

# Tracking

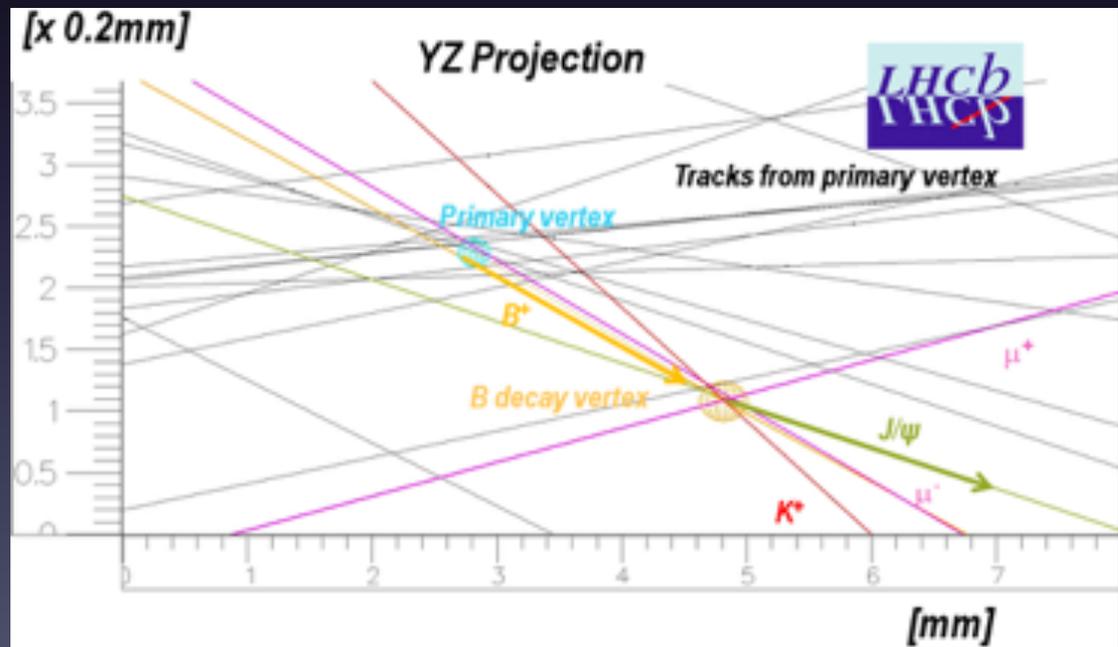
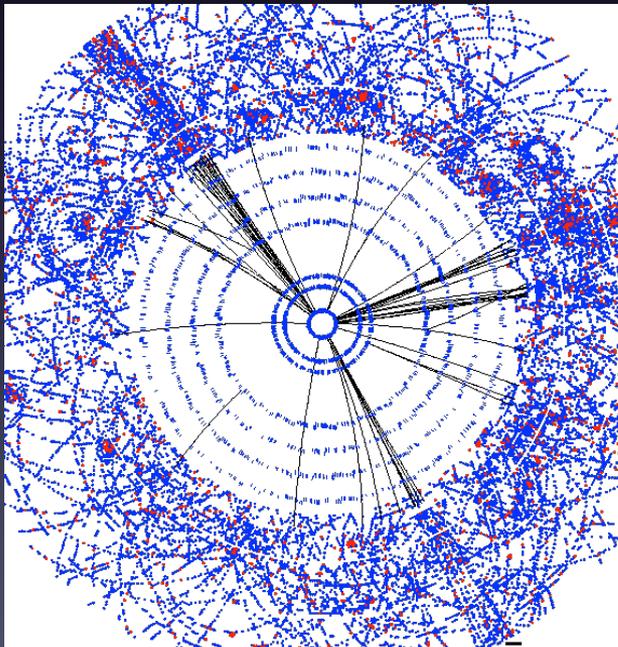
- Fundamental issues in tracking or how to design a tracker ?
- Silicon detectors
- New ideas and developments for the HL-LHC

**D. Bortoletto**

**University of Oxford**

# Tracking detectors

- High granularity detectors close to the interaction region providing precise measurements of the position of charged particles
  - Measure the trajectory using “hits” to determine the momentum of charged particles from their curvature in a magnetic field
  - Extrapolate to the origin and reconstruct
    - Primary vertices and identify the vertex associated with the “hard” interaction
    - Secondary vertices to identify tau-leptons, b and c-hadrons by lifetime tagging
  - Reconstruct strange hadrons, which decay in the detector volume
  - Identify photon conversions and nuclear interactions



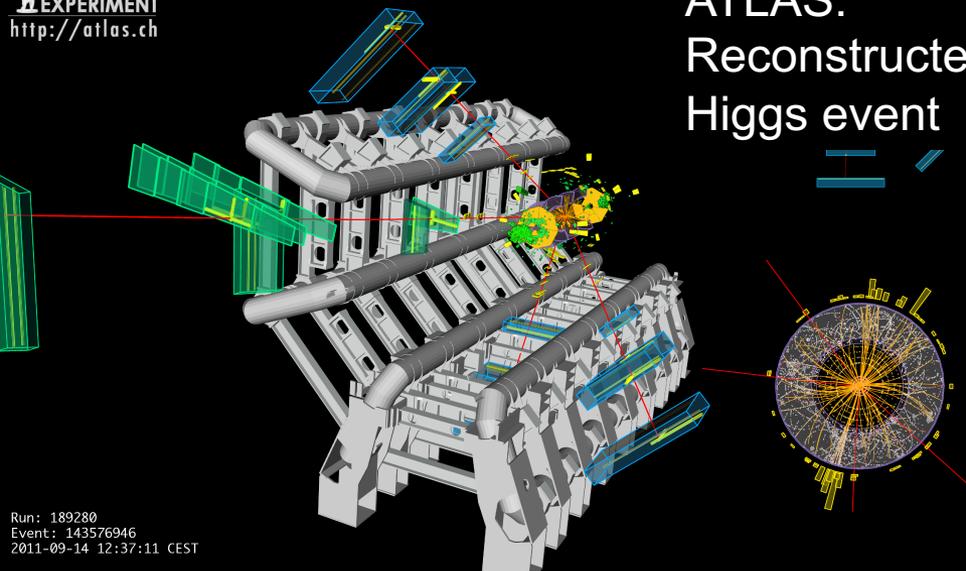


# LHC physics program

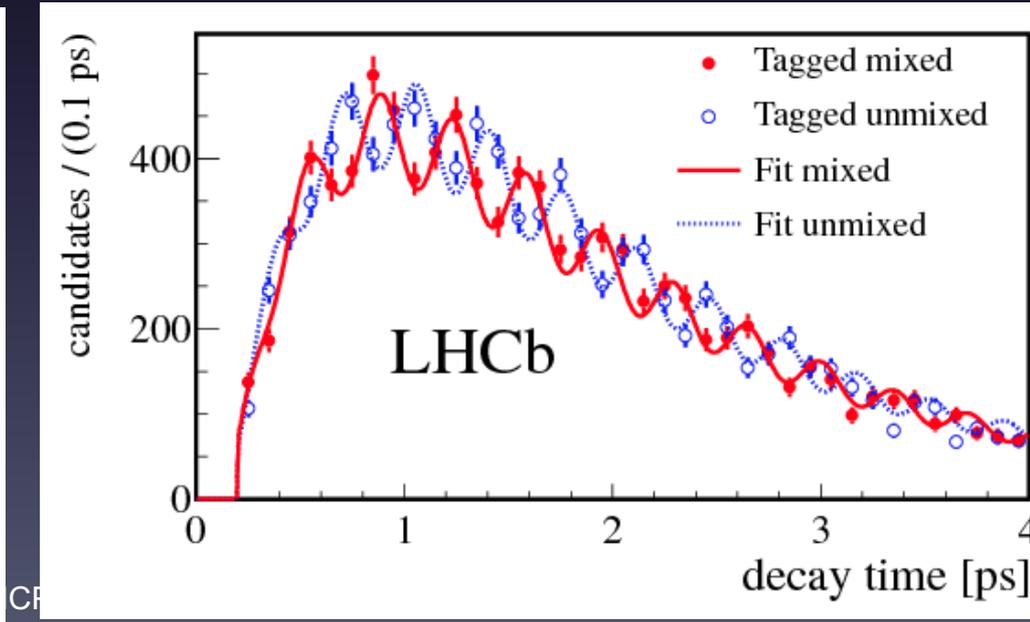
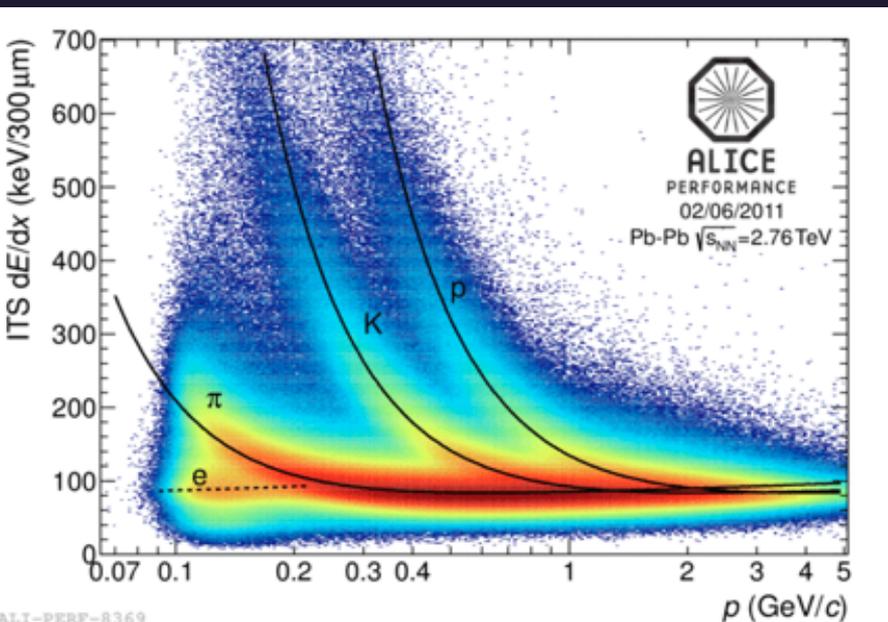
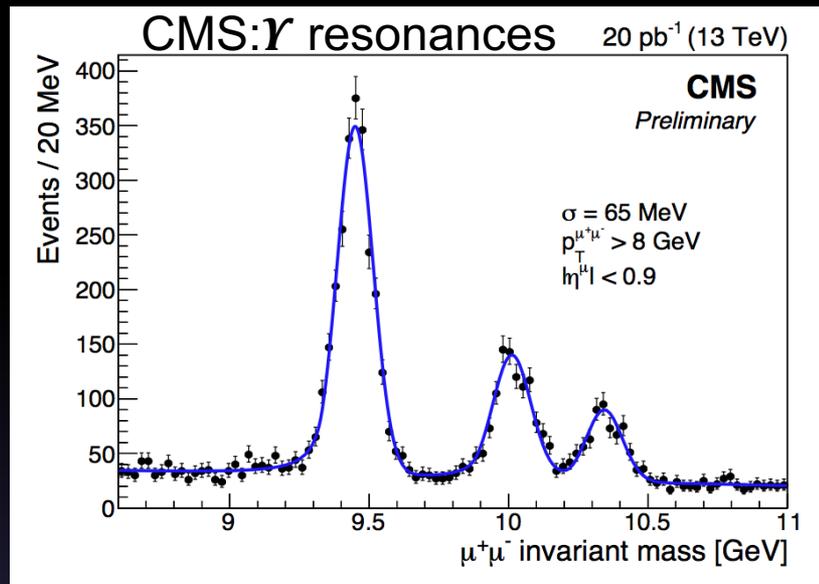
UNIVERSITY OF

ATLAS  
EXPERIMENT  
<http://atlas.ch>

ATLAS:  
Reconstructed  
Higgs event



Run: 189280  
Event: 143576946  
2011-09-14 12:37:11 CEST



# Momentum Measurements

- The determination of the momentum (and charge) of charged particles can be performed by measuring the bending of a particle trajectory (track) in a magnetic field

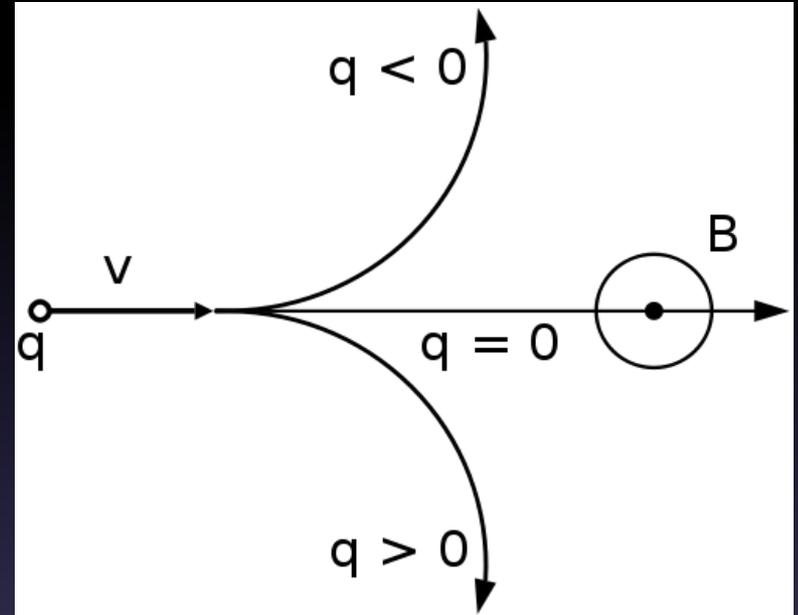
Lorentz Force

$$\vec{\mathbf{F}} = q\vec{v} \times \vec{\mathbf{B}}$$

Motion transverse to  
 an uniform B field

$$\frac{mv^2}{r} = qvB$$

$$p_T [GeV/c] = 0.3B [T] R [m]$$

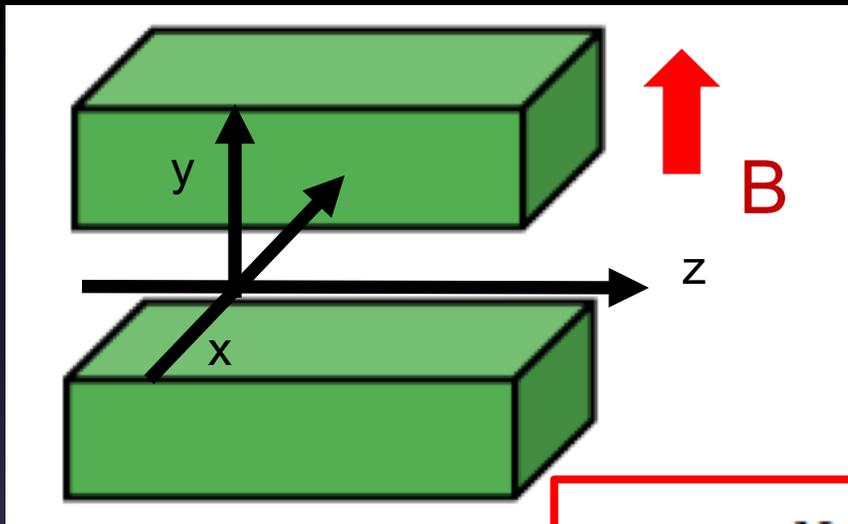


- Use layers of position sensitive detectors before and after or inside a magnetic field to measure a trajectory and determine the bending radius
- The tracker configuration depends critically on the choice of the magnet

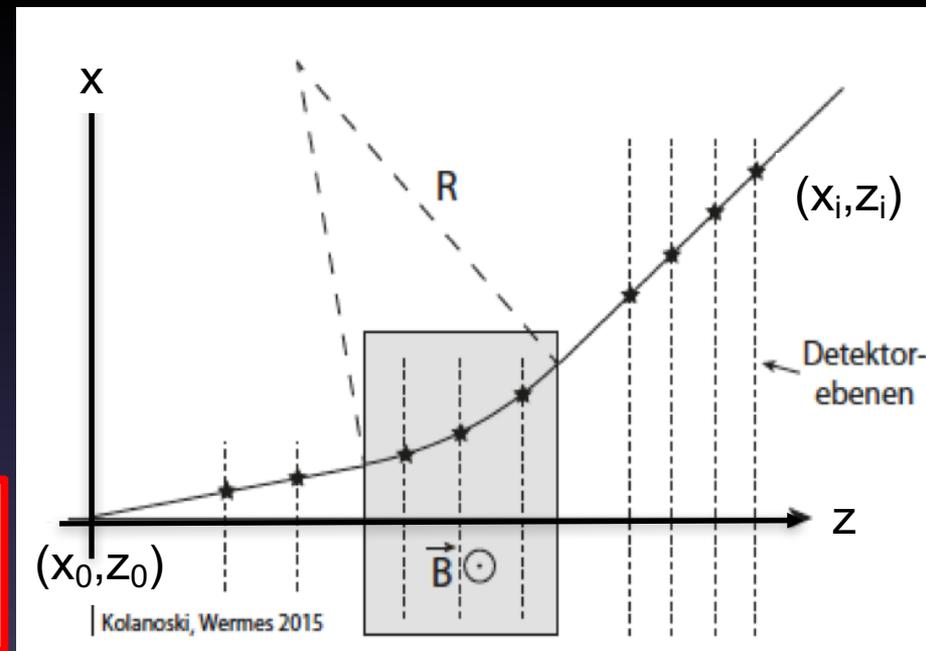
# Forward Spectrometers

Dipole LHCb  $NI = 4Tm$

Plane  
symmetry



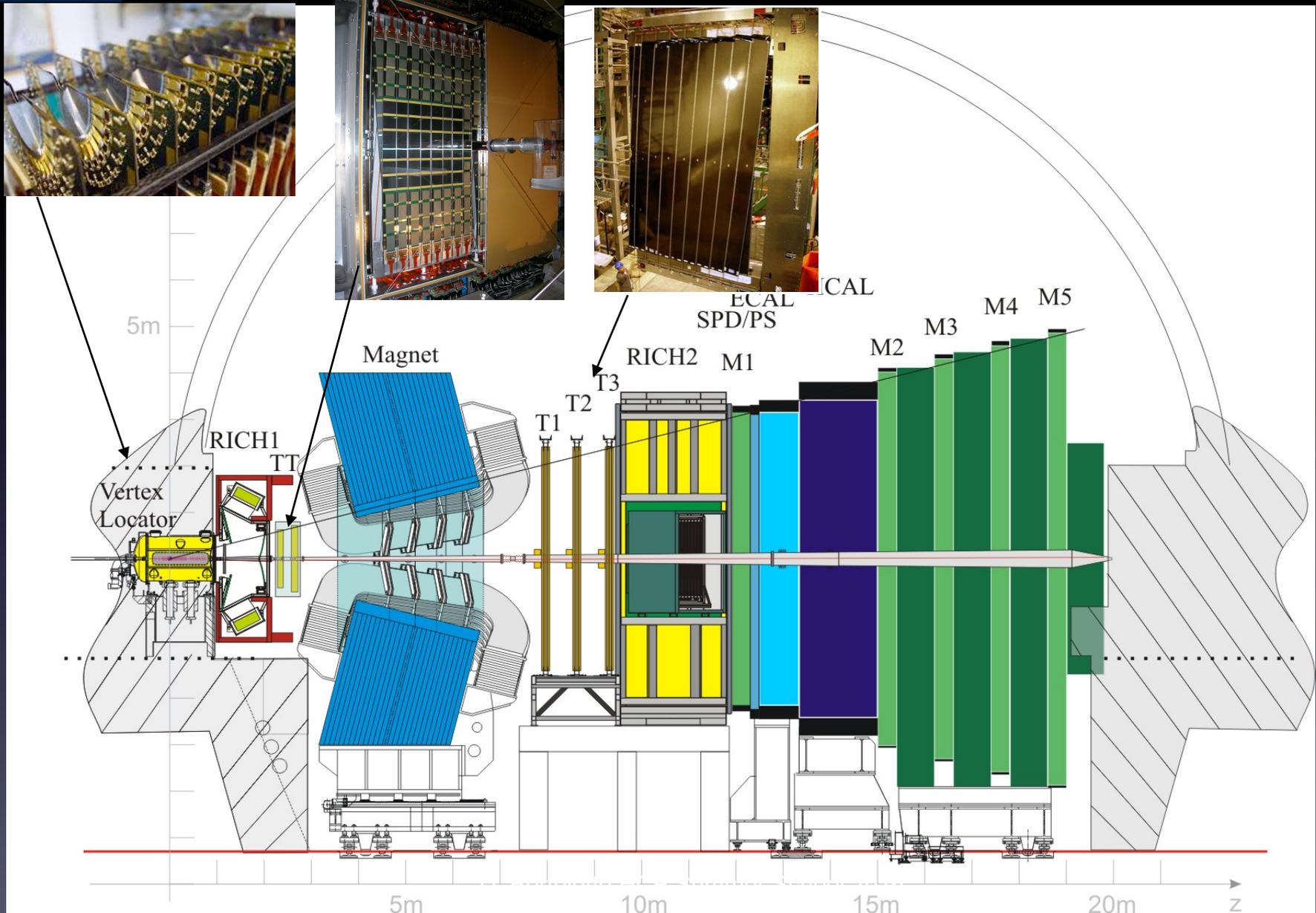
$$B \approx \frac{\mu_0 N I}{h}$$



- Particle deflected in  $x - z$  plane
- Tracking detectors are arranged in parallel planes along  $z$
- Bending from difference of the slopes before and after magnet



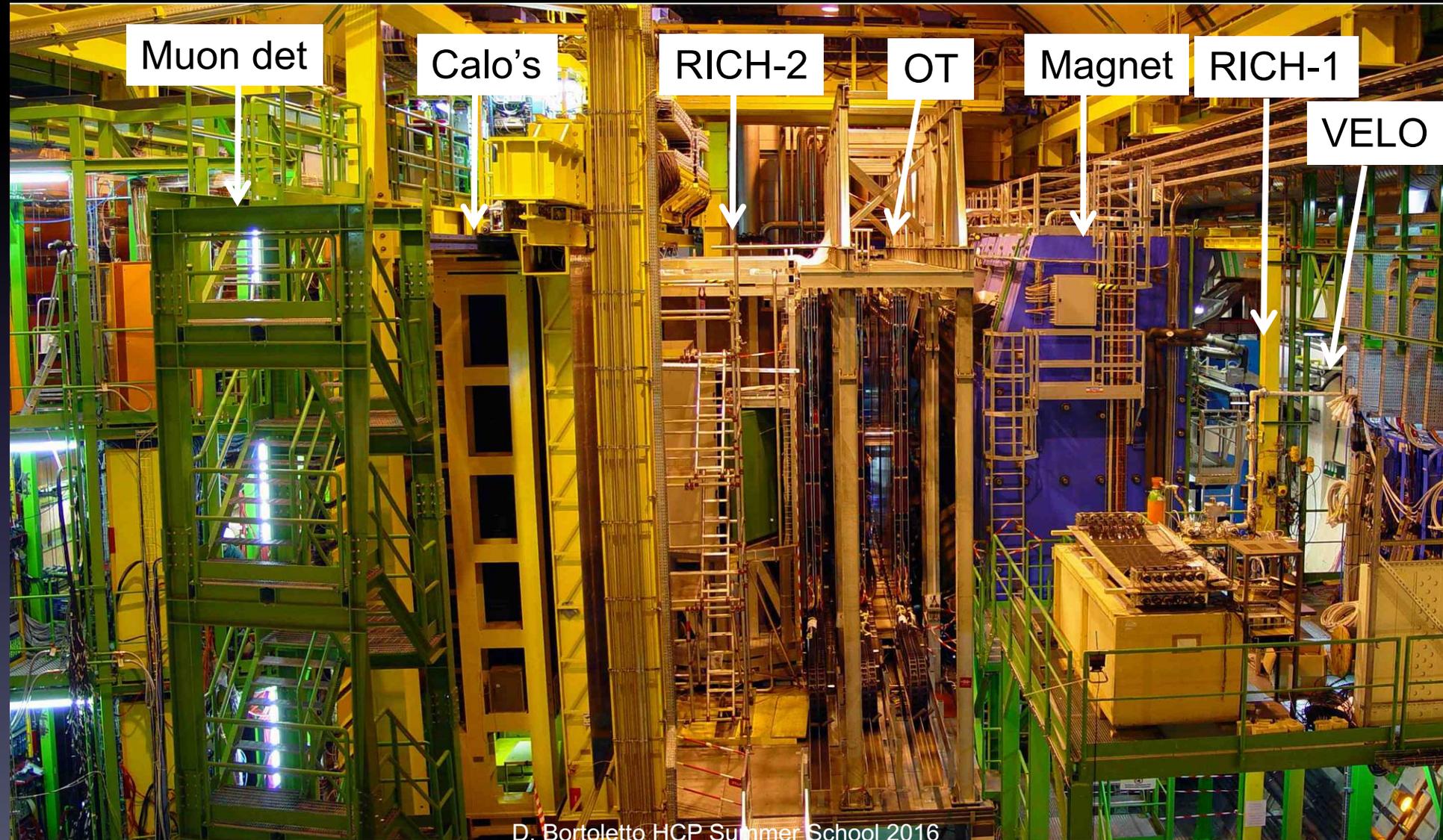
# LHCb A Forward Spectrometer





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# LHCb A Forward Spectrometer



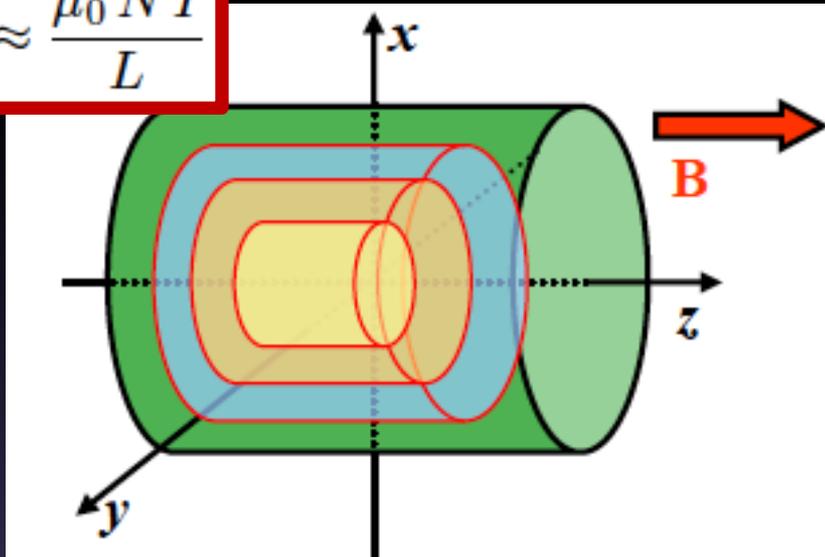


# Central Detectors

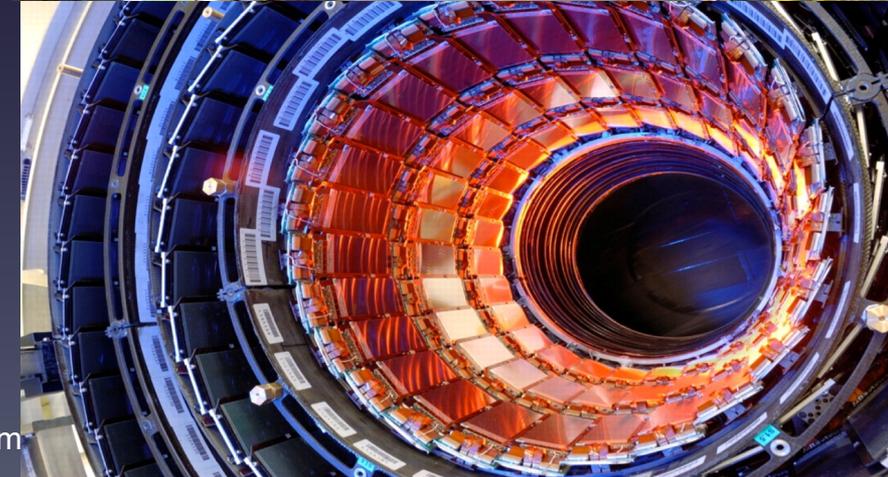
Solenoid CMS 4T, Atlas 2T

Cylindrical  
symmetry

$$B \approx \frac{\mu_0 N I}{L}$$



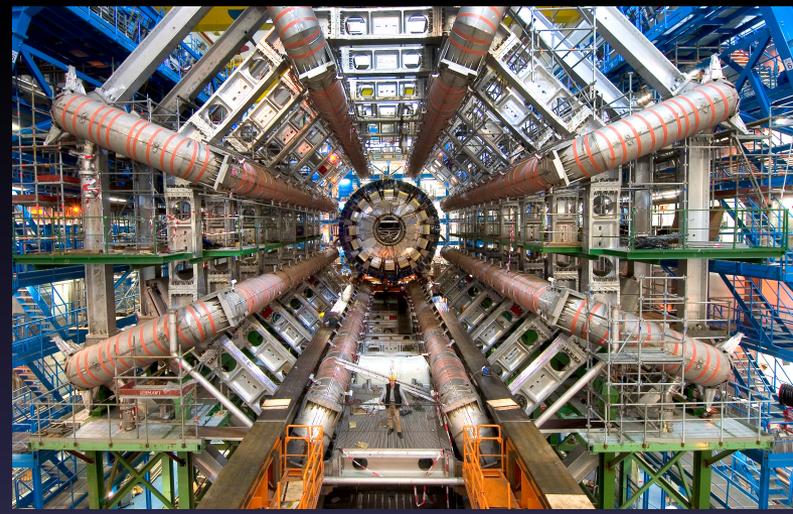
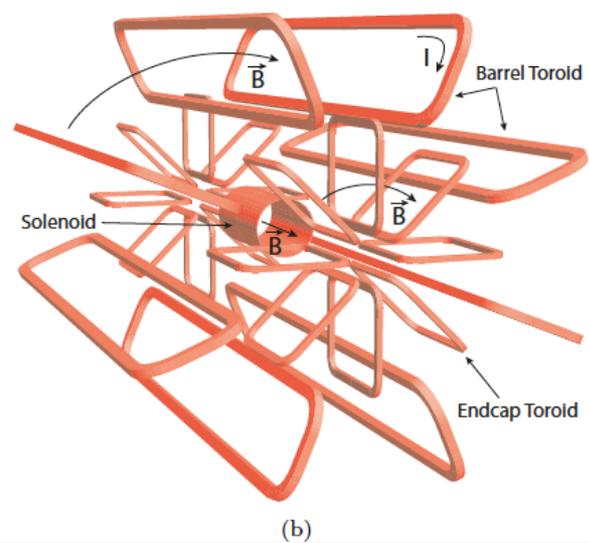
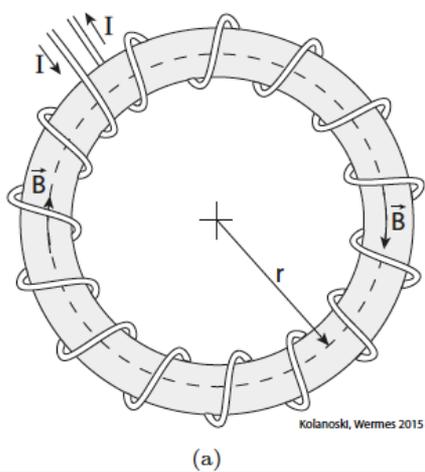
- Magnetic field along the beam
- Particle deflected in  $x - y$  ( $r - \phi$ ) plane
- Tracking detectors are arranged in cylindrical shells along  $r$
- Measurement of curved trajectories on  $r - \phi$  planes at fixed  $r$



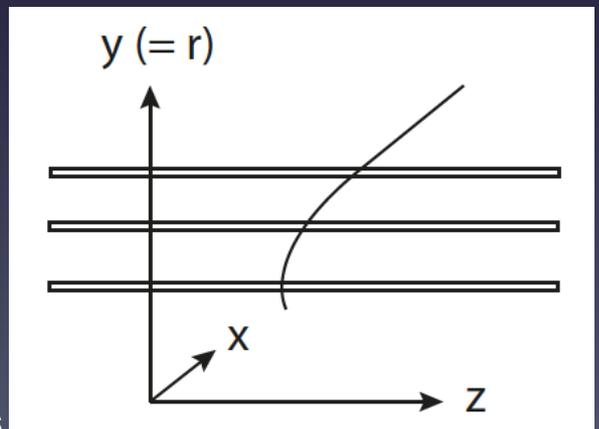
# Magnetic Spectrometers

## Toroid Atlas 0.5T

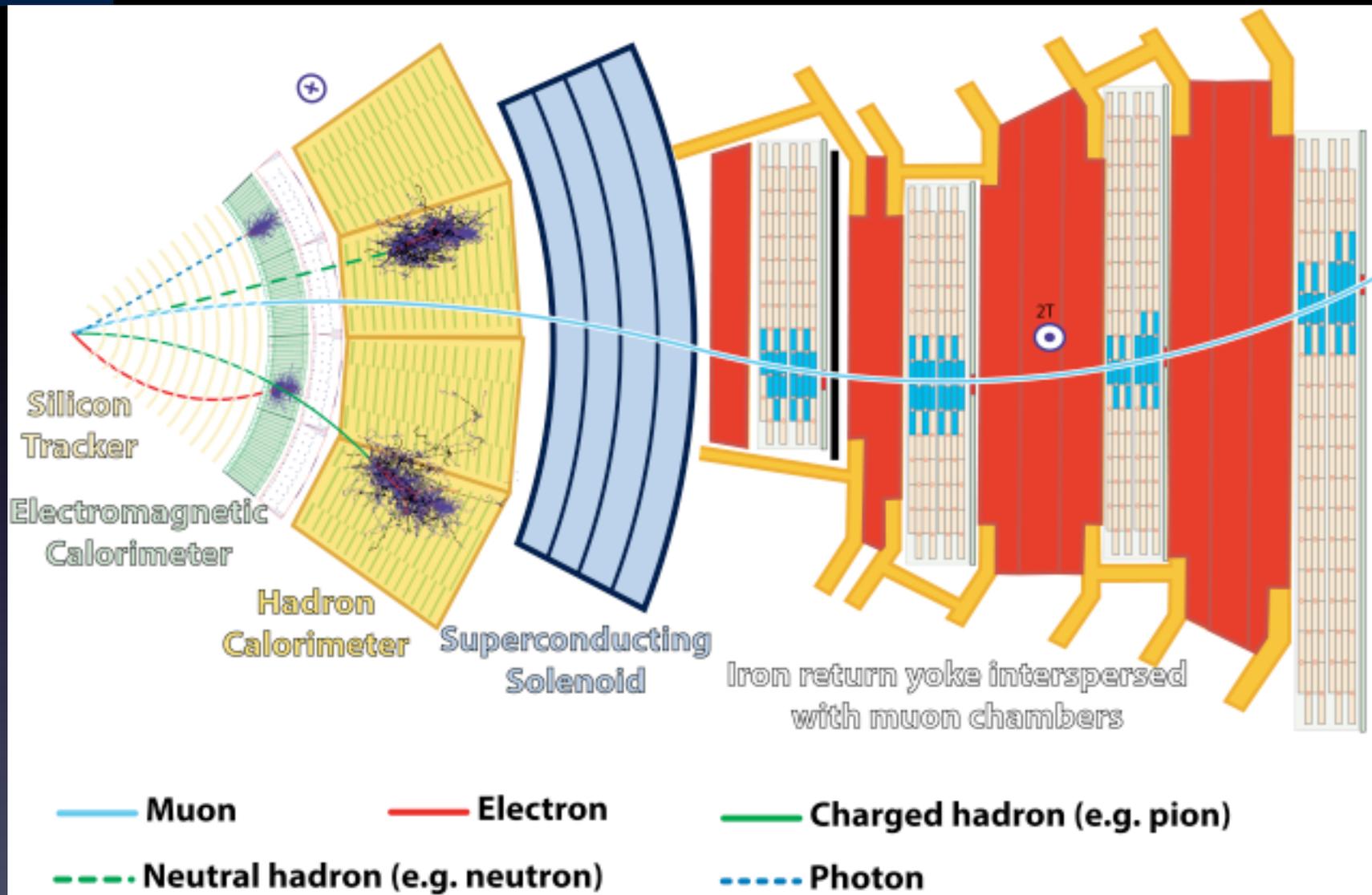
## Azimuthal symmetry



- Deflection in  $(r - z)$  – plane
- Tracking detectors are arranged in cylindrical shells providing measurement of curved trajectories in  $r-z$  planes at fixed  $r$

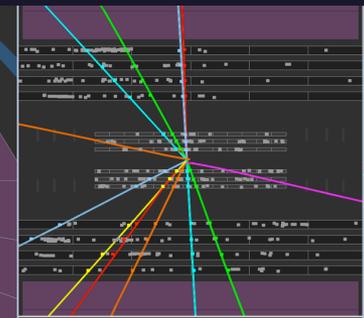
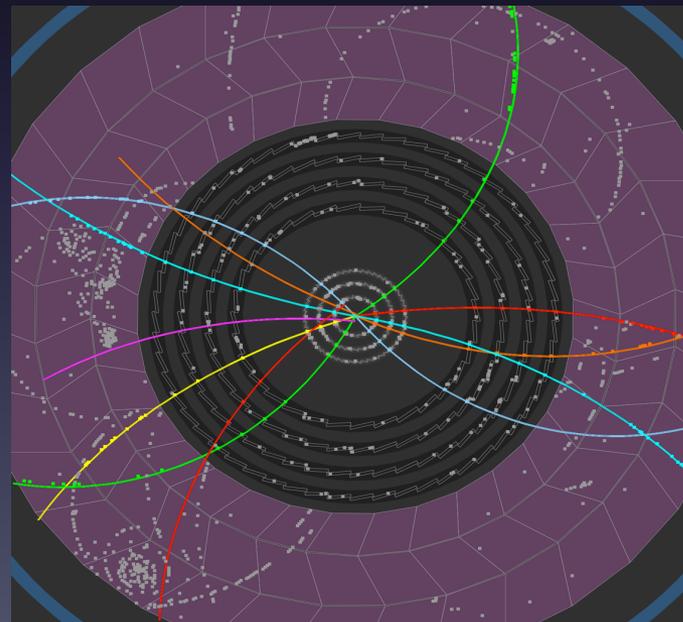
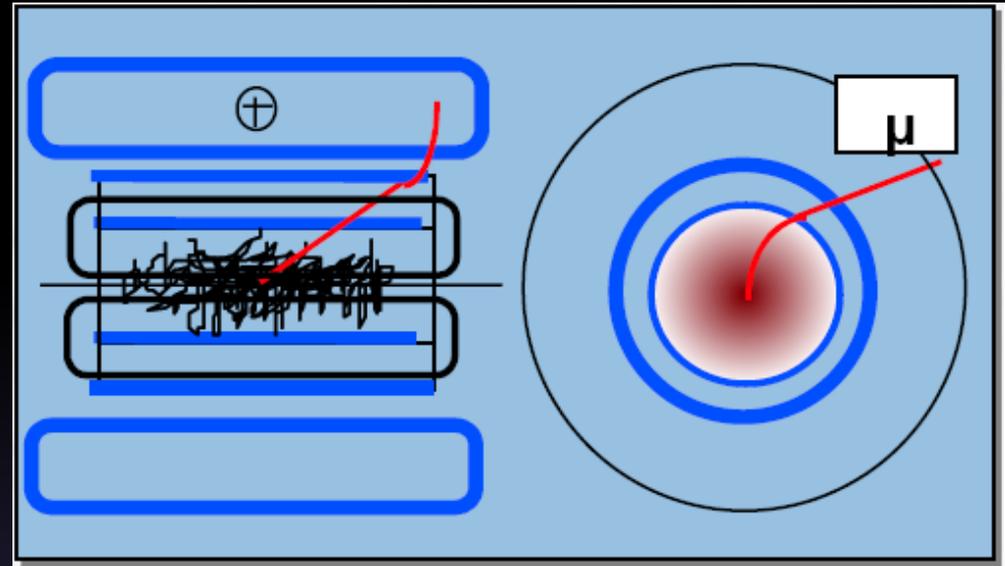
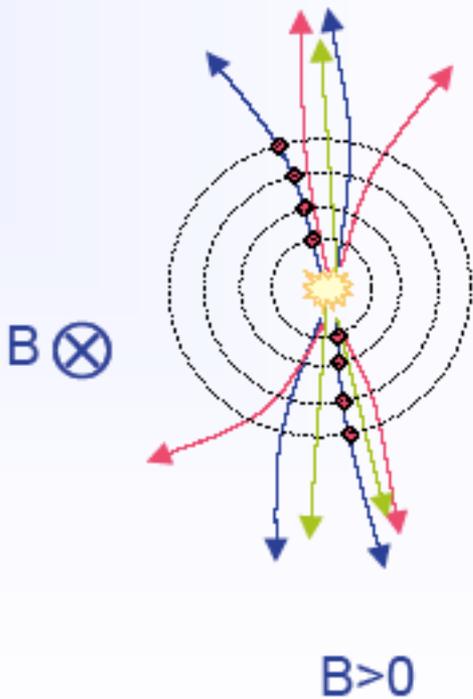
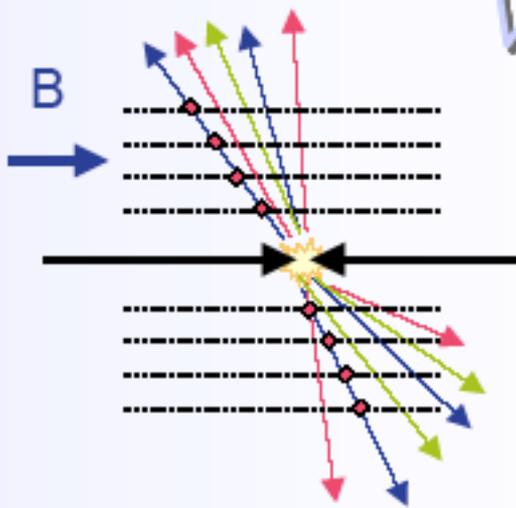


# CMS





# Tracking in ATLAS

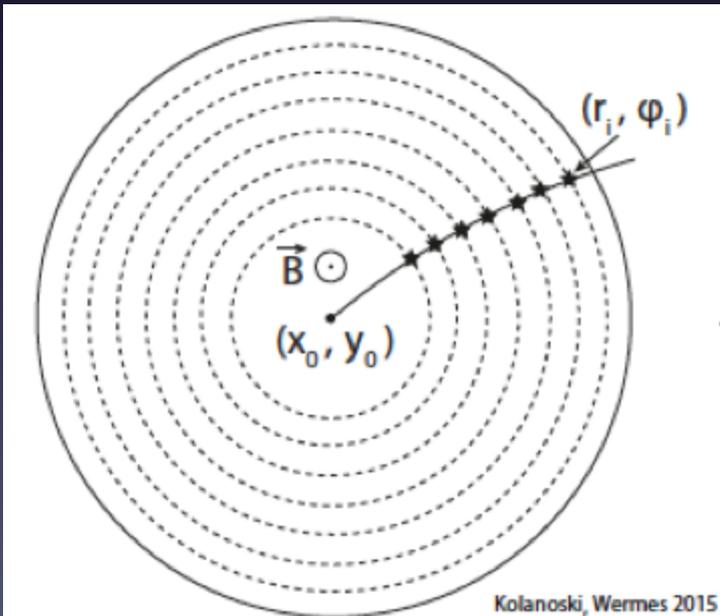
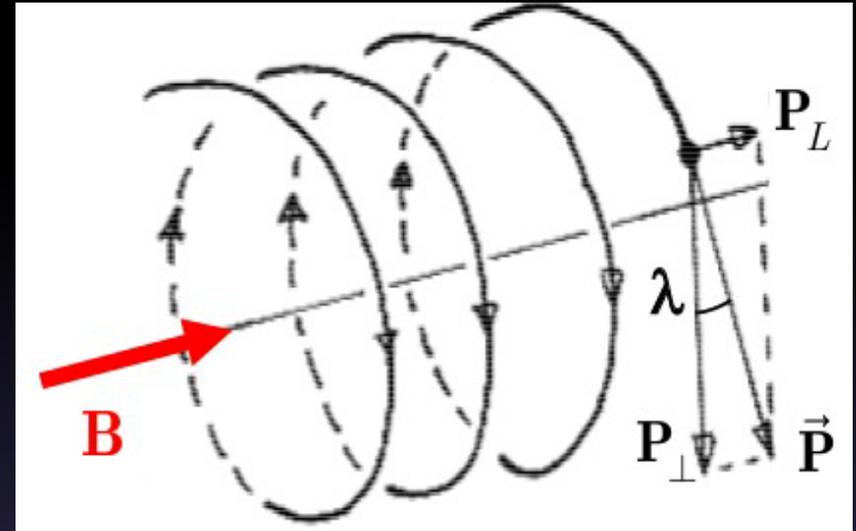


**ATLAS EXPERIMENT**  
 2009-12-06, 10:03 CET  
 Run 141749, Event 405315  
**Collision Event**



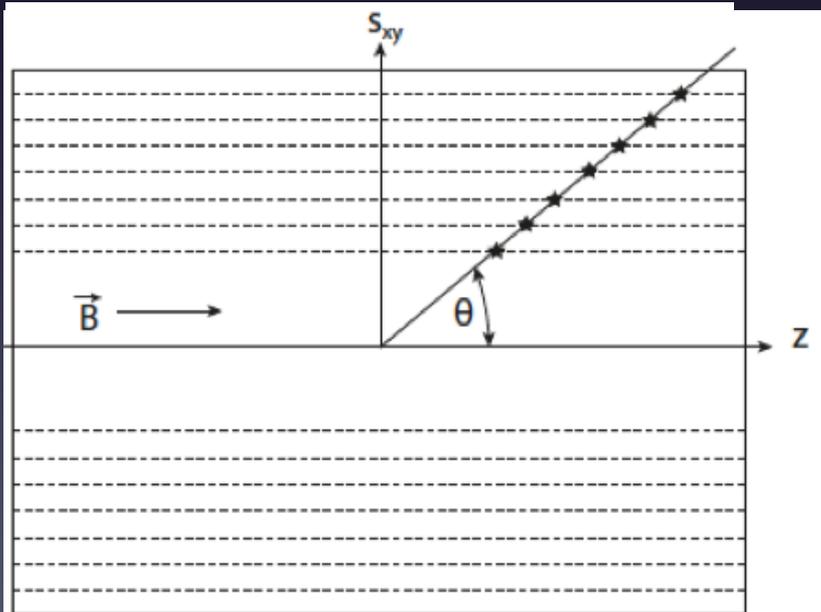
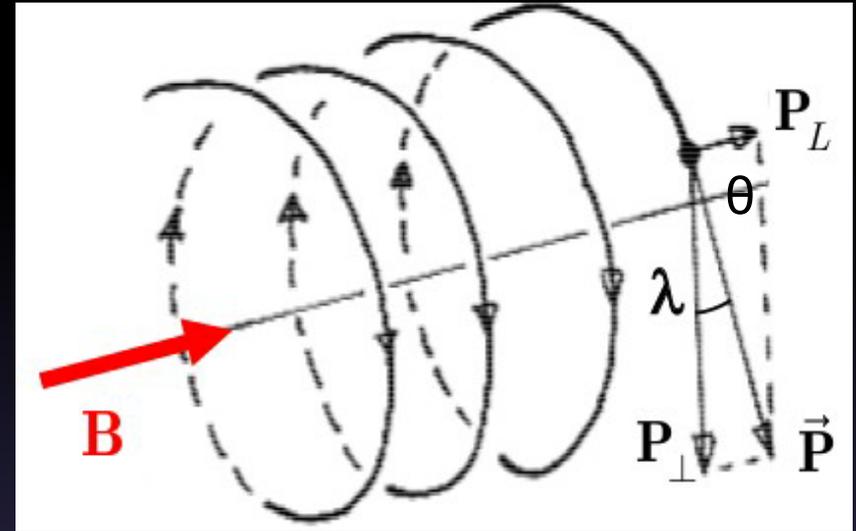
# Tracking in a solenoidal B

- The trajectory of a charged particle in a uniform B field along the beamline is a helix
  - Transverse (xy) and Longitudinal (rz) projections.
  - $\Phi$ =azimuthal angle is measured in transverse plane
  - $\theta$ =polar angle is measured from z axis
  - Dip,  $\lambda = \pi/2 - \theta$
  - Pseudorapidity,  $\eta = -\ln \tan (\theta/2)$
  - Transverse momentum,  $p_T = p \sin\theta$

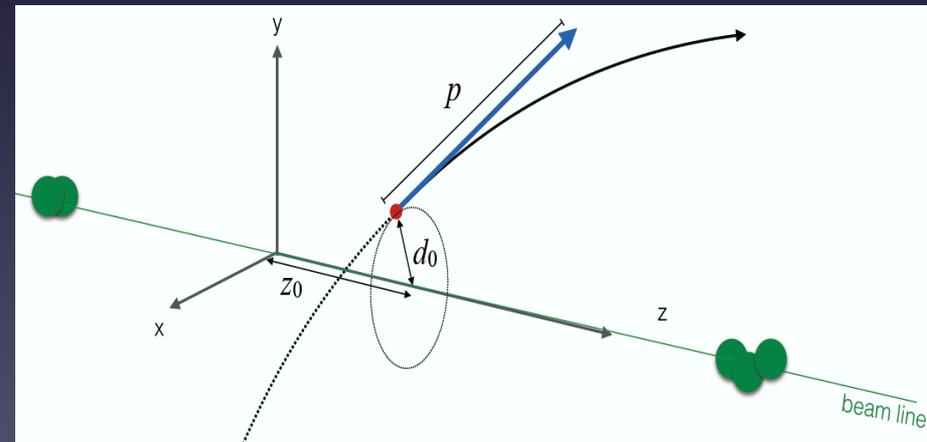


# Tracking in a solenoidal B

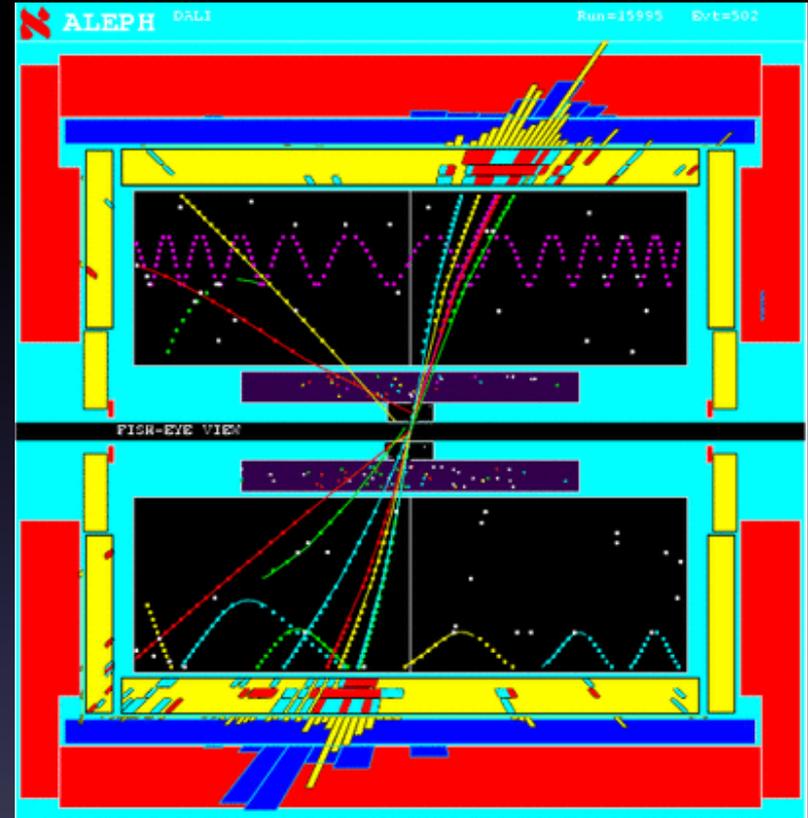
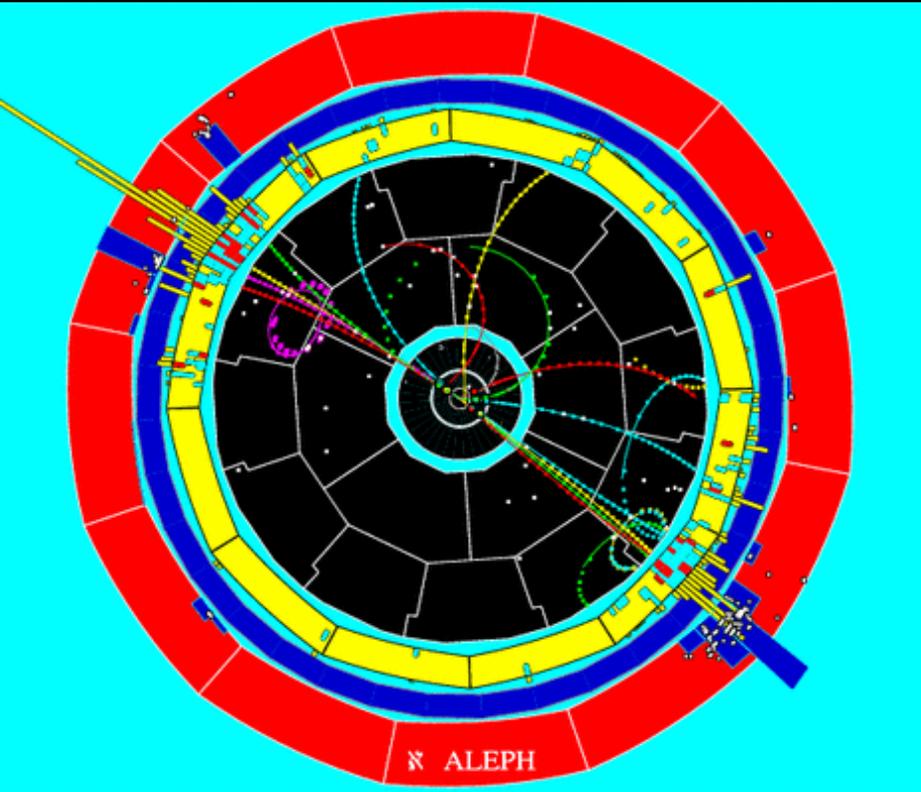
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- Impact parameter  $d_0$



# The Helix ... seen in an experiment



- For small momenta  $y$  is a periodic function of  $z$
- For large momenta we have a straight line as a function of  $z$



# What we need to do?

- Measure the transverse momentum and the dip angle  $\lambda$

$$P = \frac{P_{\perp}}{\cos \lambda} = \frac{0.3BR}{\cos \lambda}$$

- The error on the momentum is given by the measurement errors on the curvature radius  $R$  and the dip angle  $\lambda$

$$\frac{\partial P}{\partial R} = \frac{P_{\perp}}{R}$$

$$\frac{\partial P}{\partial \lambda} = -P_{\perp} \tan \lambda$$

$$\left(\frac{\Delta P}{P}\right)^2 = \left(\frac{\Delta R}{R}\right)^2 + (\tan \lambda \Delta \lambda)^2$$

- For central detector configurations with solenoid magnets
  - the error on the radius measured in the bending plane  $r - \varphi$
  - the error on the dip angle in the  $r - z$  plane
  - The contribution of multiple scattering to the the momentum resolution
- In a hadron collider like LHC the main emphasis is on transverse momentum measurement

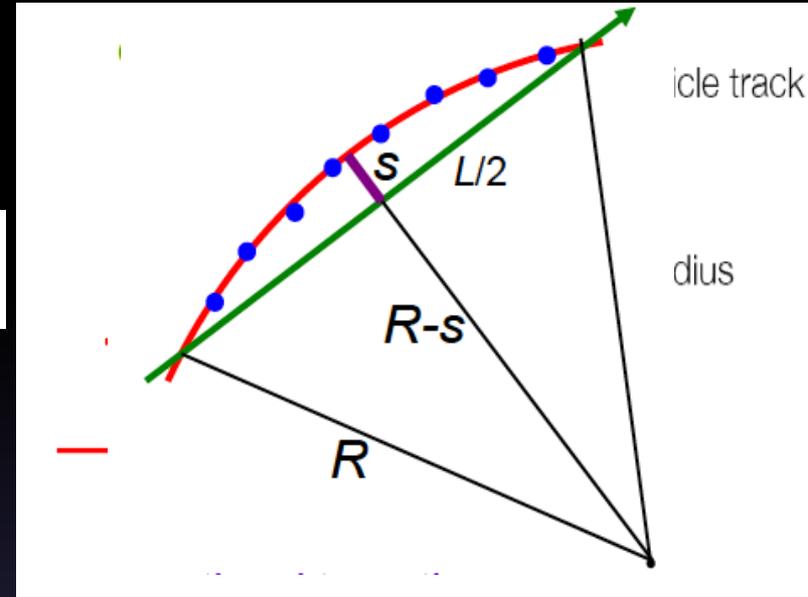


# Momentum measurement

- Motion transverse to uniform B field

$$p_T [GeV/c] = 0.3B [T] R [m]$$

Measure the sagitta,  $s$ , from radius of curvature,  $R$ . If  $s \ll L$



$$R = \frac{L^2}{8s} + \frac{s}{2} \approx \frac{L^2}{8s}$$

$$\frac{\Delta p_T}{p_T} = \frac{\Delta R}{R}$$

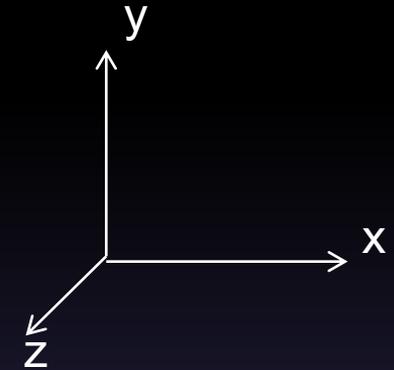
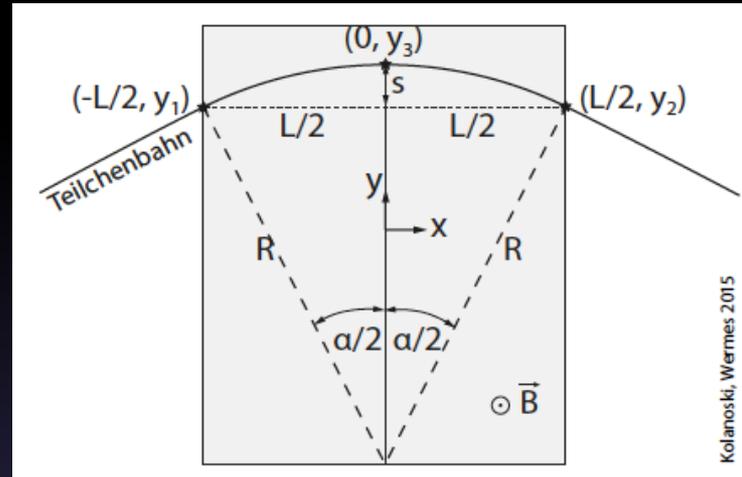
$$\frac{\sigma_{p_T}}{p_T} = \frac{8p_T}{0.3BL^2} \sigma_s$$

Good relative momentum requires small  $\sigma_s$ , strong B field, long path length  $L$  (as  $L^2 \Rightarrow$  often use beam constraint).

Momentum resolution gets worse at large  $p_T$

# Momentum resolution

- Let us assume that we have 3 measurements of the position of the particle



$$s = y_3 - \frac{y_1 + y_2}{2}$$

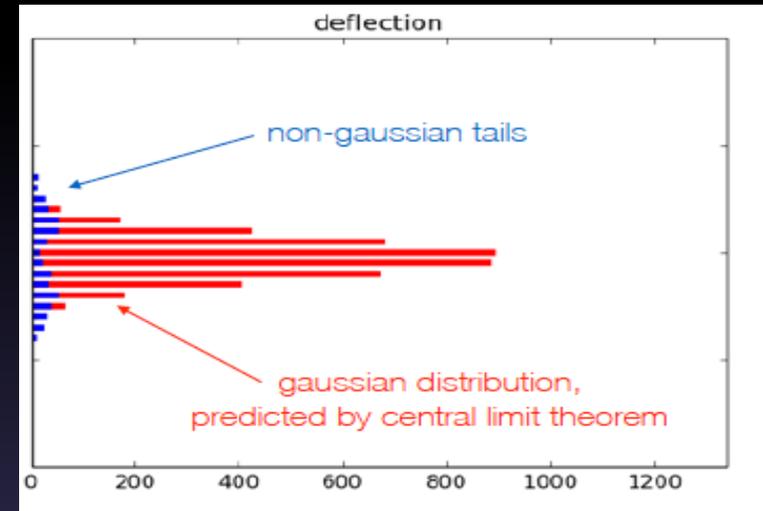
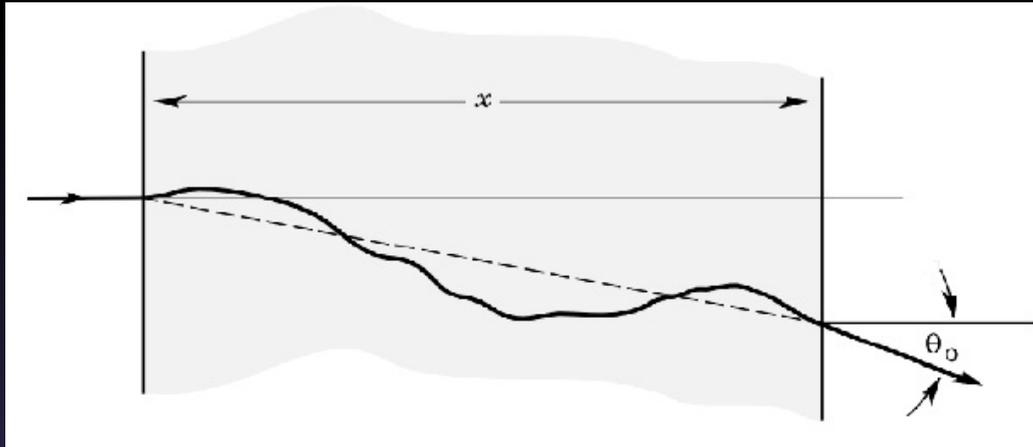
$$\sigma_s = \sqrt{\sigma_{r\phi}^2 + \frac{1}{4} 2\sigma_{r\phi}^2} = \sqrt{\frac{3}{2}} \sigma_{r\phi}$$

- For N measurements all with the uncertainty

Small  $\sigma_s \implies$  small  $\sigma_{r\phi}$  and large N (many measurement points, but only as  $\sqrt{N}$ )

# Multiple scattering

- A charged particle in medium undergoes random deflections caused
  - by multiple (Coulomb) scattering off the core of atoms
  - single large (Rutherford) scattering



$$\theta_0 = \frac{13.6 \text{ MeV}/c}{p\beta} Z \sqrt{\frac{x}{X_0}} \left( 1 + 0.038 \ln \frac{x}{X_0} \right)$$

- This introduces an error on the sagitta
  - Multiple scattering is reduced by: low  $Z$ , thin materials, long  $X_0$



# Momentum resolution

- The point error,  $\sigma_{r\phi}$ , has a part from intrinsic measurement precision and a multiple scattering part. Therefore:

$$\frac{\sigma_{p_T}}{p_T} = \sqrt{\left(\frac{\sigma_{p_T}}{p_T}\right)_{r\phi}^2 + \left(\frac{\sigma_{p_T}}{p_T}\right)_{MS}^2}$$

$$\left(\frac{\sigma_{p_T}}{p_T}\right)_{r\phi} = \frac{p_T}{0.3L^2B} \sqrt{\frac{720}{N+4}} \sigma_{r\phi}$$

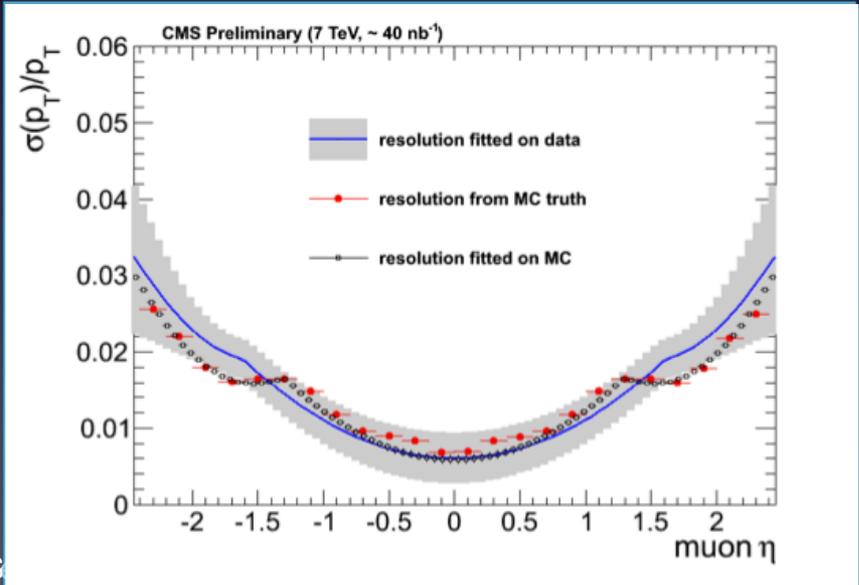
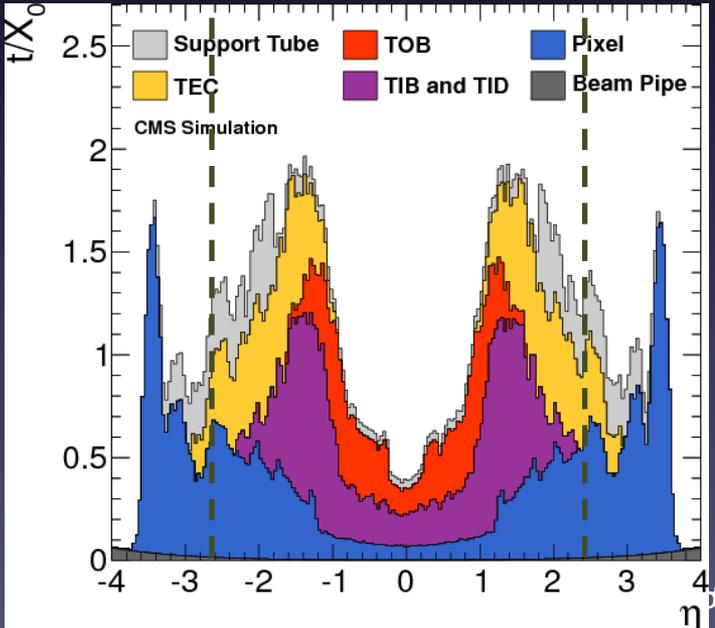
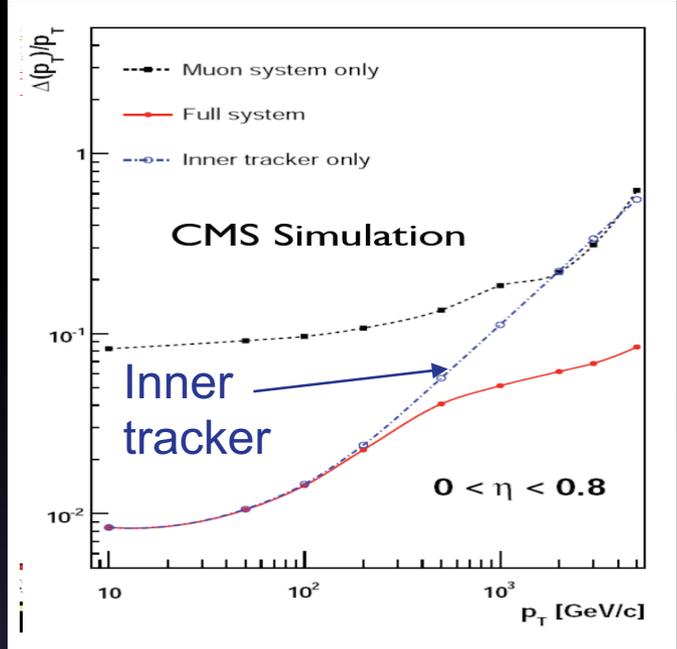
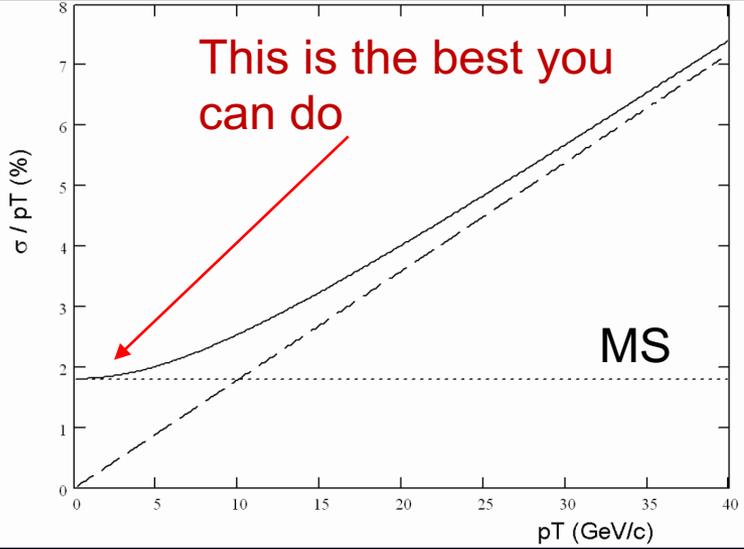
Radiation length=mean length of a material to reduce the energy of an electron by 1/e. It can be approximated as:

$$\left(\frac{\sigma_{p_T}}{p_T}\right)_{MS} = \frac{0.054}{LB\beta} \sqrt{\frac{L}{X_0} \sin \theta}$$

- Thickness of detector often expressed in 'fraction of radiation length'  $x/X_0$ :

Good momentum resolution requires long  $X_0$ , and therefore small Z and thin materials

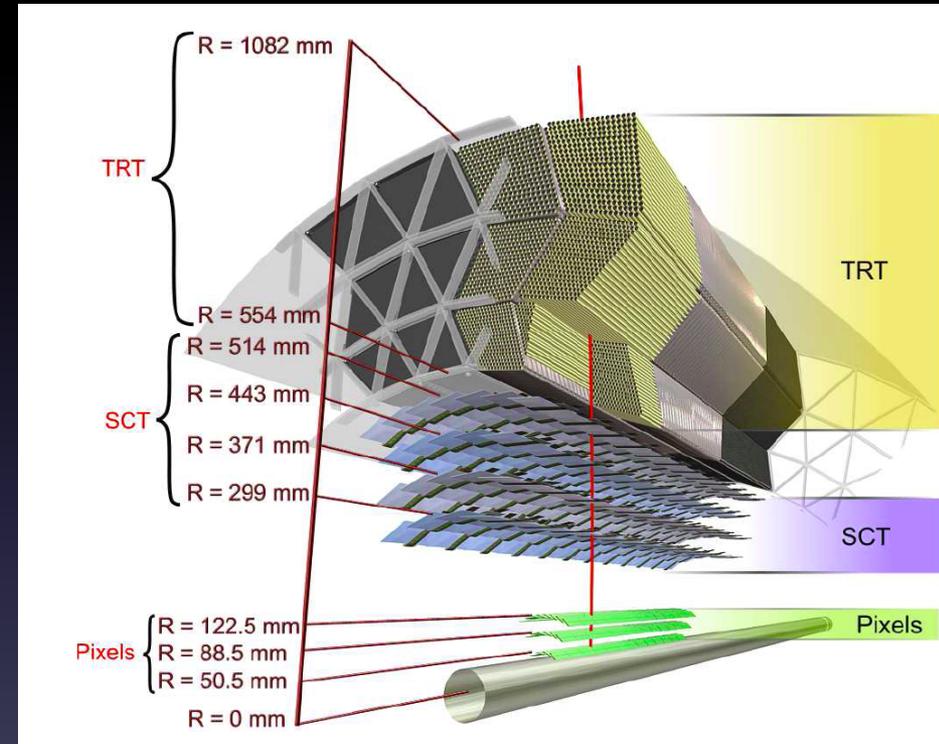
# Total momentum resolution



# Estimate the ATLAS momentum resolution

## Simplification:

- Assume high momenta (no MS)
- $R_{\min} = 5.05 \text{ cm}$ ,  $R_{\max} = 1082 \text{ cm}$
- Pixels (5cm to 12cm)
  - $N=3$  (up to 2012),  $\sigma = 12 \mu\text{m}$
- SCT (30cm to 55cm)
  - $N=4$  layers,  $\sigma = 16 \mu\text{m}$
- TRT (55cm to 105 cm)
  - $N = 36$ ,  $\sigma = 170 \mu\text{m}$
  - Use as a single point with  $\sigma = 28 \mu\text{m}$  at  $R = 80 \text{ cm}$  ( $= R_{\max} \Rightarrow L = 75 \text{ cm}$ )
- $N = 3 + 4 + 1 = 8$
- $\sigma = 12, 16, 28 \mu\text{m} \Rightarrow \langle \sigma \rangle \sim 16 \mu\text{m}$
- $L=75 \text{ cm}$



$$\left( \frac{\sigma_{p_T}}{p_T} \right)_{r\phi} = \frac{p_T}{0.3L^2B} \sqrt{\frac{720}{N+4}} \sigma_{r\phi} = 7.74 \frac{p_T}{0.3L^2B} \sigma_{r\phi}$$

# Estimate: ATLAS momentum resolution

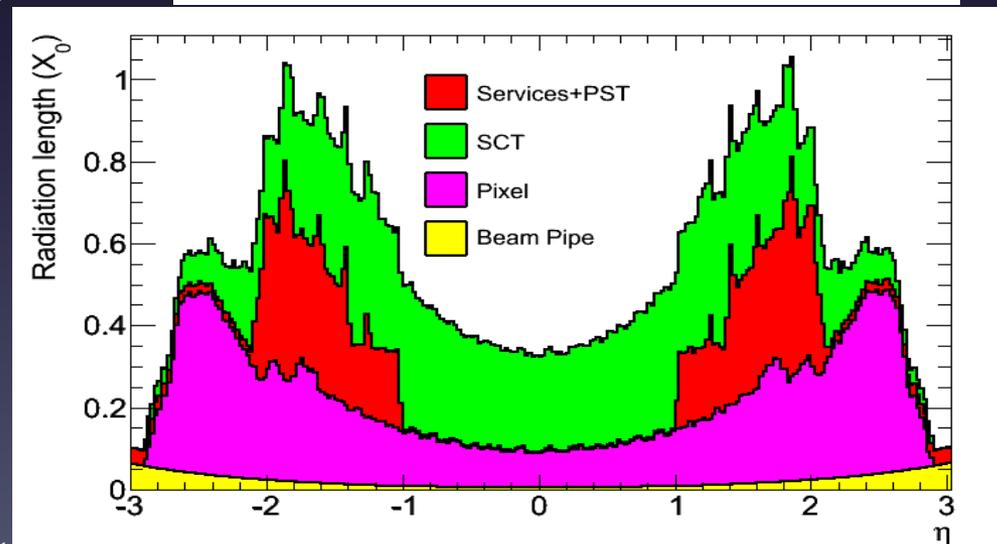
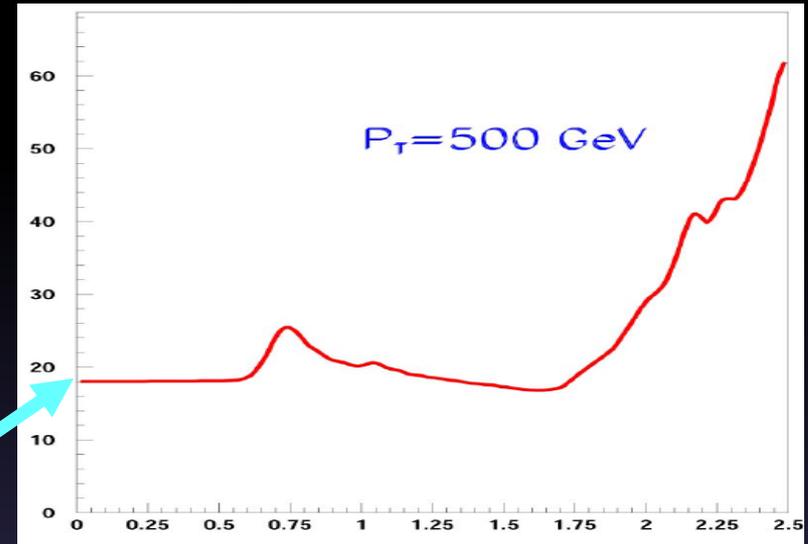
- $B=2T$ ,  $L=0.75m$

$$\left(\frac{\sigma_{p_T}}{p_T}\right)_{r\phi} = 7.74 \frac{p_T}{0.3L^2B} \sigma_{r\phi}$$

$$= 3.6 \times 10^{-4} p_T [GeV]$$

- At  $p_T=500$  GeV

$$\frac{dp}{p} = 18\%$$

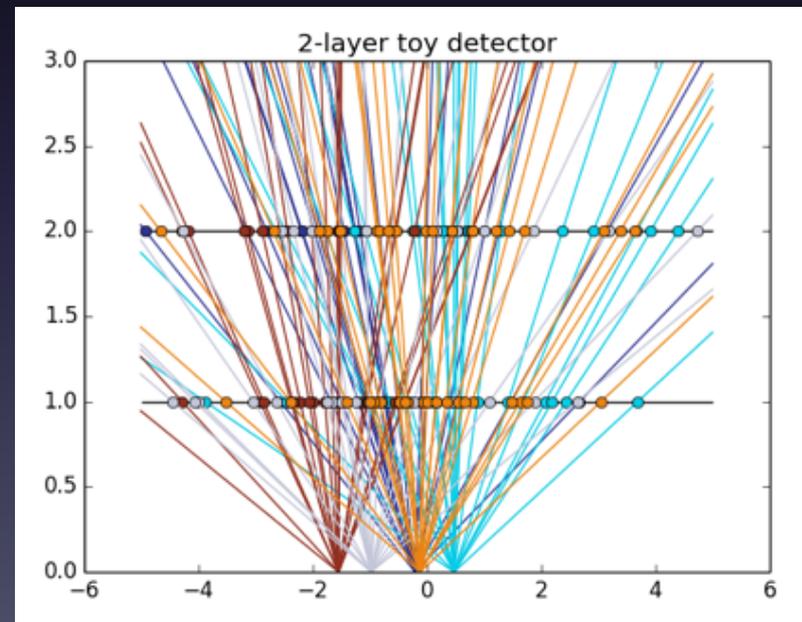
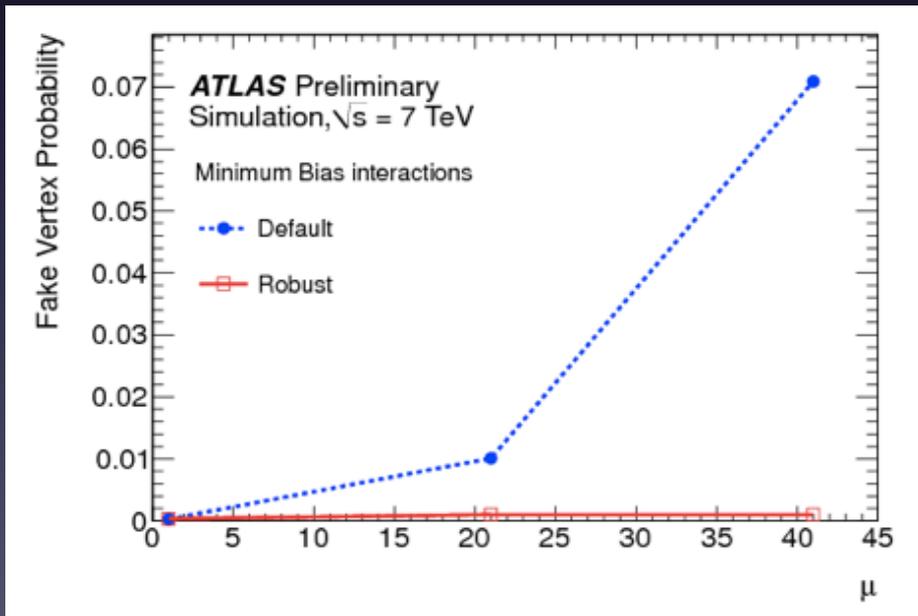
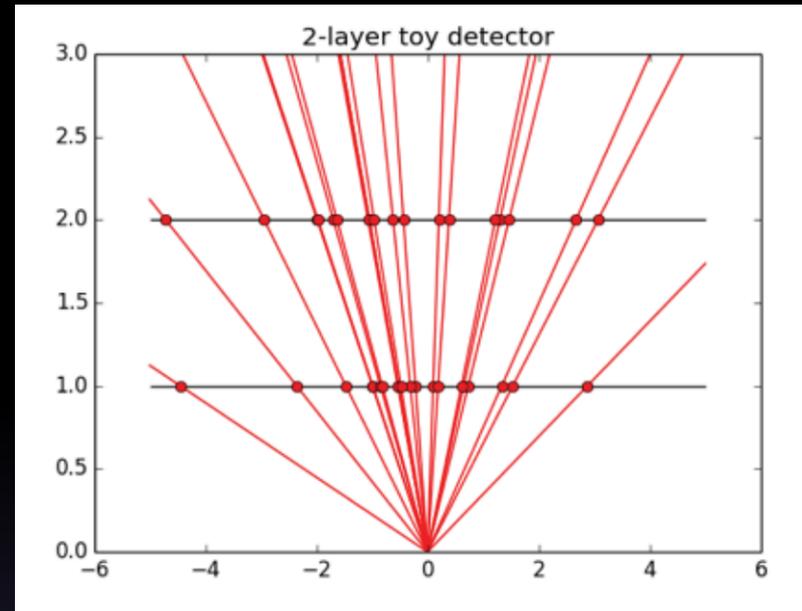




# Vertex

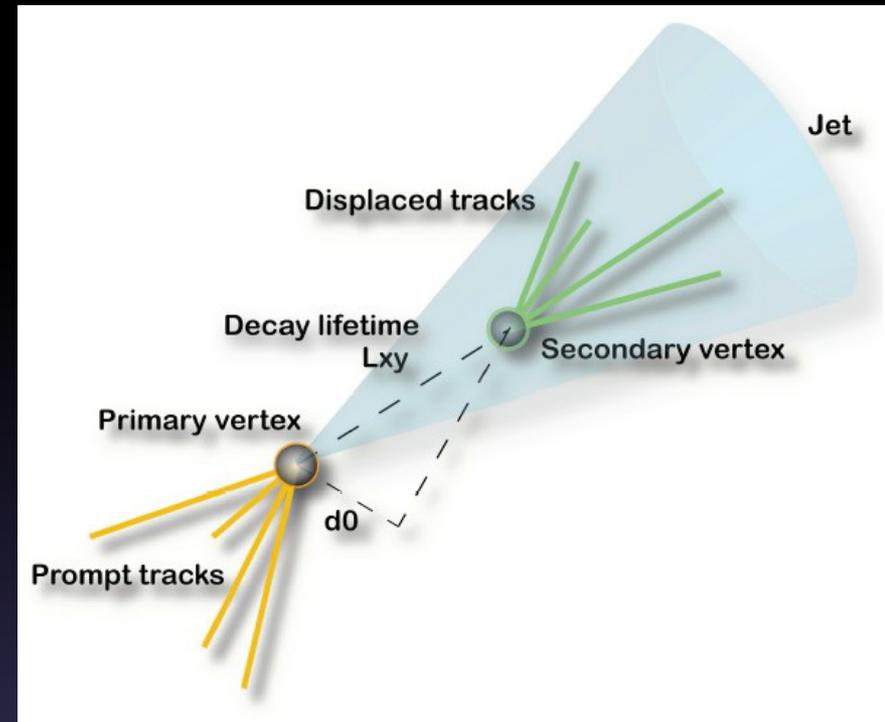
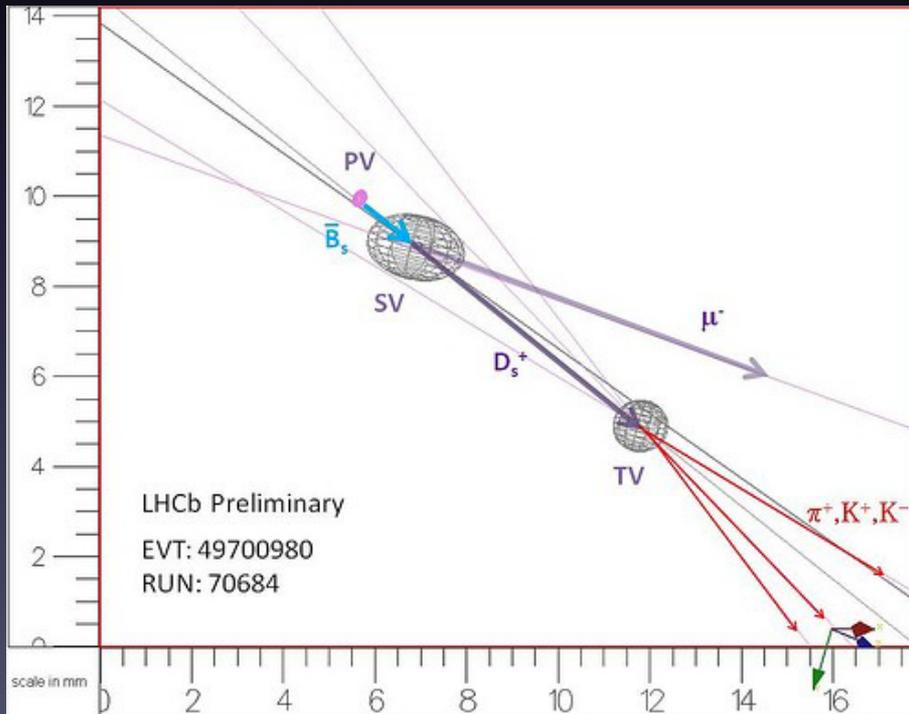
## reconstruction

- Use reconstructed tracks, to extrapolate back and find the primary vertex
- To maximise the physics potential, LHC runs in a regime of multiple instantaneous collisions: pile-up
- Pile-up renders tracks reconstruction and vertex finding more complex: more seeds and CPU time explodes



# Lifetime tagging

- Tracks with significant impact parameter,  $d_0$ , can be used to form a reconstructed secondary vertex
  - Essential to study the heavy quarks (t, b, c)
  - Tagging the Higgs since  $BR(H \rightarrow b\bar{b}) \approx 58\%$
  - Studying the Higgs potential (HH)



Example of a fully reconstructed event from LHCb, with primary, secondary and tertiary vertex.

# Impact parameter resolution

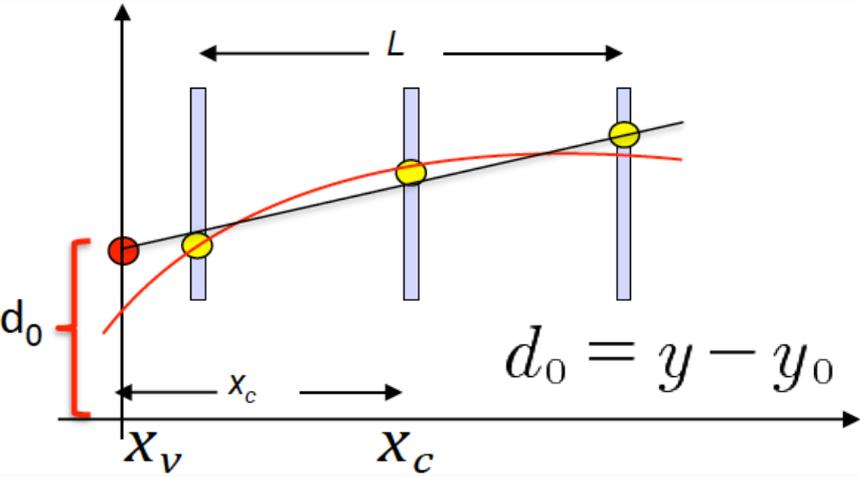
- Vertex extrapolation

- Linear (B=0)

$$y = a + bx$$

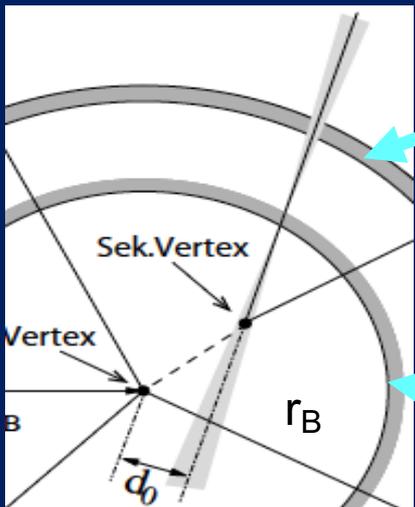
- Parabolic (with B field)

$$y = a + bx + \frac{1}{2}cx^2$$



- Linear approximation

$$\sigma_{d_0}^{meas} = \sqrt{\sigma_a^2 + x_0^2 \sigma_b^2} = \frac{\sigma_{meas}}{\sqrt{N}} \sqrt{1 + \frac{12(N-1)}{(N+1)} r^2}$$



First Layer MULTIPLE SCATTERING

$$\sigma_{d_0}^{MS} = \theta_0 r_B$$

Beam Pipe

$r =$  extrapolation length

$$r = \frac{x_0}{L}$$



# Impact parameter resolution

$$r = \frac{x_0}{L}$$

- In the linear case

$$\sigma_{d_0} = \sigma_{d_0}^{meas} \oplus \sigma_{d_0}^{MS} = \frac{\sigma_{meas}}{\sqrt{N}} \sqrt{1 + \frac{12(N-1)}{(N+1)} r^2} \oplus \theta_0 r_B$$

- To have good impact parameter resolution:
  - Small measurement errors  $\sigma_{meas}$
  - Large lever arm  $L \implies r$
  - Place measurement plane as near as possible to the production point: small  $x_0 \implies r$
  - Limit multiple scattering  $\implies$  Low Z thin beam pipe and measurement layers
  - Increasing number of points also improves the  $d_0$  resolution ( $1/\sqrt{N}$ )



# Example ATLAS

- ATLAS Pixel detector

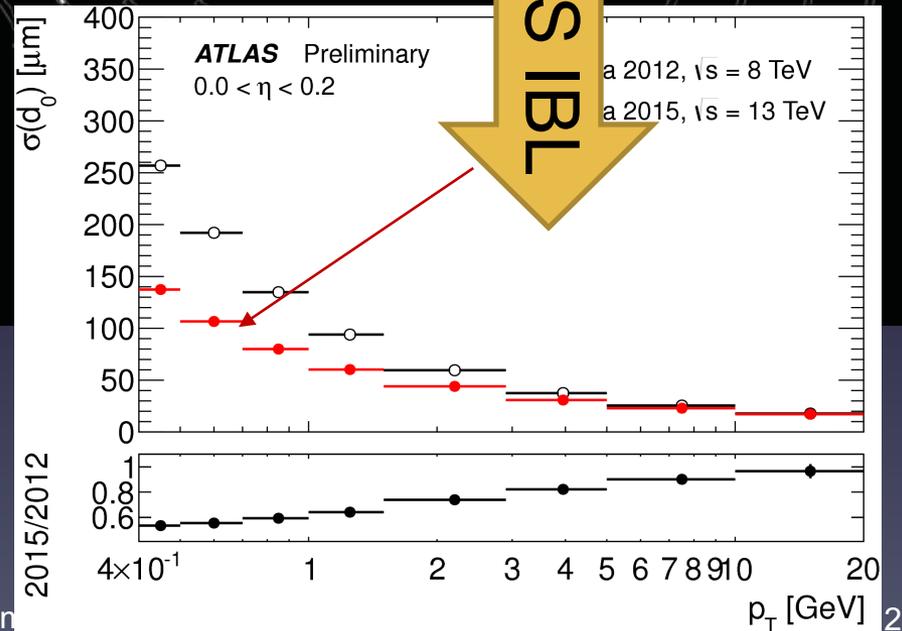
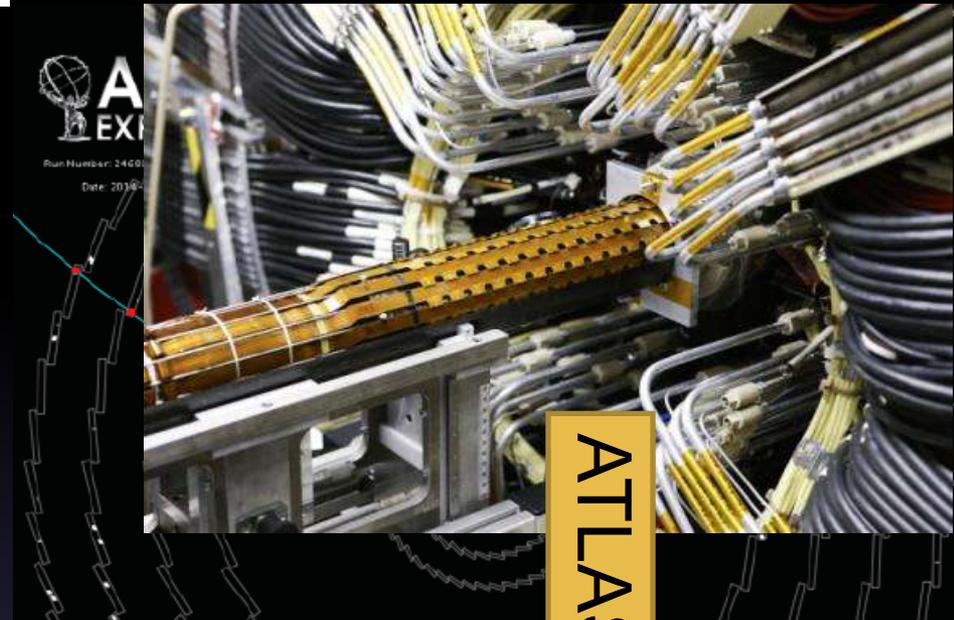
- $N = 3, \sigma = 10 \mu m$
- $x_1 = 5.05 \text{ cm}$
- $x_2 = 8.85 \text{ cm}$
- $x_3 = 12.25 \text{ cm}$
- $L = 7.2 \text{ cm}$
- $r = x_2/L = 1.22$

- Neglecting Multiple scattering

$$\sigma_{do}^{meas} = \frac{\sigma_{meas}}{N} \sqrt{1 + \frac{12(N-1)}{(N+1)} r^2} = 18 \mu m$$

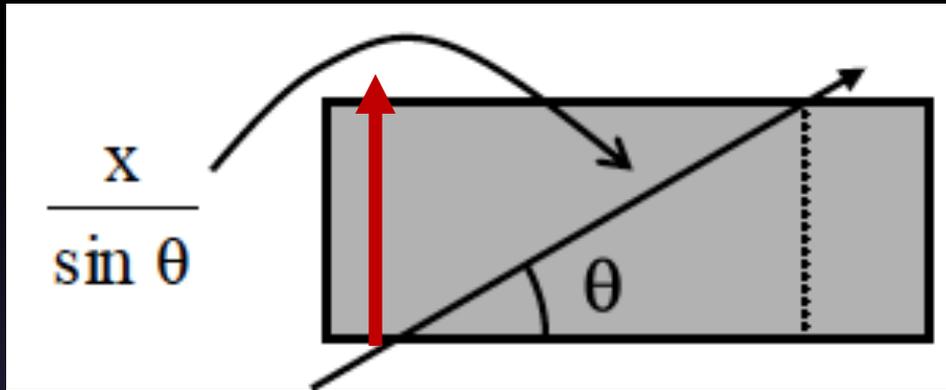
- With IBL:  $N = 3, \sigma = 10 \mu m$  and  $x_1 = 3.55 \text{ cm}$

$$\sigma_{do}^{meas} \approx 10 \mu m$$



# Tracker resolution with MS

- For low  $p_T$  tracks the momentum resolution and the impact parameter resolution are dominated by multiple scattering
- The amount of material traversed by the particles depends on polar angle



## Momentum resolution:

$$\frac{\sigma_p}{p^2} \rightarrow k_p \frac{\sqrt{x/X_0}}{p \sqrt{\sin \theta}}$$

## Impact parameter resolution:

$$\sigma_{d_0} \rightarrow k_{d_0} \frac{\sqrt{x/X_0}}{p \sqrt{\sin \theta}}$$

- The MS error and the point measurement error are independent of each other,
- The total error is the sum in quadrature of the 2 terms
- ATLAS detector Monte Carlo studies show:

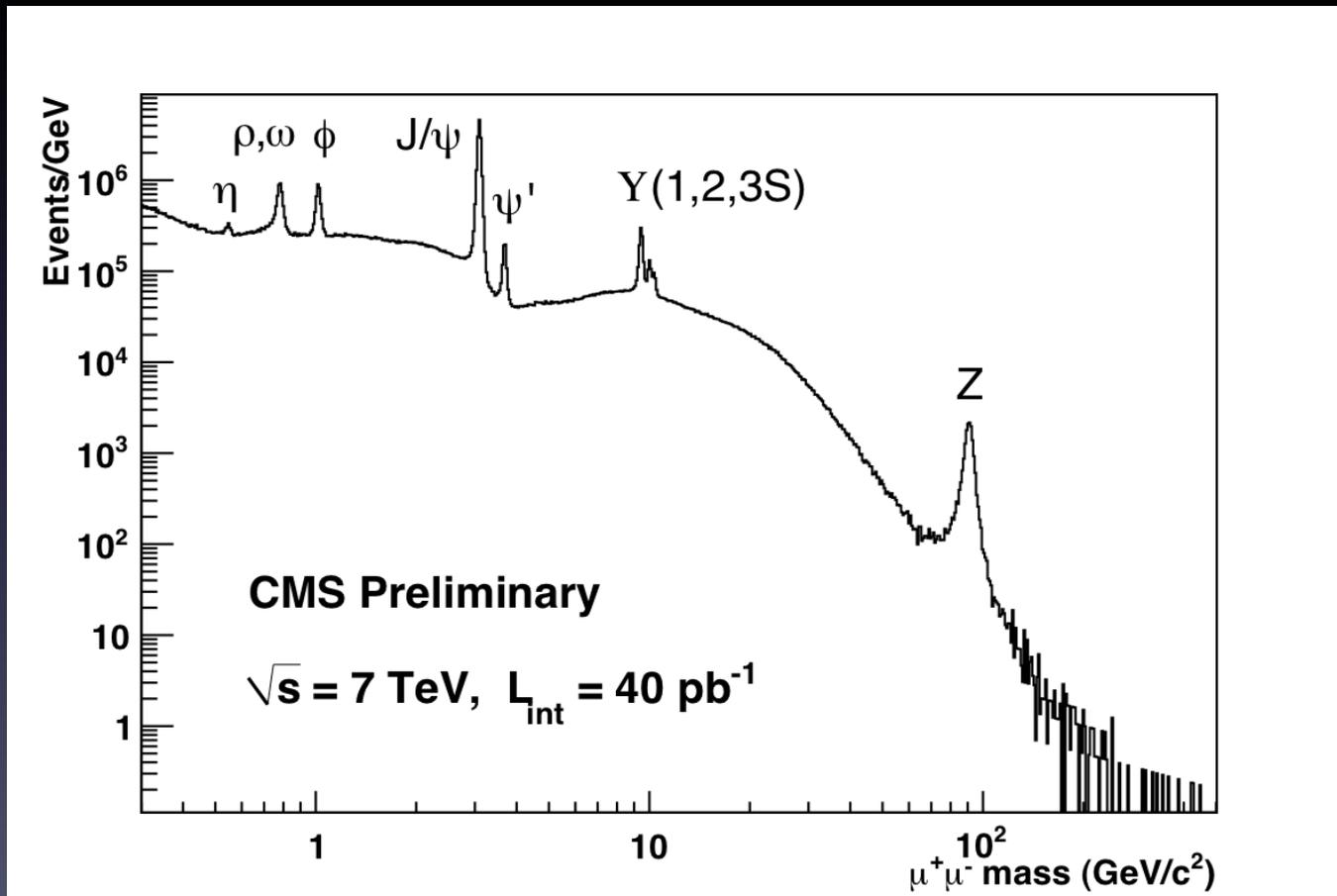
$$\frac{\sigma_{pT}}{p_T^2} = 0.00036 \oplus \frac{0.013}{p_T \sqrt{\sin \theta}} (1/GeV)$$

$$\sigma_{d_0} = 11 \mu m \oplus \frac{73 \mu m}{p_T \sqrt{\sin \theta}}$$



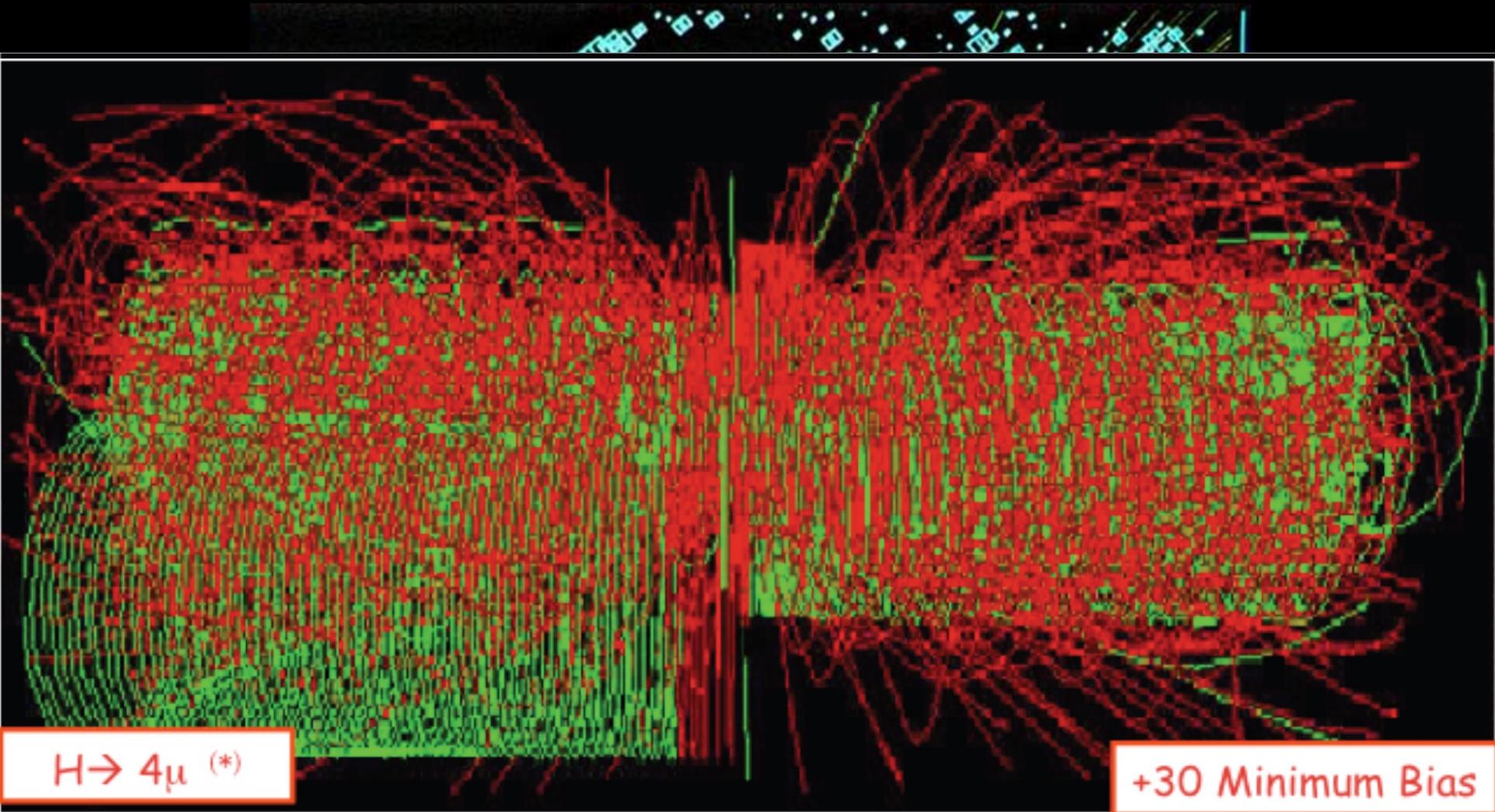
# Systematic effects

- Alignment
- Knowledge of the B field
- Material





# Tracking is more challenging

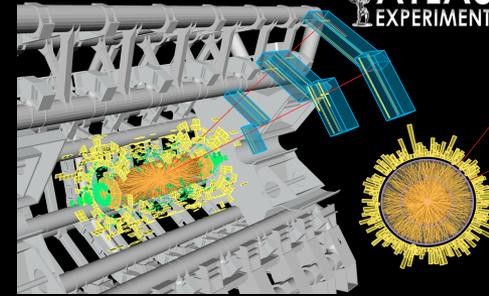


Simulation.  
Higgs boson at LHC



# Tracking at the LHC

Run 169226, Event 379791  
Time 2010-11-16 02:53:54 CET



- ~1200 tracks every 25 ns or  $\sim 10^{11}$ /second
  - high radiation dose  $10^{15}$  n<sub>eq</sub> / cm<sup>2</sup> / 10 yrs
  - 600 kGy (60 Mrad) through the ionisation of mipis in 250  $\mu$ m bulk silicon

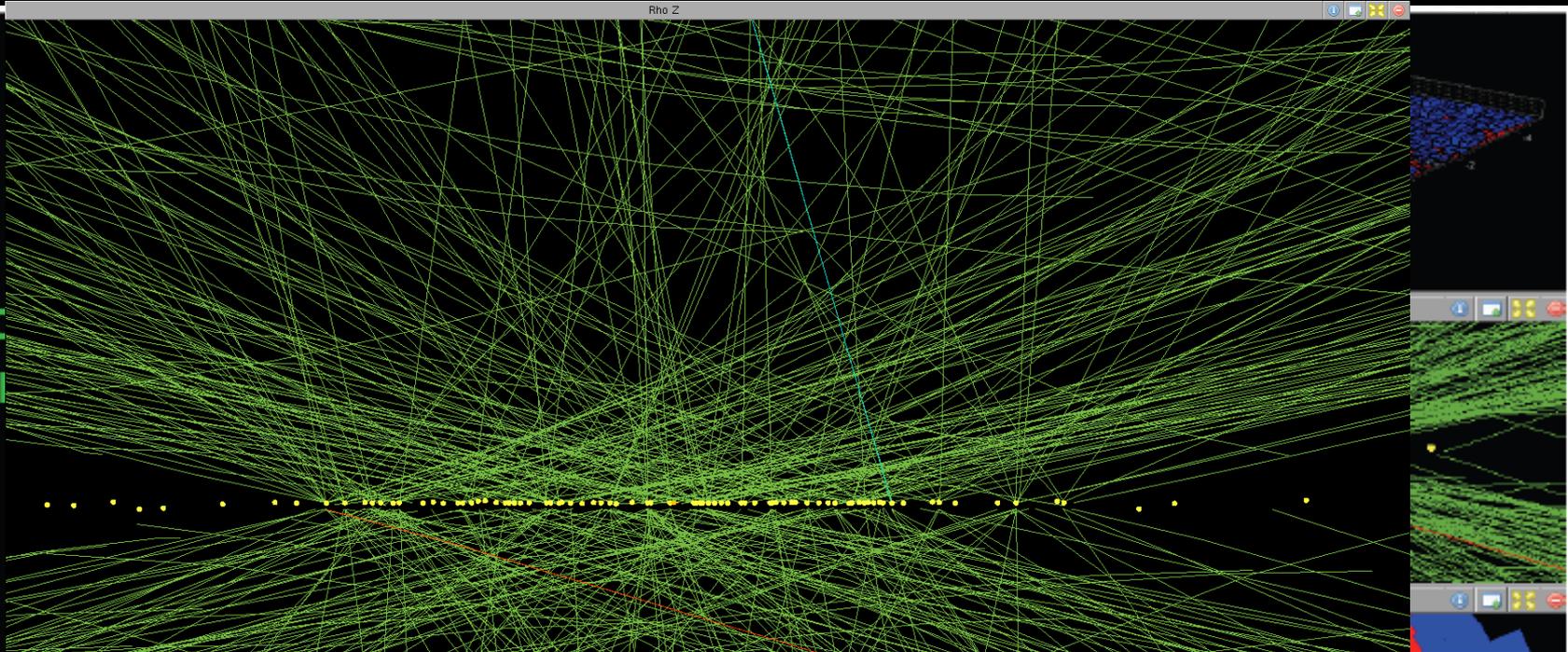
## Requirements:

- Response times of the detector elements and their read-out electronics must be fast enough to process the event in less than 25 ns to minimize the pile-up to one bunch crossing;
- High granularity to keep the occupancy low;
- All elements of the detector, including active material, read-out electronics and cables must be rad-hard.



# Tracking and Vertex Detectors

- Solid state detectors especially silicon offer high segmentation
- Determine position of primary interaction vertex and secondary decays



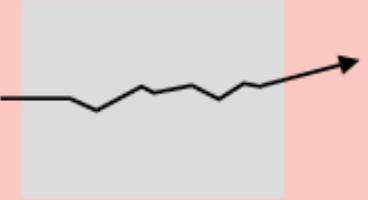
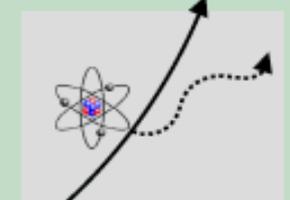
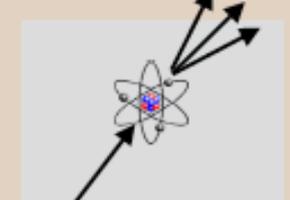
Track  
work

This would have not been possible  
without semiconductor (pixel and strip)  
trackers



- The interaction of a particle with matter can be used as a working principle for a particle detector.
- The interaction of a particle with matter impact the precision of the measurement



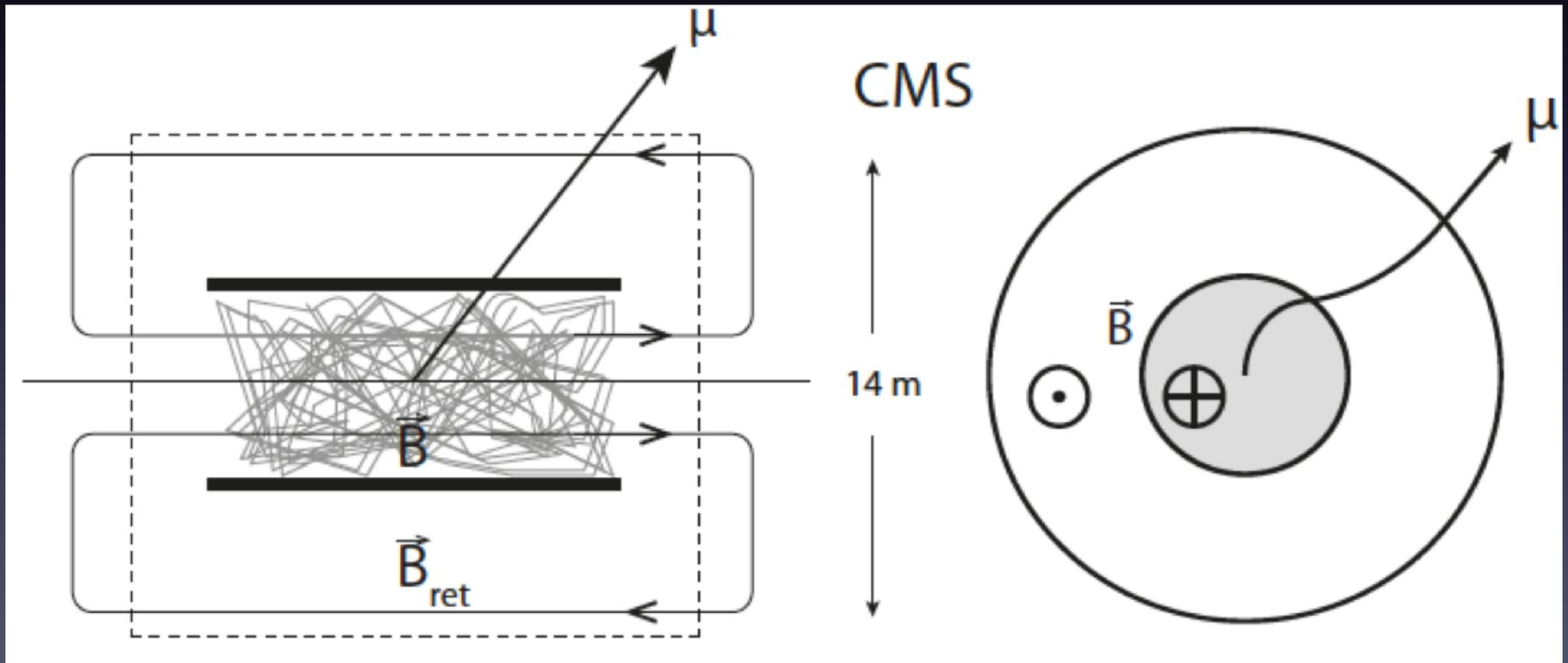
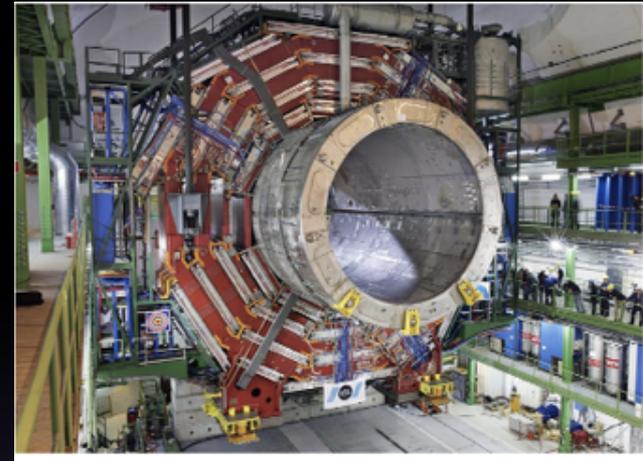
Type	particles	fund. parameter	characteristics	effect
<b>Multiple Scattering</b> 	all charged particle	radiation length $X$	almost gaussian average effect 0 depends $\sim 1/p$	deflects particles, increases measurement uncertainty
<b>Ionisation loss</b> 	all charged particle	effective density $A/Z * \rho$	small effect in tracker, small dependence on $p$	increases momentum uncertainty
<b>Bremsstrahlung</b> 	all charged particle, dominant for e	radiation length $X$	highly non- gaussian, depends	introduces measurement bias
<b>Hadronic Int.</b> 	all hadronic particles	nuclear interaction length $\Lambda$	destroys particle, rather constant effect in $p$	main source of track reconstruction inefficiency



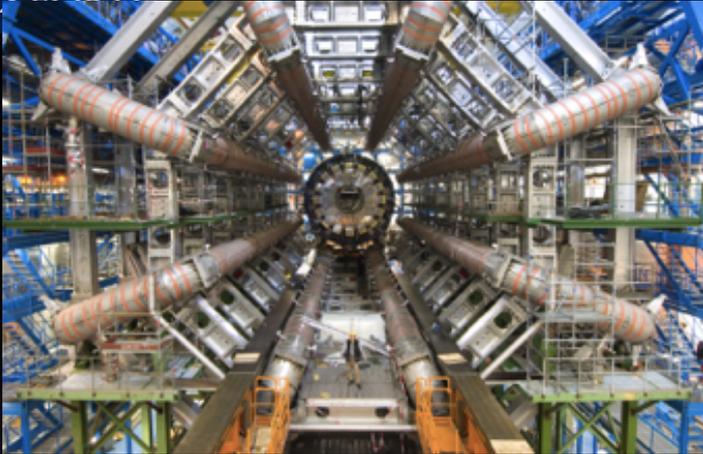
# Measuring Muons

## CMS:

- measurement of momentum in tracker and B return flux;
- Solenoid with Fe flux return
- Property:  $\mu$  tracks point back to vertex in r-z plane

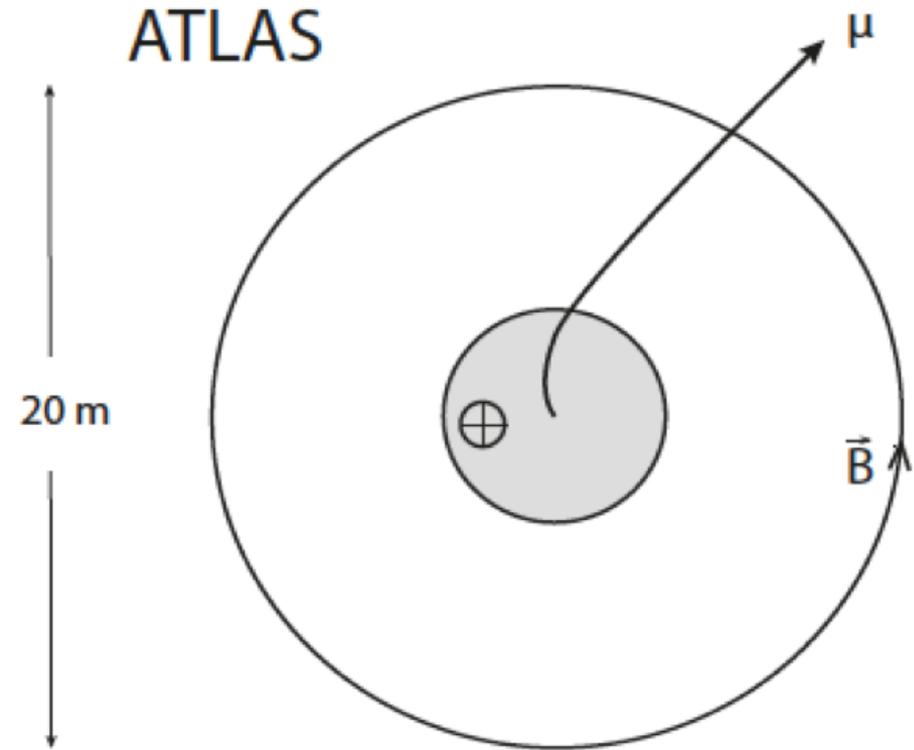
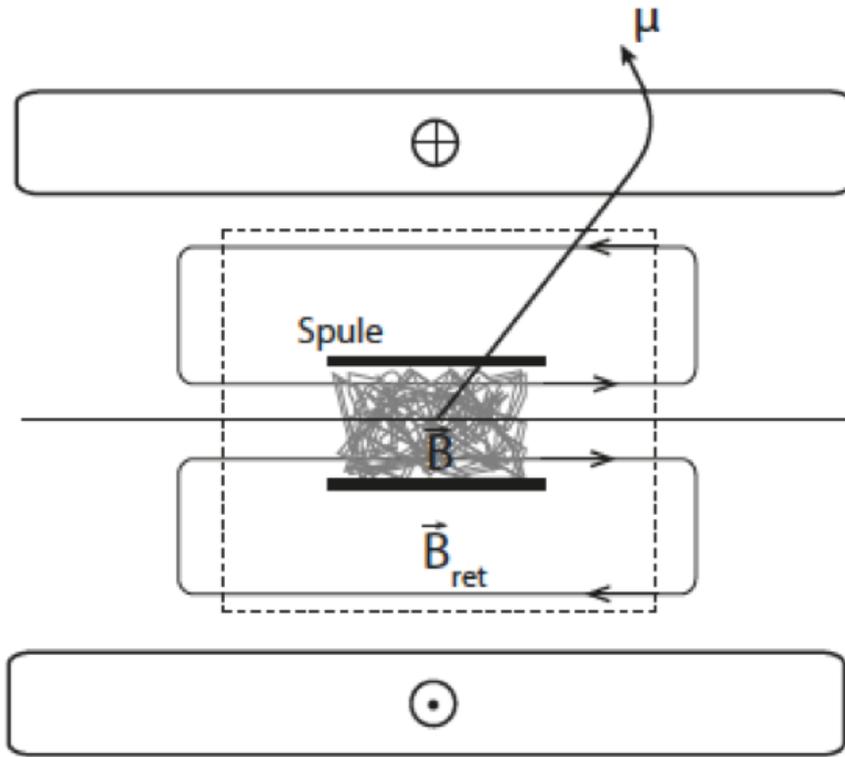


# Measuring Muons



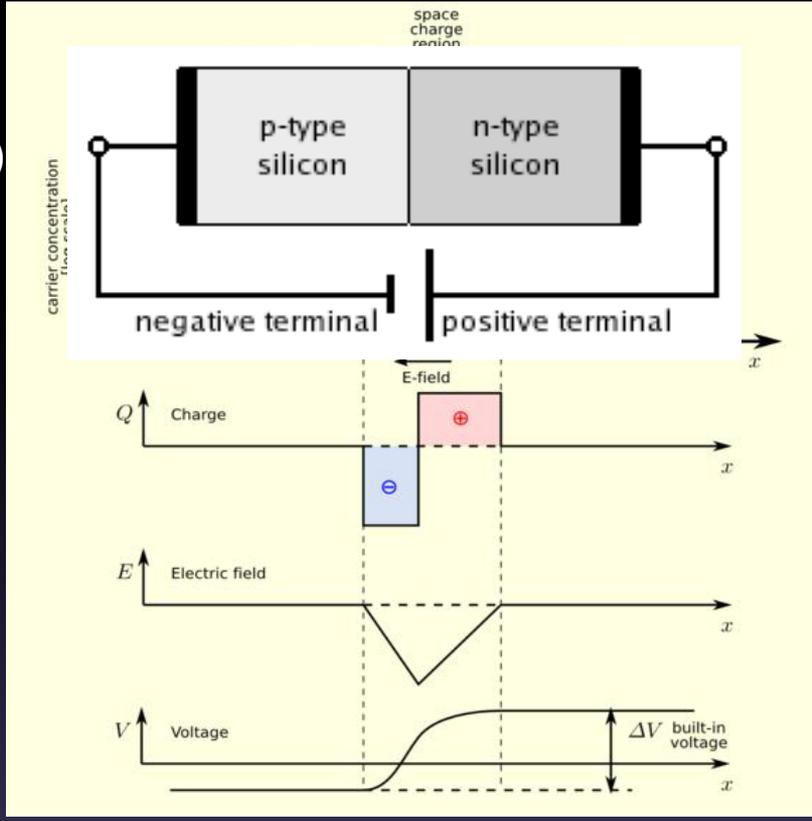
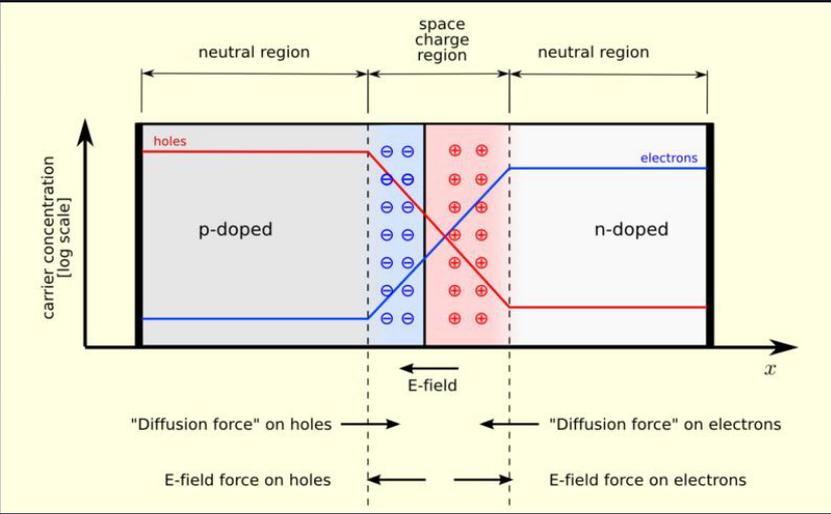
## ATLAS

- standalone  $\mu$  momentum measurement
- Air-core toroid safe for high multiplicities
- Property:  $\sigma_p$  flat with  $\eta$



# Silicon Detectors

- A silicon detector is a p-n diode
  - n-type ( P, As, Sb doping  $\Rightarrow$  more electrons)
  - p-type ( B, Al, Ga doping  $\Rightarrow$  more holes)
- p-n junction without external voltage
  - Free charges diffuse until equilibrium is reached and create the built-in potential



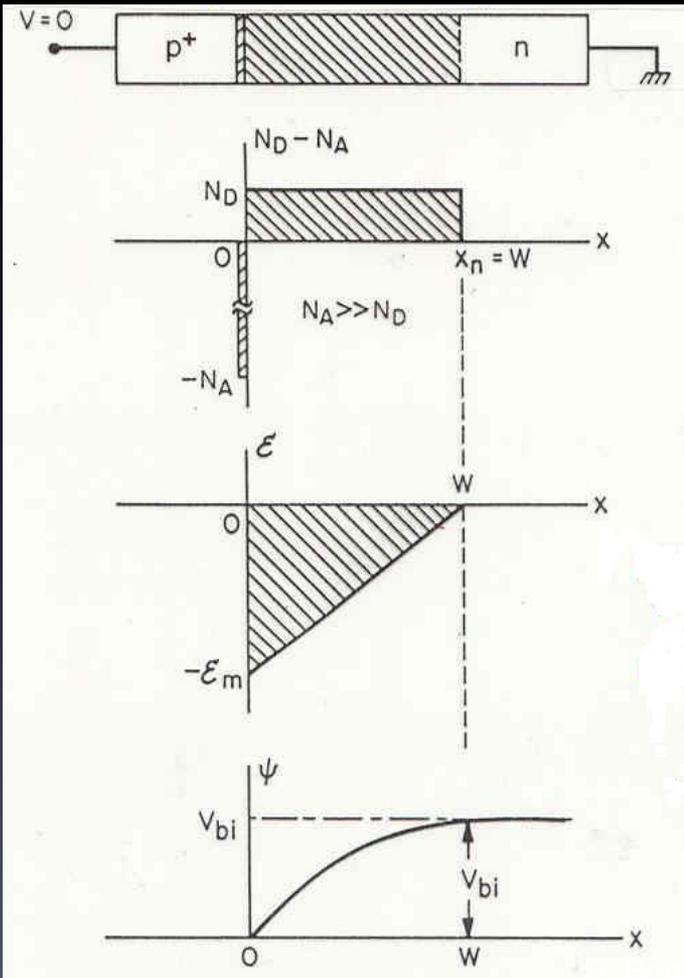
The  $W$  of the depletion region can be found by applying Poisson equation and depends on  $V$

$$W = W_p + W_n = \sqrt{\frac{2\epsilon}{q} \left( \frac{1}{N_A} + \frac{1}{N_D} \right) (V_{bi} + V)}$$

- The space charge (depletion) region can be made bigger by applying a reverse bias voltage

# p<sup>+</sup>-n sensors

- P<sup>+</sup>-n sensors consists of a thin ( $\sim\mu\text{m}$ ), highly doped p<sup>+</sup> ( $\sim 10^{19}\text{ cm}^{-3}$ ) layer on lightly doped n- ( $\sim 10^{12}\text{ cm}^{-3}$ ) substrate
- Since  $N_A \gg N_D$  most of the n-type silicon is depleted



$$W = \sqrt{\frac{2\epsilon}{q} \left( \frac{1}{N_A} + \frac{1}{N_D} \right) (V_{bi} + V)}$$

$$\approx \sqrt{\frac{2\epsilon}{q} \frac{1}{N_D} V}$$

$$W \sim \sqrt{2\epsilon_0 \epsilon_r \mu \rho |V|}$$

$$\rho = \frac{1}{e\mu N_D}$$

V ... External voltage

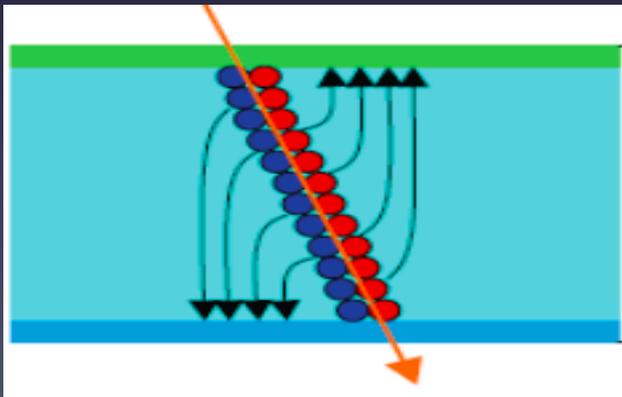
$\rho$ .... resistivity

$\mu$  ... mobility of majority charge carriers

$N_{\text{eff}}$ ..effective doping concentration

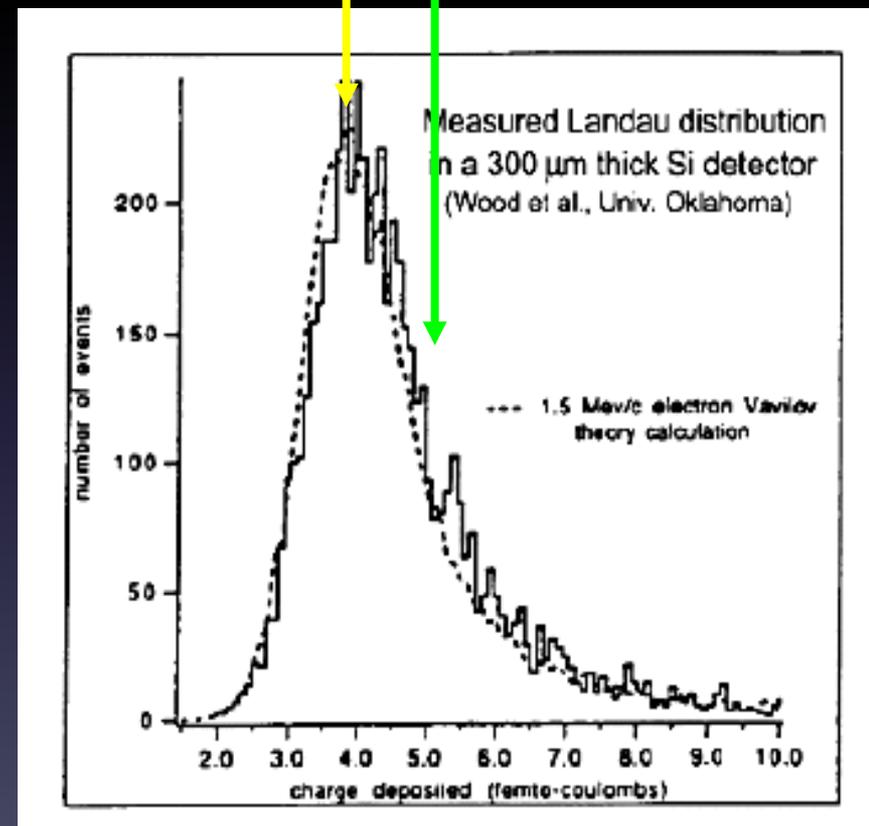
# Signal

- The signal generated in a silicon detector depends on the thickness of the depletion zone and on the  $dE/dx$  of the particle.
  - The distribution is given by the Landau distribution
  - In silicon the most probable  $dE/dX$  of a MIP is  $300 \text{ eV}/\mu\text{m}$  and the mean ionization energy  $I_0 = 3.62 \text{ eV}$ . Therefore a charged particle creates  $\approx 80 \text{ e-h}^+/\mu\text{m}$ .
  - For  $300 \mu\text{m}$  silicon the most probable charge is  $\approx 24000 \text{ e-h}$  pairs



Most probable charge  $\approx 0.7 \times$  mean

Mean charge

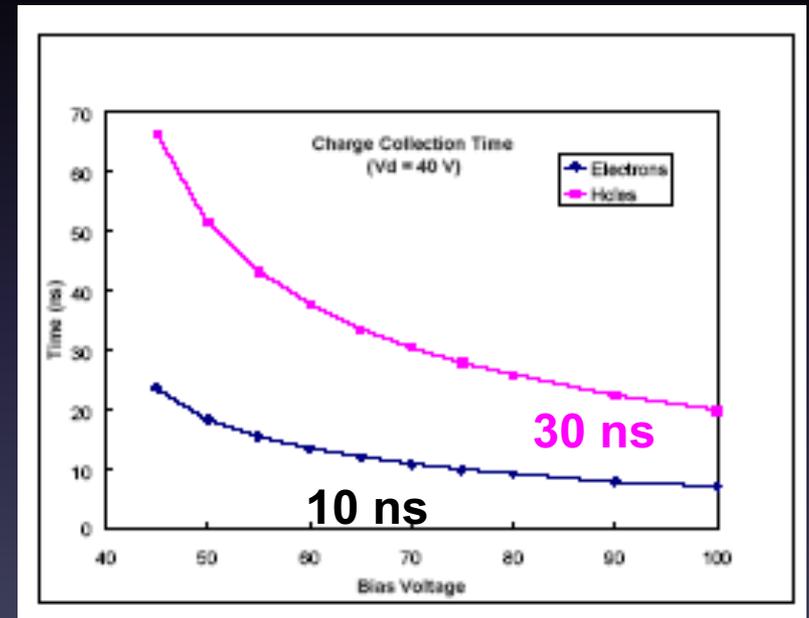
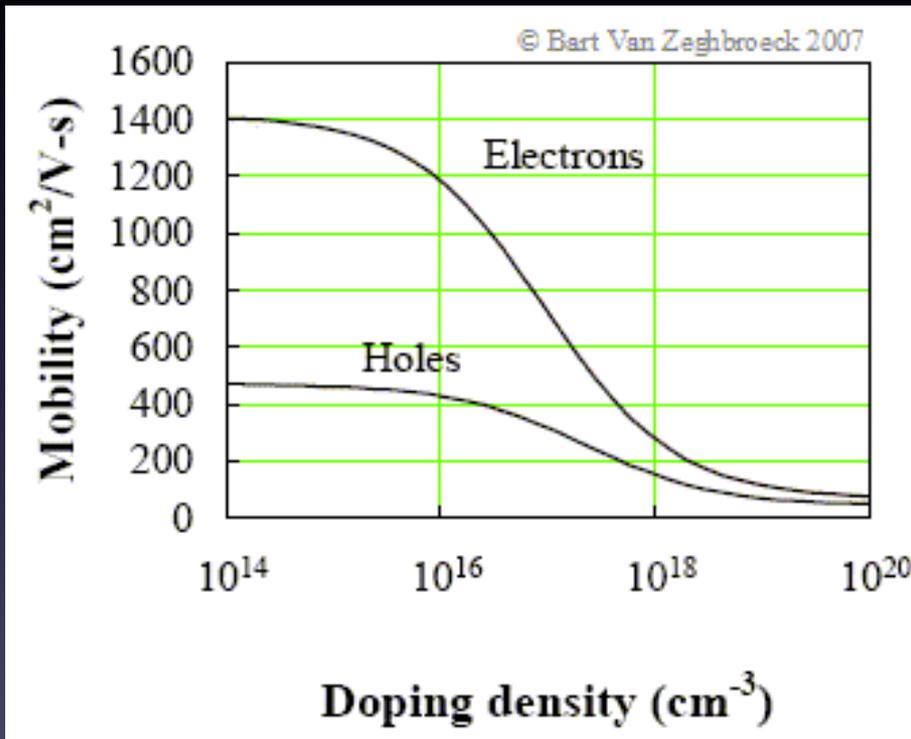


# Collection by drift

- Electrons and holes move in an E field  $F=qE$

$$v_{e,h} = \mu_{e,h} E$$

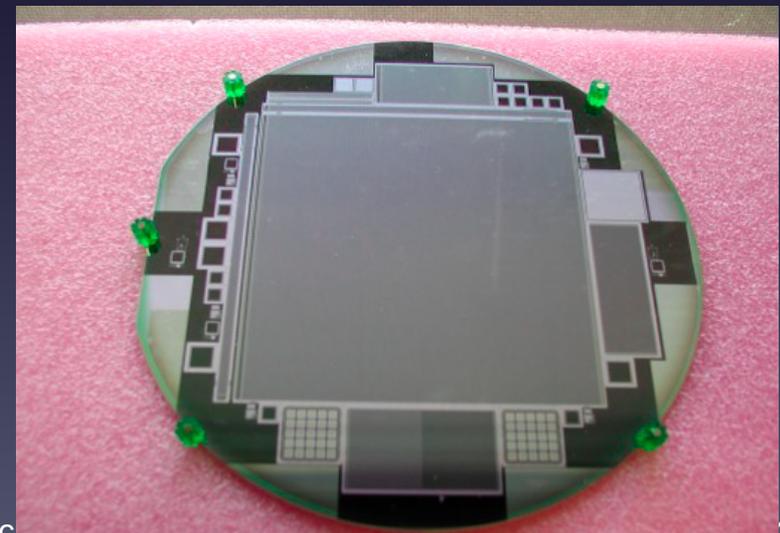
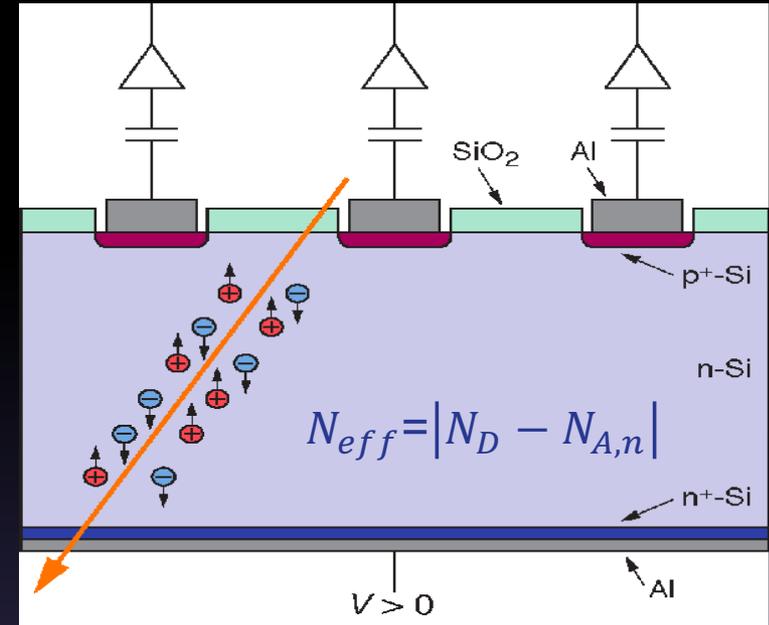
- The time required for a carrier to traverse the sensitive volume is the collection time.



- The collection time can be reduced by over-biasing the sensor

# DC Silicon Strip Detectors

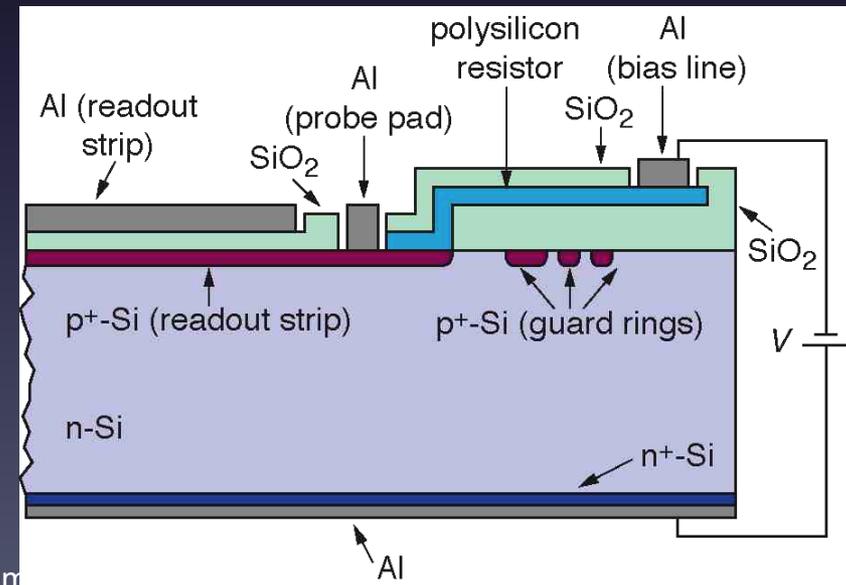
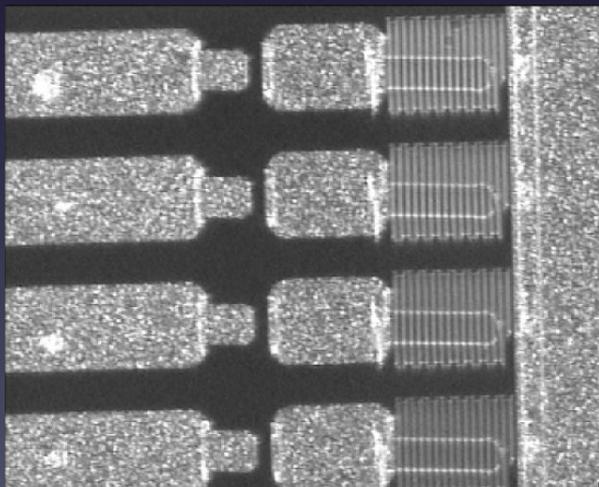
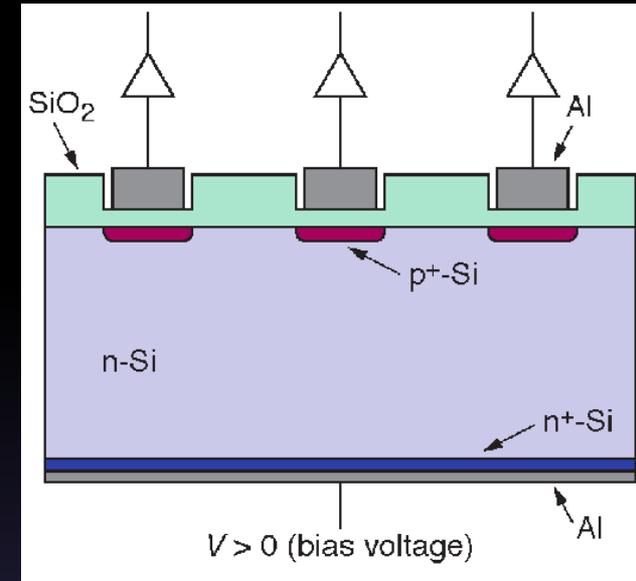
- The drift (current) creates a signal which is amplified by an amplifier connected to each strip allowing precise position determination
- Standard configuration:
  - p<sup>+</sup>n junction:  $N_A \approx 10^{19} \text{ cm}^{-3}$ ,  $N_D \approx 1-5 \cdot 10^{12} \text{ cm}^{-3}$
  - Substrate n doped ( $\sim 2-10 \text{ k}\Omega\text{cm}$ ) and  $\sim 300\mu\text{m}$  thick
  - n<sup>+</sup> layer on backplane to improve ohmic contact
  - Aluminum metallization





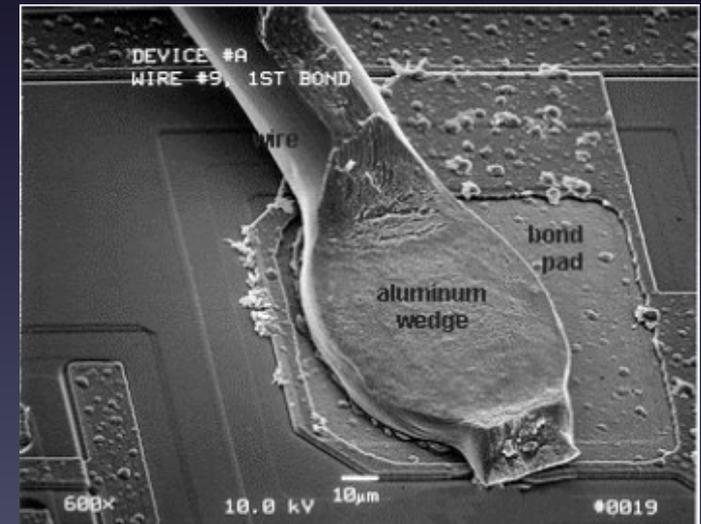
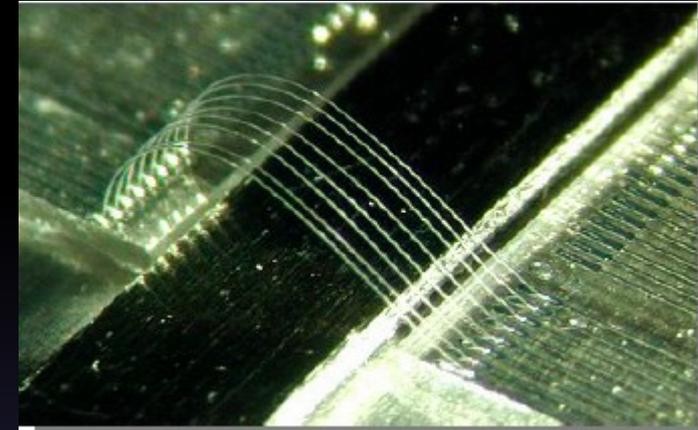
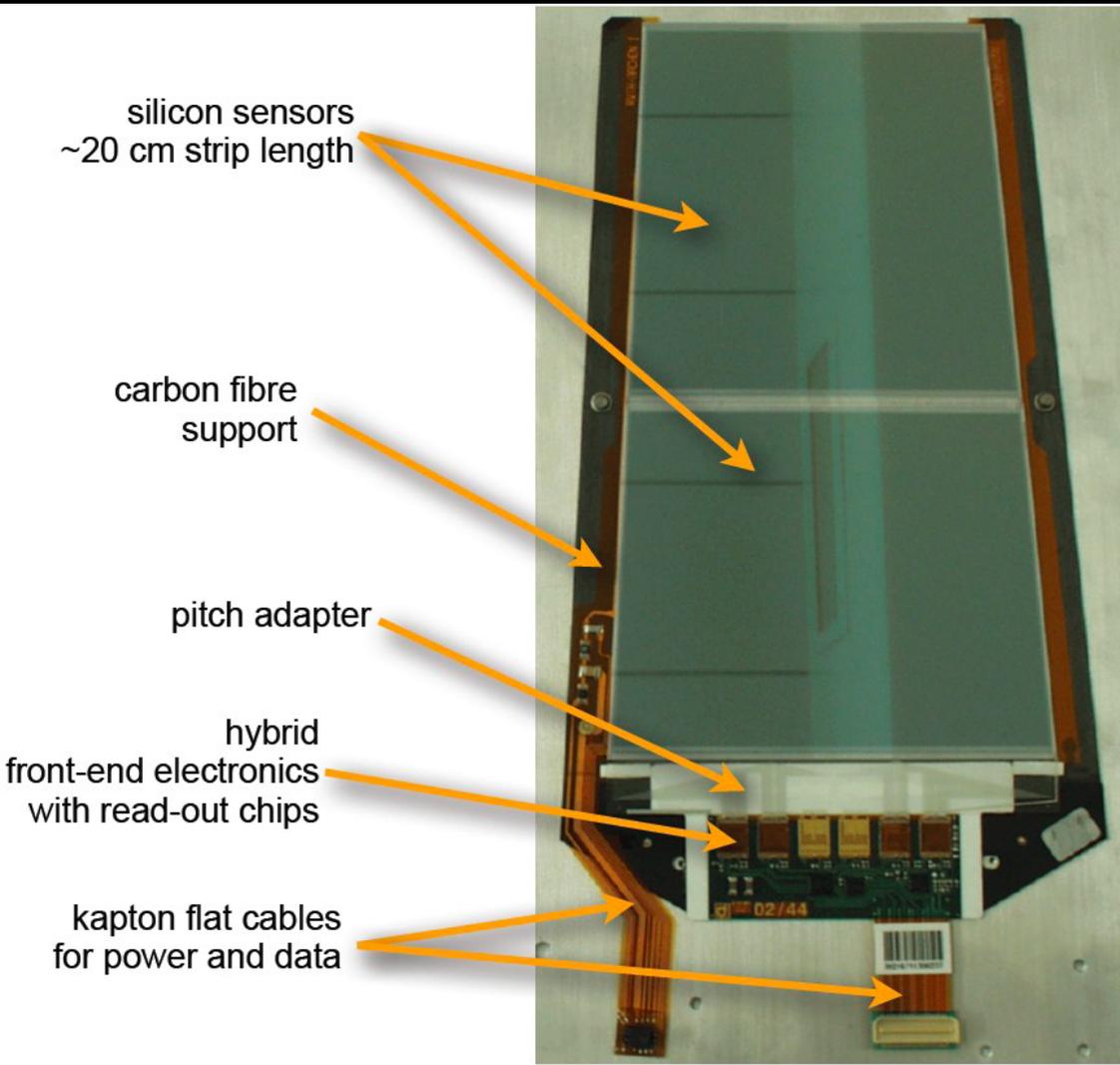
# AC coupled Strip Detector

- AC coupling blocks DC leakage current
- Integration of coupling capacitances in standard planar process.
  - Deposition of  $\text{SiO}_2$  with a thickness of 100–200 nm between p+ and aluminum strip
  - Increase quality of dielectric by a second layer of  $\text{Si}_3\text{N}_4$ .
- Coupling capacitance  $\approx 8\text{--}2 \text{ pF/cm}$
- Long poly silicon resistor with  $R > 1\text{M}\Omega$  to connect the bias voltage to the strips:





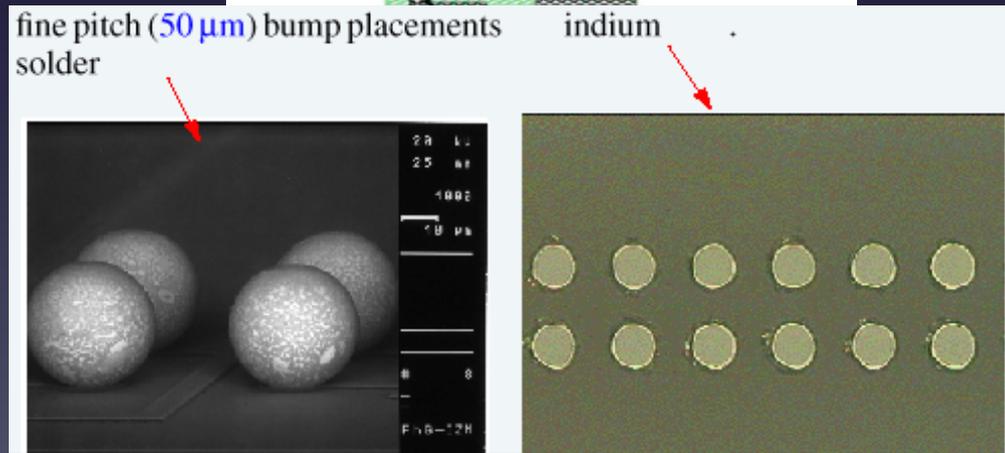
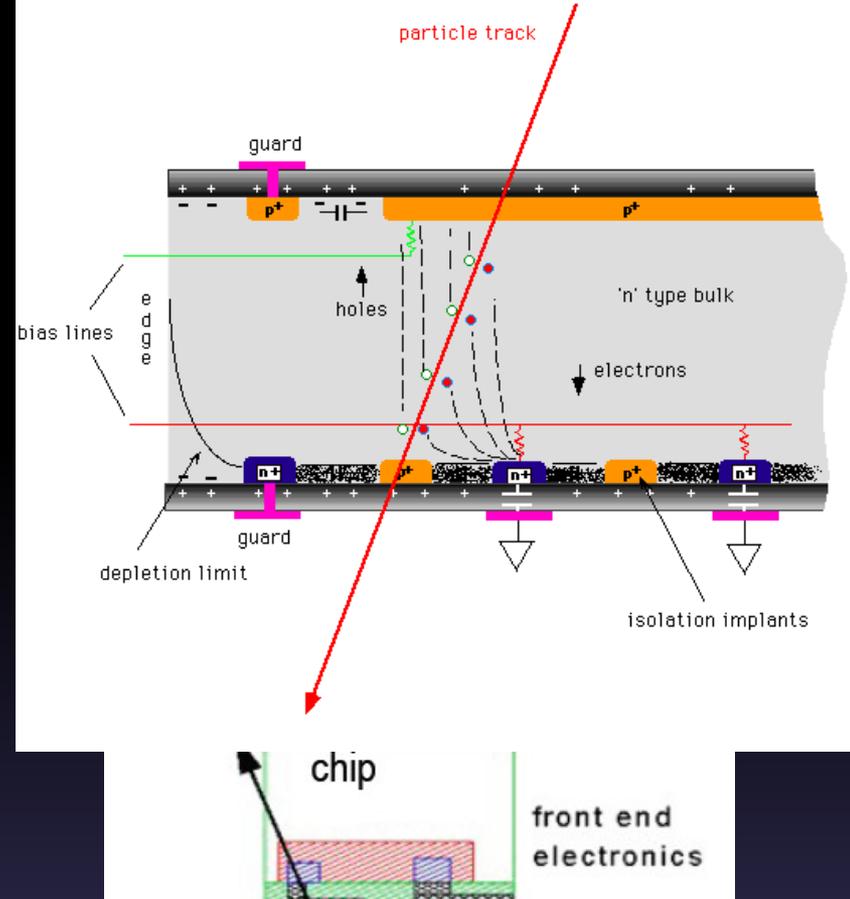
# A typical strip module (CMS)





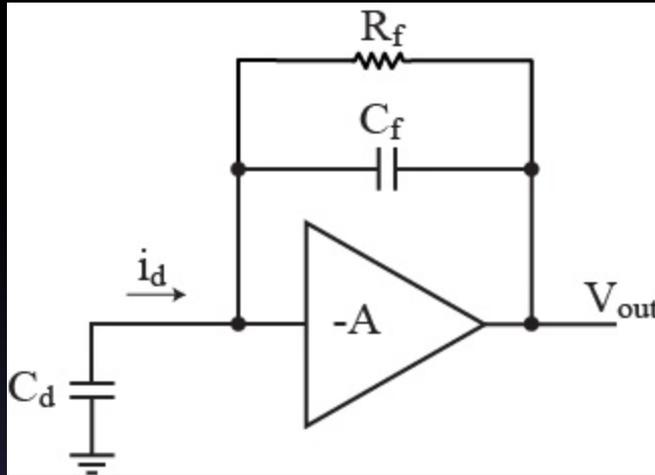
# Pixel detector

- Advantages
  - Pixel detectors provides space-point information removing hit ambiguities
- Small pixel area
  - low detector capacitance ( $\approx 1$  fF/Pixel)
  - large signal-to-noise ratio (e.g. 150:1).
- Small pixel volume
  - low leakage current ( $\approx 1$  pA/Pixel)
- $n^+$ -on n for the LHC
  - Electron have faster collection time
- Disadvantages:
  - Large number of readout channels
  - Large bandwidth
  - Large power consumption
  - Bump bonding is costly and complex



# Readout

- The signal of a silicon detector is readout by a charge sensitive amplifier



$$V_o = \frac{Q_D}{C_f}$$

$$\tau_f = R_f C_f$$

- The most simple CSA has a feedback capacitor  $C_f$  between the input and output stores the charge from the detector.
- The gain of the preamplifier is  $1/C_f$ .
- The resistor in parallel with the feedback capacitor can be used to reset the CSA
- Each pulse of current from the detector causes an output voltage proportional to the integral of the detector current

$$V_{out}(t) \propto Q(t) = \int i_d d\tau$$



# Readout Noise

- Noise is given as “equivalent noise charge” ENC.

$$ENC = \frac{\text{noise output voltage (rms)}}{\text{signal output voltage for the input charge of } 1e^-}$$

$$ENC_{tot}^2 = ENC_{shot}^2 + ENC_{therm}^2 + ENC_{1/f}^2$$

Reference  
Rossi, Fischer,  
Rohe, Wermes  
Pixel Detectors

$$ENC_{shot} = \sqrt{\frac{I_{leak}}{2q} \tau_f} = 56e^- \times \sqrt{\frac{I_{leak} \tau_f}{nA \mu s}}$$

$$ENC_{therm} = \frac{C_f}{q} \sqrt{\langle v_{therm}^2 \rangle} = \sqrt{\frac{kT}{q} \frac{2C_D}{3q} \frac{C_f}{C_{load}}} = 104e^- \times \sqrt{\frac{C_D}{100 \text{ fF}} \frac{C_f}{C_{load}}}$$

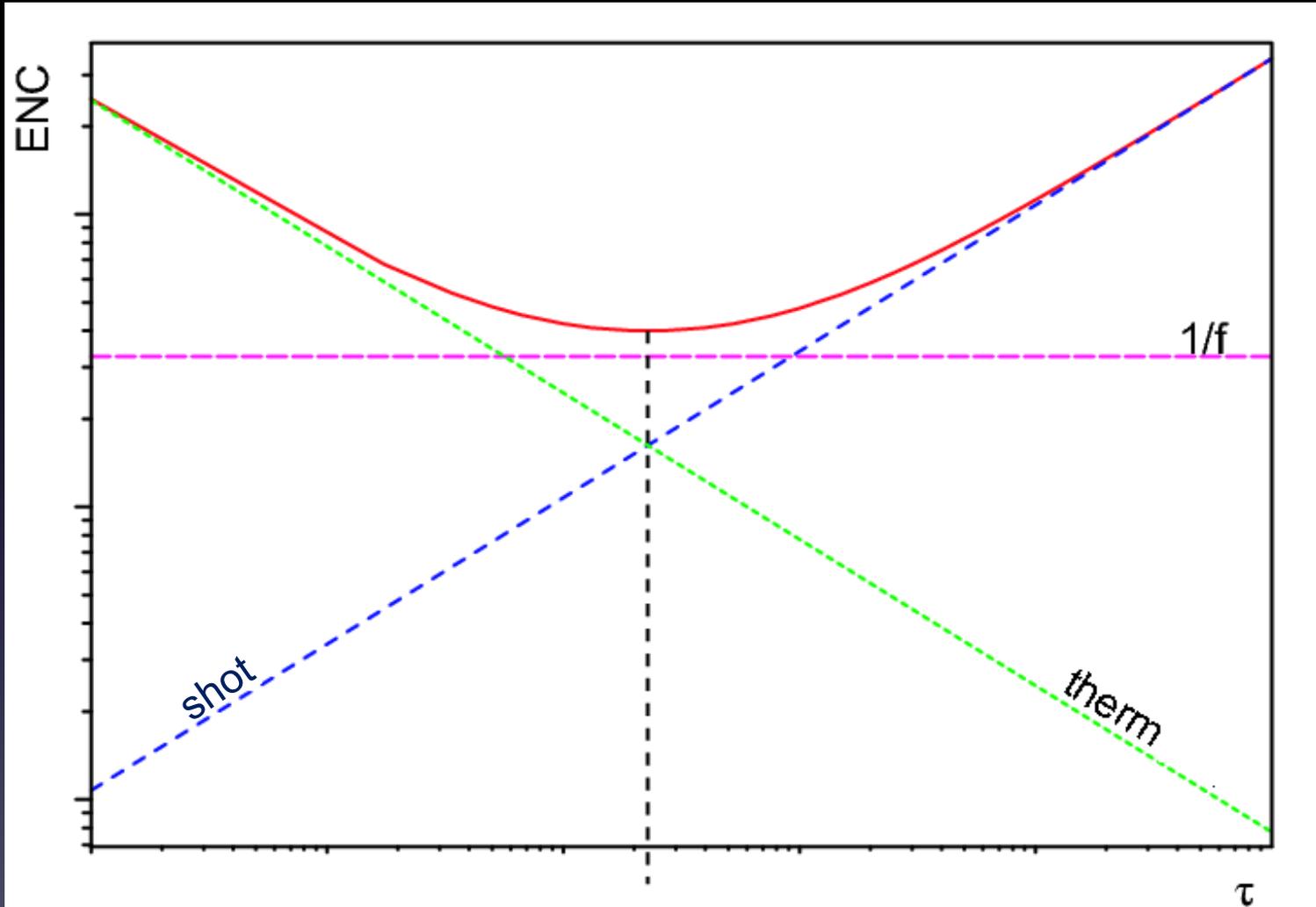
$$ENC_{1/f} \approx \frac{C_D}{q} \sqrt{\frac{K_f}{C_{ox}WL}} \sqrt{\ln\left(\tau_f \frac{g_m}{C_{load}} \frac{C_f}{C_D}\right)} = 9e^- \times \frac{C_D}{100 \text{ fF}} \text{ (for NMOS trans.)}$$

$W, L$  = width and length of trans. gate  
 $K_f$  = 1/f noise coefficient  
 $C_{ox}$  = gate oxide capacitance

$C_f$  = feedback capacitance  
 $C_{load}$  = load capacitance  
 $C_D$  = detector capacitance  
 $\tau_f$  = feedback time constant



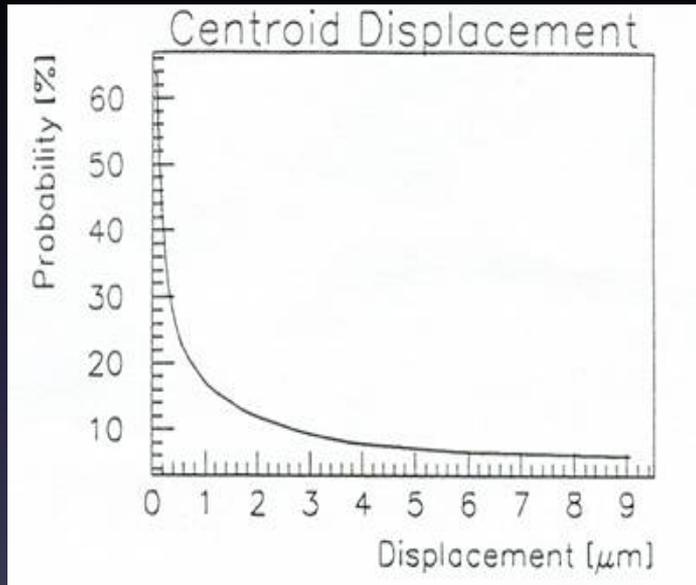
# Noise



# Position resolution

The position resolution depends on various factors

- Physics processes:
  - Diffusion of charge carriers
  - Statistical fluctuations of the energy loss
- External parameters
  - Binary readout or read out of analogue signal value
  - Distance between strips/pixels (pitch)
  - Signal to noise ratio



Low probability  $\delta(E)$  release  
 additional electrons drifting  
 perpendicularly to the track and  
 spoiling position resolution

- Strip detector with binary readout

$$\sigma_X = \frac{p}{\sqrt{12}}$$

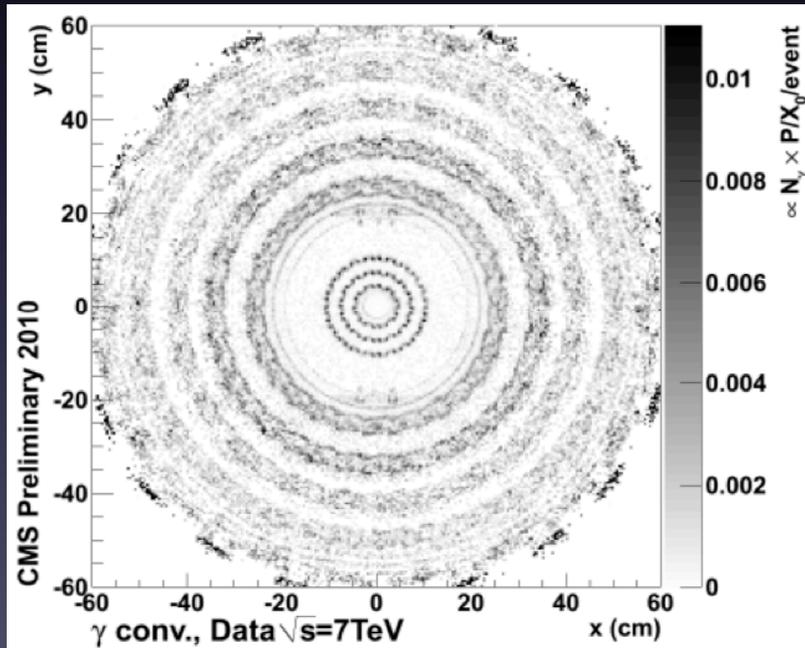
- Typical pitch (distance between strips) 100-50  $\mu\text{m} \implies \sigma_x \simeq 10\text{-}30 \mu\text{m}$
- One can do better with analog readout

$$\sigma_X \propto \frac{p}{SNR}$$

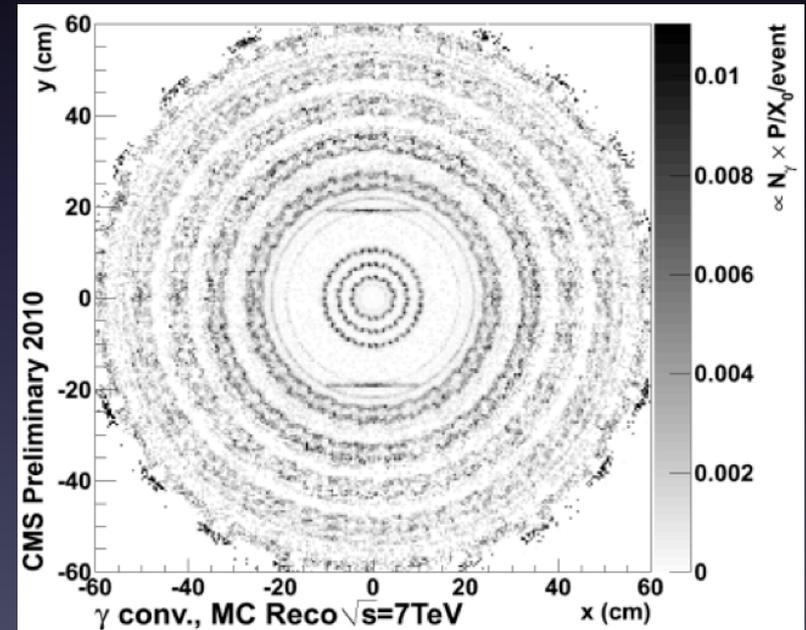
# Material

- Reconstruction of photon conversions ( $\gamma \rightarrow e^+e^-$ ) can provide precise map of the material
  - The number of photon conversion in a volume  $\approx$  amount of material  $\times$  reconstruction efficiency
  - The reconstructed vertices can be used to build detailed maps of the Tracker material

## DATA

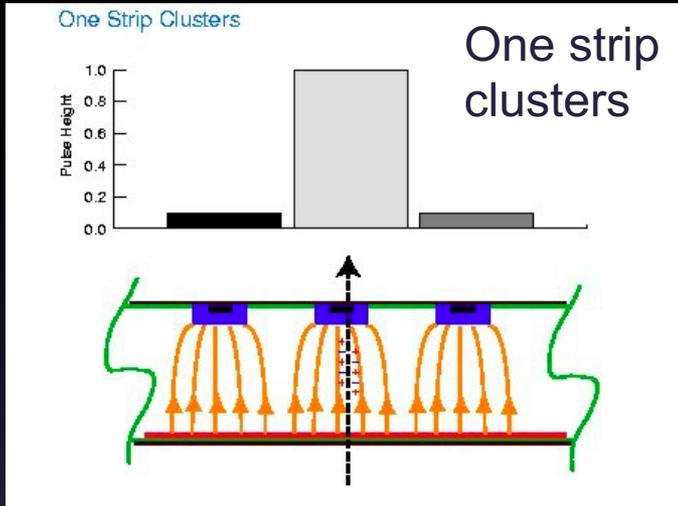


## MC

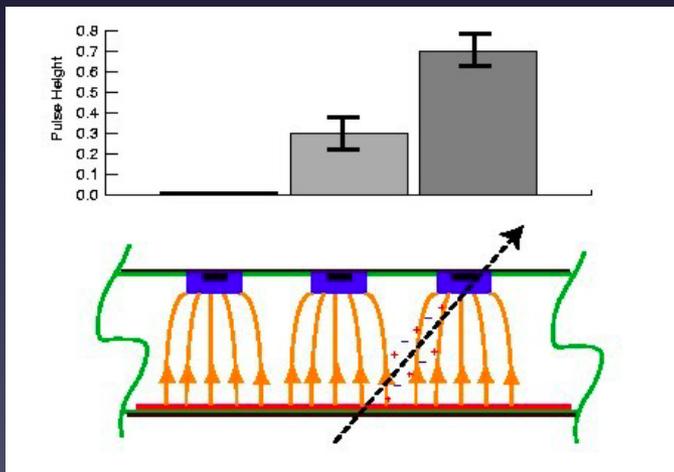
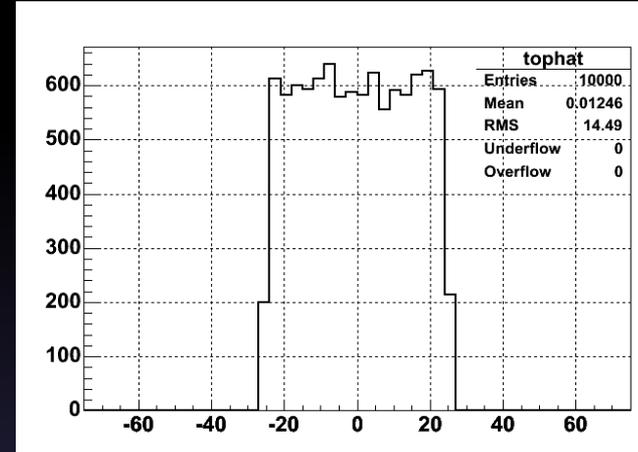


# Position resolution

- Resolution is the spread of the reconstructed position minus the true position

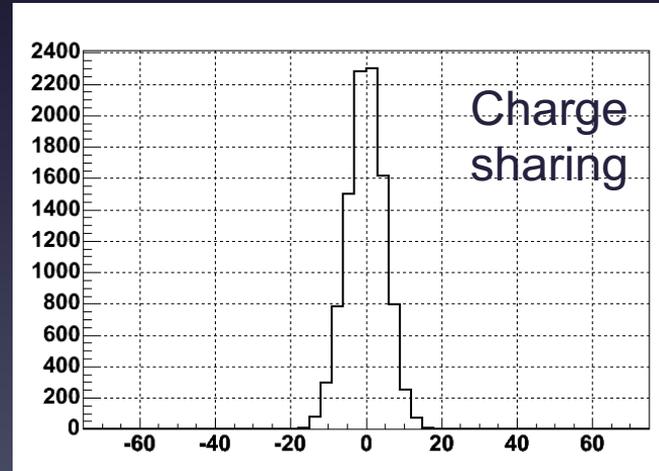


$$\sigma = \frac{pitch}{\sqrt{12}}$$

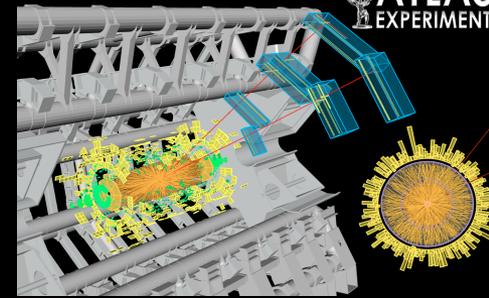


$$\sigma \approx \frac{pitch}{1.5 \cdot \sqrt{12}}$$

$$= \frac{PH_R}{PH_L + PH_R}$$



# Tracking at the LHC



- ~1200 tracks every 25 ns or  $\sim 10^{11}$ /second
  - high radiation dose  $10^{15}$   $n_{\text{eq}} / \text{cm}^2 / 10$  yrs
  - 600 kGy (60 Mrad) through the ionisation of mipis in 250  $\mu\text{m}$  bulk silicon
- Vertexing is critical to distinguish high  $p_{\text{T}}$  collision from pile up:
  - LHC has a Gaussian sigma along the beam direction of  $\sim 8$  cm
  - Vertices of the different inelastic collisions are separated by  $\approx 1$  cm on average
- Tracker must deal with very complex pattern recognition
  - Many measurement layers
- Complexity increases as a function of the occupancy (  $\langle \text{number of hits} \rangle / \text{event in one elementary detector element}$  )
  - Need to have occupancy  $< 1\%$
- Most particles are inside the detector in the next bunch crossing
  - high  $p_{\text{T}}$  particles travel  $\approx 7$  m from the interaction point in 25 ns
  - low  $p_{\text{T}}$  particle may curl 2–3 times inside the tracker



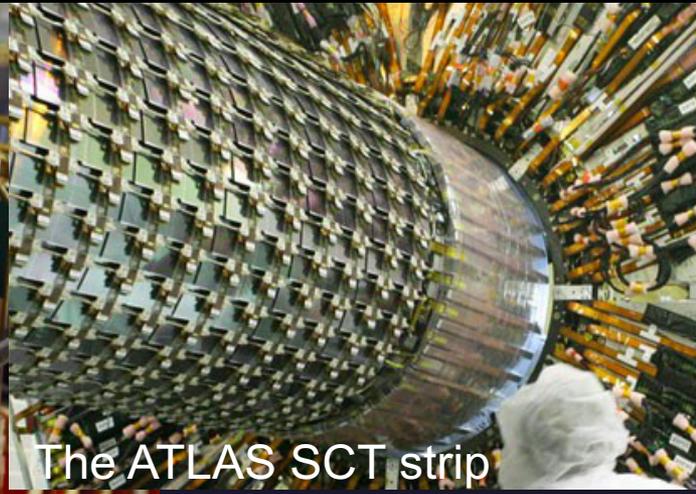
# The LHC detectors



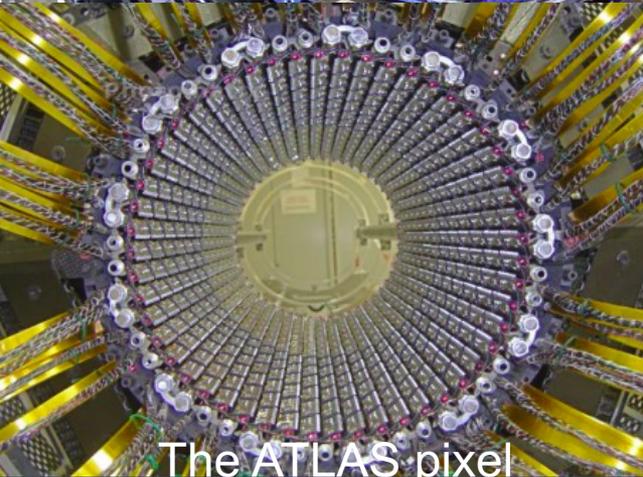
The CMS TIB strip



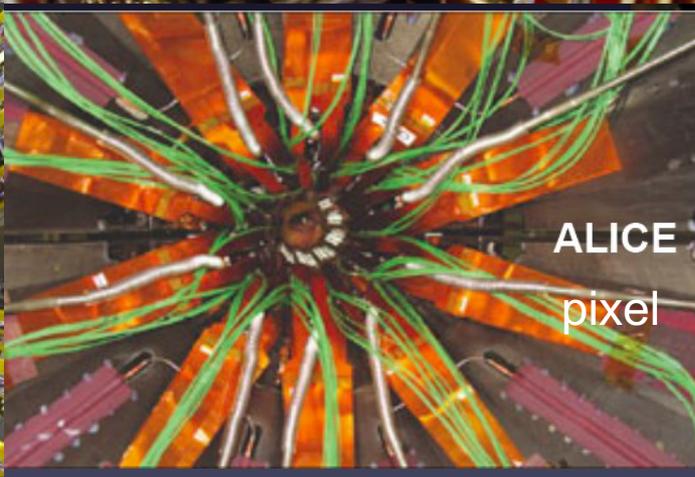
The LHCb-VELO strip



The ATLAS SCT strip



The ATLAS pixel



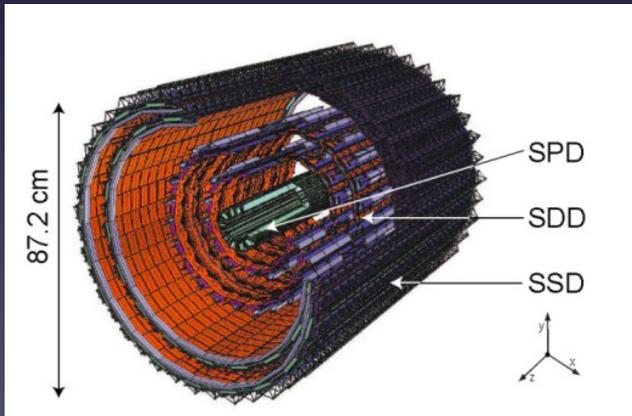
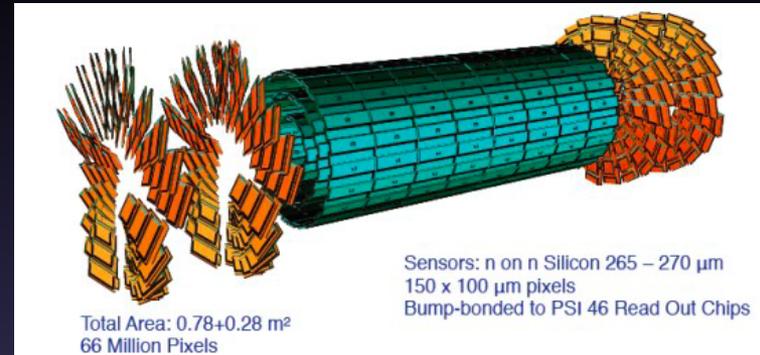
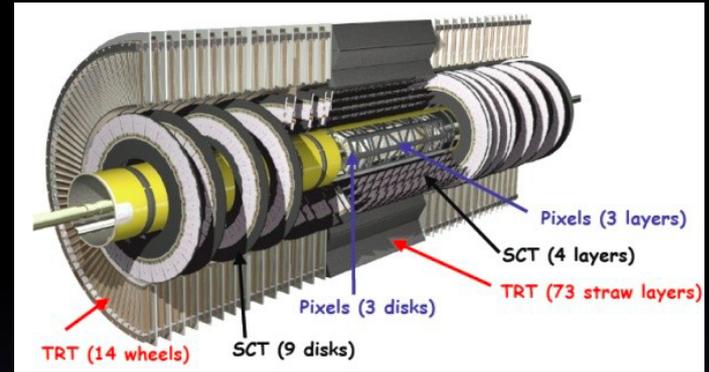
ALICE  
pixel



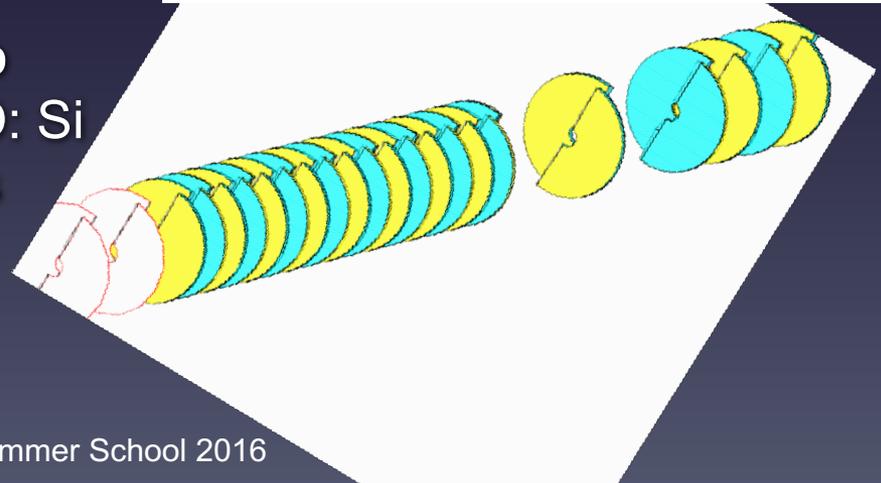
The CMS pixel

# The LHC silicon detectors

- **ATLAS Strips:** 61 m<sup>2</sup> of silicon, 4088 modules, 6x10<sup>6</sup> channels  
**Pixels:** 1744 modules, 80 x 10<sup>6</sup> channels
- **CMS** the world largest silicon tracker 200 m<sup>2</sup> of strip sensors (single sided) 11 x 10<sup>6</sup> readout channels ~1m<sup>2</sup> of pixel sensors, 60x10<sup>6</sup> channels
- **ALICE** Pixel sensors, Drift detectors  
 Double sided strip detectors



- **LHCb**  
 VELO: Si Strips

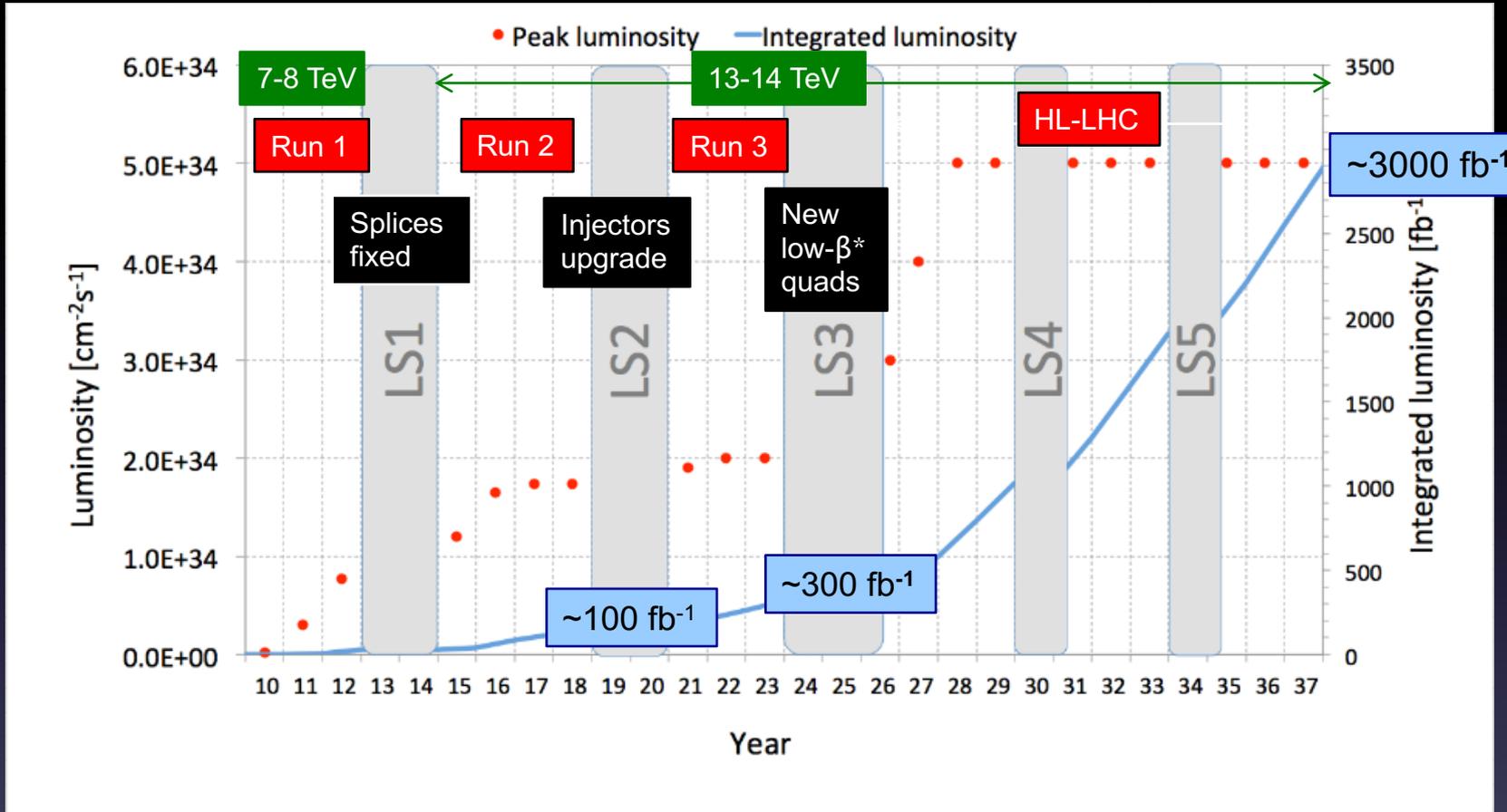




# Comparison of LHC trackers

	ALICE	ATLAS	CMS
R inner	3.9 cm	5.0 cm	4.4 cm
R outer	3.7 m	1.1 m	1.1 m
Length	5 m	5.4 m	5.8 m
$ \eta $ range	0.9	2.5	2.5
B field	0.5 T	2 T	4 T
Total $X_0$ near $\eta=0$	0.08 (ITS) + 0.035 (TPC) + 0.234 (TRD)	0.3	0.4
Power	6 kW (ITS)	70 kW	60 kW
$r\phi$ resolution near outer radius	$\sim 800 \mu\text{m}$ TPC $\sim 500 \mu\text{m}$ TRD	130 $\mu\text{m}$ per TRT straw	35 $\mu\text{m}$ per strip layer
$p_T$ resolution at 1 GeV and at 100 GeV	0.7% 3% (in pp)	1.3% 3.8%	0.7% 1.5%

# The LHC Future

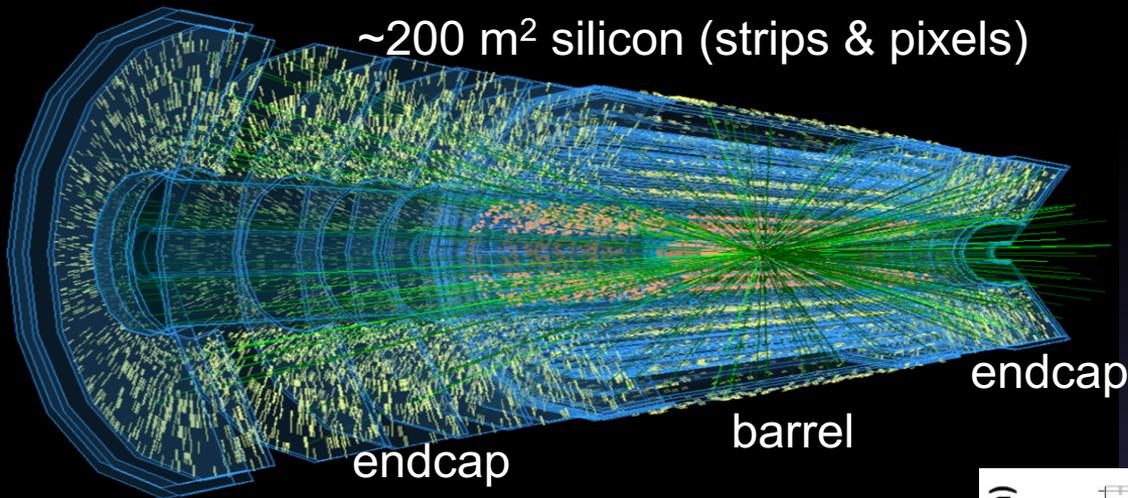


- ❑ LIU/HL-LHC Cost & Schedule reviews in March 2015 and October 2016
- ❑ ATLAS and CMS: “scoping documents” presented to Resources Review Board October 2015  
→ scale of funding defined, now proceeding to TDRs
- ❑ ALICE and LHCb: major upgrades under construction for installation in LS2



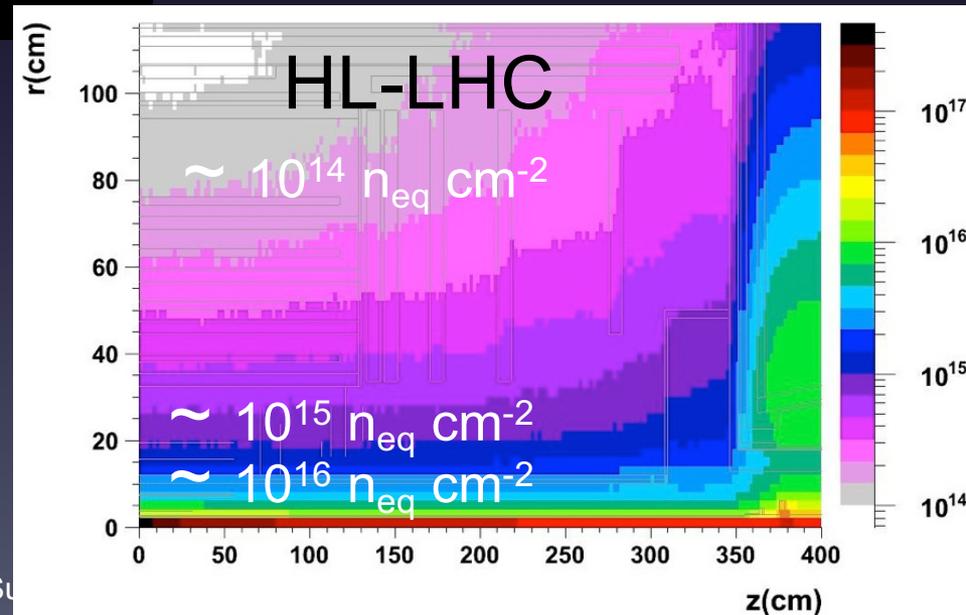
# HL-LHC tracker upgrades

- New all-silicon trackers for ATLAS and CMS



- Increased luminosity and larger area require
  - Higher hit-rate capability
  - Increased granularity
  - Higher radiation tolerance
  - Lighter detectors
  - Cheaper price tag !!

- Radiation hardness and rate performance must increase compared to LHC Run I
  - Run 2 (2015)  $\approx x5$
  - Run 3 (2018)  $\approx x 5-10$
  - HL-LHC (>2025)  $\approx x 10-30$
- In the inner pixel layers:
  - $10^{16} n_{eq} cm^{-2}$  and TID > 1 Grad





# References

- Interaction with Matter & detectors:
  - CERN Summer school lectures (D. Bortoletto, W. Reigler): <https://indico.cern.ch/event/387976/>
  - The Physics of Particle detectors- DESY- organized by E. Garutti  
[http://www.desy.de/~garutti/LECTURES/ParticleDetectorSS12/Lectures\\_SS2012.ht](http://www.desy.de/~garutti/LECTURES/ParticleDetectorSS12/Lectures_SS2012.ht)
  - CERN-Fermilab Hadron Collider Physics Summer School: <http://hcpss.fnal.gov/hcpss14/>
- Silicon: Manfred Krammer  
[http://www.hephy.at/fileadmin/user\\_upload/Lehre/Unterlagen/Praktikum/Halbleiterdetektoren.pdf](http://www.hephy.at/fileadmin/user_upload/Lehre/Unterlagen/Praktikum/Halbleiterdetektoren.pdf)
- CMOS:
  - I. Peric : <https://indico.cern.ch/event/237380/>
  - W.Snoyes  
<https://agenda.infn.it/getFile.py/access?contribId=62&resId=0&materialId=slides&confId=8834>
- Tracking
  - Excellent lectures on tracking algorithms by A. Saltzburger at HCPSS2014
  - Previous CERN academic lecture by P. Wells <https://indico.cern.ch/event/526765/>
- New ideas for silicon detectors:
  - Great summary by Norbert Wermes at VCI 2016:  
<https://indico.cern.ch/event/391665/sessions/160850/#20160215>
  - TWEPP: Topical Workshop on electronic for Particle Physics. Excellent talk by F. Faccio on radiation effects on electronics
  - VCI, VERTEX, PIXEL, Trento workshops



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