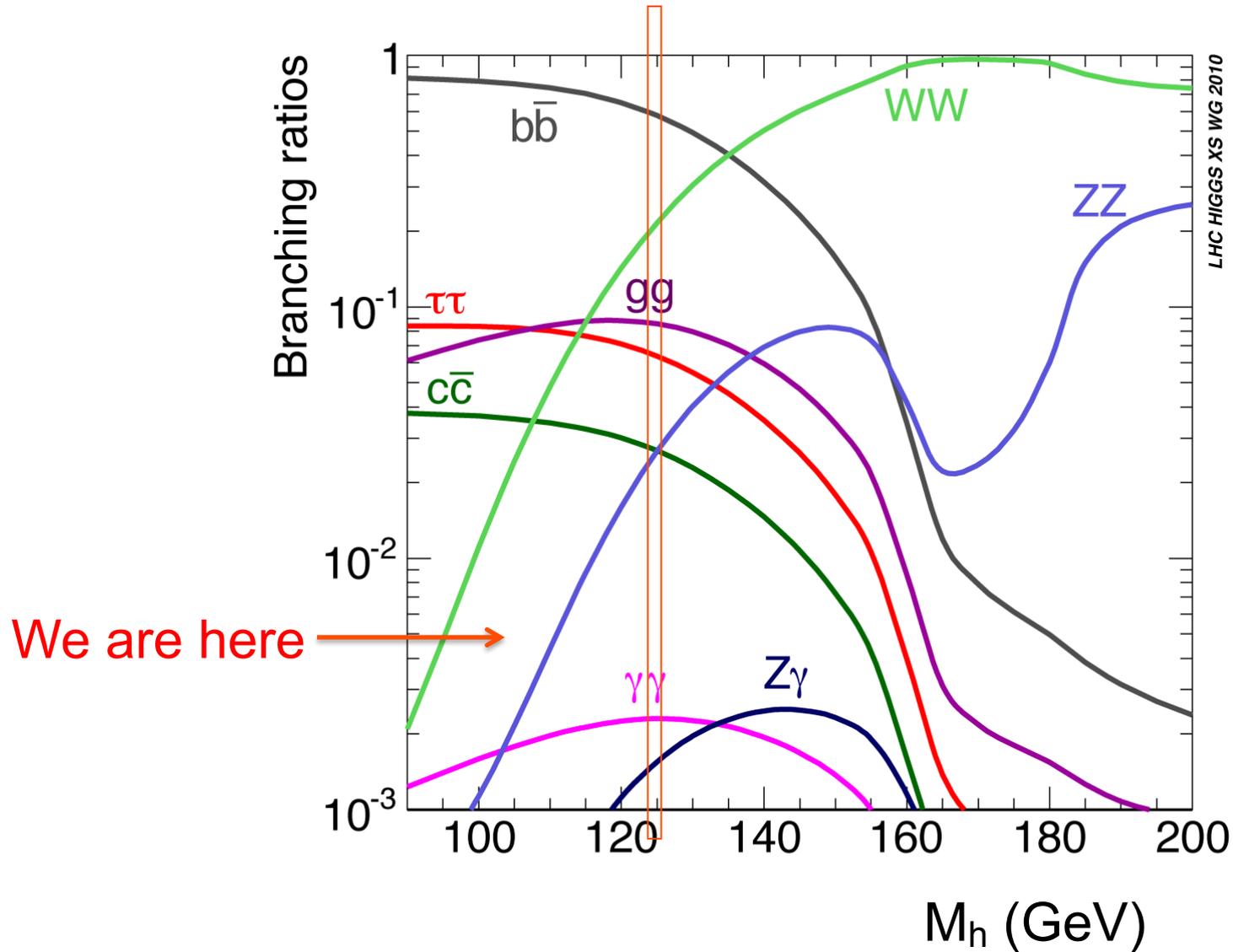
- Rescale top quark Yukawa:  $c_F \frac{m_t}{v} \bar{t} t h$
- Rescale W Yukawa:  $c_V g M_W W^{+\mu} W_{\nu}^{-} h$

$$\frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{SM}} \sim \left(1 - .2 \frac{c_F}{c_V}\right)^2$$

- Or put something (without color) in loop to enhance rate...popular theorist's sport



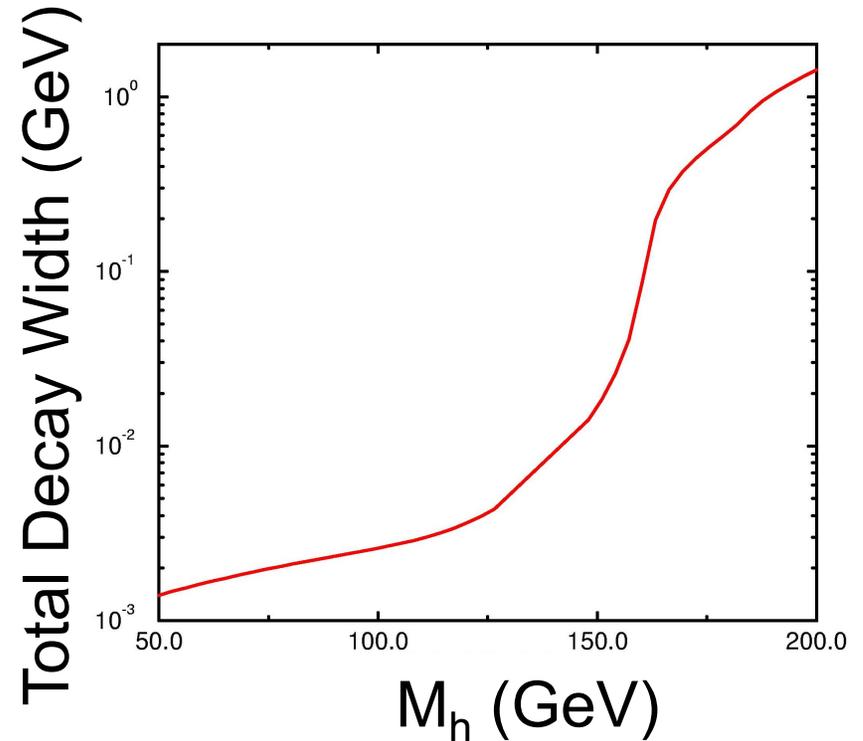
# Higgs Branching Ratios



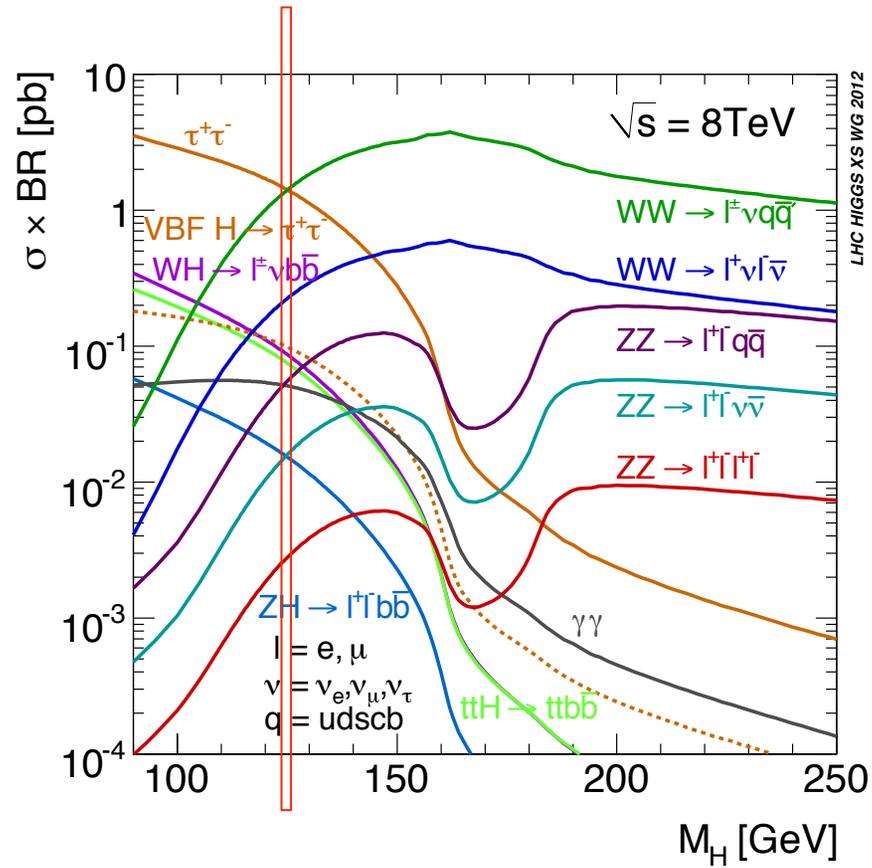
# Total Higgs Width

- Small  $M_h$ , Higgs is narrower than detector resolution
- As  $M_h$  becomes large, width also increases
  - No clear resonance
  - For  $M_h \sim 1.4$  TeV,  
 $\Gamma_{\text{tot}} \sim M_h$

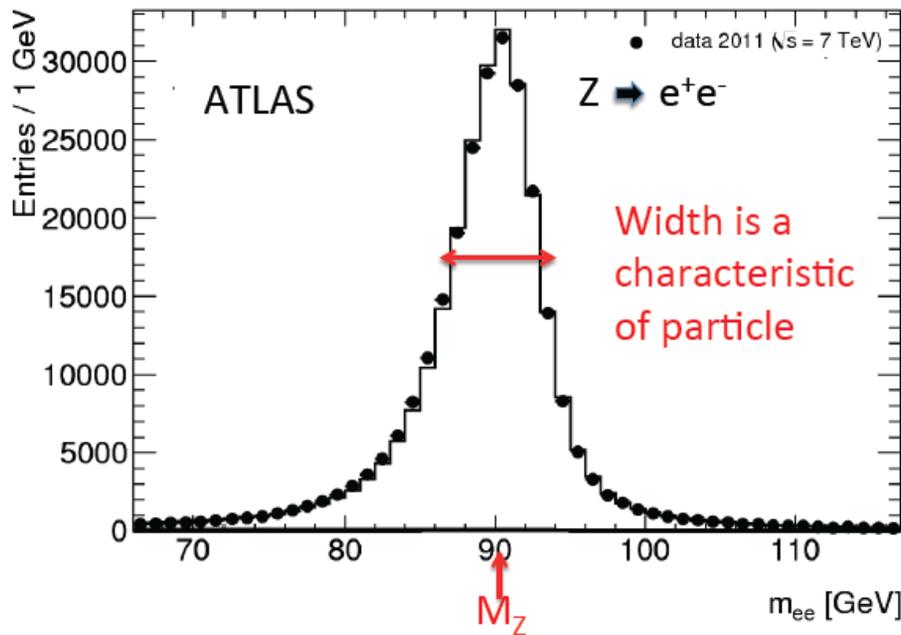
$$\Gamma(h \rightarrow W^+W^-) \approx \frac{\alpha}{16 \sin^2 \theta_w} \frac{M_h^3}{M_W^2}$$
$$\approx 330 \text{ GeV} \left( \frac{M_h}{1 \text{ TeV}} \right)^3$$



# Production + Decay



# Higgs Mass from Bump Hunting

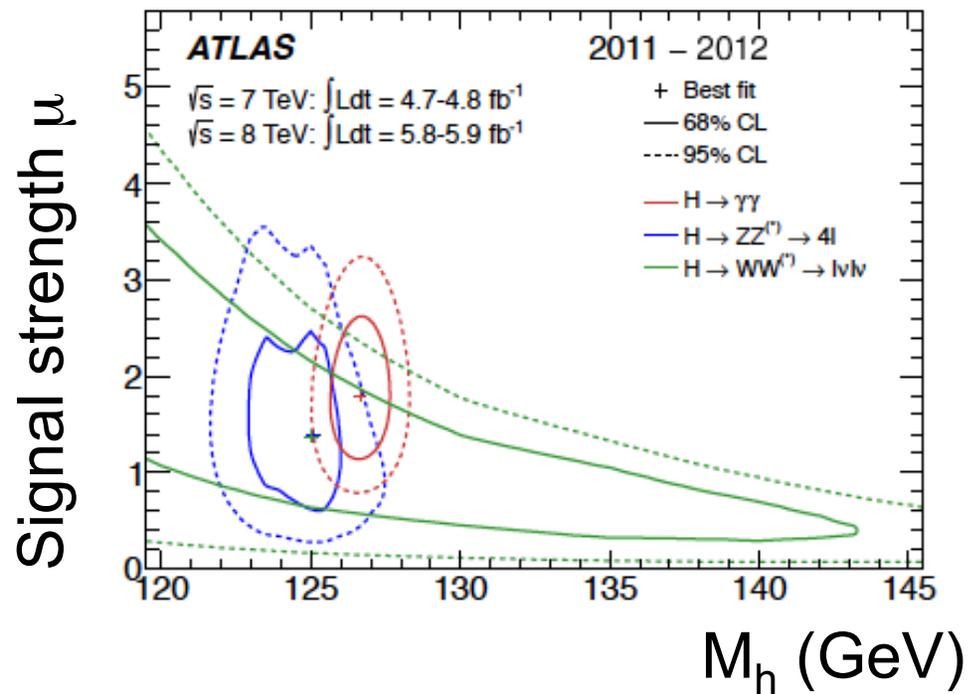


$$M^2 = (E_+ + E_-)^2 - (\vec{p}_+ + \vec{p}_-)^2$$

Use this technique for  $h \rightarrow \gamma\gamma$  and  $h \rightarrow ZZ$

$$\Gamma_h \sim \text{MeV}$$

Can't reconstruct mass in  $h \rightarrow W^+W^-$



ATLAS

$h \rightarrow W^+W^- \rightarrow l\nu l\nu$

# Is it a (*the*) Higgs?

- How do we know what we've found?
- Measure couplings to fermions & gauge bosons

$$\frac{\Gamma(h \rightarrow b\bar{b})}{\Gamma(h \rightarrow \tau^+\tau^-)} \approx 3 \frac{m_b^2}{m_\tau^2}$$

- Measure spin/parity

$$J^{PC} = 0^{++}$$

- Measure self interactions

$$V = \frac{M_h^2}{2} h^2 + \frac{M_h^2}{2v} h^3 + \frac{M_h^2}{8v^2} h^4$$

# Parameterize deviations from SM

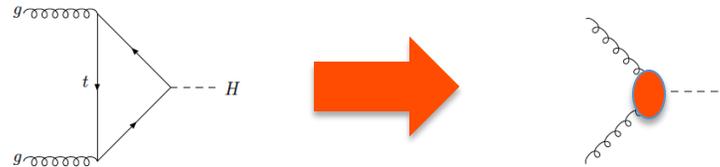
- Many possible parameterizations (only some terms shown here)

$$L \sim c_V \left( M_W^2 W_\mu^+ W^{-\mu} + \frac{M_Z^2}{2} Z_\mu Z^\mu \right) \frac{2h}{v} - c_t m_t \bar{t} t \frac{h}{v} - c_b m_b \bar{b} b \frac{h}{v} \\ + \frac{g^2}{16\pi^2} \left( F_{\mu\nu} F^{\mu\nu} c_{\gamma\gamma} + G_{\mu\nu} G^{\mu\nu} c_{gg} \right) \frac{h}{v} + \dots$$

- In Standard Model,  $c_V=c_t=c_b=1$ ,  $c_{\gamma\gamma}=c_{gg}=0$
- No FCNC in Higgs sector parameterization
- No isospin violation in Higgs sector parameterization
- Assume no new light states

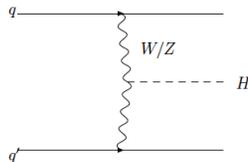
# Coupling Measurements

- Production:
  - Gluon Fusion



$$\sigma_{ggh} \sim c_t^2, c_b^2, c_{gg}$$

- VBF



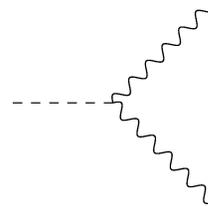
$$\sigma_{VBF} \sim c_V^2$$

# Decay

- $h \rightarrow \gamma\gamma$ :  $c_F, c_V, c_{\gamma\gamma}$

$$\frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{SM}} \sim \left(1 - .2 \frac{c_F}{c_V}\right)^2$$

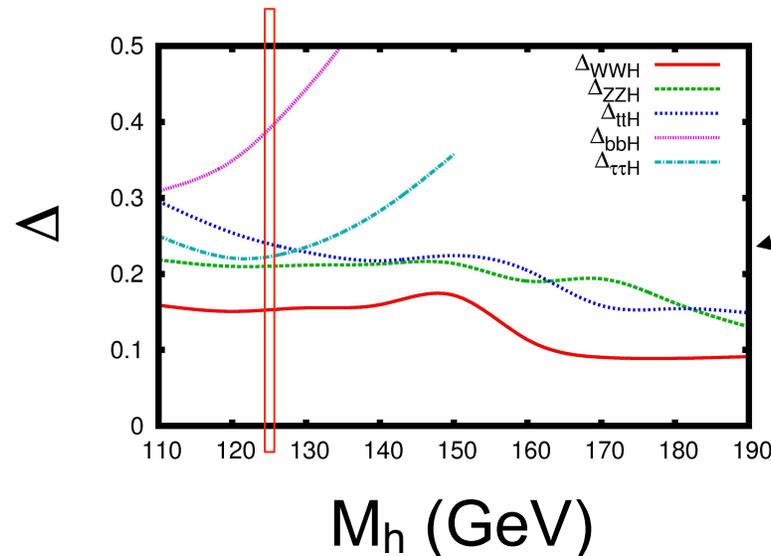
- $h \rightarrow WW, h \rightarrow ZZ$ ;  $c_V$



- $h \rightarrow bb$ :  $c_F$
- Could include decay to invisible particles
  - Desirable to explain dark matter
  - Severely restricted by current measurements

# Measuring Higgs Couplings

- SM coupling measurements with  $30 \text{ fb}^{-1}$  at 14 TeV



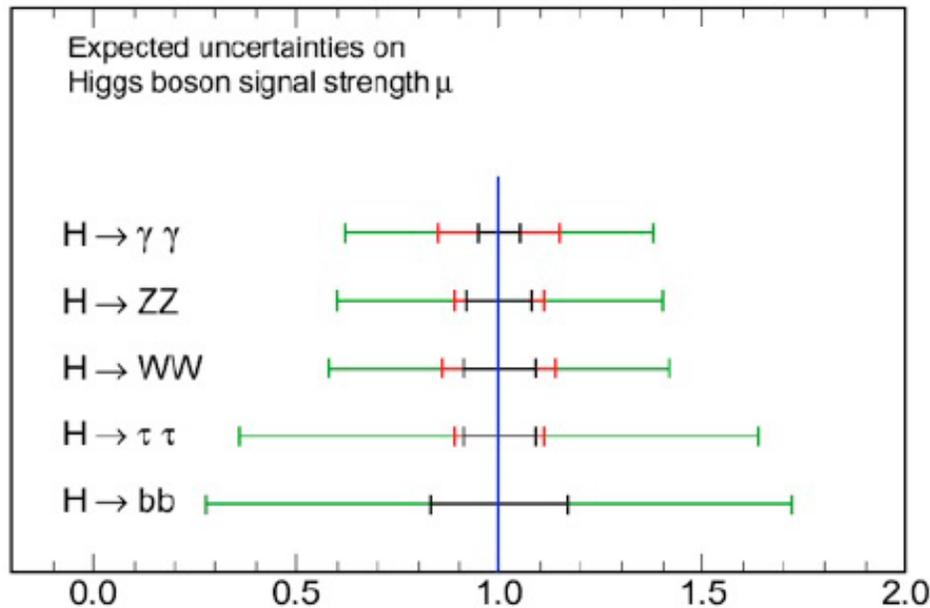
10-30% measurements  
for  $M_h = 120$  GeV

- Parameterize couplings in terms of deviation from SM
  - $\Delta_F = c_F - 1$ ,  $\Delta_V = c_V - 1$

Coupling measurements: Rauch, arXiv:1110.1196; Lafaye, Plehn, Rauch, Zerwas, arXiv: 0904.3806

# How well can we do with couplings?

CMS Projection



— 10 fb<sup>-1</sup> at  $\sqrt{s}=7/8$  TeV

— 300 fb<sup>-1</sup> at  $\sqrt{s}=14$  TeV

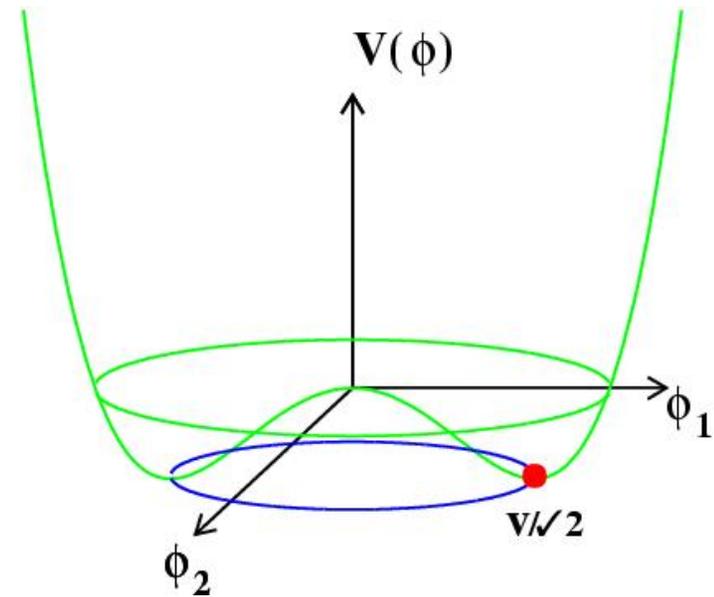
5-10% uncertainties on couplings with 300 fb<sup>-1</sup>

Some channels ( $c\bar{c}$ ,  $\mu^+\mu^-$ ) extremely difficult at LHC mostly due to low rates

# Can we reconstruct the Higgs potential?

$$V = \frac{M_h^2}{2} h^2 + \lambda_3 v h^3 + \frac{\lambda_4}{4} h^4$$

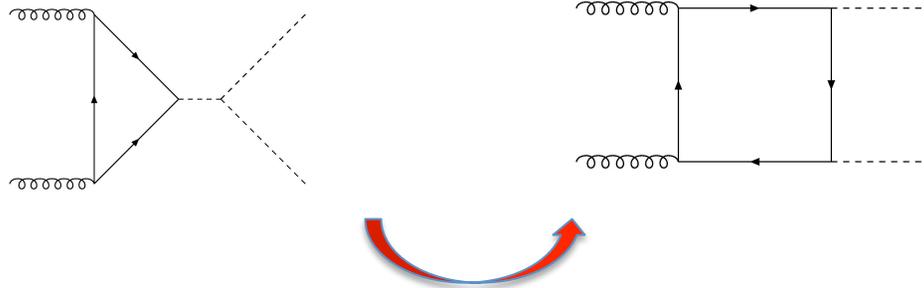
$$SM : \lambda_3 = \lambda_4 = \frac{M_h^2}{2v^2}$$



- Fundamental test of model!
- We have no idea how to measure  $\lambda_4$

# Double Higgs Production

- Sensitive to hhh coupling,  $\lambda_{hhh} = 3 M_h^2/M_Z^2$

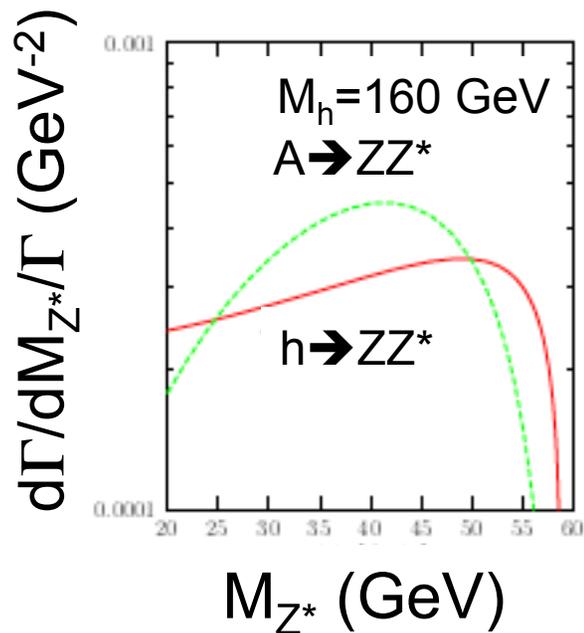
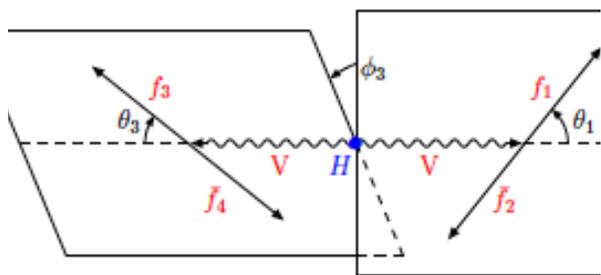


Contributions tend to cancel

$\sigma \sim 2$  fb (then you need branching ratios to observable final states....)

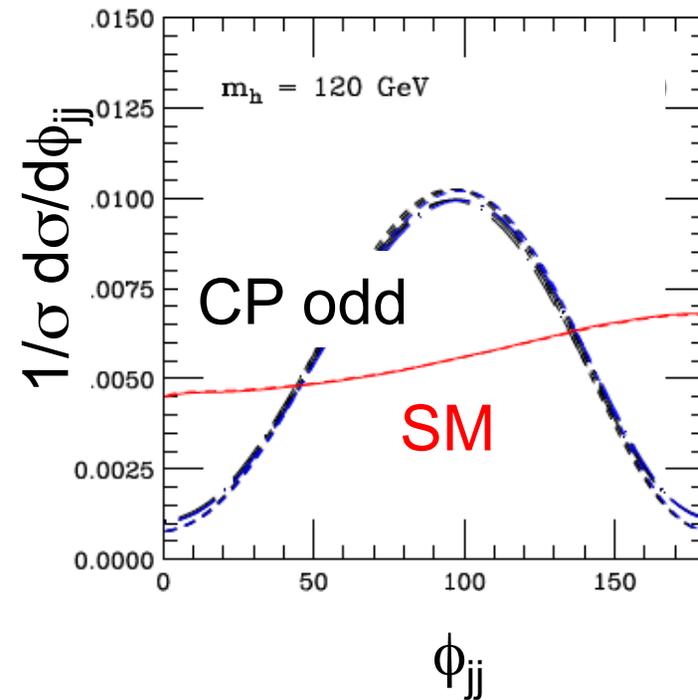
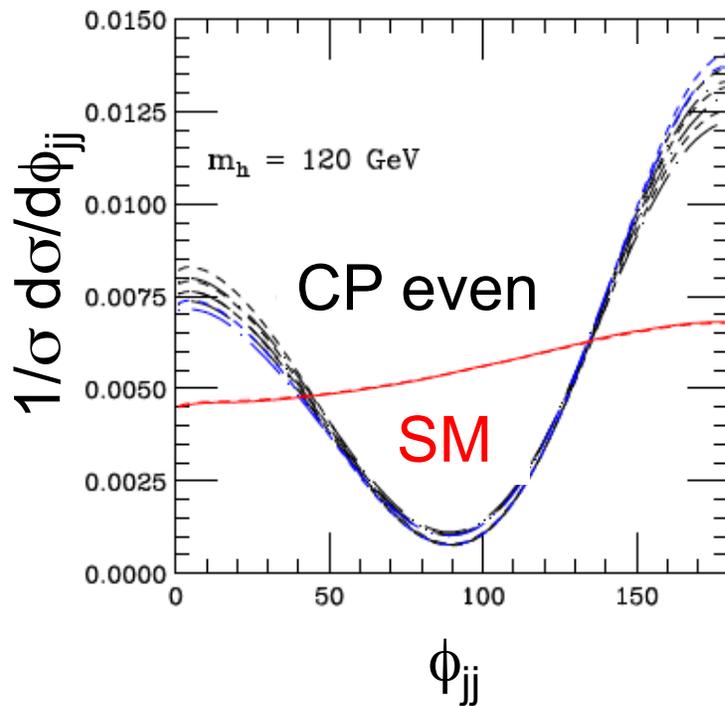
# CP Properties

- Look at  $h \rightarrow ZZ^* \rightarrow l^+ l^- l^+ l^-$
- Angular correlations depend on  $J^{PC}$
- Compare predictions for  $0^{++}$  with  $0^{+-}$  boson
- Remember rate is small



# CP Properties

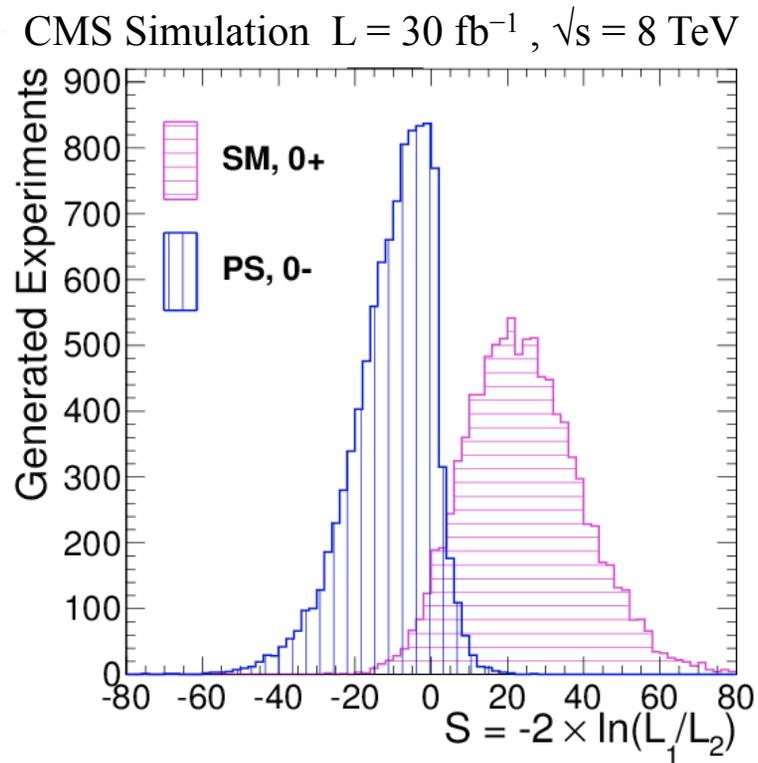
- In vector boson fusion measure angle between tagging jets
- Sensitive to CP properties



[Zeppenfeld]

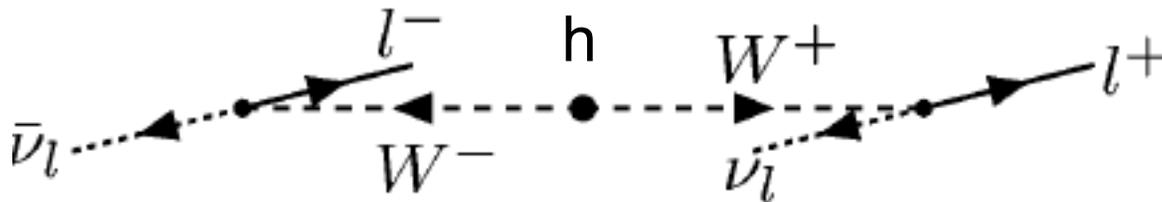
# Scalar vs pseudoscalar: How well can we distinguish?

$h \rightarrow ZZ^* \rightarrow 4l$  SM predicts  $0^{++}$  state



# Spin properties of Higgs-like Particle

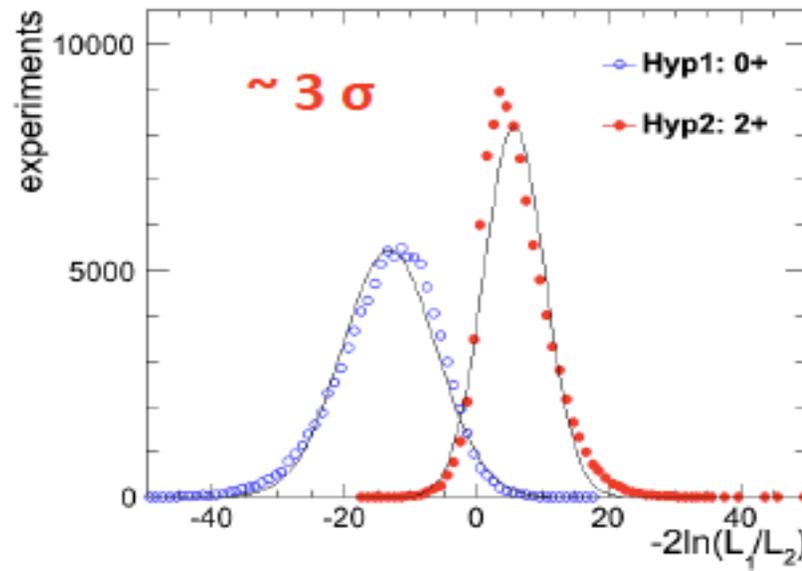
- $h \rightarrow \gamma\gamma$ , so it can't be spin 1
- Could be spin 0 or spin 2
- Look at  $h \rightarrow ZZ \rightarrow l^+l^-l^+l^-$
- Angular correlations are different for spin 0 and spin 2
- VBF,  $h \rightarrow W^+ W^- \rightarrow l\nu l\nu$
- Leptons from W decays tend to go in the same direction\*



\*Used in event selection

# Spin Measurements

- $h \rightarrow W^+W^- \rightarrow l\nu l\nu$
- Angular correlation of outgoing particles in  $h \rightarrow ZZ \rightarrow 4l$



30 fb<sup>-1</sup>

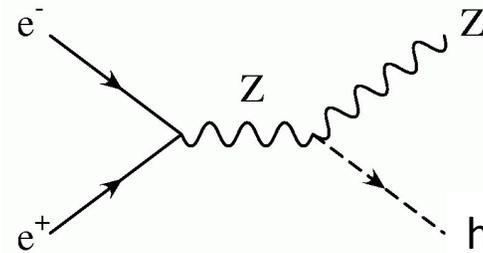
## Bottom Line

- With  $30 \text{ fb}^{-1}$ , should have a good handle on  $J^{\text{PC}}$
- Coupling measurements at the 25% level in many channels

*So are we done?????*

## Higgs Searches in e<sup>+</sup>e<sup>-</sup> Colliders

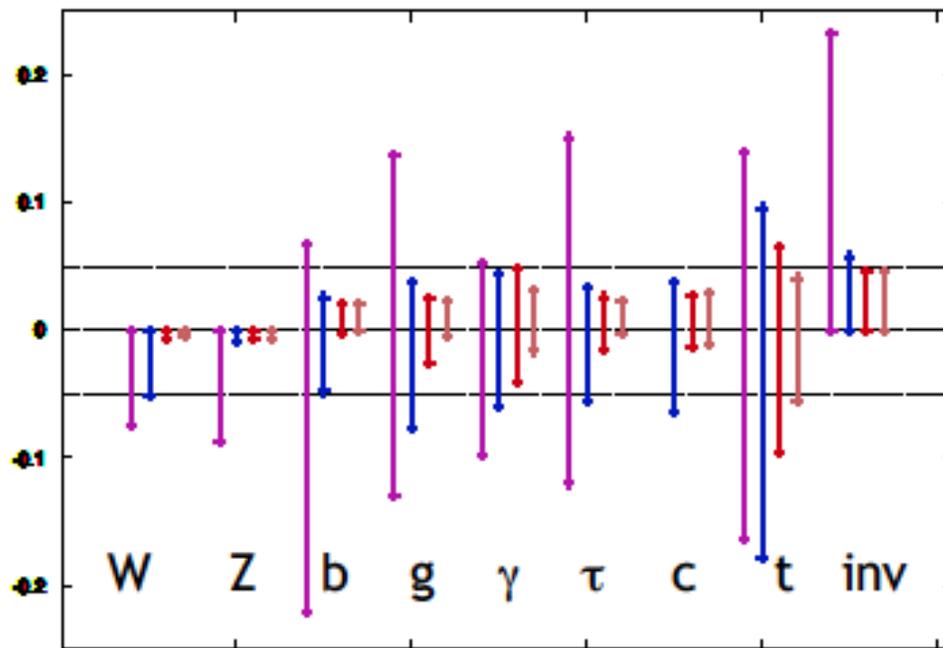
- LEP2 searched for e<sup>+</sup>e<sup>-</sup>→Zh
- Rate turns on rapidly after threshold, peaks just above threshold,  $\sigma \sim \beta^3/s$
- Measure recoil mass of Higgs; **result independent of Higgs decay pattern**
- Momentum conservation:
  - $(P_{e^-} + P_{e^+} - P_Z)^2 = P_h^2 = M_h^2$
  - $s - 2\sqrt{s} E_Z + M_Z^2 = M_h^2$



LEP2 limit,  $M_h > 114.1 \text{ GeV}$

# Coupling measurements at future colliders

$g(hAA)/g(hAA)|_{SM^{-1}}$  LHC/HLC/ILC/ILCTeV



LHC: 300 fb<sup>-1</sup> at 14 TeV  
HLC: 250 fb<sup>-1</sup> at 250 GeV  
ILC: 500 fb<sup>-1</sup> at 500 GeV  
ILCTeV: 1 ab<sup>-1</sup> at 1 TeV

What do we learn from the observation of  
a 125 GeV Higgs (like) boson?

Why we think there might be something  
else.....

Why particle physics isn't done....

# The Standard Model Works

- Any discussion of the Standard Model has to start with its success
- This is unlikely to be an accident!
- It's not perfect
  - Chimney plot: Consistency of the Standard Model
  - Higgs mass renormalization
  - Unitarity constraints

# Is the Standard Model Self-Consistent?

- $M_h$  is a free parameter in the Standard Model
- Can we derive limits on the basis of consistency?
- Consider a scalar potential:

$$V = \frac{M_h^2}{2} h^2 + \frac{\lambda}{4} h^4$$

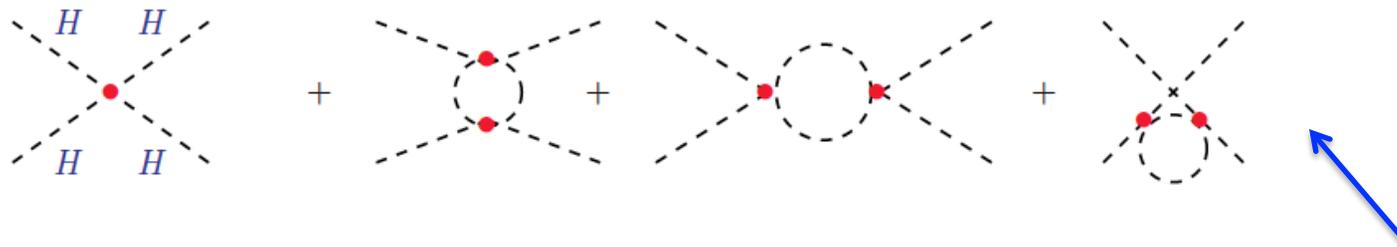
- This is potential at electroweak scale
- Parameters evolve with energy in a calculable way

Standard Model:  $\lambda = M_h^2 / (2v^2) = .13$  for  $M_h = 125$  GeV

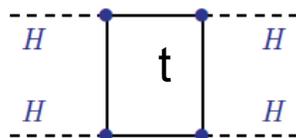
*Perturbative Regime*

# Higgs Potential for Large $h$

- Self interactions of Higgs cause  $\lambda$  to grow at high energy



- Top interactions decrease  $\lambda$  at high energy



Trade-off

## High Energy Behavior of $\lambda$

- Renormalization group scaling

$$16\pi^2 \frac{d\lambda}{dt} = 12\lambda^2 + 12\lambda g_t^2 - 12g_t^4 + (\text{gauge})$$

$$t \equiv \log\left(\frac{Q^2}{\mu^2}\right) \quad g_t = \frac{M_t}{v}$$

- **Large  $\lambda$  (Heavy Higgs):** self coupling causes  $\lambda$  to grow with scale
- **Small  $\lambda$  (Light Higgs):** coupling to top quark causes  $\lambda$  to become negative

# Does Spontaneous Symmetry Breaking Happen?

- SM requires spontaneous symmetry breaking
- This requires

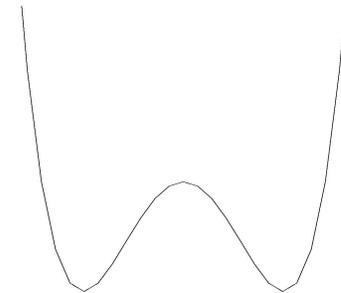
$$V(v) < V(0)$$

- For small  $\lambda$

$$16\pi^2 \frac{d\lambda}{dt} \approx -12g_t^4$$

- Solve

$$\lambda(\Lambda) \approx \lambda(v) - \frac{3g_t^4}{4\pi^2} \log\left(\frac{\Lambda^2}{v^2}\right)$$

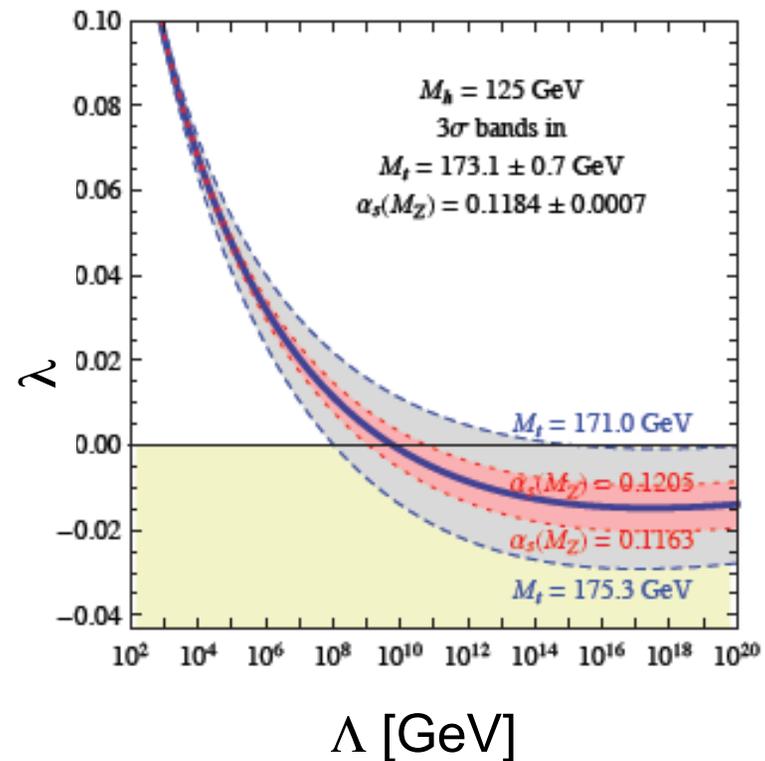


# Does Spontaneous Symmetry Breaking Happen?

- $\lambda(\Lambda) > 0$  gives lower bound on  $M_h$

$$M_h^2 > \frac{3v^2}{2\pi^2} g_t^2 \log\left(\frac{\Lambda^2}{v^2}\right)$$

- For any given  $M_h$ , there is an upper bound on  $\Lambda$



This is very sensitive to  $M_h$

[DeGrassi et al, 1205.6497]

## Don't want $\lambda$ to be infinite

- Point where  $\lambda \rightarrow \infty$  called Landau pole
- Without  $\lambda h^4$  interactions, theory is non-interacting
- Require quartic coupling be finite gives upper bound

$$\frac{1}{\lambda(\Lambda)} > 0$$

$$M_h^2 < \frac{32\pi^2 v^2}{9 \log\left(\frac{\Lambda^2}{v^2}\right)}$$

Maybe vacuum can be unstable if lifetime is longer than lifetime of the universe

[Ellis,0906.0954]

