

# New Physics Beyond the Standard Model

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# Spectrum

SM int.	gauge boson, spin-1	Super-partner, spin-1/2
$SU(3)_C$	$g^a, a = 1, 2, \dots, 8$	gluino: $\tilde{g}^a$
$SU(2)_L$	$W_{1,2,3}$	wino: $\tilde{W}_{1,2,3}$
$U(1)_Y$	$B_\mu$	bino: $\tilde{B}$

squarks, quarks ( $\times 3$ families)	$Q$ $\bar{u}$ $\bar{d}$	$(\tilde{u}_L \ \tilde{d}_L)$ $\tilde{u}_R^*$ $\tilde{d}_R^*$	$(u_L \ d_L)$ $u_R^\dagger$ $d_R^\dagger$	$(\mathbf{3}, \mathbf{2}, \frac{1}{6})$ $(\bar{\mathbf{3}}, \mathbf{1}, -\frac{2}{3})$ $(\bar{\mathbf{3}}, \mathbf{1}, \frac{1}{3})$
sleptons, leptons ( $\times 3$ families)	$L$ $\bar{e}$	$(\tilde{\nu} \ \tilde{e}_L)$ $\tilde{e}_R^*$	$(\nu \ e_L)$ $e_R^\dagger$	$(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$ $(\mathbf{1}, \mathbf{1}, 1)$
Higgs, higgsinos	$H_u$ $H_d$	$(H_u^+ \ H_u^0)$ $(H_d^0 \ H_d^-)$	$(\tilde{H}_u^+ \ \tilde{H}_u^0)$ $(\tilde{H}_d^0 \ \tilde{H}_d^-)$	$(\mathbf{1}, \mathbf{2}, +\frac{1}{2})$ $(\mathbf{1}, \mathbf{2}, -\frac{1}{2})$

## Minimal Supersymmetric Standard Model (MSSM)

gaugino:  $\tilde{g}, \tilde{W}_{1,2,3}, \tilde{B}$

neutralino:  $\tilde{B}, \tilde{W}_3, \tilde{H}_u^0, \tilde{H}_d^0$

$\tilde{N}_i$

chargino:  $\tilde{W}^\pm, \tilde{H}_u^\pm, \tilde{H}_d^\pm$

$\tilde{C}_i$

# SUSY: interactions

# Interactions.

More details: for example, S. Martin “Supersymmetry Primer”

- Superpartners have the same gauge quantum numbers as their SM counter parts.
  - ▶ Similar gauge interactions.

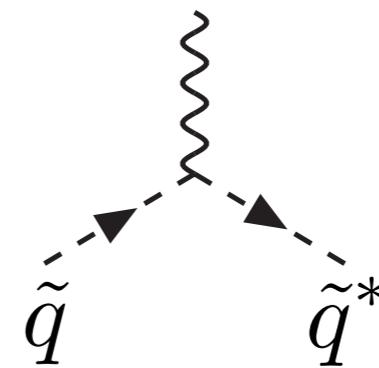
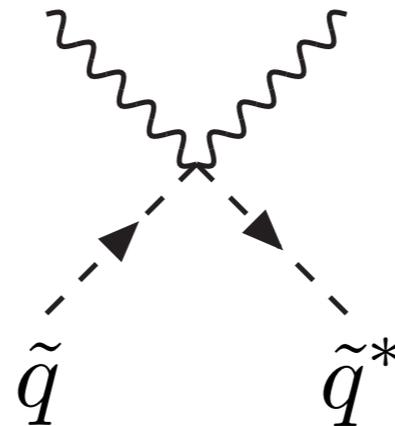
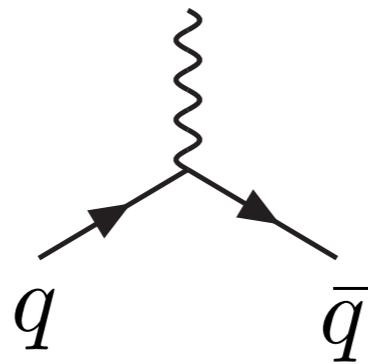
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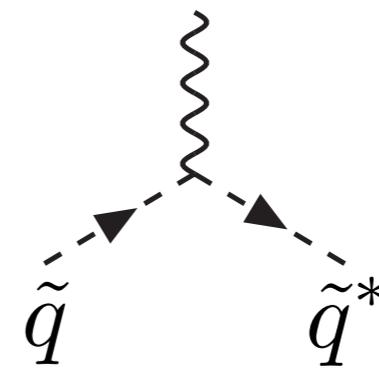
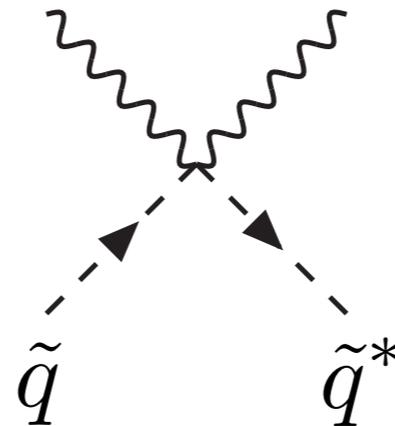
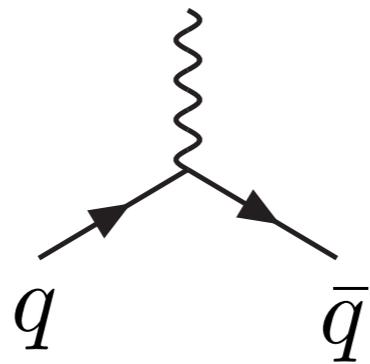
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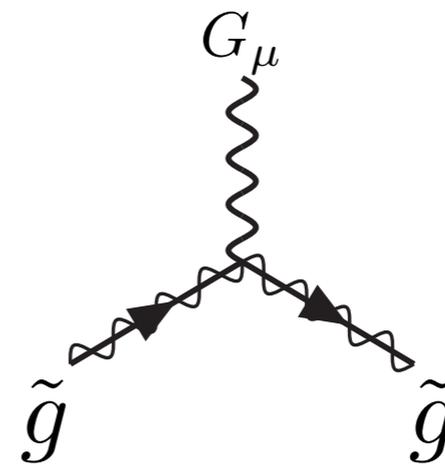
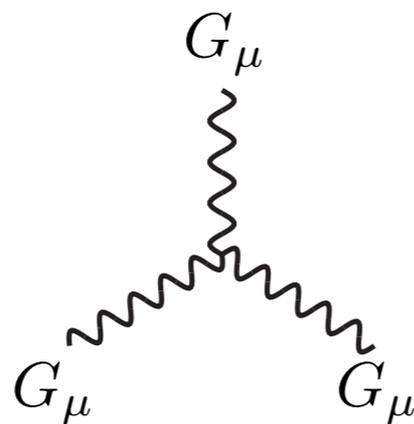
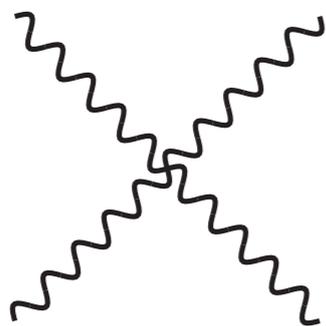
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non-Abelian



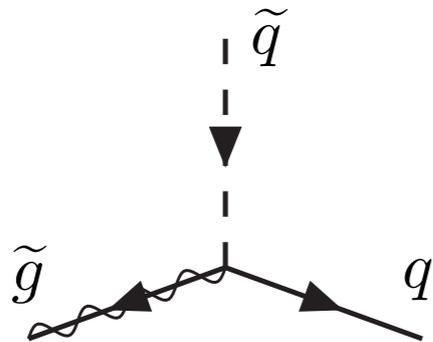
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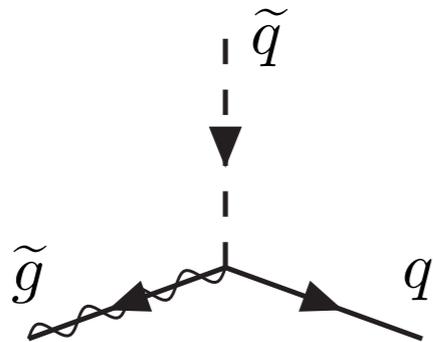
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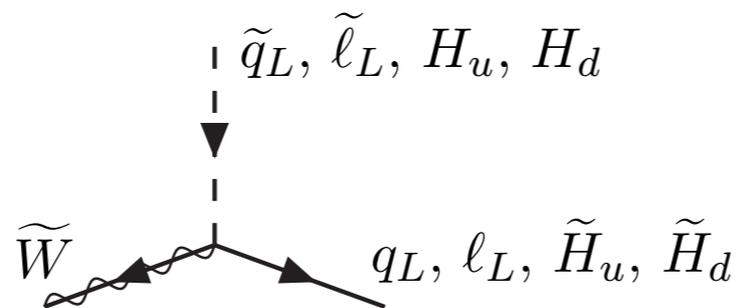
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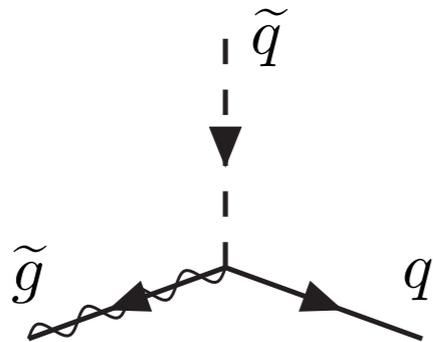
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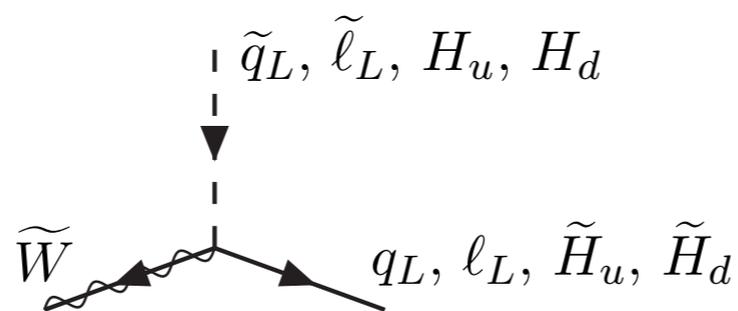
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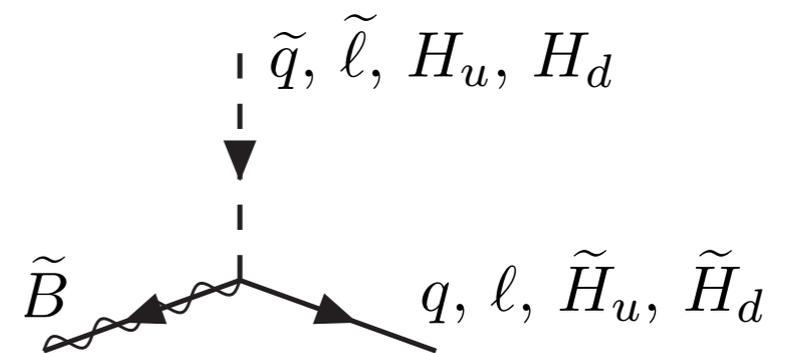
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$SU(2)_L$



$U(1)_Y$

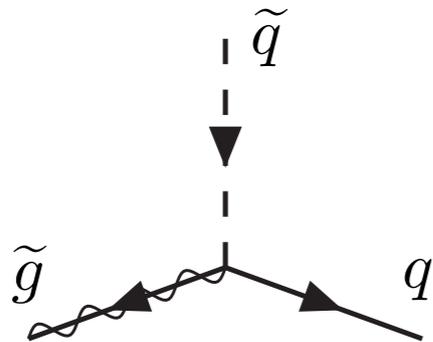


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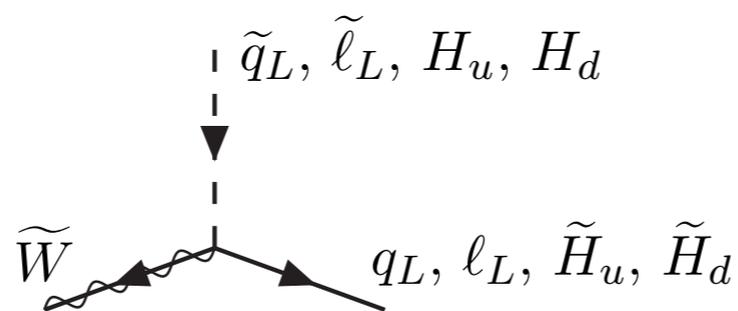
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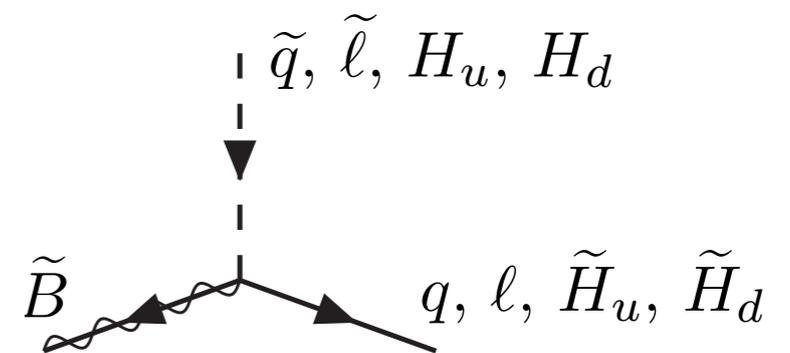
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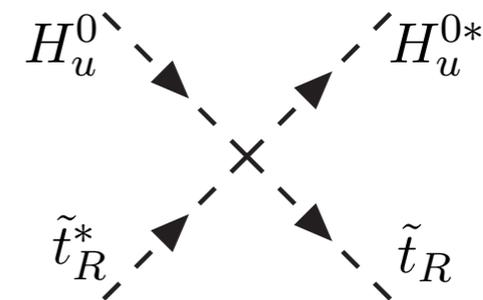
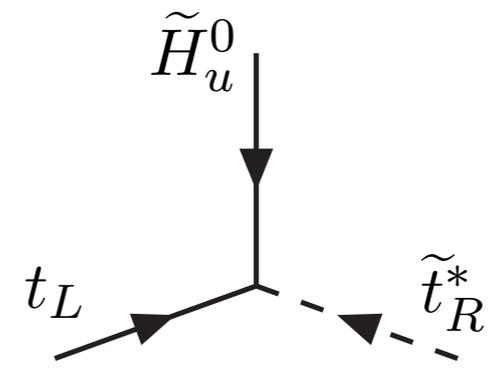
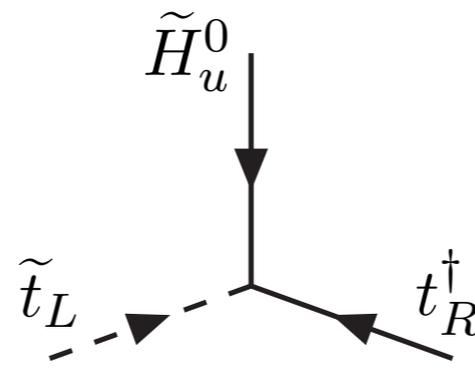
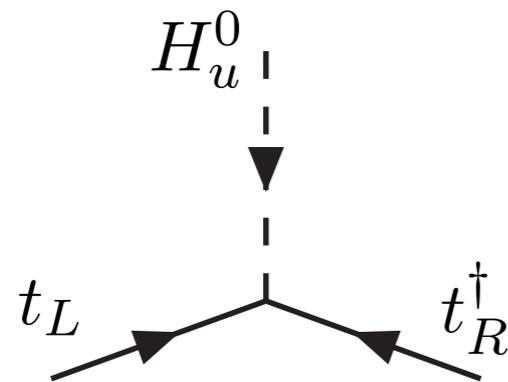


D-term:  $\propto g^2$



# Interactions.

- SM fermions (such as the top quark) receive masses by coupling to the Higgs boson.
- ▶ Yukawa couplings  $\Rightarrow$  SUSY counter parts.



# Superpartners.

- We have not seen any of the superpartner yet.
  - ▶ They must be heavier than the SM particles.
- Therefore, SUSY must be a broken symmetry.
- Are we back to the beginning?
  - ▶ No.
  - ▶ SUSY can be broken in a controlled way so that the theory stays natural, soft SUSY breaking.

# Superpartner mass and naturalness

- $m_h^2$  (physical) =  $m_0^2 + c \Lambda^2$ ,  $c$  some  $O(0.01)$  number.
- New physics needed at  $\Lambda \approx 100\text{s GeV} - \text{TeV}$ 
  - ▶ This should be the superpartner mass for a natural theory.
- At higher energies, the theory is approximately supersymmetric. Therefore, scalar mass would be sensitive to what happens at higher energy scales.
  - ▶  $m_h^2$  (physical) =  $m_0^2 + c m(\text{superpartner})^2$

# The masses of the superpartners

$$\begin{aligned}\mathcal{L}_{\text{soft}}^{\text{MSSM}} = & -\frac{1}{2} \left( M_3 \tilde{g} \tilde{g} + M_2 \tilde{W} \tilde{W} + M_1 \tilde{B} \tilde{B} + \text{c.c.} \right) \\ & - \left( \tilde{u} \mathbf{a}_u \tilde{Q} H_u - \tilde{d} \mathbf{a}_d \tilde{Q} H_d - \tilde{e} \mathbf{a}_e \tilde{L} H_d + \text{c.c.} \right) \\ & - \tilde{Q}^\dagger \mathbf{m}_Q^2 \tilde{Q} - \tilde{L}^\dagger \mathbf{m}_L^2 \tilde{L} - \tilde{u} \mathbf{m}_u^2 \tilde{u}^\dagger - \tilde{d} \mathbf{m}_d^2 \tilde{d}^\dagger - \tilde{e} \mathbf{m}_e^2 \tilde{e}^\dagger \\ & - m_{H_u}^2 H_u^* H_u - m_{H_d}^2 H_d^* H_d - (b H_u H_d + \text{c.c.}) .\end{aligned}$$

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Gaugino masses

# The masses of the superpartners

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trilinear,  
similar to Yukawa

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# General parameterization

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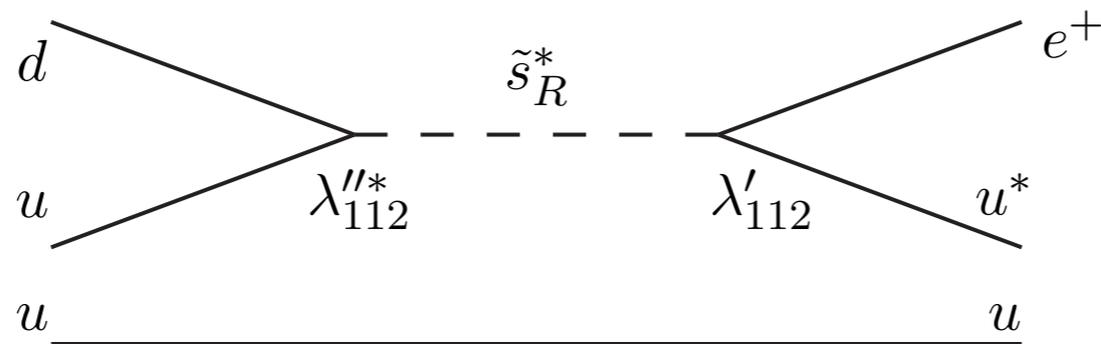
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– > 100 parameters.

- ▶ Too many? Have to include all of them in the most general theory.
- ▶ Most of them, flavor mixing, CP phases, are strongly constrained to vanish.
- ▶ A theory of SUSY breaking typically contain much less (< 10-ish) parameters.

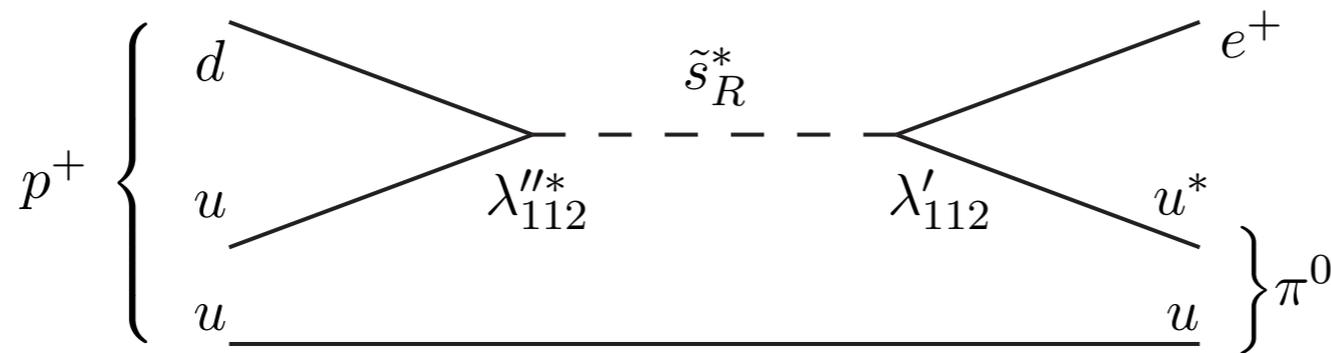
# More couplings?

- Gauge invariance and SUSY allows for more couplings. For example



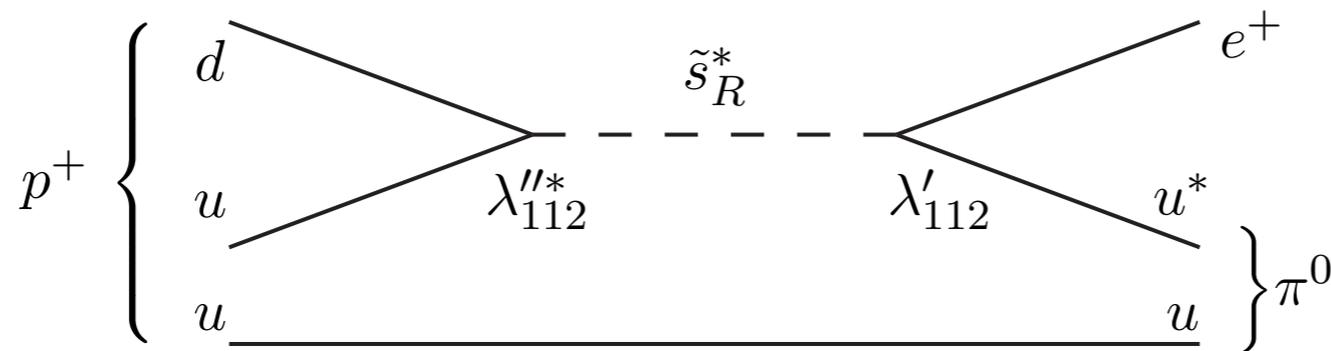
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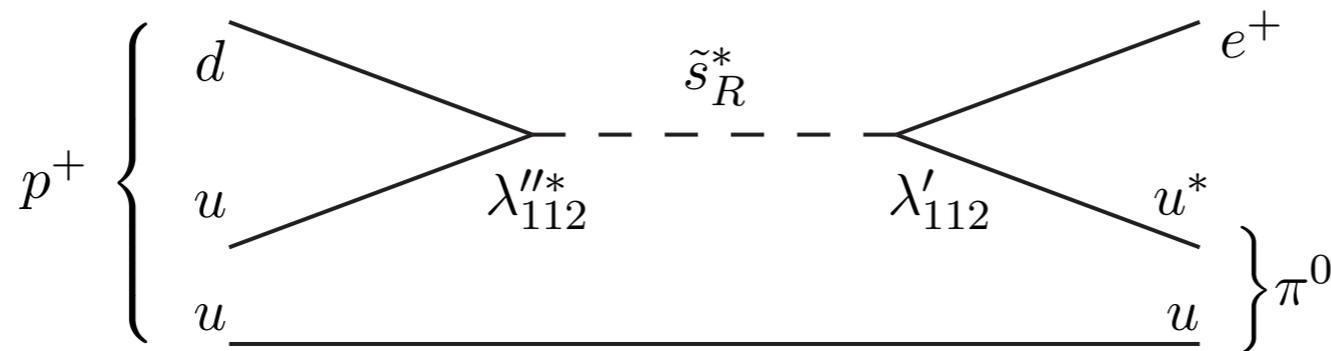
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Proton decay: 
$$\Gamma_{p \rightarrow e^+ \pi^0} \sim m_{\text{proton}}^5 \sum_{i=2,3} |\lambda'^{11i} \lambda''^{11i}|^2 / m_{\tilde{d}_i}^4$$

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**These couplings must be extremely tiny!**

# A symmetry:

- Vanishing couplings usually come from a symmetry principle.
- Could impose B ( $B_{\text{quark}} = 1/3$ ) or L ( $L_{\text{lepton}} = 1$ ) symmetry. Slightly uncomfortable
  - ▶ Not exact symmetries in the SM.
- An interesting choice: R-parity

$$P_R = (-1)^{3(B-L)+2s}$$

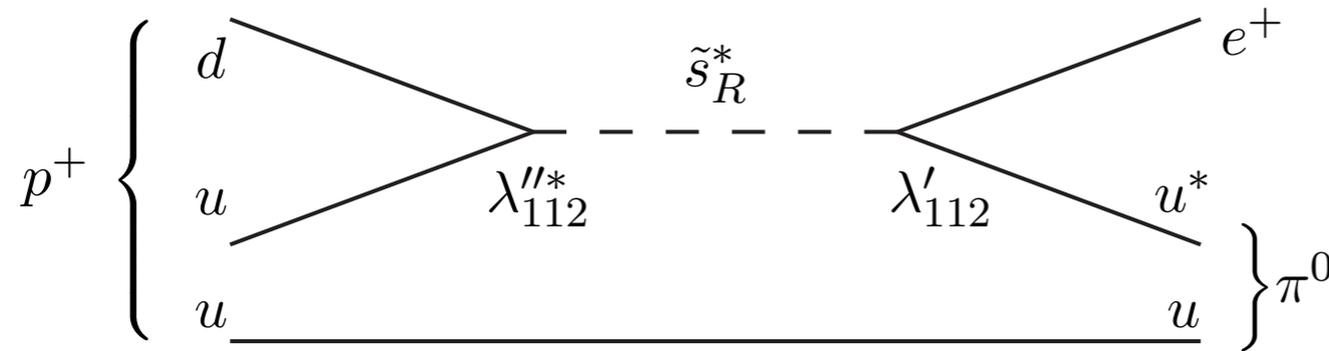
# R-parity

$$P_R = (-1)^{3(B-L)+2s}$$

	spin		spin
gluon, $g$	1	gluino: $\tilde{g}$	1/2
$W^\pm, Z$	1	gaugino: $\tilde{W}^\pm, \tilde{Z}$	1/2
quark: $q$	1/2	squark: $\tilde{q}$	0
...		...	
SM		(super)partner	

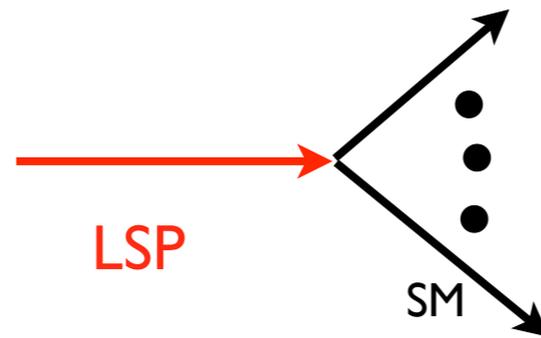
- All superpartners are odd under R-parity.

# R-parity

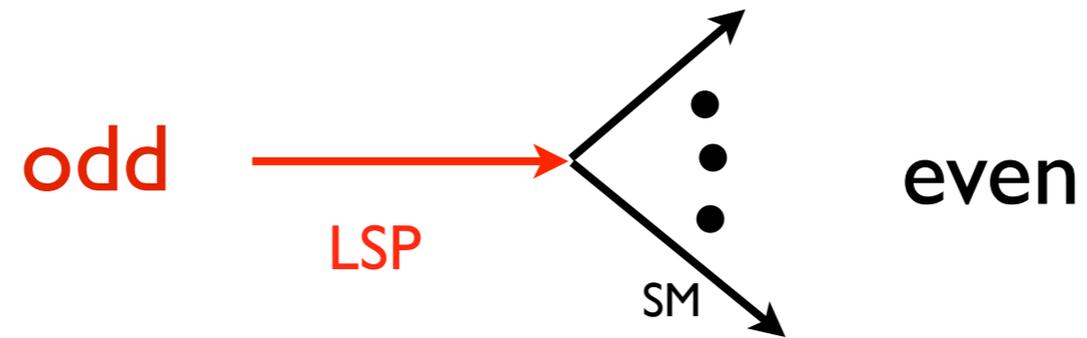


forbidden!

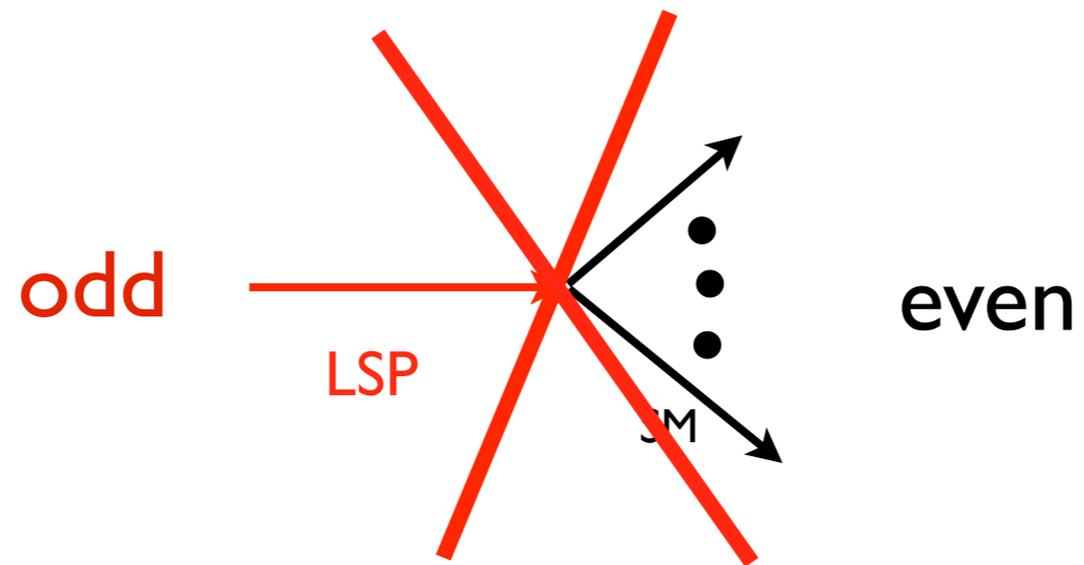
# Lightest SuperPartner (LSP) is stable



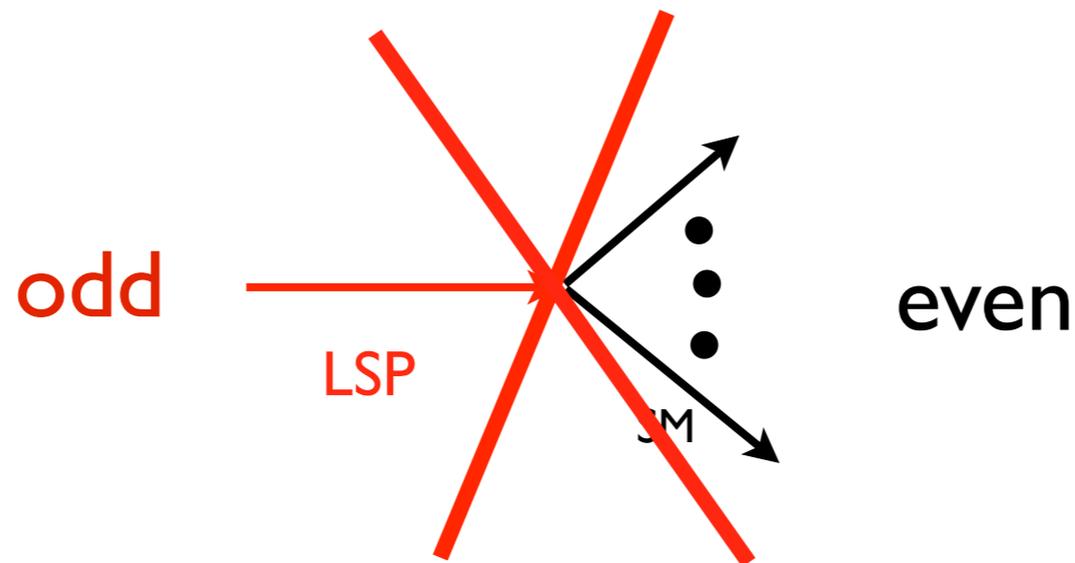
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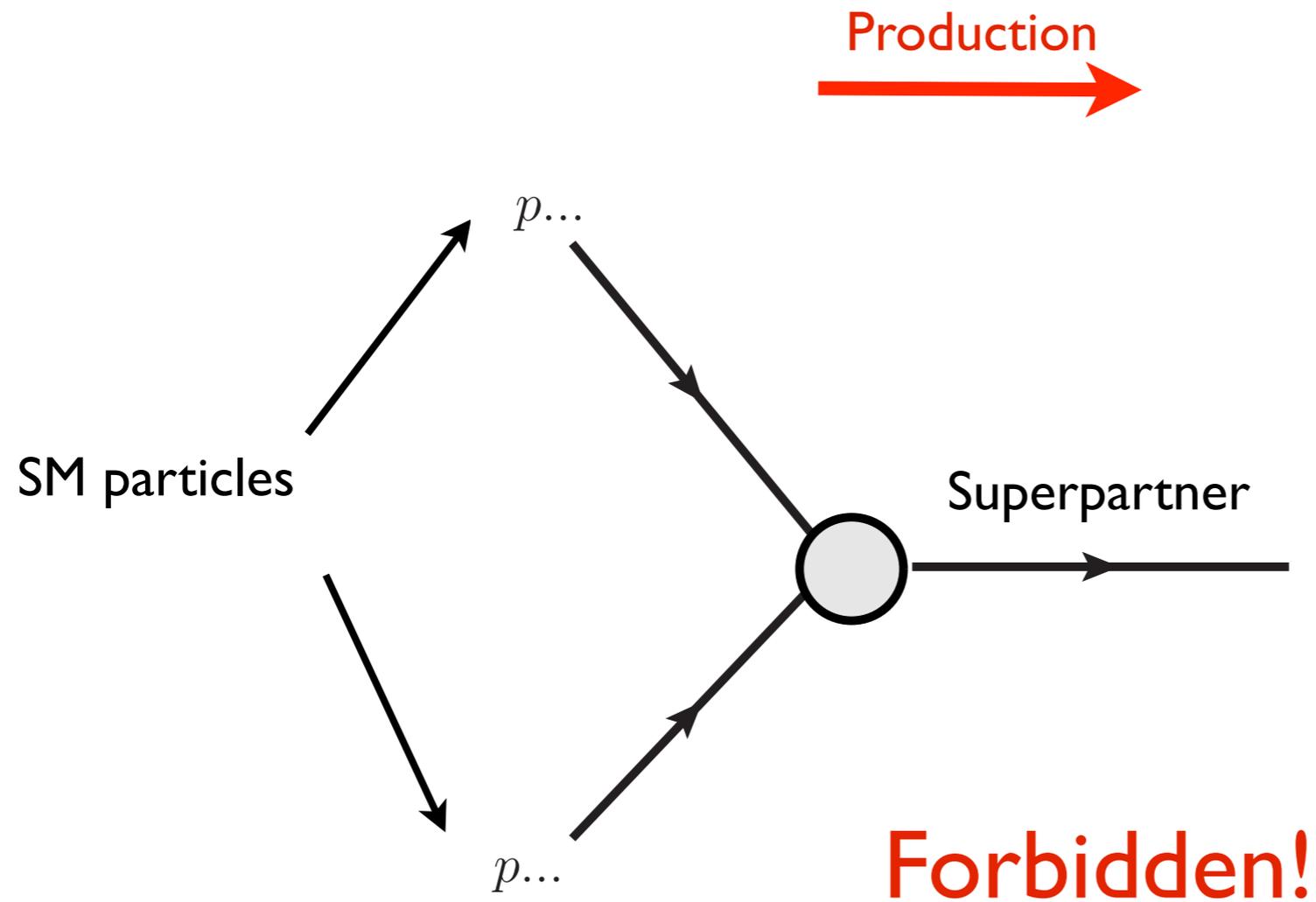
# Lightest SuperPartner (LSP) is stable



- Neutral LSP a natural candidate for WIMP dark matter.
  - ▶  $O(\Lambda_{EW})$
  - ▶ Weakly coupled.
  - ▶ Can have similar states in other new physics scenarios. With SUSY, a consequence of forbidding proton decay.

# SUSY at colliders

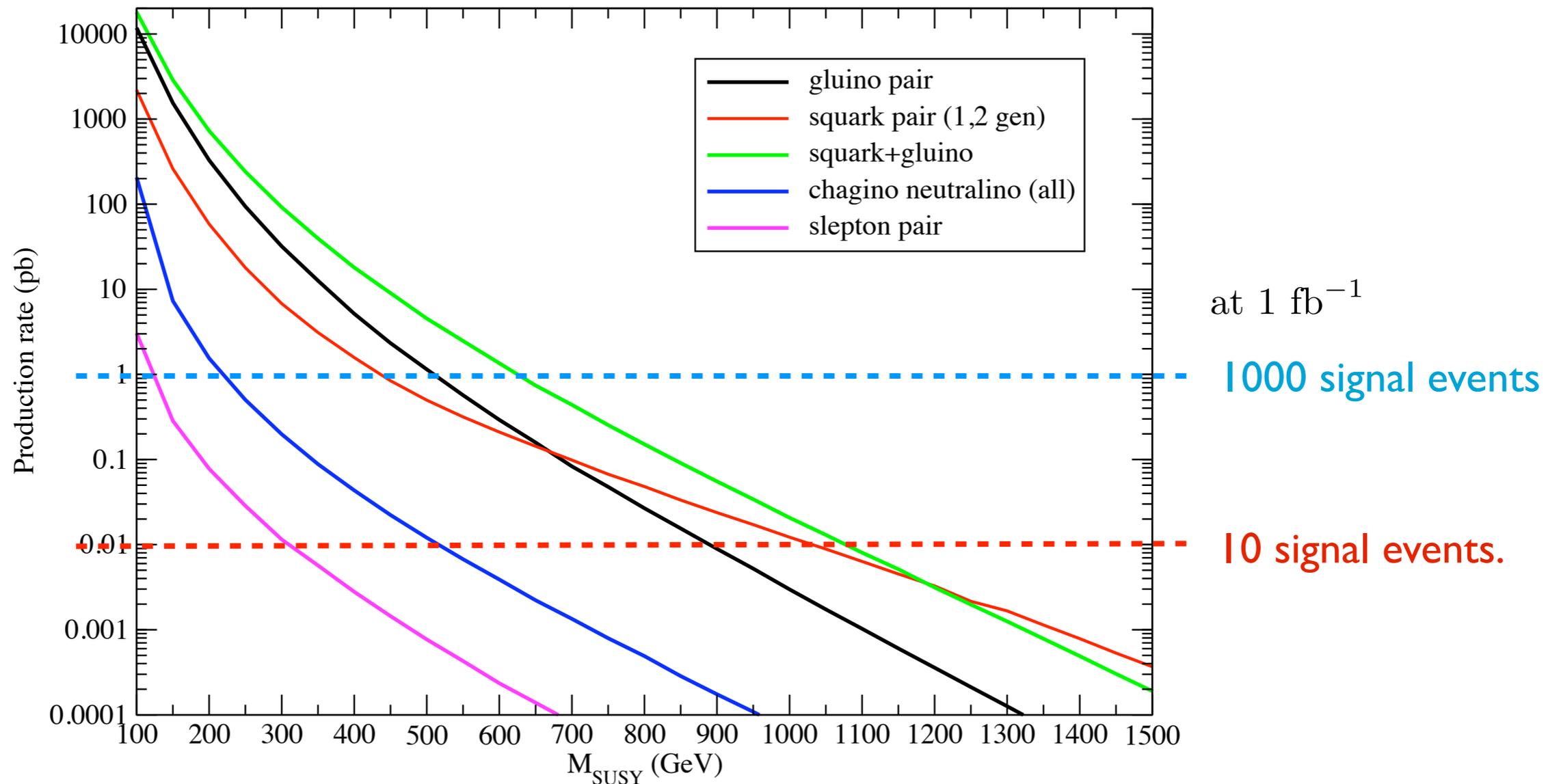
- Superpartners must be pair produced!





# Production.

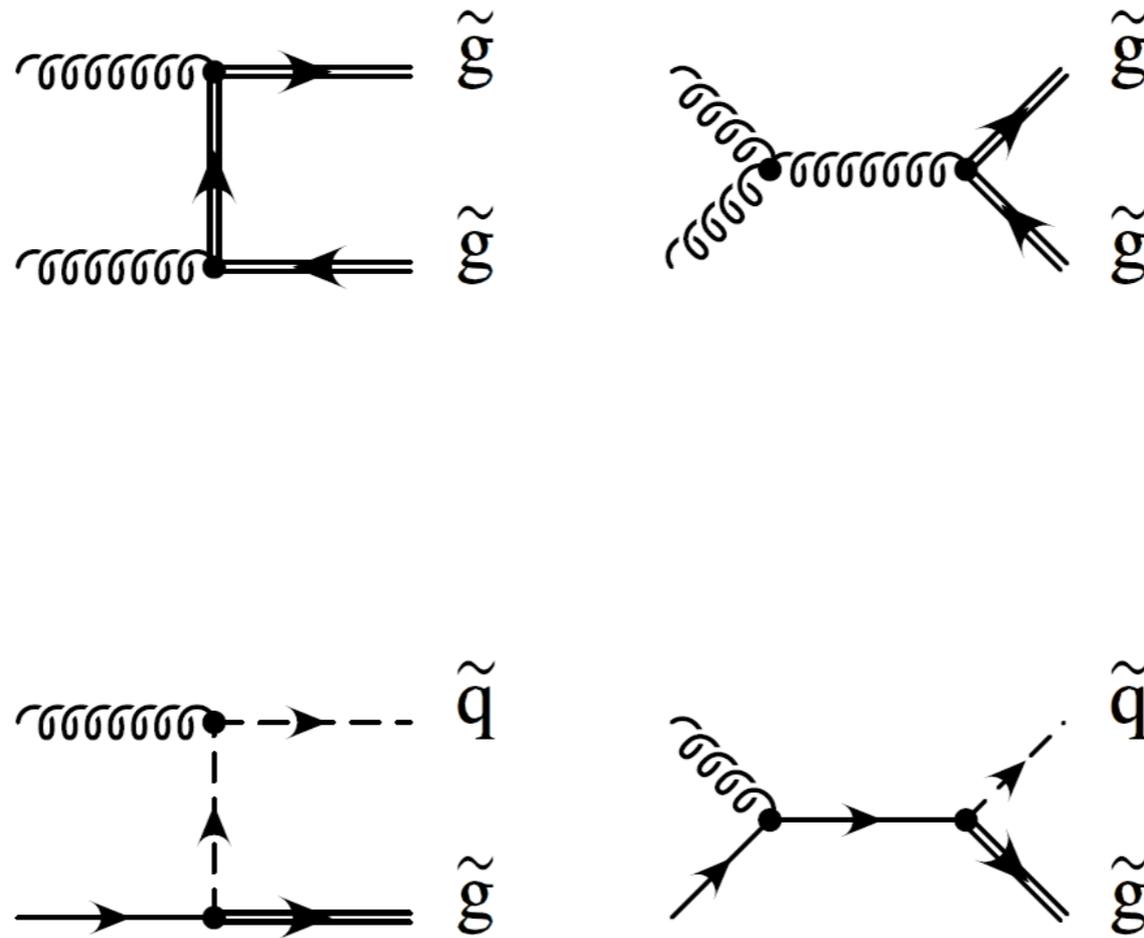
SUSY production rates at 7 TeV



**Dominated by the production of colored states.**  
Similar pattern for other scenarios. Overall rates scaled by spin factors.

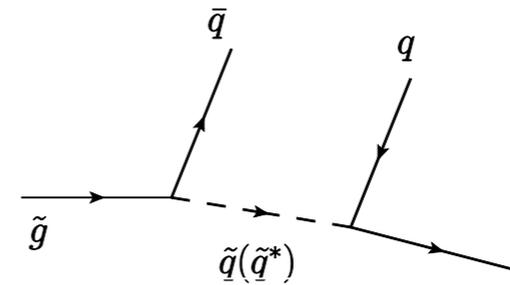
# Examples of production: colored

- Squark and gluino production.



# Decay of squark and gluino

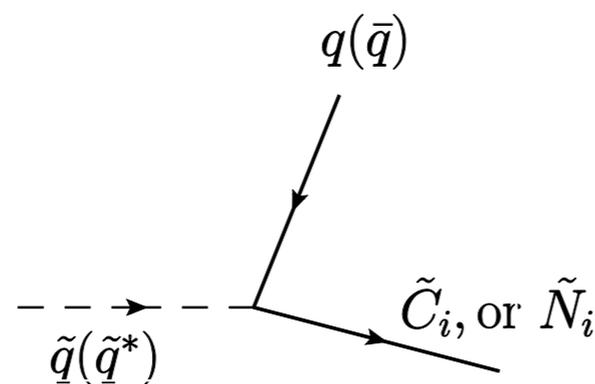
- Gluino always decays into squark (on or off-shell).
  - Gluino  $\rightarrow$  squark + Jets



- Squark decay.

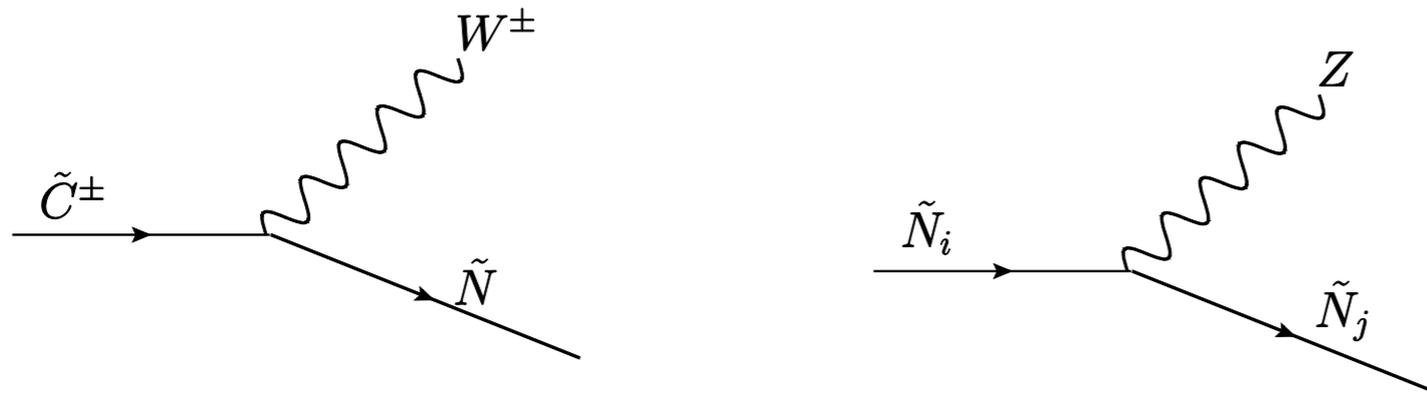
- Jet +

- To gluino, then go through off-shell squark.
- To chargino or neutralino.



# Next steps

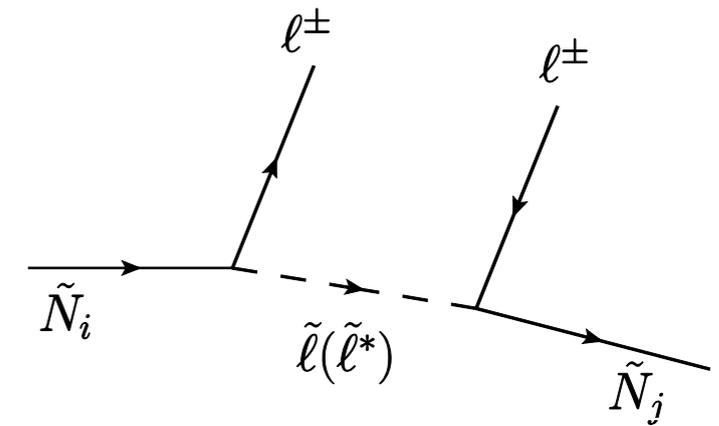
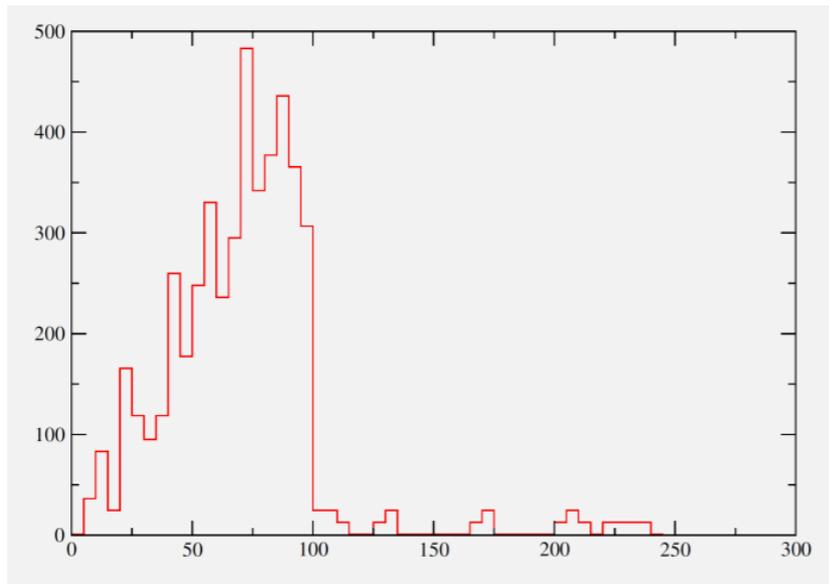
- To W or Z (maybe Higgs.)



- Lepton (suppressed by  $W/Z \rightarrow$  lepton BR.)
  - 1 or 2 leptons.
- Jets (softer, constrained by W and Z mass).

# More leptons if we are lucky

- A lot of leptons. No branching ratio suppression.
- On shell slepton, very distinctive feature.
  - Edge in di-lepton invariant mass.



$$m_{\tilde{\ell}} < M_{\tilde{N}_2} \longrightarrow \tilde{N}_2 \rightarrow \tilde{N}_1 + [\tilde{\ell}] \rightarrow \tilde{N}_1 + \ell^+ + \ell^-$$

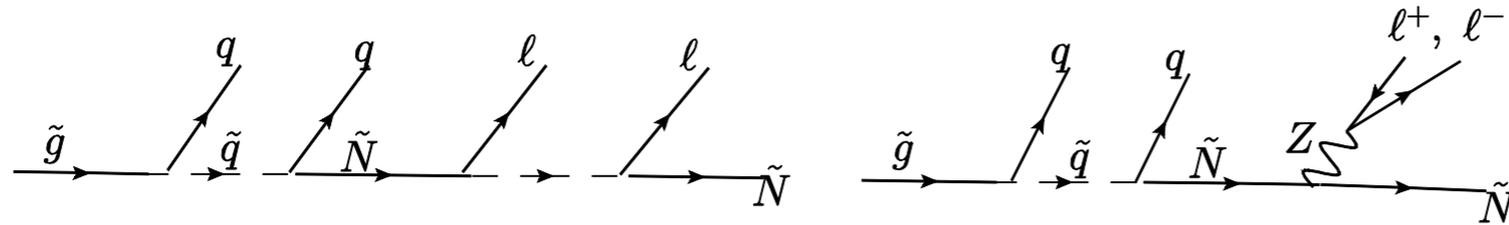
$$M_{\ell\ell}^{\max} = M_{\tilde{N}_2} \sqrt{1 - \frac{m_{\tilde{\ell}}^2}{M_{\tilde{N}_2}^2}} \sqrt{1 - \frac{M_{\tilde{N}_1}^2}{m_{\tilde{\ell}}^2}}$$

- More complicated edges useful, but need high statistics.

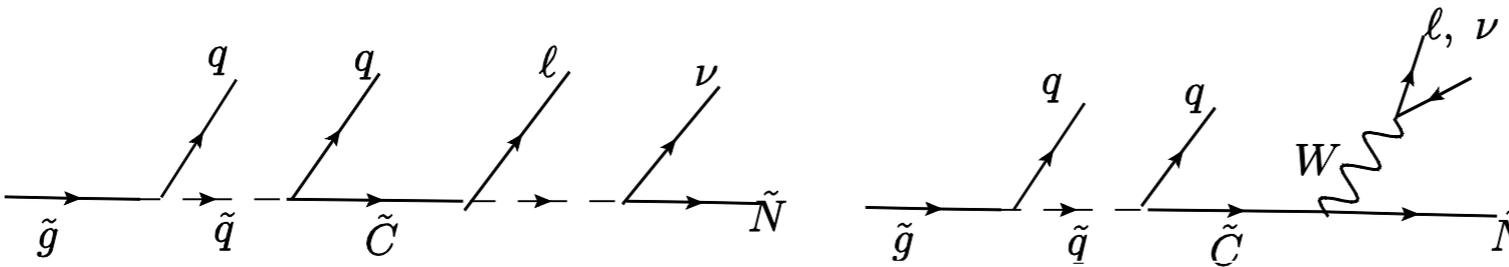
See several papers by: Miller, Osland.

# Long decay chains

- Putting the pieces together.
- Many channels, many final states.



2-lepton chain

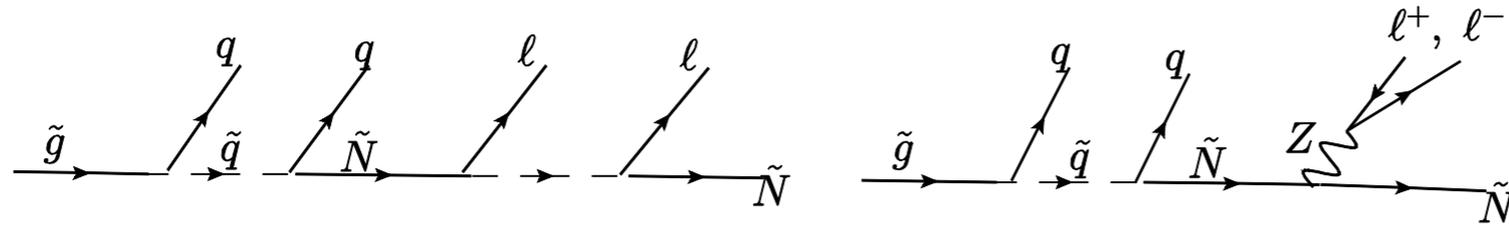


1-lepton chain

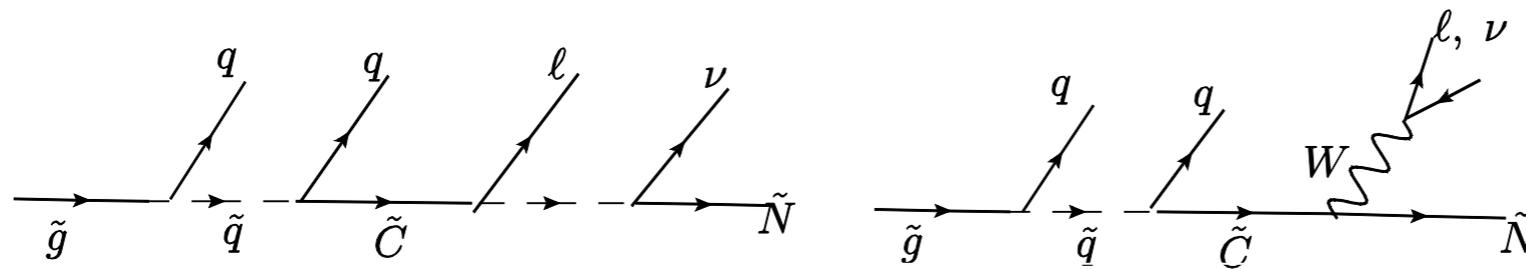
$$\begin{aligned}
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2 \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{N}_i] \rightarrow q_1 q_2[Z]\tilde{N}_0 \rightarrow q_1 q_2 q_3 q_4 \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{C}_i] \rightarrow q_1 q_2[W]\tilde{N}_0 \rightarrow q_1 q_2 q_3 q_4 \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{N}_i] \rightarrow q_1 q_2[Z]\tilde{N}_0 \rightarrow q_1 q_2 l^+ l^- \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{N}_i] \rightarrow q_1 q_2 q_3 q_4 (l^+ l^-) \tilde{N}_0
 \end{aligned}$$

# Long decay chains

- Putting the pieces together.
- Many channels, many final states.



2-lepton chain



1-lepton chain

$$\begin{aligned}
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2 \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{N}_i] \rightarrow q_1 q_2[Z]\tilde{N}_0 \rightarrow q_1 q_2 q_3 q_4 \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{C}_i] \rightarrow q_1 q_2[W]\tilde{N}_0 \rightarrow q_1 q_2 q_3 q_4 \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{N}_i] \rightarrow q_1 q_2[Z]\tilde{N}_0 \rightarrow q_1 q_2 l^+ l^- \tilde{N}_0 \\
 \tilde{g} &\rightarrow q_1[\tilde{q}] \rightarrow q_1 q_2[\tilde{N}_i] \rightarrow q_1 q_2 q_3 q_4 (l^+ l^-) \tilde{N}_0
 \end{aligned}$$

Exercise: draw diagrams for tri-lepton, same sign di-lepton

# Classification of SUSY signal

- Inclusive counts.

$n_j \times \text{jet}$

+

$n_\ell \times \text{lepton}$

+

$n_\gamma \times \gamma$

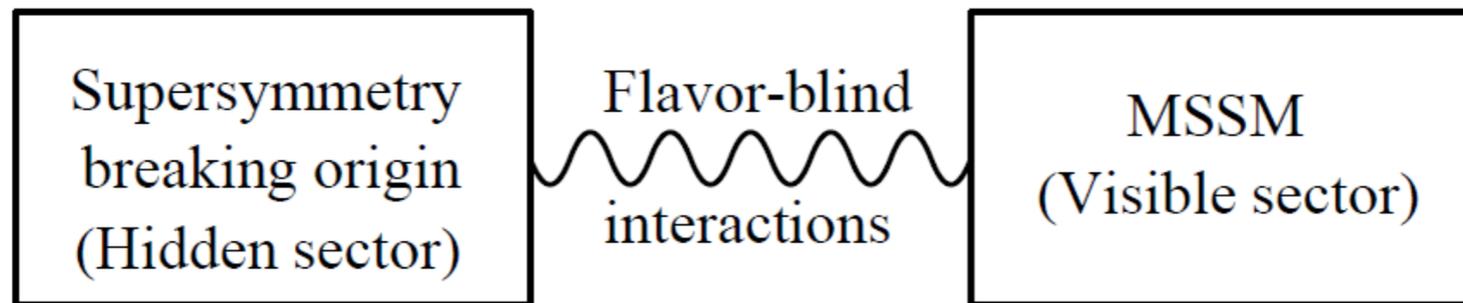
b-jet

non-b-jet

$\ell$  all flavor and charge  
combo: e.g.  $2\ell \rightarrow 21$  comb.

# Supersymmetry: Models

# SUSY breaking and mediation



- Simplest setup does not work.
  - ▶ Renormalizable coupling and at tree level
  - ▶ Sum rules like:  $m_{\tilde{e}_1}^2 + m_{\tilde{e}_2}^2 = 2m_e^2$ , not acceptable!
- Non-renormalizable coupling: gravity, moduli mediation
- Loop: gauge mediation...

# High scale mediation

- SUSY broken at very high energy scale
- Mediated to MSSM through higher dimensional operator suppressed by some high mass scale.
- Low energy SUSY breaking masses obtained after taking into account (significant) renormalization effects
  - ▶ Renormalization group (RG) evolution.
- Gravity mediation, moduli mediation, ....

# High scale mediation

– Gravity mediation: non-renormalizable, suppressed by  $M_{\text{Pl}}$  by def.

▶ SUSY breaking scale:  $\Lambda_S$  about  $10^{11}$  GeV

▶  $m_{\tilde{q}} \sim m_{\tilde{\ell}} \sim M_{\text{gaugino}} \simeq \frac{\Lambda_S^2}{M_{\text{Pl}}} \sim 100(s) \text{ GeV} - \text{TeV}$

□ Follows from dimensional analysis.

□ Vanishes as  $\Lambda_S \Rightarrow 0$ , suppressed by  $M_{\text{Pl}}^{-1}$ .

▶ Need Renormalization Group Evolution to low energy to obtain physical masses.

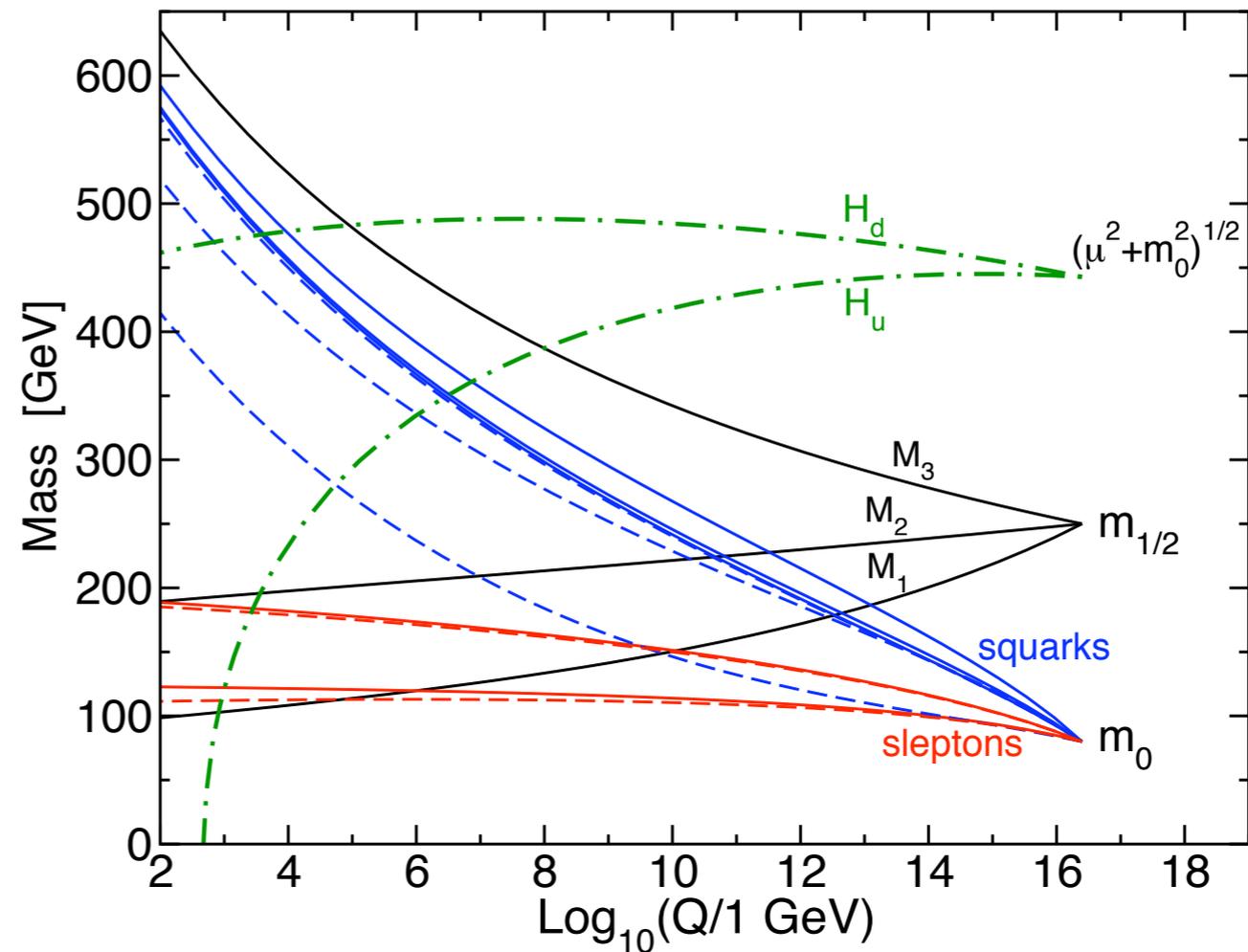
▶ Gravitino (spin 3/2 superpartner of the graviton)

$$m_{3/2} \sim \frac{\Lambda_S^2}{M_{\text{Pl}}}$$

gravitino Very weakly coupled,  $\propto M_{\text{Pl}}^{-1}$

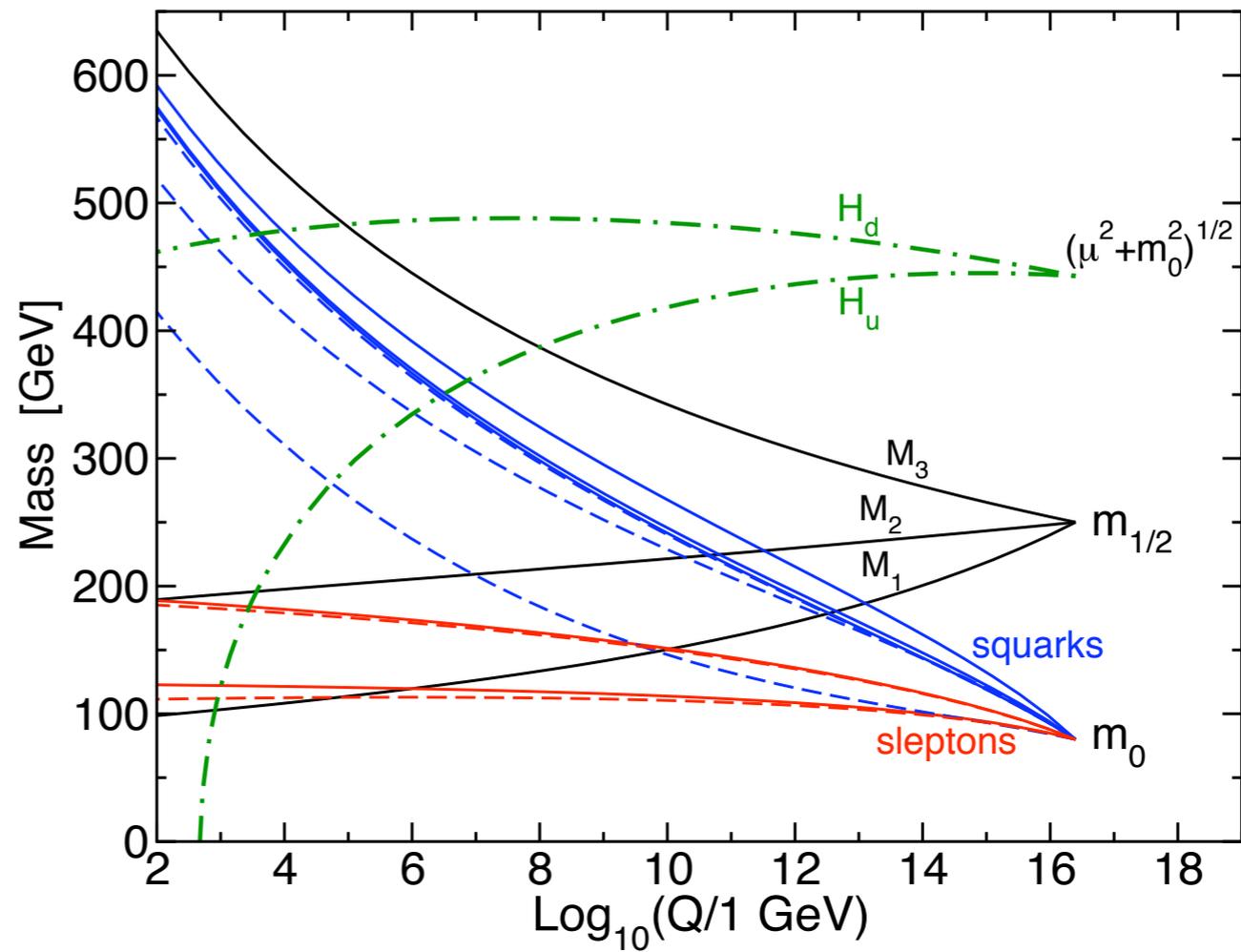
Not affecting collider signals

# RG evolution



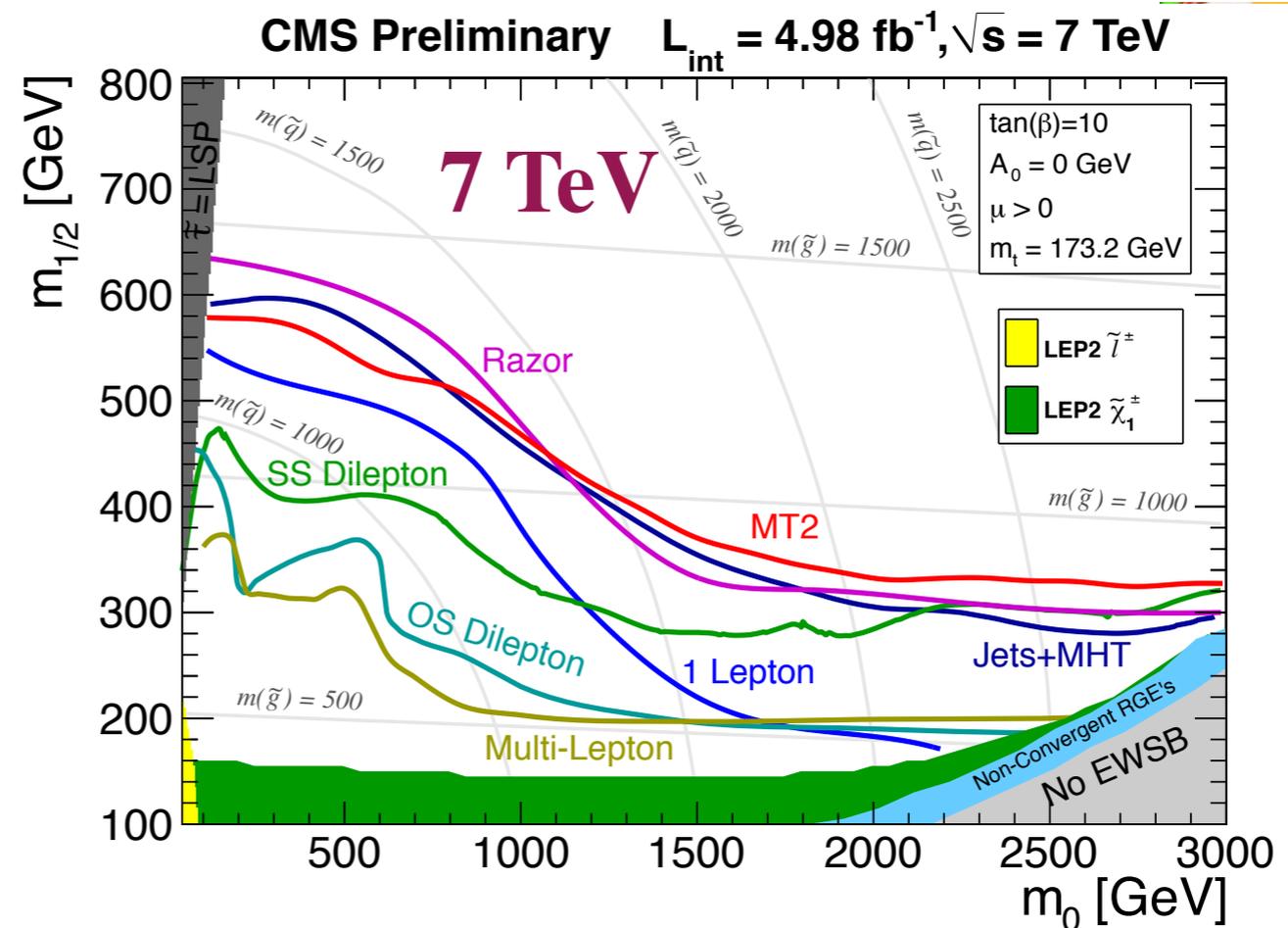
- RGE evolution down  $\Rightarrow$  physical masses we measure.
- Colored particles “run”s more.
  - ▶ Large,  $O(\text{several})$ , corrections.

# RG evolution



- Parameterizes full spectrum with 2 mass parameters,  $m_{1/2}$  (common gaugino mass) and  $m_0$  (common scalar mass).
- mSUGRA.

# mSUGRA

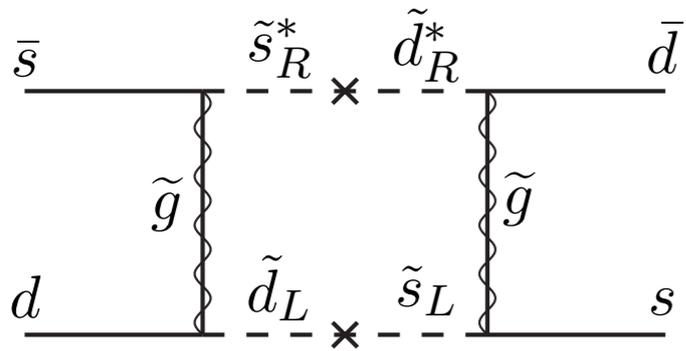


- Useful, simple parameterization. Good for understanding basic features of SUSY signal.
  - ▶ Good for classroom demo.
- But I will bet this is not the model.

# Pros and Cons

- Gravity exists, + SUSY  $\Rightarrow$  supergravity. Necessary coupling to mediated SUSY breaking is always there.
- However, gravity does not know flavor (equivalence principle)
  - ▶  $-\tilde{Q}^\dagger m_{\tilde{Q}}^2 \tilde{Q} - \tilde{L}^\dagger m_{\tilde{L}}^2 \tilde{L} - \tilde{u} m_{\tilde{u}}^2 \tilde{u}^\dagger - \tilde{d} m_{\tilde{d}}^2 \tilde{d}^\dagger - \tilde{e} m_{\tilde{e}}^2 \tilde{e}^\dagger$
  - ▶ soft mass  $m^2$ s are 3x3 matrices in flavor space
- Gravity mediation will generate off-diagonal term with the same size as the diagonal term.
  - ▶ Large flavor violation.

# A serious problem (SUSY flavor).

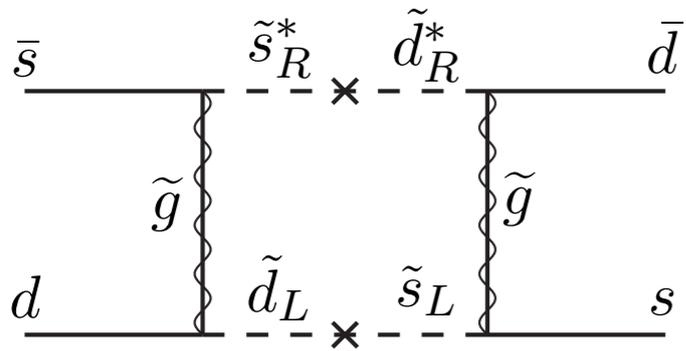


Kaon mixing

$$\frac{|\text{Re}[m_{\tilde{s}_R^* \tilde{d}_R}^2 m_{\tilde{s}_L^* \tilde{d}_L}^2]|^{1/2}}{m_{\tilde{q}}^2} < \left( \frac{m_{\tilde{q}}}{1000 \text{ GeV}} \right) \times \begin{cases} 0.0016 & \text{for } m_{\tilde{g}} = 0.5m_{\tilde{q}}, \\ 0.0020 & \text{for } m_{\tilde{g}} = m_{\tilde{q}}, \\ 0.0026 & \text{for } m_{\tilde{g}} = 2m_{\tilde{q}}. \end{cases}$$

- Too heavy to be a natural theory.
- For viable gravity mediation, addition flavor symmetry (alignment) is necessary.

# A serious problem (SUSY flavor).



Kaon mixing

$$\frac{|\text{Re}[m_{\tilde{s}_R^* \tilde{d}_R}^2 m_{\tilde{s}_L^* \tilde{d}_L}^2]|^{1/2}}{m_{\tilde{q}}^2} < \left( \frac{m_{\tilde{q}}}{1000 \text{ GeV}} \right) \times \begin{cases} 0.0016 & \text{for } m_{\tilde{g}} = 0.5 m_{\tilde{q}}, \\ 0.0020 & \text{for } m_{\tilde{g}} = m_{\tilde{q}}, \\ 0.0026 & \text{for } m_{\tilde{g}} = 2 m_{\tilde{q}}. \end{cases}$$

~1 for gravity mediation

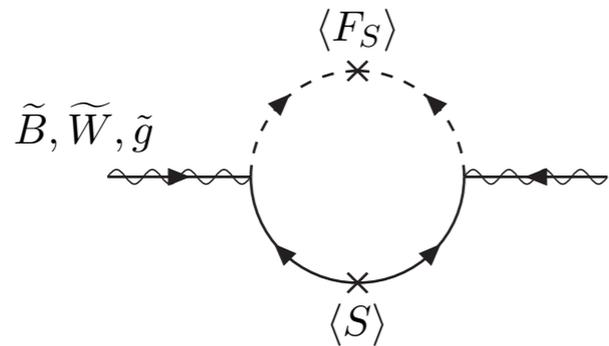
$$m_{\tilde{q}} > 100s \text{ TeV!}$$

- Too heavy to be a natural theory.
- For viable gravity mediation, addition flavor symmetry (alignment) is necessary.

# Low scale mediation.

- In comparison with gravity mediation
  - ▶ Lower SUSY breaking scale.
  - ▶ Stronger coupling.
- Main attraction: new interaction may know about flavor.
- Best known example: gauge mediation.

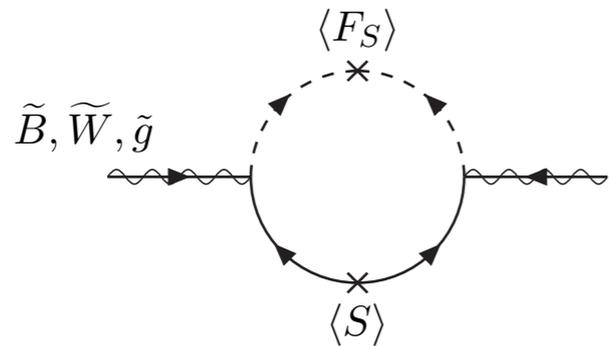
# Gauge mediation (loop induced)



$$M_a = \frac{\alpha_a}{4\pi} M_S, \quad M_S = \frac{\langle F_S \rangle}{\langle S \rangle}$$

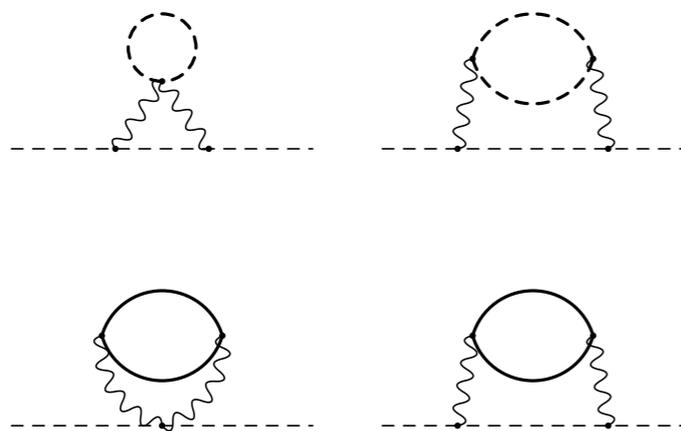
**S: messengers which feels SUSY breaking, with SM gauge couplings.**  
 $F_S \approx (\Lambda_S = \text{SUSY breaking scale})^2 \Rightarrow \text{SUSY breaking order parameter.}$

# Gauge mediation (loop induced)



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**S: messengers which feels SUSY breaking, with SM gauge couplings.**  
 $F_S \approx (\Lambda_S = \text{SUSY breaking scale})^2 \Rightarrow$  SUSY breaking order parameter.



$$+ \dots \quad m_{\text{scalar}}^2 = \left( \frac{\alpha}{4\pi} \right)^2 M_S^2$$

# Gauge mediation

$$M_a = \frac{\alpha_a}{4\pi} M_S, \quad M_S = \frac{\langle F_S \rangle}{\langle S \rangle} \quad m_{\text{scalar}}^2 = \left( \frac{\alpha}{4\pi} \right)^2 M_S^2$$

- $M_a \sim m_{\text{scalar}}$
- $M_S \sim 10 \text{ TeV} \Rightarrow M_a \sim m_{\text{scalar}} \sim \text{TeV}$ .
- Gravity mediation (also there), but subdominant if  $F_S \approx (\Lambda_S)^2 \ll (10^{11} \text{ GeV})^2$ .
- Gauge couplings, just like QED, can be flavor diagonal!!

# Gravitino LSP

- Gravitino does not have gauge interactions. Its' mass is still determined by gauge mediation. Gravitino is the LSP.

$$m_{3/2} \sim \frac{F_S}{M_{\text{Pl}}} \ll M_{\text{gaugino, squark...}}$$

- MSSM “LSP”, such as a neutralino would be NLSP.
- NLSP decaying into gravitino
  - ▶ Could be long lived on collider time scale.

$$\Gamma(\tilde{N}_1 \rightarrow \gamma \tilde{G}) = 2 \times 10^{-3} \kappa_{1\gamma} \left( \frac{m_{\tilde{N}_1}}{100 \text{ GeV}} \right)^5 \left( \frac{\sqrt{\langle F \rangle}}{100 \text{ TeV}} \right)^{-4} \text{ eV}$$

$$d = 9.9 \times 10^{-3} \frac{1}{\kappa_{1\gamma}} (E^2/m_{\tilde{N}_1}^2 - 1)^{1/2} \left( \frac{m_{\tilde{N}_1}}{100 \text{ GeV}} \right)^{-5} \left( \frac{\sqrt{\langle F \rangle}}{100 \text{ TeV}} \right)^4 \text{ cm}$$

# Comments

- Typically assumed bino NLSP, with decay  $\text{bino} \Rightarrow \text{photon} + \text{gravitino}$ . But, this is not necessary.

Any superpartner could be NLSP.

General gauge mediation: Meade, Seiberg, Shih

- No flavor problem!
- Can be low scale, decoupled from unknown high scale physics (string compactification, etc.).

# Comments

- Have to assume a more special structure.
  - ▶ Messenger sector feels SUSY breaking, also have SM gauge couplings.
  - ▶ Gauge coupling unification now needs to be arranged.
- Light Gravitino can not account for dark matter.
  - ▶ Other cosmological problems: light moduli...
- $\mu$ ,  $B_\mu$  problem.
- Having trouble with giving 125 GeV Higgs mass
  - ▶ Need additional structure.

# Trying to be smart

- Many mediation mechanisms:
  - ▶ Anomaly mediation.
  - ▶ Gaugino mediation.
  - ▶ Mirage, R-symmetric,  $\mu$ -driven,  $U(1)'$ , ....
- Many challenge: flavor (CP) problem, naturalness, experimental constraints.
- None of them is perfect. Some are getting quite complicated.
- Do we need to be smart? Are we lucky?  
Experiment will tell.